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HI JENA Helmholtz Institute lena

Nonlinear QED effects:

Quantum Vacuum Nonlinearities @ Gamma Factory

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Can the Gamma Factory be used to detect quantum vacuum nonlinearities, e.g., vacuum birefringence?

> classical ED is very successful in describing the physics of macroscopic e.m. fields

$$\mathcal{L}_{MW} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \quad \text{(in vacuo)} \downarrow E.o.M. \partial_{\mu} F^{\mu\nu} = 0 \quad \rightarrow \quad \text{linear, superposition principle } \checkmark \rightarrow \quad \text{there is no } \hbar$$

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- > however, we believe in quantum (field) theory
 - ightarrow "quantum vacuum"
 - \rightarrow classical theory should arise in formal limit of $\hbar \rightarrow 0$; quantum corrections are to be expected for $\hbar \neq 0$
- > What is the "true" theory of ED accounting for quantum corrections?

(2/2)

"true" theory of ED of macroscopic fields

[Heisenberg, Euler: Z. Phys. **98** (1936)], [Weisskopf: Mat. Fys. Medd. **14** (1936)], [Schwinger: Phys. Rev.: **82** (1951)]

- > QED: + macroscopic field e
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$$\mathcal{L}_{HE} = \mathcal{L}_{MW} + \times \mathcal{N} + \cdots$$

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$$\mathcal{L}_{\rm HE} = \mathcal{L}_{\rm MW} + \mathbf{x} +$$

where $\alpha = \frac{e^2}{4\pi\hbar c\epsilon_0} \simeq \frac{1}{137}$, $E_{\rm cr} = \frac{m^2 c^3}{\hbar e} \simeq 1.3 \times 10^{18} \, \frac{\rm V}{\rm m}$, $B_{\rm cr} = \frac{E_{\rm cr}}{c} \simeq 4.4 \times 10^9 \, {\rm T}$

A promising signature: vacuum birefringence (1/2)

A decomposition of $F^{\mu\nu} \to \overline{F}^{\mu\nu} + f^{\mu\nu}$ and linearization of E.o.M. in probe light field

pump probe

 \rightarrow transverse eigenmodes with different speeds of light / refractive indices



A promising signature: vacuum birefringence (1/2)

- > decomposition of $F^{\mu\nu} \rightarrow \bar{F}^{\mu\nu} + f^{\mu\nu}$ and linearization of E.o.M. in probe light field
 \$\overline{f}\$ \$\overline{f}\$ \$\overline{f}\$ pump probe
 - \rightarrow transverse eigenmodes with different speeds of light / refractive indices



A promising signature: vacuum birefringence (1/2)

- A decomposition of $F^{\mu\nu} \rightarrow \bar{F}^{\mu\nu} + f^{\mu\nu}$ and linearization of E.o.M. in probe light field
 Implement the probe
 - \rightarrow transverse eigenmodes with different speeds of light / refractive indices



A promising signature: vacuum birefringence (2/2)

planned experiments with pump = high-intensity laser at XFEL facilities [HIBEF, European XFEL]



A promising signature: vacuum birefringence (2/2)

planned experiments with pump = high-intensity laser at XFEL facilities [HIBEF, European XFEL]



Can something similar be done @ GF?

- > typical starting point in studies of previously mentioned approaches: Heisenberg-Euler effective Lagrangian $\mathcal{L}_{HE}(F^{\mu\nu})$ for small frequency fields
 - \rightarrow neglects derivative terms $\sim \partial_{\alpha}^{n} F^{\mu\nu}$ with $n \geq 1$, or powers of energies $\sim \omega^{n} F^{\mu\nu}$ in spectral domain, respectively
 - ightarrow genuine reference scale is ~m , i.e., contributions $~\sim (rac{\omega}{mc^2})^n~$ not accounted for
- ▶ for GF: $\omega \simeq 400 \,\mathrm{MeV} \quad \leftrightarrow \quad \frac{\omega}{mc^2} \gg 1$

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- → for GF: $\omega \simeq 400 \,\text{MeV}$ \leftrightarrow $\frac{\omega}{mc^2} \gg 1$ \rightarrow use polarization tensor!

 $\Pi^{\mu\nu}(\omega|F^{\mu\nu}) = \underbrace{\overset{*}}_{\sim} \underbrace{\overset{*}}_{\leftarrow} \underbrace{\overset{*}}_{\leftarrow} \underbrace{\overset{*}}_{\sim} \underbrace{\overset{*}}_{\leftarrow} \underbrace{\overset{*}}_{$

2 plane waves

[Batalin, Shabad: JETP **60** (1971)]

[Becker, Mitter: J.Phys. A 8 (1975)], [Baier, et al.: JETP 42 (1976)]

(1/!)

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 $\Pi^{\mu\nu}(\omega|F^{\mu\nu}) = \underbrace{}_{\kappa} \underbrace$

> (1) \rightarrow reliable study of the effect for $\vec{B} = const$. envisioning the use of spare LHC magnet(s): $L \simeq 15 \,\mathrm{m}$, $B \simeq 8.4 \,\mathrm{T}$

 \succ find the same formulas for $~n_{\parallel,\perp}~$ as from $~\mathcal{L}_{
m HE}~$

$$\begin{cases} n_{\parallel} \\ n_{\perp} \end{cases} \simeq 1 + \frac{1}{90} \frac{\alpha}{\pi} \left(\frac{B}{B_{\rm cr}}\right)^2 \begin{cases} 7\\ 4 \end{cases}, \qquad B_{\rm cr} \simeq 4.4 \cdot 10^9 \,\mathrm{T}$$

given that $k^2 \simeq 0$, $\frac{B}{B_{\rm cr}} \ll 1$ and $\left(\frac{B}{B_{\rm cr}}\right)^2 \left(\frac{\omega}{mc^2}\right)^2 \ll 1$ [FK: PRD 88 (2013)]

