

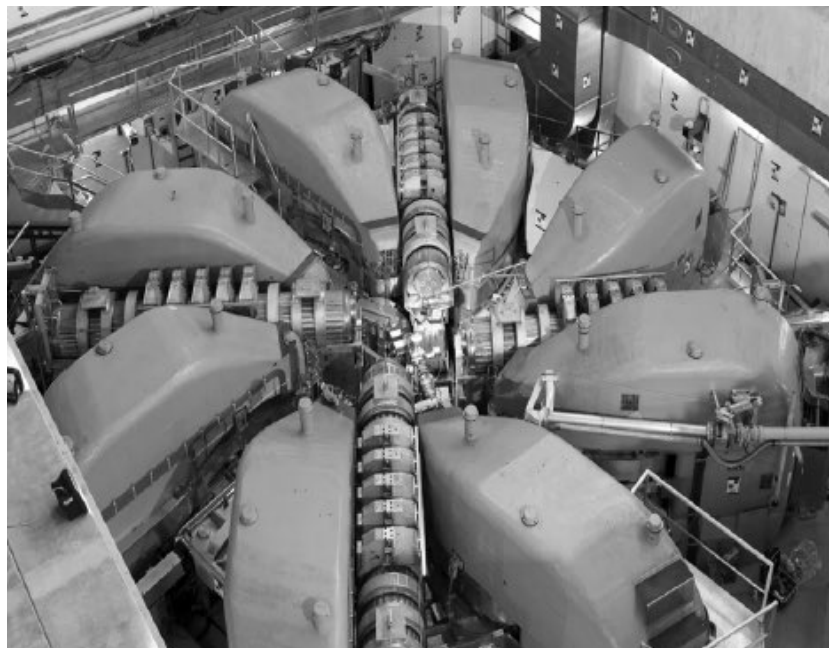


# Muon physics and PSI muon beam lines & future developments

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Angela Papa, Paul Scherrer Institut and University of Pisa/INFN On behalf of the HiMB and muCool group  
Physics Opportunity with Gamma Factory (virtual meeting)

**MITP Uni-Mainz 2020, Nov 30th - Dec 4th**



# Outline

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- The role of low energy precision physics
- The High Intensity Muon Beam project at PSI (HiMB)
- Towards High-Brightness low energy muon beams (muCool)
- Muon collider and Neutrino factory developments (in connection with low energy muon beam?)



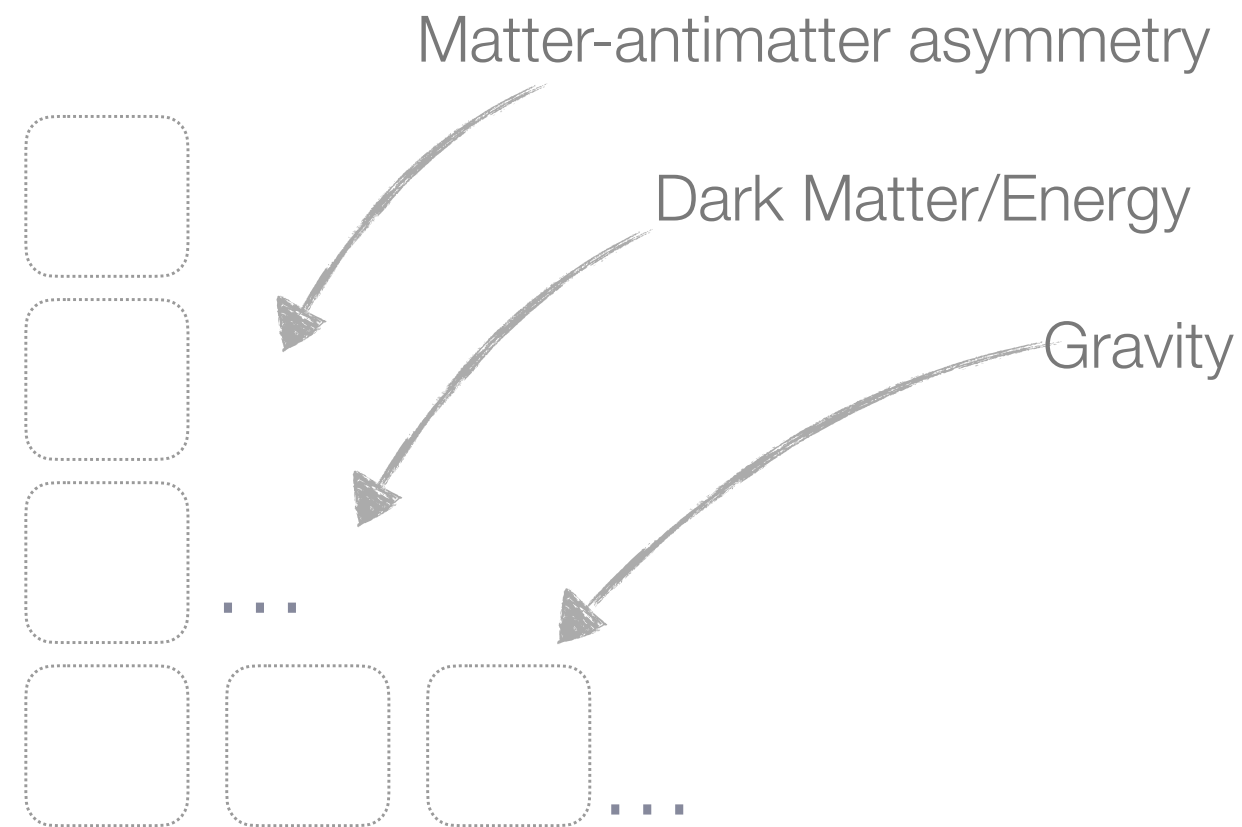
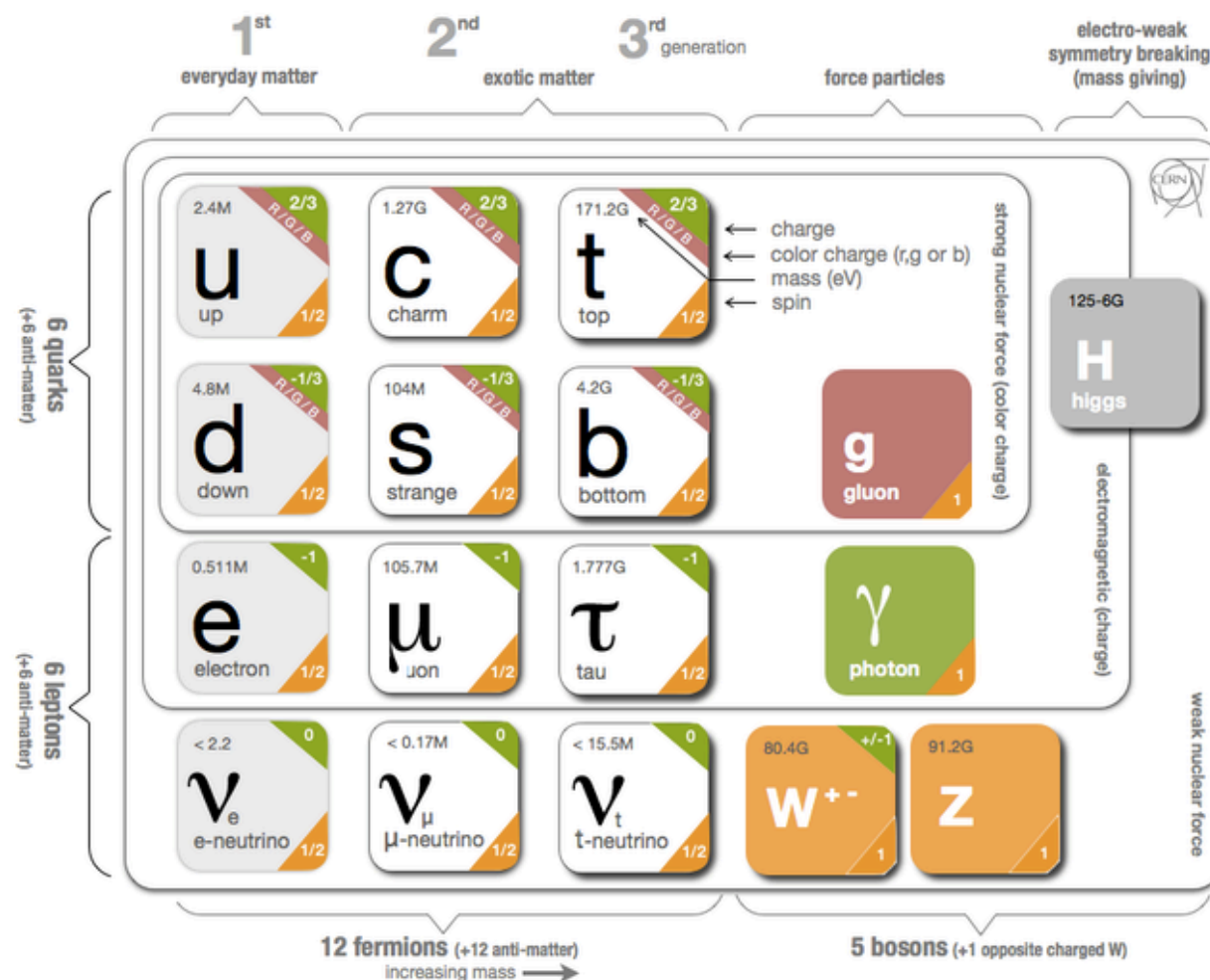
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- **The role of low energy precision physics**
- The High Intensity Muon Beam project at PSI (HiMB)
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# The role of the low energy precision physics

