

The open-charm exotic hadrons $X_0(2900)$ and $X_1(2900)$

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On behalf of the LHCb Collaboration

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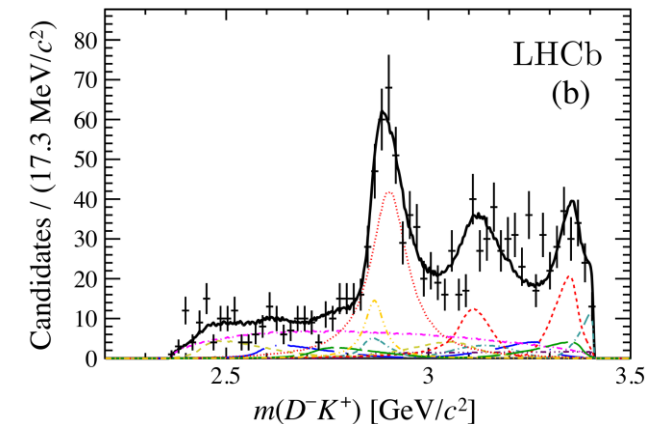
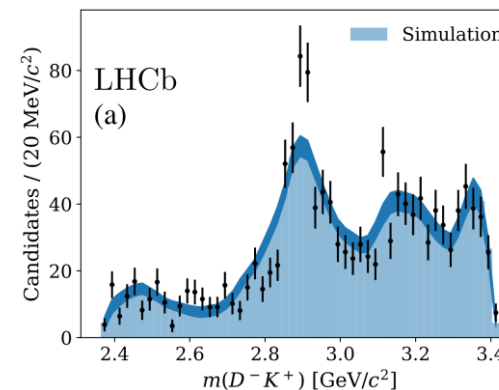
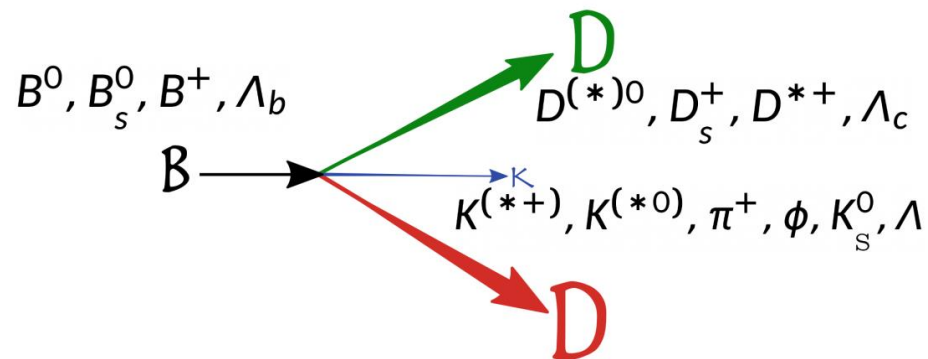


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- The $B \rightarrow DDh$ decays
- Model-independent analysis
- Amplitude analysis
- Conclusion and next step

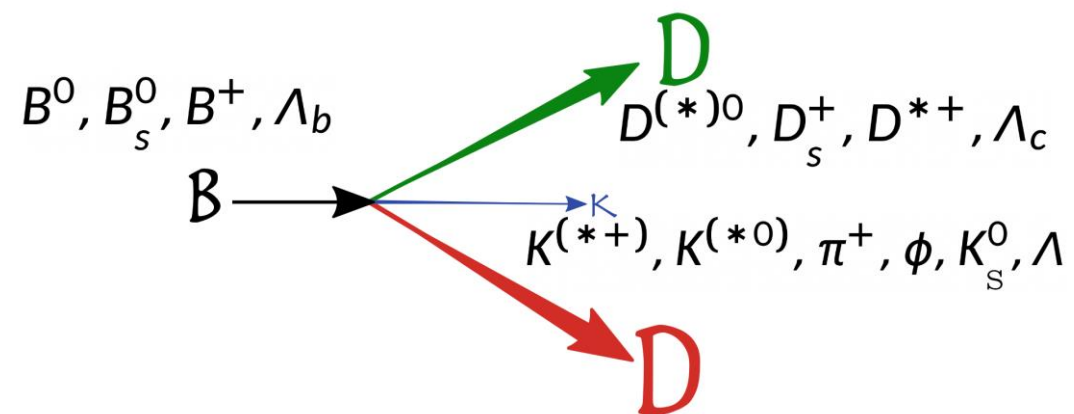
PRL 125, 242001 (2020)

PRD 102, 112003 (2020)



The $B \rightarrow DDh$ decays

- The $B \rightarrow DDh$ decays involve huge family of **topologically similar decays**.

