

# Cosmology with PeV scale gauged B-L symmetry

U. A. YAJNIK, *Indian Institute of Technology Bombay*



*Crossroads of Neutrino Physics,*  
MITP, *Johannes Gutenberg Universität, Mainz*, 06 August 2015



# Overview

- left-right symmetric models as JSBM
  - the renormalisable SUSY version
  - intermediate  $U(1)_{B-L}$
- Constraint of exact Parity
  - Domain wall dynamics and successful Cosmology
  - Non-thermal leptogenesis
- SUSY breaking and Parity breaking – a study

# Left-right as JBSM

Just Beyond the Standard Model ...  $SU(2)_L \otimes SU(2)_R \otimes U(1)_X$

$$\begin{array}{c}
 \begin{array}{ccccc}
 & \tau_L^3 & \tau_R^3 & \frac{1}{2}X & Q \\
 \left[ \begin{array}{c} \nu_L \\ e_L^- \end{array} \right] & +\frac{1}{2} & 0 & -\frac{1}{2} & 0 \\
 \left[ \begin{array}{c} \nu_R \\ e_R^- \end{array} \right] & 0 & +\frac{1}{2} & -\frac{1}{2} & 0 \\
 \left[ \begin{array}{c} \nu_R \\ e_R^- \end{array} \right] & 0 & -\frac{1}{2} & -\frac{1}{2} & -1
 \end{array} \\
 \\
 \begin{array}{ccccc}
 & \tau_L^3 & \tau_R^3 & \frac{1}{2}X & Q \\
 \left[ \begin{array}{c} u_L \\ d_L \end{array} \right] & +\frac{1}{2} & 0 & +\frac{1}{6} & +\frac{2}{3} \\
 \left[ \begin{array}{c} d_L \\ u_L \end{array} \right] & -\frac{1}{2} & 0 & +\frac{1}{6} & -\frac{1}{3} \\
 \left[ \begin{array}{c} u_R \\ d_R \end{array} \right] & 0 & +\frac{1}{2} & +\frac{1}{6} & +\frac{2}{3} \\
 \left[ \begin{array}{c} d_R \\ u_R \end{array} \right] & 0 & -\frac{1}{2} & +\frac{1}{6} & -\frac{1}{3}
 \end{array}
 \end{array}$$

- Need a new hypercharge  $X \rightarrow$  turns out to be exactly  $B - L$   
 ... the only global charge of SM waiting to be gauged!

# Minimal SUSY L-R Model – MSLRM

Higgs superfields

$$\begin{aligned}
 \Phi_i &= (1, 2, 2, 0), & i &= 1, 2, \\
 \Delta &= (1, 3, 1, 2), & \bar{\Delta} &= (1, 3, 1, -2), \\
 \Delta_c &= (1, 1, 3, -2), & \bar{\Delta}_c &= (1, 1, 3, 2), \\
 \Omega &= (1, 3, 1, 0), & \Omega_c &= (1, 1, 3, 0)
 \end{aligned}$$

- triplets doubled for anomaly cancellation.
- bidoublet doubling needed to accommodate CKM matrix.
- without the  $\Omega$ 's supersymmetric vacua necessarily break  $U(1)_{EM}$  along with parity.
- alt fixes, non-renormalisable terms or singlets not pursued here.

Requirement of discrete parity,

$$\begin{aligned}
 Q &\leftrightarrow Q_c^*, & L &\leftrightarrow L_c^*, & \Phi_i &\leftrightarrow \Phi_i^\dagger, \\
 \Delta &\leftrightarrow \Delta_c^*, & \bar{\Delta} &\leftrightarrow \bar{\Delta}_c^*, & \Omega &\leftrightarrow \Omega_c^*.
 \end{aligned} \tag{1}$$

The F-flat and D-flat SUSY vacua imply breaking to  $SU(2)_L \otimes U(1)_R \otimes U(1)_{B-L}$

$$\langle \Omega_c \rangle = \begin{pmatrix} \omega_c & 0 \\ 0 & -\omega_c \end{pmatrix}, \quad \langle \Delta_c \rangle = \begin{pmatrix} 0 & 0 \\ d_c & 0 \end{pmatrix}, \quad \langle \Phi_i \rangle = \begin{pmatrix} \kappa_i & 0 \\ 0 & \kappa'_i \end{pmatrix} \quad (2)$$

This ensures spontaneous parity violation [Aulakh, Bajc, Melfo, Rasin, Senjanovic (1998 ...)]

