

# Heavy Quarks & Leptons 2014

Dalitz plot analysis of charmless b-hadron decays

---

Jeremy Dalseno

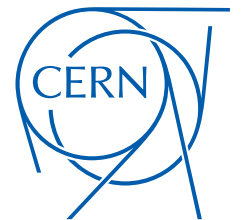
on behalf of the LHCb collaboration

J.Dalseno [at] bristol.ac.uk

26 August 2014



University of  
BRISTOL



# Outline

1. Motivation

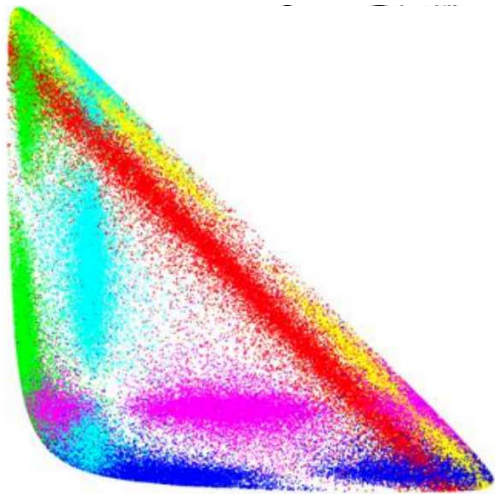
2. LHCb Detector

3.  $B^\pm \rightarrow K^\pm K^+ K^-$  and  $B^\pm \rightarrow K^\pm \pi^+ \pi^-$  (penguin dominated)

4.  $B^\pm \rightarrow \pi^\pm K^+ K^-$  and  $B^\pm \rightarrow \pi^\pm \pi^+ \pi^-$  (tree dominated)

5.  $B^\pm \rightarrow K^\pm p \bar{p}$  and  $B^\pm \rightarrow \pi^\pm p \bar{p}$

6. Summary



Toy MC Dalitz plot (DP)

Dalitz plot contains all kinematic and dynamic information of decay

Amplitude analysis one of the most powerful techniques

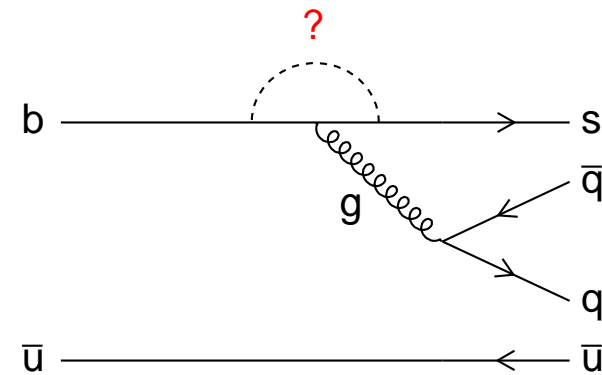
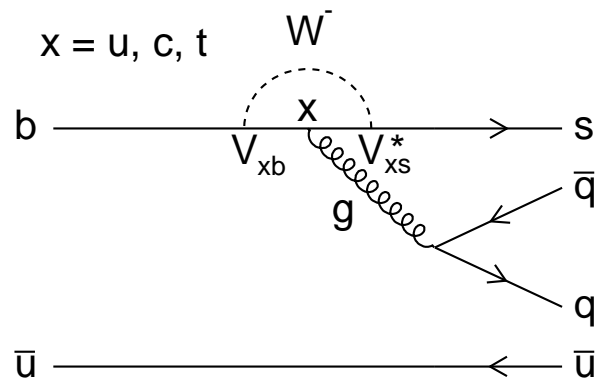
Extract amplitude-level information rather than amplitude-squared information

Interference between intermediate states allows measurement of relative magnitudes and phases

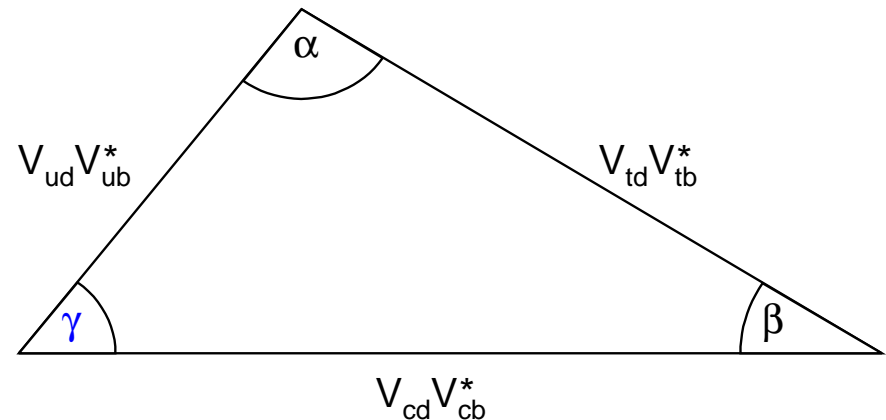
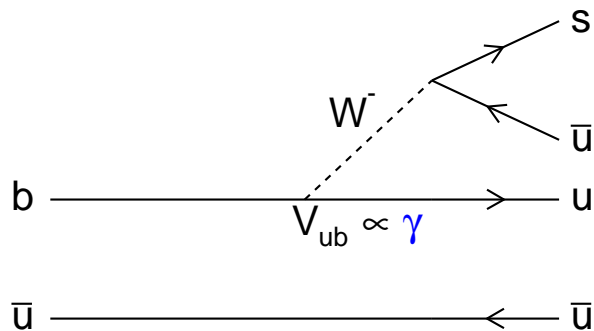
# Motivation

Charmless  $B \rightarrow 3h$  decay channels provide a rich environment for physics observables

Unknown heavy particle in the loop could carry a new  $CP$  violating phase



Tree sensitive to  $\gamma = \phi_3 \equiv -\arg\left(\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}\right)$



# Motivation

In charged  $B$  decays, presence of multiple amplitudes may lead to direct  $CP$  violation

$$A(B \rightarrow f) = \sum_i |A_i| e^{i(\delta_i + \phi_i)}$$

$$\bar{A}(\bar{B} \rightarrow \bar{f}) = \sum_i |\bar{A}_i| e^{i(\delta_i - \phi_i)}$$

Strong phase ( $\delta$ ) invariant under  $CP$ , while weak phase ( $\phi$ ) changes sign under  $CP$

$$\mathcal{A}_{CP}(B \rightarrow f) \equiv \frac{|\bar{A}|^2 - |A|^2}{|\bar{A}|^2 + |A|^2} \propto \sum_{i,j} \sin(\delta_i - \delta_j) \sin(\phi_i - \phi_j)$$

3 conditions required for direct  $CP$  violation

At least 2 amplitudes

Non-zero strong phase difference,  $\delta_i - \delta_j \neq 0$

Non-zero weak phase difference,  $\phi_i - \phi_j \neq 0$

Source of weak phase differences come from different CKM phases of each amplitude

# Motivation

Direct  $CP$  violation more complicated in  $B \rightarrow 3h$  decay channels compared to 2-body decays

There are at least 4 possible sources of strong phase

## 1. Short-distance contributions (quark level)

BSS mechanism, PRL **43** 242 (1979)

Penguin diagram (b) contains 3 quark generations in loop

If gluon in penguin is timelike (on-shell)

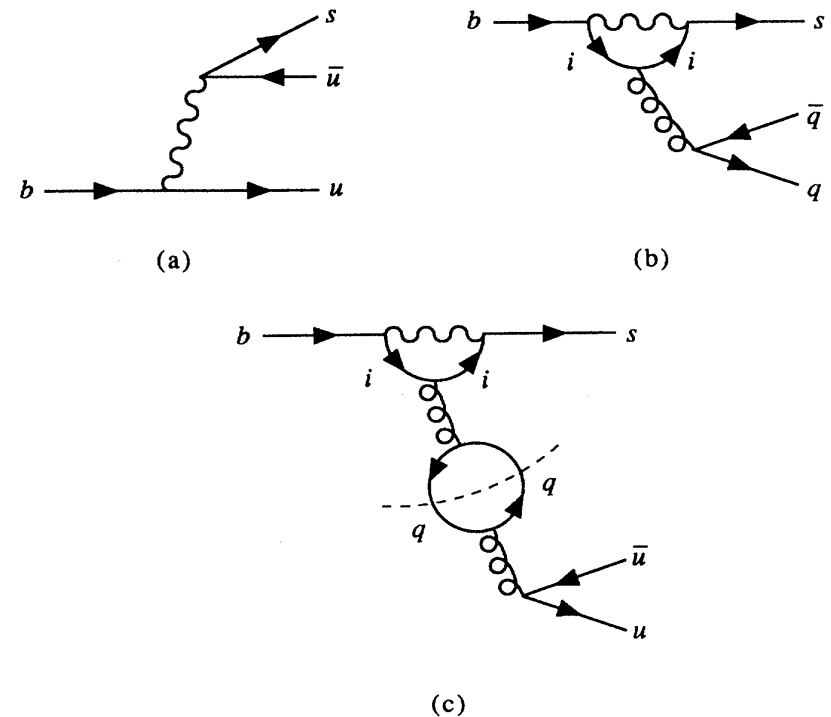
Momentum transfer  $q^2 > 4m_i^2$  where  $i = u, c$