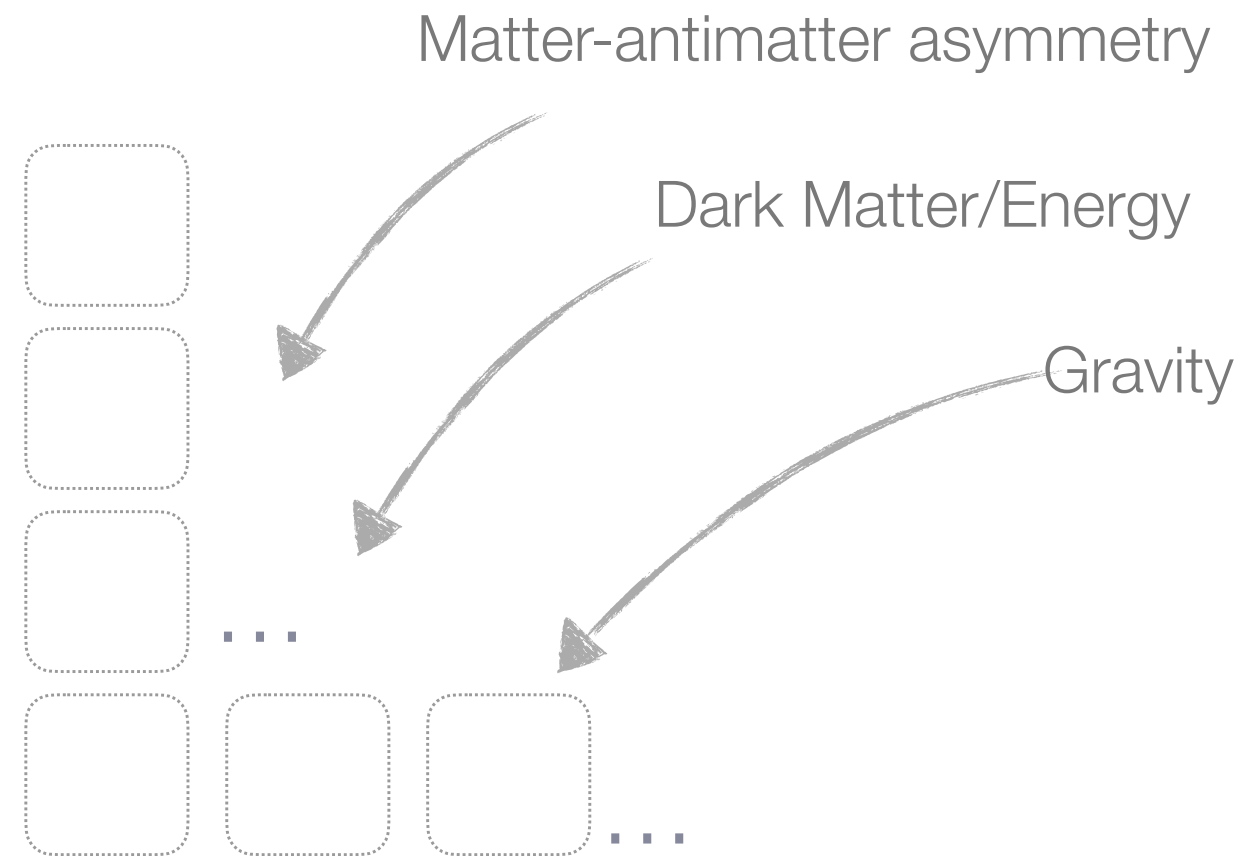
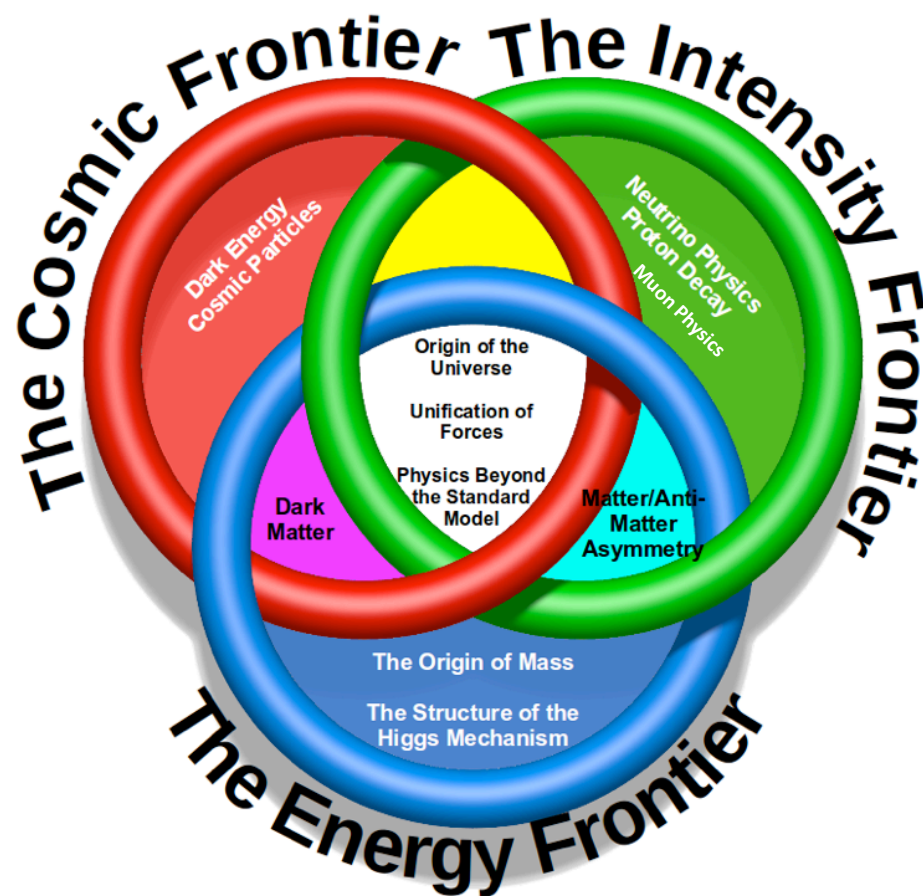
- The Standard Model of particle physics: A great triumph of the modern physics but not the ultimate theory