### The Mass scale see-saw

- An  $R$  symmetry ensures  $\Omega$  mass terms in superpotential are vanishing, no new spurious mass scale
- Usual  $R$  parity preserved
- Leads naturally to a see-saw relation

$$M_{B-L}^2 = M_{EW} M_R$$

- Leptogenesis postponed to a scale closer to  $M_{EW}$  below  $M_R$  !!

# Genesis of baryogenesis

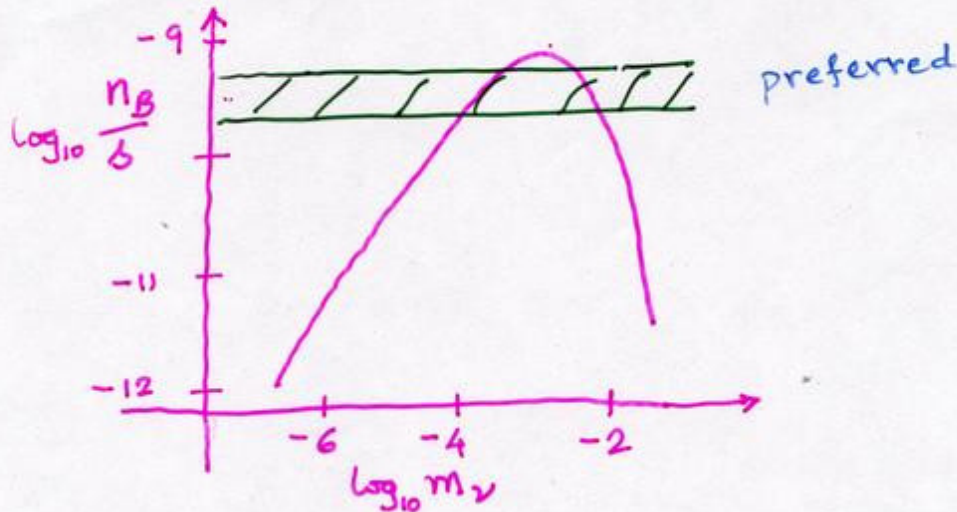
- CP violation discovery 1964
- CMBR discovery also 1965 ...
- The possibility of *dynamical origins* of baryon asymmetry

$$\frac{n_B}{s} \simeq 10^{-9}$$

- Weinberg Brandeis lectures 1965; specific model Sakharov 1967

## Leptogenesis - thermal case

Thermal leptogenesis in SO(10) (Buchmüller, Plümacher et al)



$m_\nu$  too small : Yukawa couplings too small to bring heavy  $N$  into equilibrium

$m_\nu$  too large : Erasure processes too efficient

$$M_N \gtrsim O(10^9) \text{ GeV} \left( \frac{2.5 \times 10^{-3}}{Y_N} \right) \left( \frac{0.05 \text{ eV}}{m_\nu} \right)$$

$M_N \gtrsim 10^9$  GeV – does not sit well with hierarchy in non-SUSY case

- Conflicts with Supersymmetric unification  $\rightarrow$  gravitino overproduction