Particle rescattering (c) generates a phase difference

Tree contribution (a) carries different strong phase

$CP$  violation in 2-body processes caused by this effect

eg.  $B^0 \rightarrow K^+ \pi^-$



# Motivation

Remaining sources unique to multibody decays

Long-distance contributions ( $q\bar{q}$  level)

## 2. Breit-Wigner phase

Represents intermediate resonance states

$$F_R^{\text{BW}}(s) = \frac{1}{m_R^2 - s - im_R\Gamma_R(s)}$$

Phase varies across the Dalitz plot

## 3. Relative $CP$ -even phase in the isobar model

$$A(B \rightarrow f) = \sum_i |A_i| e^{i(\delta_i + \phi_i)}$$

$$\bar{A}(\bar{B} \rightarrow \bar{f}) = \sum_i |\bar{A}_i| e^{i(\delta_i - \phi_i)}$$

Related to final state interactions between different resonances

# Motivation

Each source of strong phase leaves a unique signature in the Dalitz plot

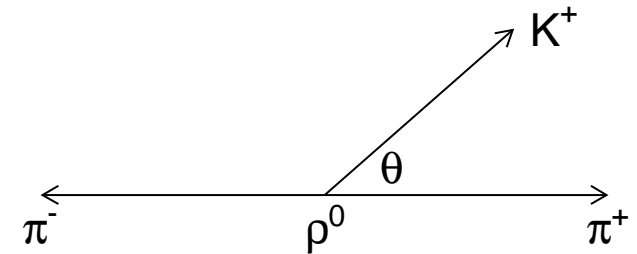
Illustrate with series of examples

Consider  $B^\pm \rightarrow K^\pm \pi^+ \pi^-$  with only 2 isobars

$B^\pm \rightarrow K^\pm \rho^0$  and non-resonant (NR) component

$\rho$  lineshape a Breit-Wigner,  $F_\rho^{\text{BW}}$

$\rho^0$  is a vector resonance, so angular distribution follows  $\cos \theta$



$$A_+ = a_+^\rho e^{i\delta_+^\rho} F_\rho^{\text{BW}} \cos \theta + a_+^{\text{NR}} e^{i\delta_+^{\text{NR}}} F^{\text{NR}}$$

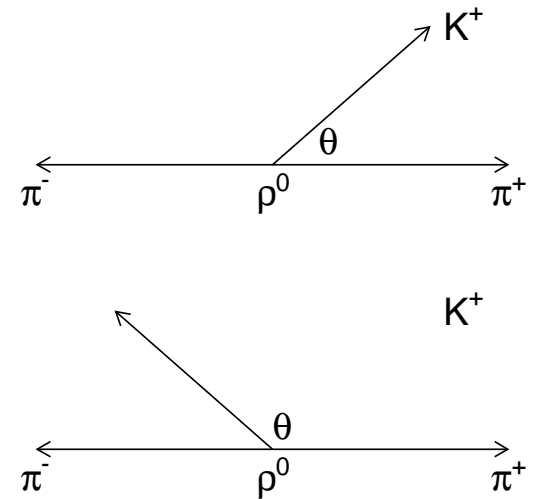
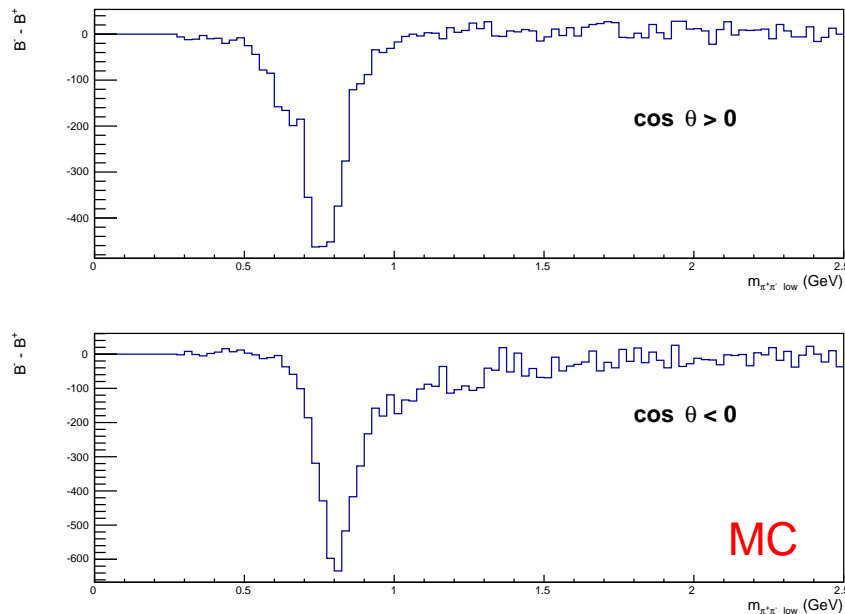
$$A_- = a_-^\rho e^{i\delta_-^\rho} F_\rho^{\text{BW}} \cos \theta + a_-^{\text{NR}} e^{i\delta_-^{\text{NR}}} F^{\text{NR}}$$

$$\begin{aligned} \mathcal{A}_{CP} &\propto |A_-|^2 - |A_+|^2 \\ &\propto [(a_-^\rho)^2 - (a_+^\rho)^2] |F_\rho^{\text{BW}}|^2 \cos^2 \theta + \dots \\ &\quad - 2(m_\rho^2 - s) |F_\rho^{\text{BW}}|^2 |F^{\text{NR}}|^2 \cos \theta \dots \\ &\quad + 2m_\rho \Gamma_\rho |F_\rho^{\text{BW}}|^2 |F^{\text{NR}}|^2 \cos \theta \dots \end{aligned}$$

# Motivation

$$\begin{aligned} \mathcal{A}_{CP} \propto & [(a_-^\rho)^2 - (a_+^\rho)^2] |F_\rho^{\text{BW}}|^2 \cos^2 \theta + \dots \\ & - 2(m_\rho^2 - s) |F_\rho^{\text{BW}}|^2 |F^{\text{NR}}|^2 \cos \theta \dots \\ & + 2m_\rho \Gamma_\rho |F_\rho^{\text{BW}}|^2 |F^{\text{NR}}|^2 \cos \theta \dots \end{aligned}$$

Only depends on  $\rho$  resonance, maximum difference at  $\rho$  pole, quadratic in helicity



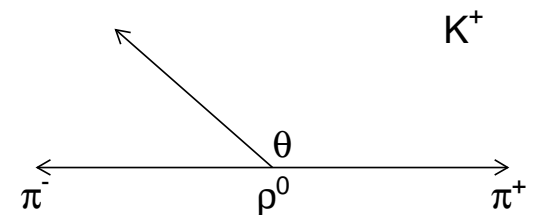
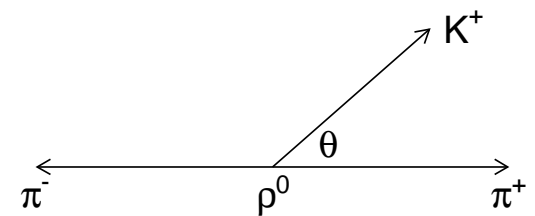
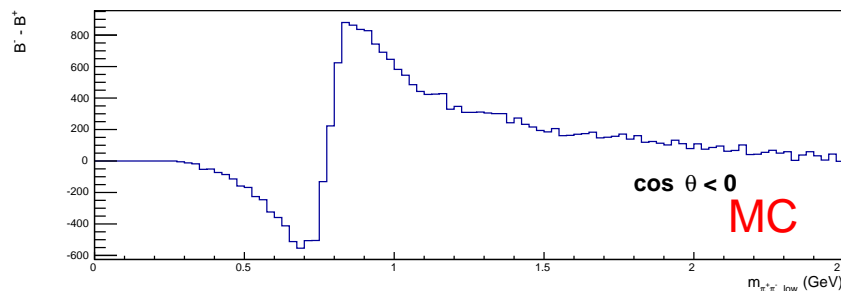
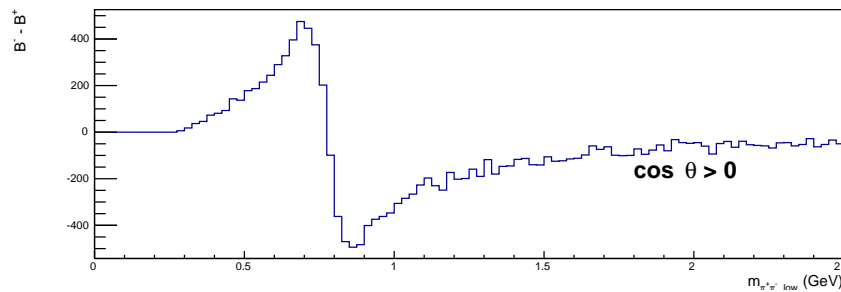
Only short-distance effects can create  $a_+^\rho \neq a_-^\rho$