- Low energy precision physics: Rare/forbidden decay searches, symmetry tests, precision measurements very sensitive tool for unveiling new physics and probing very high energy scale

# The role of the low energy precision physics

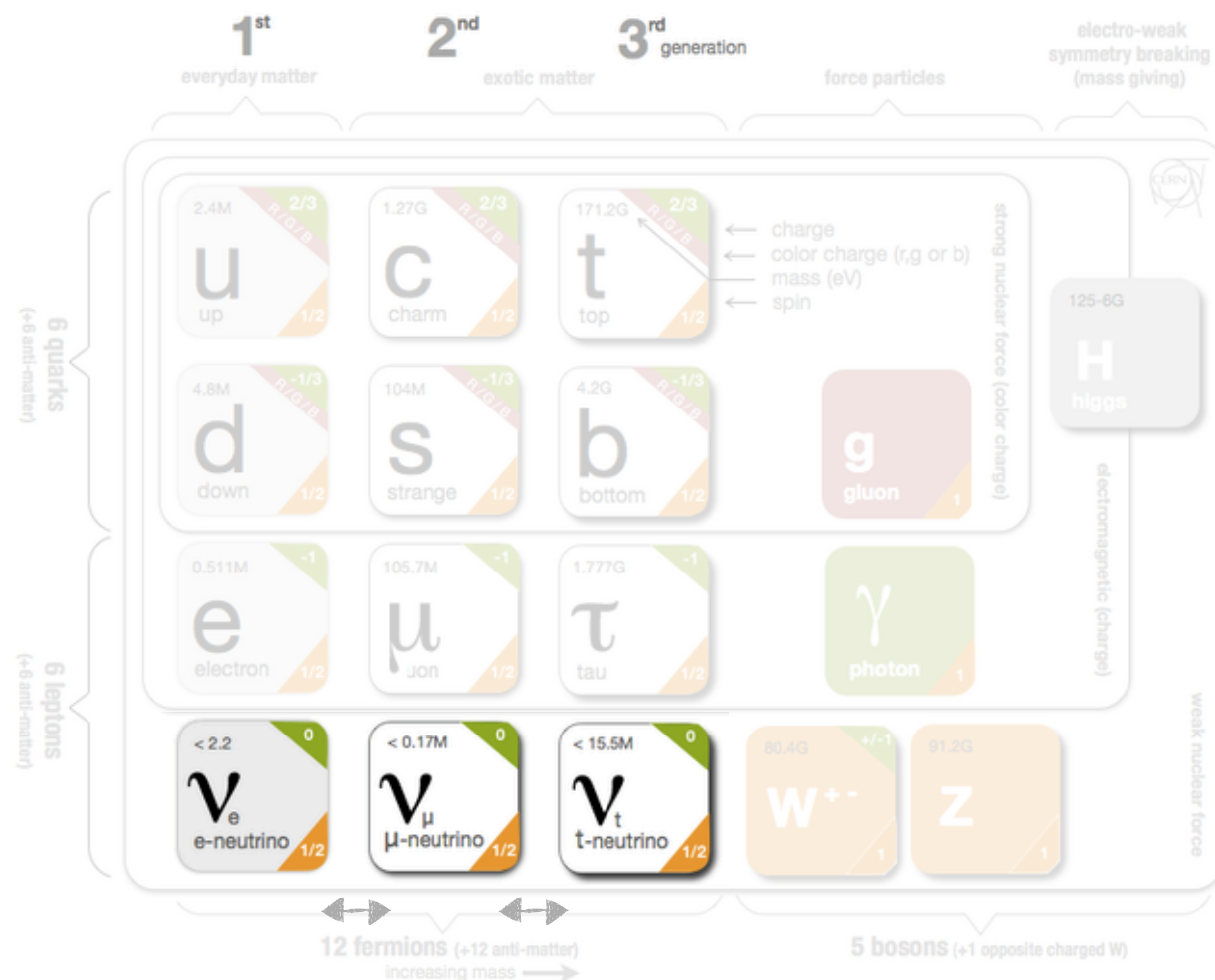
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# Charged lepton flavour violation