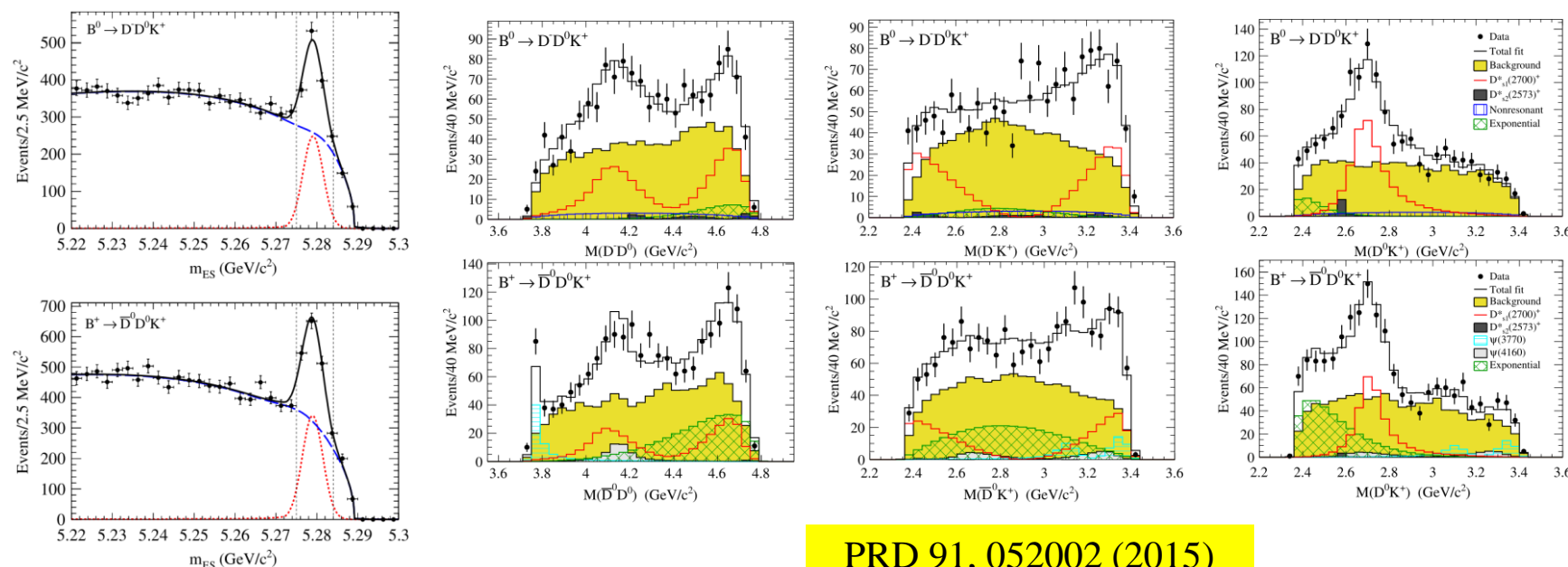


- Many intermediate states include:
 - Charmonium(-like) states ($D^{(*)}\bar{D}^{(*)}, \Lambda_c^+ \Lambda_c^-,$ etc.)
 - $D_{sJ}, \Lambda_c^{*+}, \Sigma_c^*$ spectroscopy ($D^{(*)0}K^+, \Lambda_c^{(*)-}\pi^+,$ etc.)
 - Exotic states ($D^{(*)0}D^{(*)-}, D^{(*)0}\Lambda_c^-, D^-K^+,$ etc.)
- **Powerful** exclusive decays for **hadron spectroscopy** studies.

- Several $B \rightarrow DDh$ branching fractions have been measured.
- Amplitude analyses of **only two decays** have been performed from **Belle** and **BaBar**:
 - $B^0 \rightarrow D^- D^0 K^+$, $B^+ \rightarrow \bar{D}^0 D^0 K^+$

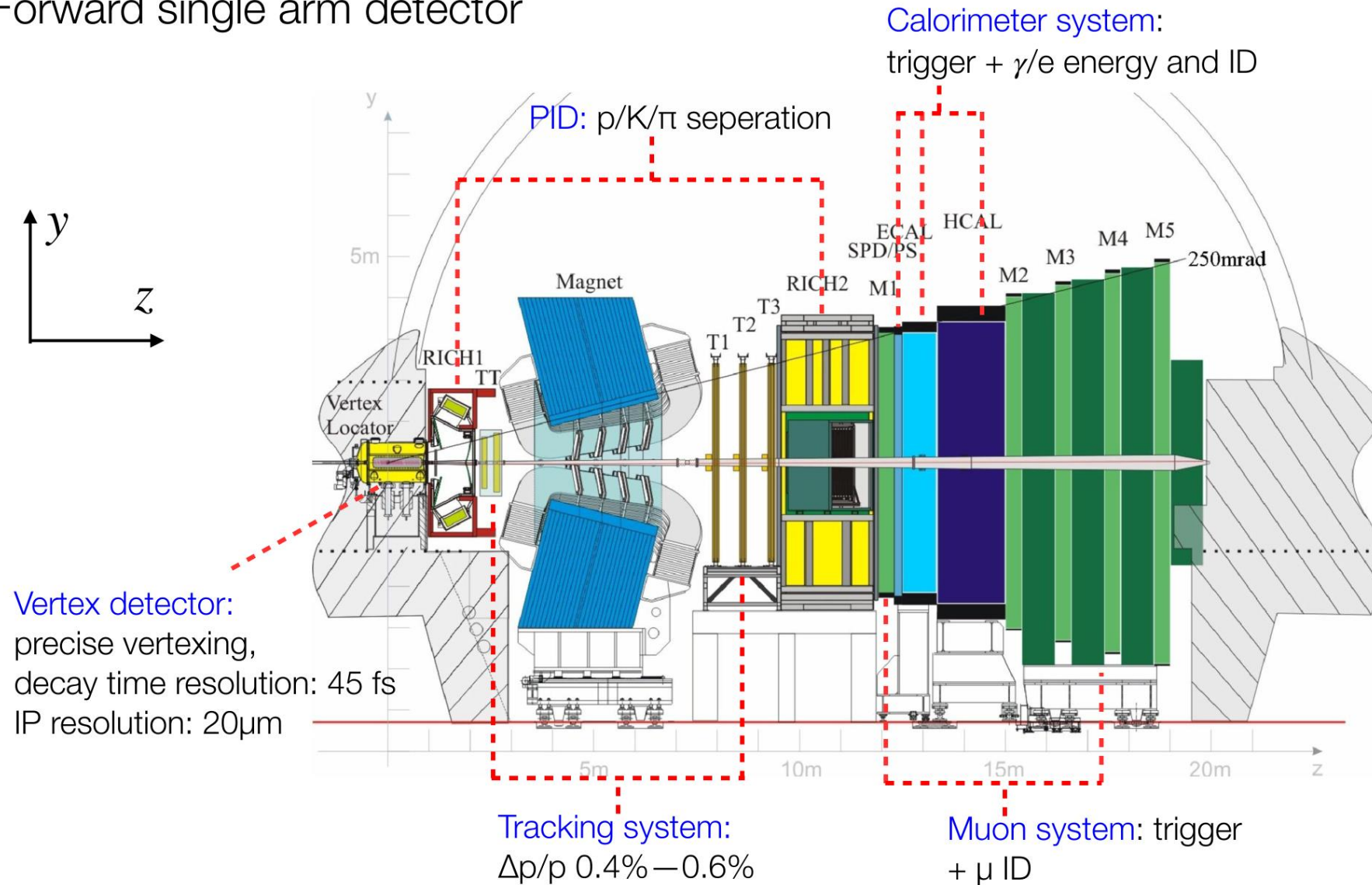
PRL 100, 092001 (2008)

PRD 91, 052002 (2015)
 - 400 – 800 signals with $\sim 40\%$ purity.
- Could be improved by LHCb collaboration!



PRD 91, 052002 (2015)

Forward single arm detector



- $B \rightarrow DDh$ branching fractions measurements in LHCb:

- Measurement of the branching fractions for $B \rightarrow D^* DK$ decays.