# Motivation

$$\begin{aligned} \mathcal{A}_{CP} \propto & [(a_-^\rho)^2 - (a_+^\rho)^2] |F_\rho^{\text{BW}}|^2 \cos^2 \theta + \dots \\ & - 2(m_\rho^2 - s) |F_\rho^{\text{BW}}|^2 |F^{\text{NR}}|^2 \cos \theta \dots \\ & + 2m_\rho \Gamma_\rho |F_\rho^{\text{BW}}|^2 |F^{\text{NR}}|^2 \cos \theta \dots \end{aligned}$$

Interference term from real part of Breit-Wigner, zero at  $\rho$  pole, linear in helicity

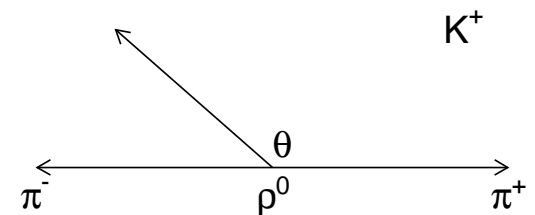
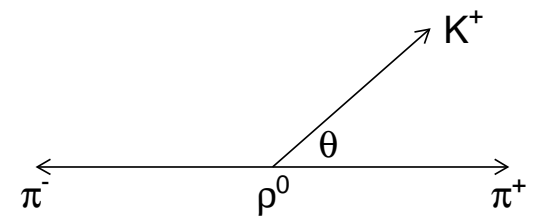
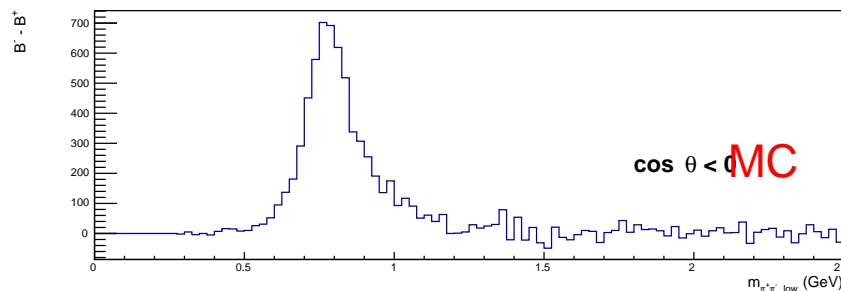
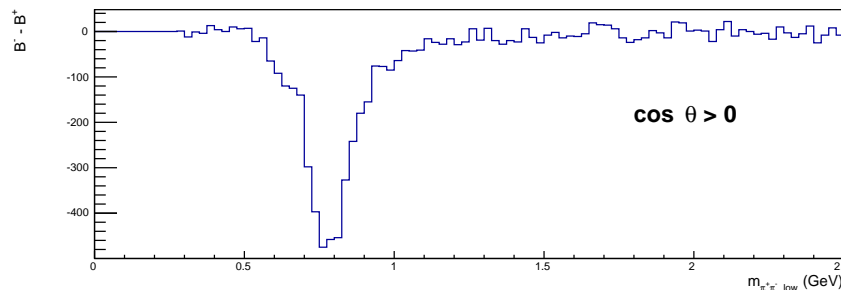


Caused by long distance effects from final state interactions

# Motivation

$$\begin{aligned} \mathcal{A}_{CP} \propto & [(a_-^\rho)^2 - (a_+^\rho)^2] |F_\rho^{\text{BW}}|^2 \cos^2 \theta + \dots \\ & - 2(m_\rho^2 - s) |F_\rho^{\text{BW}}|^2 |F^{\text{NR}}|^2 \cos \theta \dots \\ & + 2m_\rho \Gamma_\rho |F_\rho^{\text{BW}}|^2 |F^{\text{NR}}|^2 \cos \theta \dots \end{aligned}$$

Interference term from imaginary part of Breit-Wigner, maximum at  $\rho$  pole, linear in helicity



Caused by long distance effects from Breit-Wigner phase and final state interactions

# Motivation

Last source of strong phase

## 4. Final state $KK \leftrightarrow \pi\pi$ rescattering

Can occur between decay channels with the same flavour quantum numbers

$$\text{eg. } B^\pm \rightarrow K^\pm K^+ K^- \text{ and } B^\pm \rightarrow K^\pm \pi^+ \pi^-$$

$CPT$  conservation constrains hadron rescattering

For given quantum numbers, sum of partial widths equal for charge-conjugate decays

$KK \leftrightarrow \pi\pi$  rescattering generates a strong phase

Look into rescattering region

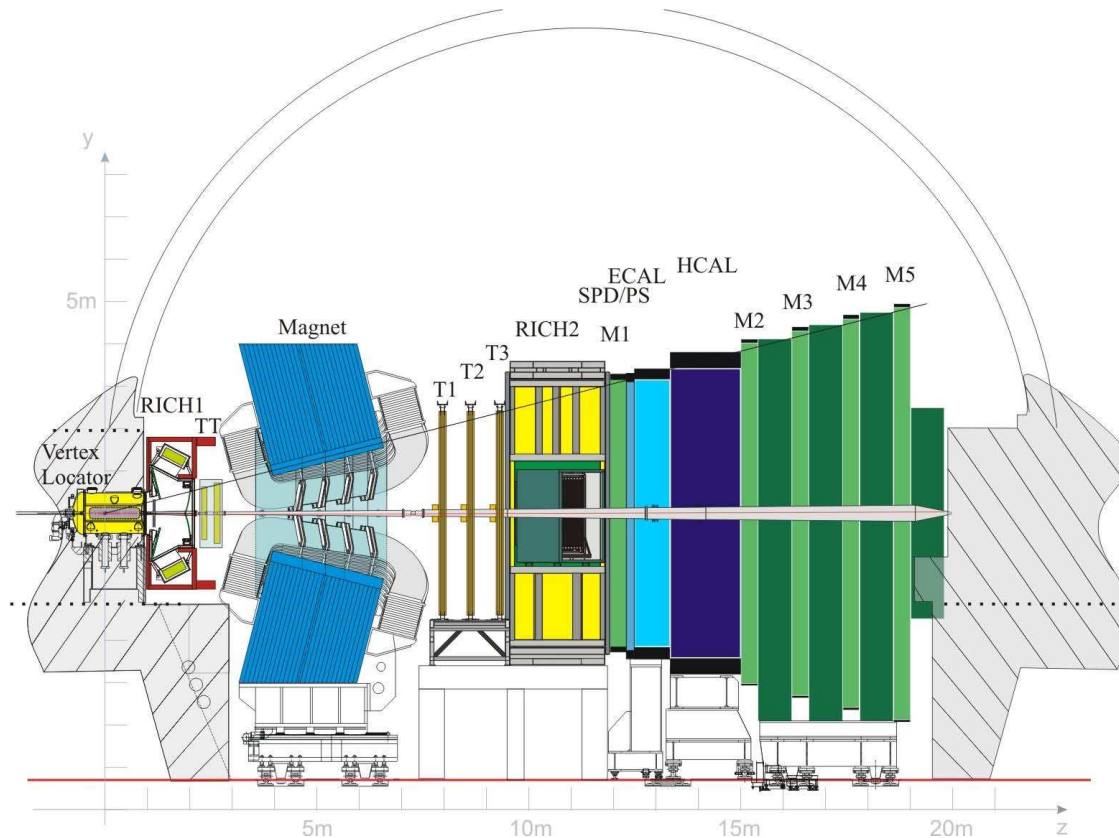
If rescattering phase in one decay channel generates direct  $CP$  violation in this region,

Rescattering phase should generate opposite sign direct  $CP$  violation in partner decay channel

