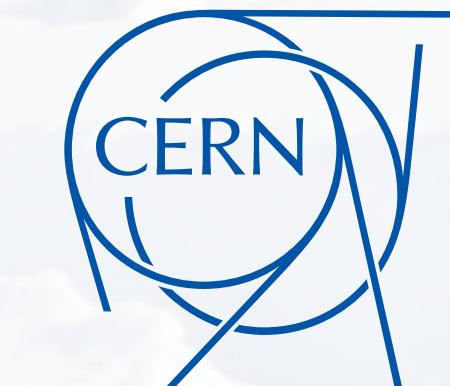


# Charm quarks from production to hadronisation in heavy-ion collisions



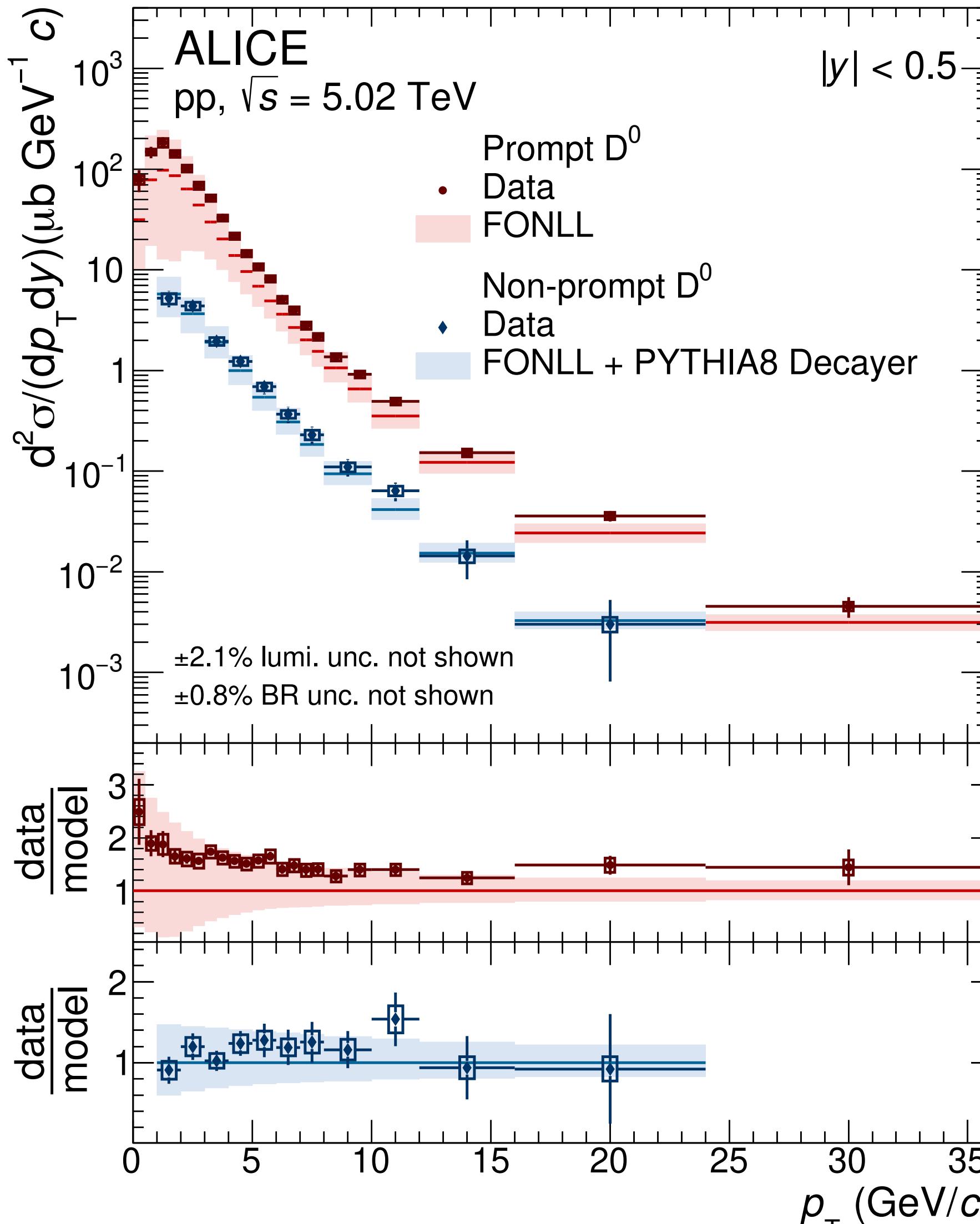
Fabrizio Grosa  
CERN

59<sup>th</sup> International Winter Meeting on Nuclear Physics  
*Bormio | 26/01/2023*

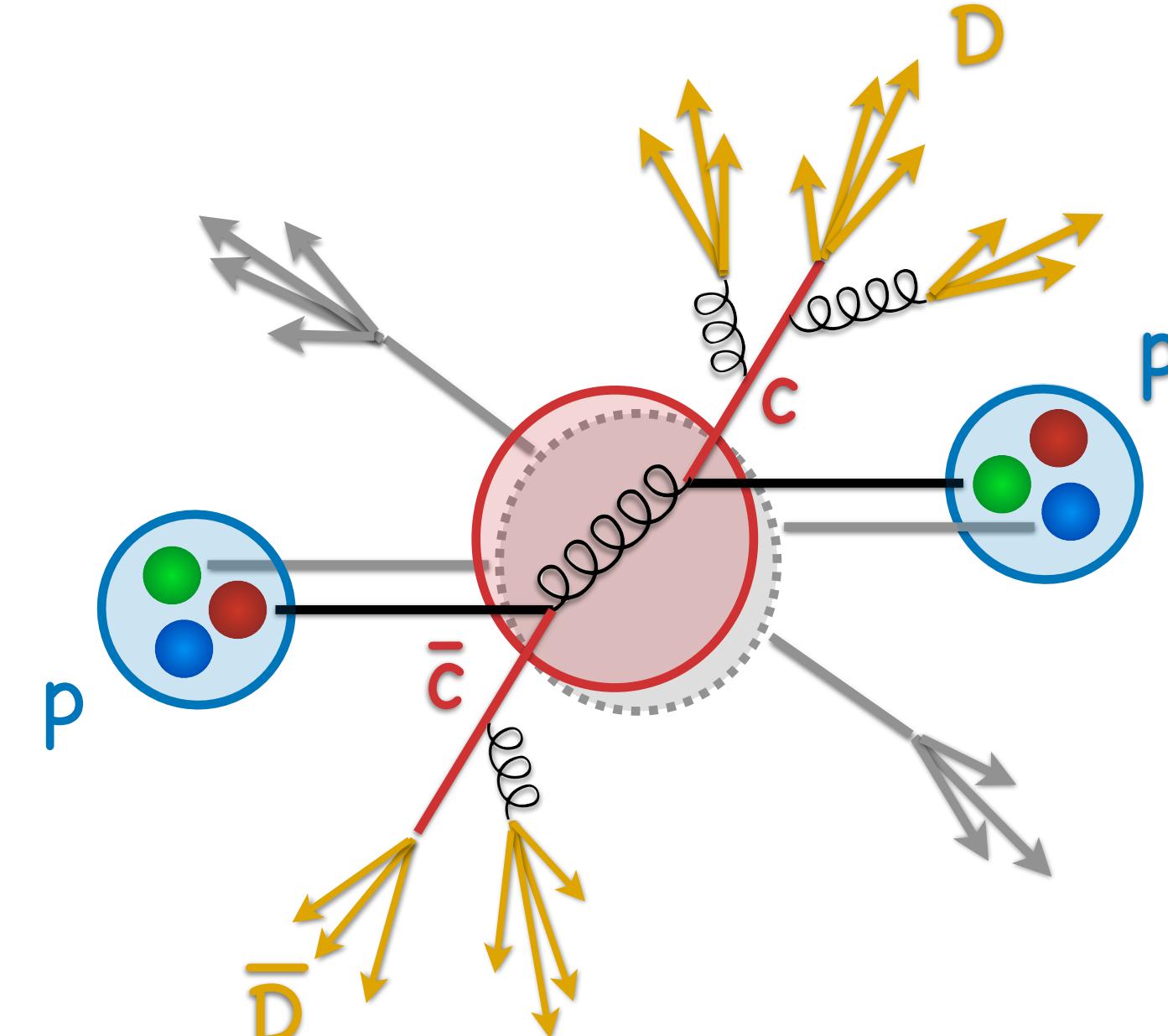
# Production of heavy quarks in proton–proton collisions

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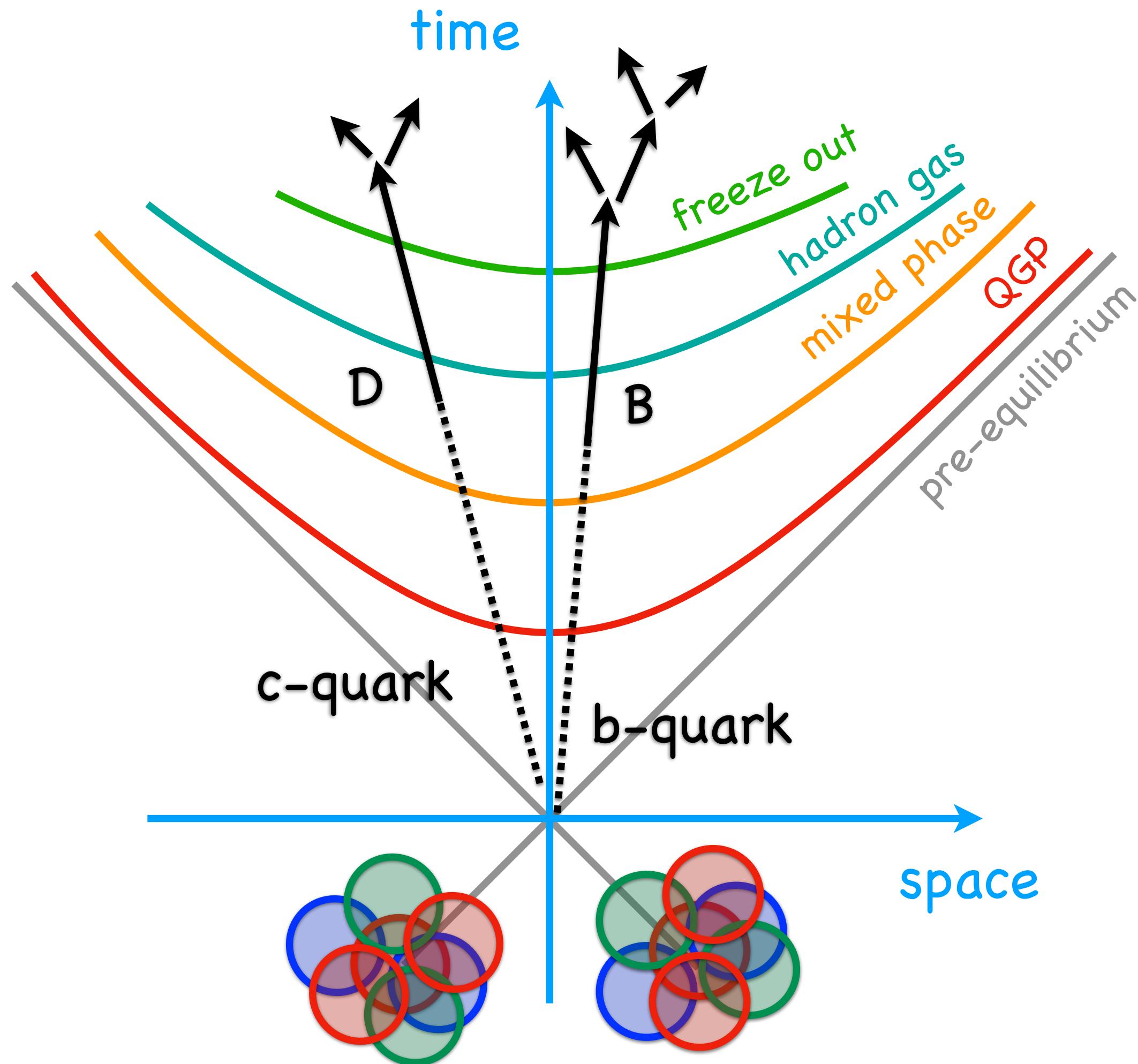


- Charm and beauty quarks are produced in hard-scattering processes
- perturbative QCD calculations based on the factorisation theorem



$$\sigma_{hh \rightarrow Hh} = \text{PDF}(x_a, Q^2) \text{ PDF}(x_b, Q^2) \otimes \sigma_{ab \rightarrow q\bar{q}} \otimes D_{q \rightarrow h}(z_q, Q^2)$$

Parton distribution functions (non perturbative)      Partonic cross section (perturbative)      Fragmentation functions (non perturbative)

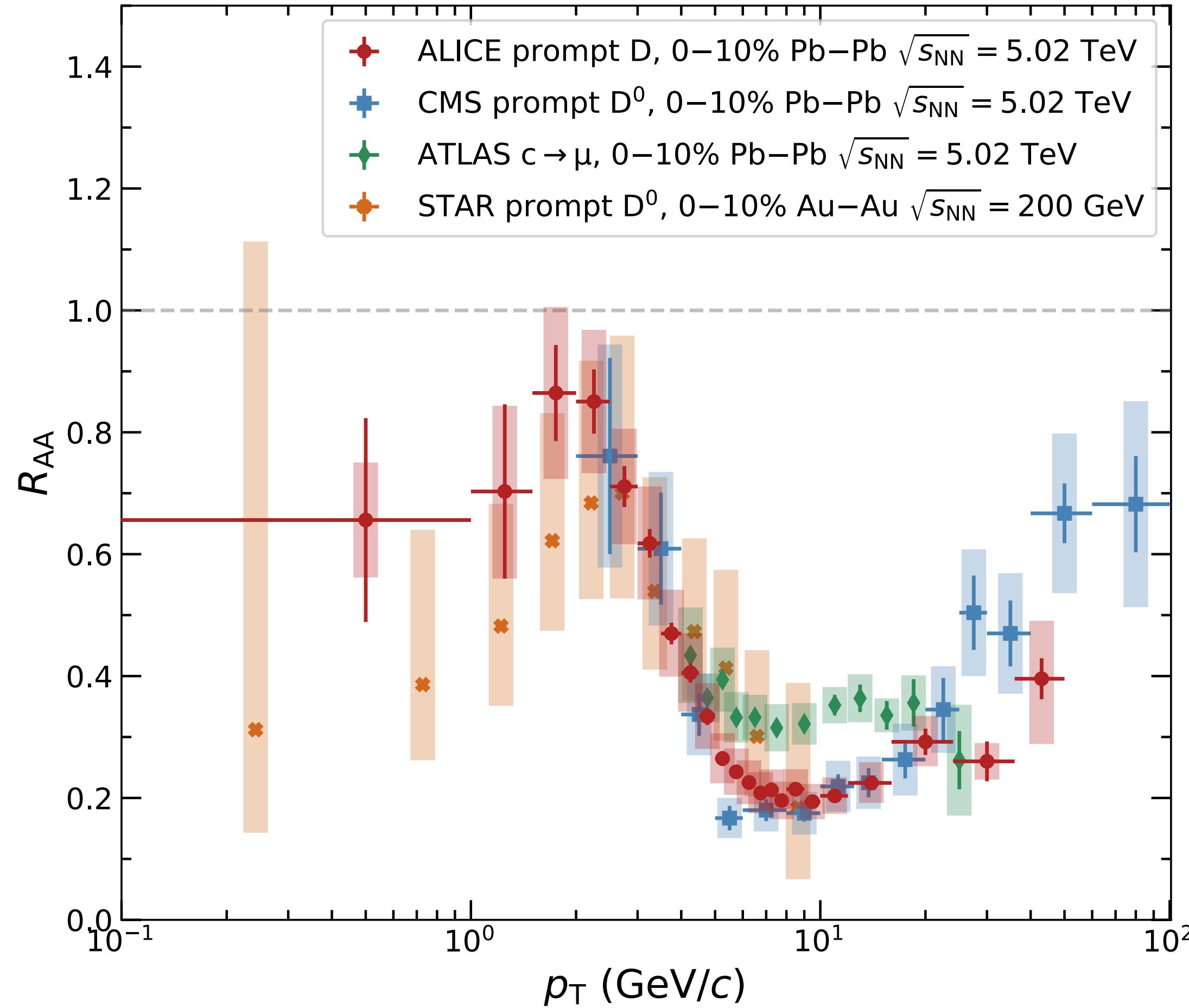


- Lattice QCD calculations predict a phase transition from the ordinary nuclear matter to a *quark-gluon plasma* (QGP)
  - very high energy density  $\varepsilon > 15 \text{ GeV/fm}^3$
  - after a pre-equilibrium phase expands hydrodynamically
- Heavy quarks: produced in shorter time scales than QGP
  - $\tau_{\text{HF}} \lesssim \hbar/m \approx 0.05\text{-}0.1 \text{ fm}/c$  depending on  $p_T$
  - $\tau_{\text{QGP form (LHC)}} \approx 0.3 \text{ fm}/c$
- Low- $p_T$ :
  - Multiple elastic collisions with the medium constituents
    - ▶ Diffusion (Brownian) motion
    - ▶ Possible (partial) thermalisation in the medium
- High- $p_T$ :
  - Radiative energy loss (gluon emission)
  - ▶ Study properties of in-medium energy loss

PRC 89 (2014) 034906

# The main observables

$$\text{Nuclear modification factor } R_{\text{AA}} = \frac{dN_{\text{AA}}/dp_T}{\langle N_{\text{coll}} \rangle \cdot dN_{\text{pp}}/dp_T}$$



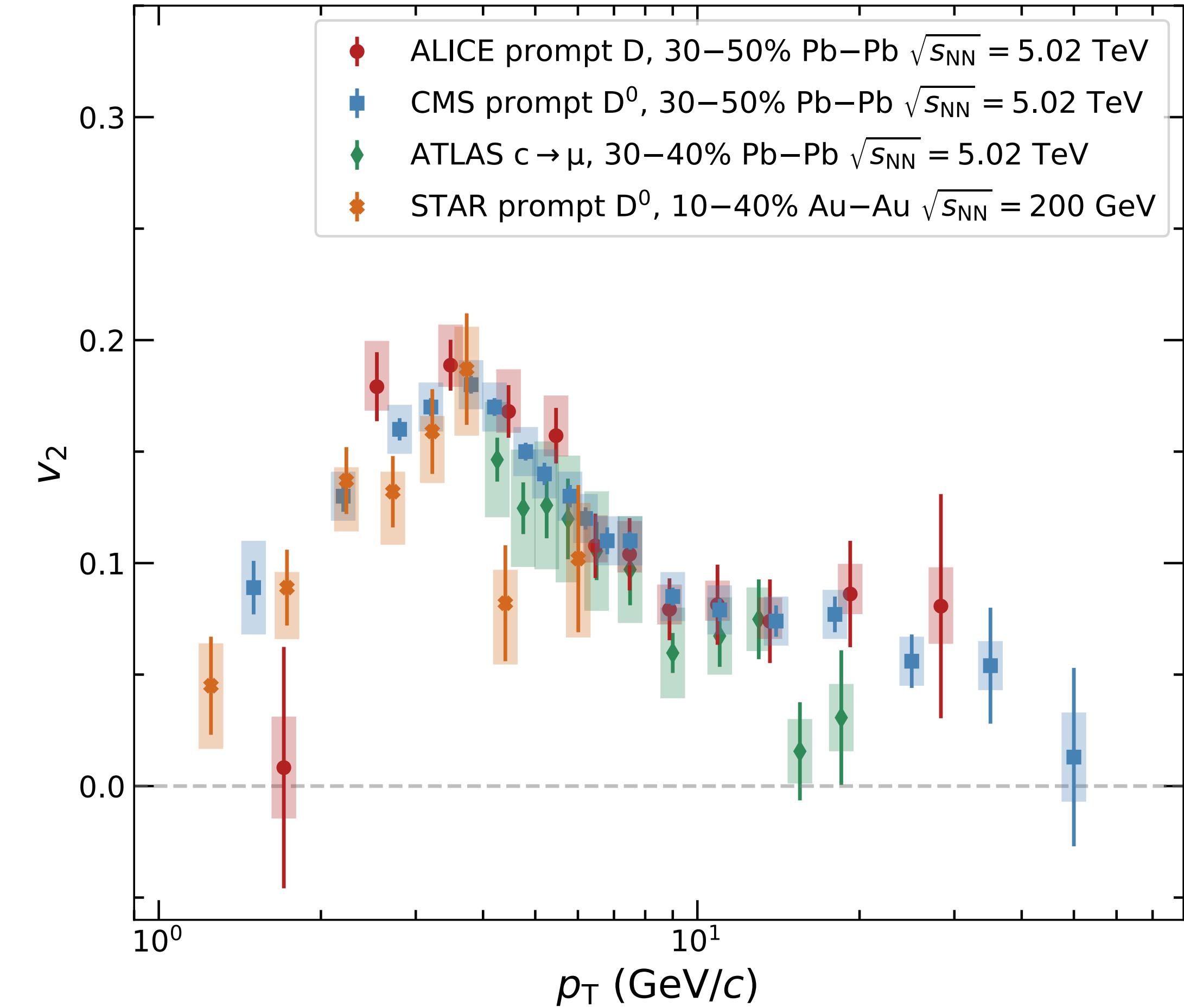
ALICE, JHEP 01 (2022) 174

ALICE, PLB 813 (2021) 136054

ATLAS, PLB 829 (2022) 137077

ATLAS, PLB 807 (2020) 135595

$$\text{Elliptic flow } v_2 = \langle \cos 2(\varphi - \Psi_{\text{RP}}) \rangle$$



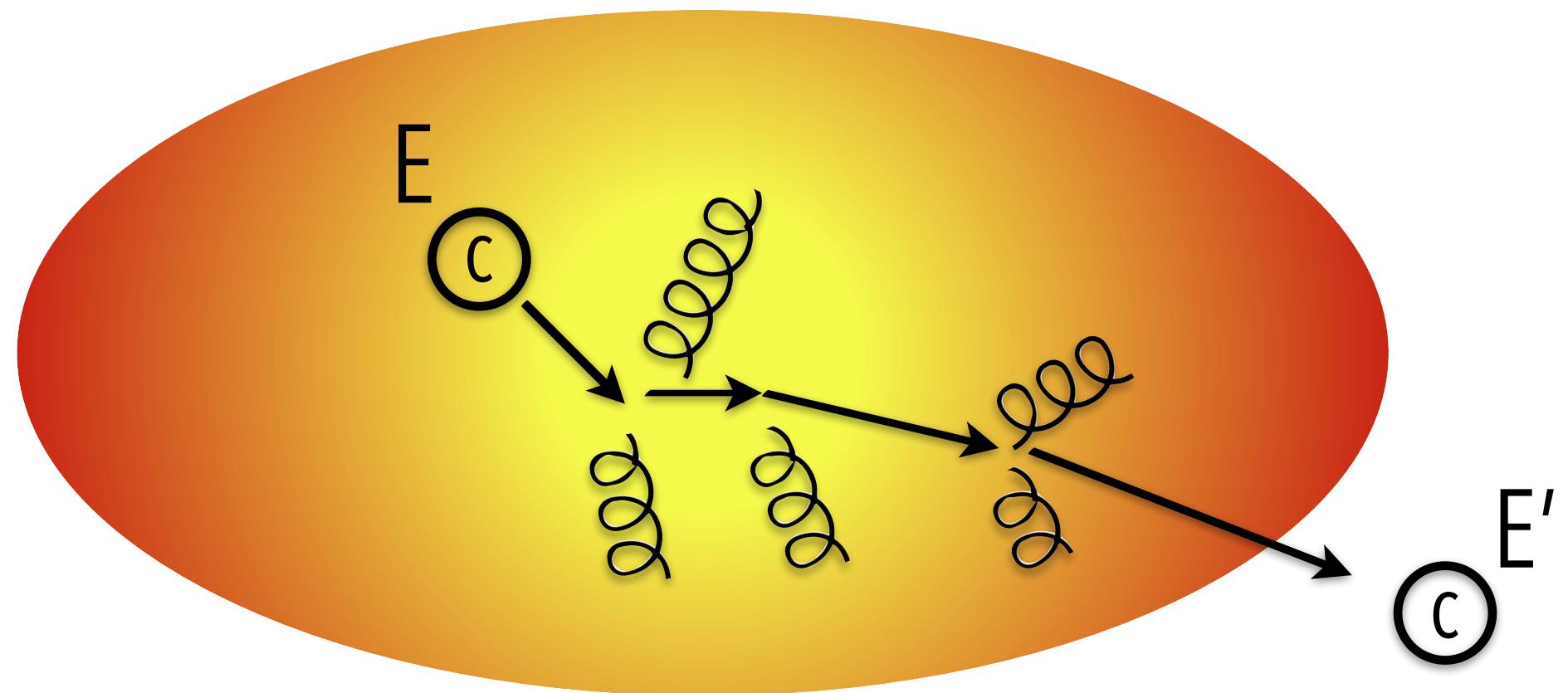
CMS, PLB 782 (2018) 474

CMS, PLB 816 (2021) 136253

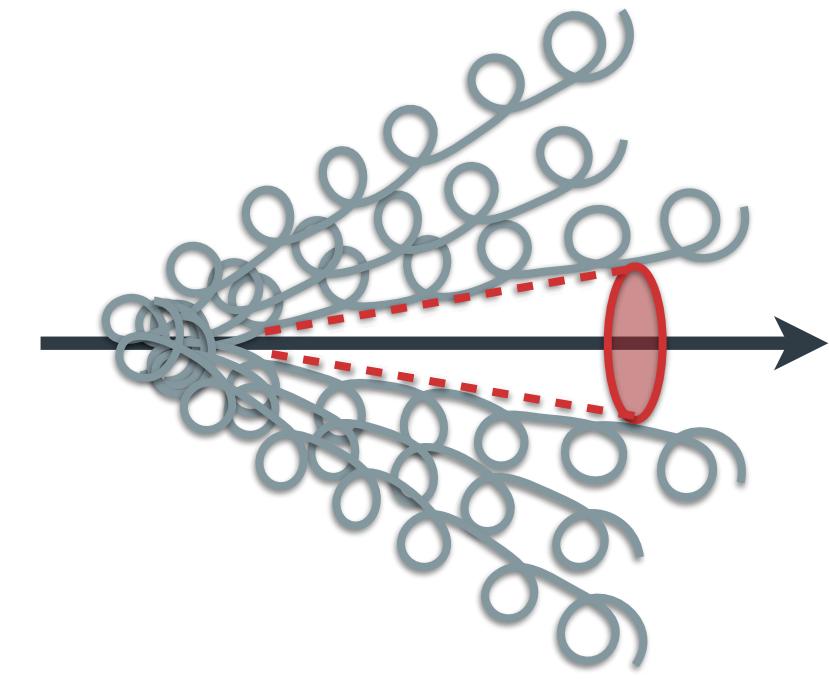
STAR, PRC 99 (2019) 34908

STAR, PRL 118 (2017) 212301

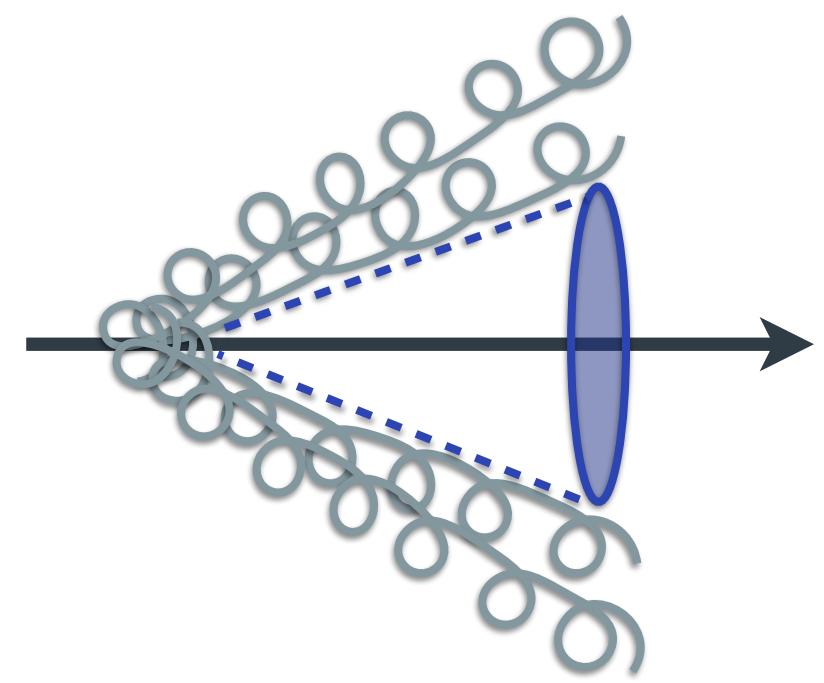
- Dominant effect: energy loss of charm and beauty quarks in the medium
- Goal: study the colour-charge and quark-mass dependence of the in-medium energy loss



small parton mass



large parton mass



Dead cone effect: gluon radiation suppressed at angles smaller than  $\vartheta < m/E$

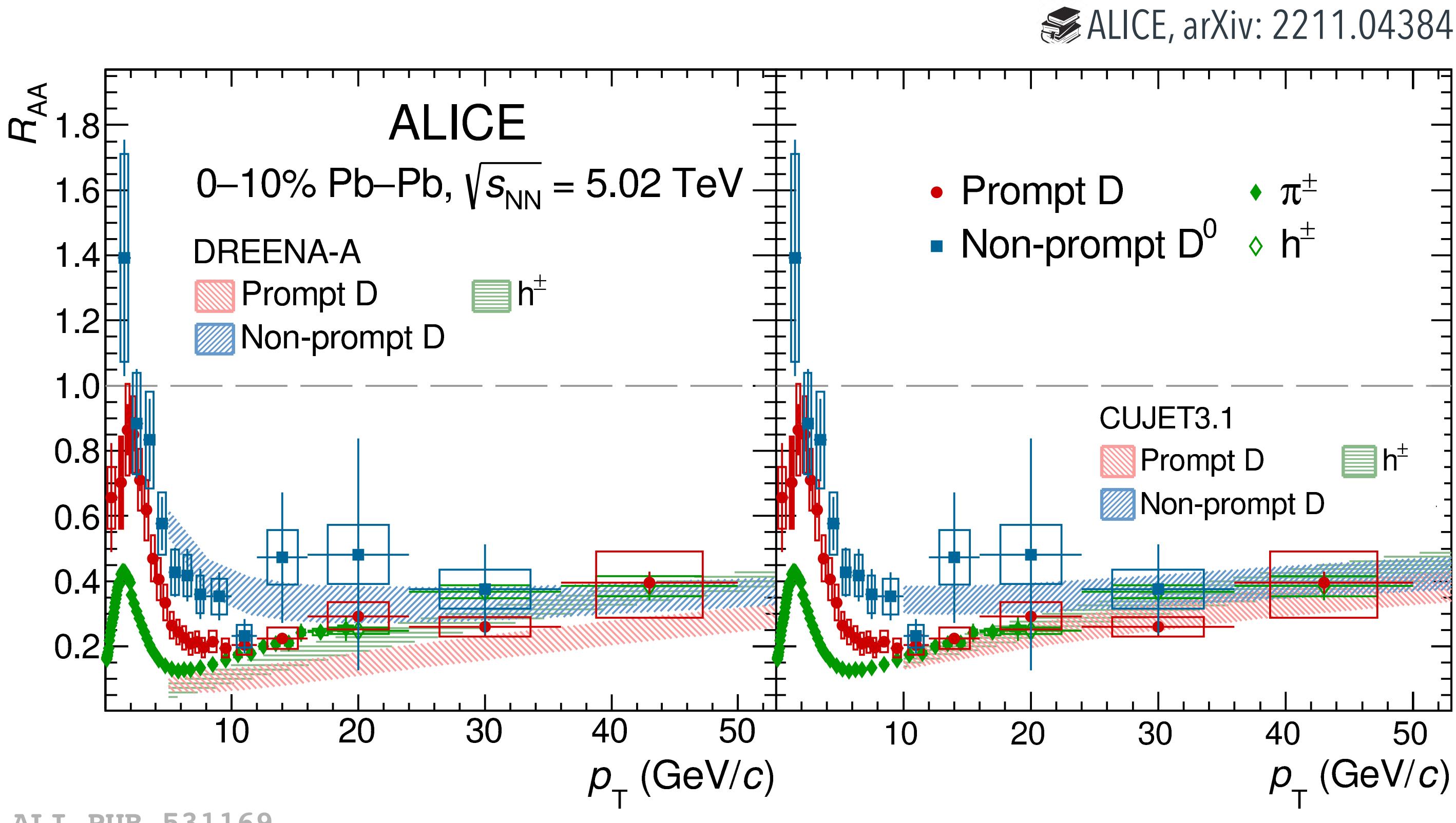
$$\langle \Delta E \rangle \propto \alpha_s C_R \hat{q} L^2$$

Strong coupling constant

Transport coefficient (average of the square of the transverse momentum exchanged with the QGP per unit mean free path)

Casimir factor = 3 for gluons and 4/3 for quarks

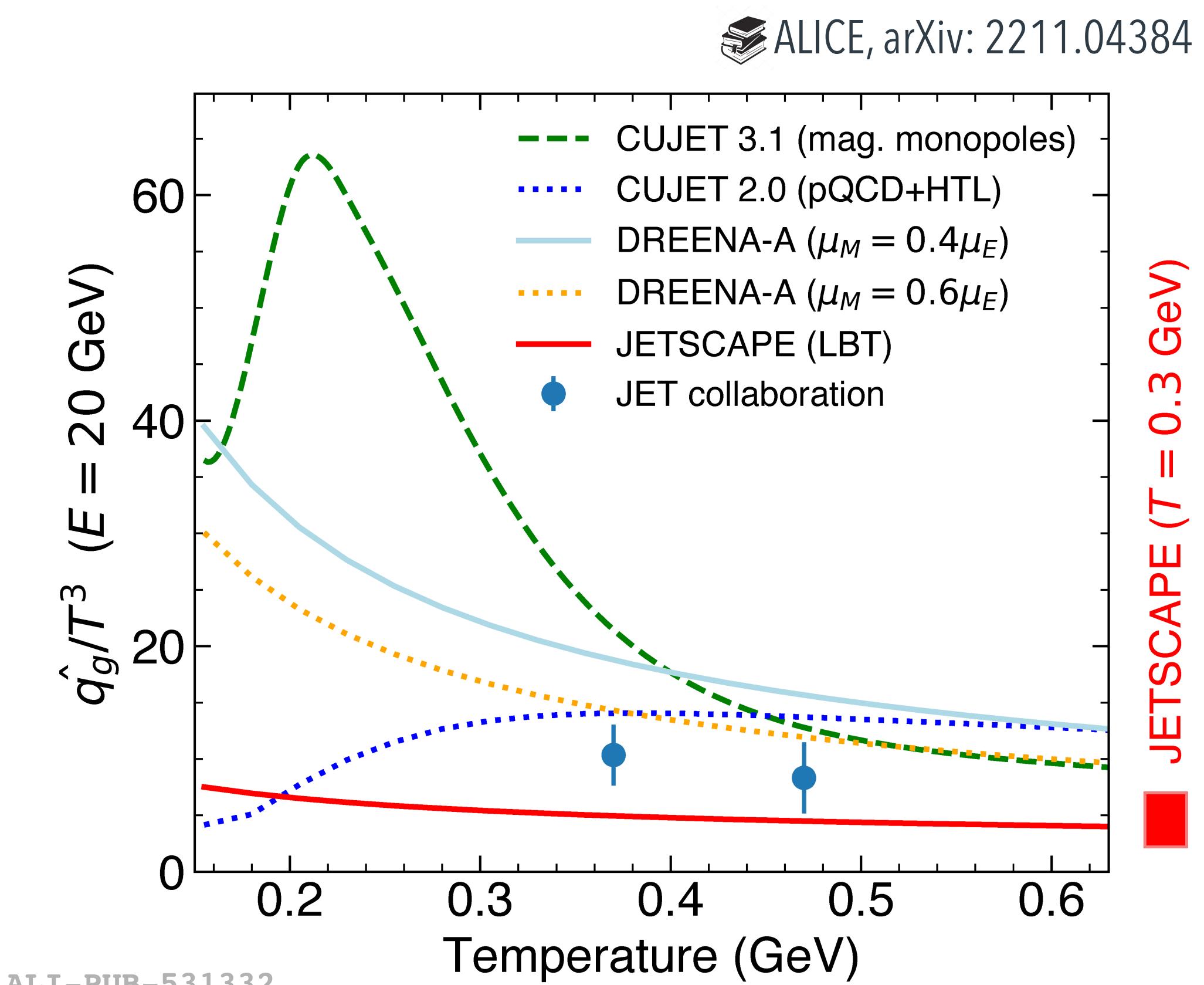
# The high- $p_T$ regime



- Data-to-model comparison seems to favour the scenario of weak coupling for high temperatures
- Less constraints for models at low temperatures
- Different observables needed

- Hierarchy of suppression as expected from dead cone effect

$$R_{AA}(b) > R_{AA}(c) \gtrsim R_{AA}(\text{light})$$



JETSCAPE ( $T = 0.3$  GeV)



- Models based on the charm-quark transport on a hydrodynamically expanding QGP
  - Typical momentum transfers in scatterings between charm quarks and medium constituents (heat bath) are small
  - Charm quarks undergo soft and incoherent collisions → Brownian motion
  - Boltzmann equation can be reduced to a Langevin or Fokker-Plank equation

$$\frac{\partial}{\partial t} f_Q(t, \mathbf{p}) = \frac{\partial}{\partial p^i} \left\{ A^i(\mathbf{p}) \cdot f_Q(t, \mathbf{p}) + \frac{\partial}{\partial p^j} [B^{ij}(\mathbf{p}) \cdot f_Q(t, \mathbf{p})] \right\}$$

- In case of a medium in thermal equilibrium
  - $A^i(\mathbf{p}) = A(\mathbf{p})p_i$  friction
  - $B^{ij}(\mathbf{p}) = B_0(p) \cdot P_{ij}^\perp(\mathbf{p}) + B_1(p) \cdot P_{ij}^\parallel(\mathbf{p})$  momentum broadening

- Brownian motion of heavy quarks in QGP governed by the coupling of heavy quarks to the medium
  - Spatial diffusion coefficient

$$D_s = \frac{T}{m_{\text{charm}} A(p=0)}$$



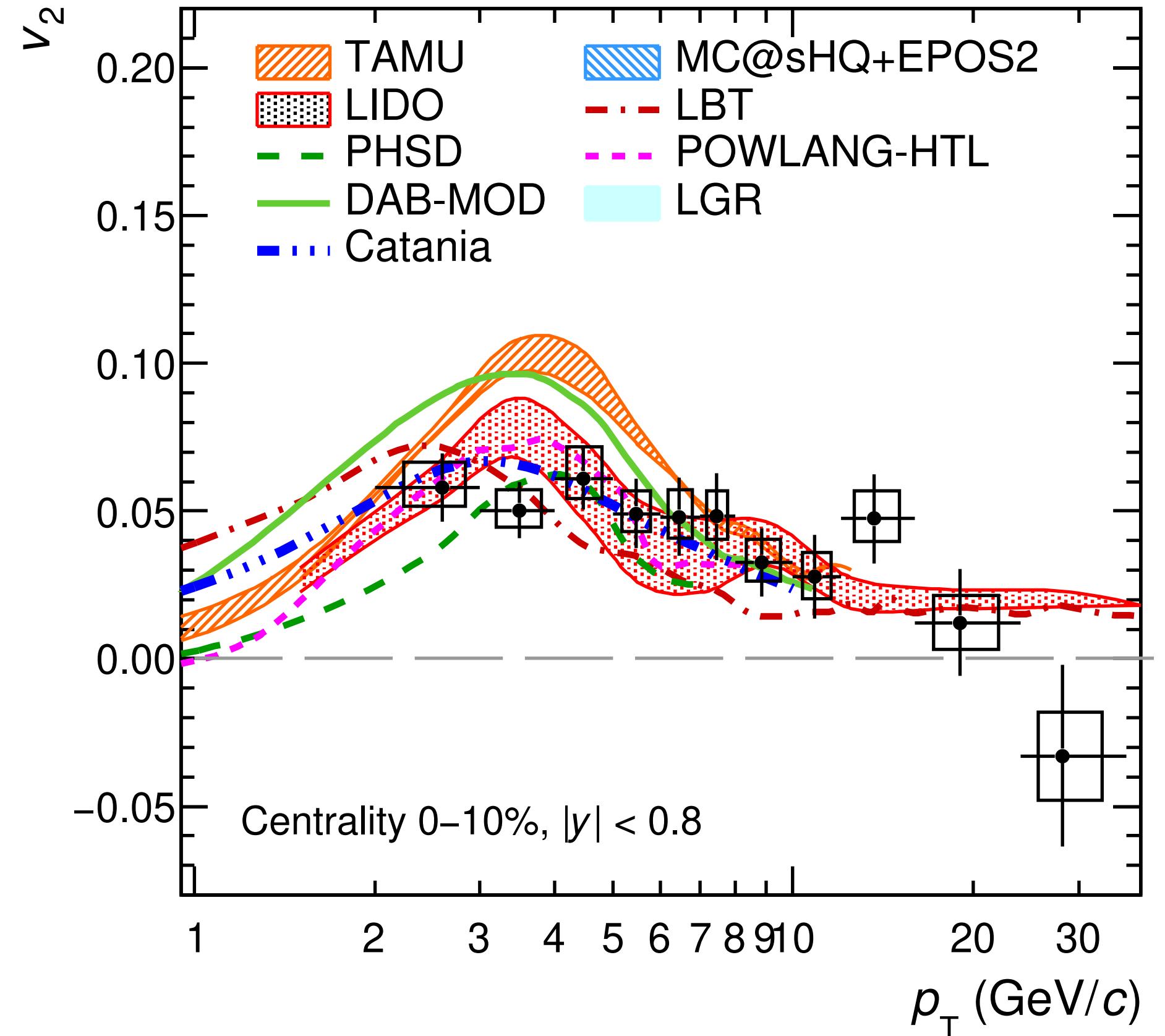
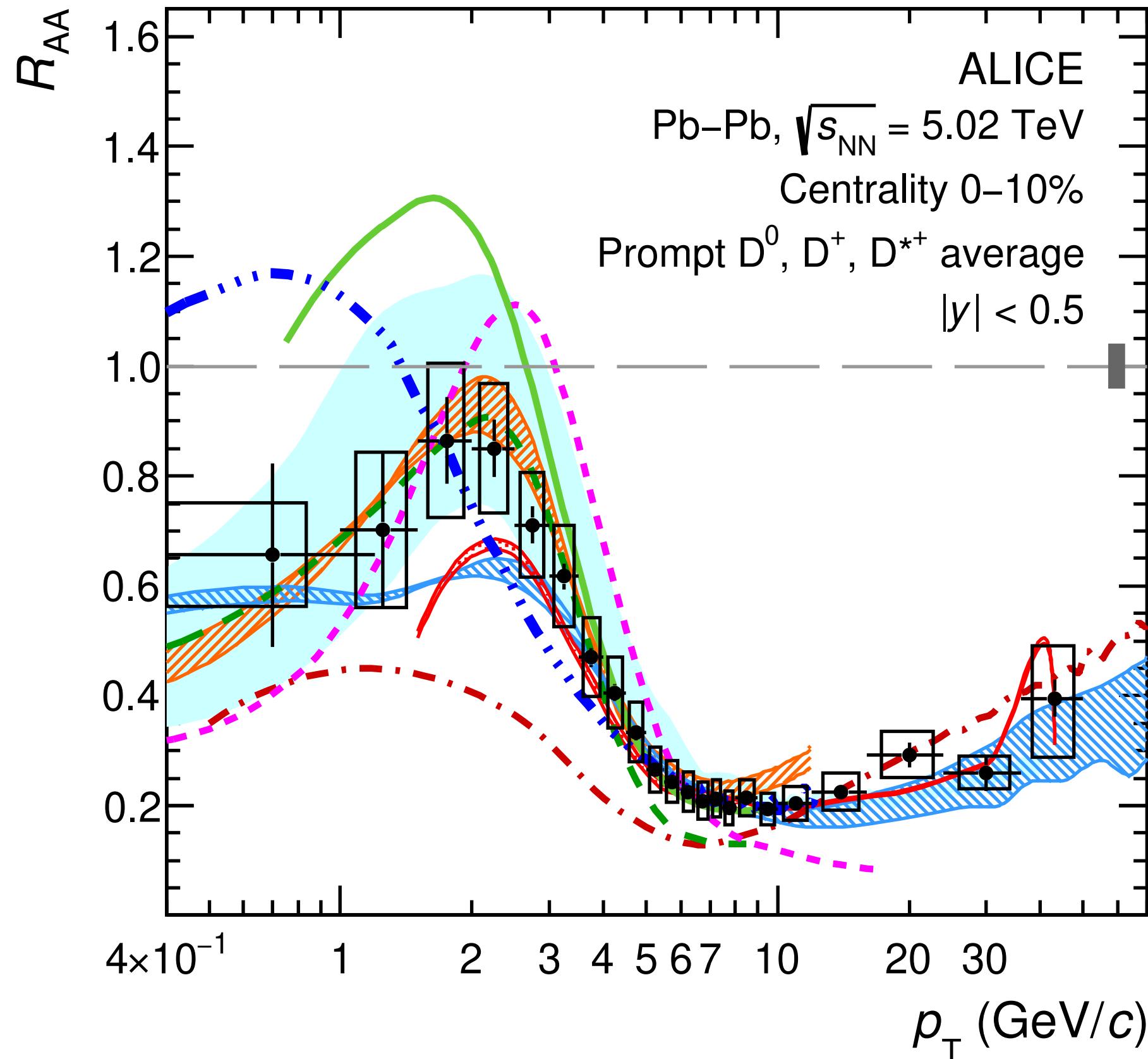
Related to the thermalisation time of the charm quark

Approximately  $A(p=0) \propto 1/m_{\text{charm}}$

$$\tau_{\text{charm}} = (m_{\text{charm}}/T) \cdot D_s$$

# Transport models for charm quarks

ALICE, JHEP 01 (2022) 174



- Additional model ingredients
- Initial state conditions
- Nuclear PDFs
- Hadronisation via different mechanisms
- Hadronic phase

TAMU: PRL 124 (2020) 042301  
MC@sHQ+EPOS2: PRC 89 (2014) 014905  
LGR: arXiv:1912.08965

LIDO: PRC 98 (2018) 064901  
PHSD: PRC 93 (2016) 034906  
Catania: PLB 805 (2020) 135460

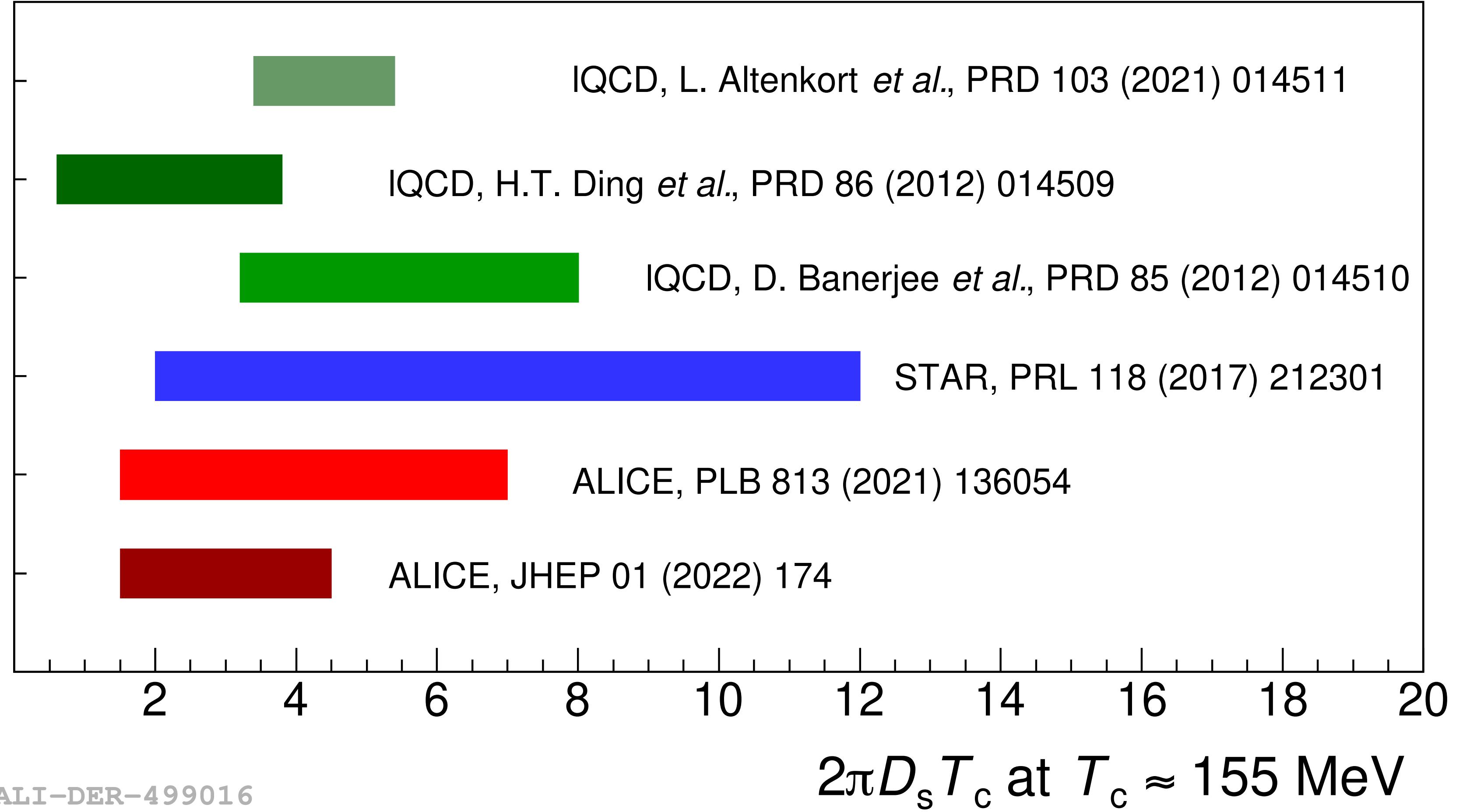
POWLANG: EPJC (2019) 79:494  
LBT: PRC 94 (2016) 014909  
DAB-MOD: arXiv:1906.10768

# Estimates of the spatial-diffusion coefficient

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ALICE, JHEP 01 (2022) 174



- Can we state that the transport coefficient in a model that describes the data is correct?