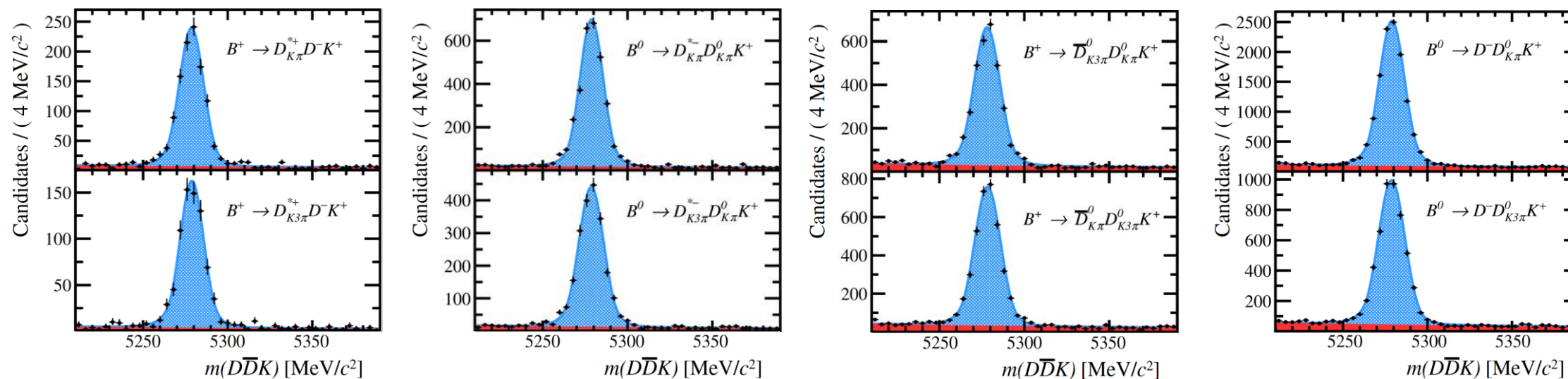
JHEP 12 (2020) 139

- First observation of the decay $B \rightarrow D^0 \bar{D}^0 K^+ \pi^-$.

PRD 102, 051102 (2020)

- High statistic & High purity unprecedented datasets

- Ideal $B \rightarrow DDh$ data samples for amplitude analyses.



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Model-independent analysis of $B^+ \rightarrow D^+ D^- K^+$ decay

● Why $B^+ \rightarrow D^+ D^- K^+$?

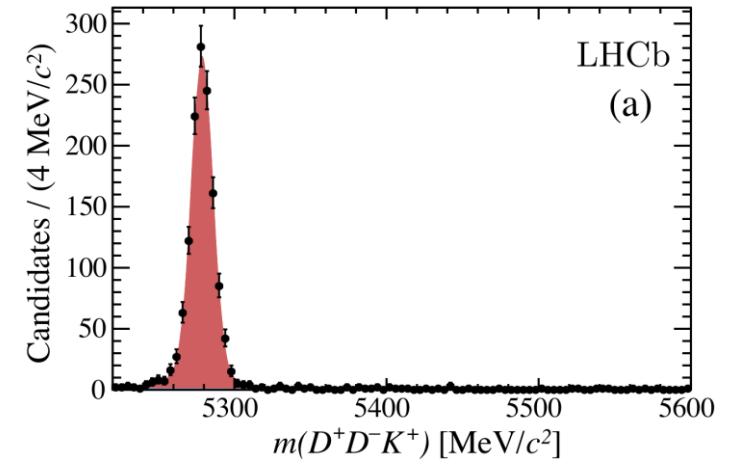
- Haven't been explored yet.
- Only the charmonium states ($D^+ D^-$) are expected.

● Dataset

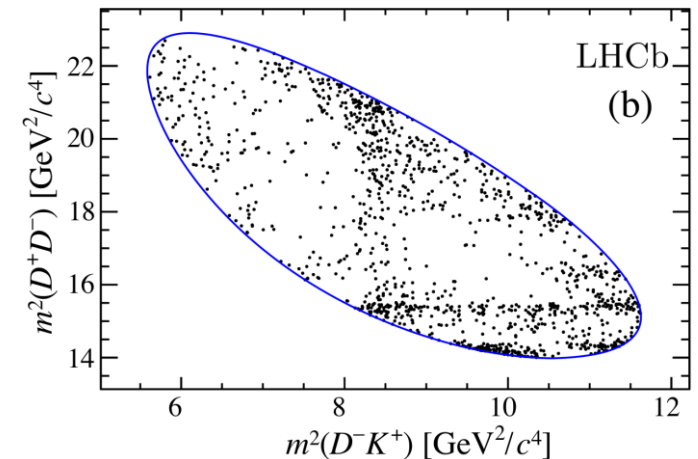
- Full LHCb Run 1 and Run 2 pp collision datasets (9 fb^{-1}).
- Reconstructed through $B^+ \rightarrow [K^- \pi^+ \pi^+]_D + [K^+ \pi^- \pi^-]_D - K^+$.
- Uniform BDT with topological and PID variables.

● Signal yields

- **1260 candidates** with in $\pm 20 \text{ MeV}/c^2$ of known B^+ mass.
- **99.5% purity!**