# LHCb Detector

$pp$  collisions

$b$  quark tends to forward/backward direction



Forward spectrometer

Vertex Locator (VeLo)  
Precision tracking

Tracker Turicensis (TT)  
Tracking,  $p$  measurement

Ring Imaging Cherenkov (RICH)  
Particle identification

Electromagnetic Calorimeter (ECAL)  
 $e, \gamma$  ID

Hadronic Calorimeter (HCL)  
Hadronic showers

Muon Detector

Magnet polarity reversal

Data set:  $1 \text{ fb}^{-1}$  @ 7 TeV and  $2 \text{ fb}^{-1}$  @ 8 TeV

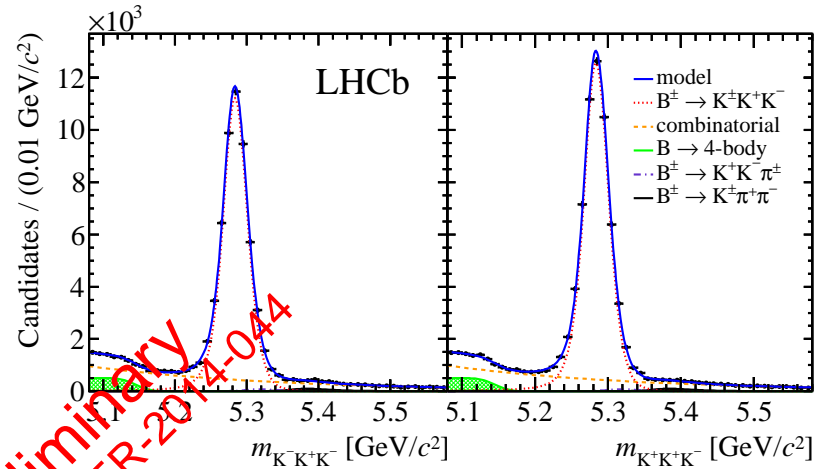
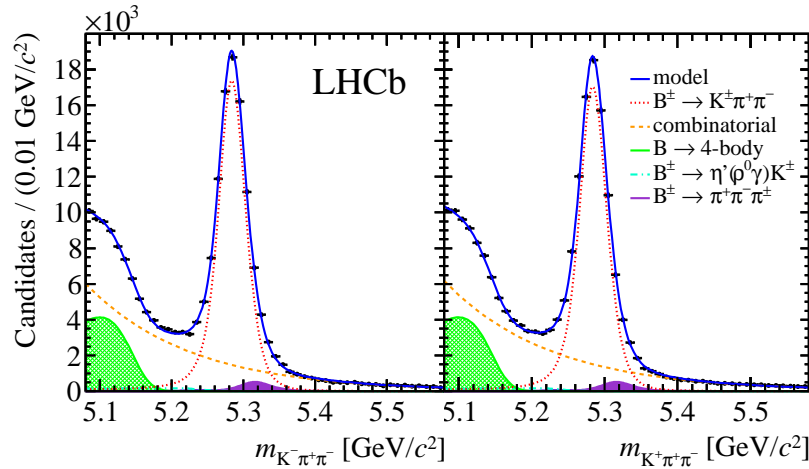
# $B^\pm \rightarrow K^\pm h^+ h^-, \pi^\pm h^+ h^-$

$$B^- \rightarrow K^- \pi^+ \pi^- \quad B^+ \rightarrow K^+ \pi^+ \pi^-$$

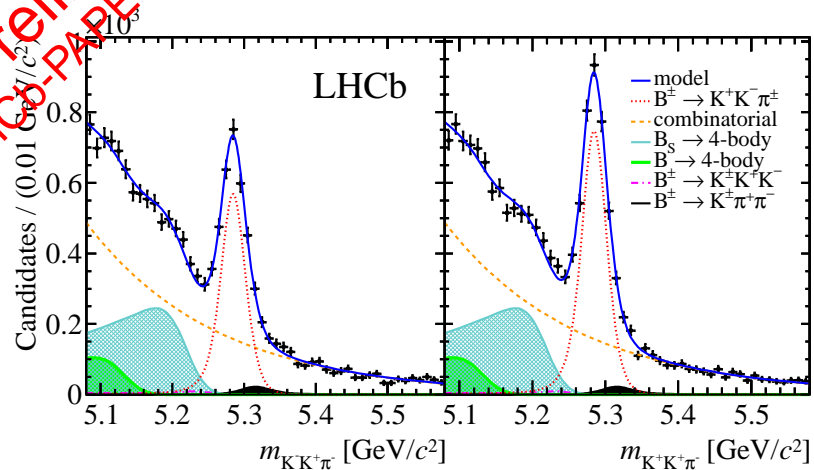
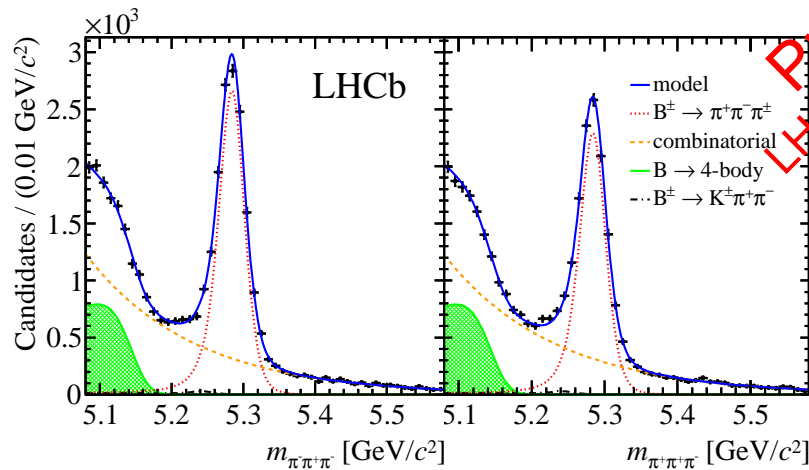
$$N_{\text{Sig}} = 181069 \pm 404 \text{ (stat)}$$

$$B^- \rightarrow K^- K^+ K^- \quad B^+ \rightarrow K^+ K^+ K^-$$

$$N_{\text{Sig}} = 109240 \pm 354 \text{ (stat)}$$



Penguin



Tree

$$B^- \rightarrow \pi^- \pi^+ \pi^- \quad B^+ \rightarrow \pi^+ \pi^+ \pi^-$$

$$N_{\text{Sig}} = 24907 \pm 222 \text{ (stat)}$$

$$B^- \rightarrow \pi^- K^+ K^- \quad B^+ \rightarrow \pi^+ K^+ K^-$$

$$N_{\text{Sig}} = 6161 \pm 172 \text{ (stat)}$$

$$B^\pm \rightarrow K^\pm h^+ h^-, \pi^\pm h^+ h^-$$

Global direct  $CP$  asymmetry

$$\mathcal{A}_{CP}^{\text{Raw}} = \frac{N_{B^-} - N_{B^+}}{N_{B^-} + N_{B^+}}$$

Correct for  $B^\pm$  production asymmetry and unpaired hadron (eg.  $B^\pm \rightarrow K^\pm \pi^+ \pi^-$ ) detection asymmetry

$$\mathcal{A}_{CP} = \mathcal{A}_{CP}^{\text{Raw}} - \mathcal{A}_P - \mathcal{A}_D^h$$

$\mathcal{A}_P$  and  $\mathcal{A}_D^K$  from  $B^\pm \rightarrow J/\psi[\mu^+ \mu^-]K^\pm$ , PRL **108** 201601 (2012)

$\mathcal{A}_D^\pi$  from prompt  $D^+$  studies, PLB **713** 186 (2012)

$$\mathcal{A}_{CP}(B^\pm \rightarrow K^\pm \pi^+ \pi^-) = +0.025 \pm 0.004 \text{ (stat)} \pm 0.004 \text{ (syst)} \pm 0.007 \text{ (} J/\psi K^\pm \text{)} \quad (2.8\sigma)$$