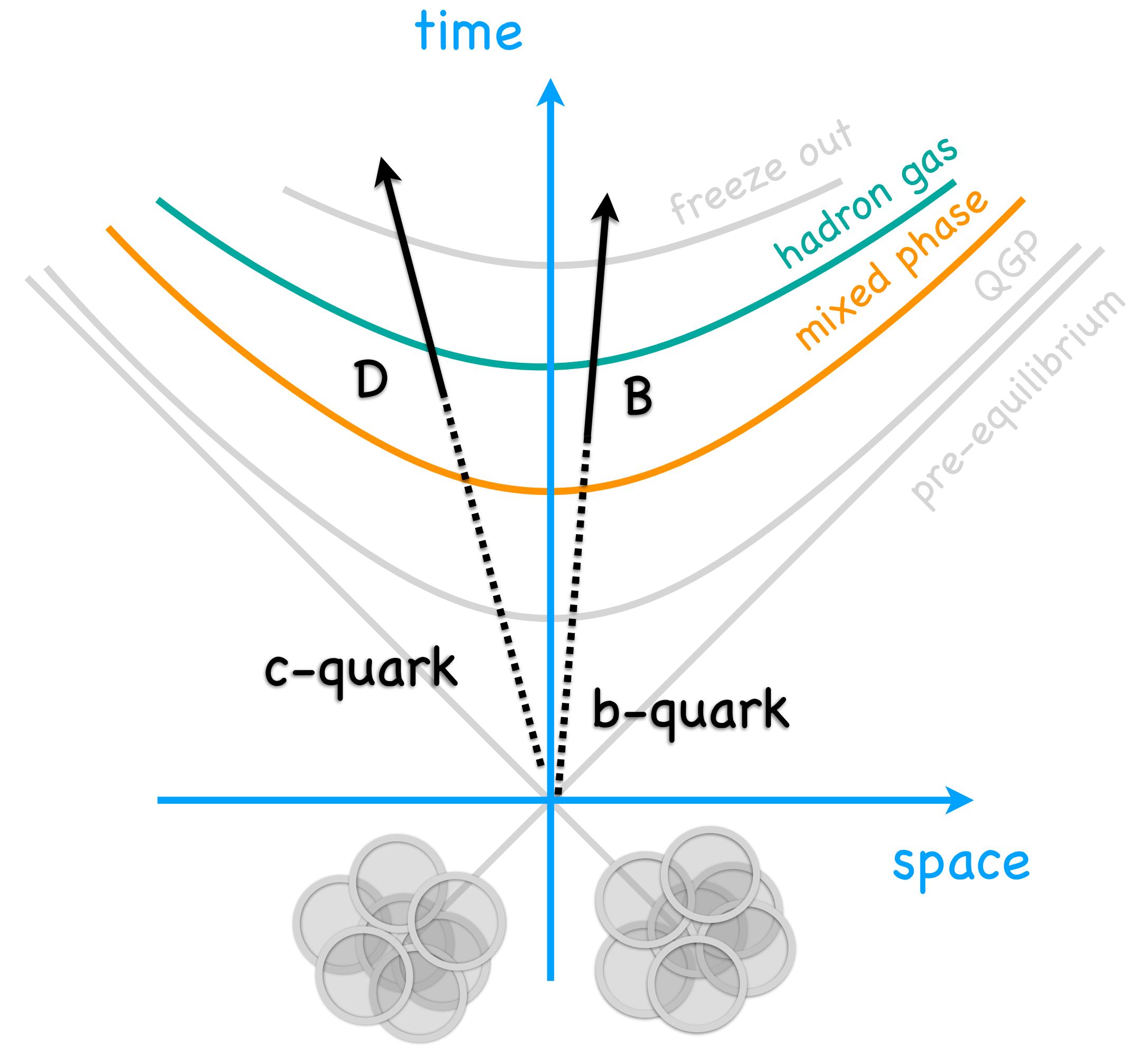
- Interval of spatial diffusion coefficient obtained by considering the values used in the transport models that reproduce the data
  - $2.5 < 2\pi D_s T_c < 4.5$  which corresponds to  $2 < \tau_{\text{charm}} < 6$  fm/c
  - Indicates a thermalisation time of the charm quark comparable with the QGP lifetime
  - Compatible with values obtained with QCD calculations on lattice

# Charm-quark hadronisation from the medium

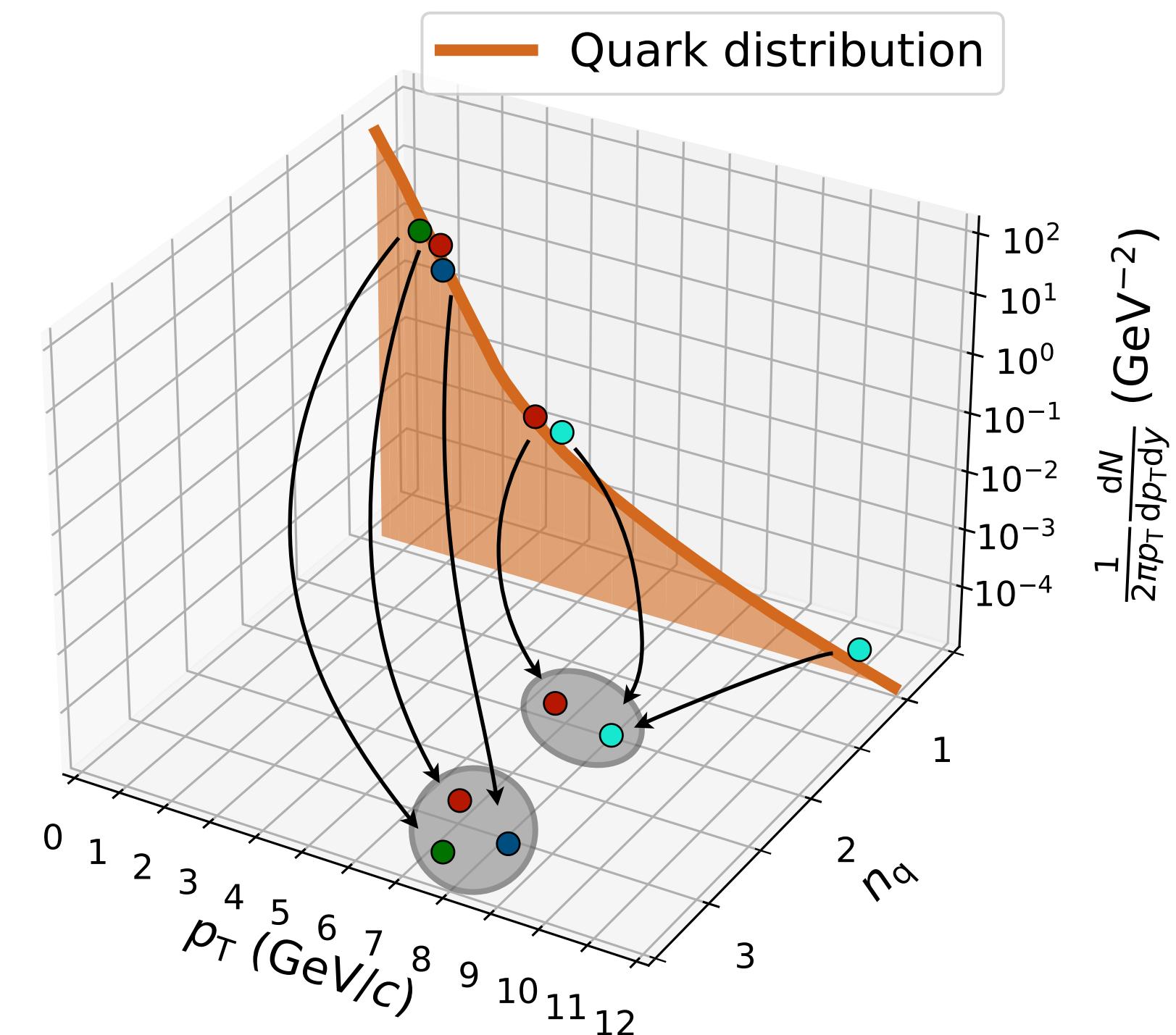
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- Hadronisation expected to be modified in presence of the colour-deconfined medium



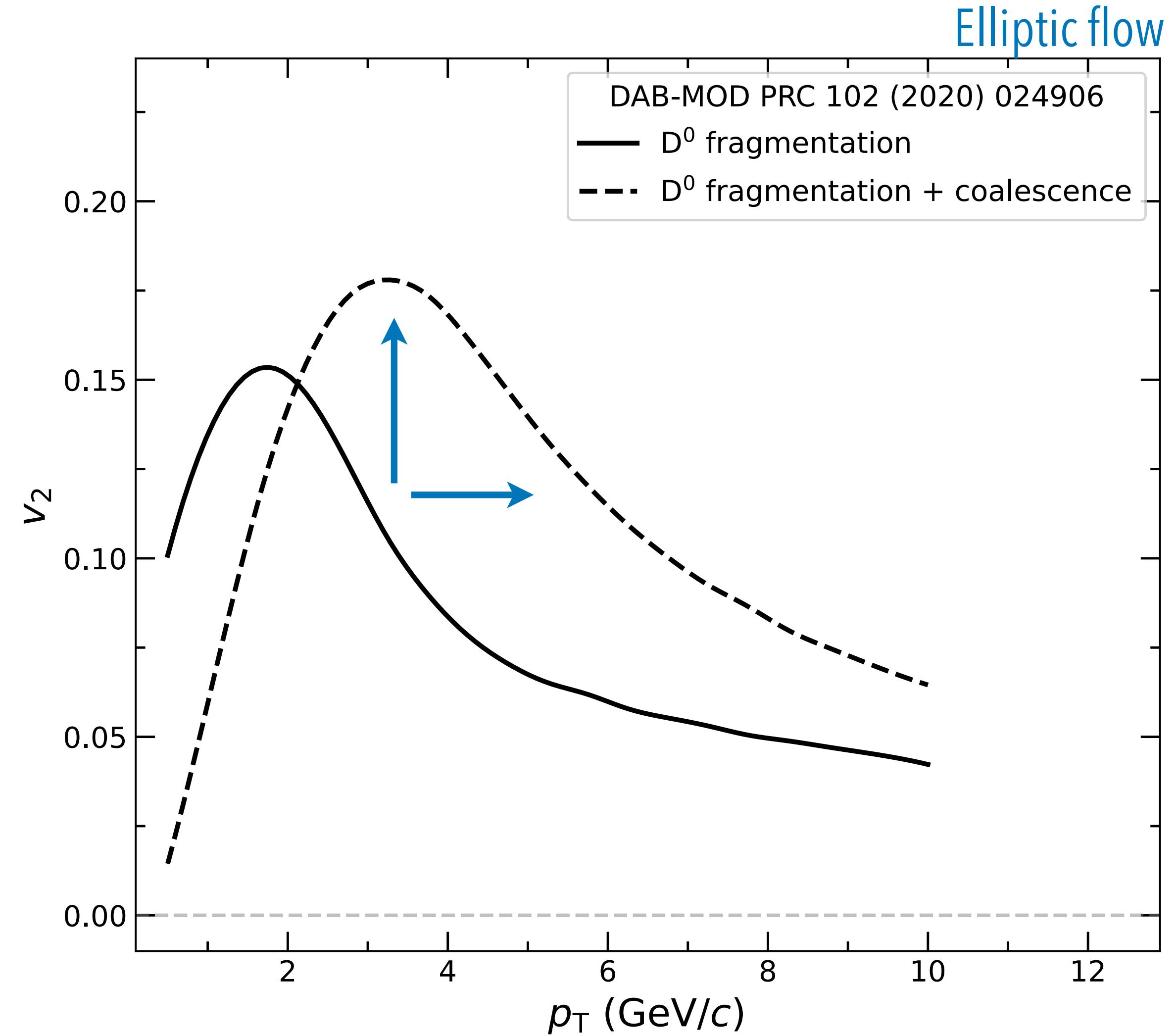
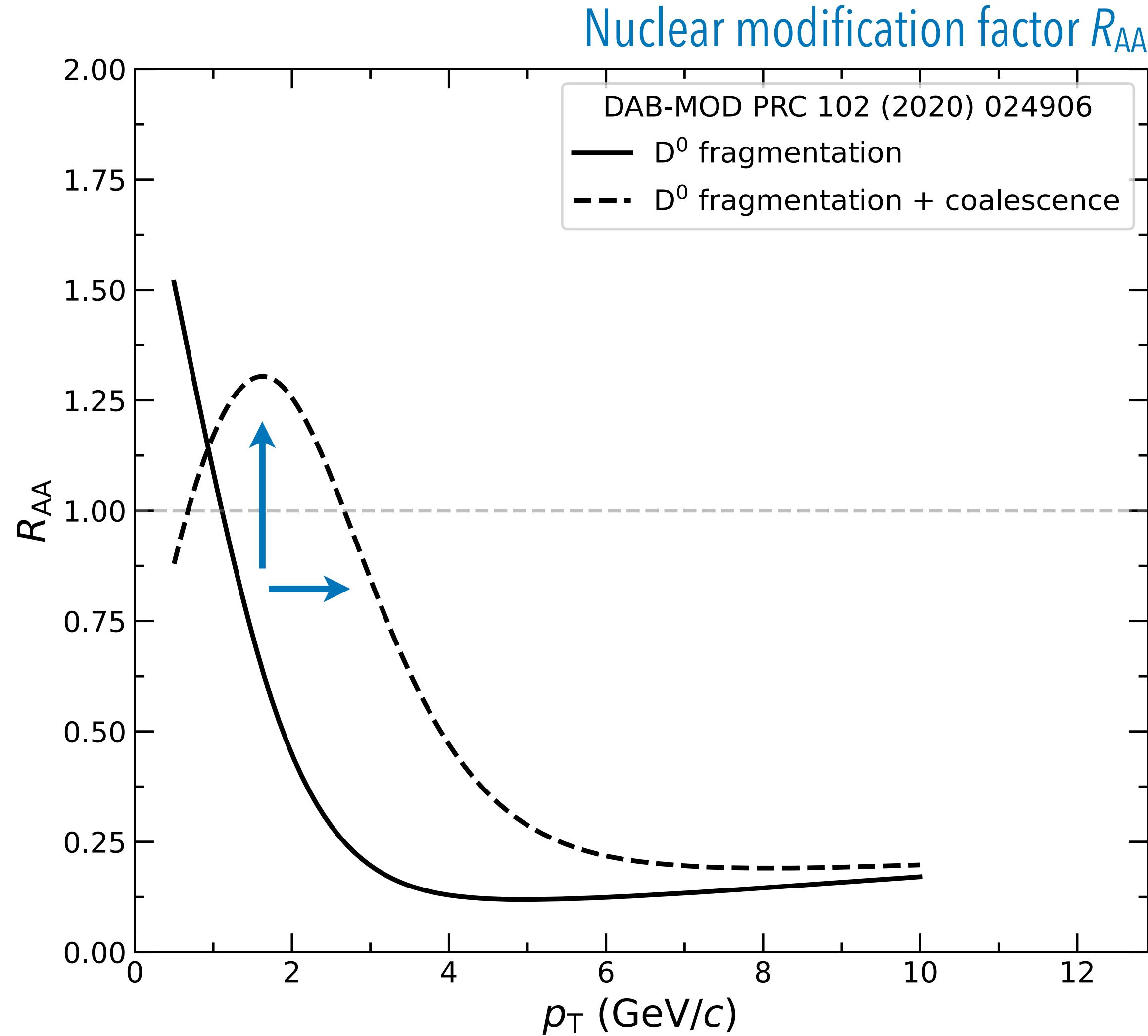
- (i) **Fragmentation  $D_{q \rightarrow h}(z_q, Q^2)$** 
  - A fraction of the parton momentum  $z_q$  is taken by the hadron
  - Can be modified by energy loss in the QGP
- (ii) **Recombination/coalescence**
  - Partons close in phase space can recombine
  - Enhances baryon-to-meson ratio at intermediate  $p_T$



# Charm-quark hadronisation from the medium

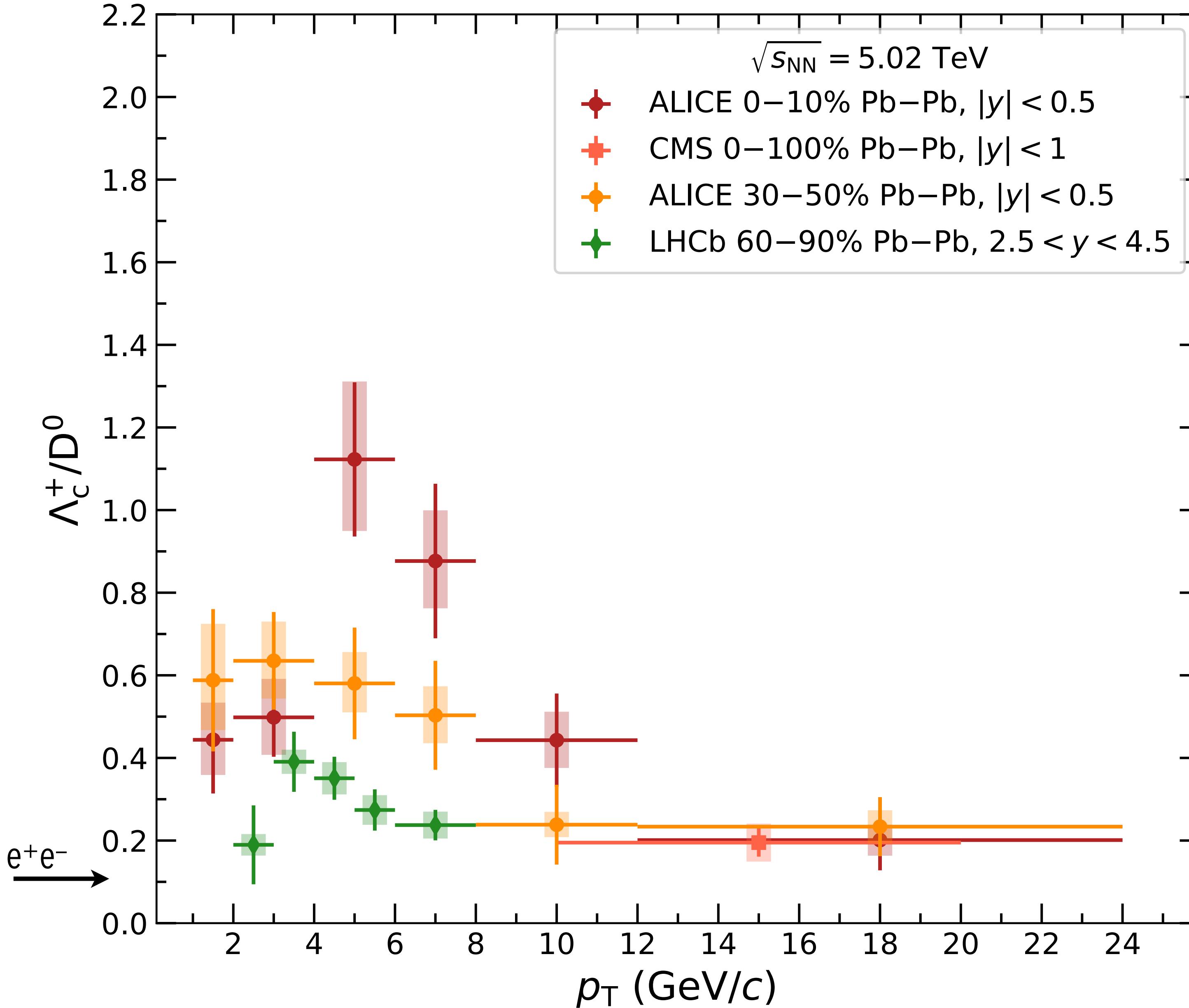
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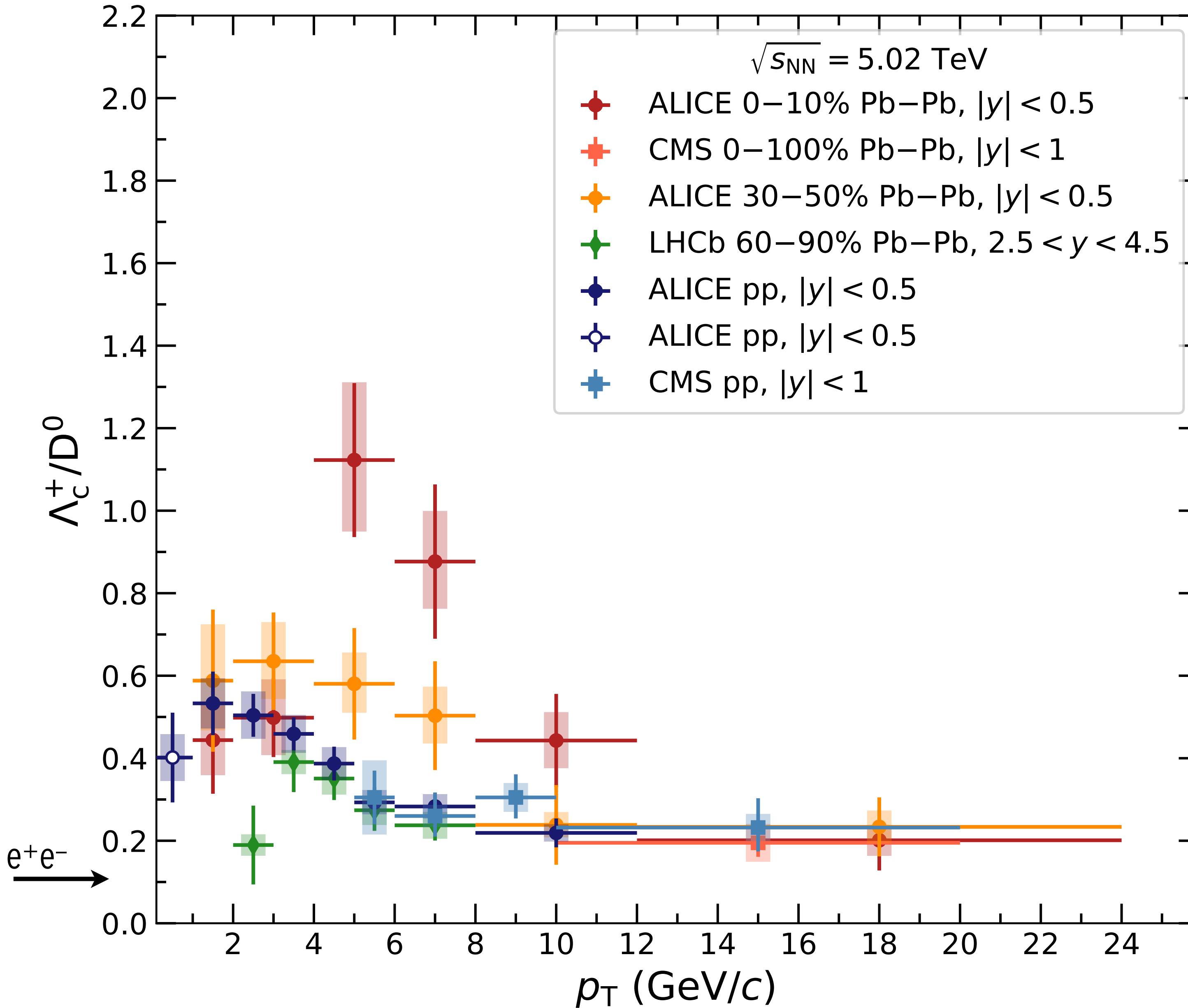
- Formation of a peak structure at intermediate  $p_T$

R. Katz et al, PRC 102 (2020) 024906



- $\Lambda_c^+/D^0$  ratio largely enhanced compared to  $e^+e^-$  and  $ep$  collisions
- $\Lambda_c^+/D^0$  ratio higher in more central collisions at intermediate  $p_T$ 
  - Higher probability of hadronisation via coalescence?
  - Radial flow?
  - Interplay of radial flow and coalescence?

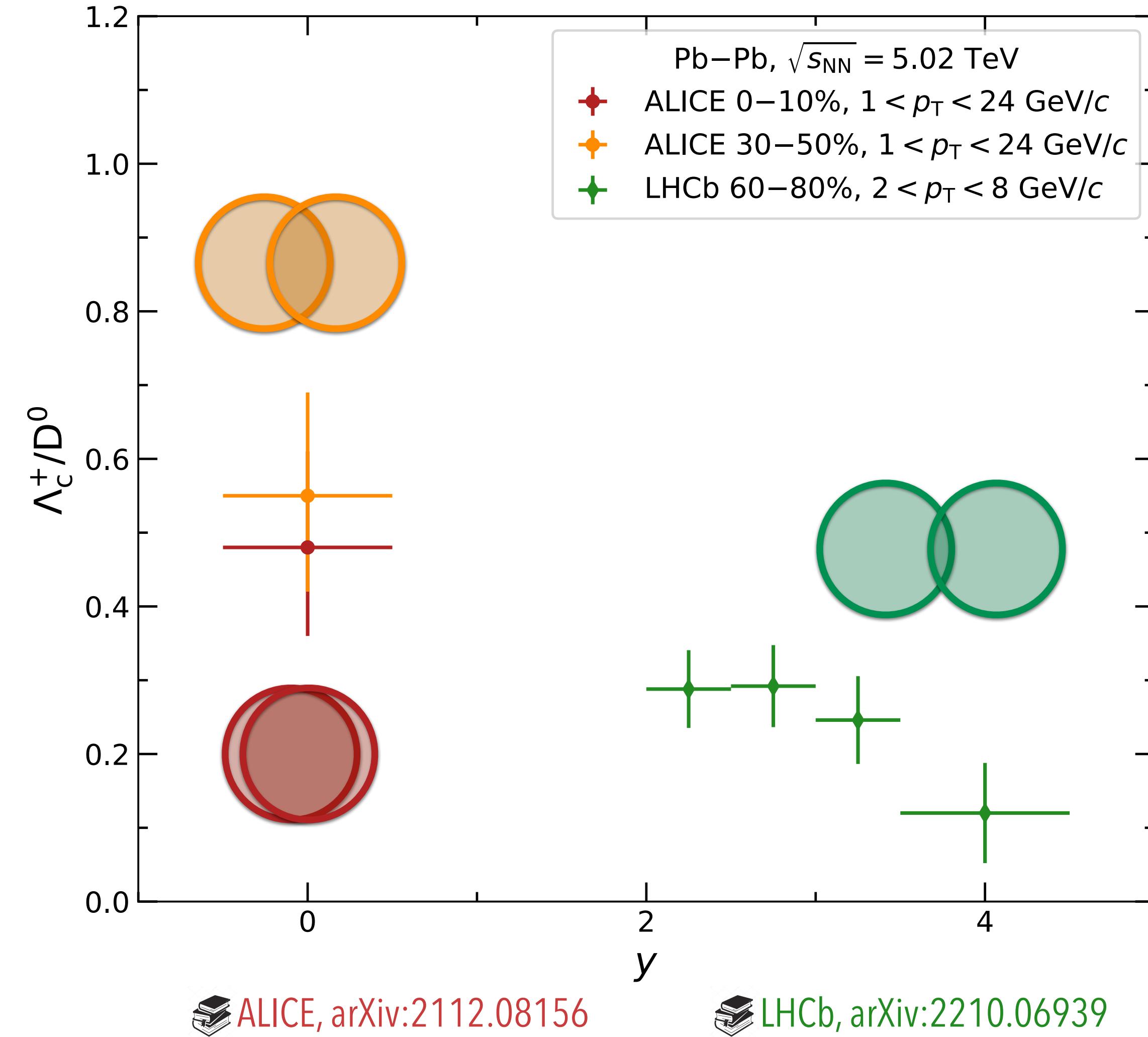
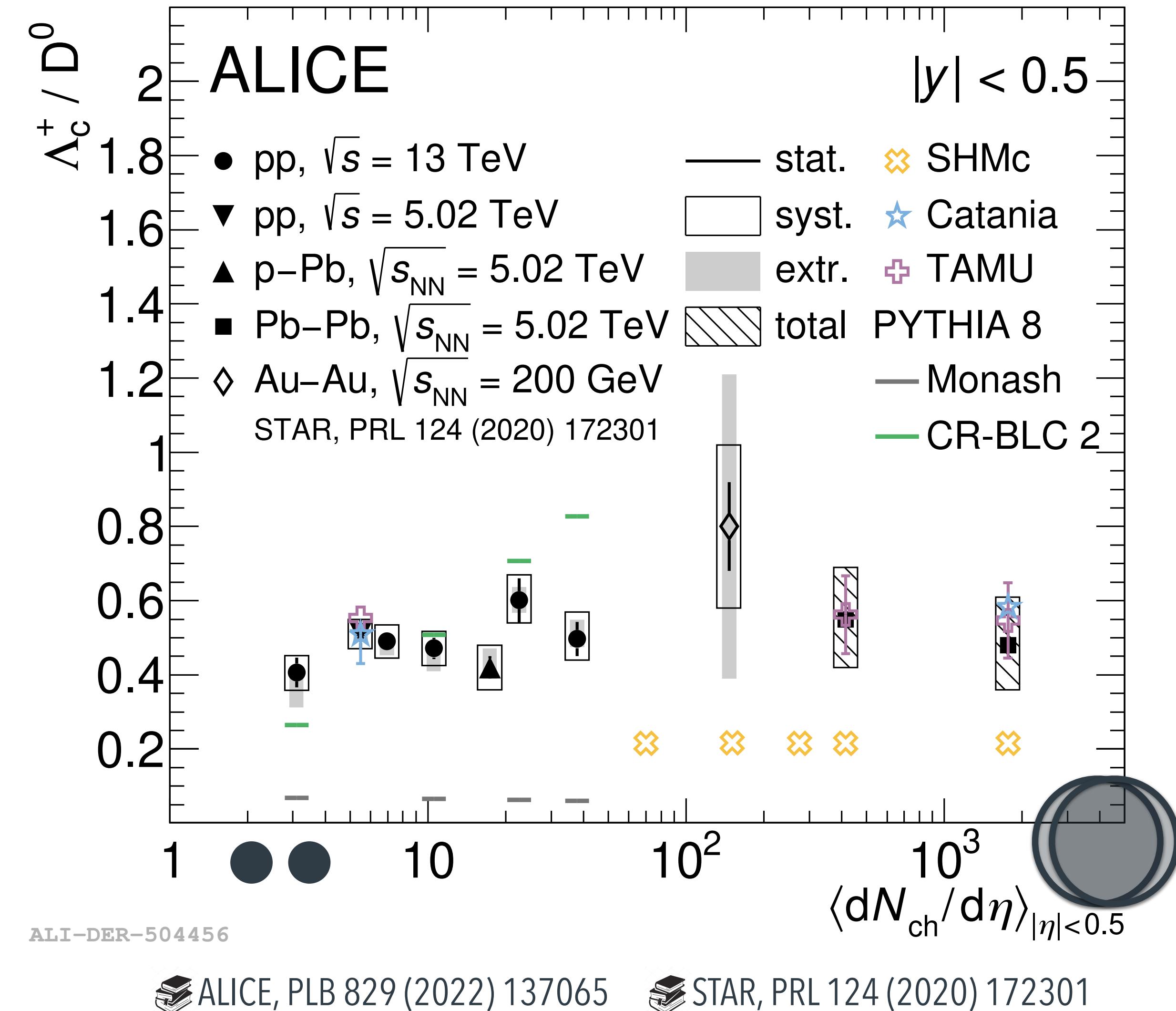




- $\Lambda_c^+/\bar{D}^0$  ratio largely enhanced compared to  $e^+e^-$  and ep collisions
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  - Higher probability of hadronisation via coalescence?
  - Radial flow?
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- 
- ALICE, arXiv:2112.08156
  - CMS, PLB 803 (2020) 135328
  - ALICE, arXiv:2112.08156
  - LHCb, arXiv:2210.06939
  - ALICE, PRL 127 (2021) 20, 202301
  - ALICE, arXiv:2211.14032
  - CMS, PLB 803 (2020) 135328

# Charm-quark baryonisation

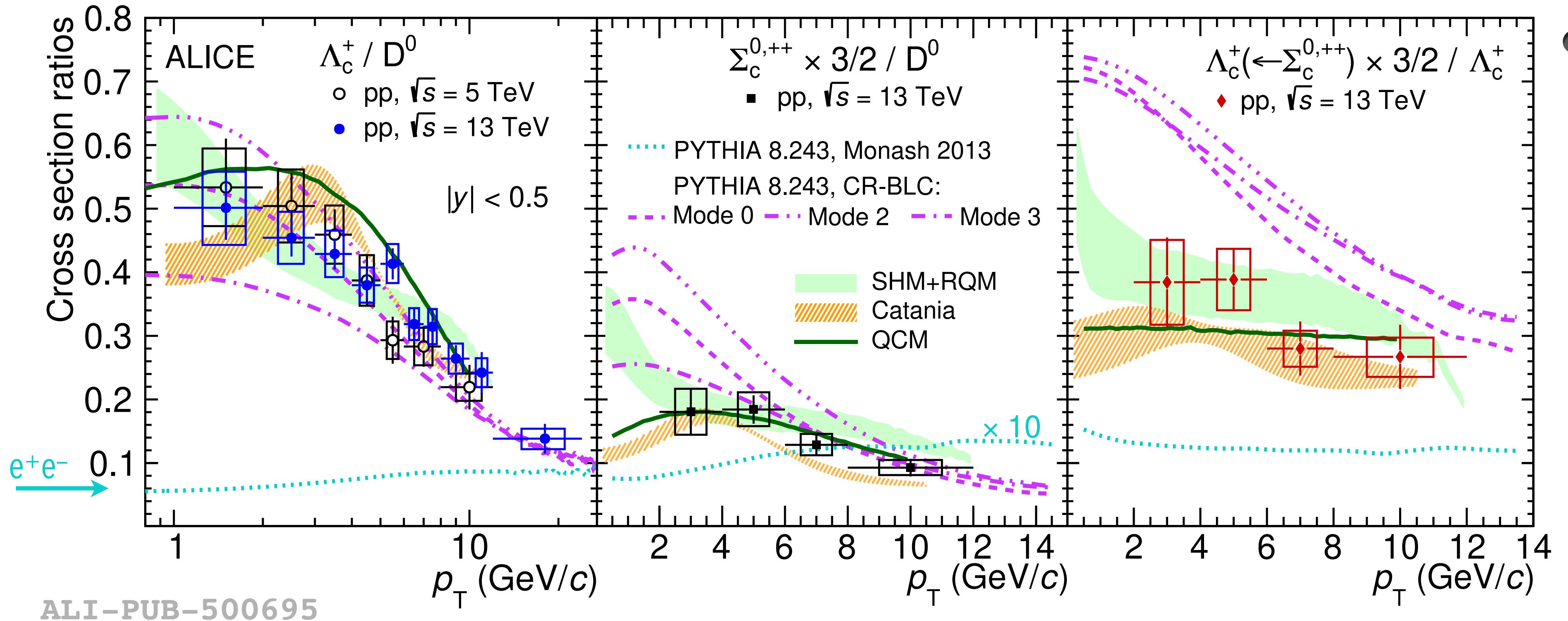


- No indication of modification of  $p_T$ -integrated  $\Lambda_c^+/D^0$  ratio from pp to Pb-Pb collisions
- Possible hint of rapidity dependence

# Charm baryon enhancement in pp collisions

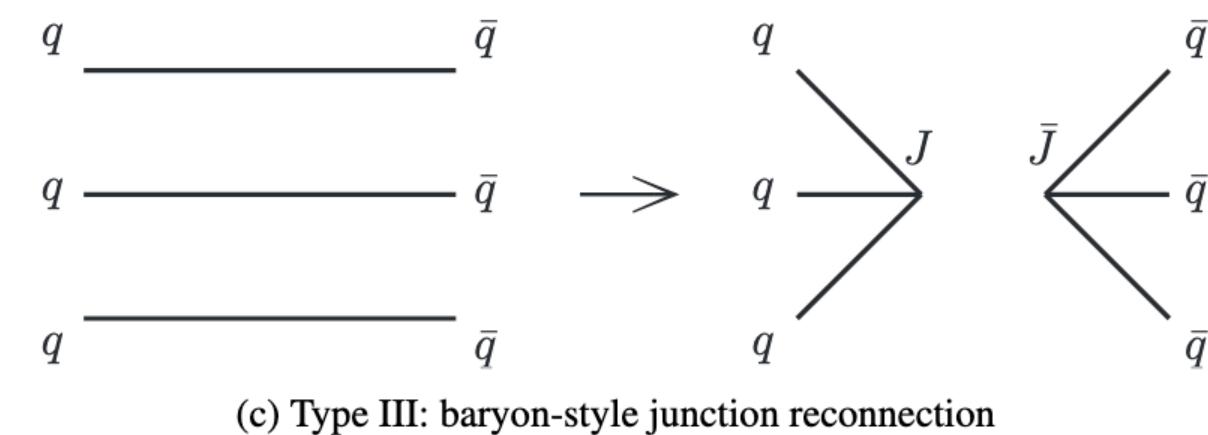
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- Color Reconnection (PYTHIA8)

J.P. Christiansen, P. Z. Skands, JHEP 08 (2015) 003



- Quark coalescence (+fragmentation)

V. Minissale, S. Plumari, V. Greco PLB 821 (2021) 136622  
 J. Song, H. Li, F.-I. Shao et al EPJC (2018) 78: 344

- Statistical hadronisation model with augmented set of charm-baryon excited states from lattice QCD

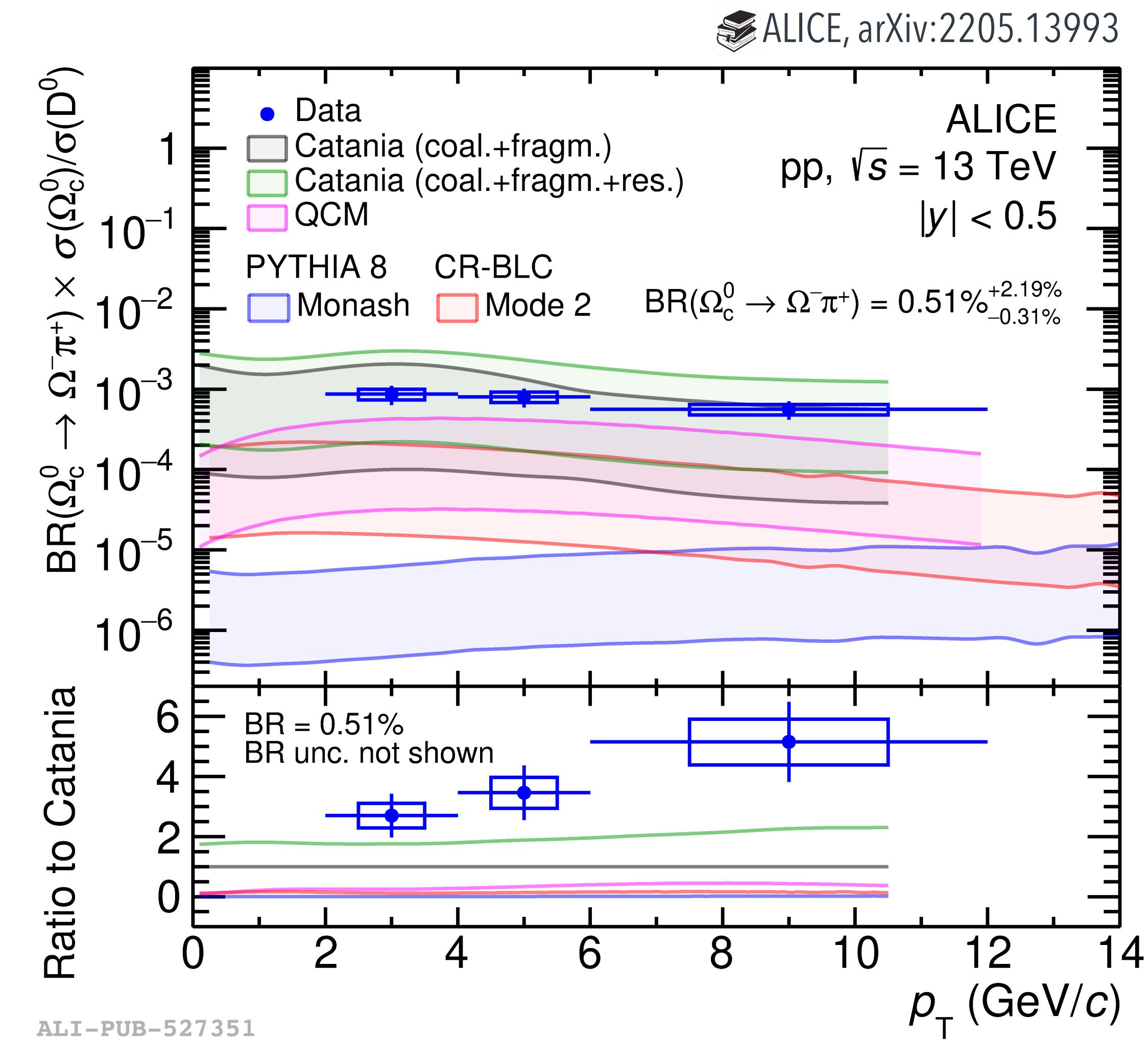
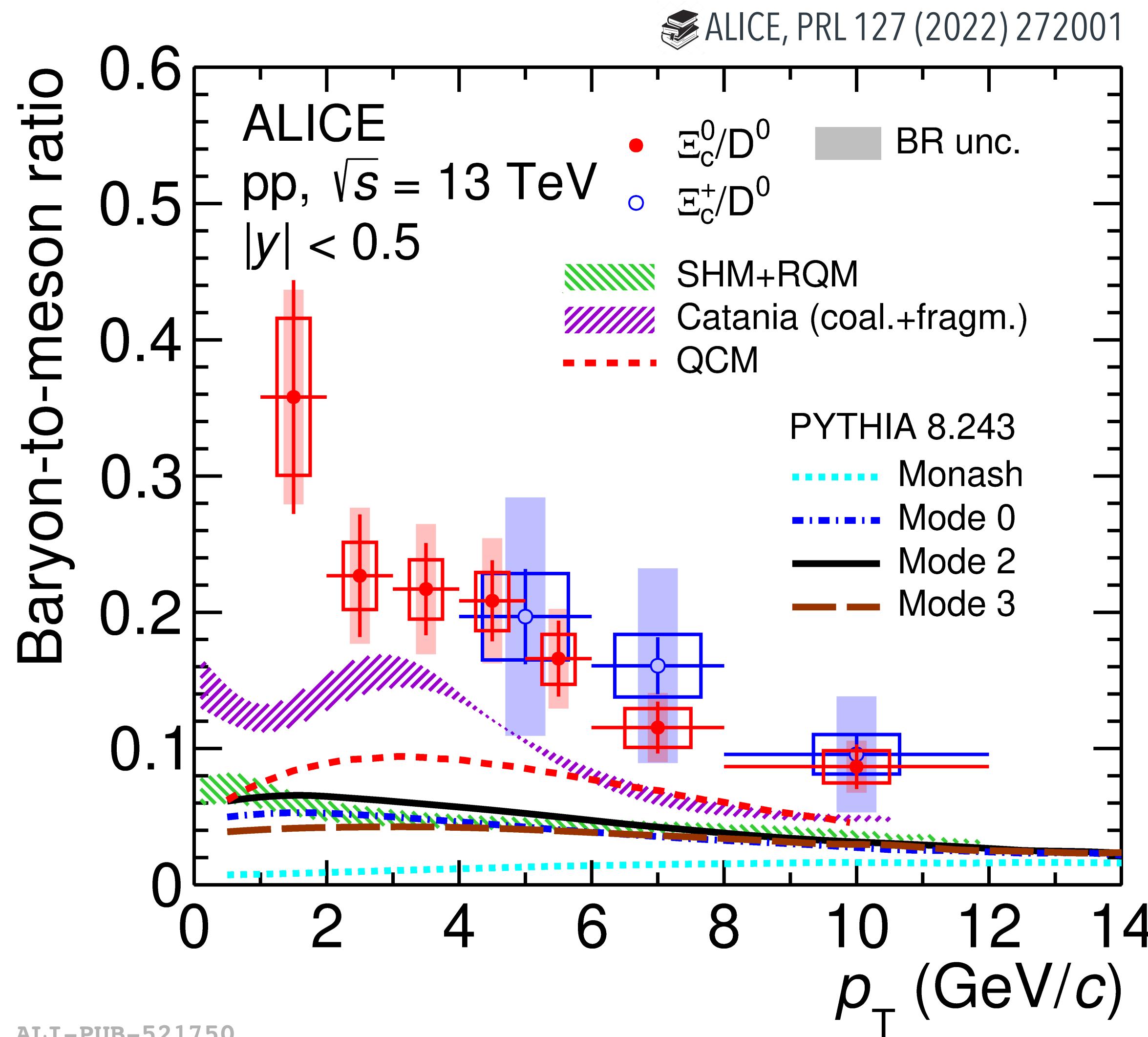
M. He, R. Rapp, PLB 795 (2019) 117-121