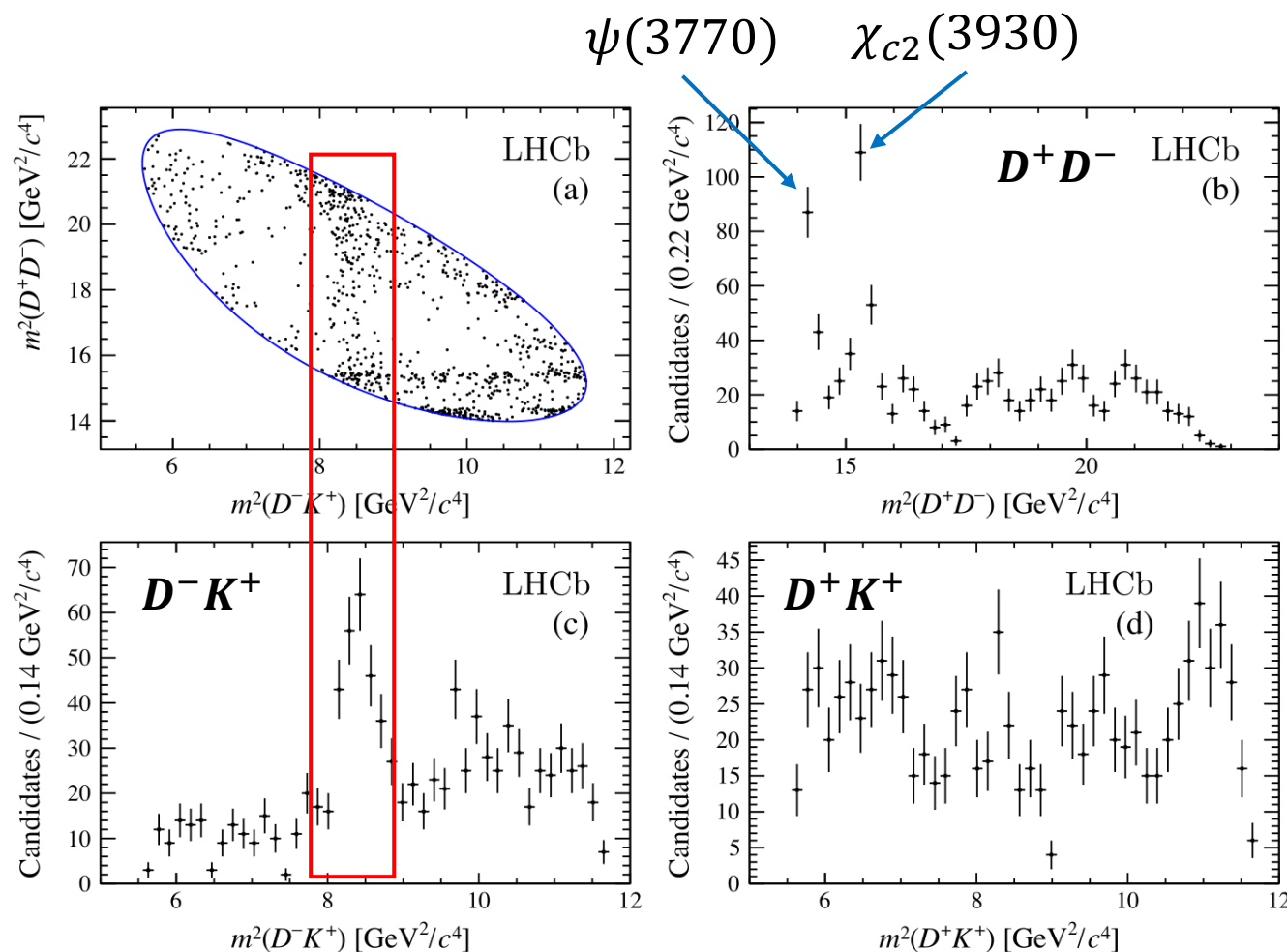


Invariant mass fit



Dalitz distribution

- Clear $\psi(3770)$ and $\chi_{c2}(3930)$ peaks in D^+D^- spectrum.
- Obvious peaking structures in D^-K^+ spectrum at $8.5 \text{ GeV}^2/c^4$ ($2.9 \text{ GeV}/c^2$).
- Is it a **new exotic state**? Or **reflection** from D^+D^- resonance?



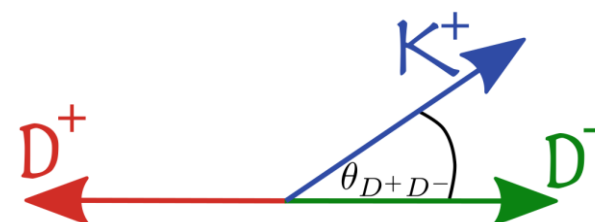
- Decompose the $h(D^+D^-)$ according to the basis of Legendre polynomials:

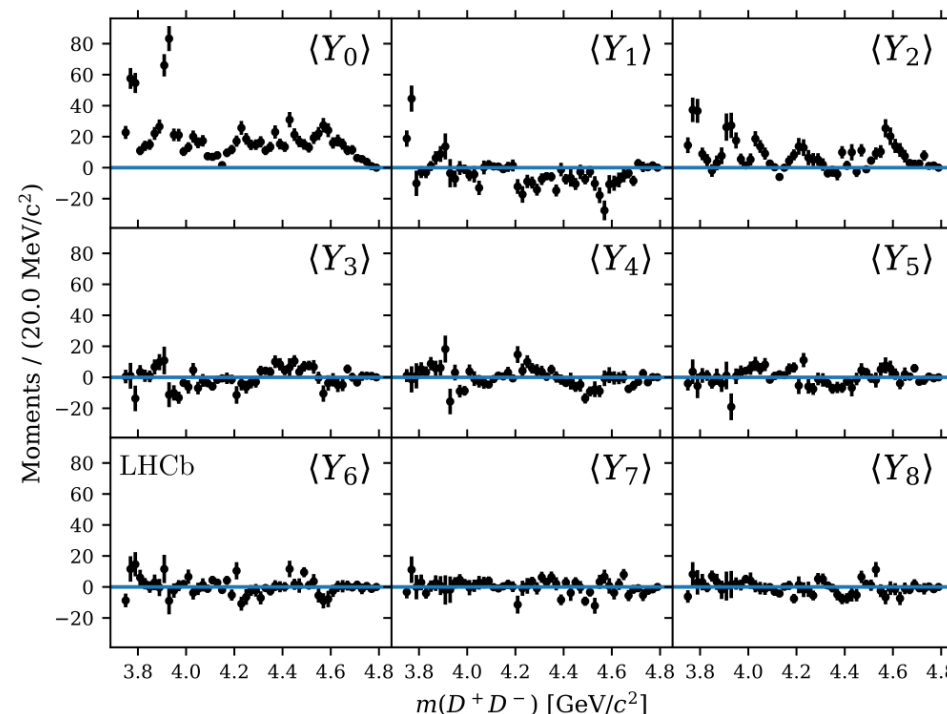
$$P_k[h(D^+D^-)] = \sqrt{\frac{2k+1}{2}} \times 2^k \sum_{r=0}^k [h(D^+D^-)]^r \binom{k}{r} \left(\frac{k+r-1}{2} \right)$$

- Divide the $m(D^+D^-)$ into slices, the **coefficient of bin j** weighted by **order- k** Legendre polynomial can be expressed as:

$$\langle Y_k^j \rangle = \sum_{l=1}^{N_j^{Data}} w_l P_k[h_l(D^+D^-)]$$

- The $\langle Y_k \rangle$ with $k = 2J_{\max}$ could account for the contribution of the charmonium resonances with spin up to J_{\max} .

$$h(D^+D^-) = \cos(\theta_{D^+D^-})$$




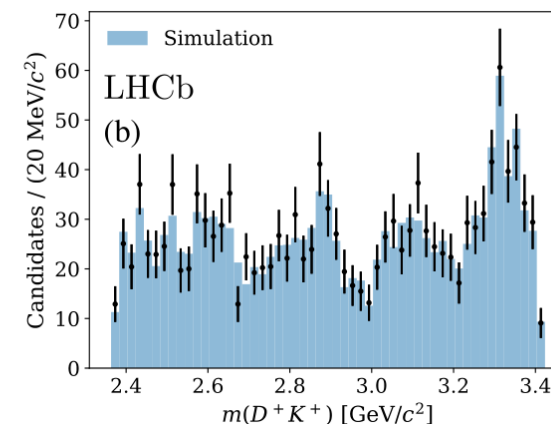
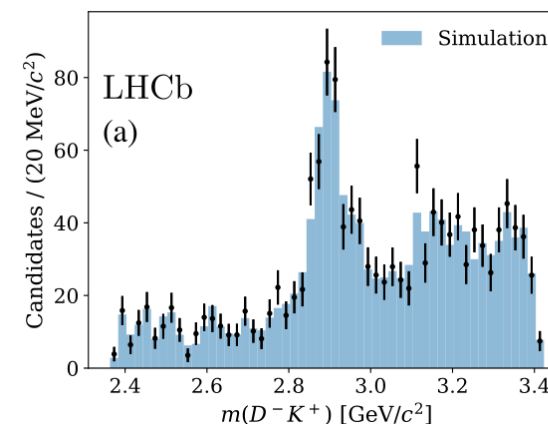
Distributions of unnormalized moments $\langle Y_k^j \rangle$