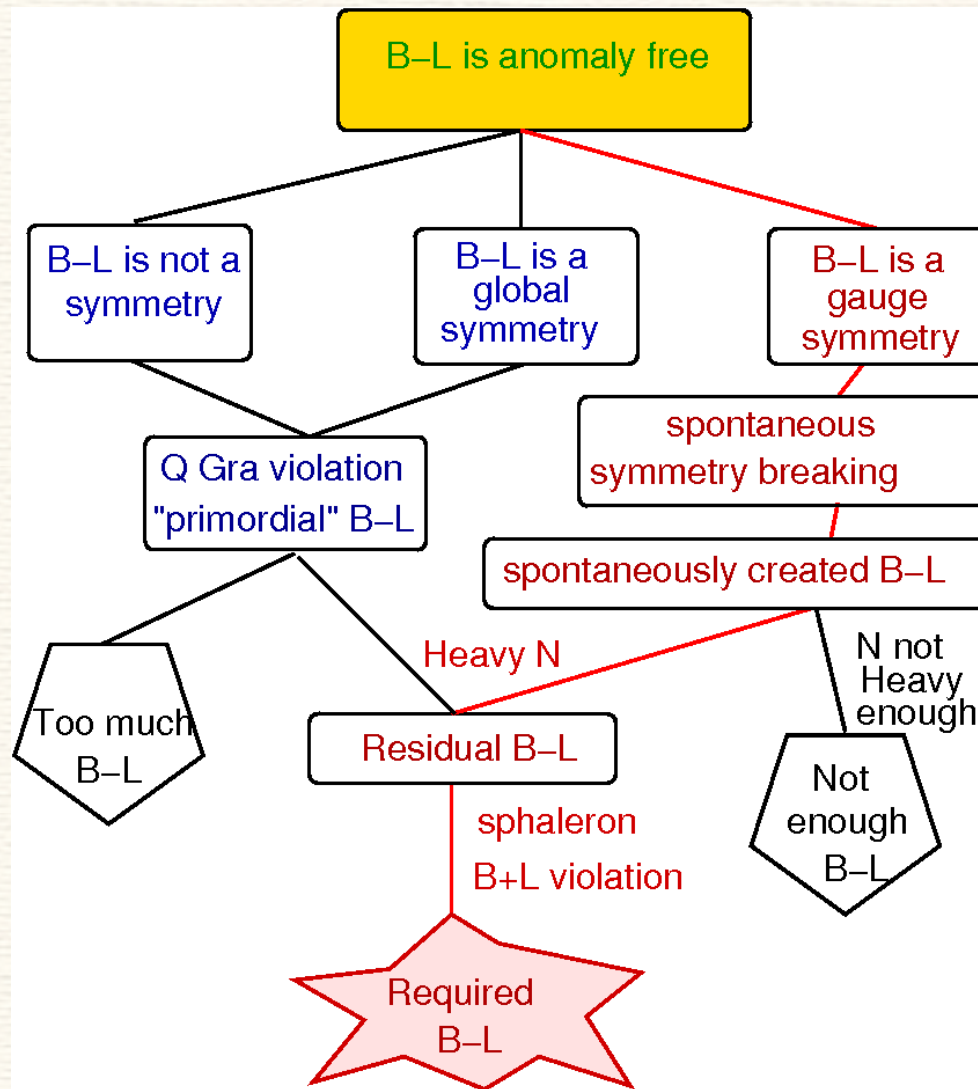
## Neutrino mass and $CP$ phase constraint

- Analysis of see-saw formula with three generations taken into account show, for thermal leptogenesis, (Davidson and Ibarra)

$$|\varepsilon_{CP}| \leq 10^{-7} \left( \frac{M_1}{10^9 \text{GeV}} \right) \left( \frac{m_3}{0.05 \text{eV}} \right)$$

- Generically too small for producing the asymmetry

# What choices did der Alte have?



# Neutrino mass and (?) unification

How do we accommodate the neutrino mass?