- Ground and excited charm baryons enhanced compared to  $e^+e^-$  collisions

# Charm-strange baryon enhancement in pp collisions

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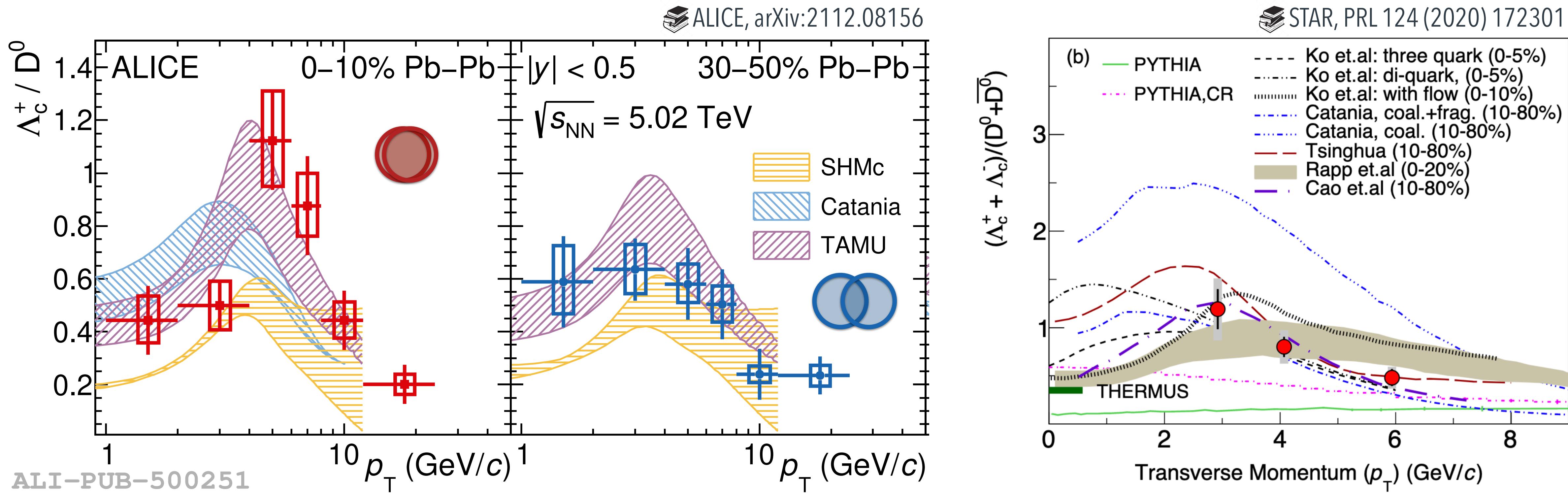


- Models do not reproduce charm-strange baryons

# Charm baryon enhancement in heavy-ion collisions

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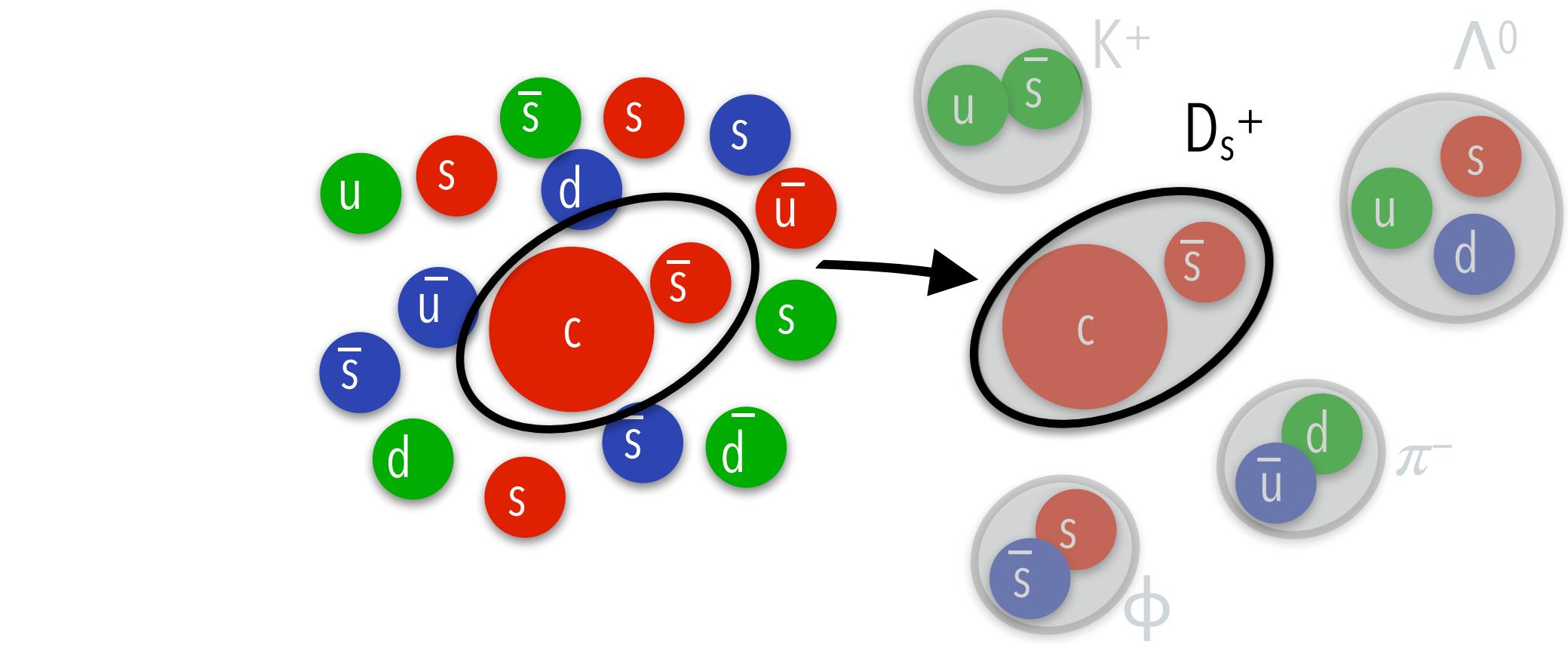
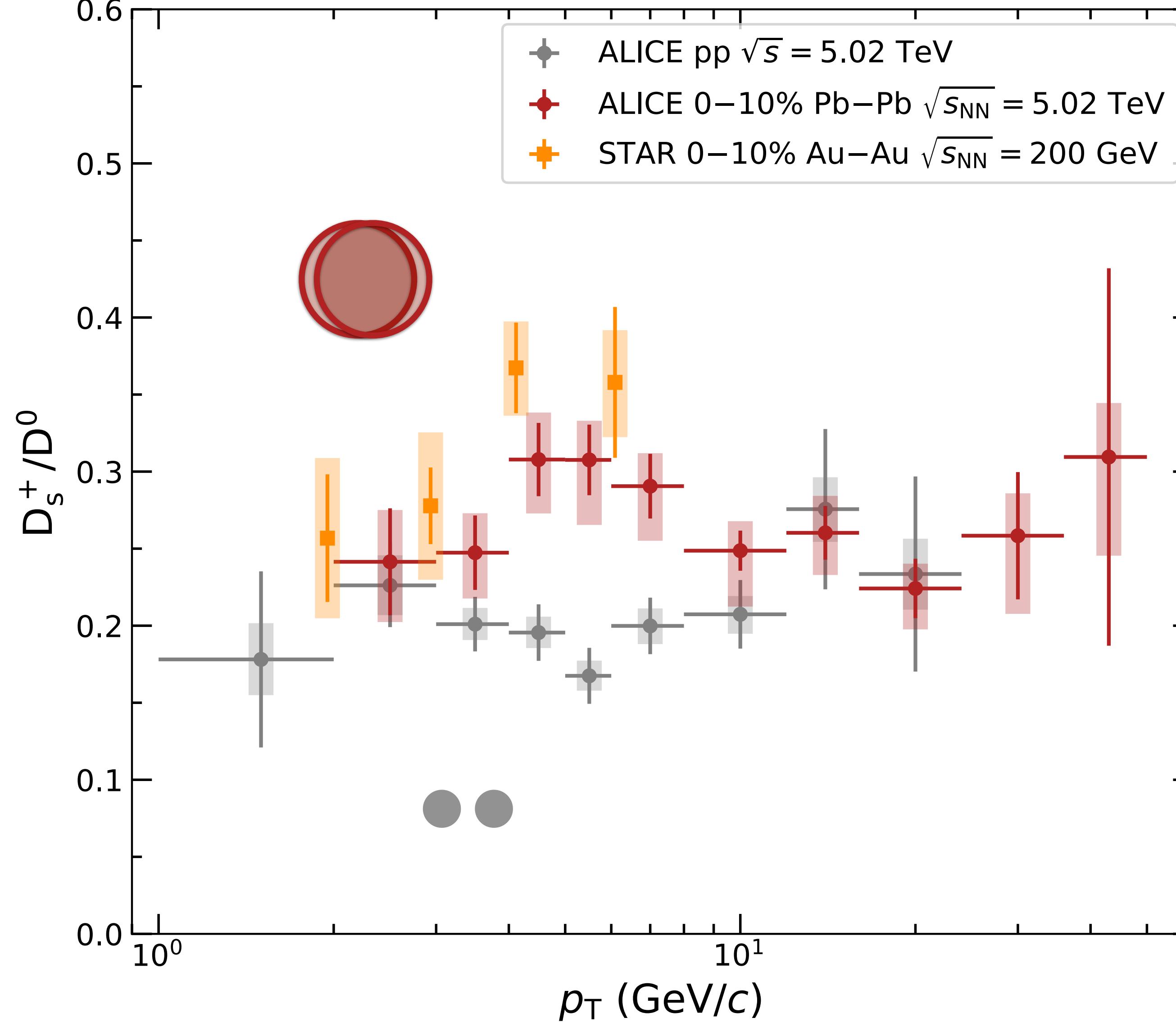
- Coalescence implementations:
  - Instantaneous [Catania, EPJC \(2018\) 78:348](#)
  - Cao et al, [PLB 807 \(2020\) 135561](#) Ko et al, [PRC 101 \(2020\) 024909](#)
  - Resonance Recombination model [TAMU, PRL 124 \(2020\) 042301](#)
  - Sequential recombination [Tsinghua, arXiv:1805.10858](#)
- Statistical hadronisation (no enhanced baryon states):
  - Input charm cross section from pp measurements, hydro-based spectrum for core and a pp scaled spectrum for corona
  - SHMc, [JHEP 07 \(2021\) 035](#)
  - Alternative implementation [THERMUS, CPC 180 \(2009\) 84](#)

# Charm-quark hadronisation and strangeness enhancement

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ALICE, PLB 827 (2022) 136986    STAR, PRL 127 (2021) 092301



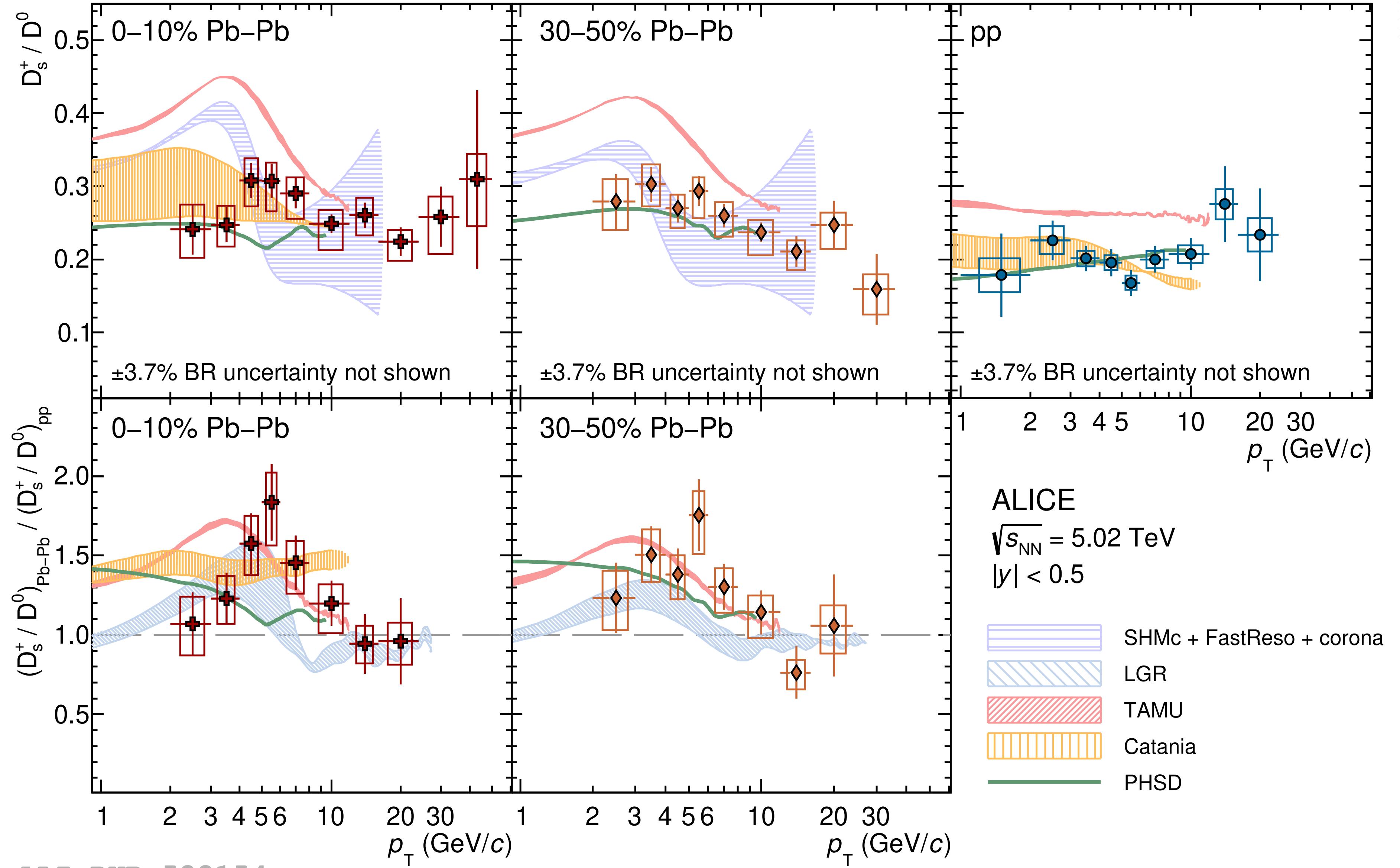
- Abundant production of strange quarks in the QGP (strangeness enhancement)
- Hadronisation via recombination (at least partial thermal equilibrium required)
  - strange hadrons expected to be enhanced
- Strange-to-nonstrange ratio higher in Pb-Pb than pp in charm sector
  - Also modification of the  $p_T$  distribution

ALICE, JHEP 05 (2021) 220

# Charm-quark hadronisation and strangeness enhancement

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ALICE, PLB 827 (2022) 136986

- Enhancement of strange-to-nonstrange production ratio in Pb–Pb collisions with respect to pp collisions typically well described by models, but absolute value still challenging to be reproduced

# Statistical hadronisation model for charm hadrons

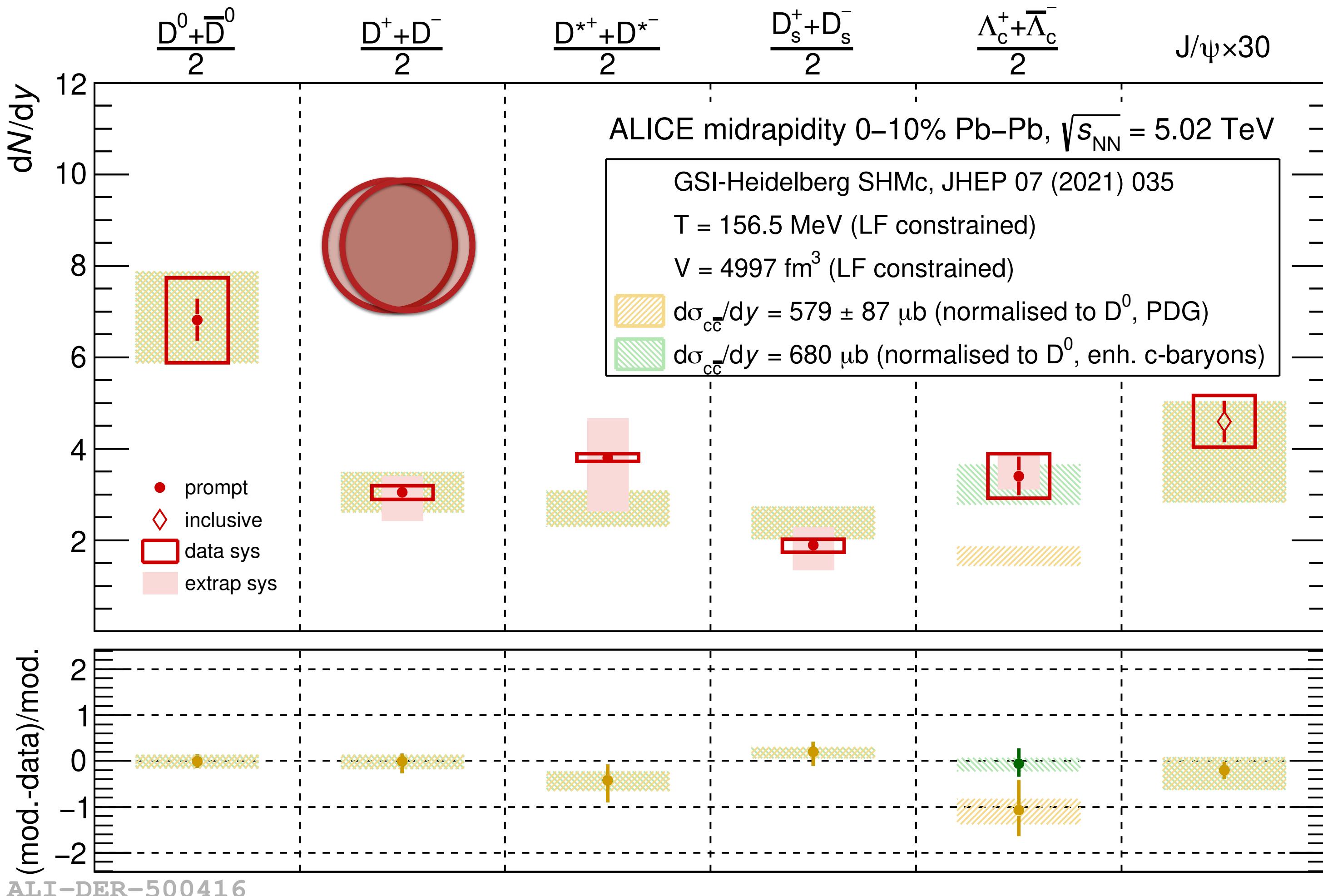
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- Assumptions:
  - Charm quarks created in initial hard scatterings (thermal production negligible) and survive the entire evolution
  - They reach thermal equilibrium and hadronise at the phase boundary

$$N_{c\bar{c}}^{\text{dir}} = \frac{1}{2} g_c V \left\{ \sum_i n_{D_i} + \dots \right\} + g_c^2 V \left\{ \sum_i n_{J/\psi_i} + \dots \right\}$$

Charm fugacity factor, constrained from measurements of charm production cross sections in pp collisions



- Charm-hadron abundances described by SHM
  - $\Lambda_c^+$  underestimated if no enhanced set of excited baryon states
  - Indication of charm quark thermalisation in the QGP

SHMc, JHEP 07 (2021) 035



ALICE, JHEP 01 (2022) 174



ALICE, PLB 827 (2022) 136986

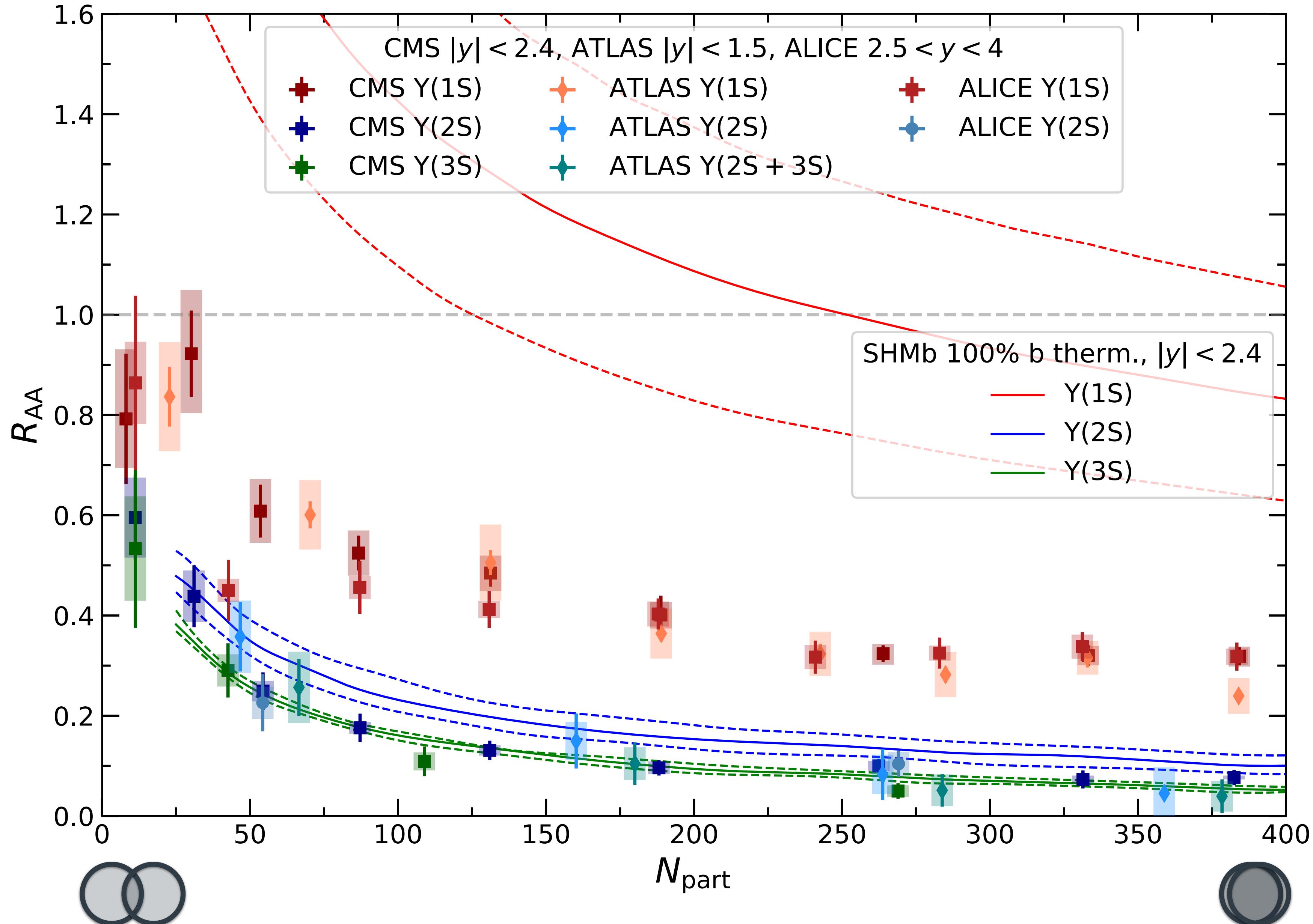


ALICE, arXiv:2112.08156

# Statistical hadronisation model – a beauty parenthesis

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- $\Upsilon$  largely overestimated by SHM if 100% of beauty quarks assumed to be thermalised in the QGP
  - Do beauty quarks reach thermal equilibrium?
  - $\Upsilon$  elliptic flow compatible with zero within large uncertainties

ALICE, PLB 822 (2021) 136579

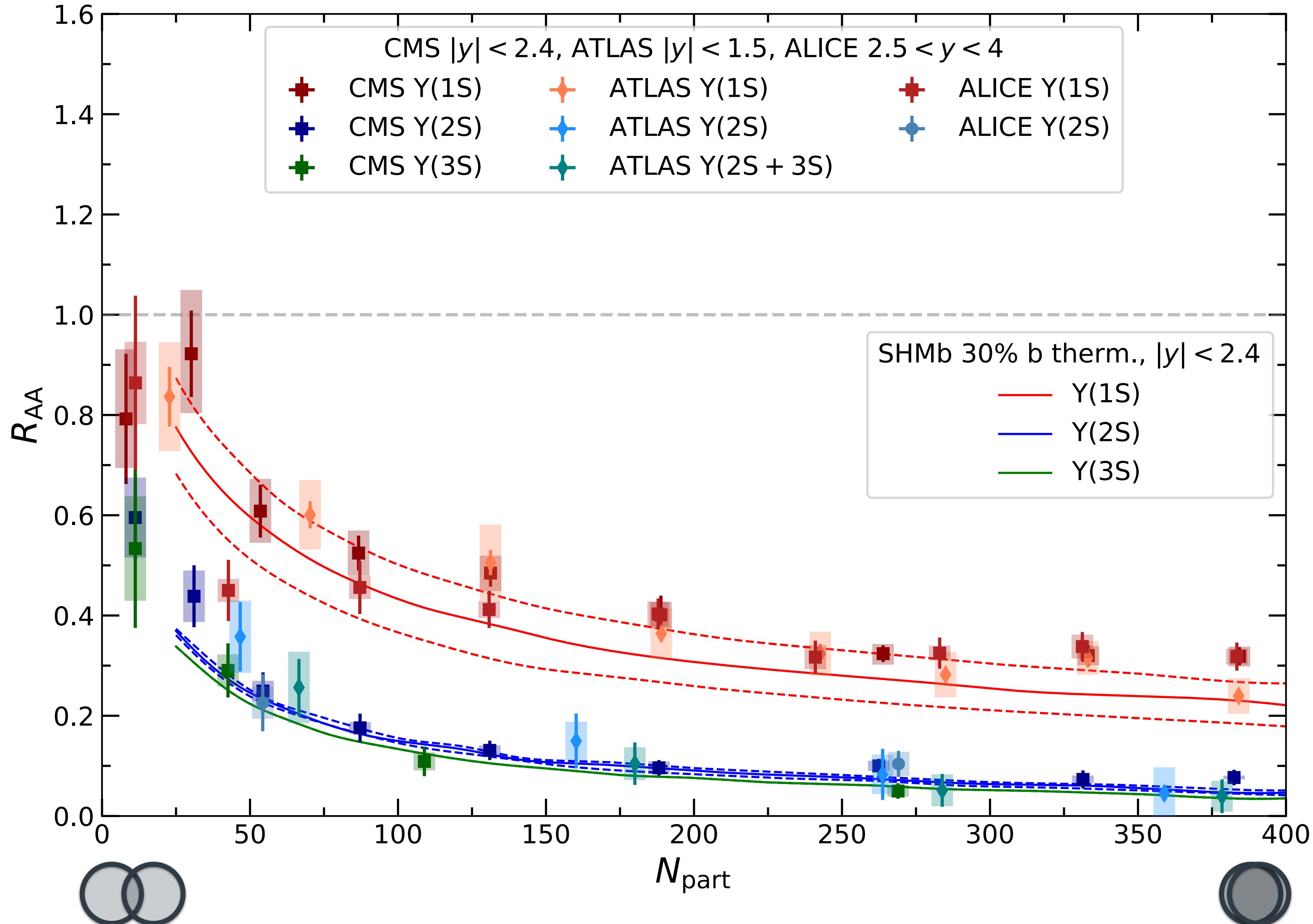
ATLAS, arXiv:2205.03042

CMS preliminary, CMS-PAS-HIN-21-007

# Statistical hadronisation model – a beauty parenthesis

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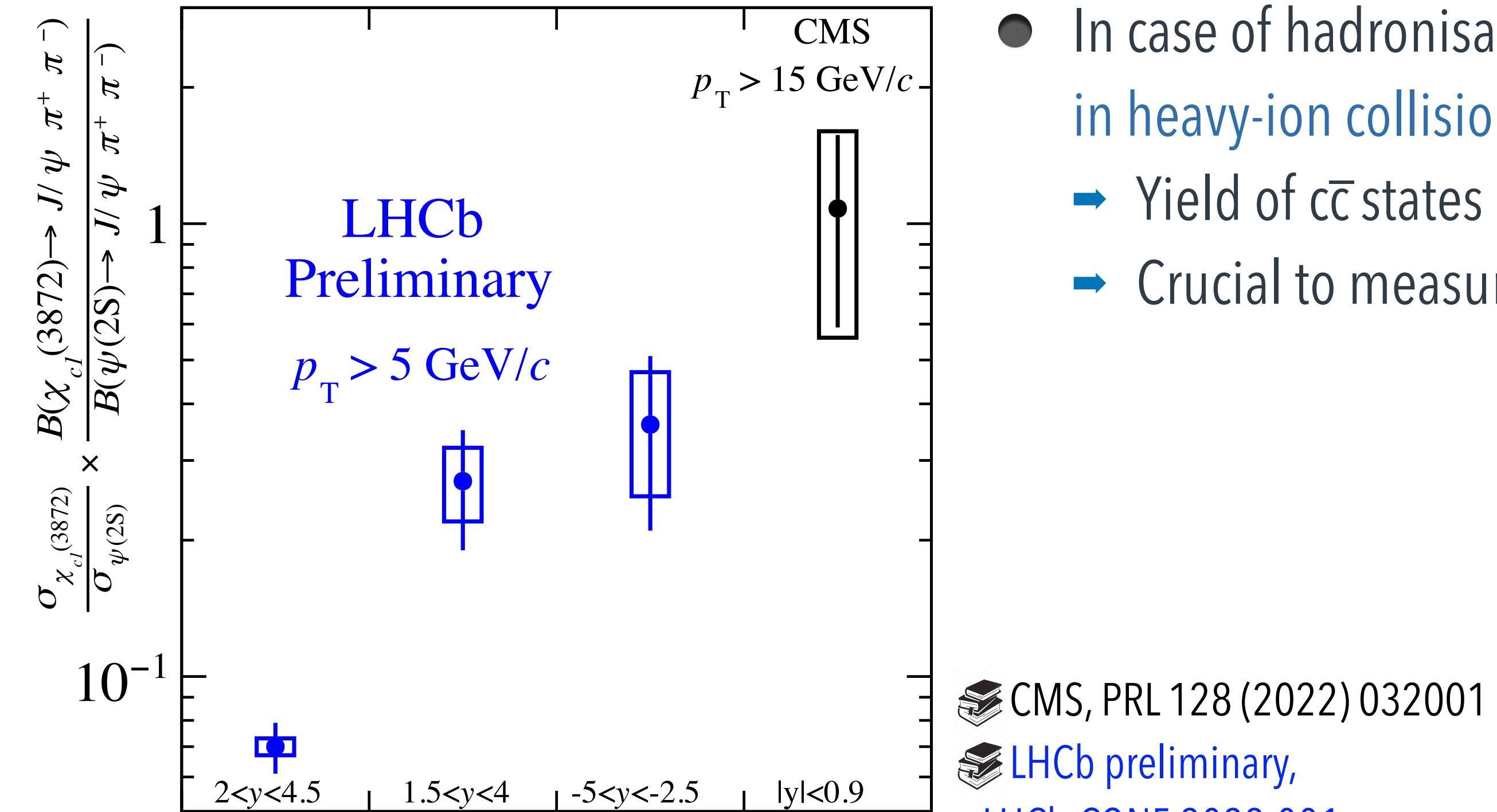


- $\Upsilon$  described by SHM if 30% of beauty quarks assumed to be thermalised in the QGP
  - Beauty quarks likely reach partial thermalisation
- $\Upsilon(1S)$ ,  $\Upsilon(2S)$ , and  $\Upsilon(3S)$  yields depend differently on thermalisation fraction
  - Ratios sensitive to degree of thermalisation

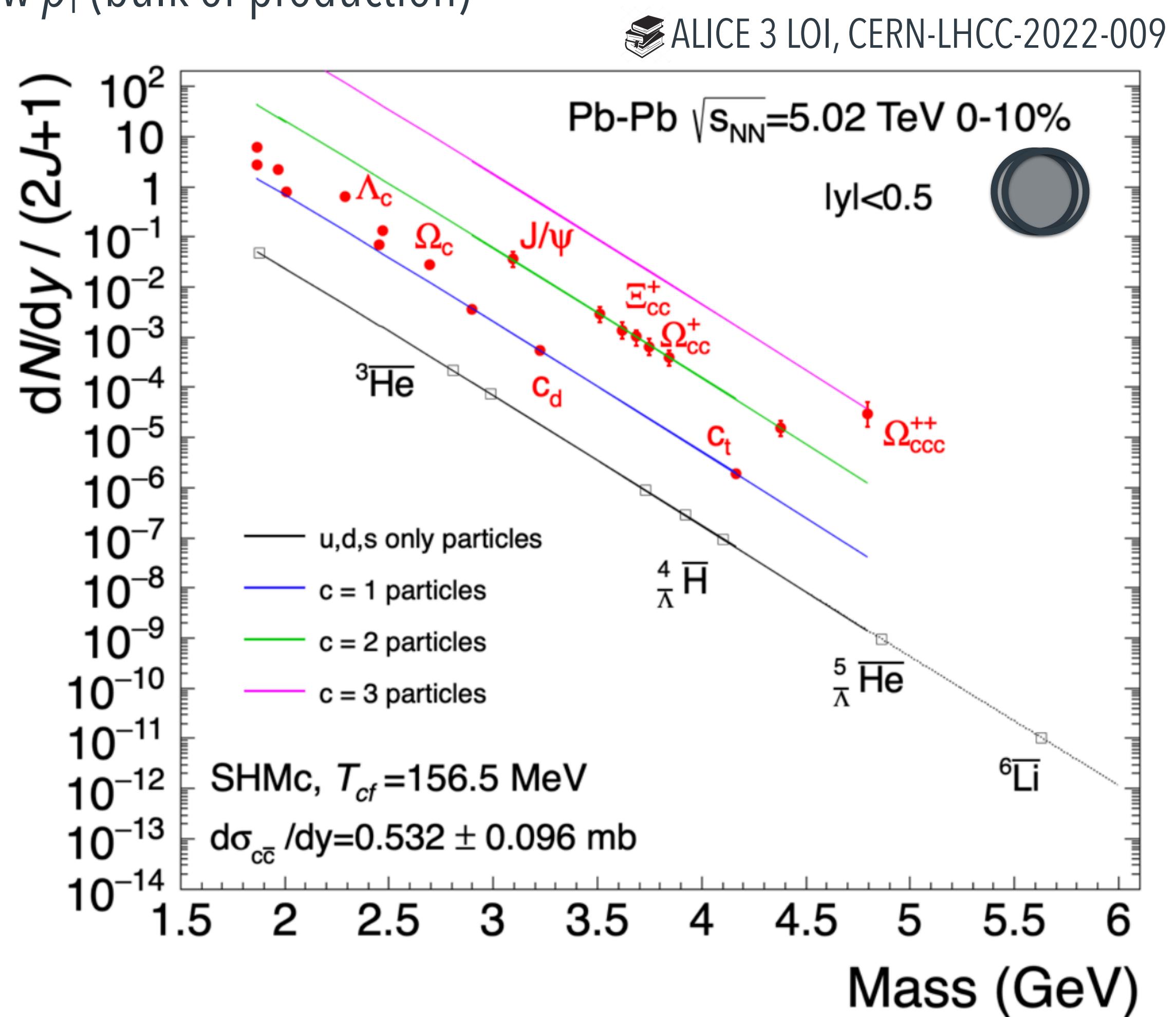
ALICE, PLB 822 (2021) 136579

ATLAS, arXiv:2205.03042

CMS preliminary, CMS-PAS-HIN-21-007



- In case of hadronisation via recombination exotic  $c\bar{c}$  states expected to be **enhanced** in **heavy-ion collisions** compared to pp collisions
  - Yield of  $c\bar{c}$  states depends on **binding energy and size**
  - Crucial to measure low  $p_T$  (bulk of production)

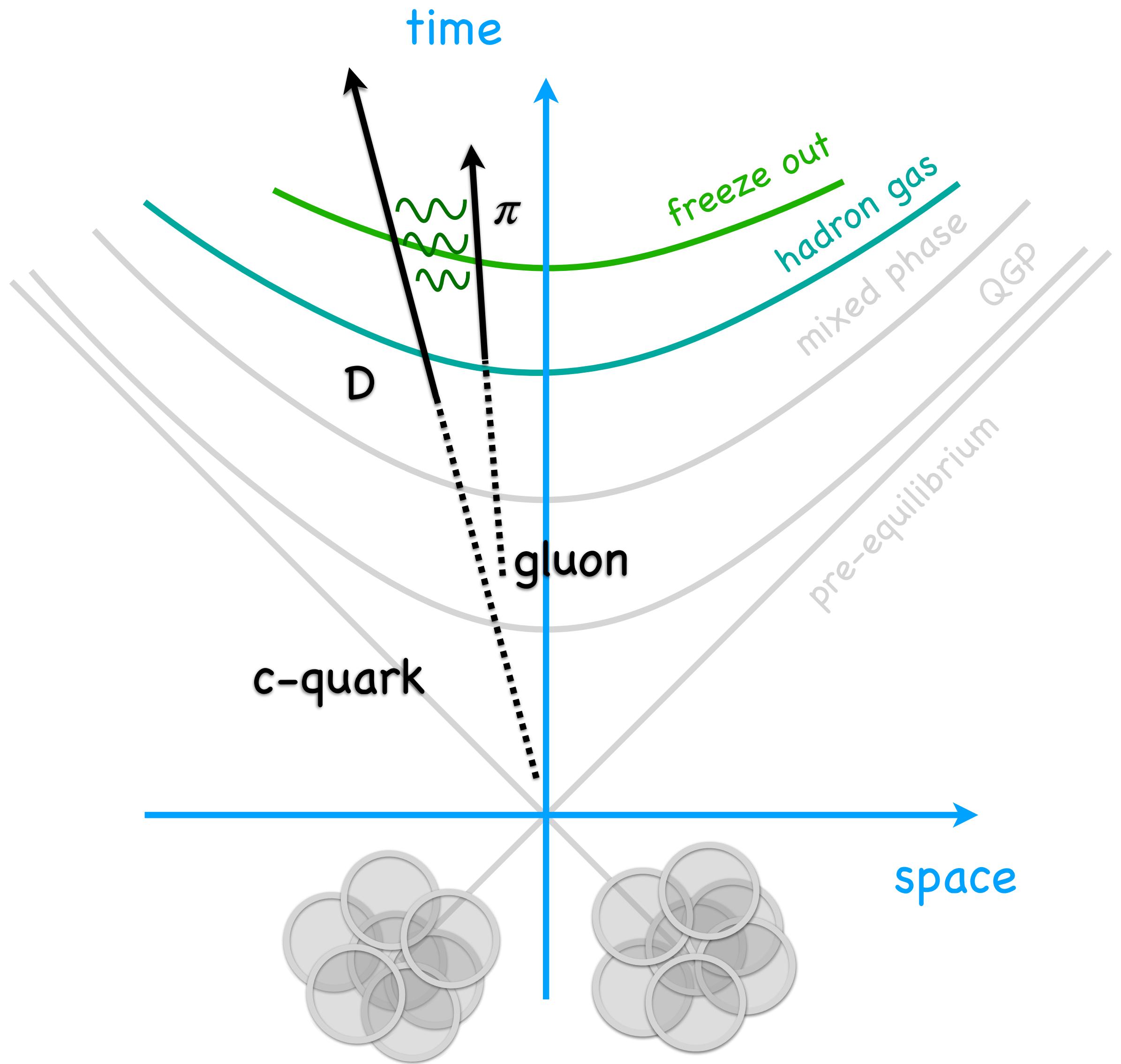


- Multicharm states production in single-parton scattering strongly disfavoured compared to single-charm hadrons in pp collisions
  - Expected **significant enhancement in heavy-ion collisions**
- SHM: emergence of unique pattern due to  $g_c^n$  dependence

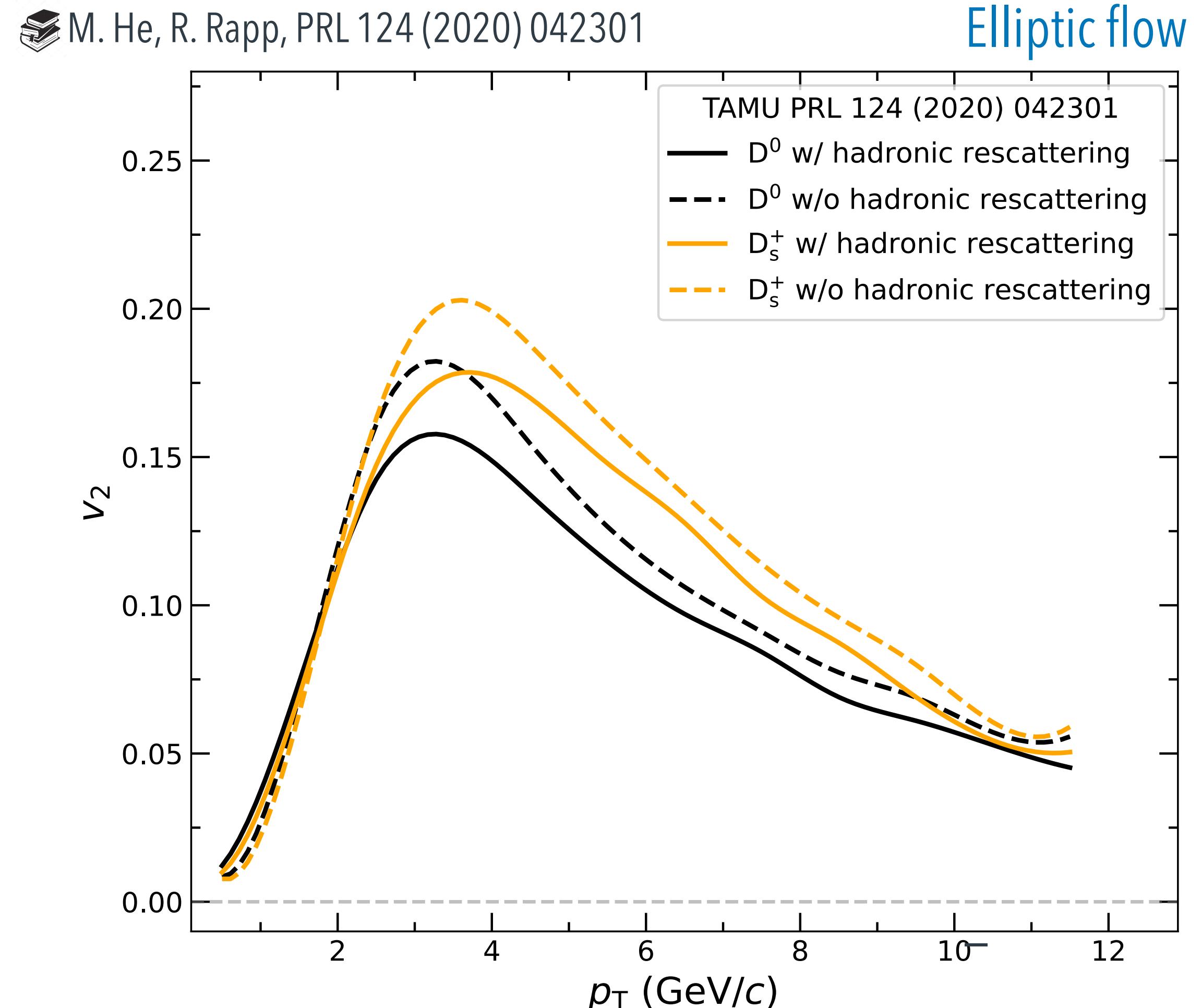
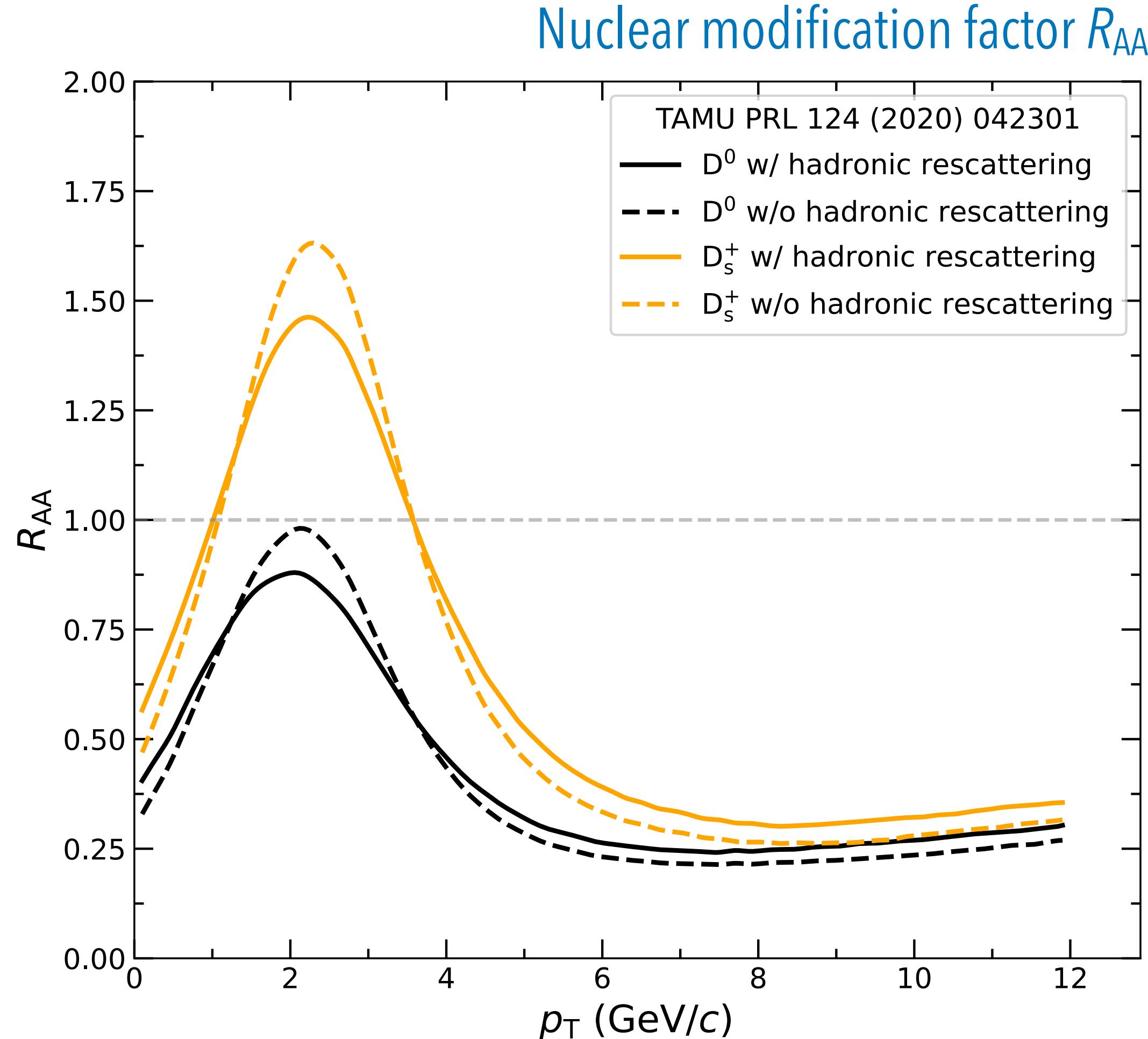
# Charm hadrons in the hadronic phase

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- After the hadronisation, charm quarks hadrons might still interact with the light hadrons produced  
→ How much does the hadronic phase influence the heavy-ion observables?