- Phase space MC samples are generated, and weighted by:

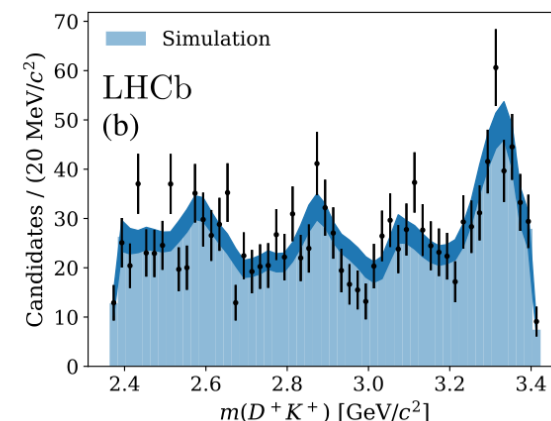
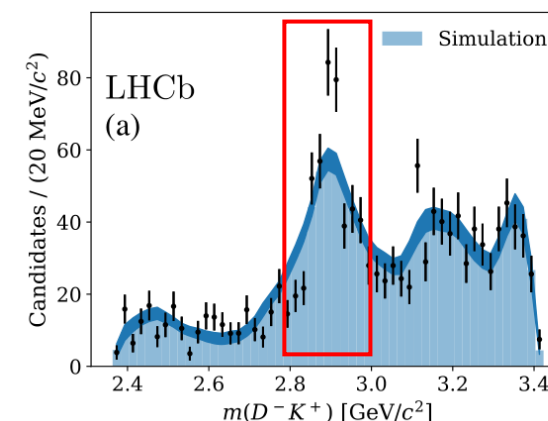
$$\eta_i = \frac{2}{N_j^{Sim}} \times \sum_{k=0}^{k_{\max}} \langle Y_k^j \rangle P_k[h_i(D^+ D^-)]$$

then project to $m(D^- K^+)$ and $m(D^- K^+)$ spectra.

- $m(D^- K^+)$ could be well described with **high** k_{\max} .
- Clear deviation** on $m(D^- K^+)$ spectrum around 2.9 GeV/c² with $k_{\max} = 4$ ($J_{\max} = 2$).
- The **significance** of disagreement is estimated to be **3.9σ** with $k_{\max} = 4$ and **3.7σ** with $k_{\max} = 6$ by using test statistic.



$k_{\max} = 29$



$k_{\max} = 4$

Indicate a new exotic charm-strange resonance!

Model-dependent analysis of $B^+ \rightarrow D^+ D^- K^+$ decay

- Based on Laura++ Dalitz plot fitter.

➤ **Likelihood:**

$$\mathcal{L} = \exp \left[- \sum_c \left(\frac{(p_c - \mu_c)^2}{2\sigma_c^2} \right) \right] \times \prod_{j=1}^{N_c} (N_{sig} \mathcal{P}_{sig}(\vec{x}_j) + N_{bg} \mathcal{P}_{bg}(\vec{x}_j))$$

Gaussian constraints
Signal model
Background model

➤ **Signal PDF:**

$$\mathcal{P}_{sig}(\vec{x}) = \frac{1}{\mathcal{N}} \times \epsilon_{total}(\vec{x}) \times |\mathcal{A}_{sig}(\vec{x})|^2$$

➤ **Signal Amplitude:**

$$\mathcal{A}_{sig}(\vec{x}) = \sum_{j=1}^N c_j \mathbf{F}_j(\vec{x})$$

➤ **Resonant Amplitude:**

$$\mathbf{F}_j(\vec{x}) = \mathbf{R}(m(D^+ D^-)) \times \mathbf{T}(\vec{p}, \vec{q}) \times \mathbf{X}(\vec{p}) \times \mathbf{X}(\vec{q})$$

➤ $\mathbf{R}(m(D^+ D^-))$: Relativistic Breit-Wigner function.

➤ $\mathbf{T}(\vec{p}, \vec{q})$: Angular factor – non-relativistic Zemach tensor formalism.

➤ $\mathbf{X}(\vec{p}), \mathbf{X}(\vec{q})$: Blatt-Weisskopf barrier factors.

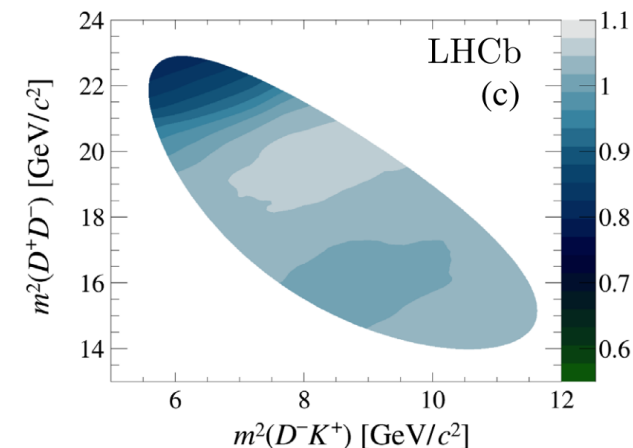
● Efficiency maps:

$$\epsilon_{\text{total}}(\vec{x}) = \epsilon_{\text{offline|reco}}(\vec{x}) \times \epsilon_{\text{reco|trig}}(\vec{x}) \times \epsilon_{\text{trig|gemo}}(\vec{x}) \times \epsilon_{\text{gemo}}(\vec{x}).$$

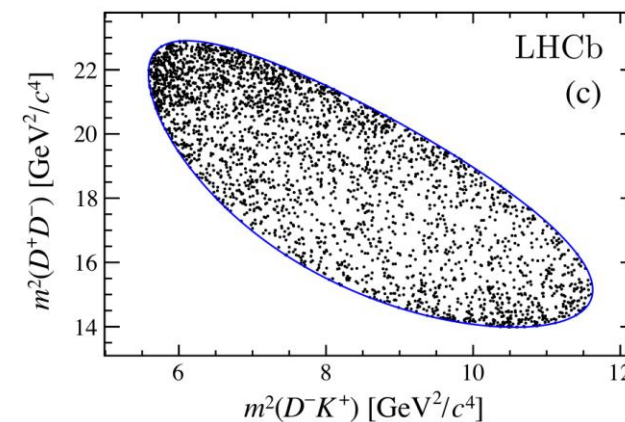
- Extracted from simulated samples with data-driven method to correct data-MC difference.
- Run 1 and Run 2 datasets are fitted simultaneously with corresponding efficiency map.