(2/5)

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 $\uparrow 8.4 \,\mathrm{T}$, 400 MeV $\uparrow L \simeq 15 \,\mathrm{m}$
 1.9×10^{-9} 2.3×10^{-12}
 $\rightarrow \text{ ellipticity: } \Delta \phi = \frac{\omega L}{\hbar c} (n_{\parallel} - n_{\perp}) \simeq \boxed{8.4 \times 10^{-6}}$

(> there are also imaginary parts \leftrightarrow polarization sensitive absorption coefficients due to the principle possibility of pair production, <u>but</u> exp. suppressed with $\frac{mc^2}{\omega} \frac{B_{cr}}{B} \gg 1$) [Baier, Katkov: PRD **75** (2007)]

(2/5)

> Alternatively (2) \rightarrow collision of γ beam with high-intensity laser field (= plane wave)

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"naive" estimate
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 \succ there are studies of vacuum birefringence with high-energy/ γ probes

[Kotkin, Serbo: Phys. Lett. B **413** (1997)], [Nakamiya, Homma: PRD **96** (2017)], [King, Elkina: PRA **94** (2016)], [Bragin, *et al*.: PRL **119** (2017)]

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2-steps: (a) Compton scatt. e^- + \text{laser light} \rightarrow \gamma (b) vacuum birefringence
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 $k^{\mu} \simeq \omega(1, \vec{e}_x)$ and $\kappa^{\mu} \simeq \Omega(1, -\vec{e}_x)$

2-steps: (a) Compton scatt. $e^- + \text{laser light} \rightarrow \gamma$ (b) vacuum birefringence

 \succ here, the wave-vectors of the γ probe and high-intensity laser pump are



 \succ in the relevant limit we find again the same formulas for $~~n_{\parallel,\perp}~$ as from $~~\mathcal{L}_{
m HE}$

$$\begin{cases} n_{\parallel} \\ n_{\perp} \end{cases} \simeq 1 + \frac{1}{90} \frac{\alpha}{\pi} \frac{I}{I_{\rm cr}} \begin{cases} 7 \\ 4 \end{cases} , \qquad I_{\rm cr} = \epsilon_0 c \left(\frac{m^2 c^3}{e\hbar}\right)^2 \simeq 10^{29} \frac{\rm W}{\rm cm^2}$$

given that $k^2 \simeq 0$, $\frac{\kappa k}{(mc^2)^2} \ll 1$ and $\frac{I}{I_{\rm cr}} \left(\frac{\omega}{mc^2}\right)^2 \ll 1$ [Gies, FK, Shaisultanov: PRD 90 (2014)]

(4/5)

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 $\uparrow 1.5 \,\mathrm{eV}$, $400 \,\mathrm{MeV} \rightarrow \left(\frac{\omega}{mc^2}\right)^2 \simeq 6 \times 10^5$
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$$\quad \xrightarrow{I}_{I_{\rm cr}} \simeq \frac{P}{I_{\rm cr} w_0^2} \quad \xrightarrow{w_0 = 1\mu {\rm m}} \quad \frac{P}{10^6 {\rm PW}} \qquad \rightarrow \quad \frac{I}{I_{\rm cr}} \left(\frac{\omega}{mc^2}\right)^2 \simeq \frac{0.6 P}{1 {\rm PW}}$$

ightarrow (principle) potential to go "beyond Heisenberg and Euler"

(4/5)

$$P = 1 \,\mathrm{PW}: \quad \Delta \phi = \frac{\omega L}{\hbar c} (n_{\parallel} - n_{\perp}) \simeq \Delta \phi \big|_{B=const.} \times \frac{10^{-6}}{15} \times \frac{10^{-6}}{(1.9 \times 10^{-9})^2}$$
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(5/5)

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➤ <a> but idealized assumptions: "perfect shots", i.e., optimal synchronization, etc. high-intensity laser pulses have pulse durations of $\mathcal{O}(fs)$ rep. rate of $\mathcal{O}(Hz)$ \leftrightarrow magnetic field scenario where "every γ photon hits"

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- ➤ → but idealized assumptions: "perfect shots", i.e., optimal synchronization, etc. high-intensity laser pulses have pulse durations of $\mathcal{O}(fs)$ rep. rate of $\mathcal{O}(Hz)$ \leftrightarrow magnetic field scenario where "every γ photon hits"
- > (+) various other <u>non-linear</u> QED effects could potentially be investigated, if

$$\frac{I}{I_{\rm cr}} \left(\frac{\omega}{mc^2}\right)^2 \simeq \frac{0.6 P}{1 \, {\rm PW}} \rightarrow \mathcal{O}(1) \quad \text{, e.g., } \gamma \text{-photon induced pair production}$$

in a strong laser field with $=$ $\underbrace{\xi \xi \dots \xi}_{=}$

Conclusions and Outlook

- In this talk I have (briefly) discussed the possibility of studying (QED) vacuum nonlinearities in macroscopic electromagnetic fields at the Gamma Factory.
- > The focus was on vacuum birefringence \rightarrow ① LHC magnet ② high-intensity laser
- The Gamma Factory may complement and become a competitor to established and planned (high-intensity laser) experiments.
- Bounds on BSM signatures, e.g., minicharged particles that might so far have successfully evaded their detection.

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Thank you very much for your attention!