- In the TAMU model the scattering lengths used for  $\pi D$  and  $K D$  are:

→  $a_{\pi D}(l=3/2) = -0.10$  fm      M. He et al, PLB 701 (2011) 445–450

→  $a_{KD}(l=1) = -0.22$  fm

→ No experimental constraints!

# The study of the residual strong interactions

- Femtoscopy technique: based on the correlation function (CF)

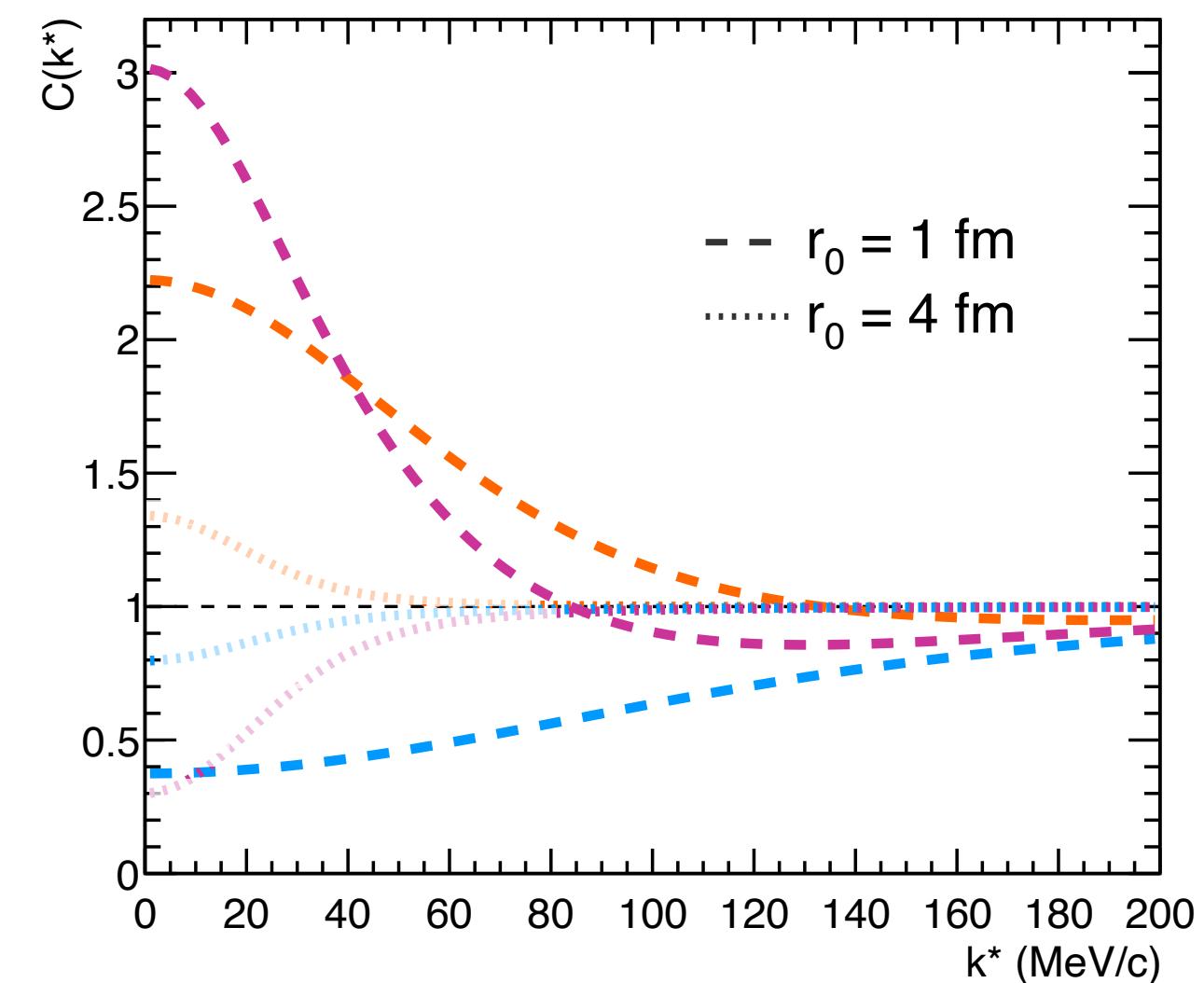
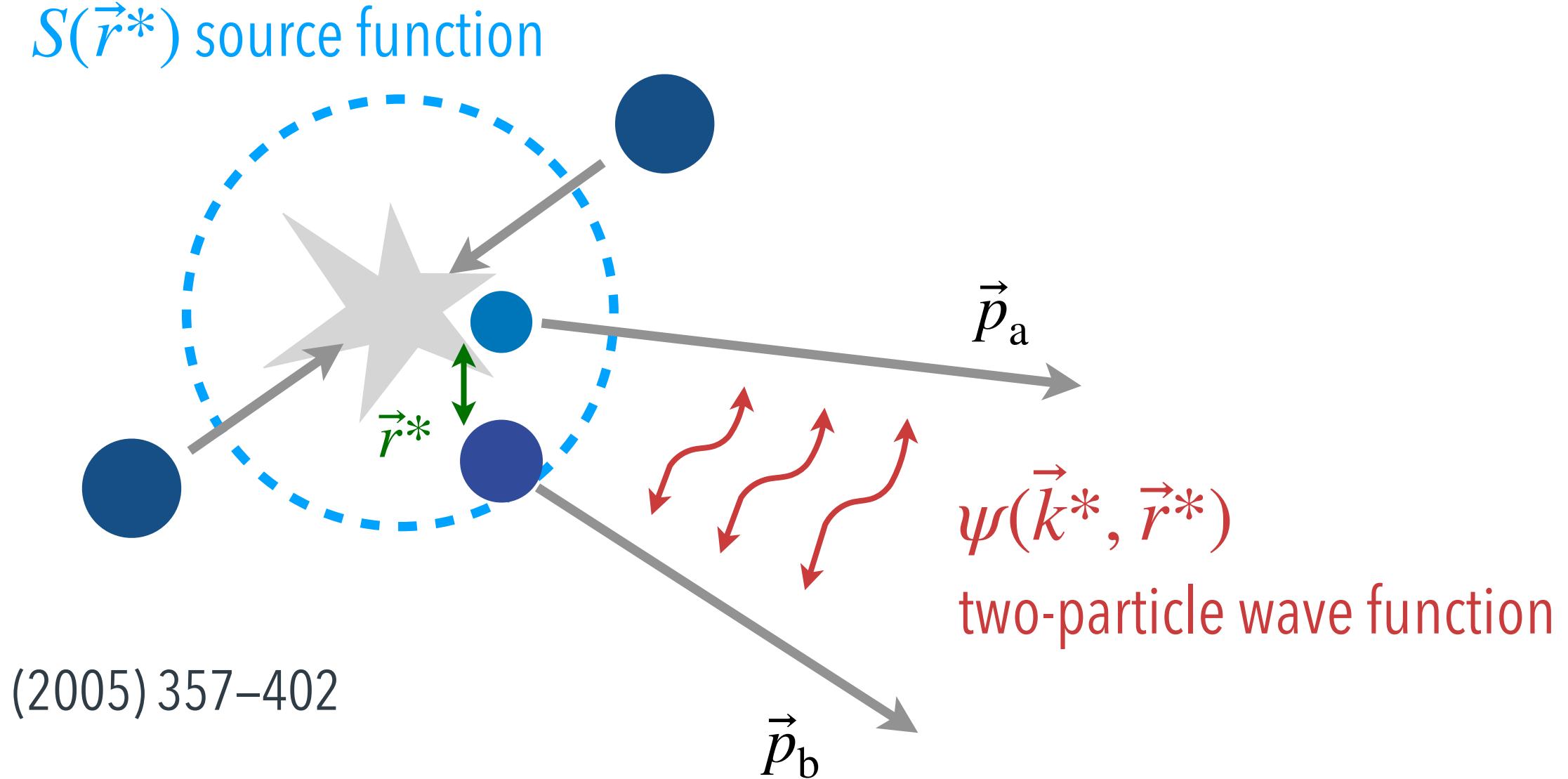
<b>Experiment</b>	<b>Theory</b>
$C(k^*) = \mathcal{N} \frac{N_{\text{pairs}}(\vec{k}^*)}{N_{\text{mixed}}(\vec{k}^*)}$	$= \int S(\vec{r}^*)  \psi(\vec{k}^*, \vec{r}^*) ^2 d^3 r^*$

Koonin-Pratt equation

Book M. Lisa, S. Pratt et al, Ann. Rev. Nucl. Part. Sci. 55 (2005) 357–402

where  $\vec{k}^* = \frac{\vec{p}_a^* - \vec{p}_b^*}{2}$  is in the rest frame of the particle pair

- Relative wave function sensitive to interaction potential
- Emitting source: hypersurface at kinematic freeze out of final-state particles
- $C(k^*)$  most sensitive to strong interaction when the source size  $\sim 1$  fm

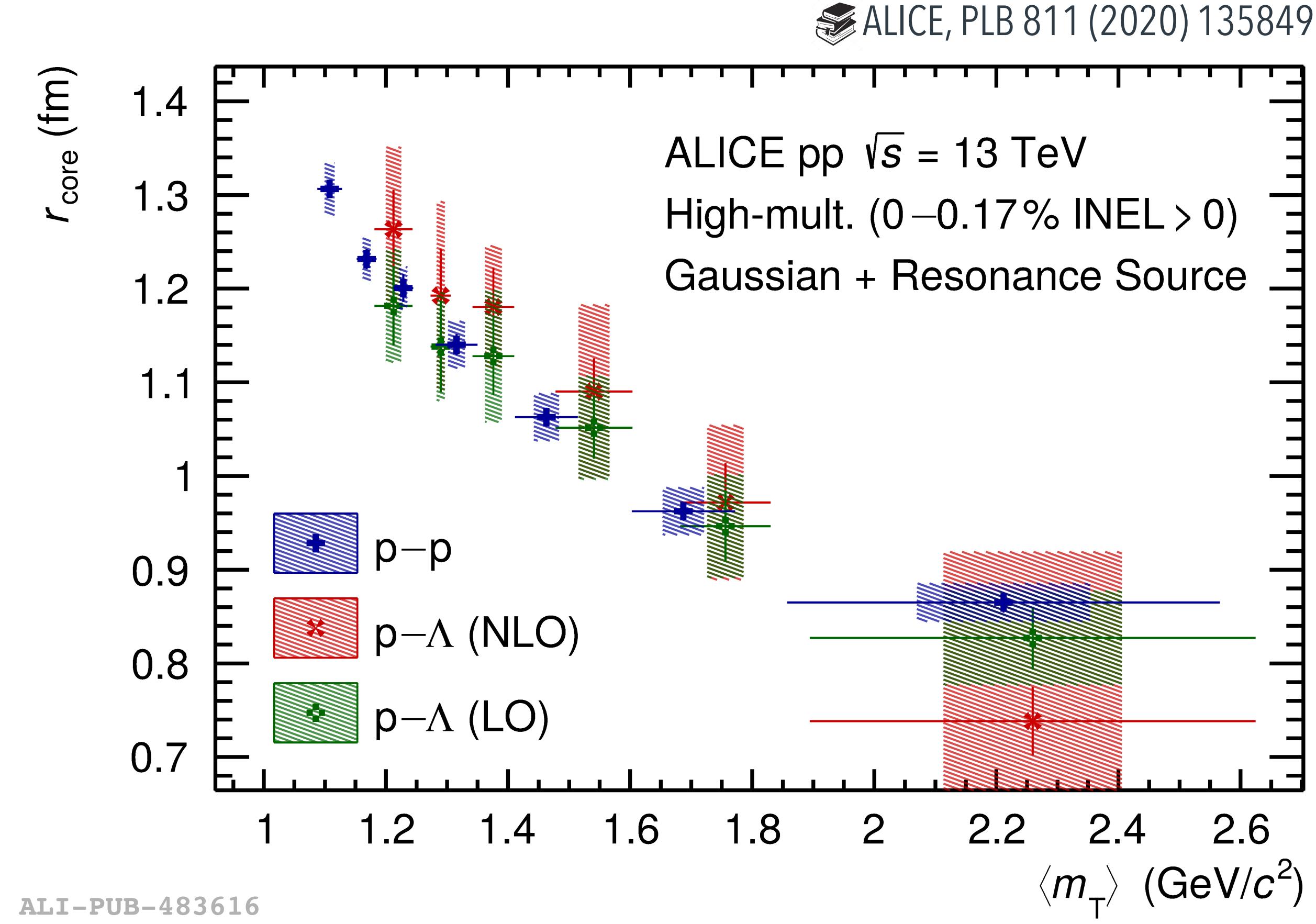
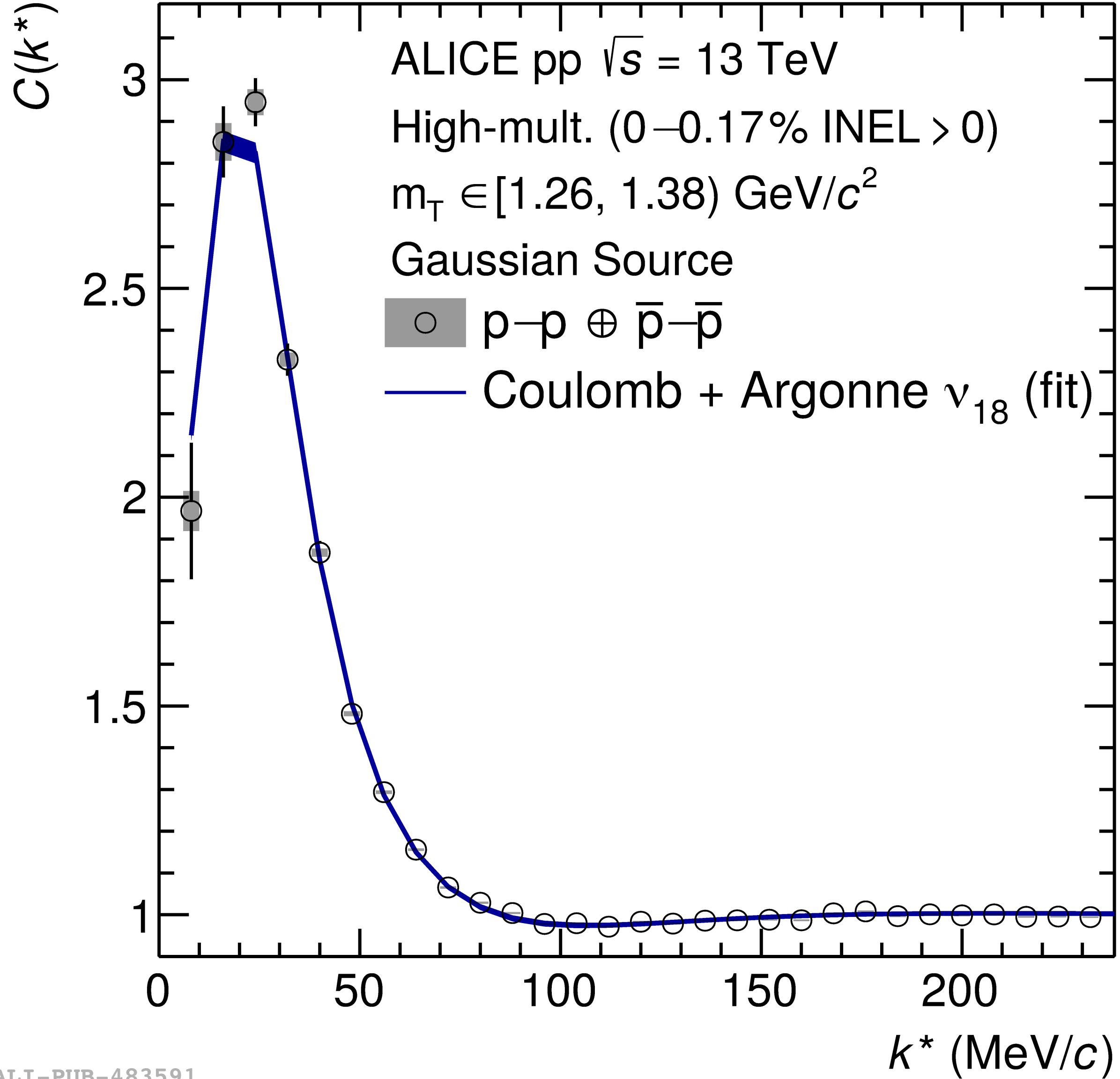


Absence of interaction  $C(k^*) = 1$   
 Attractive potential  $C(k^*) > 1$   
 Repulsive potential  $C(k^*) < 1$   
 Bound-state formation  $C(k^*) <> 1$

# Calibrating the emitting source

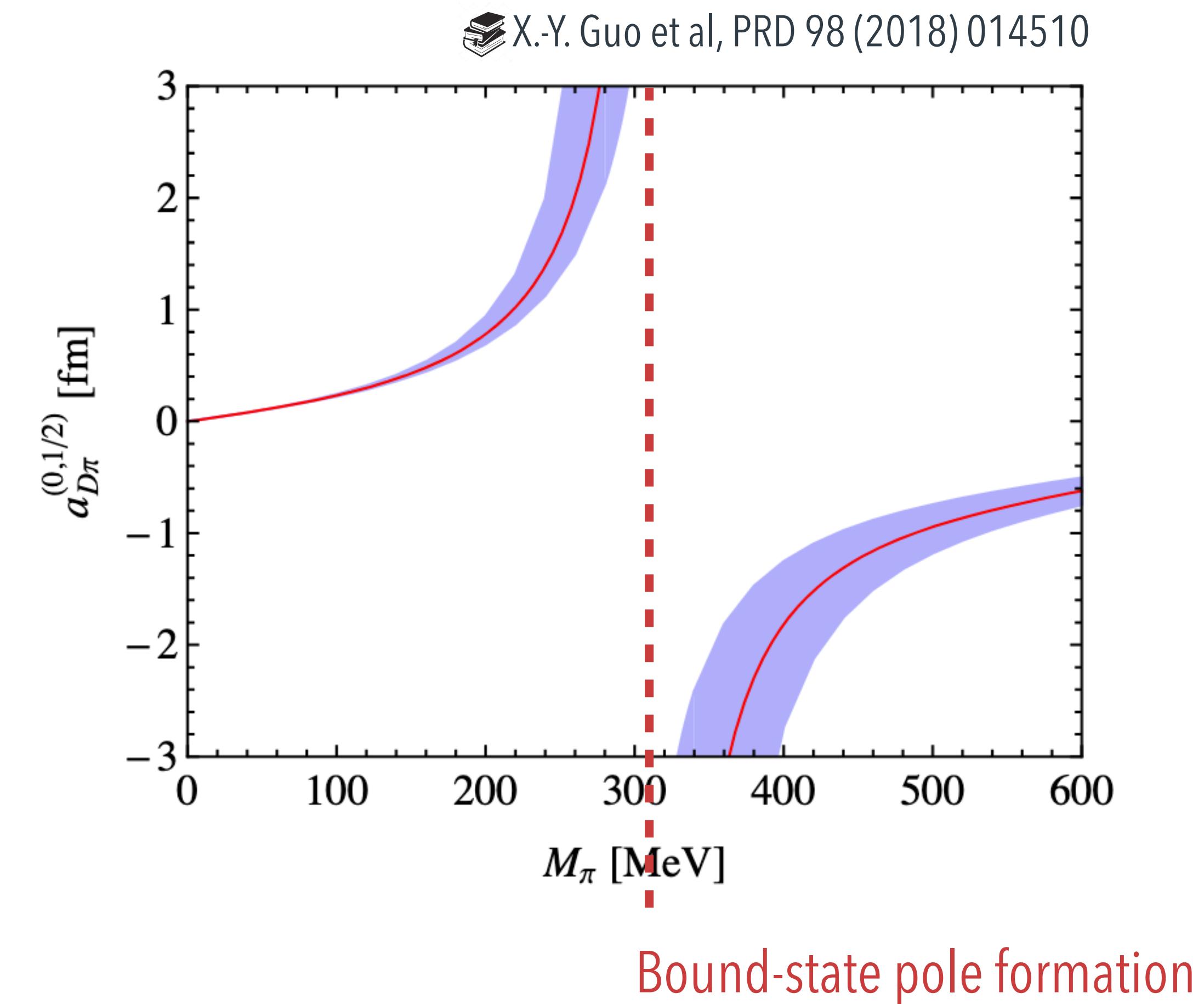
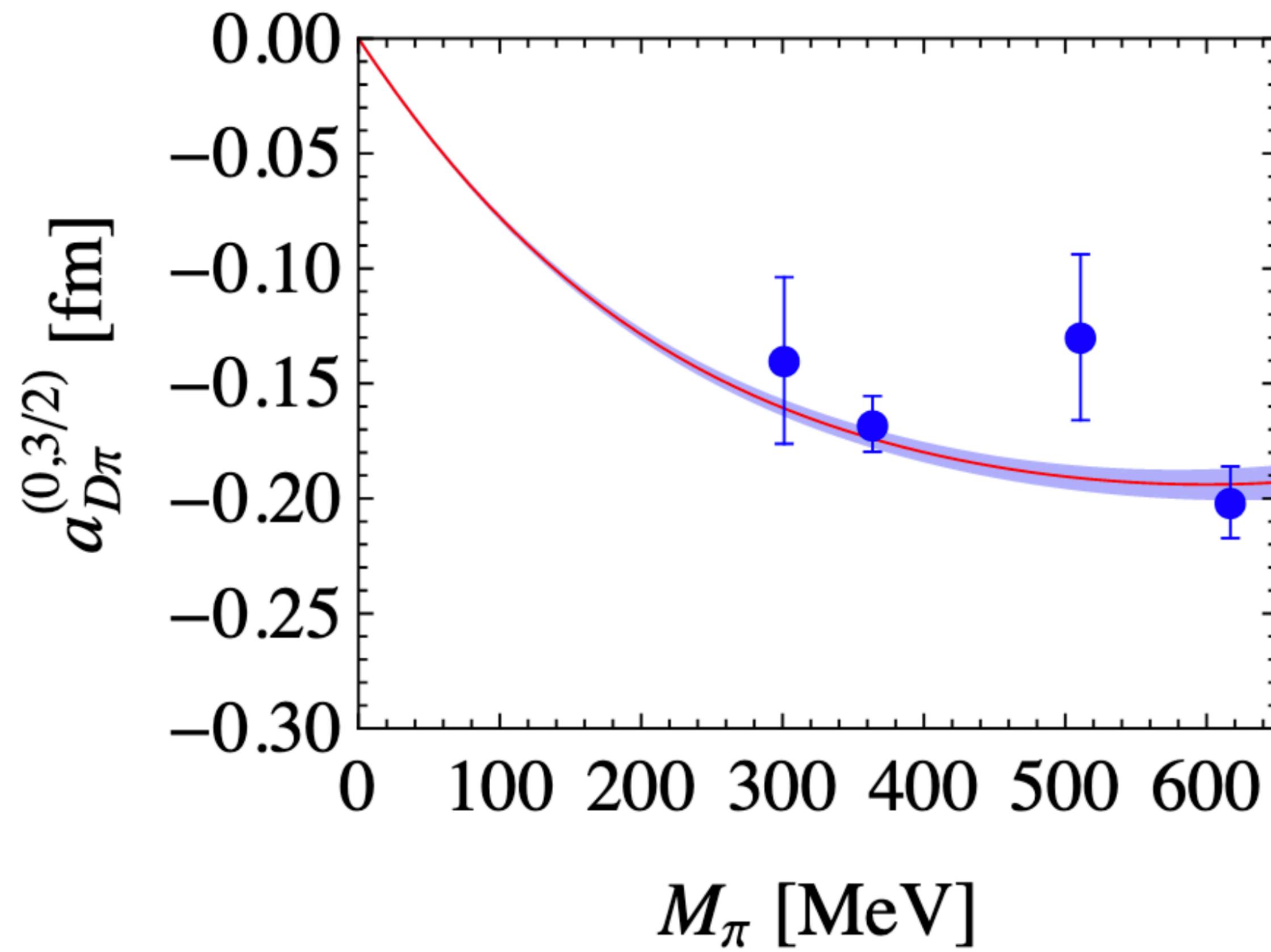
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fgrosa@cern.ch

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- Fit correlation functions of p-p and p- $\Lambda$  pairs
- Interaction precisely described
- Gaussian source with radius as free parameter
- Universal  $m_T$  scaling found

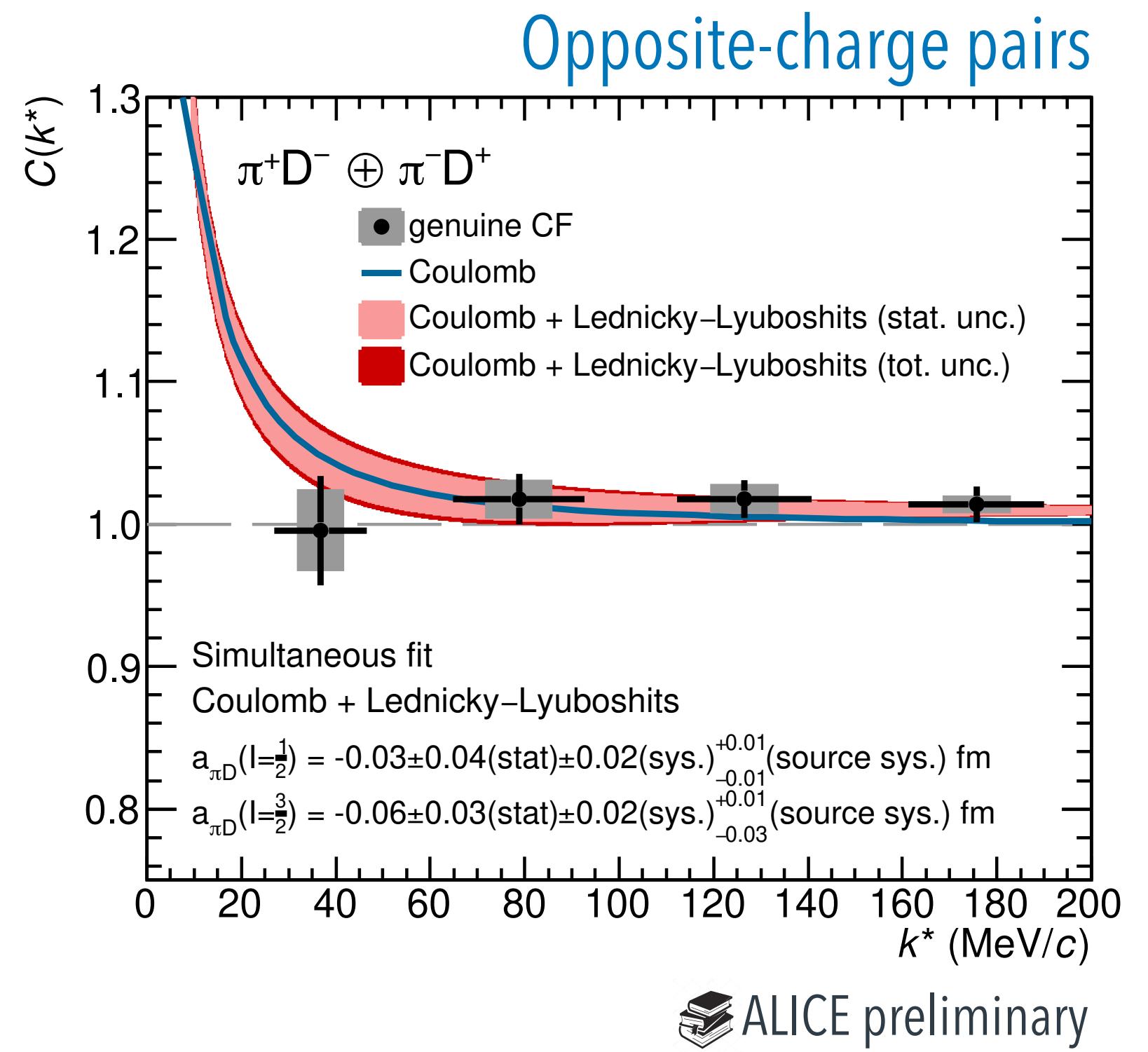
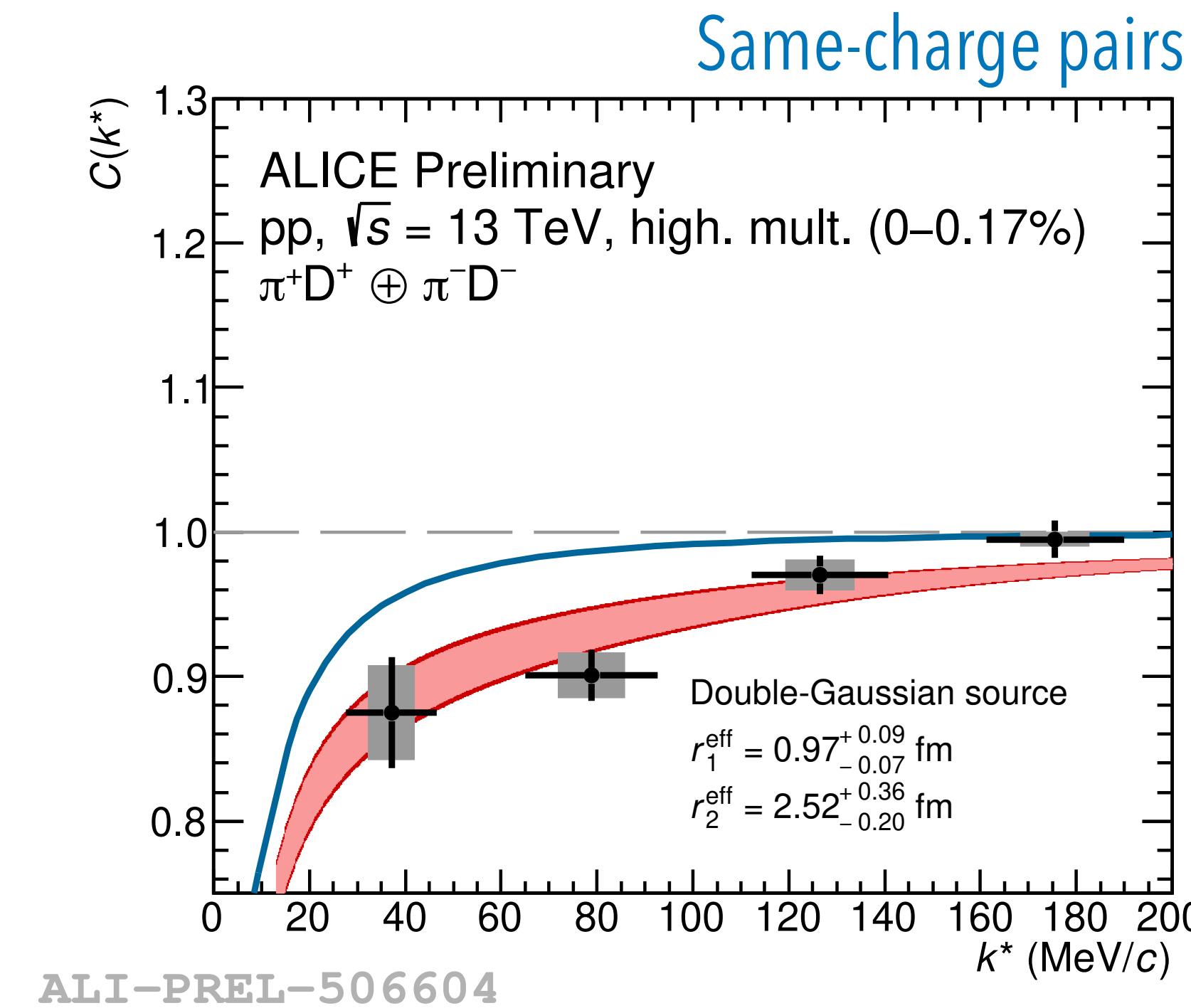
- $\pi D$  interaction: predictions of scattering lengths derived from lattice QCD calculations
  - $\sim 0.1\text{-}0.5 \text{ fm}$ : very small compared to other interactions (light-light  $\sim 7\text{-}8 \text{ fm}$ , light-strange  $\sim 1.5 \text{ fm}$ )
  - No constraints from data
  - For pions  $l=3/2$  channel more constrained than  $l=1/2$  channel



# $\pi D$ interaction: fit with Lednický-Lyuboshits formula

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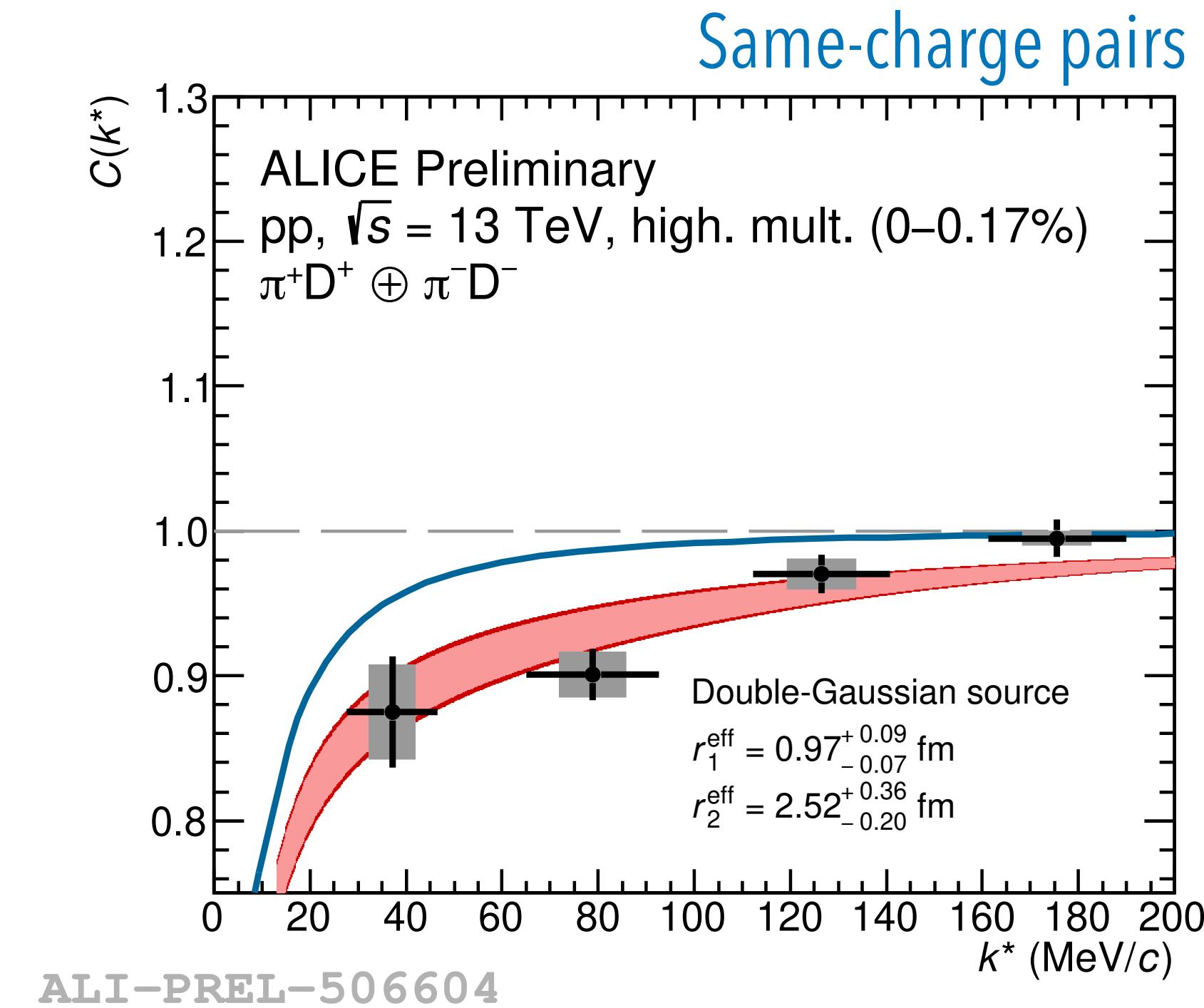


- $\pi^+D^+$   
 $\rightarrow l=3/2$  channel only
- $\pi^+D^-$   
 $\rightarrow l=3/2$  (33%),  $l=1/2$  (66%)

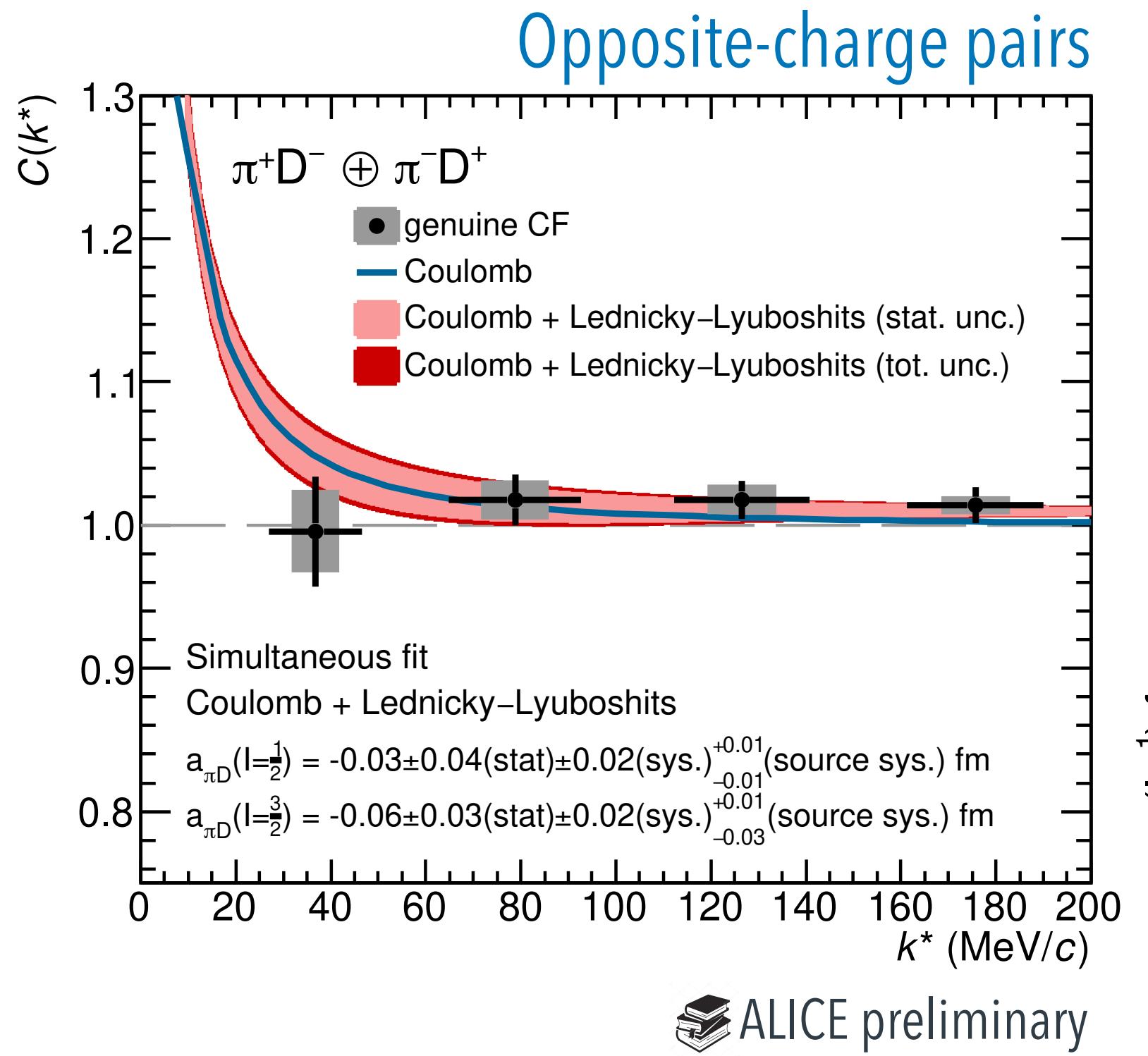
# $\pi D$ interaction: fit with Lednicky-Lyuboshits formula