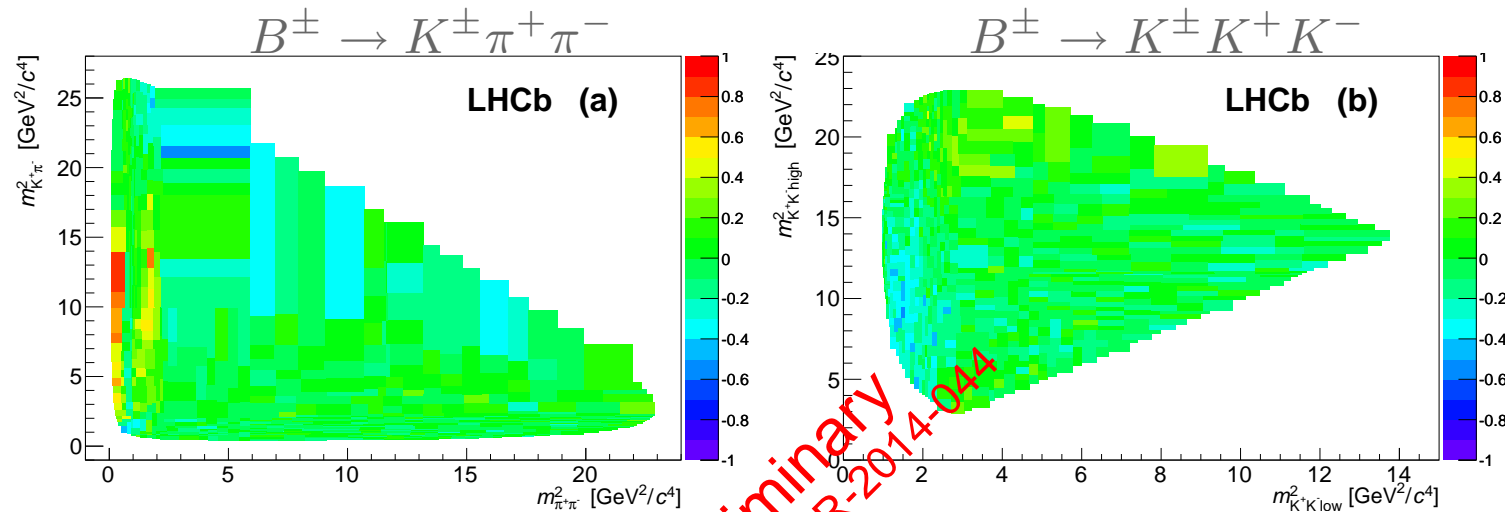
$$\mathcal{A}_{CP}(B^\pm \rightarrow K^\pm K^+ K^-) = -0.036 \pm 0.004 \text{ (stat)} \pm 0.002 \text{ (syst)} \pm 0.007 \text{ (} J/\psi K^\pm \text{)} \quad (4.3\sigma)$$

$$\mathcal{A}_{CP}(B^\pm \rightarrow \pi^\pm \pi^+ \pi^-) = +0.058 \pm 0.008 \text{ (stat)} \pm 0.009 \text{ (syst)} \pm 0.007 \text{ (} J/\psi K^\pm \text{)} \quad (4.2\sigma)$$

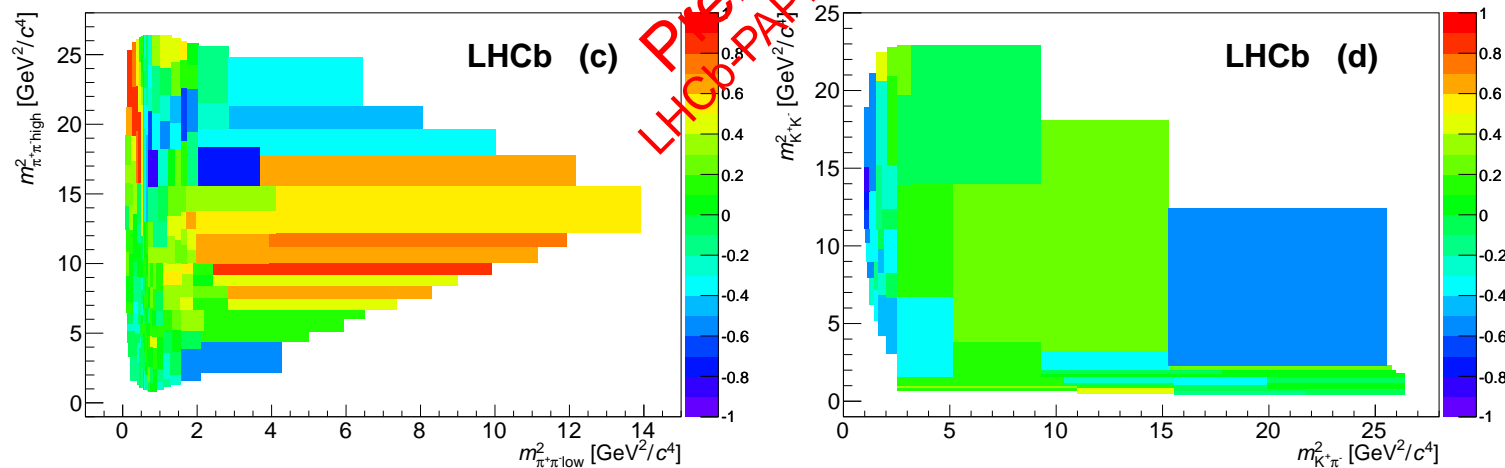
$$\mathcal{A}_{CP}(B^\pm \rightarrow \pi^\pm K^+ K^-) = -0.123 \pm 0.017 \text{ (stat)} \pm 0.012 \text{ (syst)} \pm 0.007 \text{ (} J/\psi K^\pm \text{)} \quad (5.6\sigma)$$

$$B^\pm \rightarrow K^\pm h^+ h^-, \pi^\pm h^+ h^-$$

Dalitz plot background subtracted and efficiency corrected with  $\sim (N_{B^+} + N_{B^-})$  in each bin



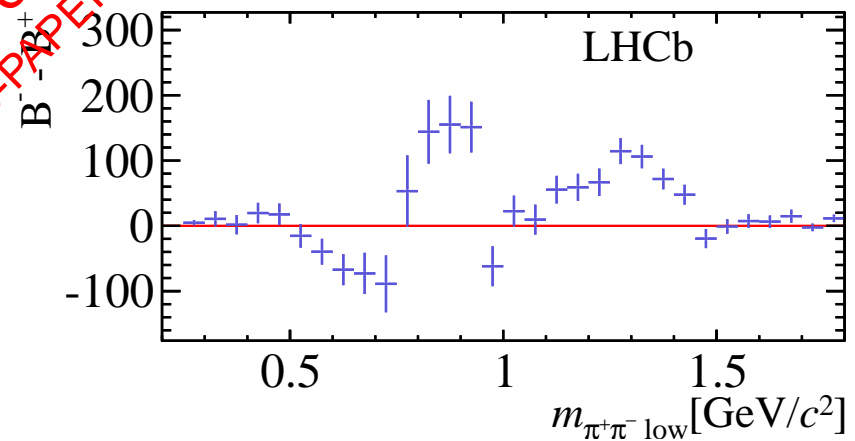
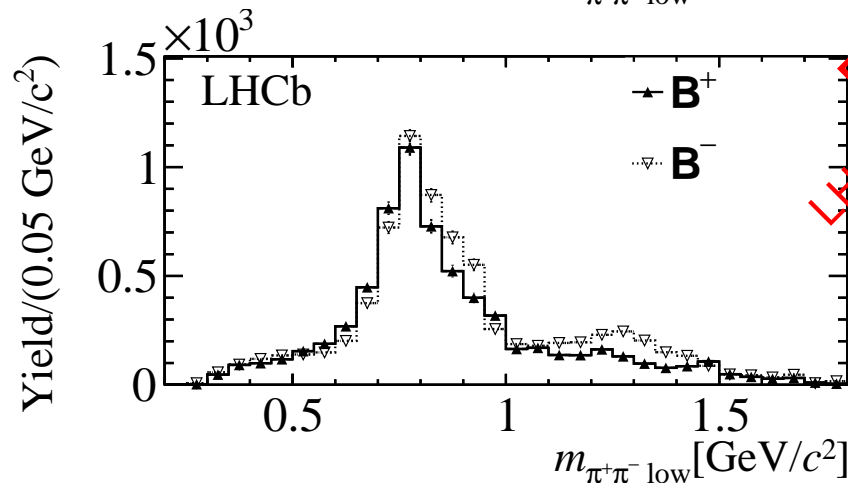
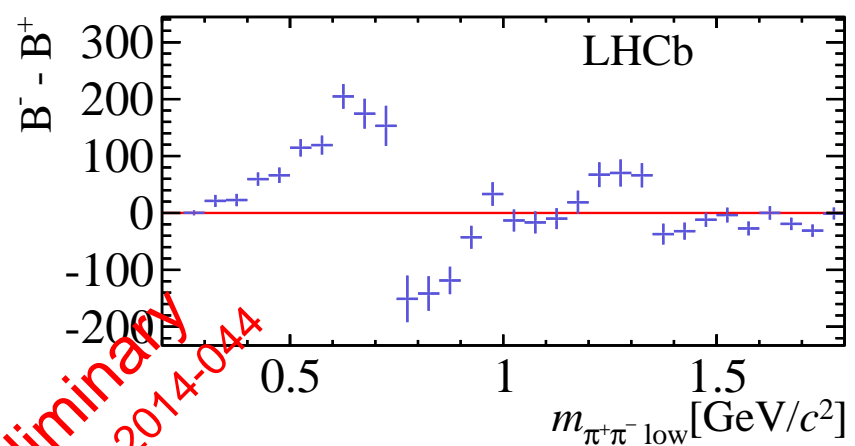
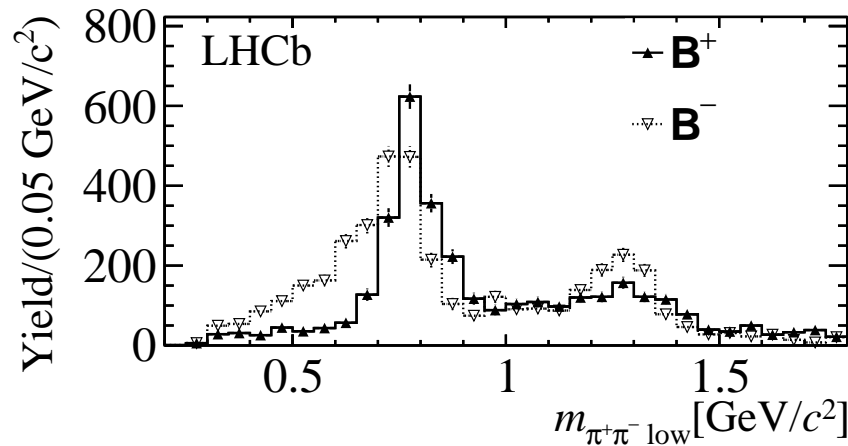
Penguin