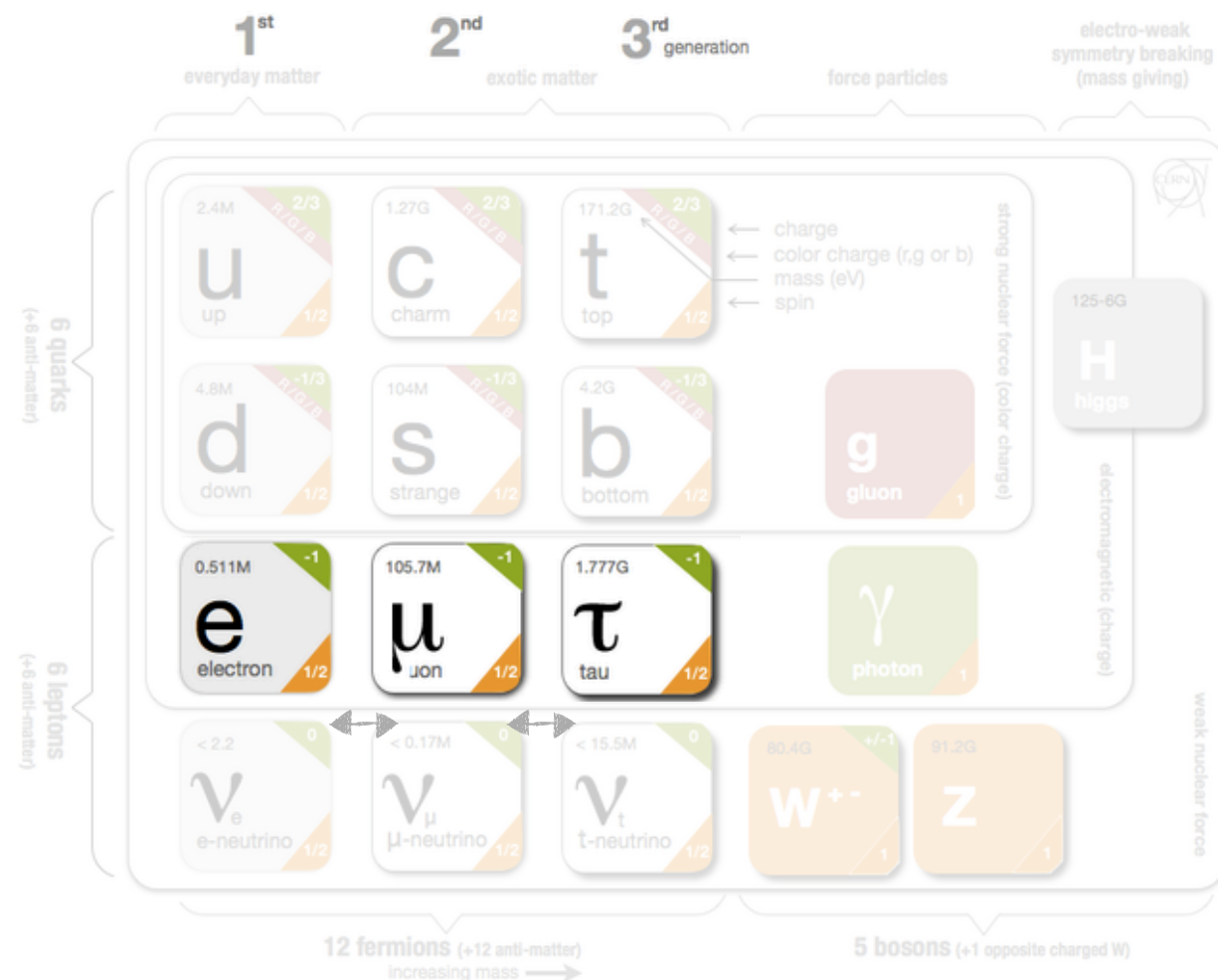
- Neutrino oscillations: Evidence of physics Behind Standard Model (BSM)  
Neutral lepton flavour violation



$$\Delta N_i \neq 0 \text{ with } i = 1, 2, 3$$

# Charged lepton flavour violation

- Neutrino oscillations: Evidence of physics Behind Standard Model (BSM)  
Neutral lepton flavour violation



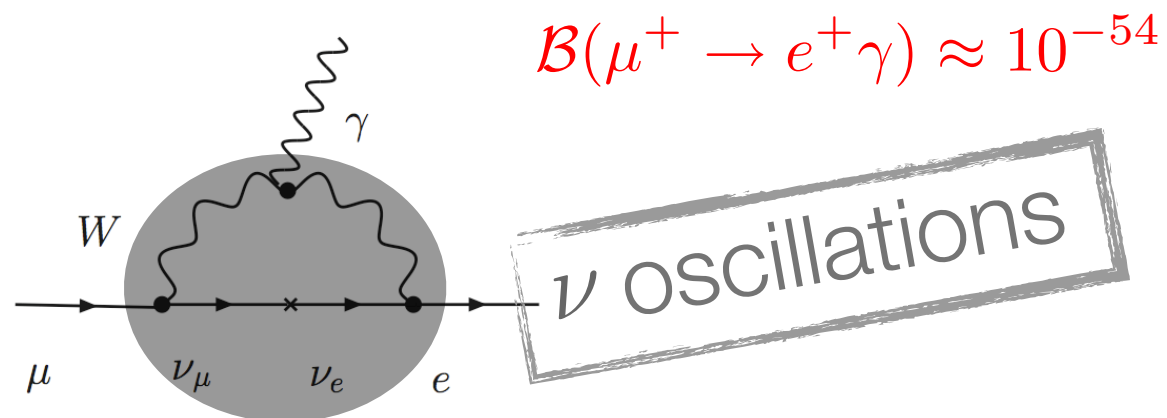
$$\Delta N_i \neq 0 \text{ with } i = 1, 2, 3$$