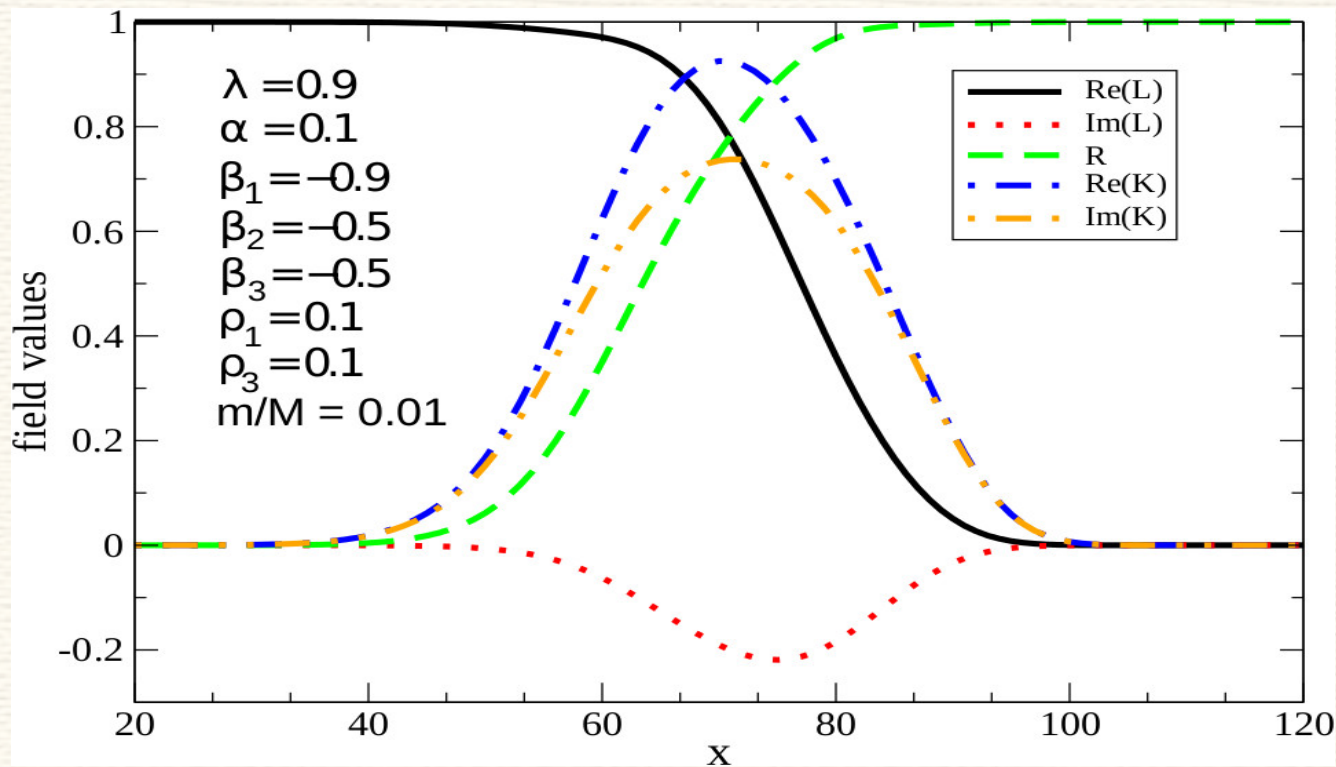
- Higher order operator :

$$\mathcal{L} \sim \frac{c_1}{\Lambda_\nu} \text{Tr} \left( \phi \tilde{\phi}^\dagger l_L \bar{l}_L^C \right) \sim \frac{c_1}{\Lambda_\nu} \overline{\nu}_L^C \langle \phi \rangle^2 \nu_L$$

- Example :  $m_\nu \sim O(0.1)$  eV  $\Rightarrow \Lambda_\nu \sim O(10^{15})$  GeV
- We have not yet seen any sign of GUT scale
  - generically expect proton decay
- JBSM ideology ...
  - sequester majorana  $M_N$  from gauge coupling unification
  - Choose a convenient “pivot” for generic see-saw leptonic Dirac mass like  $m_\tau$  or  $m_\mu$  or  $m_e$  ... ( words of stray wisdom )
  - $\Rightarrow M_N \sim 10^{11}$  GeV or  $\sim 10^8$  GeV or  $\sim 10^4$  GeV respectively