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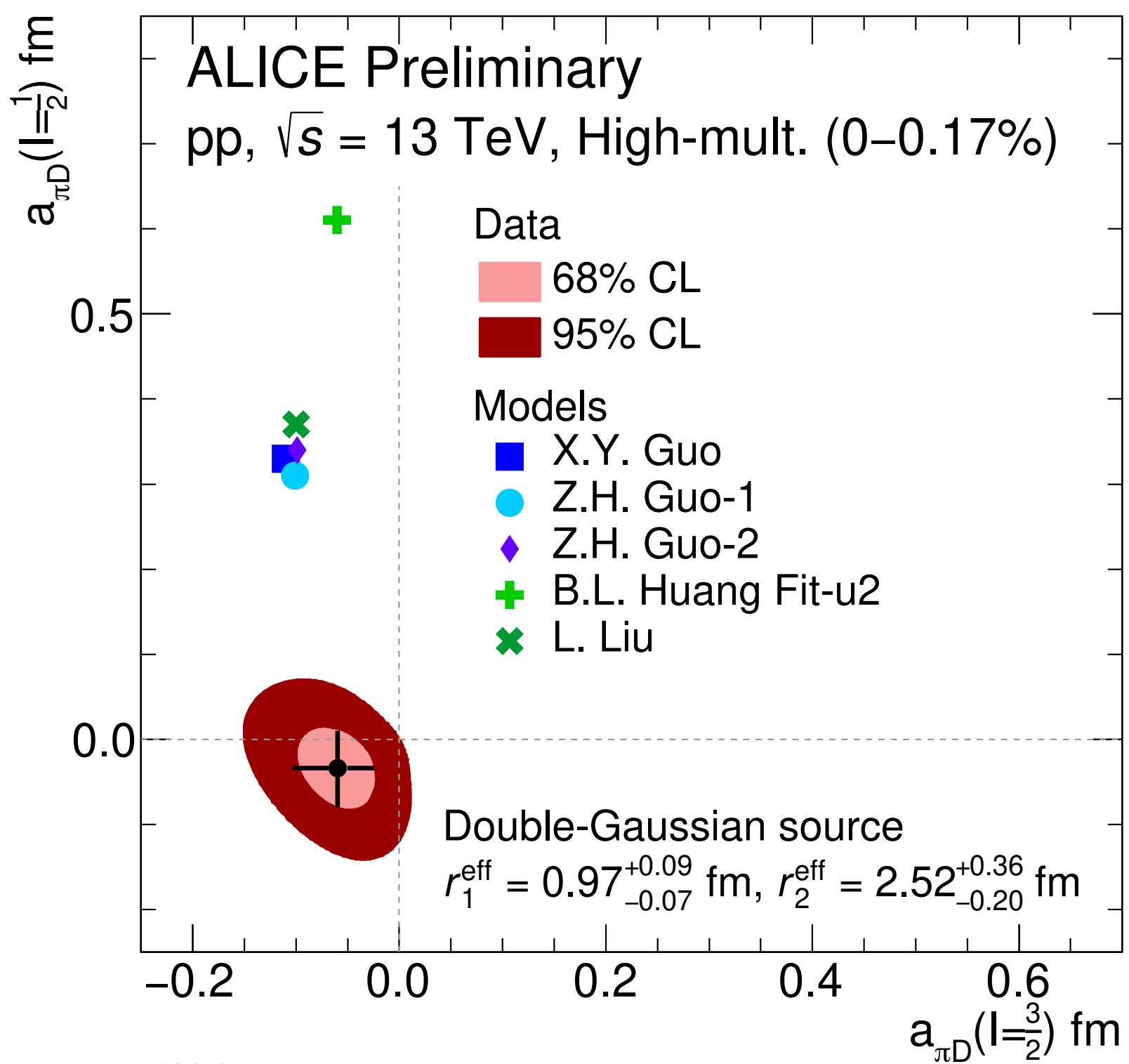
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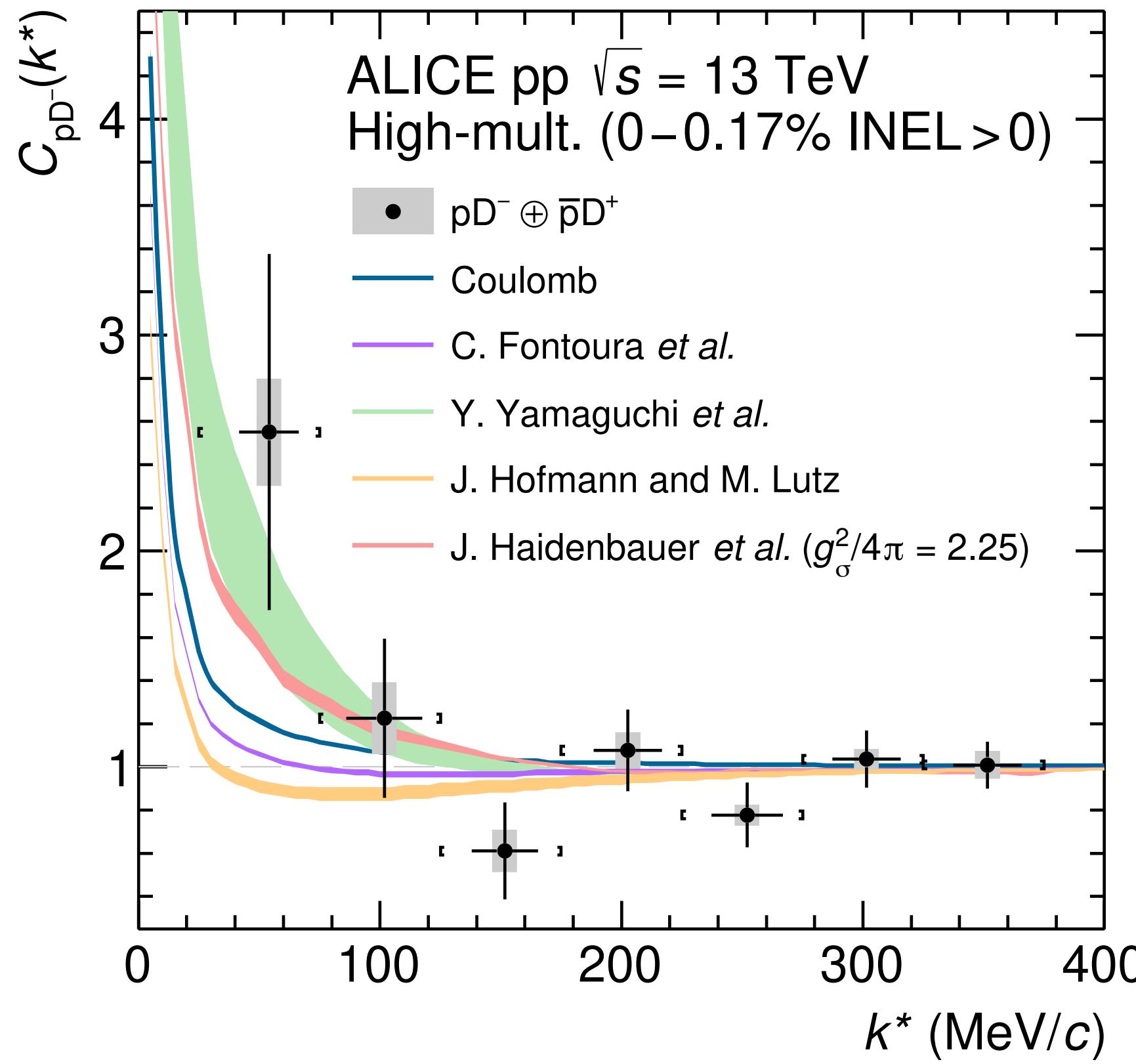
- Scattering length for  $|l|=3/2$  in agreement with models
- Scattering length for  $|l|=1/2$  significantly smaller than models
- The values found indicate a **small rescattering of D mesons in the hadronic phase of heavy-ion collisions**



ALICE preliminary



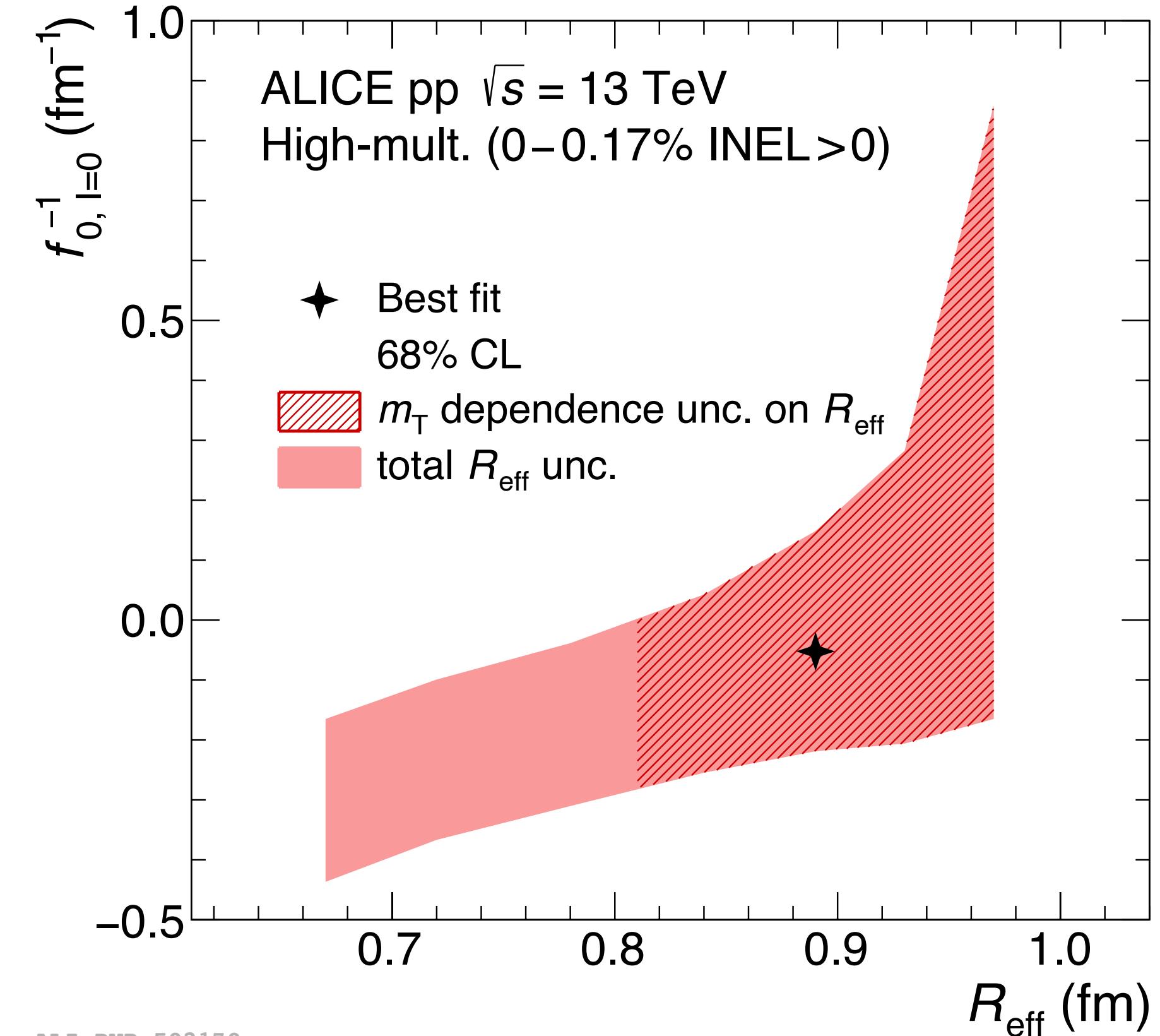
- Small compared to other interactions (scattering lengths light-light  $\sim 7\text{-}8 \text{ fm}$ , light-strange  $\sim 1.5 \text{ fm}$ )
- Most of the models predict repulsive interaction
- Possible bound state formation (Yamaguchi et al)



ALI-PUB-502166

J. Haidenbauer et al, EPJA 33 (2007) 107–117

J. Hofmann and M. Lutz, NPA 763 (2005) 90–139



ALI-PUB-502170

Fontura et al, PRC 87 (2013) 025206

Yamaguchi et al, PRD 84 (2011) 014032

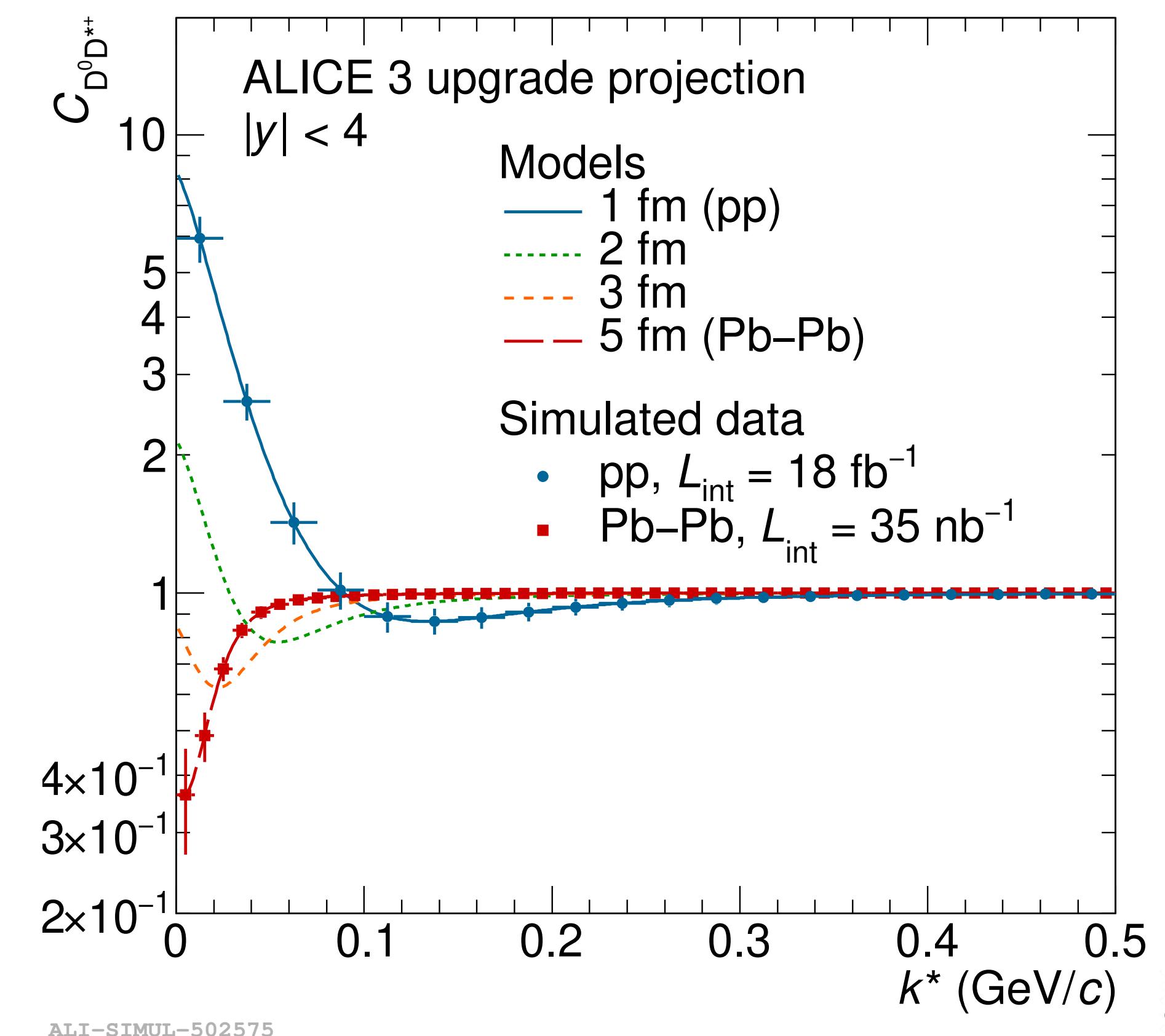
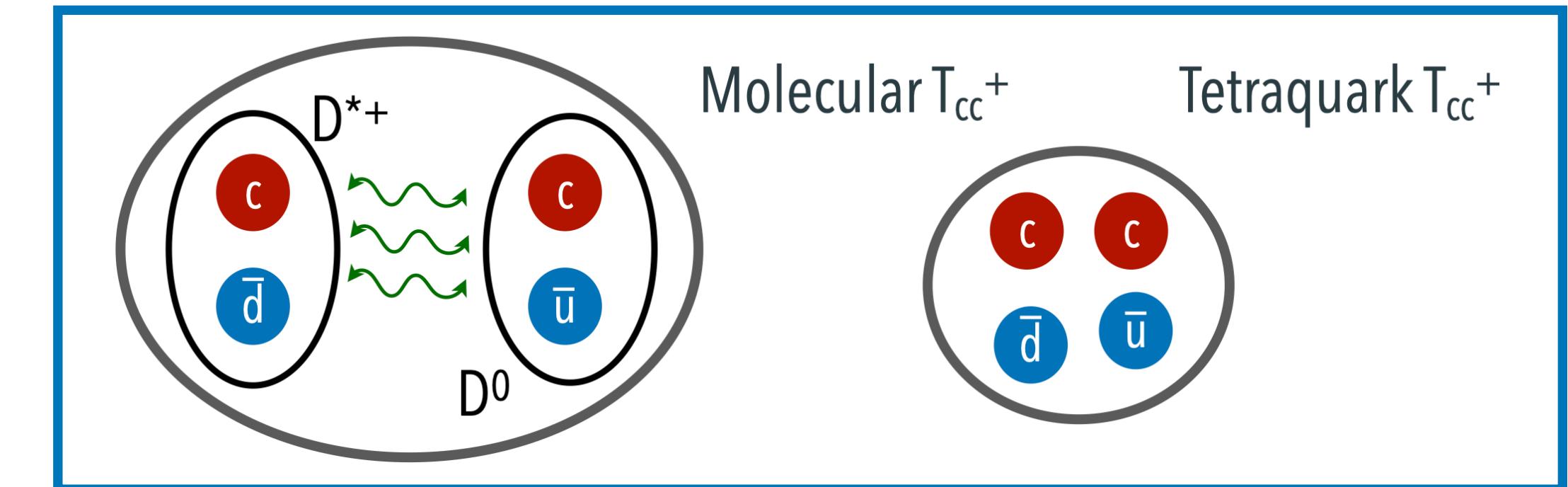
ALICE, PRD 106 (2022) 052010

- Interval of scattering length for isospin  $I=0$  at 68% CL indicates either **attractive interaction** with or without the formation of a bound state

# Charm-charm hadron interaction: hadronic physics

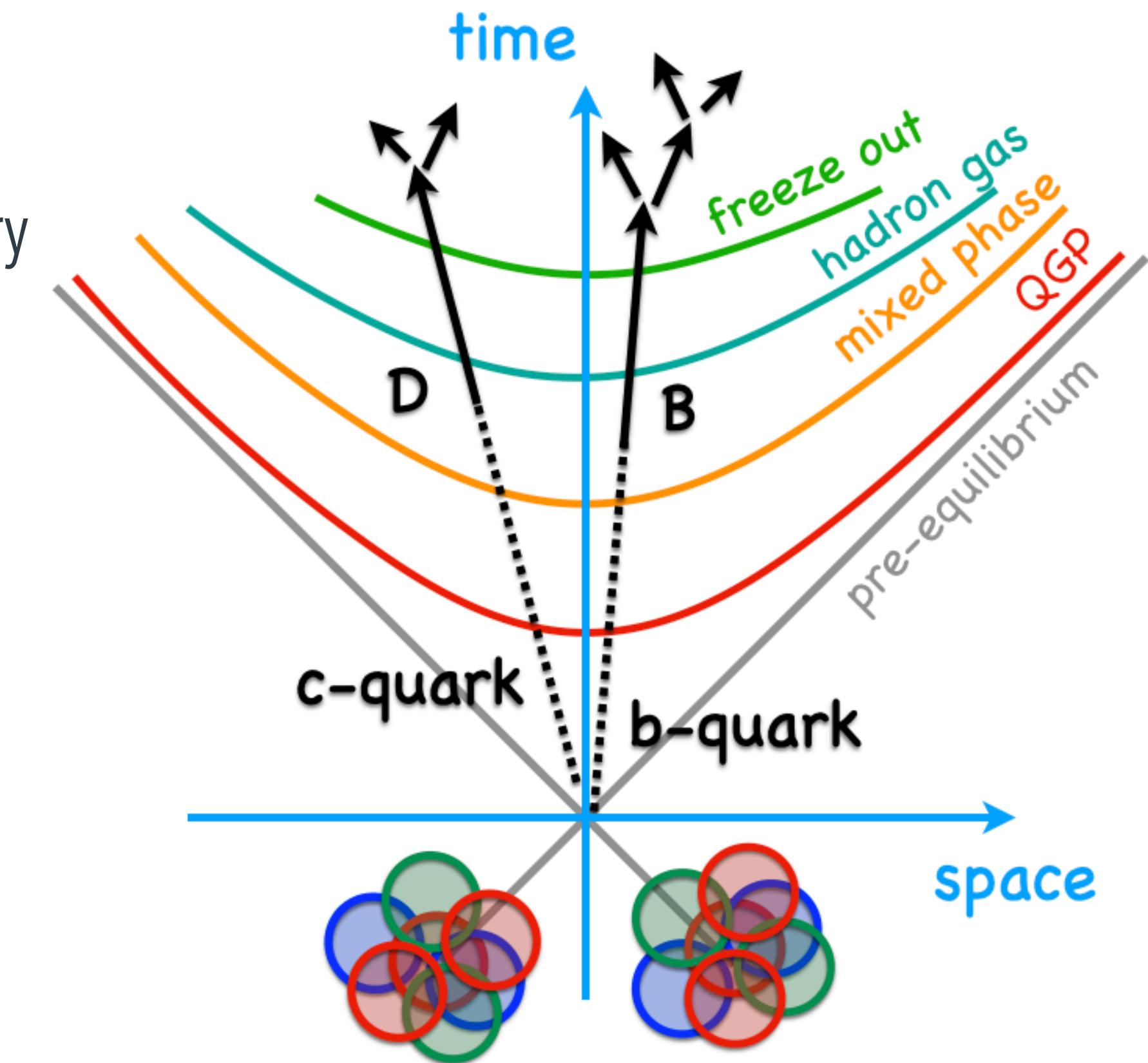
- Charm molecules?

System	$I(JP(C))$	Candidate
np	0 ( $1^+$ )	deuteron
ND	0 ( $1/2^-$ )	$\Lambda_c(2765)$
ND*	0 ( $3/2^-$ )	$\Lambda_c(2940)$
ND	0 ( $1/2^-$ )	$\Sigma_c(2800)$
$D^*\bar{D}$	0 ( $1^{++}$ )	$X(3872)$
$D^*D$	0 ( $1^+$ )	$T_{cc}$
$D_1\bar{D}$	0 ( $1^{--}$ )	$\Upsilon(4260)$
$D_1\bar{D}^*$	0 ( $1^{--}$ )	$\Upsilon(4360)$
$\Sigma\bar{D}$	1/2 ( $1/2^-$ )	$P_c(4312)$
$\Sigma\bar{D}^*$	1/2 ( $1/2^-$ )	$P_c(4457)$
$\Sigma\bar{D}^*$	1/2 ( $3/2^-$ )	$P_c(4440)$

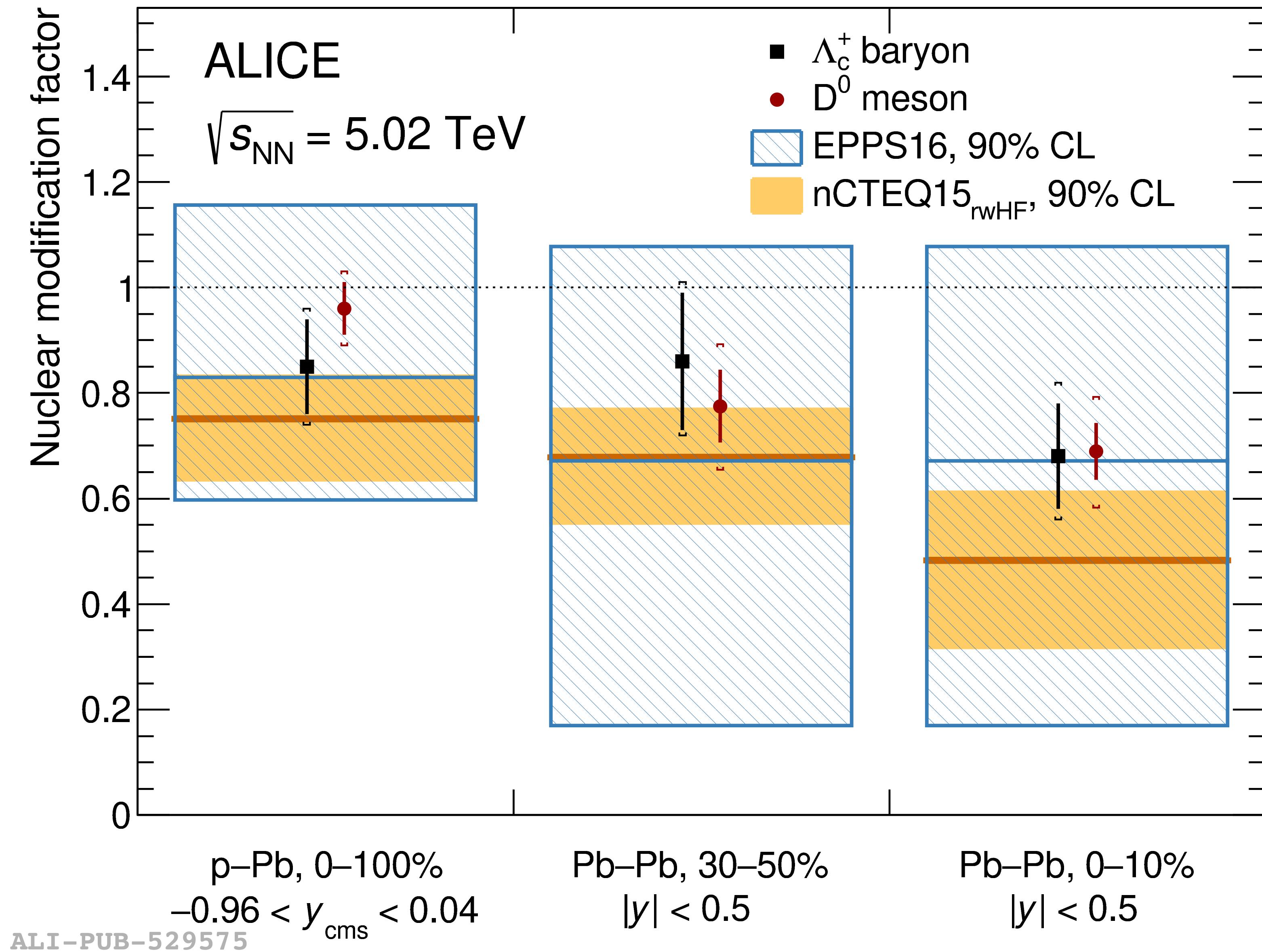


- Interplay between system size and scattering length  
→ Size-dependent modification of  $C(k^*)$  in presence of a molecular state

- Heavy quarks are very good probes of the QGP
  - Comparison with models useful to extract **transport coefficients**
  - Precise estimates: understanding of all the other model ingredients necessary
- Experimental observables to study their interaction with QGP constituents
  - Baryon-to-meson and strange-to-nonstrange ratios and production of quarkonia and multi-charm/beauty states: **hadronisation from the QGP**
  - Study residual strong interaction with femtoscopy: **hadronic rescattering**
- Future heavy-ion runs** crucial to better understand HF interactions with the QGP



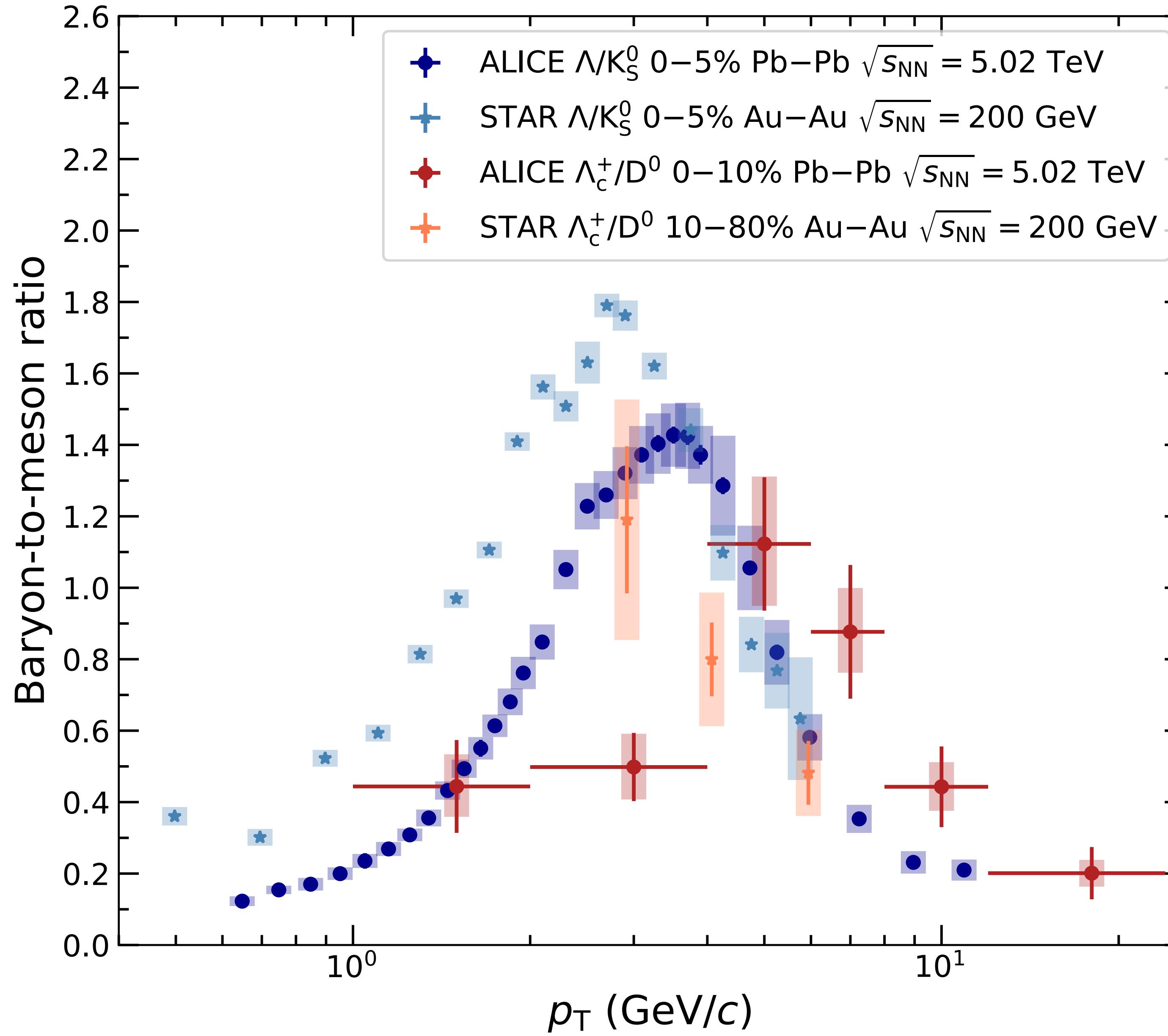
# ADDITIONAL SLIDES



# $\Lambda_c^+/D^0$ and $\Lambda/K_S^0$ at RHIC and LHC

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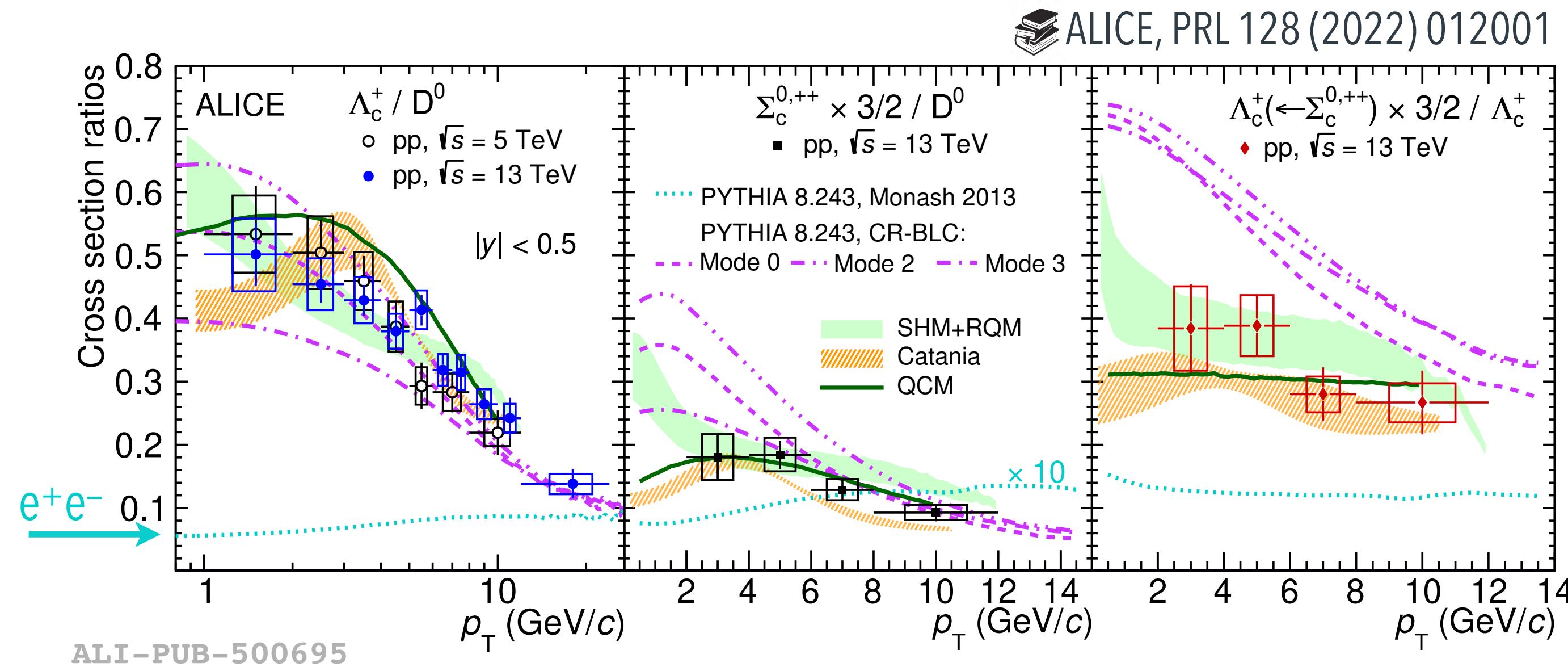


- Harder  $p_T$  distribution of baryon-to-meson ratio at LHC compared to RHIC
- Stronger radial flow

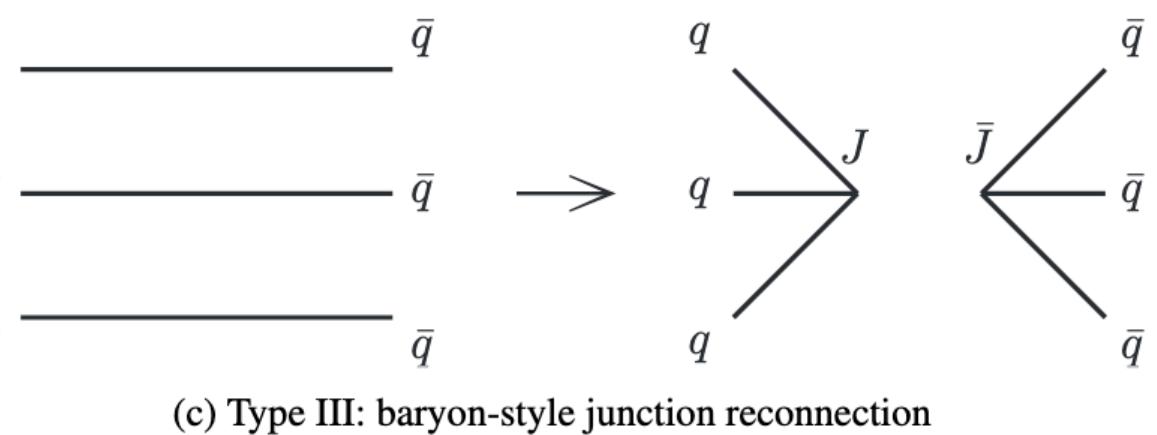
# Baryon enhancement in pp collisions

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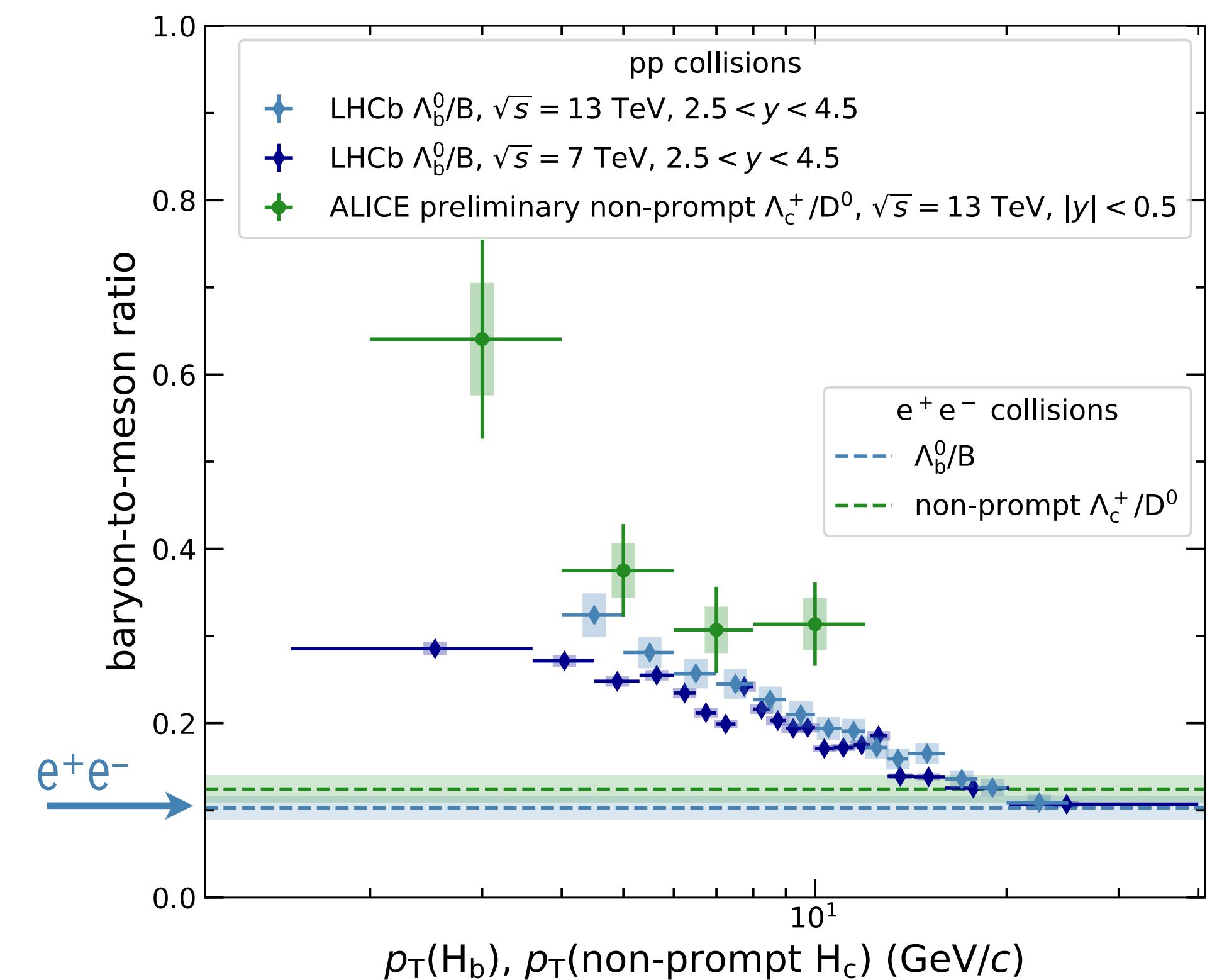
- Color Reconnection (PYTHIA8)
- J.P. Christiansen, P.Z. Skands, JHEP 08 (2015) 003



- Quark coalescence (+fragmentation)
- V. Minissale, S. Plumari, V. Greco PLB 821 (2021) 136622
- J. Song, H. Li, F.-I. Shao et al EPJC (2018) 78: 344

- Statistical hadronisation model with augmented set of charm-baryon excited states from lattice QCD
- M. He, R. Rapp, PLB 795 (2019) 117-121

- Ground and excited charm baryons enhanced compared to e<sup>+</sup>e<sup>-</sup> collisions
- **Similar enhancement observed in the beauty sector**

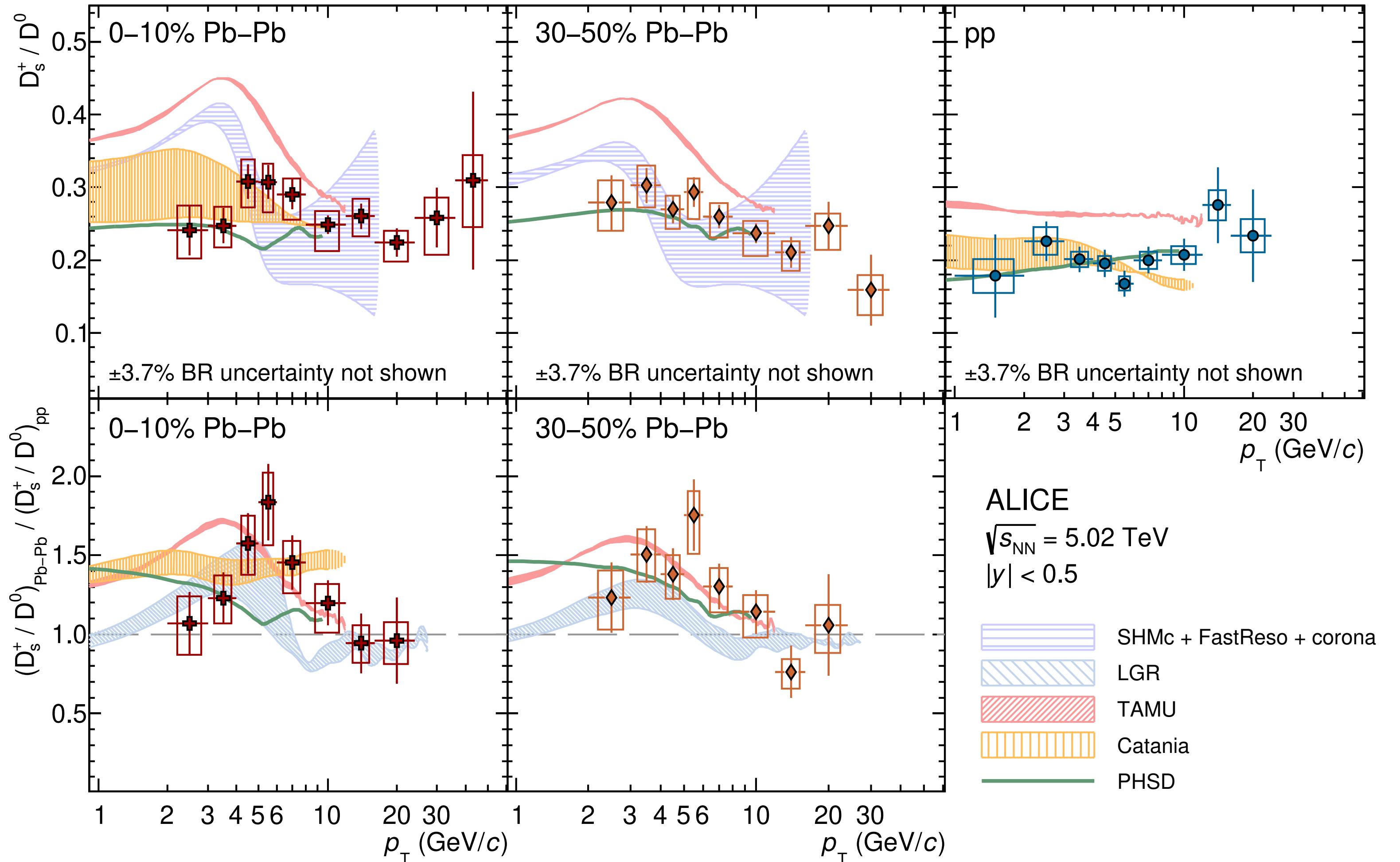


- LHCb, JHEP 08(2014)143
- LHCb, PRD 100 (2019) 3, 031102
- PDG, PTEP 8 (2020) 083C01
- ALICE, preliminary
- EPJC 75 (2015) 19

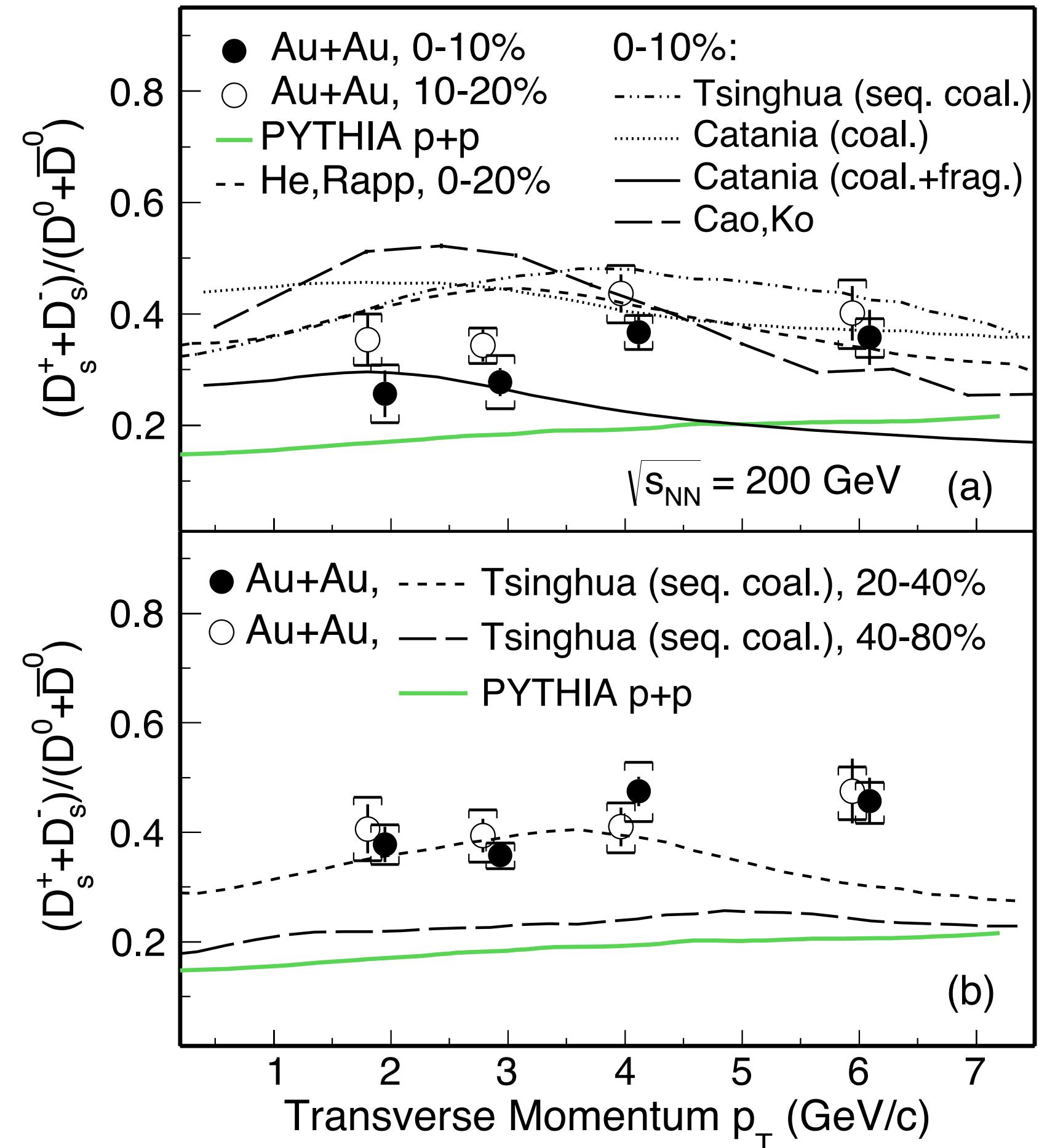
# $D_s^+ / D^0$ in Pb–Pb collisions compared with models