- Charged lepton flavour violation: NOT yet observed



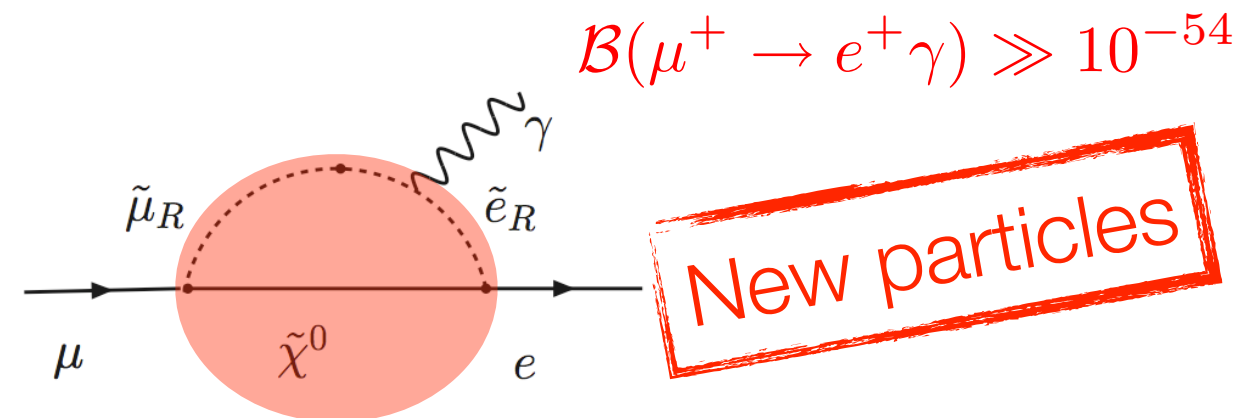
# Charged lepton flavour violation search: Motivation

SM with massive neutrinos (Dirac)



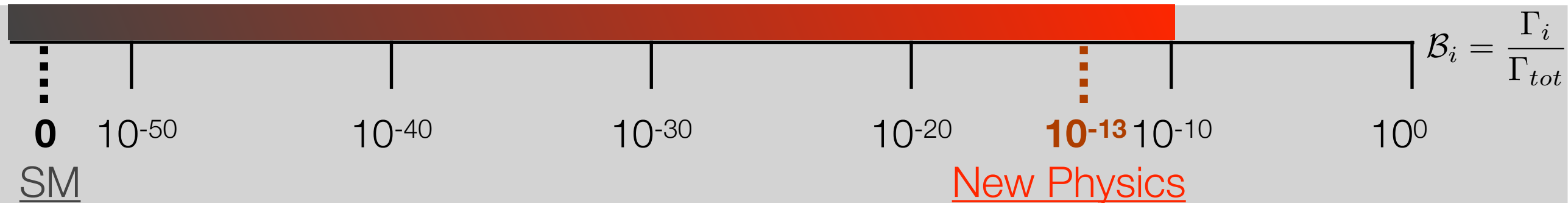
too small to access experimentally

BSM



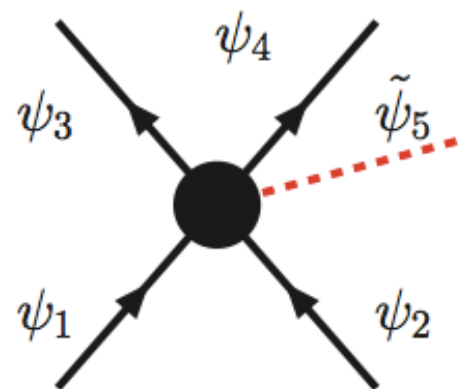
**an experimental evidence:  
a clear signature of New Physics NP**  
(SM background FREE)

Current upper limits on  $\mathcal{B}_i$



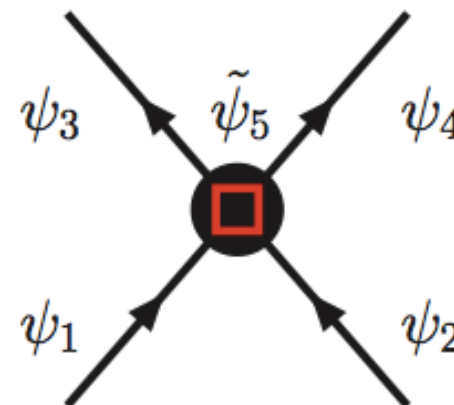
# Complementary to “Energy Frontier”

Energy frontier



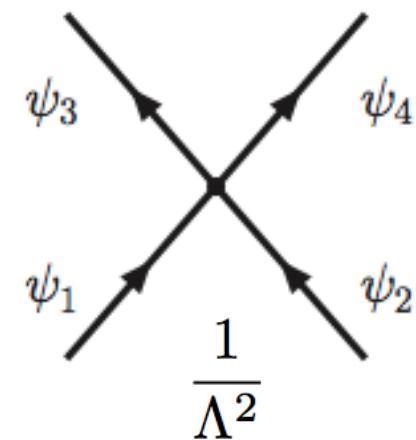
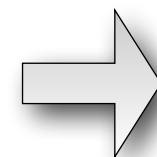
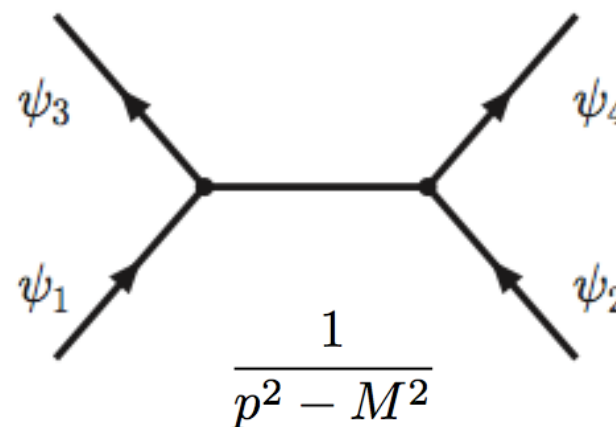
Real BSM particles

Precision and intensity frontier



Virtual BSM particles

$$\mathcal{L}_{eff} = \mathcal{L}_{SM} + \sum_{d>4} \frac{c_n^{(d)}}{\Lambda^{d-4}} \mathcal{O}^{(d)}$$