## Non-thermal leptogenesis

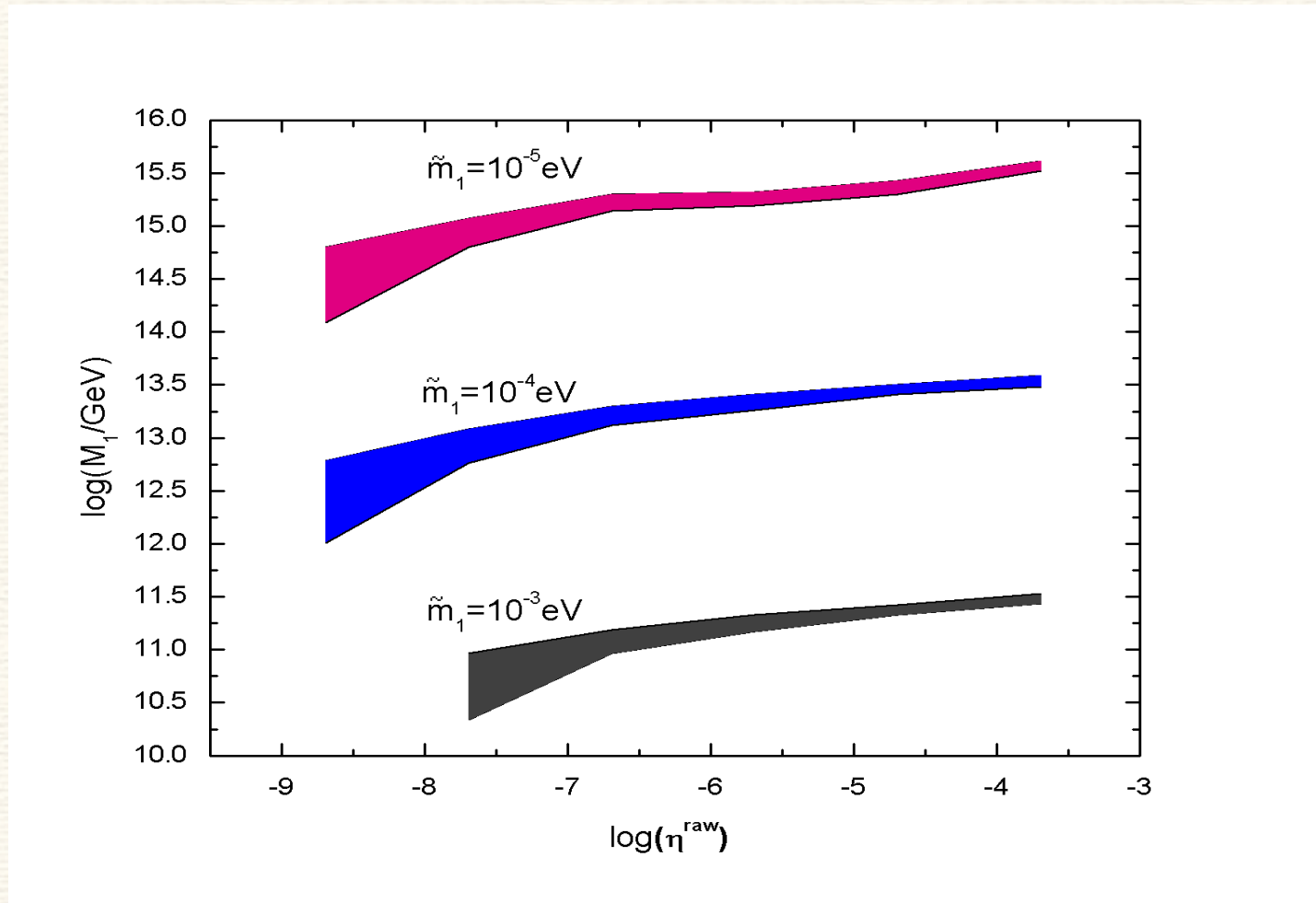
- Parity breaking transition provides domain walls,
- “First order” phase transition with bubble walls ensured
- $CP$  violating scalar condensate  $\text{Im}(\kappa)/\text{Re}(\kappa)$