Tree

# $CP$ Asymmetry by Interference

Project onto  $m_{\pi\pi}$  of  $B^\pm \rightarrow \pi^\pm \pi^+ \pi^-$

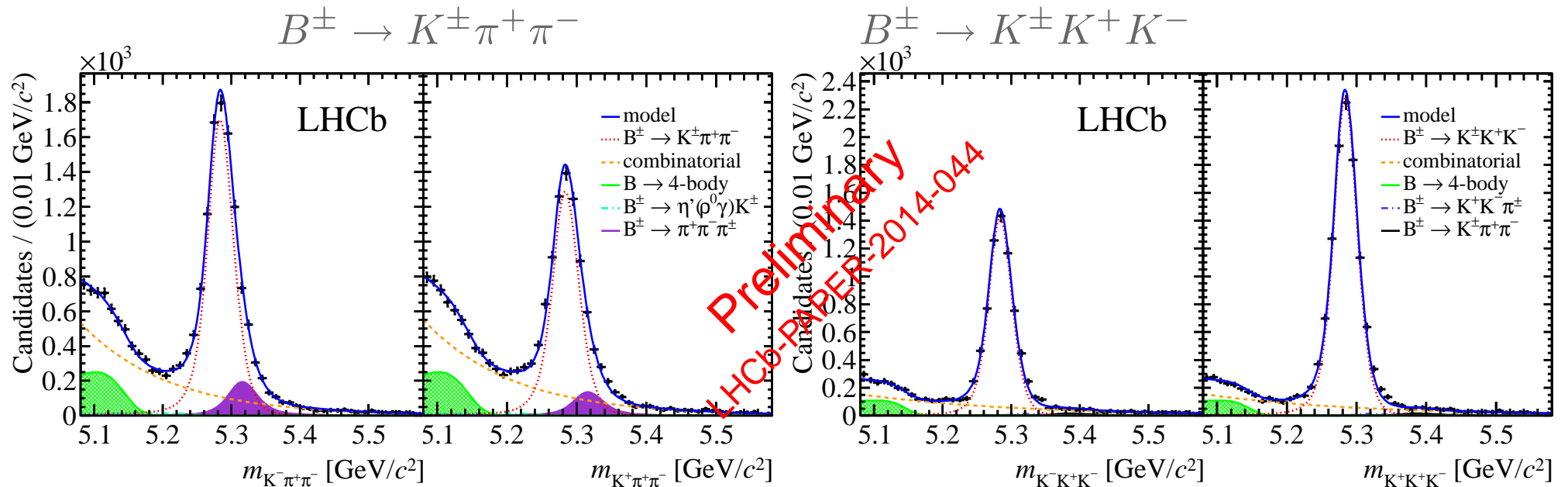


Sign-flip and zero around  $\rho^0$  pole,  $CP$  asymmetry may be dominated by real part of Breit-Wigner



# $CP$ Asymmetry by Rescattering

$\pi\pi \leftrightarrow KK$  rescattering region:  $1.0 - 1.5 \text{ GeV}/c^2$



$$\mathcal{A}_{CP}(B^\pm \rightarrow K^\pm \pi^+ \pi^-) = +0.121 \pm 0.012 \text{ (stat)} \pm 0.017 \text{ (syst)} \pm 0.007 (J/\psi K^\pm)$$

$$\mathcal{A}_{CP}(B^\pm \rightarrow K^\pm K^+ K^-) = -0.211 \pm 0.011 \text{ (stat)} \pm 0.004 \text{ (syst)} \pm 0.007 (J/\psi K^\pm)$$

Clear opposite sign  $CP$  asymmetry in  $KK/\pi\pi$  - related channels

$KK \leftrightarrow \pi\pi$  rescattering would require this by  $CPT$  conservation

# $B^\pm \rightarrow K^\pm p\bar{p}$ and $B^\pm \rightarrow \pi^\pm p\bar{p}$

New preliminary result based on full data set

$B^\pm \rightarrow K^\pm p\bar{p}$  penguin dominated

$B^\pm \rightarrow \pi^\pm p\bar{p}$  tree dominated

Similar physics to non-baryonic 3-body charmless decays

$p\bar{p} \leftrightarrow h^+h^-$  rescattering expected to be smaller than

$KK \leftrightarrow \pi\pi$  rescattering

$CP$  asymmetry could be less pronounced

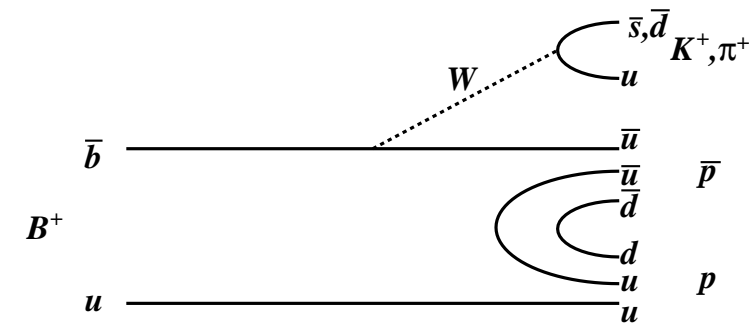
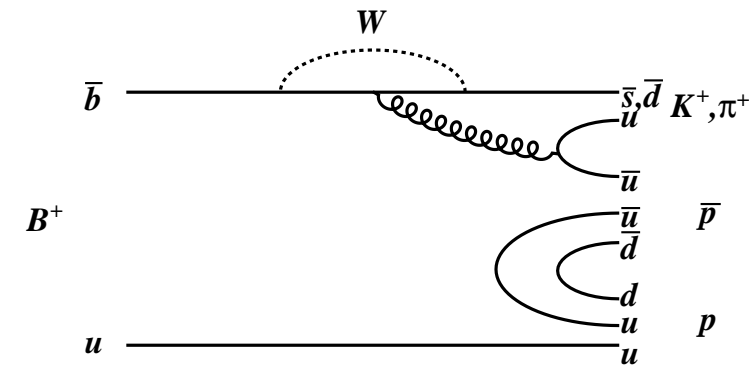
Threshold enhancement in low  $m_{p\bar{p}}$  typical in  $B \rightarrow p\bar{p}X$  decays

Need to better understand dynamics of these decays

Previous publication based on  $1 \text{ fb}^{-1}$

No evidence of  $CP$  violation

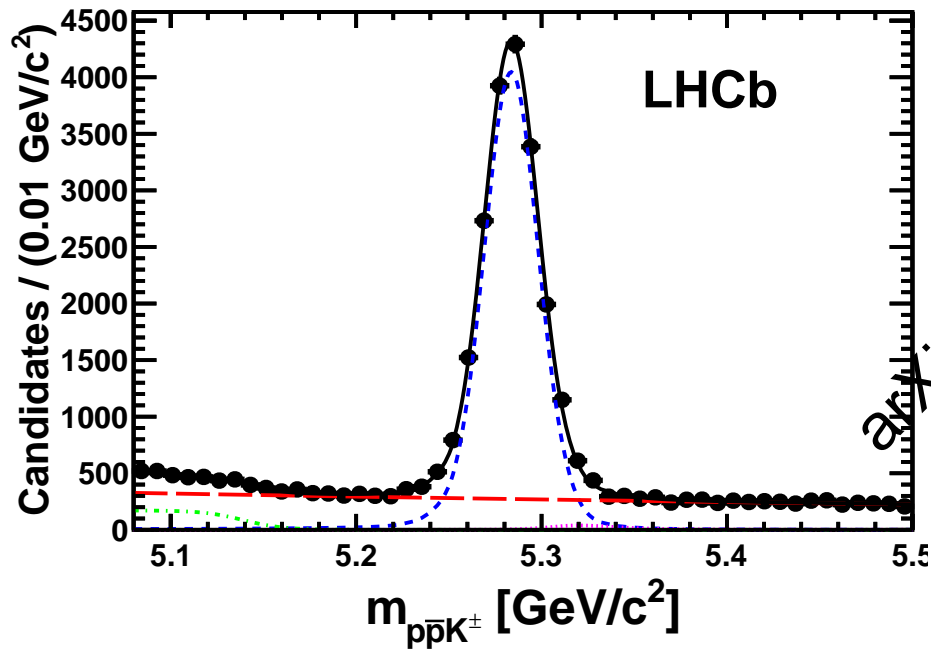
PRD **88** 052015 (2013)