● Background modelling.

- Using the B^+ sideband samples ($5.35 \text{ GeV}/c^2 < m(D^+D^-K^+) < 5.69 \text{ GeV}/c^2$).
- Relaxing BDT to increase the sample size.
- Applying kernel estimation procedure to reduce statistic fluctuations.



Relatively efficiency map



Sideband samples

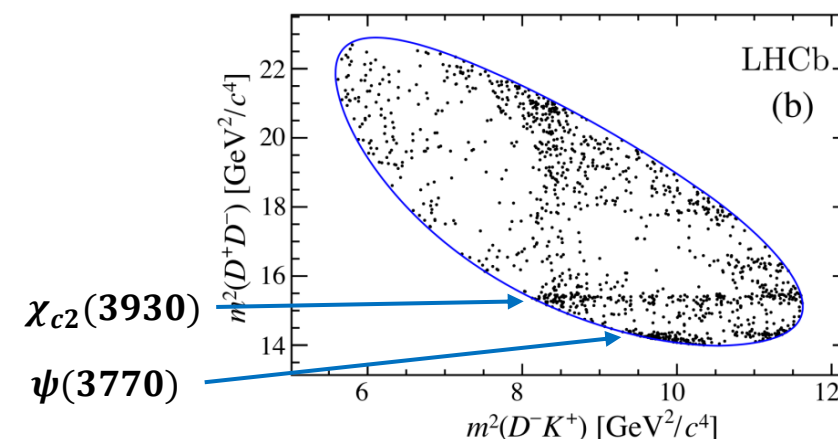
● Model content:

- MI analysis indicate possible $D^- K^+$ resonant contributions.
- First try with only charmonium resonances.
- Only states with natural J^P (0^+ , 1^- , 2^+ ...) are allowed to decay into $D^+ D^-$.

● Fitting procedure:

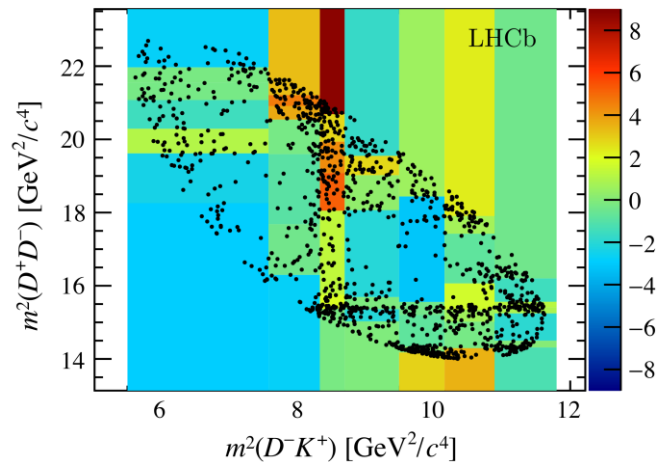
- Always include $\psi(3770)$ and $\chi_{c2}(3930)$.
- Include other components if significantly reduce NLL.
- Constrain m & σ of $\psi(3770)$, $\psi(4040)$, $\psi(4160)$, $\psi(4415)$.
- Add $\chi_{c0}(3930)$, float m & σ of $\chi_{cJ}(3930)$.
- Try various non-resonant lineshapes (uniform, exponential, polynomial, spline) with spin-0 or 1.

Partial wave (J^{PC})	Resonance	Mass (MeV/ c^2)	Width (MeV)
S wave (0^{++})	$\chi_{c0}(3860)$	3862 ± 43	201 ± 145
	$X(3915)$	3918.4 ± 1.9	20 ± 5
P wave (1^{--})	$\psi(3770)$	3778.1 ± 0.9	27.2 ± 1.0
	$\psi(4040)$	4039 ± 1	80 ± 10
	$\psi(4160)$	4191 ± 5	70 ± 10
	$\psi(4260)$	4230 ± 8	55 ± 19
	$\psi(4415)$	4421 ± 4	62 ± 20
D wave (2^{++})	$\chi_{c2}(3930)$	3921.9 ± 0.6	36.6 ± 2.1
F wave (3^{--})	$X(3842)$	3842.71 ± 0.20	2.79 ± 0.62

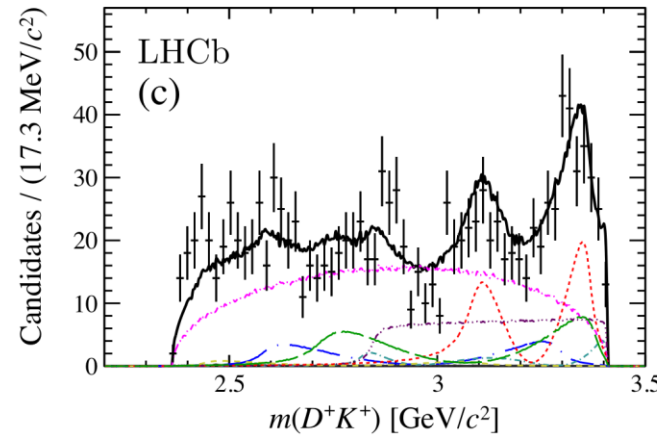
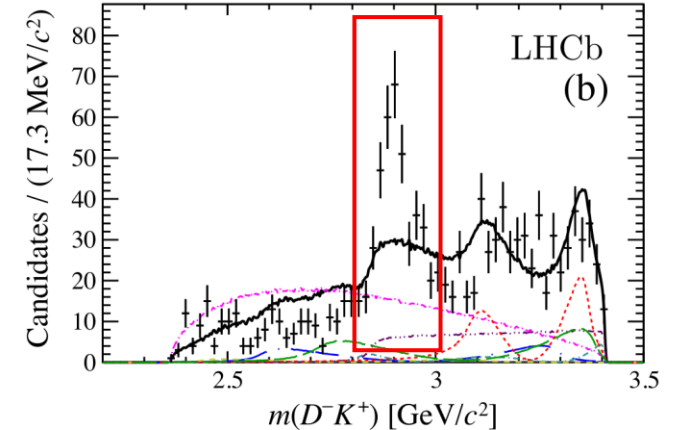
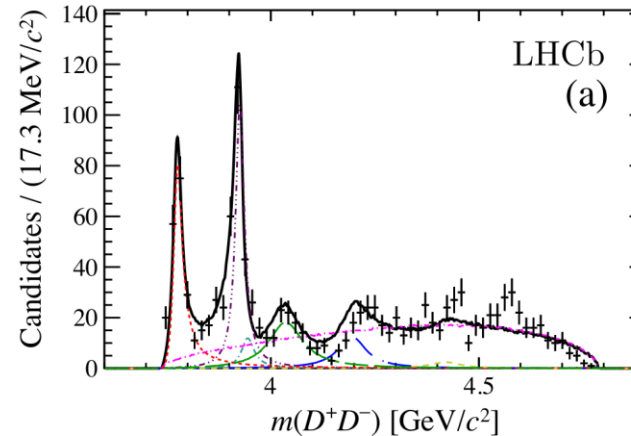