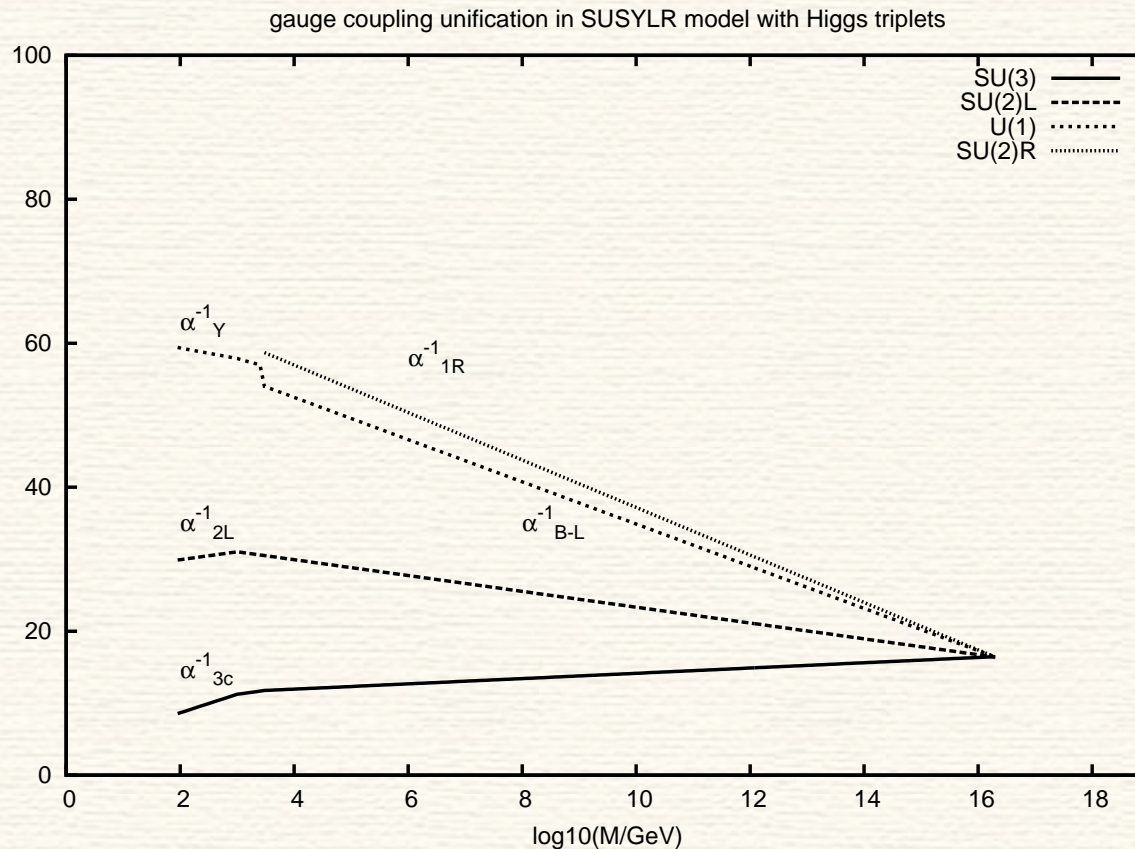
A simulated domain walls in a Left-Right symmetric model(A. Sarkar, UAY)

Can this lepton asymmetry with  $M_{B-L} \ll M_R$  survive?

Yes! ( [Narendra Sahu and UAY 2005](#) )



# Unification ... conditional (eat the cake too)



Gauge coupling unification in the MSLRM ([Debasish Borah & UAY 2010](#))

- Breaking of  $U(1)_{B-L}$  can be as low as 3 TeV
- Need to add new scalars at a higher scale. (Explored exhaustively – [Kopp, Lindner, Niro, Underwood 2009](#) )

# Parity breaking from Planck suppressed effects

Several caveats :

- Supergravity at the renormalisable level couples separately to the left sector and right sector with no mixing terms.
- It is very difficult to see how gravitational instanton effects will necessarily impact this discrete symmetry
  - However gravity horizons known to violate global symmetries
- Assume an unknown reason for (spontaneous) breaking of parity in the hidden sector, communicated by gravity.
- Use Kähler potential as the guide.

## Removal of domain walls : baby version

For the theory of a generic neutral scalar field  $\phi$ , the effective higher dimensional operators can be written as (Rai and Senjanovic)

$$V_{eff} = \frac{C_5}{M_{Pl}} \phi^5 + \frac{C_6}{M_{Pl}^2} \phi^6 + \dots \quad (3)$$

In realistic theories, the structure of such terms conditioned by

- Gauge invariance and supersymmetry
- Presence of several scalar species
- The dynamics of domain walls



## Domain wall dynamics in radiation dominated phase

The dynamics of the walls is determined by two quantities :[Kibble; Vilenkin]

- \*. Tension force  $f_T \sim \sigma / R$ , where  $\sigma$  is energy per unit area and  $R$  is the average scale of radius of curvature
- \*. Friction force  $f_F \sim \beta T^4$  for walls moving with speed  $\beta$  in a medium of temperature  $T$ .