# Signal Yield

$$B^\pm \rightarrow K^\pm p\bar{p}$$

$$N_{\text{Sig}} = 18721 \pm 142 \text{ (stat)}$$

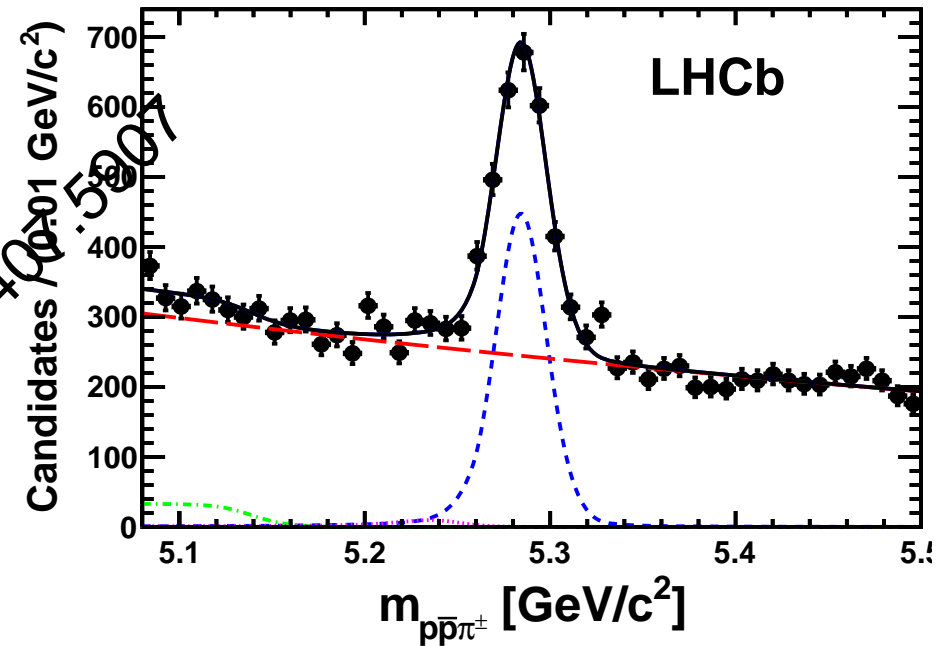


Blue: Signal

Red: Combinatorial

$$B^\pm \rightarrow \pi^\pm p\bar{p}$$

$$N_{\text{Sig}} = 1988 \pm 74 \text{ (stat)}$$



Green: Partially reconstructed

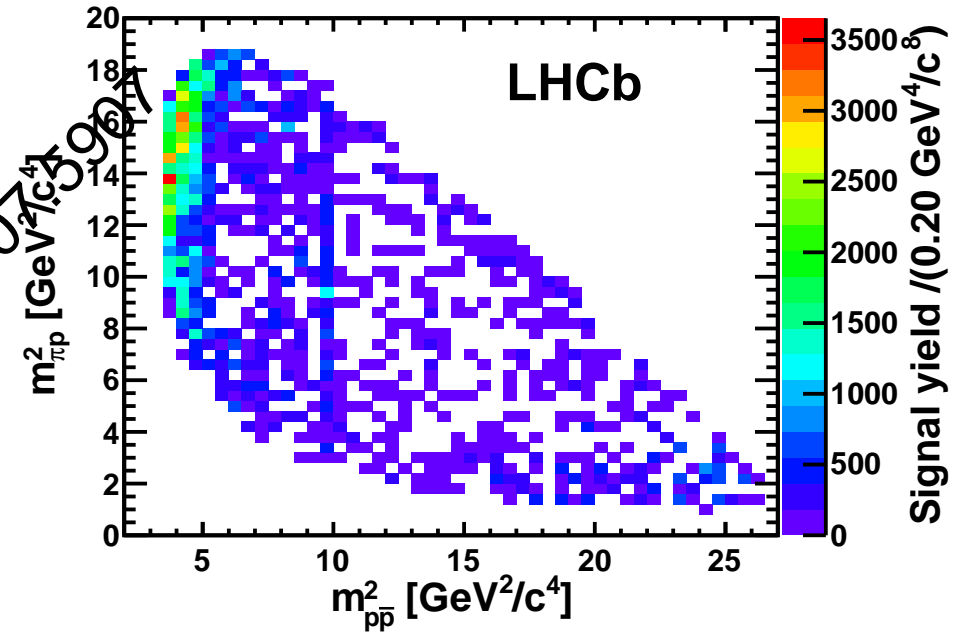
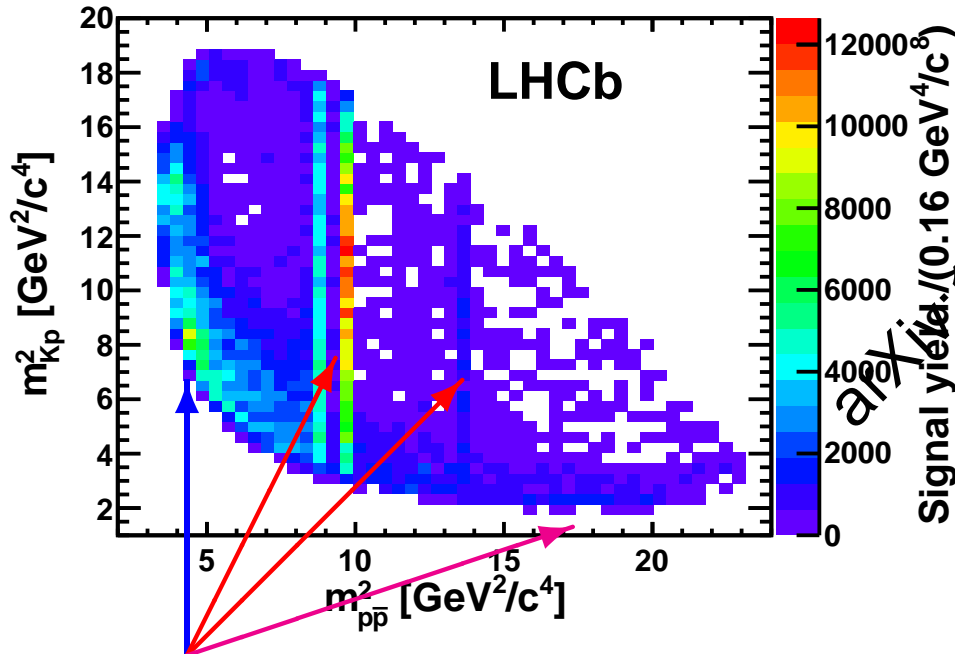
Purple: Cross-feed