Unveil new physics



Probe energy scale otherwise unreachable



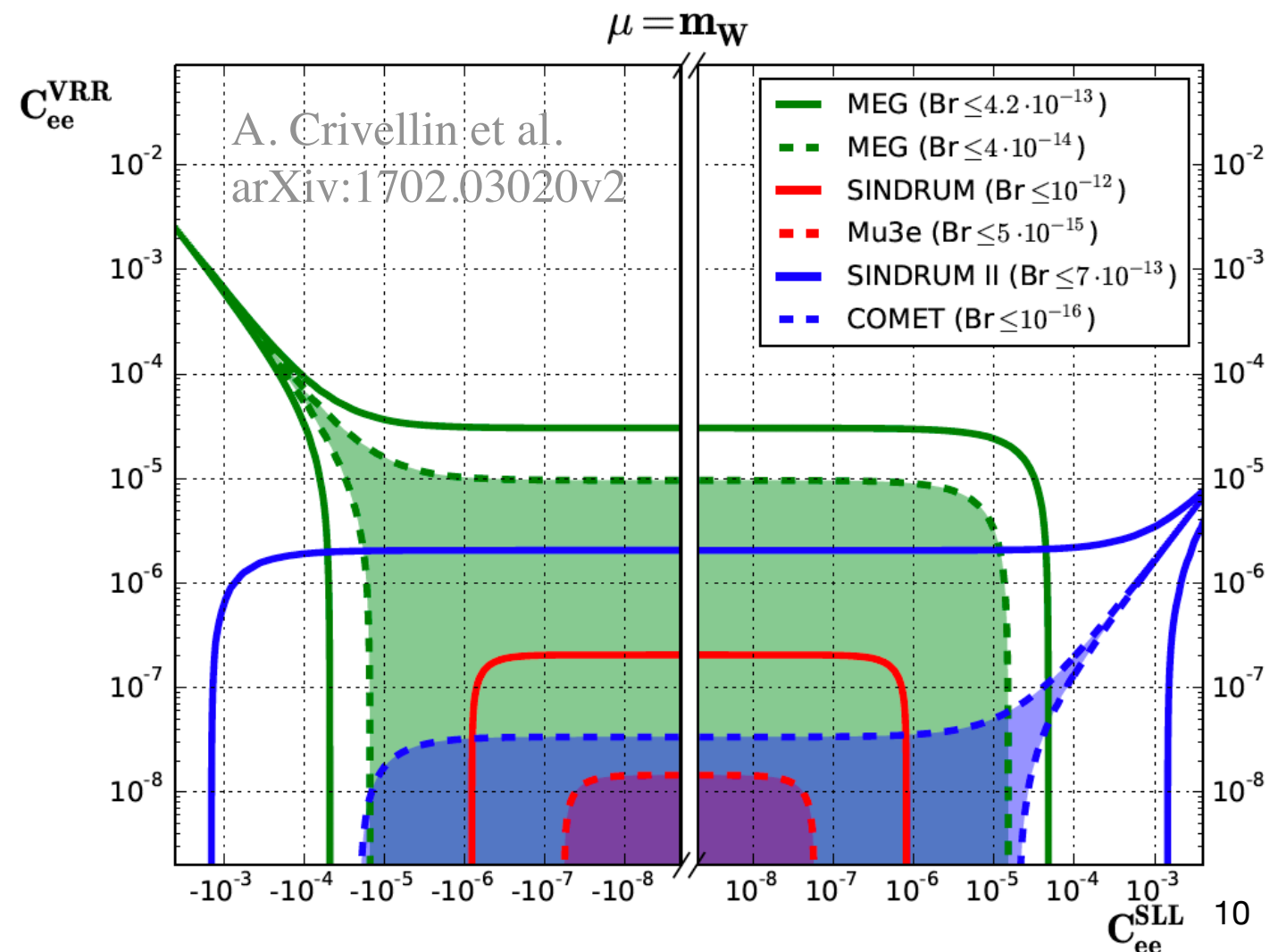
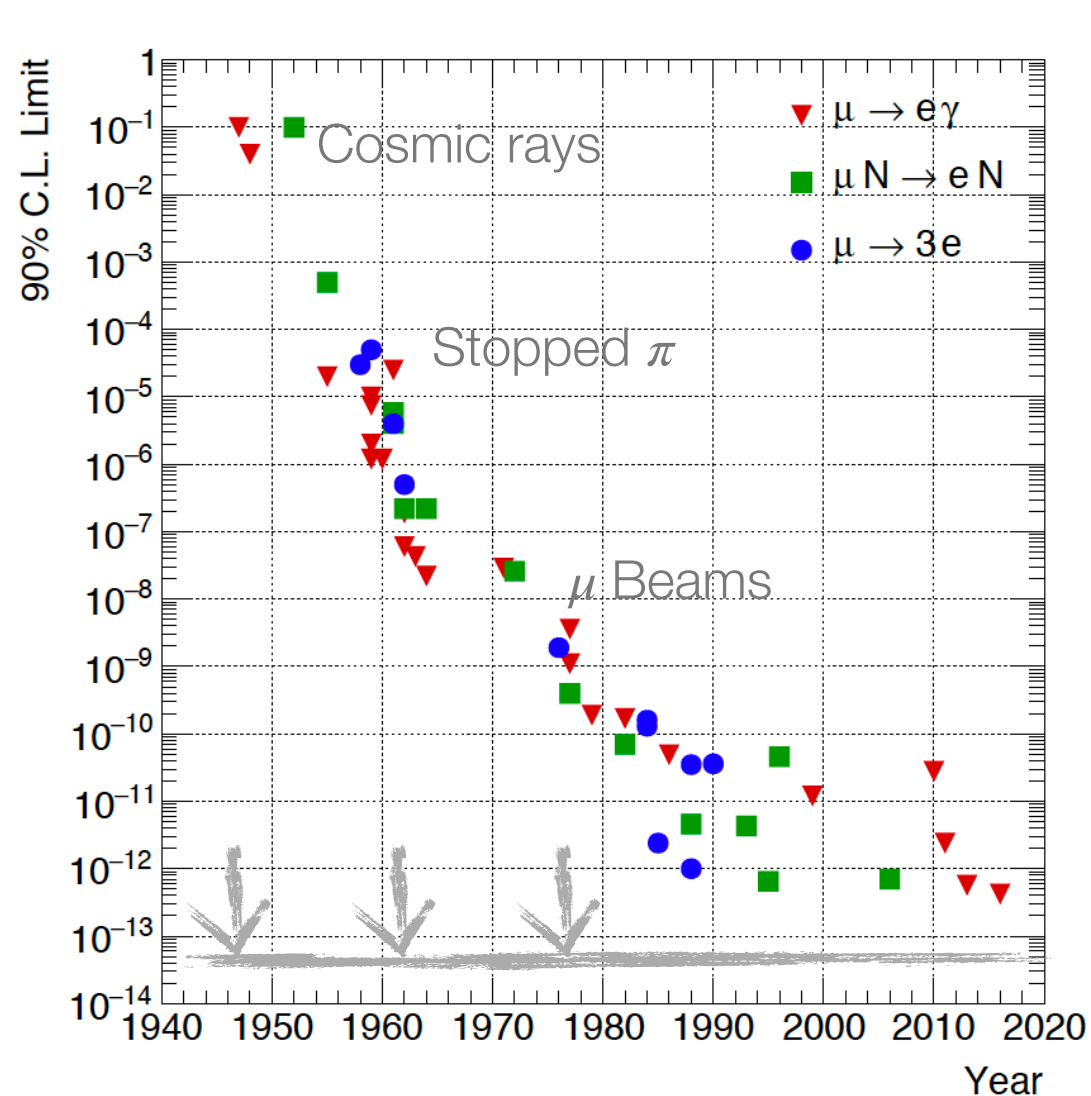
**E > 1000 TeV**