● Results with only $D^+ D^-$ resonances:

- Including $\psi(3770)$, $\chi_{c0}(3930)$, $\chi_{c2}(3930)$, $\psi(4040)$, $\psi(4160)$ and $\psi(4415)$ resonances.
- $m(D^+ D^-)$ and $m(D^+ K^+)$ could be well described.
- **Large deviation on $m(D^- K^+)$ spectrum around $2.9 \text{ GeV}/c^2$.**



Goodness of fit



- $\psi(3770) \rightarrow D^+ D^-$
- $\chi_{c0}(3930) \rightarrow D^+ D^-$
- $\chi_{c2}(3930) \rightarrow D^+ D^-$
- $\psi(4040) \rightarrow D^+ D^-$
- $\psi(4160) \rightarrow D^+ D^-$
- $\psi(4415) \rightarrow D^+ D^-$
- Nonresonant

Fitting result without $D^+ K^-$ resonance

● Results after add D^-K^+ resonances:

➤ Two D^-K^+ resonances are added:

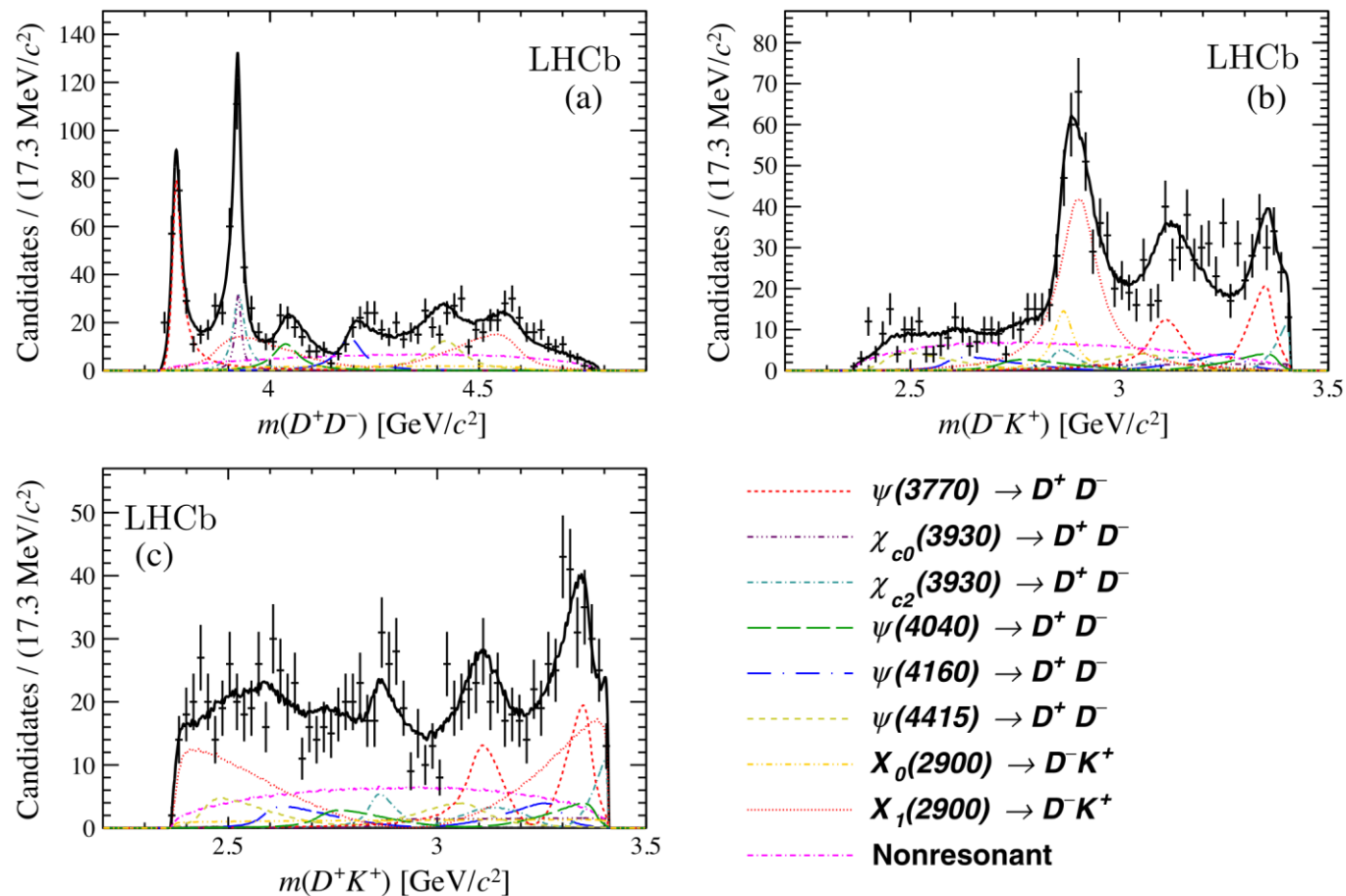
□ $X_0(2900), J^P = 0^+$

- Mass: $2866 \pm 7 \pm 2 \text{ MeV}/c^2$
- Width: $57 \pm 12 \pm 4 \text{ MeV}$

□ $X_1(2900), J^P = 1^-$

- Mass: $2904 \pm 5 \pm 1 \text{ MeV}/c^2$
- Width: $110 \pm 11 \pm 4 \text{ MeV}$

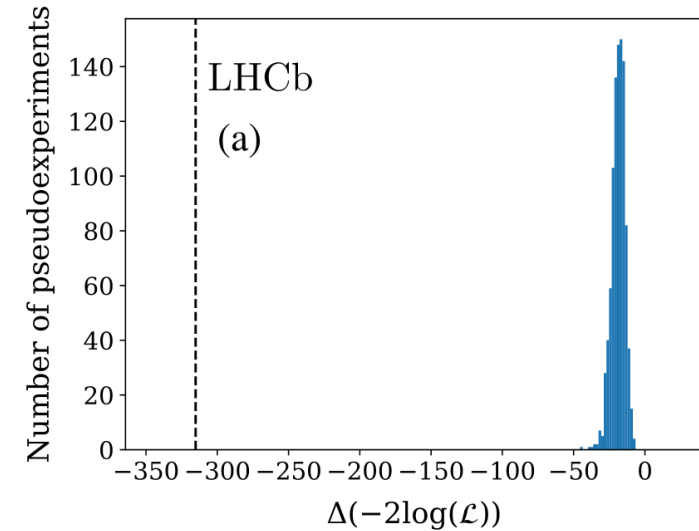
➤ Also test other models, this model gives the best description.