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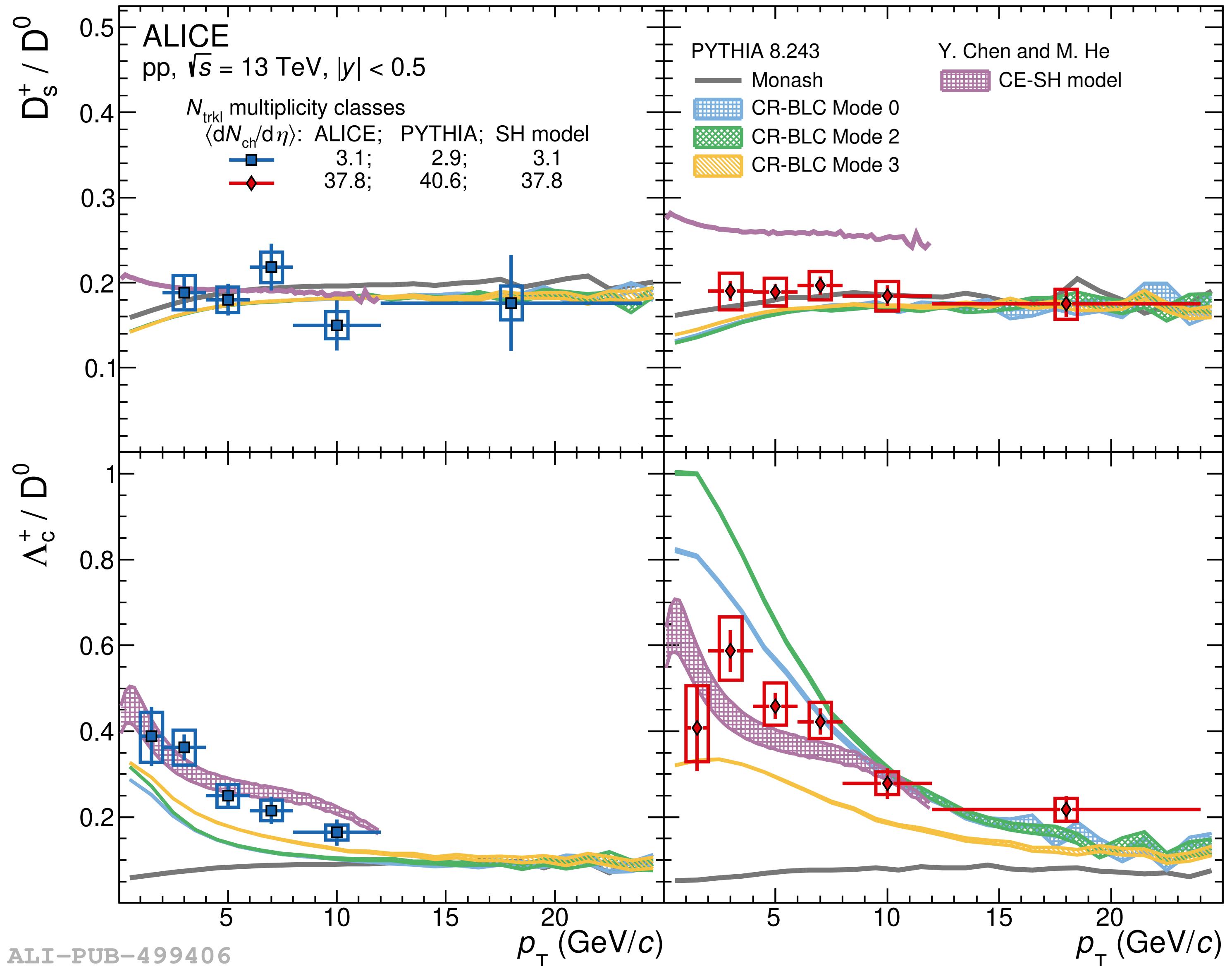
ALICE-PUB-522154



# $D_s^+/D^0$ and $\Lambda_c^+/D^0$ in pp collisions as a function of multiplicity

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- Significant modification of the  $p_T$  dependence of the  $\Lambda_c^+/D^0$  ratio as a function of multiplicity in pp collisions
- No multiplicity dependence observed for  $D_s^+/D^0$  in pp collisions

# Searches for strong magnetic fields and hadronisation

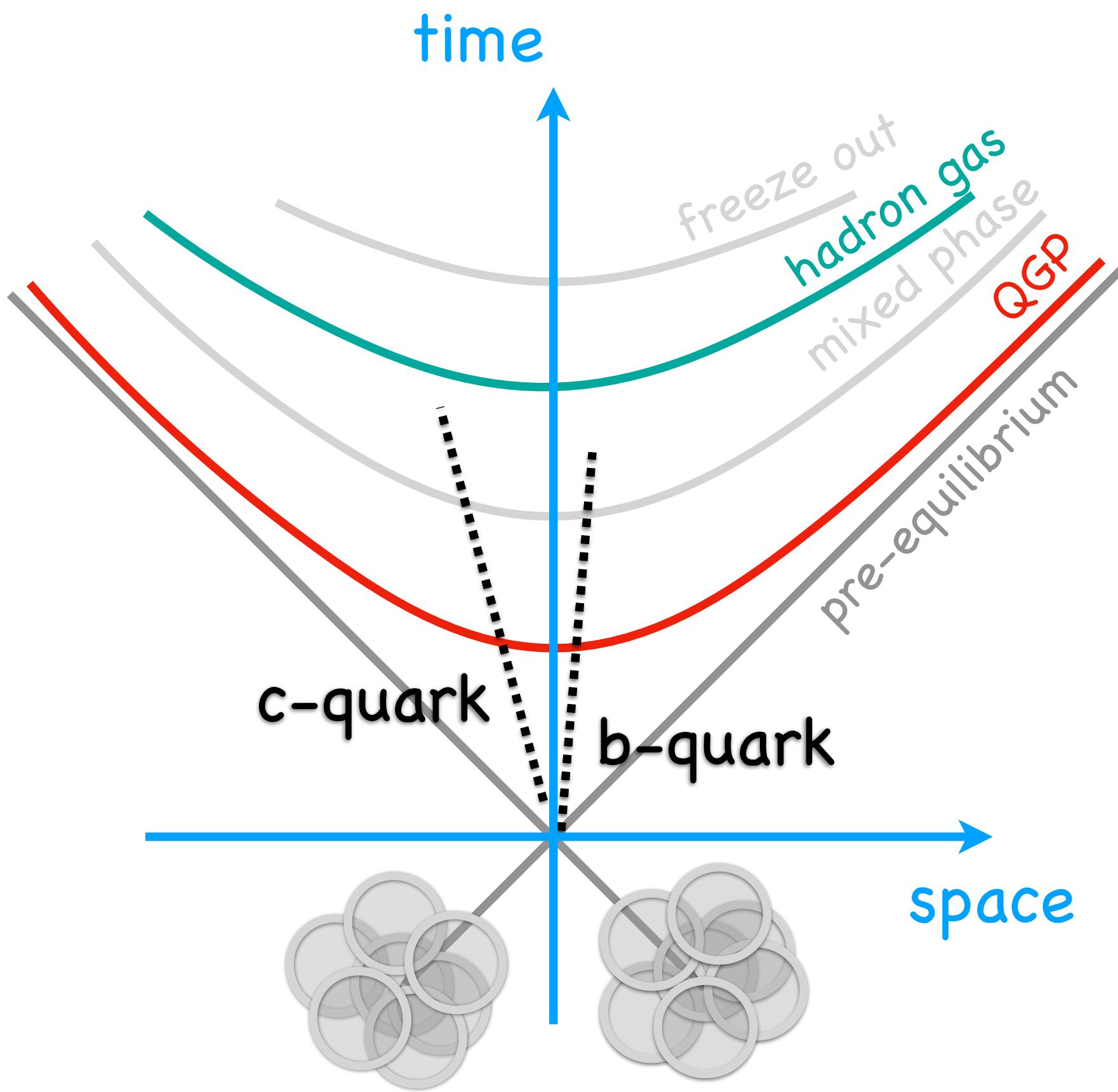
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- Non-central heavy-ion collisions
  - Large angular momentum due to the medium rotation is predicted
  - Huge initial magnetic field ( $B \sim 10^{14}$  T) is expected to be formed

Becattini et al, PRC 77 (2008) 024906

Kharzeev et al, NPA 803 (2008) 227-253



- Charm quarks are produced in the initial stage of the collision and hence are expected to be more sensitive to the magnetic field

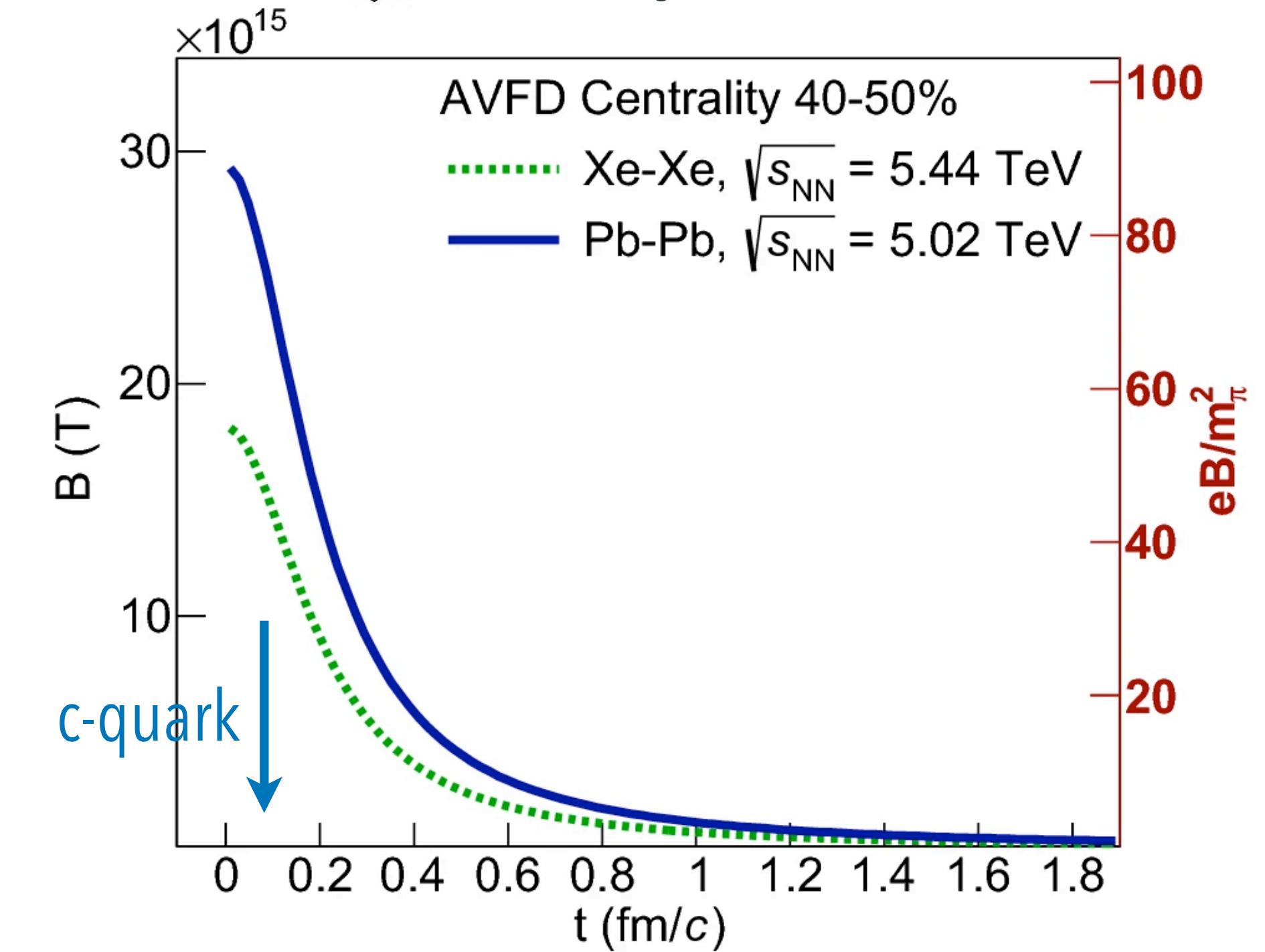
- Quark-coalescence model
  - Spin alignment:

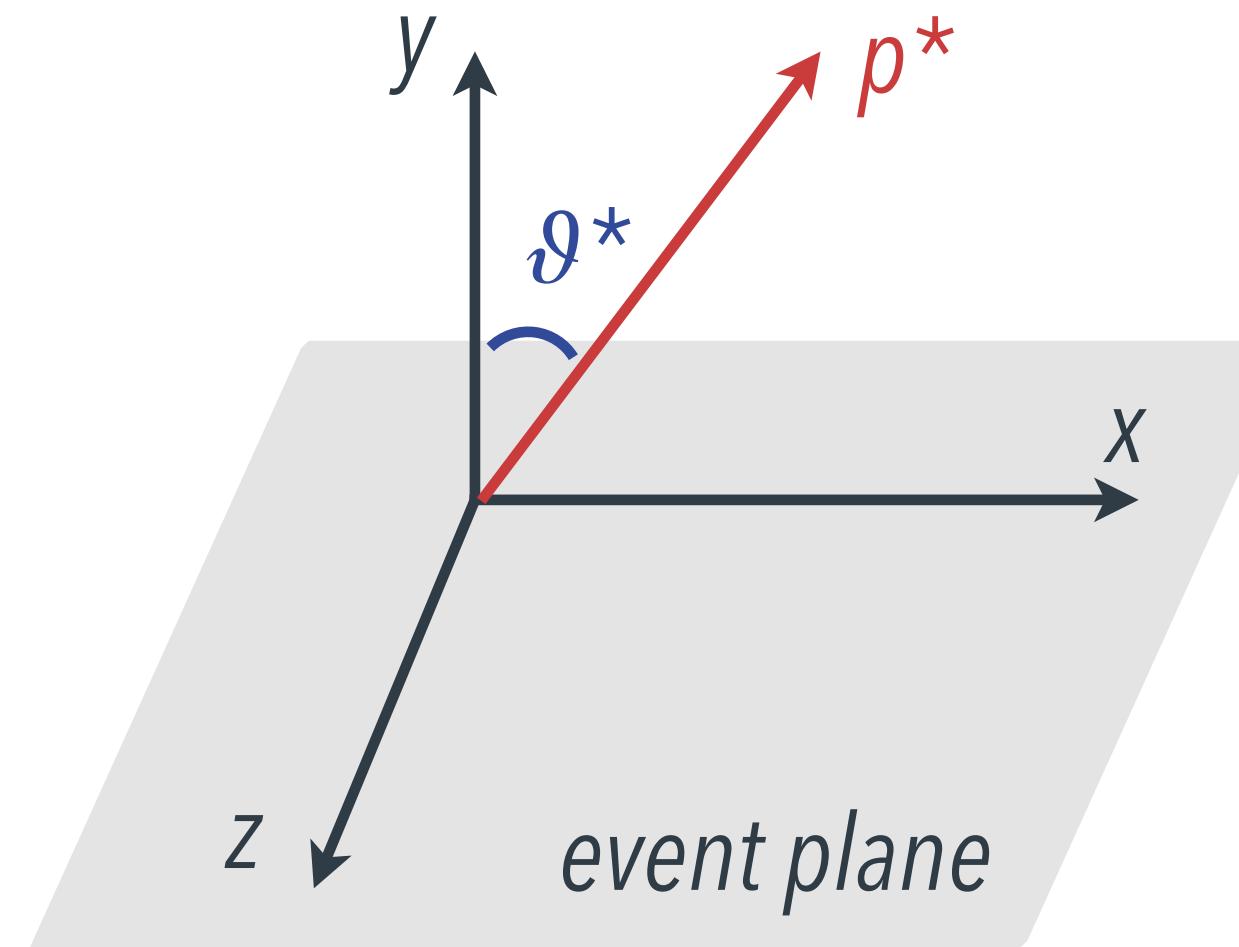
Y.-G. Yang et al, PRC 97 (2018) 034917

$$\rho_{00}(\omega, B) = \boxed{\frac{1}{3}} - \boxed{\frac{1}{9}(\beta\omega)^2} - \boxed{\frac{1}{9}\beta^2 \frac{Q_1 Q_2}{m_1 m_2} B^2}$$

no polarisation      angular momentum      magnetic field

P. Christakouglu et al, EPJC 81 (2021) 717





- Polarisation of J/ $\psi$  mesons studied with respect to event plane

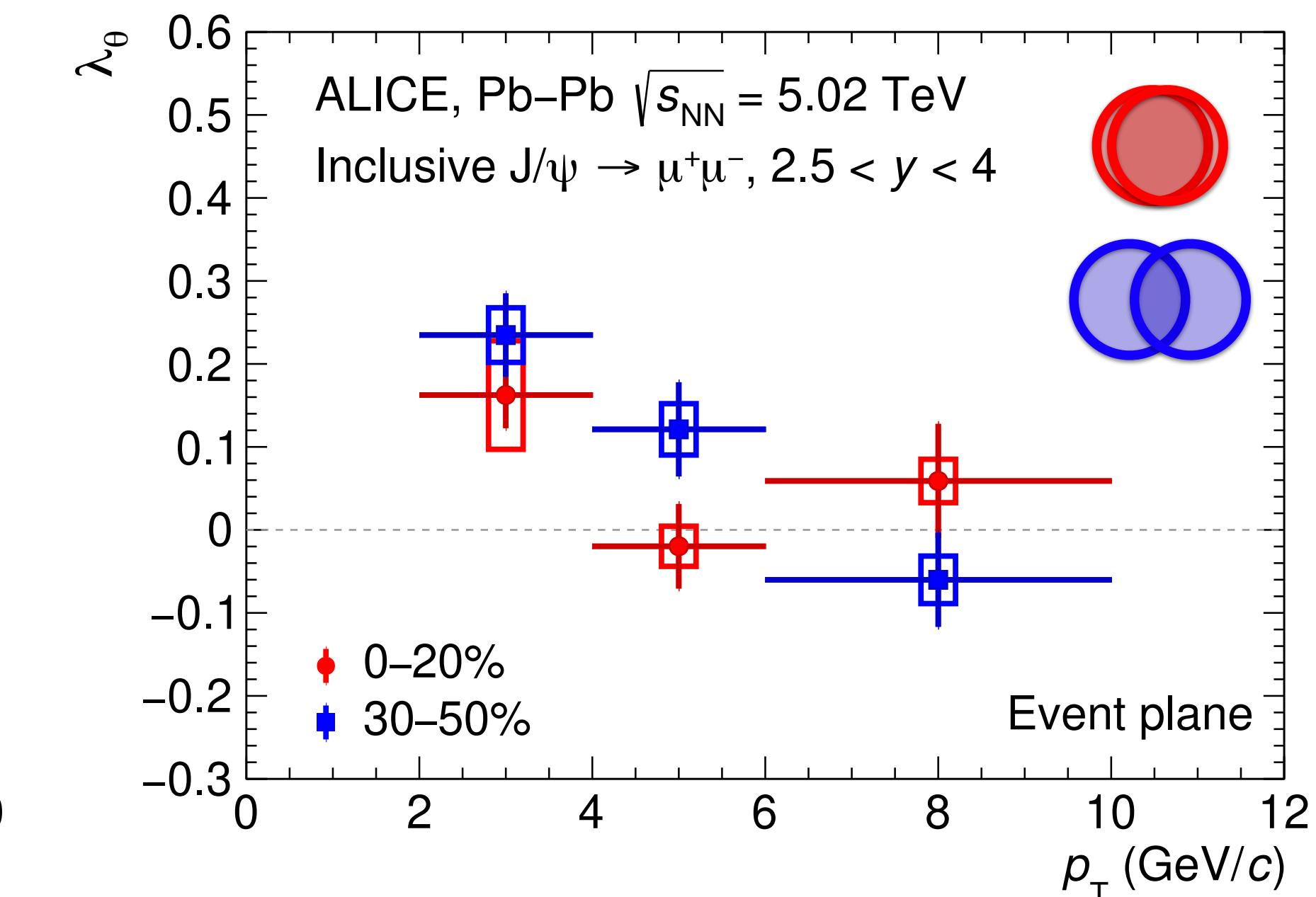
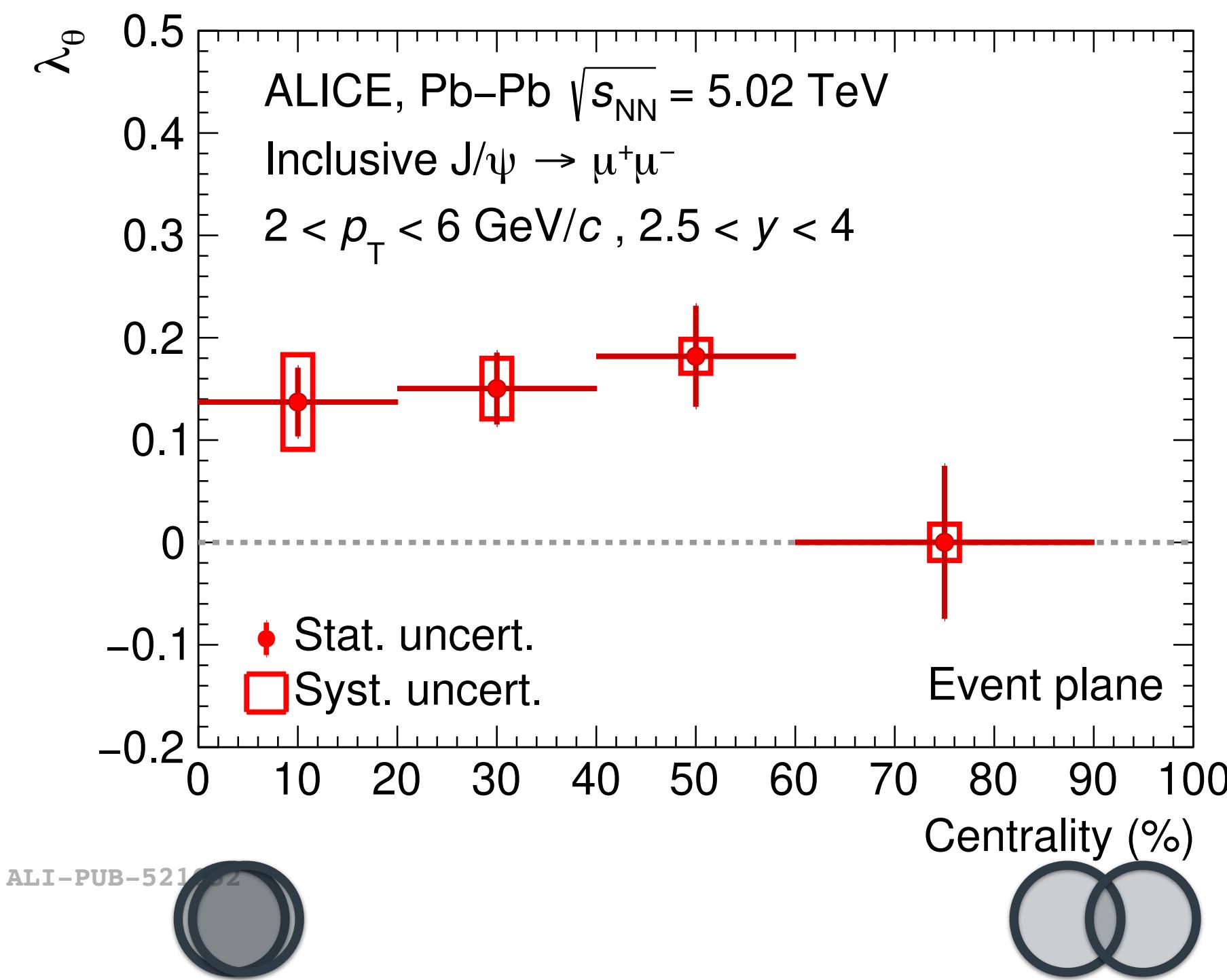
$$W(\theta) \propto \frac{1}{1 + 3\lambda_\theta} (1 + \lambda_\theta \cos^2 \theta)$$

Can be related to the spin-density matrix element  $\rho_{00}$

$$\lambda_\theta \propto (3\rho_{00} - 1)/(1 - \rho_{00})$$

- Evidence of J/ $\psi$  polarisation with respect to event plane
  - Opposite direction that of light vector mesons

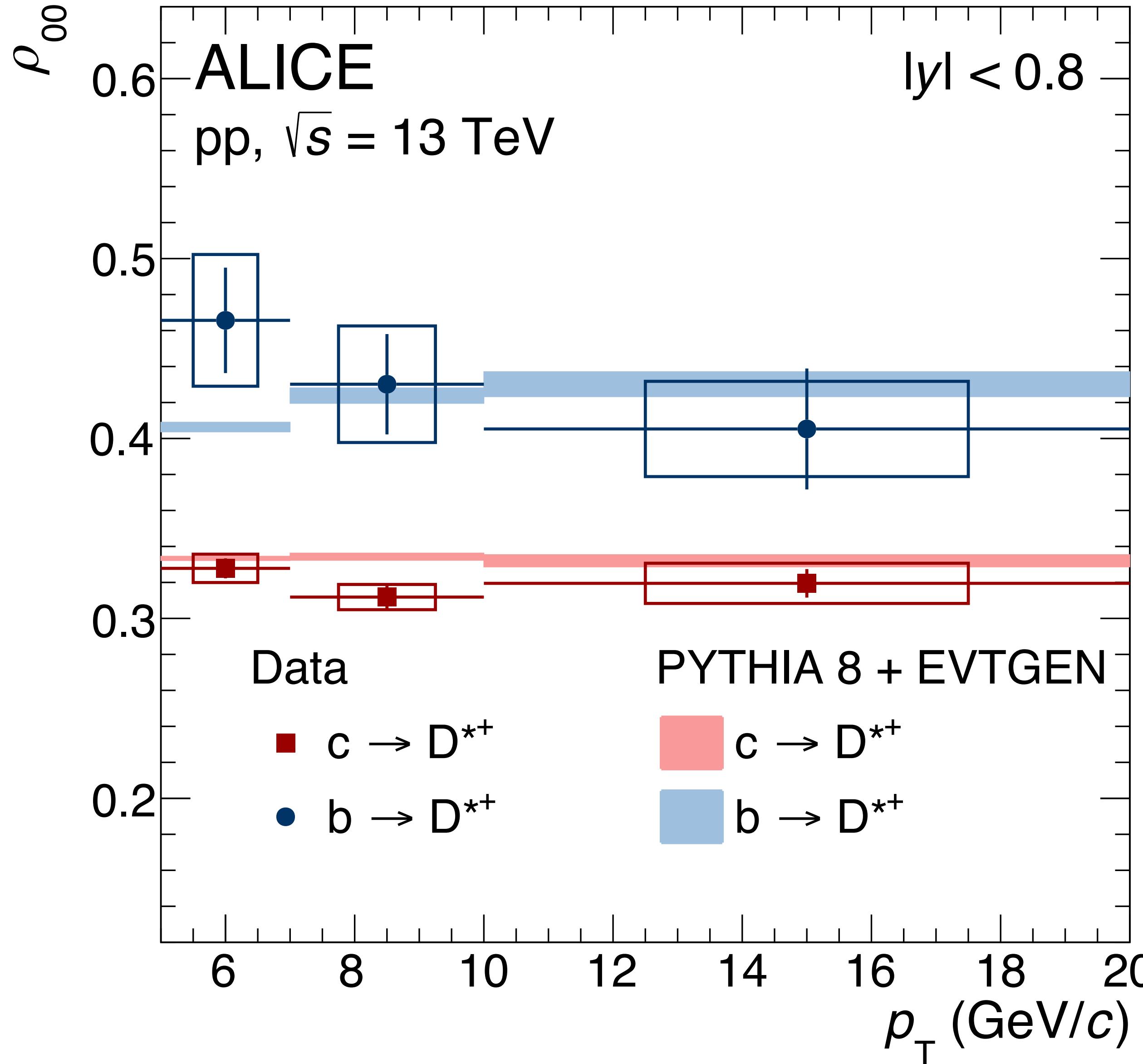
$$\lambda_\theta^{J/\psi} > 0, \rho_{00}^{\phi, K^{*0}} < 1/3$$



# Polarisation and spin alignment of more charm and beauty hadrons

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- Spin alignment of prompt and non-prompt charm vector mesons with respect to helicity axis in pp collisions
  - Prompt  $D^{*+}$  compatible with no polarisation
  - Non-prompt  $D^{*+}$   $\rho_{00} > 1/3$  (helicity conservation in  $B \rightarrow D^{*+} X$  decays)
- Measurement of  $D^{*+}$  vector mesons in heavy-ion collisions crucial to complete the picture for c-quark

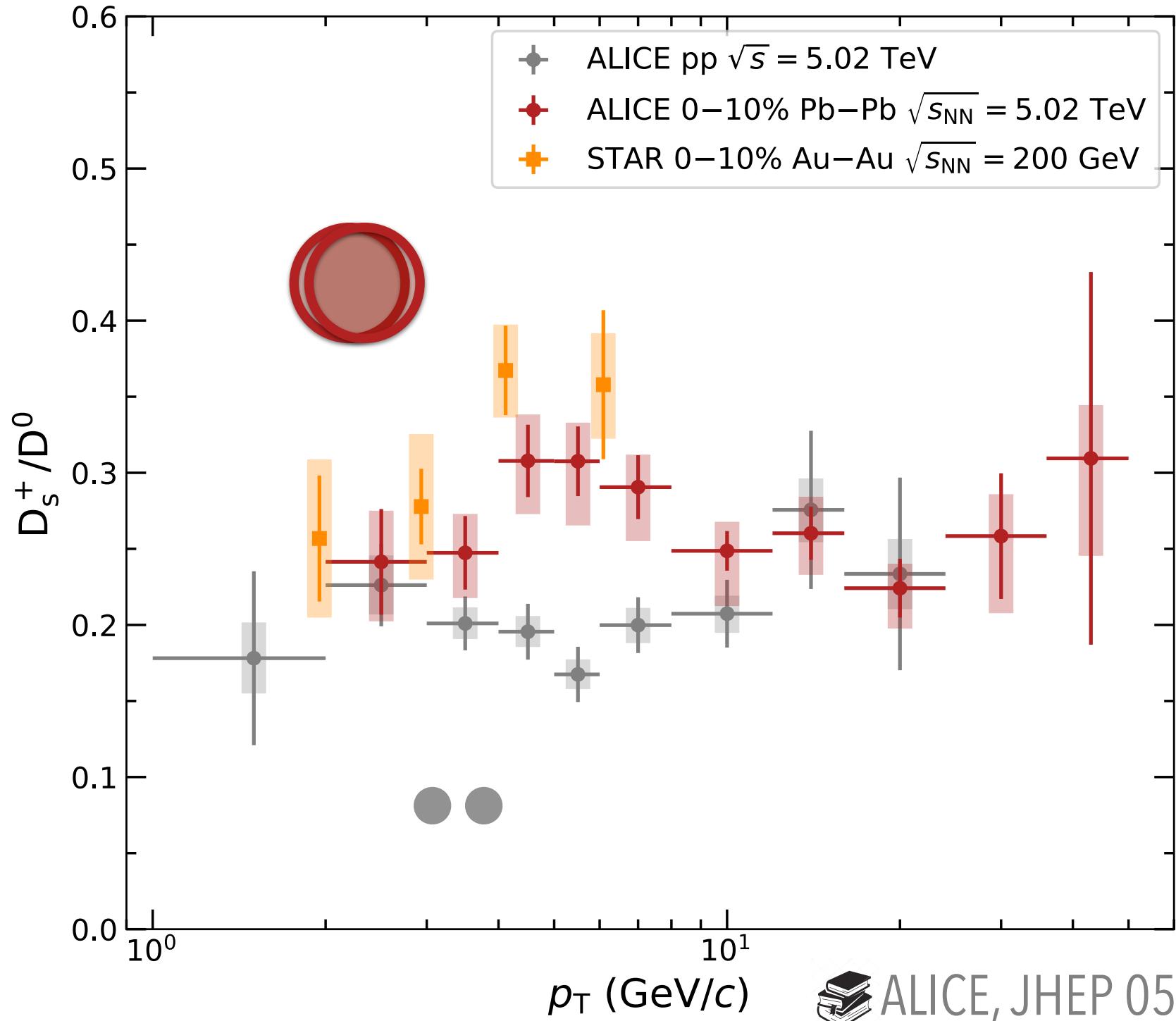
# Heavy-quark hadronisation and strangeness enhancement

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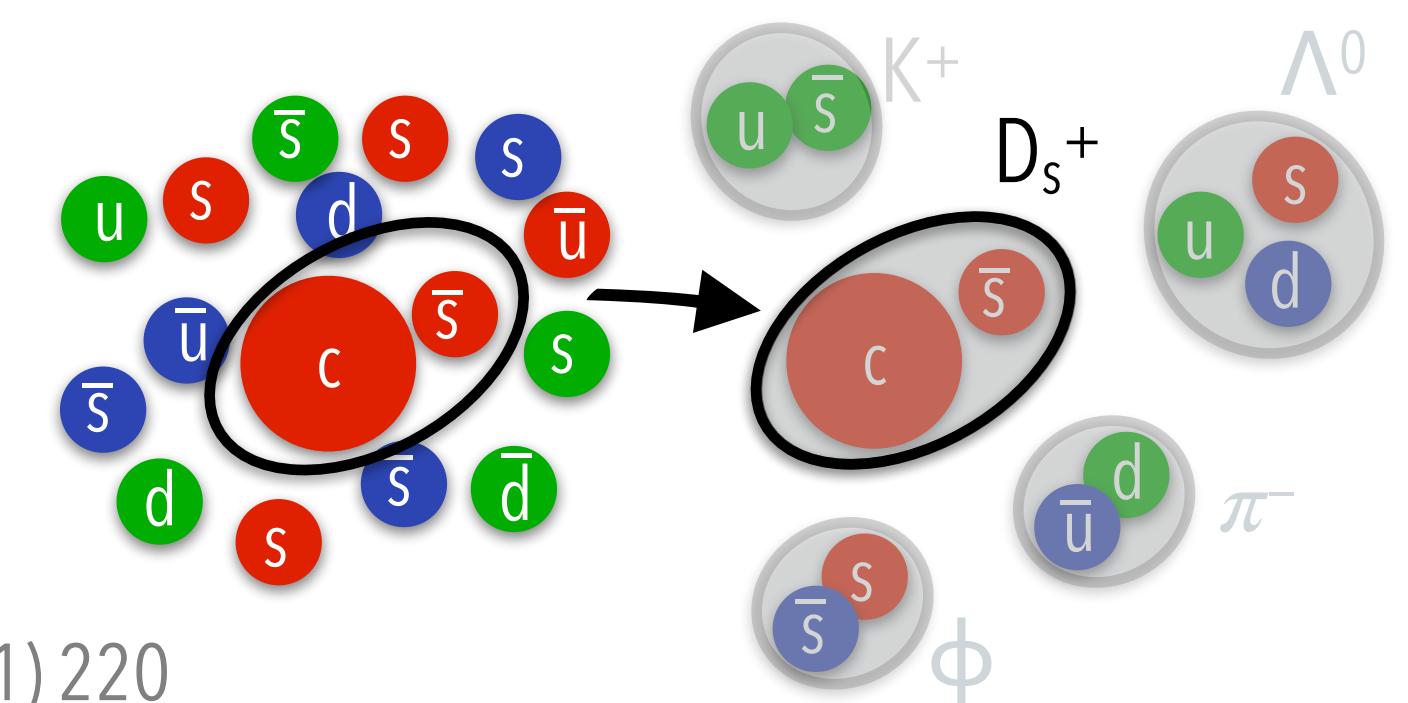
ALICE, PLB 827 (2022) 136986

STAR, PRL 127 (2021) 092301

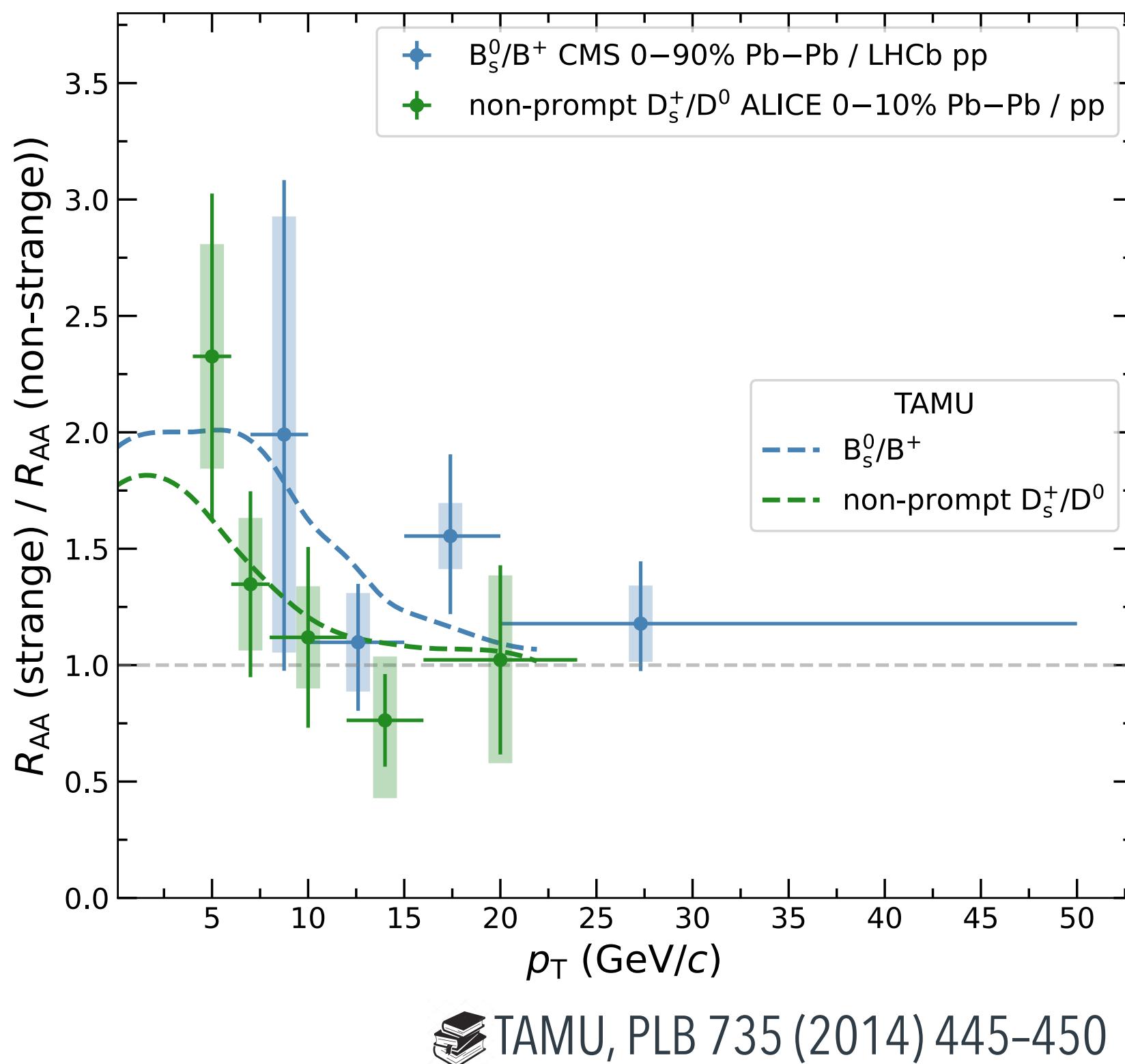


ALICE, JHEP 05 (2021) 220

- Abundant production of strange quarks in the QGP (strangeness enhancement)
- Hadronisation via recombination → strange hadrons expected to be enhanced  
→ (Partial) thermal equilibrium required
- **Strange-to-nonstrange ratio higher in Pb–Pb than pp in charm sector**



ALICE, arXiv:2204.10386  
 CMS, PLB 829 (2022) 137062  
 LHCb, PRL 124 (2020) 122002

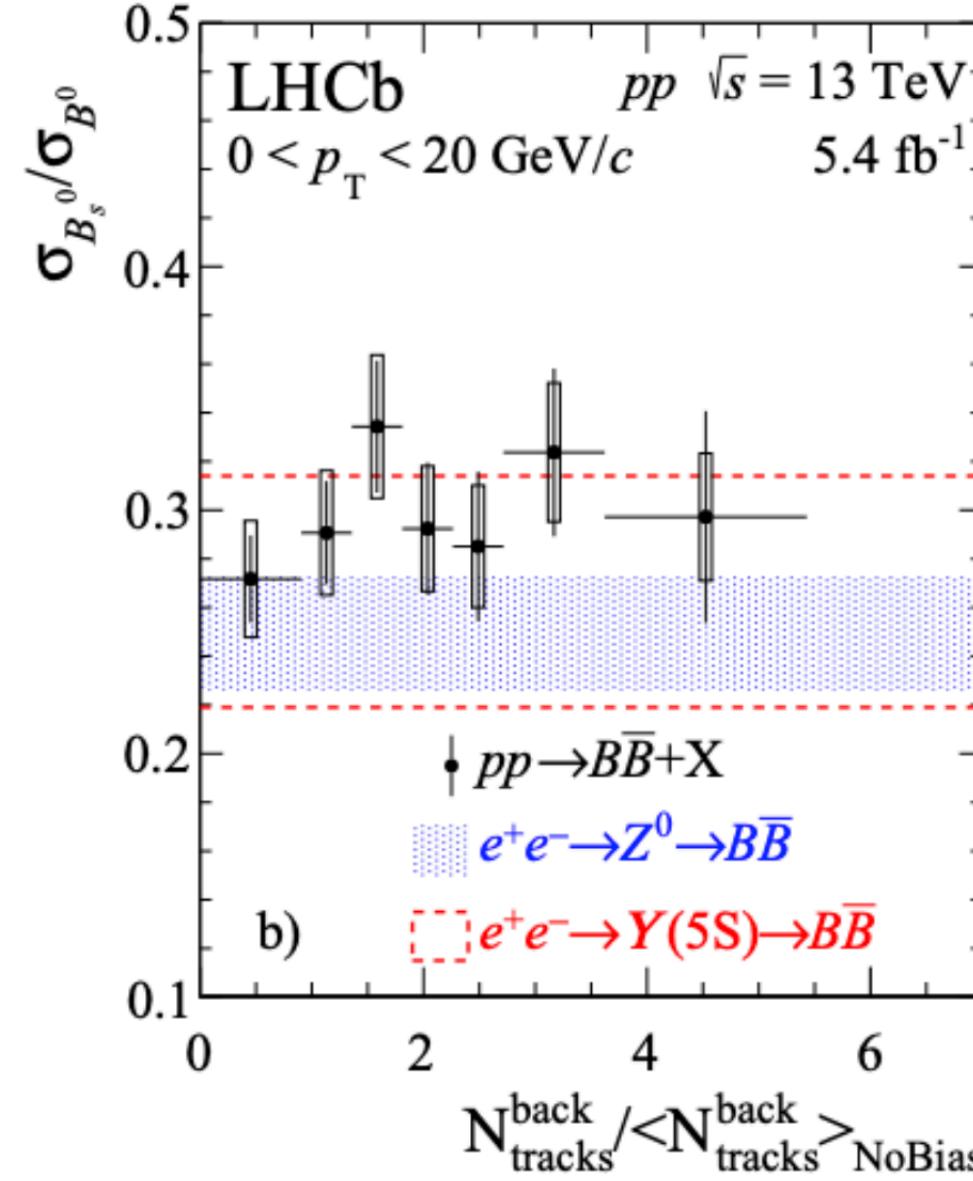
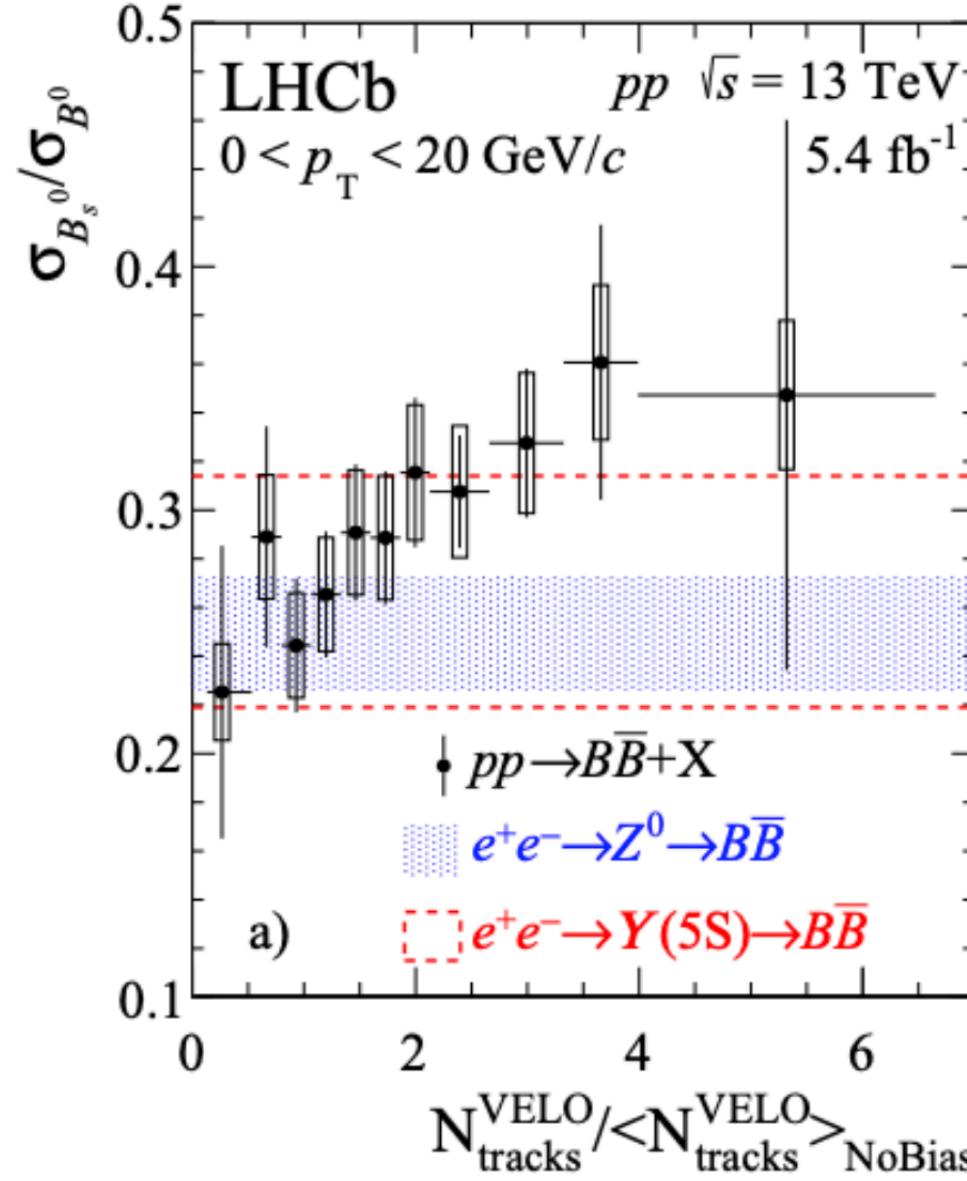


- Measurements in the beauty sector compatible with transport models implementing strangeness enhancement and hadronisation via recombination  
→ **Do beauty quarks reach (partial) thermalisation?**
- Current data precision limited: also **compatible with no enhancement scenario**  
→ Next LHC runs crucial to study the beauty sector