# cLFV searches with muons: Status and prospects

- In the near future impressive sensitivities:

	Current upper limit	Future sensitivity
$\mu \rightarrow e\gamma$	$4.2 \times 10^{-13}$	$\sim 4 \times 10^{-14}$
$\mu \rightarrow eee$	$1.0 \times 10^{-12}$	$\sim 1.0 \times 10^{-16}$
$\mu N \rightarrow eN'$	$7.0 \times 10^{-13}$	few $\times 10^{-17}$

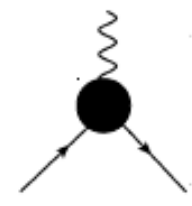
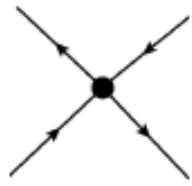
- Strong complementarities among channels: The only way to reveal the mechanism responsible for cLFV

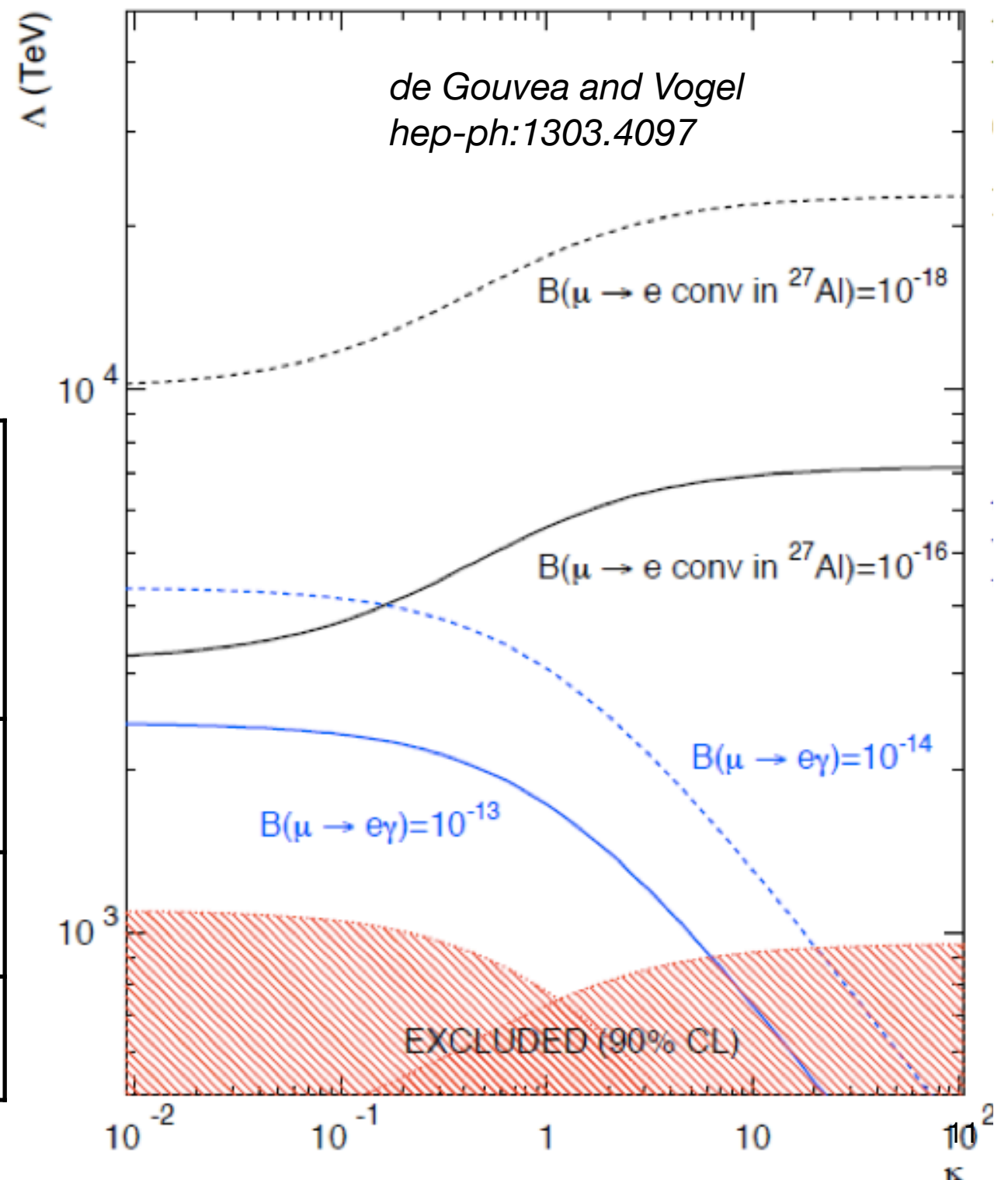


# cLFV: “Effective” lagrangian with the k-parameter

- Due to the **extremely-low** accessible **branching ratios**, muon cLFV can strongly **constrain** new physics models and scales

Model independent lagrangian

$\frac{m_\mu}{(\kappa + 1)\Lambda^2} \times$  <p>dipole term</p>	$+ \frac{\kappa}{(\kappa + 1)\Lambda^2} \times$  <p>contact term</p>
$\mu \rightarrow e\gamma$	
$\mu \rightarrow eee$	
$\mu N \rightarrow eN$	