Fitting result with D^+K^- resonances

- **Results after add D^-K^+ resonances:**

- Determining the significance with pseudo-experiments.
 - Generate 1000 toys from fit with no D^-K^+ components.
 - Fit the toy with model with and without new resonances.
- **Overwhelmingly significance $\gg 5\sigma$.**



- **Tetraquark candidates with four flavors:**

- In 2016, D0 collaboration report evidence of a $B_s^0\pi^+$ ($\bar{b}sud\bar{d}$) resonance called $X(5568)^+$, but isn't confirmed by other experiments.
- $X(2900)$ could be confirmed in the other $B \rightarrow DDK$ analyses.
- $X_0(2900)$ and $X_1(2900)$ ($c\bar{s}ud\bar{d}$) would be the **first confirmed observation** of tetraquark state with **four different flavors**.

PRL 117, 022003 (2016)

● In $\chi_{cJ}(3930)$ region:

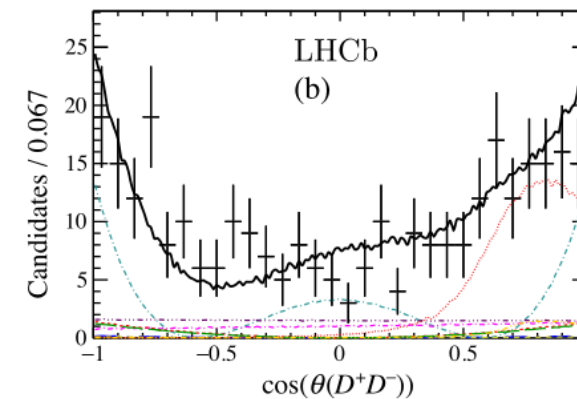
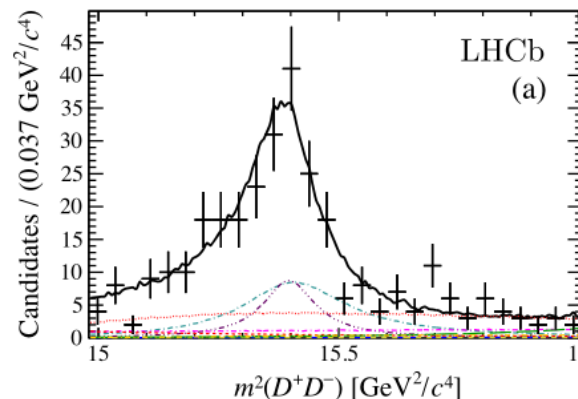
➤ Necessary to include both spin-0 and spin-2 components:

□ $\chi_{c0}(3930), J^P = 0^+$

- Mass: $3923.8 \pm 1.5 \pm 0.4 \text{ MeV}/c^2$
- Width: $17.4 \pm 5.1 \pm 0.8 \text{ MeV}$

□ $\chi_{c2}(3930), J^P = 2^+$

- Mass: $3926.8 \pm 2.4 \pm 0.8 \text{ MeV}/c^2$
- Width: $34.2 \pm 6.6 \pm 1.1 \text{ MeV}$



Zoom in on the $\chi_{cJ}(3930)$ ($15 \text{ GeV}^2/c^2 < m^2(D^+D^-) < 16 \text{ GeV}^2/c^2$)

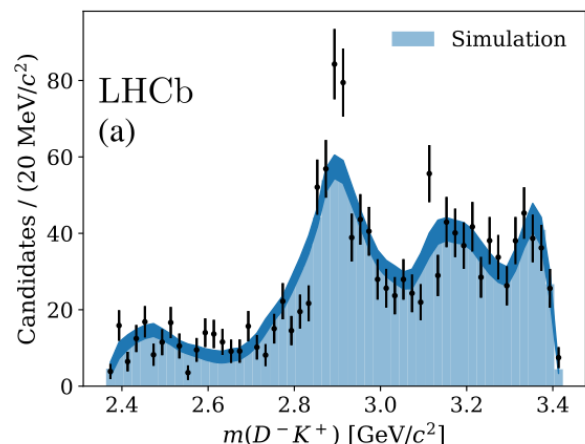
➤ $\chi_{c2}(3930)$ measured mass not consistent with inclusive study.

- **Mass:** $3921.9 \pm 0.6 \pm 0.2 \text{ MeV}/c^2$

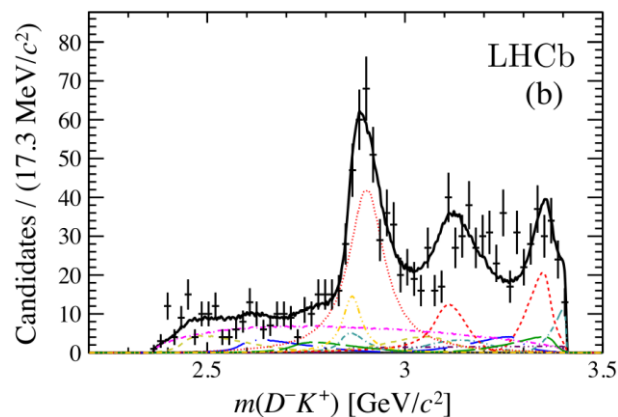
JHEP 07 (2019) 035

➤ Why $\chi_{c0}(3860)$ didn't observe in $B^+ \rightarrow D^+D^-K^+$ channel?

➤ **Need more statistic to confirm.**



Model-independent analysis



Amplitude analysis

● Conclusion

- ✓ **Model-independent analysis** indicates possible resonance on $D^- K^+$ spectrum.
- ✓ With the **amplitude analysis**, two exotic $D^- K^+$ resonances with spin-0 and spin-1 are observed.
- ✓ Discovery of contributions from spin-0 and spin-2 components in the region of the existing $\chi_{c2}(3930)$.

● Next step

- Several **ongoing $B \rightarrow DDh$ analyses** with LHCb Run 1 and Run 2 datasets.
 - B : $B^{0,+}, B_S^0, \Lambda_b^0 \dots$; D : $D^{0,+}, D^{*+}, D_S^+, \Lambda_c^+ \dots$; h : $K^+, \pi^+, p, \Lambda \dots$
- LHCb Run 3 data taking will start soon.
 - ✓ 10 times statistic, detail analysis on $B^+ \rightarrow D^+ D^- K^+$
 - ✓ More potential $B \rightarrow DDh$ channels to be explored.