# $B_s^0/B^0$ in pp collisions as a function of multiplicity

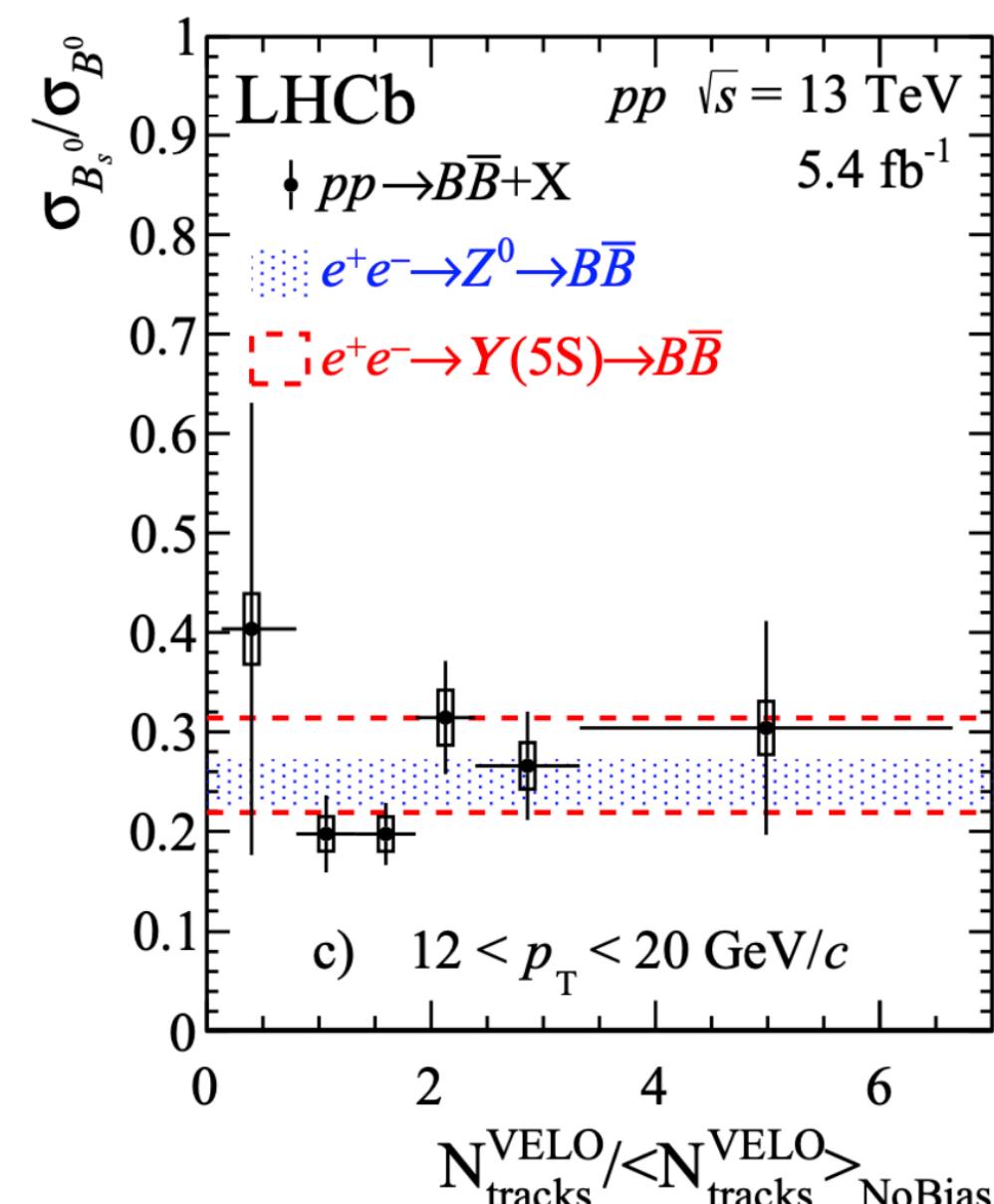
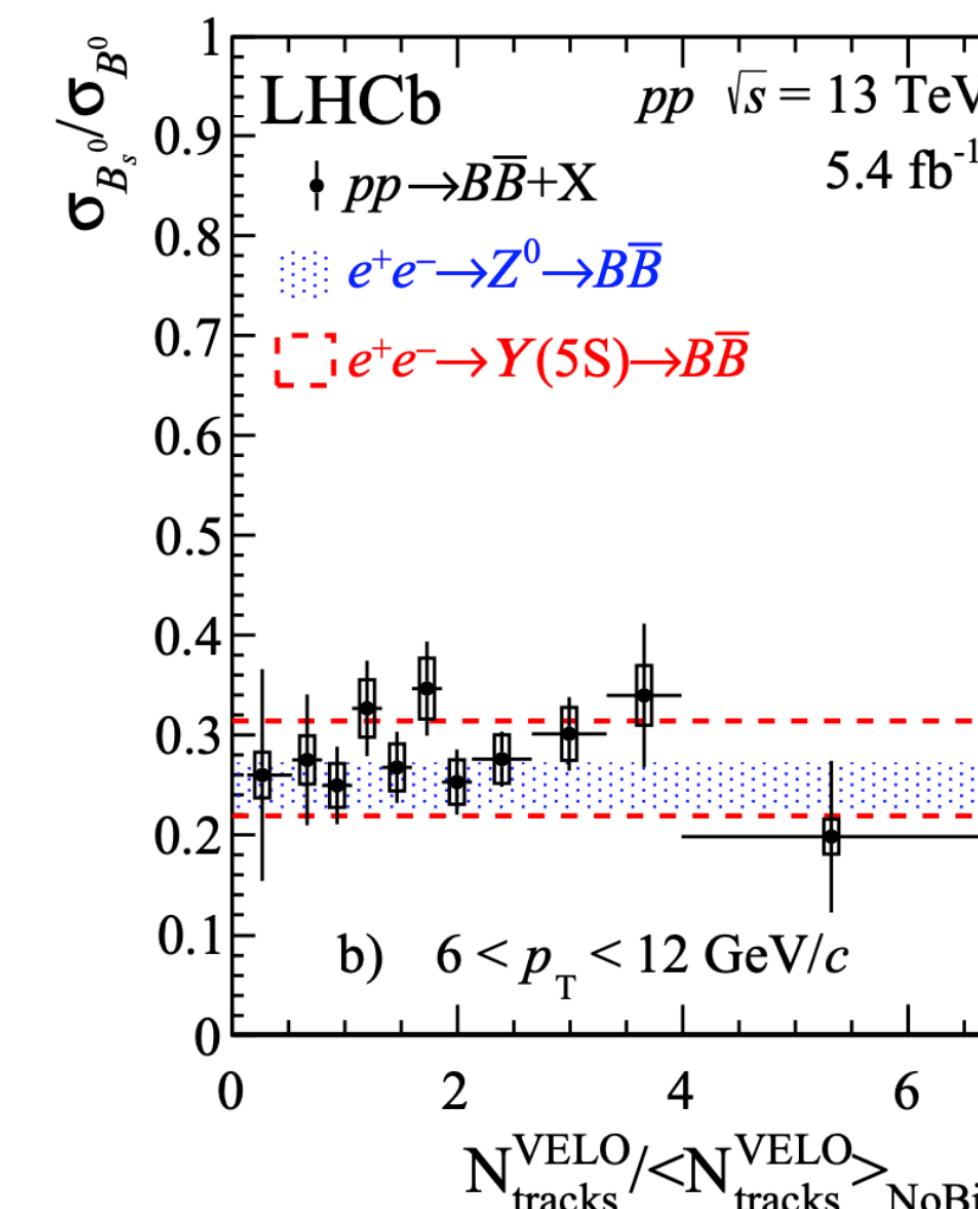
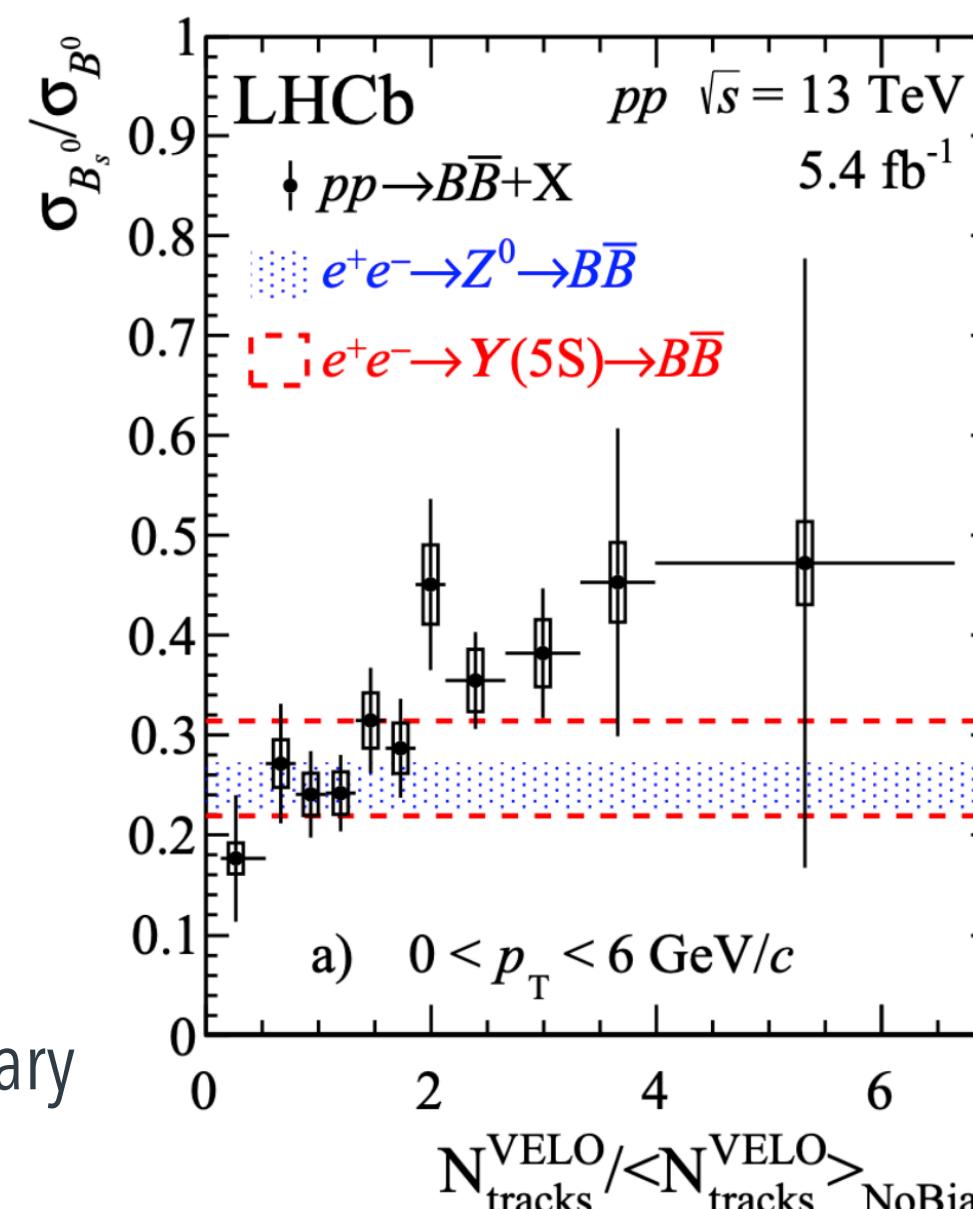
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- Multiplicity dependence of  $B_s^0/B^0$  in pp collisions
  - Significant in case of charged-particle multiplicity measured in the same rapidity range of B mesons
  - Not observed if charged-particle multiplicity measured with large pseudorapidity gap wrt B mesons

- Multiplicity dependence at low  $p_T$  only

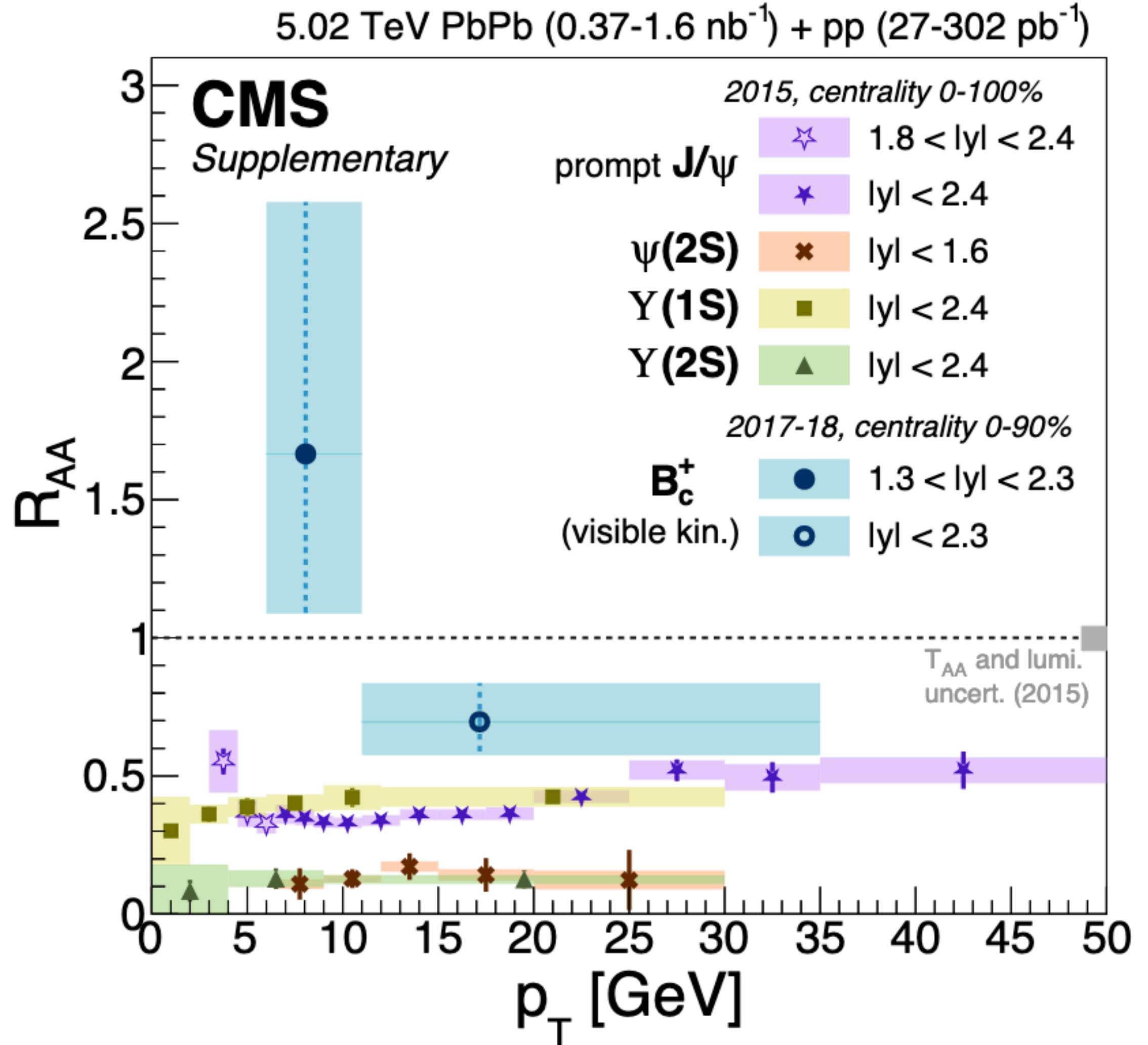
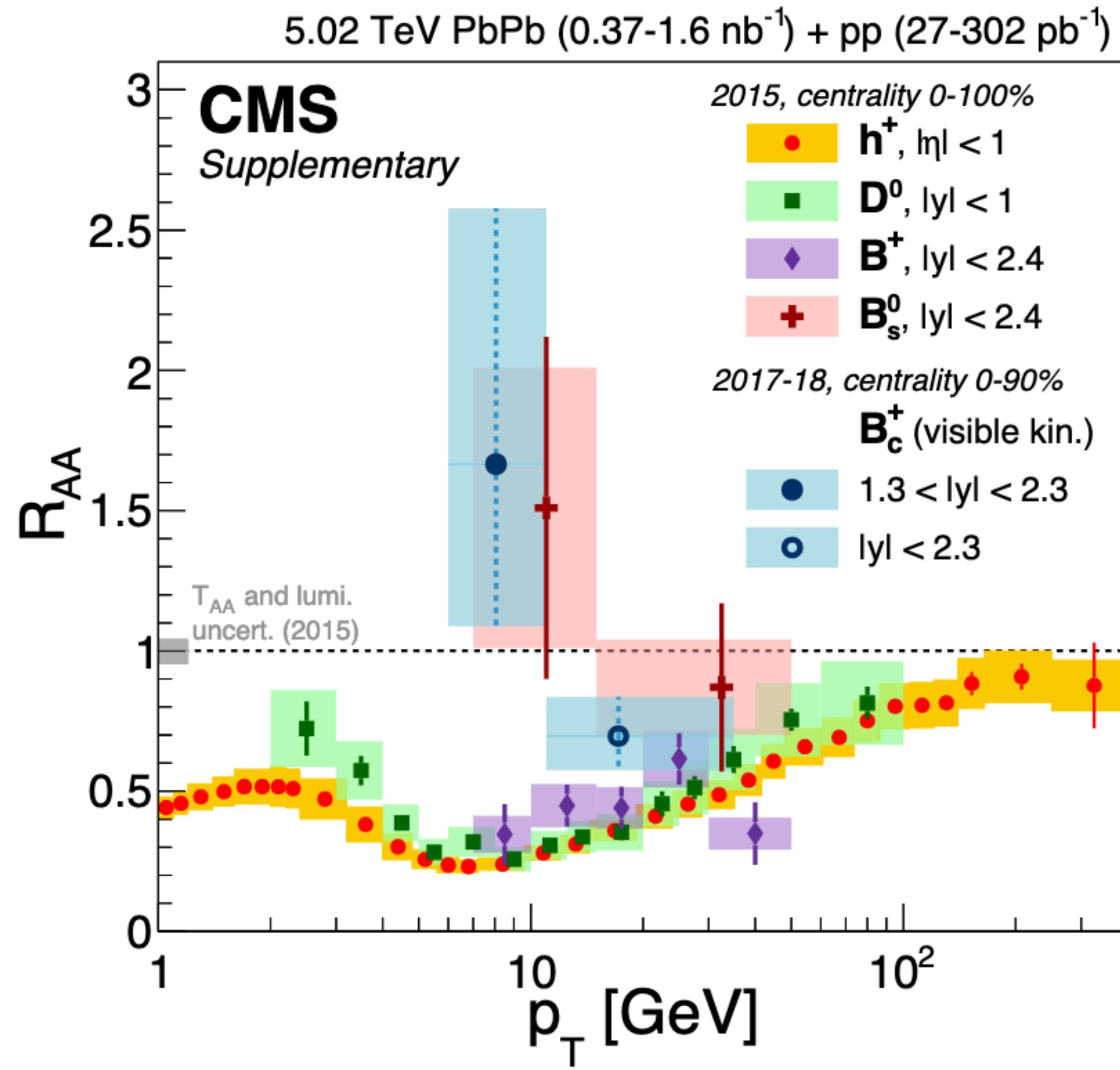


LHCb, preliminary

# $B_c^+$ production in Pb–Pb collisions

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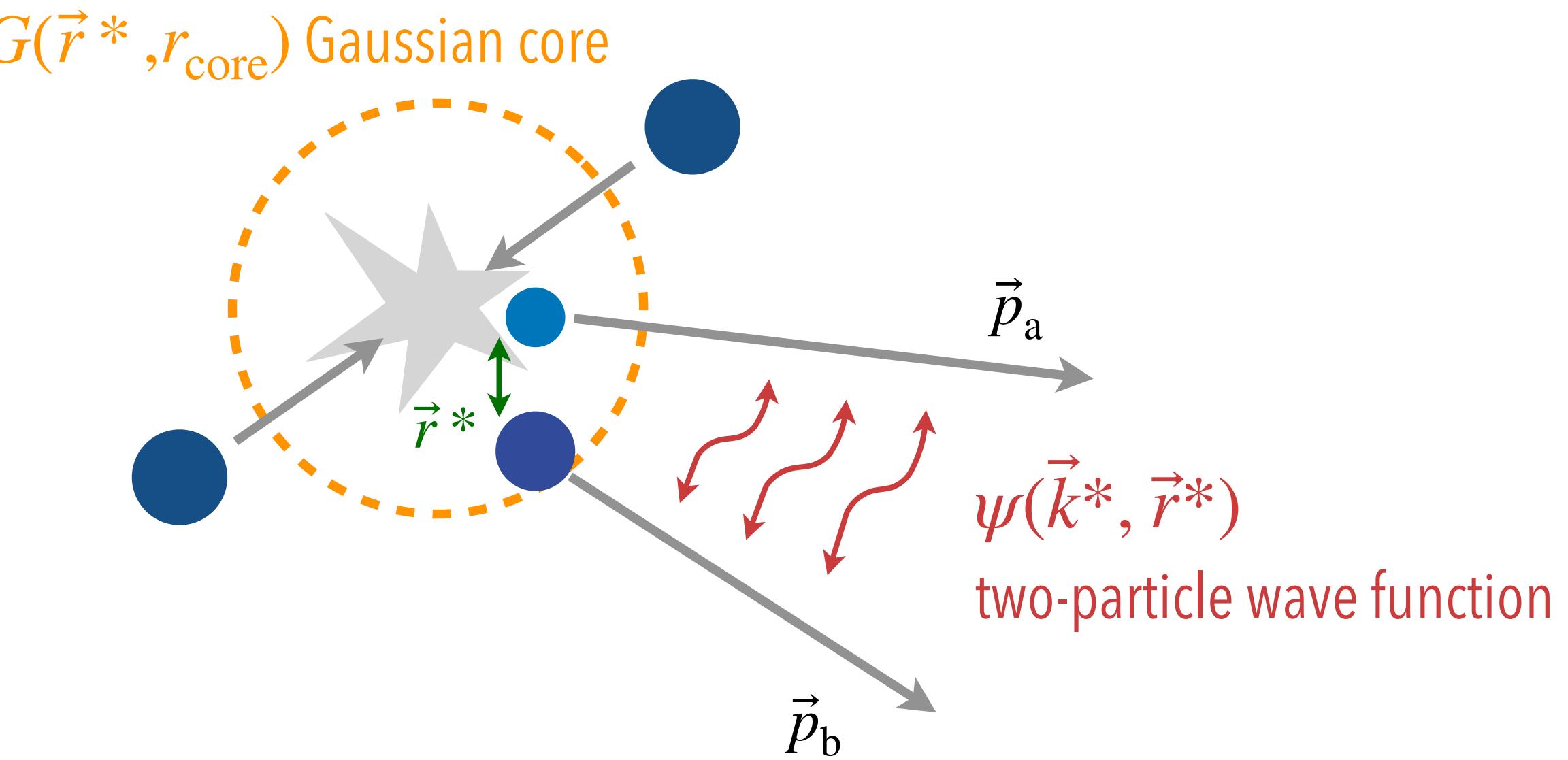
- Hint of  $R_{AA}(B_c^+) \sim R_{AA}(B_s^0) > R_{AA}(B)$  and  $R_{AA}(B_c^+) > R_{AA}(Y, J/\psi, \psi)$

# The emitting source of hadrons

$$C(\vec{k}^*) = \int S(\vec{r}^*) |\psi(\vec{k}^*, \vec{r}^*)|^2 d^3 r^*$$

- **Emitting source:** hypersurface at kinematic freezout of final-state particles
- Described with a Gaussian core

$$G(r^*, r_{\text{core}}(m_T)) = \frac{1}{(4\pi r_{\text{core}}^2(m_T))^{3/2}} \cdot \exp\left(-\frac{r^{*2}}{4r_{\text{core}}^2(m_T)}\right)$$



# The emitting source of hadrons

$$C(\vec{k}^*) = \int S(\vec{r}^*) |\psi(\vec{k}^*, \vec{r}^*)|^2 d^3 r^*$$

$S(\vec{r}^*)$  source function  
 $G(\vec{r}^*, r_{\text{core}})$  Gaussian core

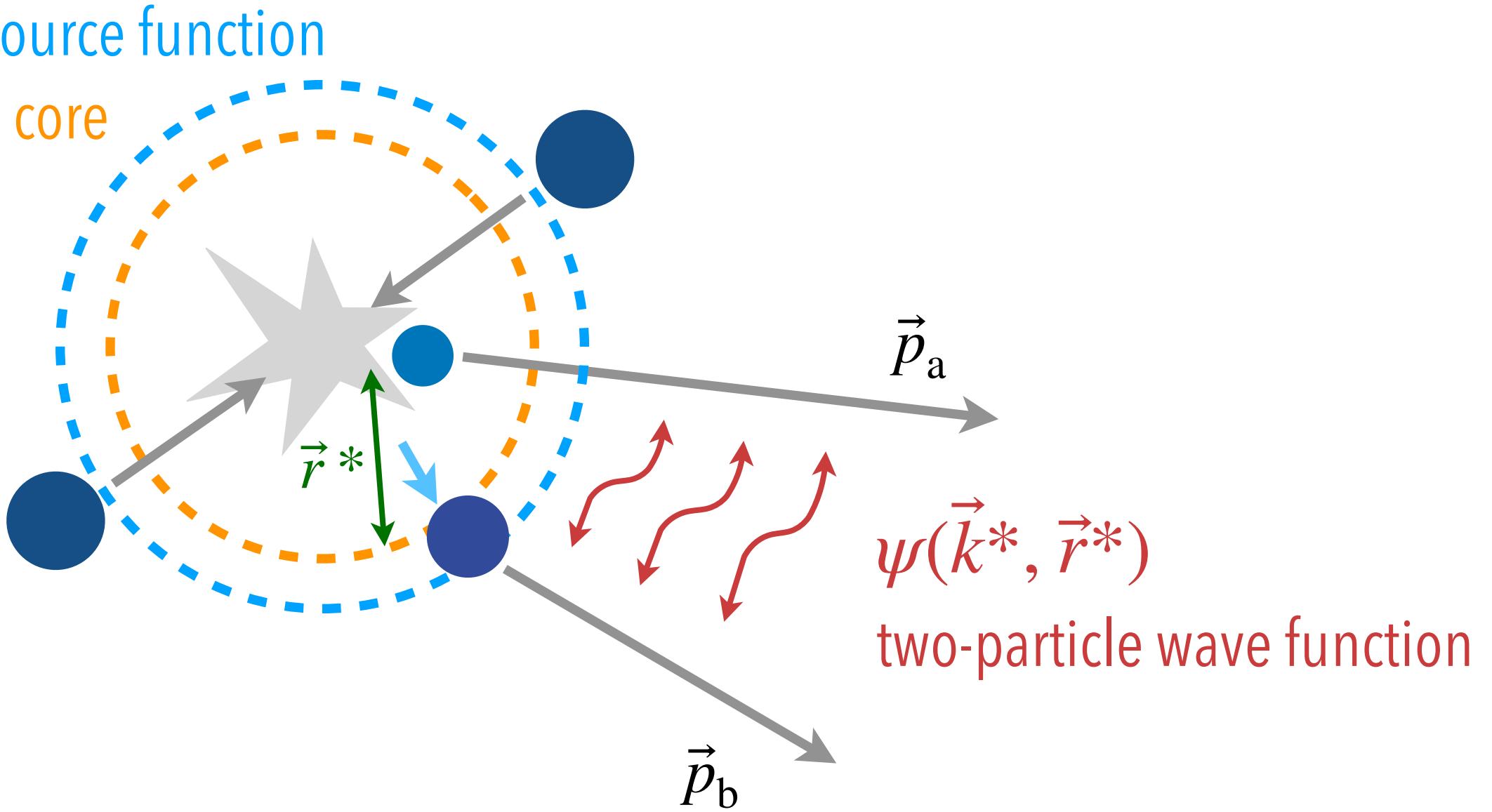
- **Emitting source**: hypersurface at kinematic freezout of final-state particles

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$$G(r^*, r_{\text{core}}(m_T)) = \frac{1}{(4\pi r_{\text{core}}^2(m_T))^{3/2}} \cdot \exp\left(-\frac{r^{*2}}{4r_{\text{core}}^2(m_T)}\right)$$

- Short-lived strongly decaying resonances effectively enlarge it

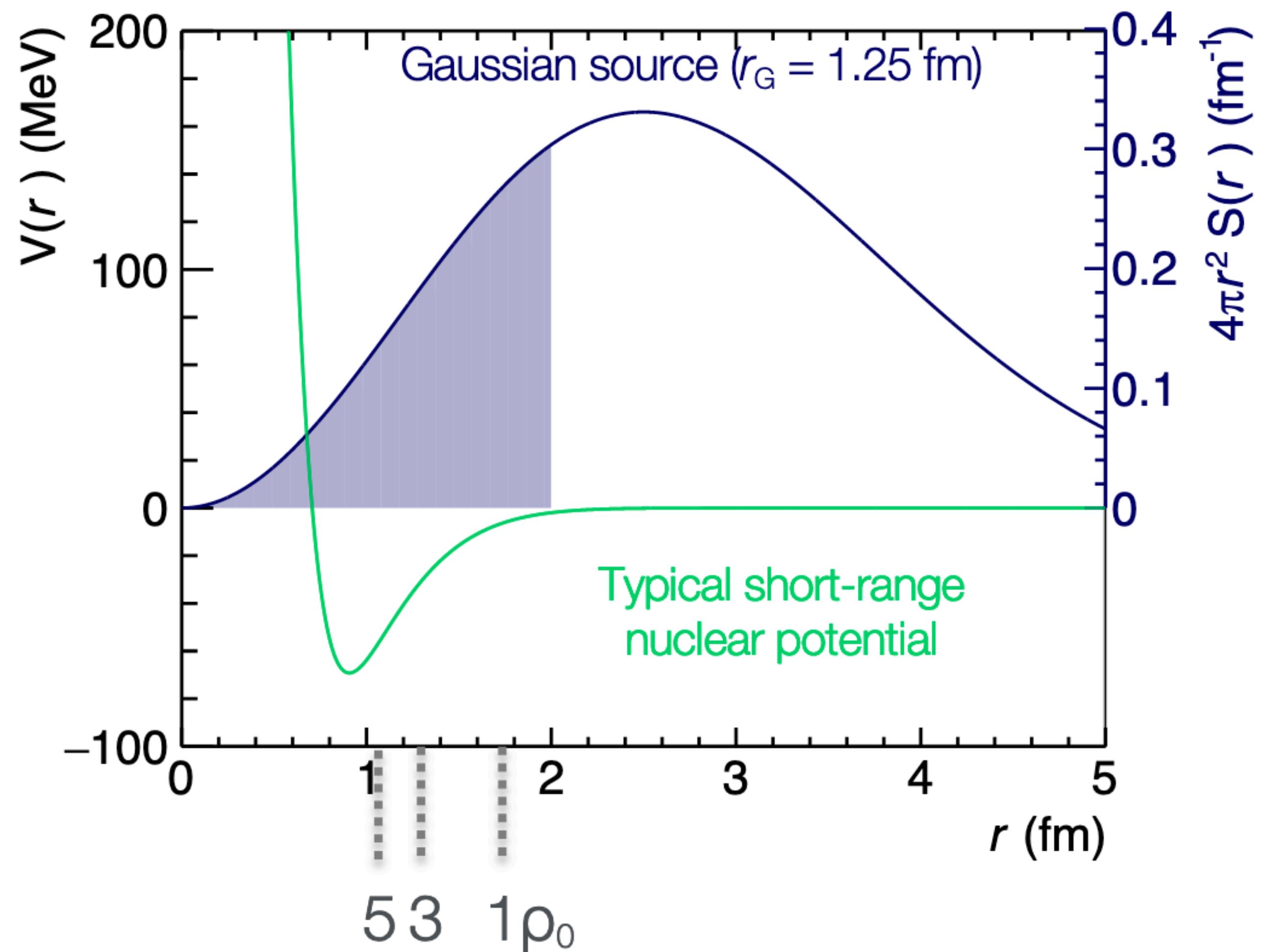
$$E(r^*, M_{\text{res}}, \tau_{\text{res}}, p_{\text{res}}) = \frac{1}{s} \exp\left(-\frac{r^*}{s}\right) \quad \text{with} \quad s = \beta \gamma \tau_{\text{res}} = \frac{p_{\text{res}}}{M_{\text{res}}} \tau_{\text{res}}$$



# Femtoscopy with small emitting sources

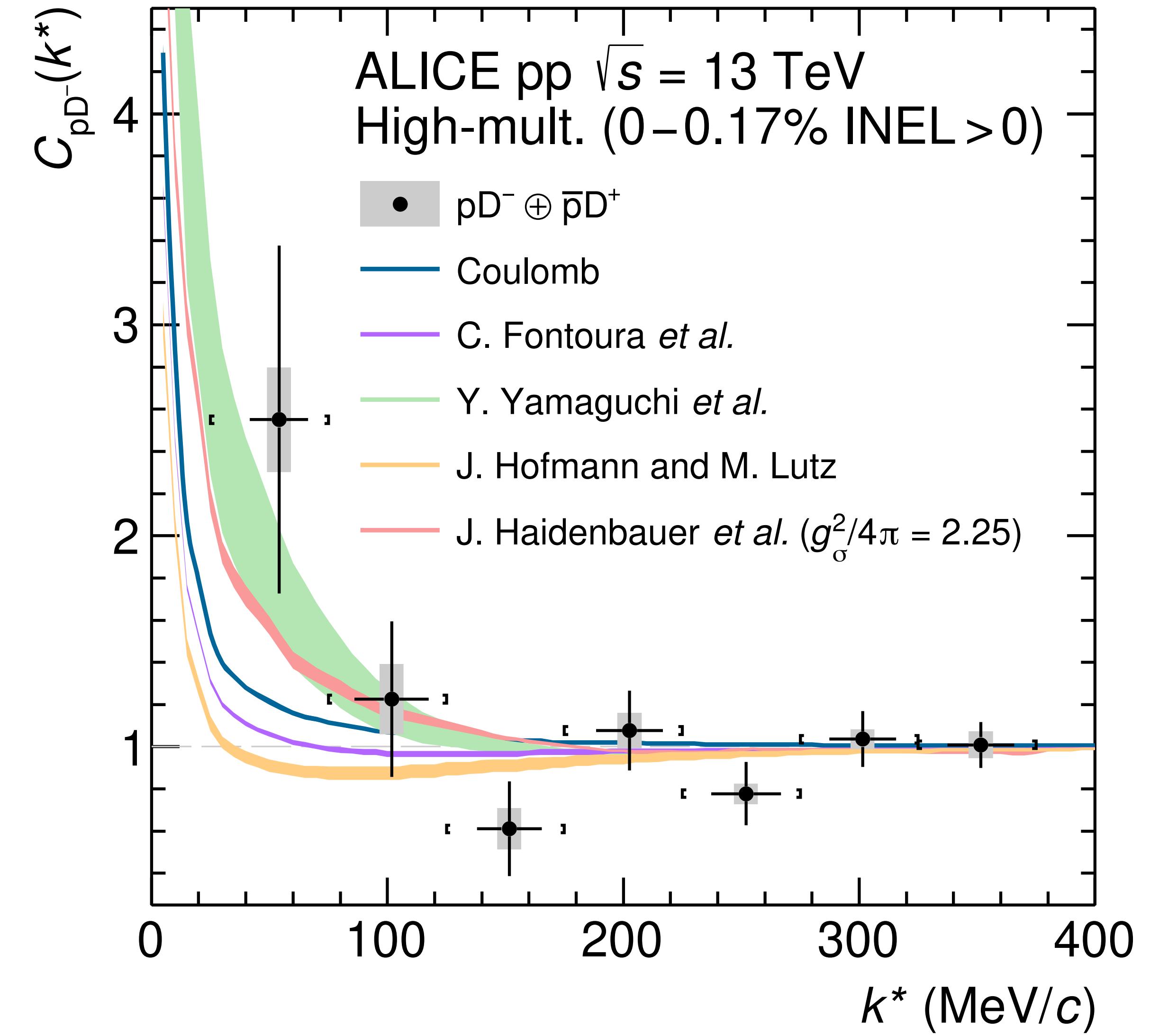
F. Grossa (CERN)  
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- Typical range of nuclear potential around 1-2 fm
  - study of strong interaction among hadrons not possible with larger sources
  - proton–proton and proton–nucleus collisions are the ideal laboratory to study the strong interaction

- pD $^-$ 
  - Typically very small compared to other interactions (light-light  $\sim 7\text{-}8$  fm, light-strange  $\sim 1.5$  fm)
  - Most of the models predict repulsive interaction
  - Possible bound state formation (Yamaguchi et al)
- Data compatible with Coulomb only interaction, but comparison slightly improves when also **attractive strong interaction** is considered



J. Haidenbauer et al, Eur. Phys. J. A33 (2007) 107–117

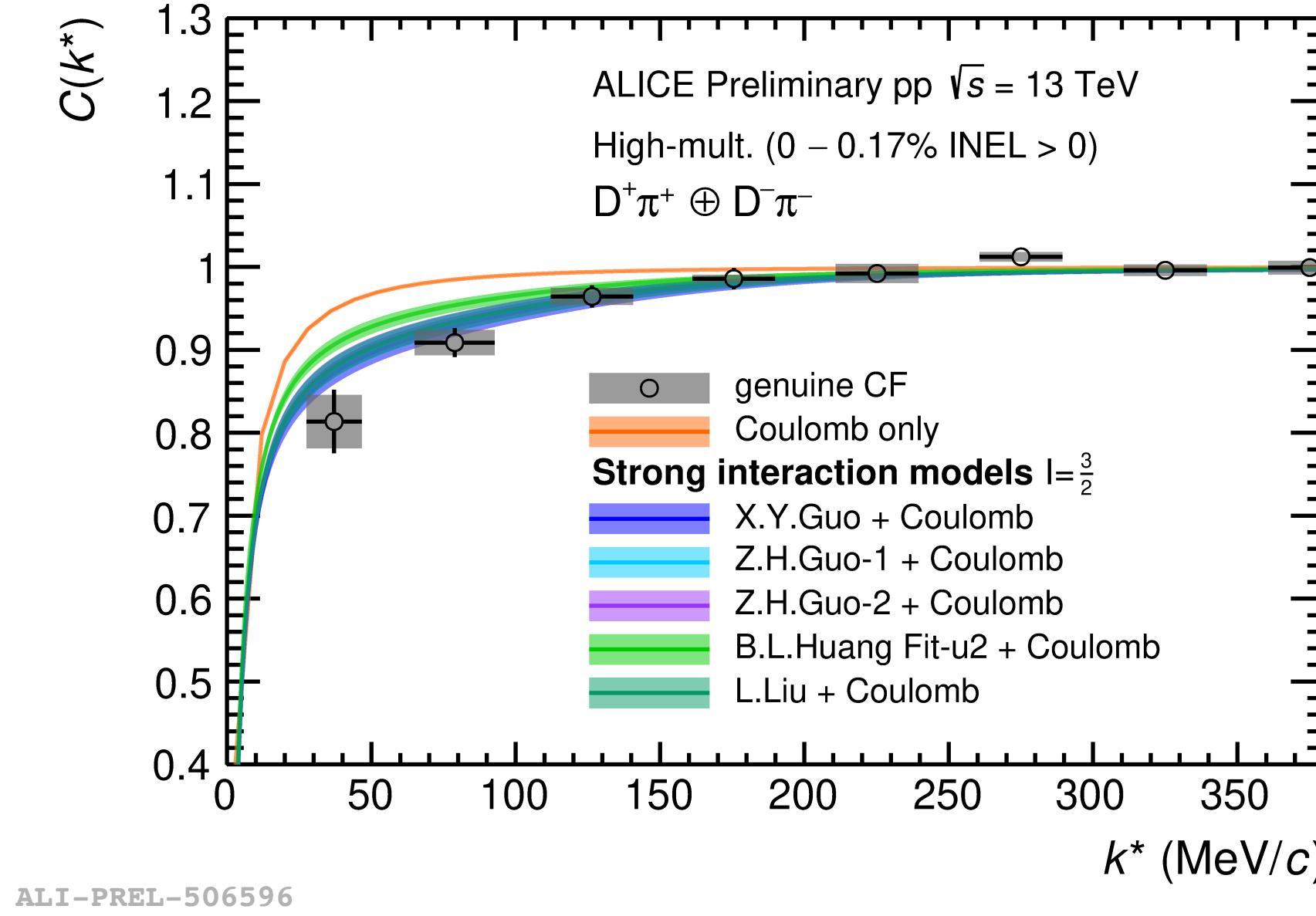
J. Hofmann and M. Lutz, Nucl. Phys. A 763 (2005) 90–139

Fontura et al, Phys. Rev. C 87 (2013) 025206

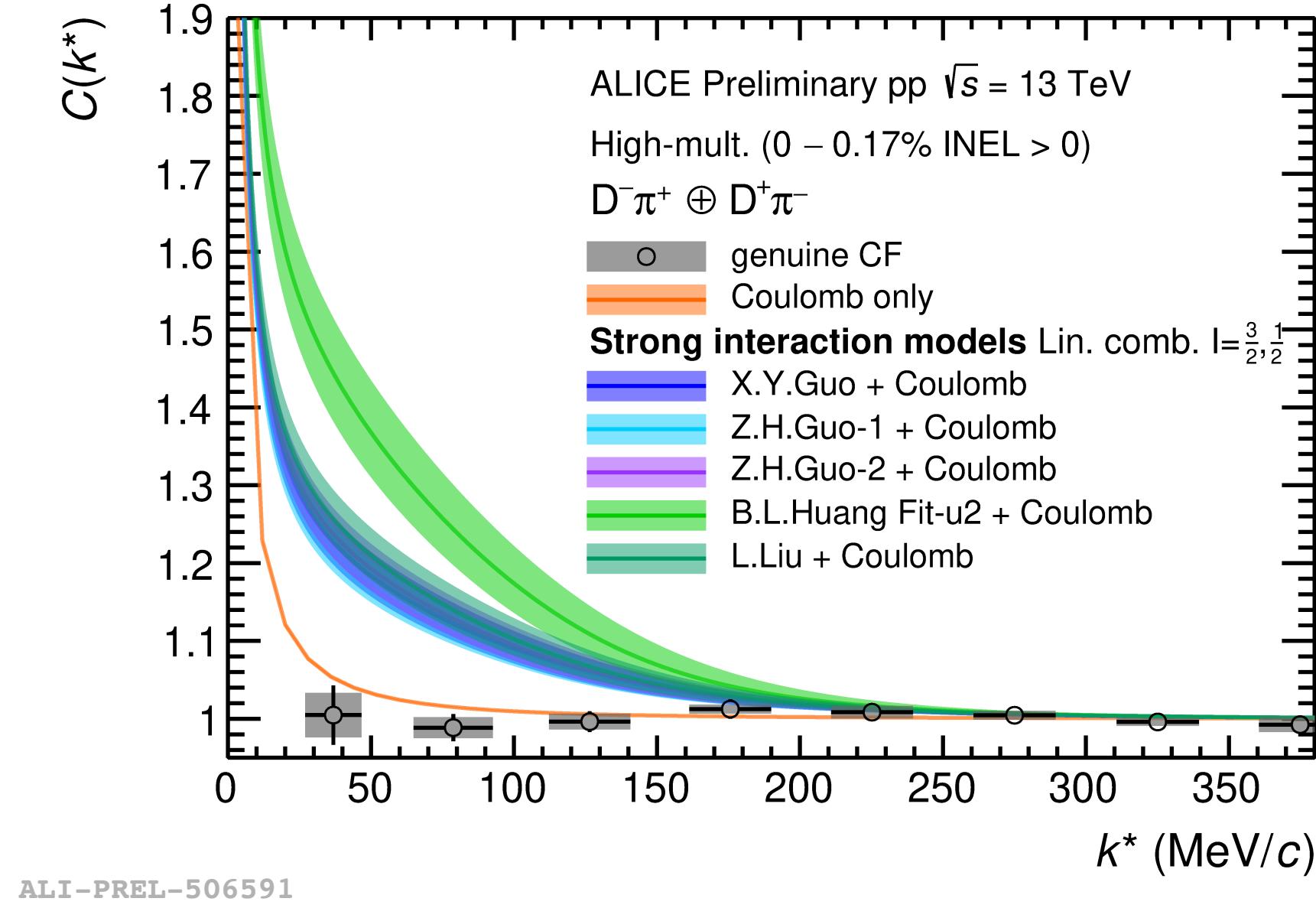
Yamaguchi et al, Phys. Rev. D84 (2011) 014032