Some dimensional analysis and “R2C2E<sup>1</sup>” yields,

$$\delta \rho \geq G \sigma^2 \approx \frac{M_R^6}{M_{Pl}^2} \sim M_R^4 \frac{M_R^2}{M_{Pl}^2} \quad (4)$$

---

1. “Reasoning too complicated to explain” in a short review; paraphrasing S. Rushdie, “Haroun and the Sea of Stories”

## Domain wall dynamics : matter domination

[Kawasaki and Takahashi(2004), Anjishnu Sarkar and UAY(2006)]

Assume the initial wall complex relaxes to roughly one wall per horizon at a Hubble value  $H_i$  with the initial energy density in the wall complex  $\rho_W^{(in)} \sim \sigma H_i$

Let the temperature at which the domain walls are formed be  $T \sim \sigma^{1/3}$ . So

$$H_i^2 = \frac{8\pi}{3} G \sigma^{\frac{4}{3}} \sim \frac{\sigma^{\frac{4}{3}}}{M_{Pl}^2} \quad (5)$$

Thus we can set  $M_{Pl}^{-2} T_D^4 \sim H_{eq}^2 \sim \sigma^{\frac{3}{4}} H_i^{\frac{1}{4}} M_{Pl}^{-3}$ . The corresponding temperature permits the estimate of the required pressure difference,

$$\delta\rho > M_R^4 \left( \frac{M_R}{M_{Pl}} \right)^{3/2} \quad (6)$$

Thus in this case we find  $(M_R / M_{Pl})^{3/2}$  a milder suppression factor than in the radiation dominated case above.

## Planck scale terms in ABMRS model

[ Sasmita Mishra and UAY 2010]

$$V_{eff}^R \sim \frac{a(c_R + d_R)}{M_{Pl}} M_R^4 M_W + \frac{a(a_R + d_R)}{M_{Pl}} M_R^3 M_W^2$$

and likewise  $R \leftrightarrow L$ . Hence,

$$\delta\rho \sim \kappa^A \frac{M_R^4 M_W}{M_{Pl}} + \kappa'^A \frac{M_R^3 M_W^2}{M_{Pl}}$$

$$\kappa_{RD}^A > 10^{-10} \left( \frac{M_R}{10^6 \text{GeV}} \right)^2$$

- For  $M_R$  scale tuned to  $10^9 \text{GeV}$  (gravitino constraint),  $\kappa_{RD} \sim 10^{-4}$
- but  $\kappa_{RD}^A \sim 10^8$  (highly unnatural) if  $M_R \sim 10^{15} \text{GeV}$

For walls which live through MD era or era off oscillating inflaton,

$$\kappa_{MD}^A > 10^{-2} \left( \frac{M_R}{10^6 \text{GeV}} \right)^{3/2},$$

- again,  $M_R \sim 10^9 \text{GeV} \Rightarrow \kappa_{MD} > 10^{5/2}$ , unnatural and worse for GUT.

Thus removal of domain walls imposes an upper bound on  $M_R$  and strongly suggests the scale is unrelated to GUT.

## Conclusions and caveats

- Thermal leptogenesis is viable and appealing  $\rightarrow$  lives necessarily at high scale and in tension with other favorite themes
- JBSM Minimal SUSY Left-Right model as an appealing model to compare PeV scale phenomena against :
  - UV completion through SUSY / extra dimensions
  - Leptogenesis through L-R domain walls  $\rightarrow$  robust conclusion about the nature of phase transition
  - Domain wall removal provides upper bound on  $M_N$
  - A very low  $B - L$  scale possible
  - Acknowledgment : Narendra Sahu, Anjishnu Sarkar, Sasmita Mishra, Debasish Borah.

$\Rightarrow$  Next page



*Dankeshön!*



Typeset using  $\text{TEX}_{\text{MACS}}$