# Dalitz Plot

Background subtracted and efficiency corrected using calibrated MC

$$B^\pm \rightarrow K^\pm p\bar{p}$$

$$B^\pm \rightarrow \pi^\pm p\bar{p}$$



Low  $m_{p\bar{p}}$  threshold enhancement

Charmonium resonances

Define  $m_{p\bar{p}} < 2.85 \text{ GeV}/c^2$  as charmless region

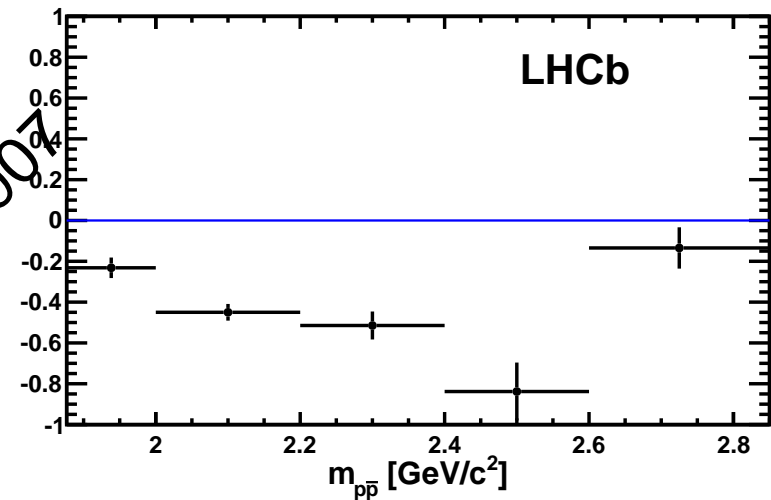
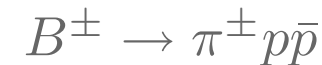
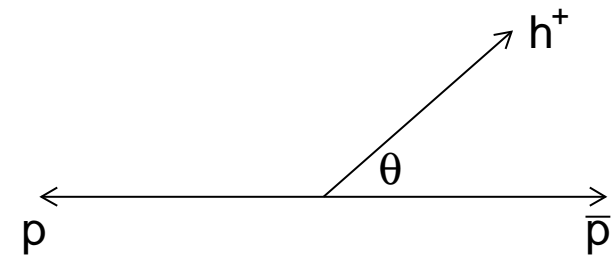
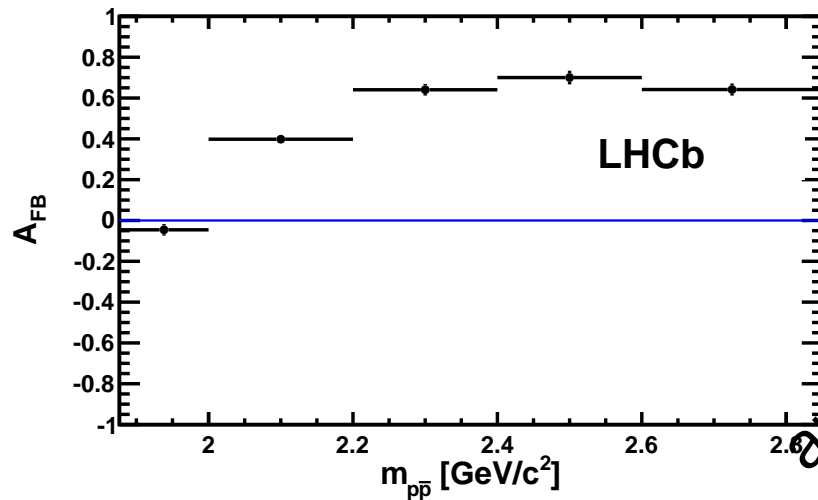
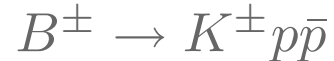
$$\Lambda(1520) \rightarrow pK$$

# Forward-Backward Asymmetry

$$A_{\text{FB}} = \frac{N(\cos \theta > 0) - N(\cos \theta < 0)}{N(\cos \theta > 0) + N(\cos \theta < 0)}$$

Measure forward-backward asymmetry in bins of  $m_{p\bar{p}}$

Gives hint on  $p\bar{p}$  waves that might contribute



$$A_{\text{FB}}^{p\bar{p}K} (m_{p\bar{p}} < 2.85 \text{ GeV}/c^2) = +0.495 \pm 0.012 \text{ (stat)} \pm 0.007 \text{ (syst)}$$

$$A_{\text{FB}}^{p\bar{p}\pi} (m_{p\bar{p}} < 2.85 \text{ GeV}/c^2) = -0.409 \pm 0.033 \text{ (stat)} \pm 0.006 \text{ (syst)}$$

Large asymmetries indicate dominance of non-resonant  $p\bar{p}$  scattering, J Phys G **34** 283 (2007)

# Direct $CP$ Asymmetry

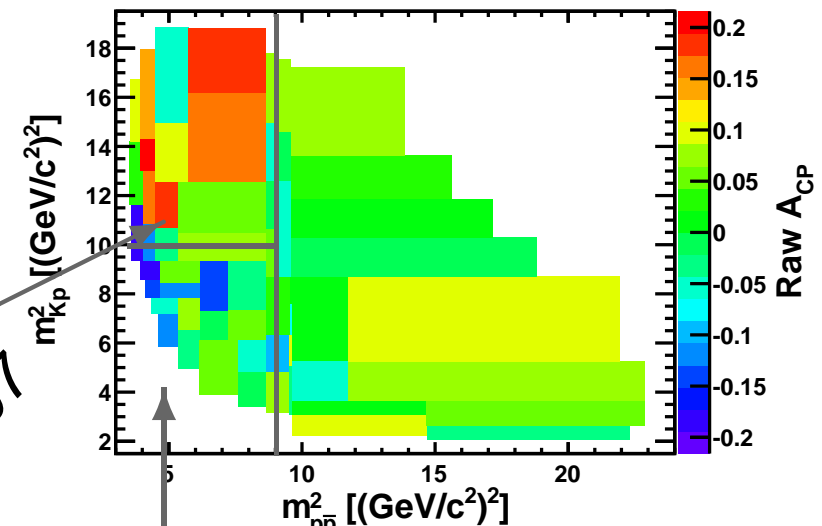
Measure  $\mathcal{A}_{CP}$  in Dalitz plot bins

Same number of events in each bin

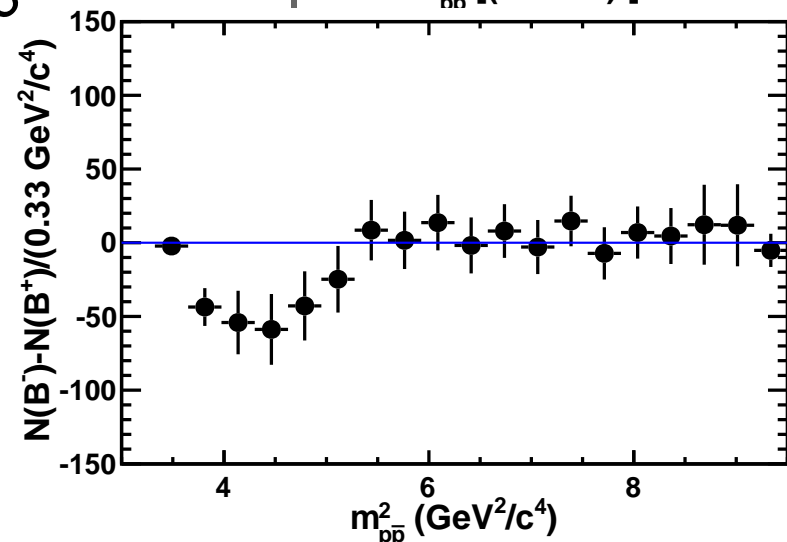
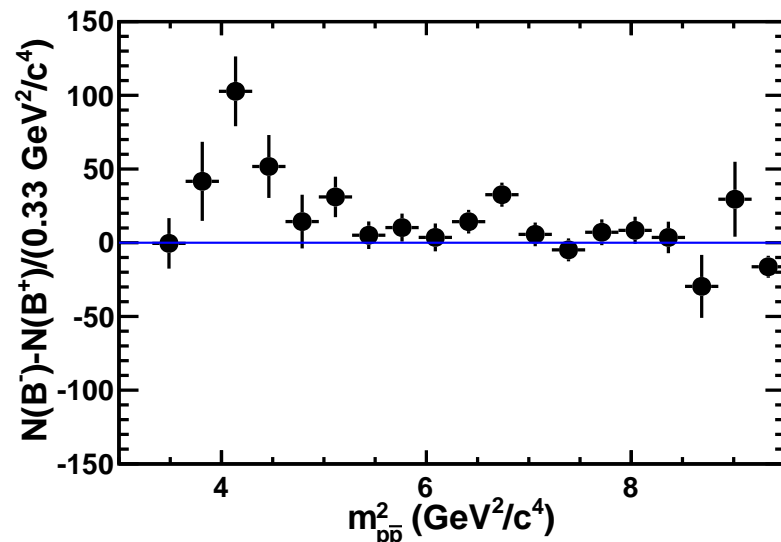
$$\mathcal{A}_{CP}(m_{p\bar{p}} < 2.85 \text{ GeV}/c^2, m_{Kp}^2 > 10 \text{ GeV}^2/c^4) \\ = +0.096 \pm 0.024 \text{ (stat)} \pm 0.004 \text{ (syst)} \quad (4.0\sigma)$$

First evidence of  $CP$  violation in any  $B$  decay involving baryons

$B^\pm \rightarrow K^\pm p\bar{p}$



arXiv:1407.5907



# Summary

New results with the full LHCb data set

$$B^\pm \rightarrow K^\pm h^+ h^- \text{ and } B^\pm \rightarrow \pi^\pm h^+ h^-$$

Evidence of global direct  $CP$  violation

Large localised  $CP$  asymmetries across the Dalitz plot

Long-distance effects play an important role in generating a strong phase

$$B^\pm \rightarrow h^\pm p\bar{p}$$

Large forward-backward asymmetries indicate dominance of non-resonant  $p\bar{p}$  scattering

First evidence  $CP$  violation in decays involving baryons

Sign-flip of  $CP$  asymmetry probably generated by interference of long-distance  $p\bar{p}$  waves

Look forward to amplitude analyses on all these channels