ALICE, arXiv: 2201.05352

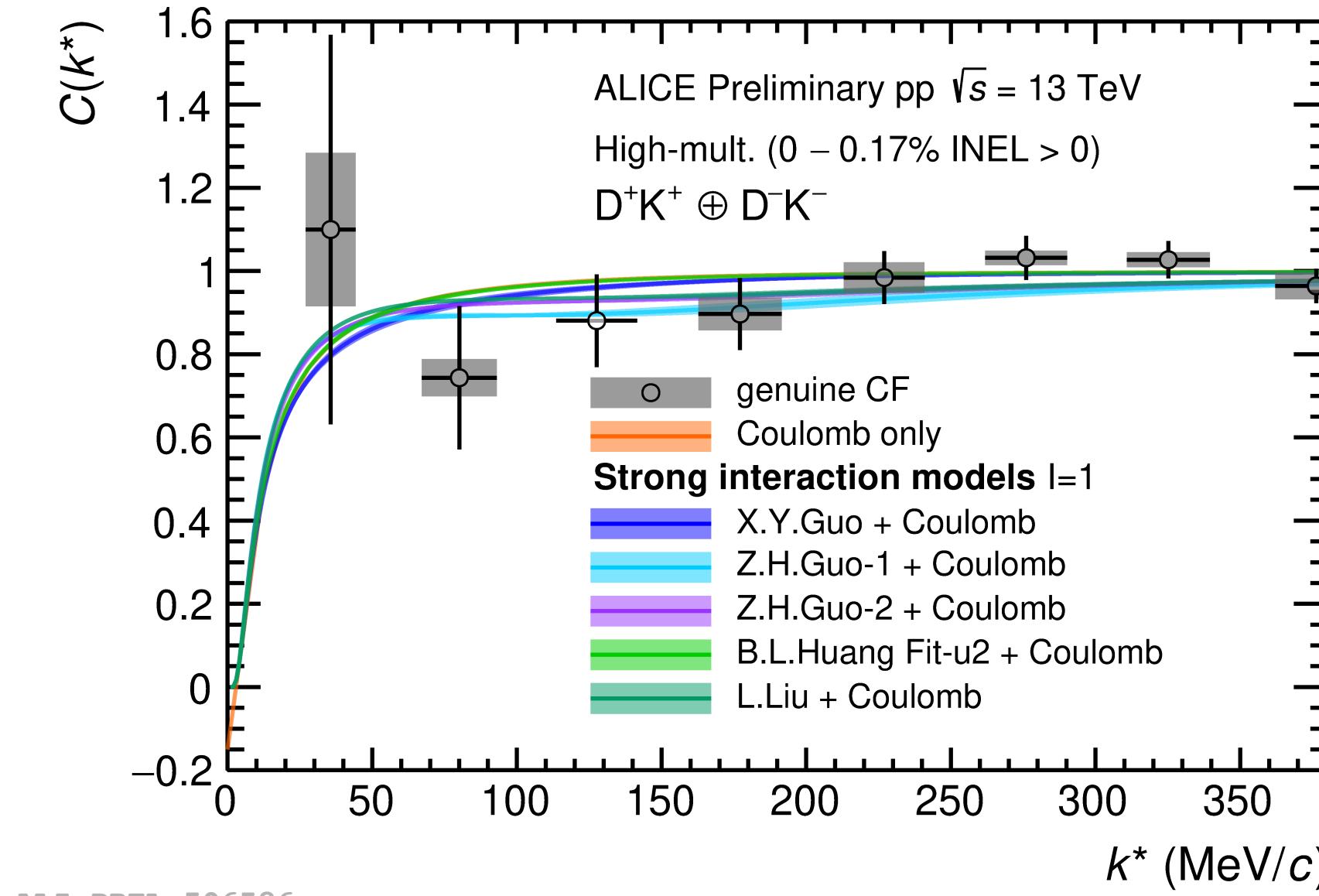
# $\pi D$ and $K D$ interactions



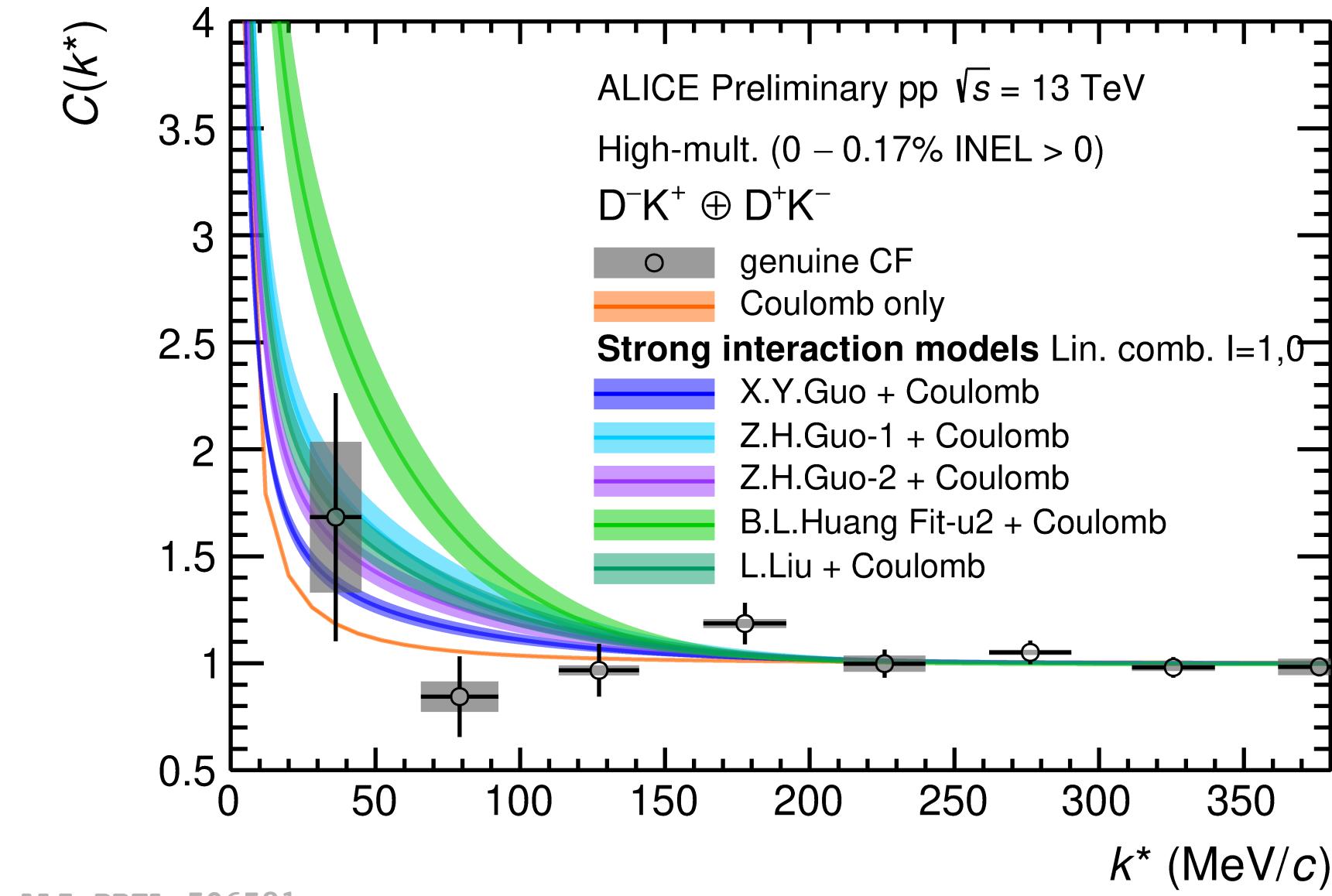
ALI-PREL-506596



ALI-PREL-506591



ALI-PREL-506586



ALI-PREL-506581

- Models agree with data in case of same-charge CF
- Models overestimate data in case of opposite-charge CF

- BOOK L. Liu et al, Phys. Rev. D87 (2013) 014508  
BOOK X.-Y. Guo et al, Phys. Rev. D 98 (2018) 014510  
BOOK B.-L. Huang et al, Phys. Rev. D 105 (2022) 036016  
BOOK Z.-H. Guo et al Eur. Phys. J. C 79 (2019) 13

# Charm-light hadron interaction: hadronic physics

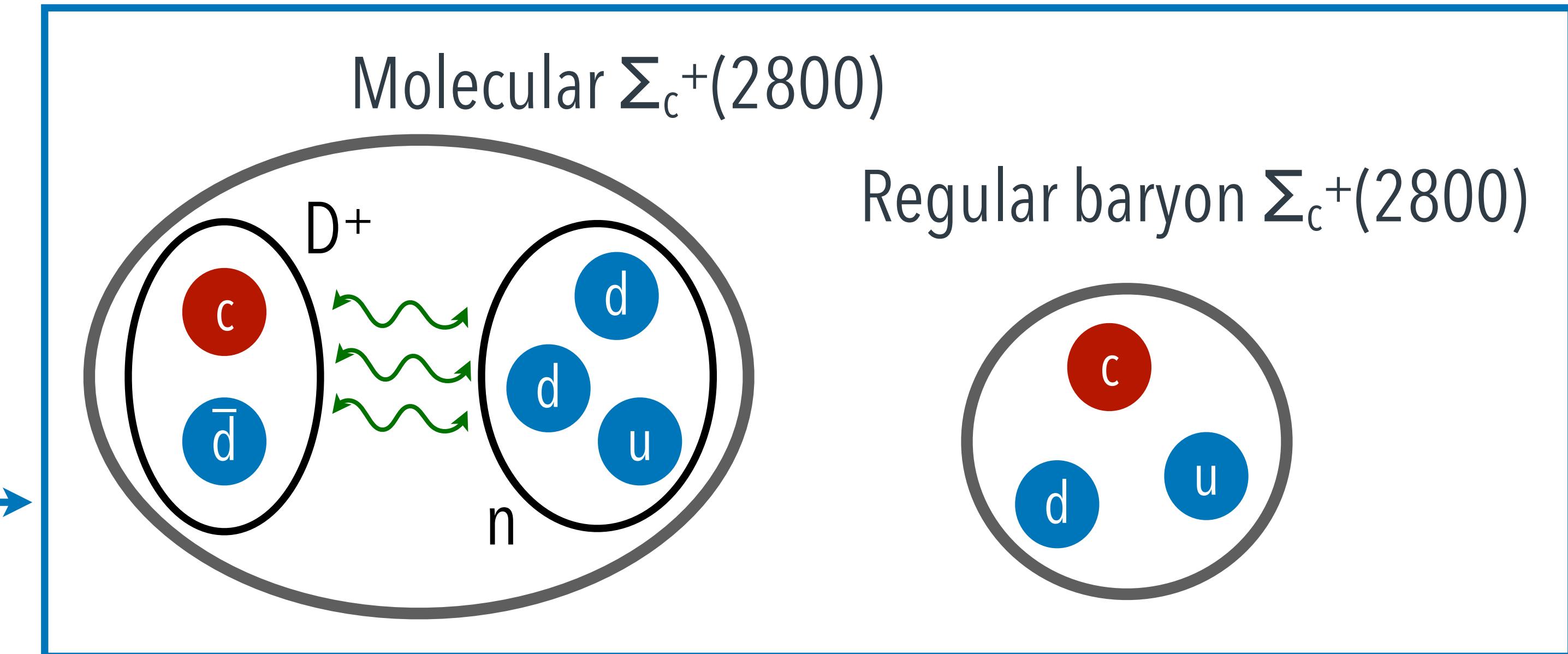
F. Gerosa (CERN)  
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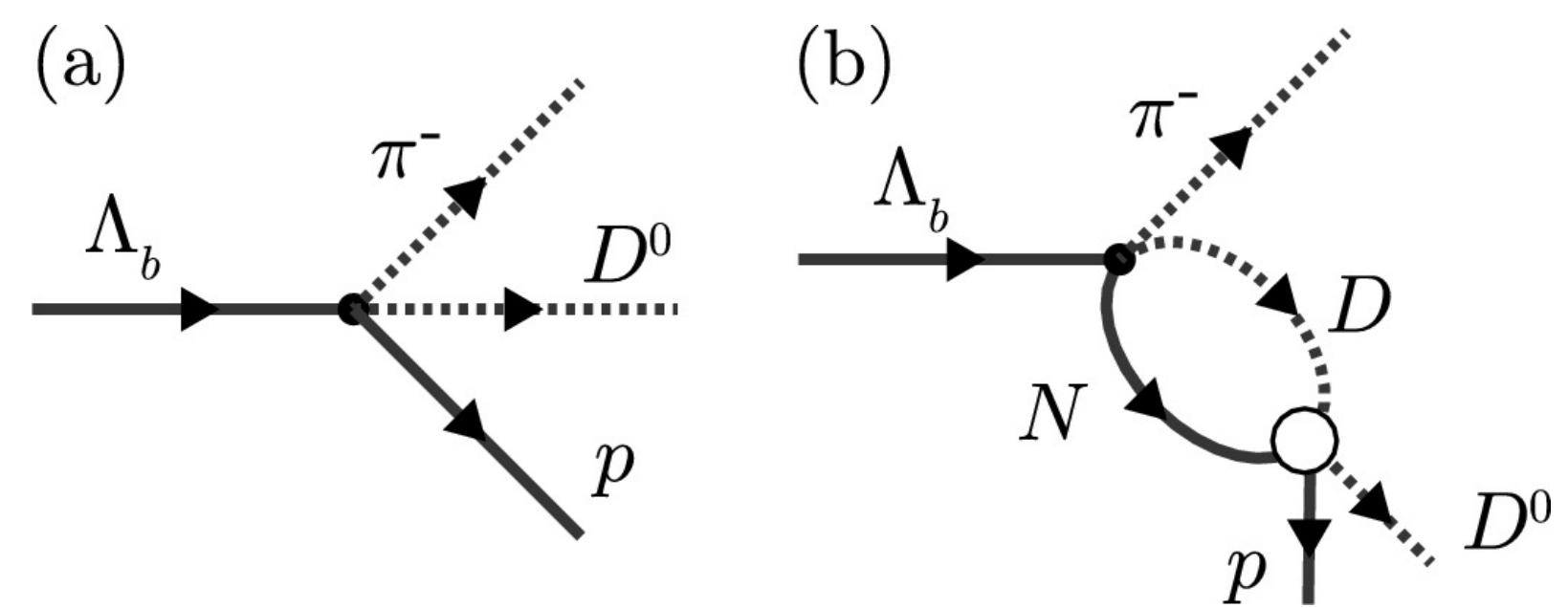
- Charm molecules?

System	$I(J^{P(C)})$	Candidate
np	0 ( $1^+$ )	deuteron
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ND	0 ( $1/2^-$ )	$\Sigma_c(2800)$
$D^*\bar{D}$	0 ( $1^{++}$ )	X(3872)
$D^*D$	0 ( $1^+$ )	$T_{cc}$
$D_1\bar{D}$	0 ( $1^{--}$ )	$\Upsilon(4260)$
$D_1\bar{D}^*$	0 ( $1^{--}$ )	$\Upsilon(4360)$
$\Sigma_c\bar{D}$	1/2 ( $1/2^-$ )	$P_c(4312)$
$\Sigma_c\bar{D}^*$	1/2 ( $1/2^-$ )	$P_c(4457)$
$\Sigma_c\bar{D}^*$	1/2 ( $3/2^-$ )	$P_c(4440)$

Fang-Zheng Peng et al, Phys. Rev. D 105, 034028 (2022)



- Proposed as molecular state in J. Haidenbauer et al, Eur. Phys. J. A 47, 18 (2011) S. Sakai et al, Phys. Lett. B 808 (2020) 135623



- Molecular states also relevant to explain some beauty-hadron decays

# $N\bar{D}$ interaction - scattering lengths in models

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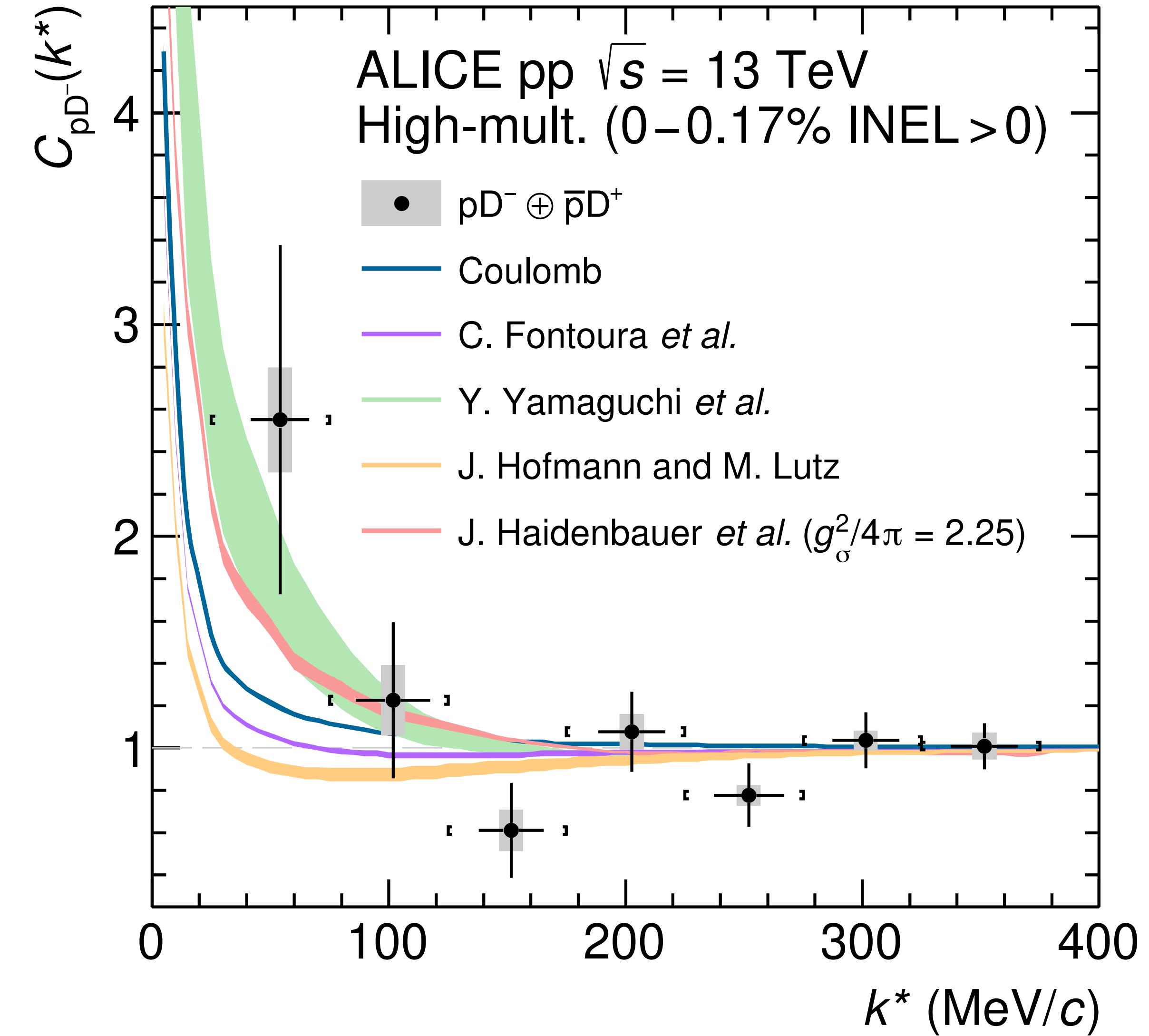
Model	$f_0(l=0)$ [fm]	$f_0(l=1)$ [fm]
Haidenbauer $g_\sigma^2/4\pi = 1$ Meson-exchange model	0,14	-0,28
Haidenbauer $g_\sigma^2/4\pi = 2.25$ Meson-exchange model	0,67	0,04
Hofmann and Lutz SU(4) contact interaction	-0,16	-0,26
Yamaguchi meson-exchange on HQ symmetry	-4,38	-0,07
Fontoura Chiral-quark model	0,16	-0,25

J. Haidenbauer et al, Eur. Phys. J. A33 (2007) 107–117

J. Hofmann and M. Lutz, Nucl. Phys. A 763 (2005) 90–139

Fontura et al, Phys. Rev. C 87 (2013) 025206

Yamaguchi et al, Phys. Rev. D84 (2011) 014032



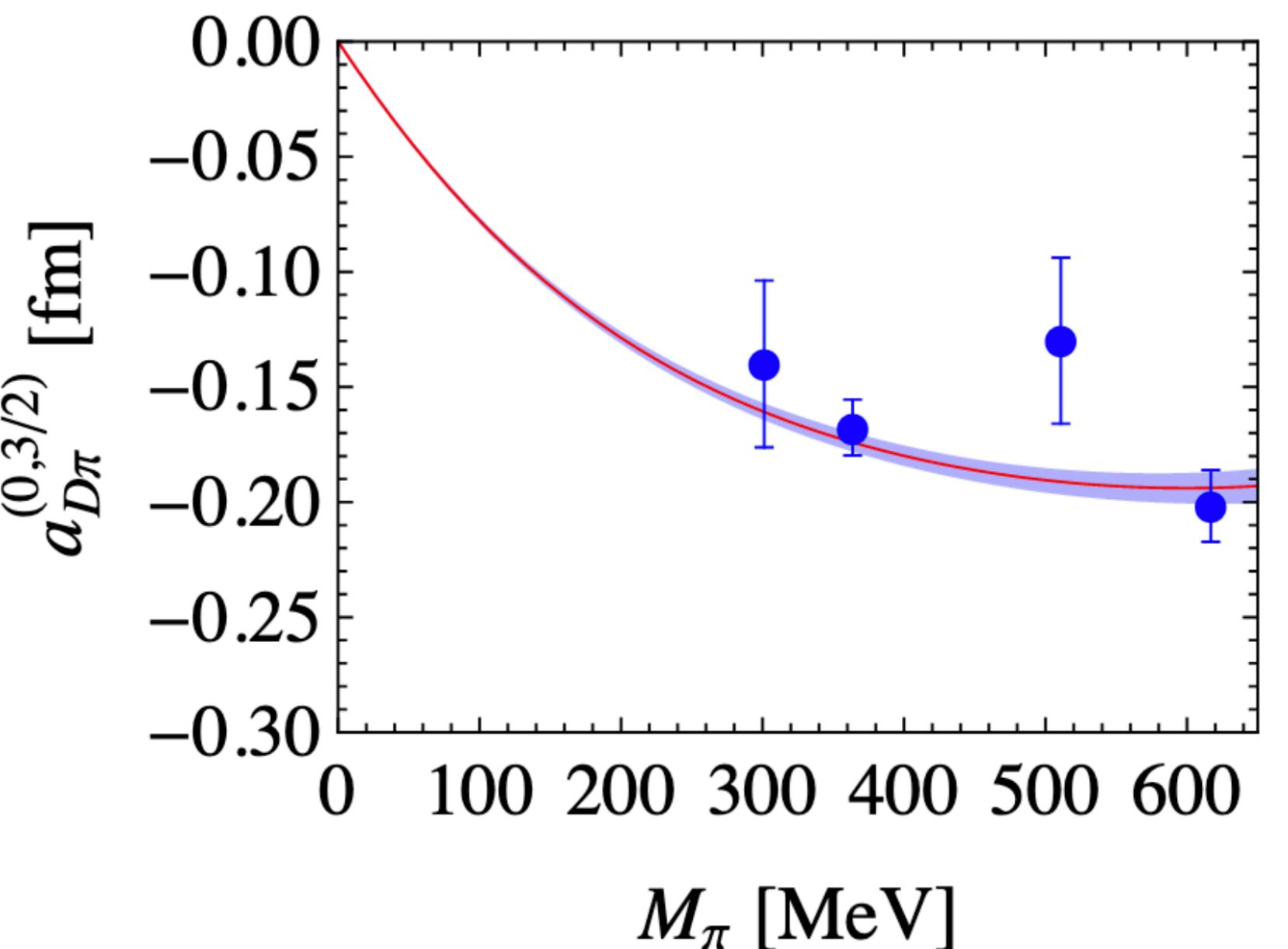
ALICE-PUB-502166

ALICE, arXiv: 2201.05352

# $\pi D$ and $K D$ interactions - scattering lengths in models

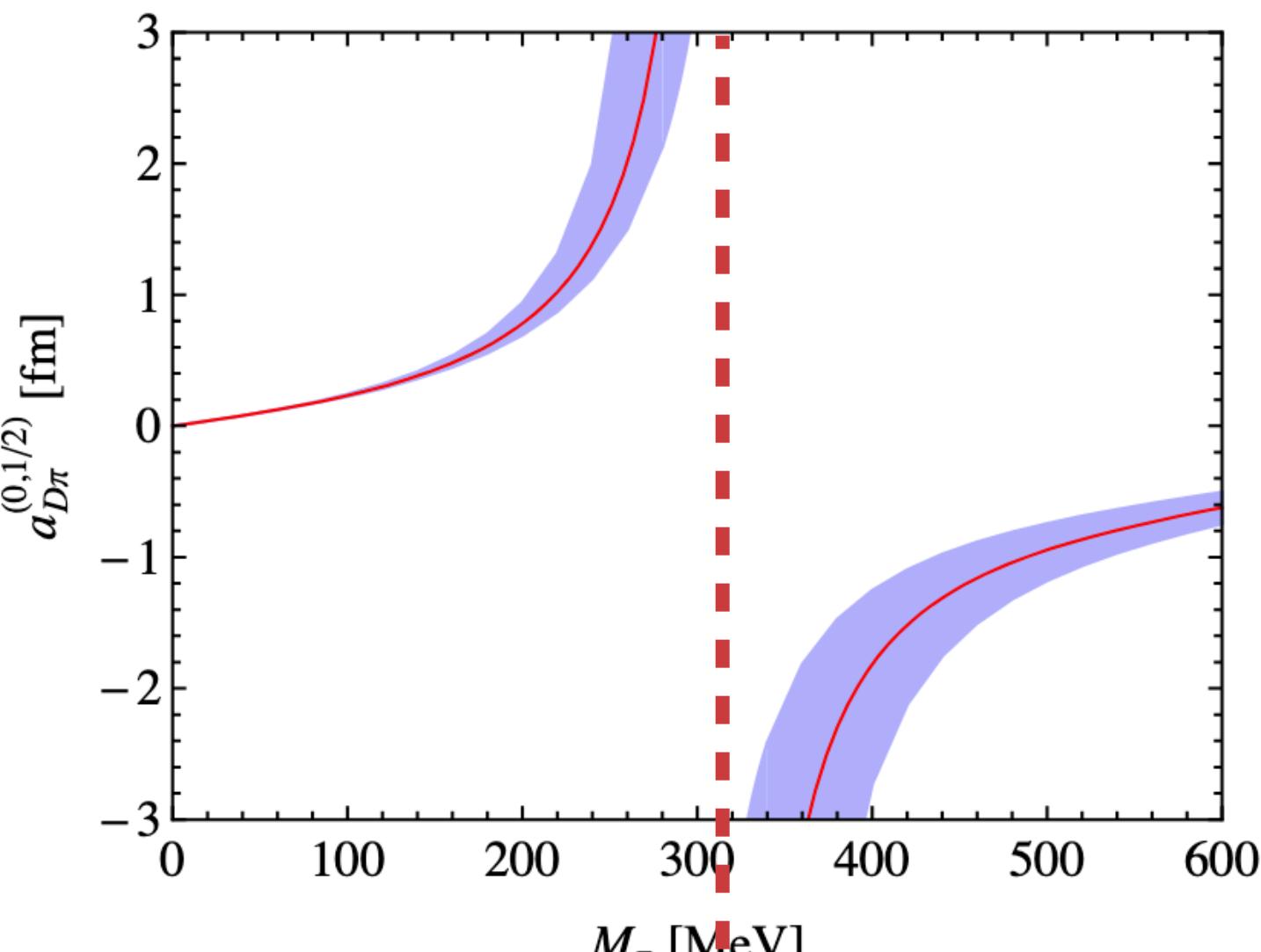
Channel	L. Liu	X.-Y. Guo	Z.-H. Guo-1	Z.-H. Guo-2	B.-L. Huang
$D\pi(l=3/2) [\text{fm}]$	-0,10	-0,11	-0,101	-0,099	-0,06
$D\pi(l=1/2) [\text{fm}]$	0,37	0,33	0,31	0,34	0,61
$DK(l=1) [\text{fm}]$	$0,07+i0,17$	-0,05	$0,06+i0,30$	$0,05+i0,17$	-0,01
$D\bar{K}(l=0) [\text{fm}]$	0,84	0,46	0,96	0,68	1,81
$D\bar{K}(l=1) [\text{fm}]$	-0,20	-0,22	-0,18	-0,19	-0,24

- Predictions of scattering lengths derived from lattice QCD calculations
  - Typically very small compared to other interactions (light-light  $\sim 7\text{-}8 \text{ fm}$ , light-strange  $\sim 1.5 \text{ fm}$ )
  - No constraints from data
  - For pions  $l=3/2$  channel more constrained than  $l=1/2$  channel



- L. Liu et al, Phys. Rev. D87 (2013) 014508
- X.-Y. Guo et al, Phys. Rev. D 98 (2018) 014510
- B.-L. Huang et al, Phys. Rev. D 105 (2022) 036016
- Z.-H. Guo et al Eur. Phys. J. C 79 (2019) 13

● X.-Y. Guo et al, Phys. Rev. D 98 (2018) 014510



Bound-state pole formation

$$C'(k^*) = A_C(k^*) \left\{ 2 \left[ \frac{1}{4} \left( \frac{|f_C(k^*)|}{r} \right)^2 \left[ 1 - \frac{d_0}{2\sqrt{\pi r}} + \frac{1}{2}(A_C(k^*) - 1)^2(1 - e^{-4(rk^*)^2}) \right] + \right. \right.$$

$$+ \mathcal{R}(f_C(k^*)) \frac{F_1(2k^*r)}{\sqrt{\pi r}} +$$

$$\left. \left. + \mathcal{J}(f_C(k^*)) \left[ \frac{F_2(2k^*r)}{2r} + (A_C(k^*) - 1)k^* \cos(rk^*)e^{-(rk^*)^2} \right] \right] + 1 \right\}$$

Where

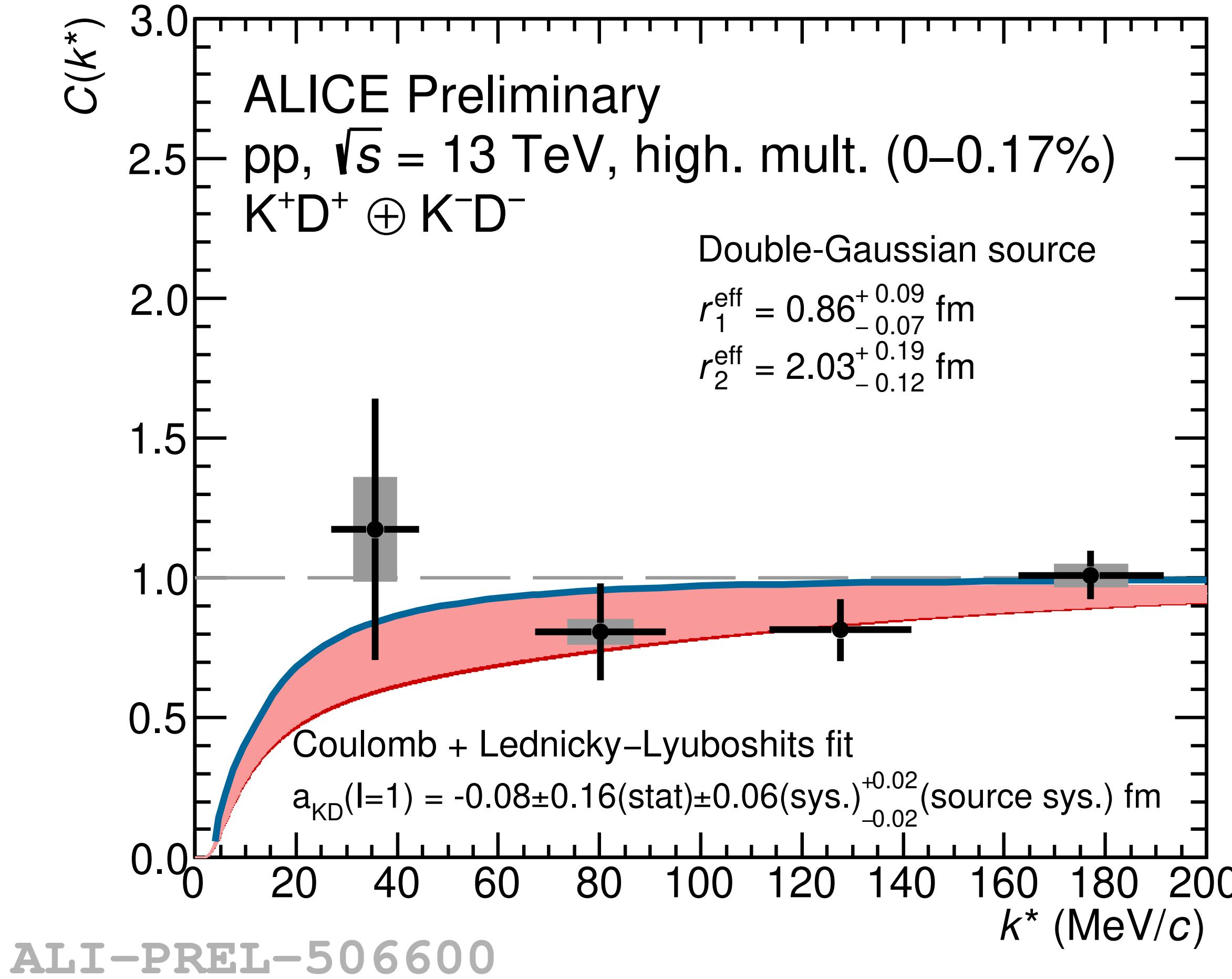
$$f_C(k^*) = \left[ \frac{1}{a_0} + \frac{1}{2}d_0 k^{*2} - \frac{2}{a_C} h(k^* a_C) - ik^* A_C(k^*) \right]^{-1}$$



# KD interaction: fit with Lednický-Lyuboshits formula

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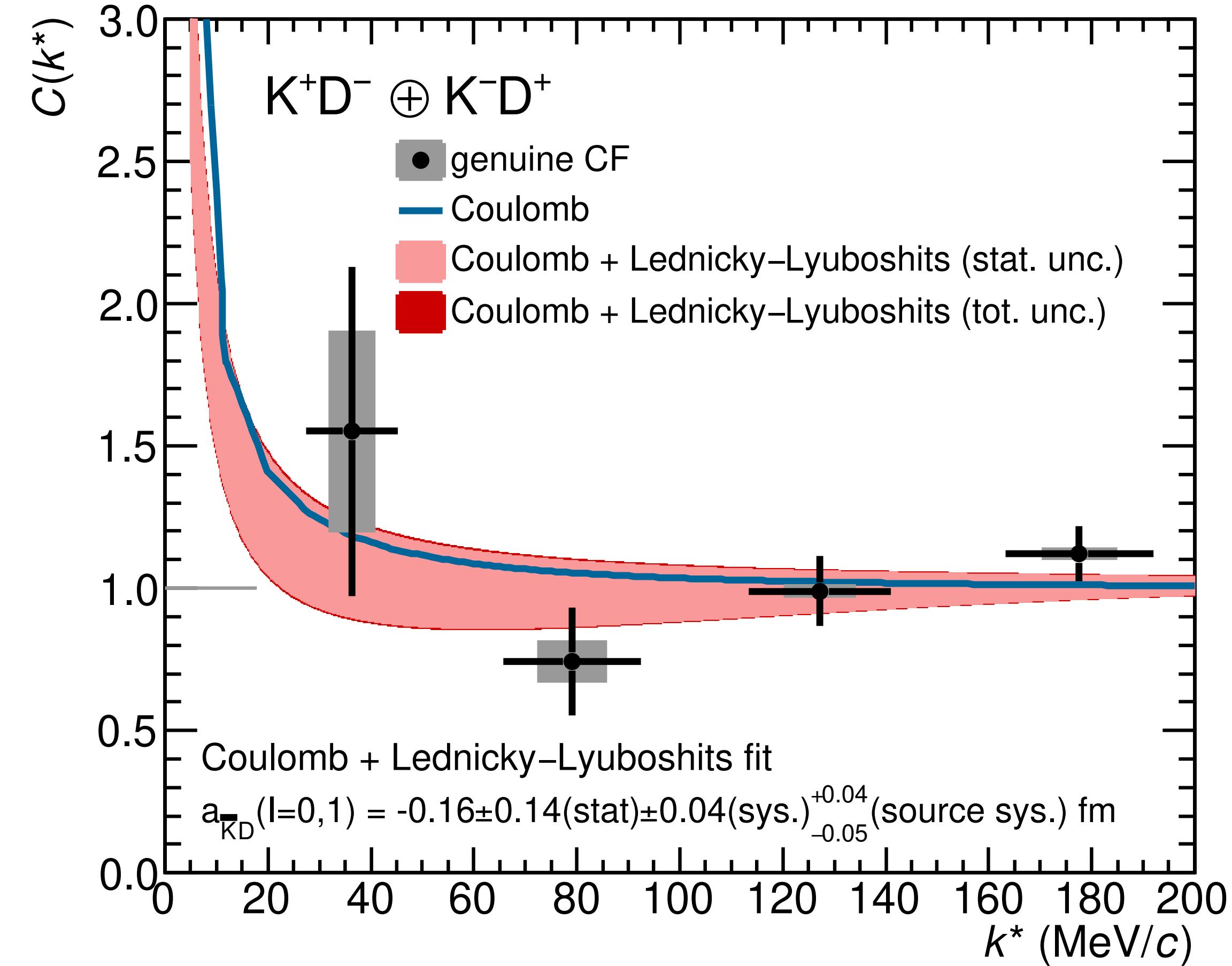


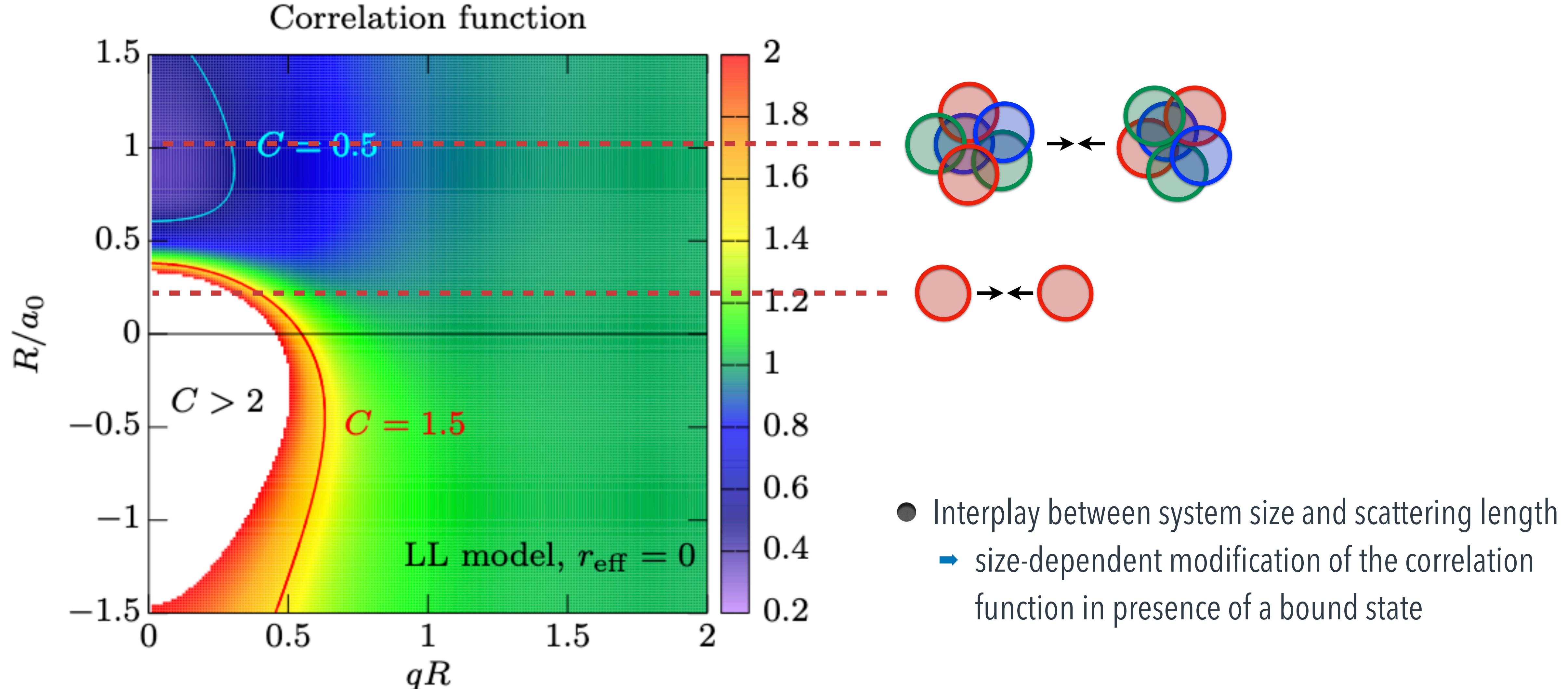
●  $K^+D^+$

→  $|l|=1$  channel only

●  $K^-D^-$

→  $|l|=0$  (50%)  
→  $|l|=1$  (50%)

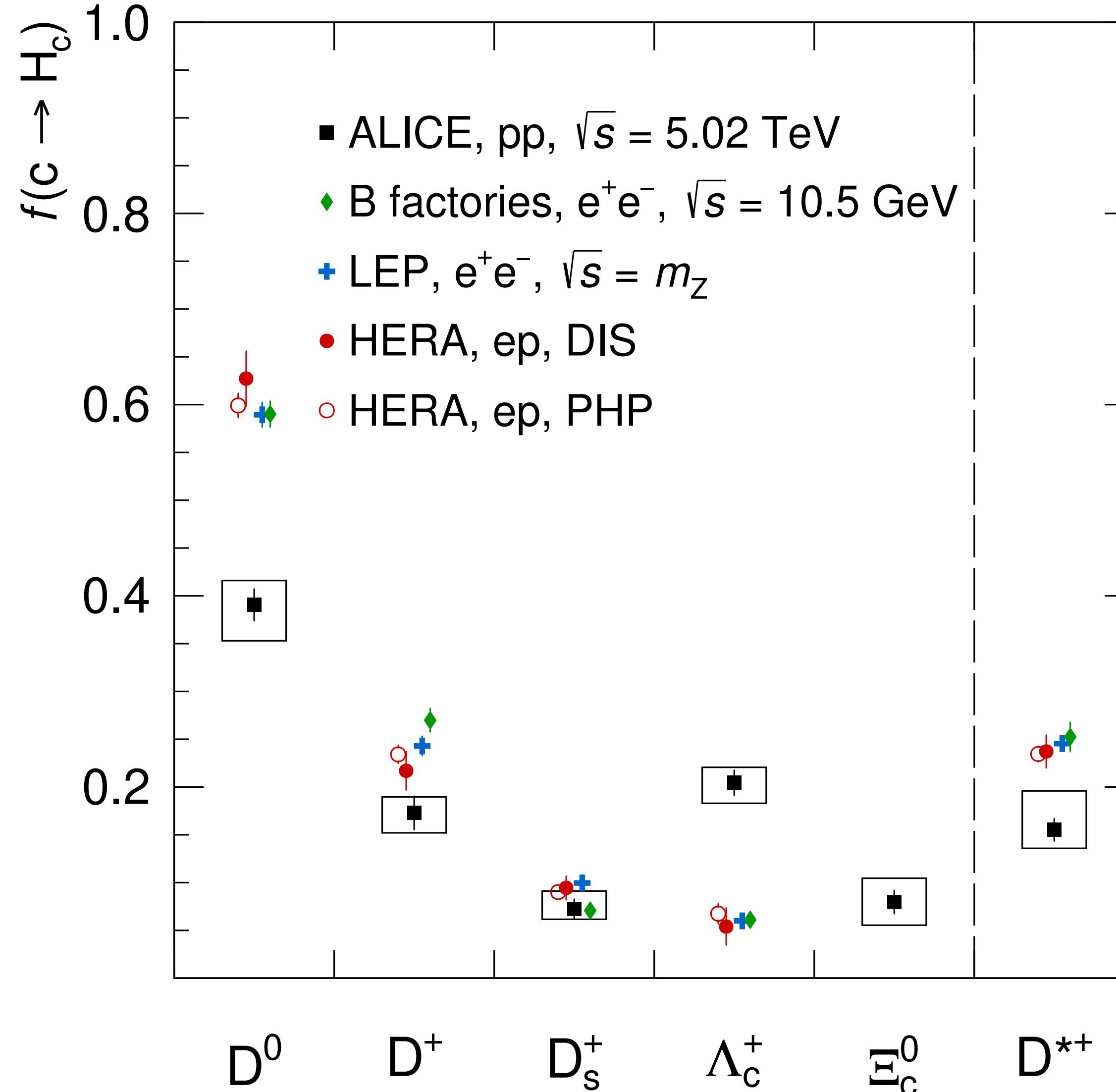




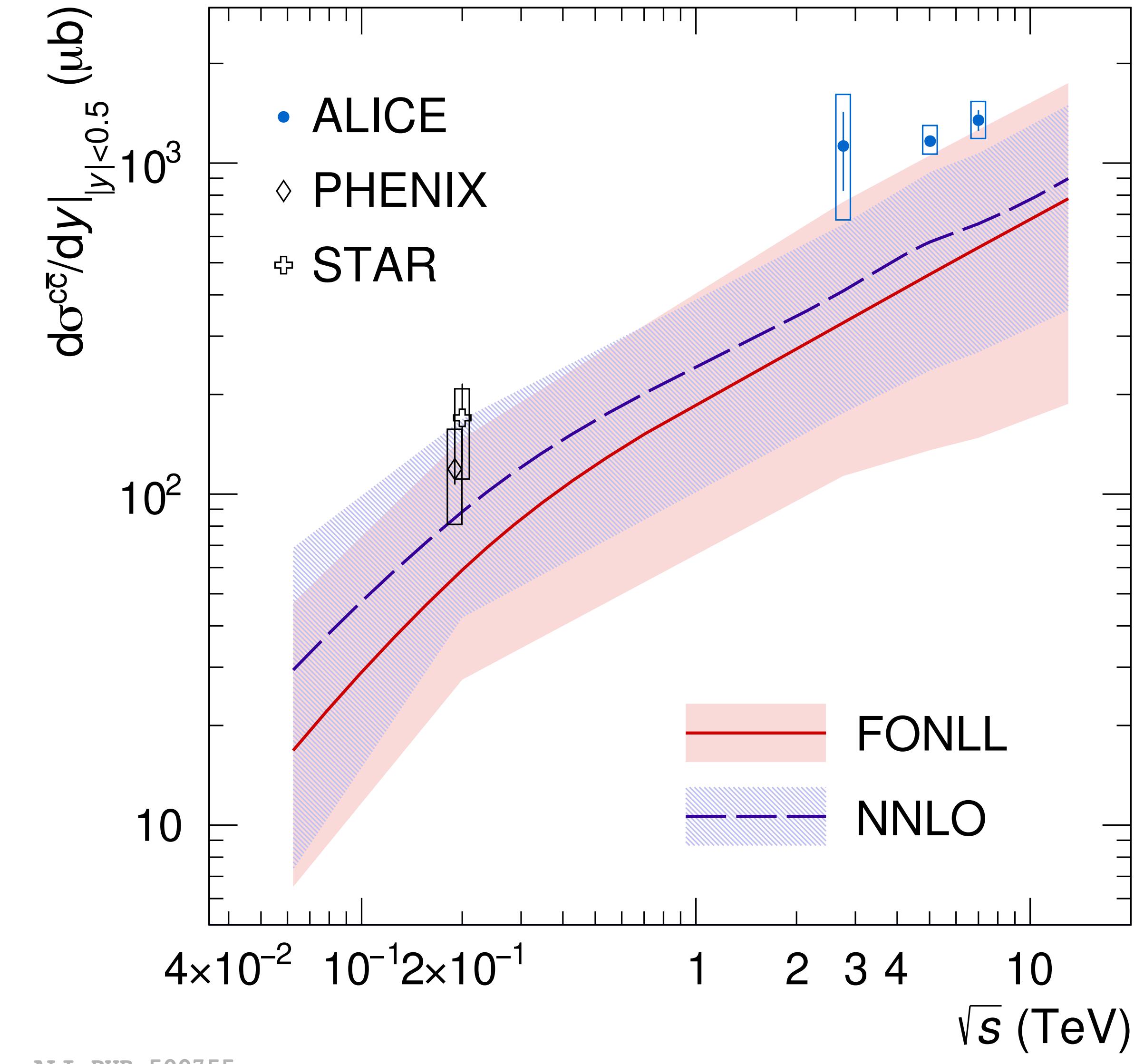
# Charm quark production cross section and fragmentation fractions

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ALI-PUB-500755