# Outline

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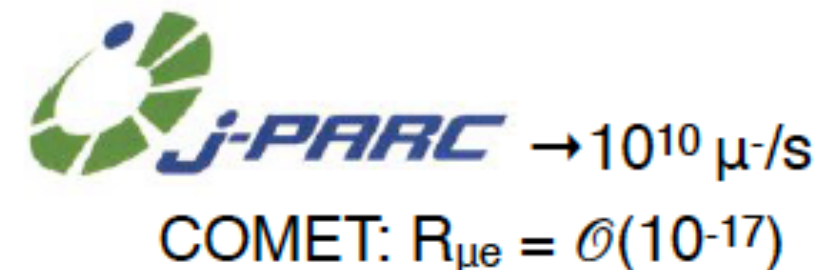
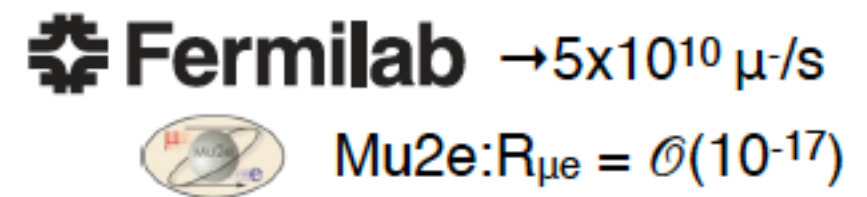
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# HiMB motivations

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- Aim:  $O(10^{10})$  muon/s; Surface (positive) muon beam ( $p = 28 \text{ MeV}/c$ ); **DC** beam
- Time schedule: **O(2025)**
- PSI delivers the highest intensity DC  $\mu^+$  beam:  
 $5 \times 10^8 \mu^+/s$
- Next generation cLFV experiments require higher muon rates
- New opportunities for future muon (particle physics) based experiments
- New opportunities for  $\mu$ SR experiments
- Different experiments demand for a variety of beam characteristics:
  - DC vs pulsed
  - Momentum depends on applications: stopped beams require low momenta
- Here focus on **DC low momenta muon beams**
- Maintain PSI leadership in DC low momentum high intensity muon beams



# Beam features vs experiment requirements

- Dedicated beam lines for high precision and high sensitive SM test/BSM probe at the world's highest beam intensities

## DC or Pulsed?

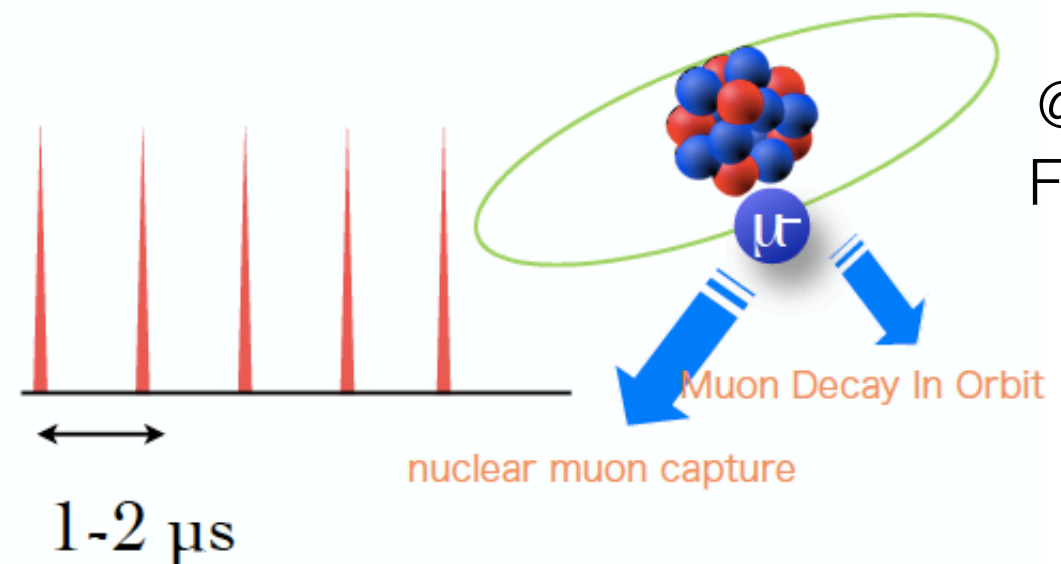
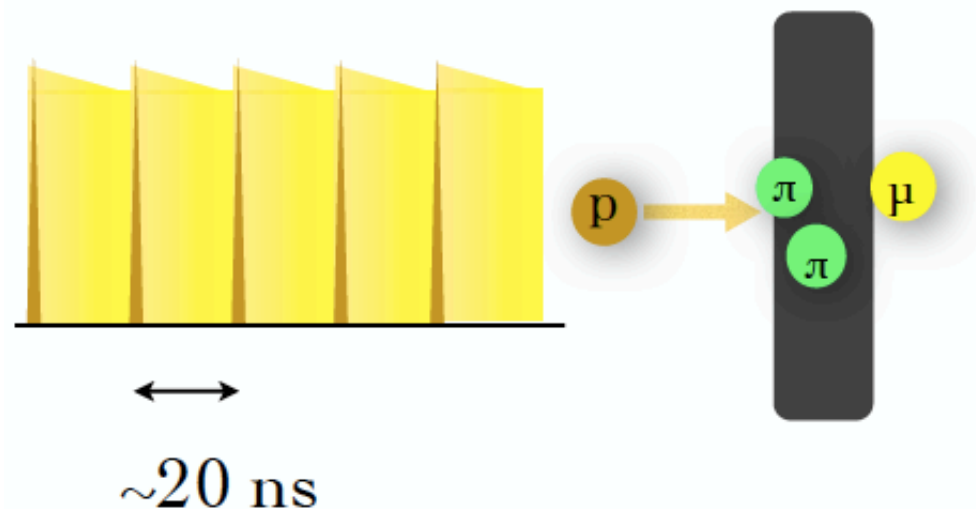
$I_{\text{beam}} \sim 10^8 - 10^{10} \mu/s$

- DC beam for coincidence experiments
- $\mu \rightarrow e \gamma, \mu \rightarrow e e e$

$I_{\text{beam}} \sim 10^{11} \mu/s$

- Pulse beam for non-coincidence experiments
- $\mu$ -e conversion

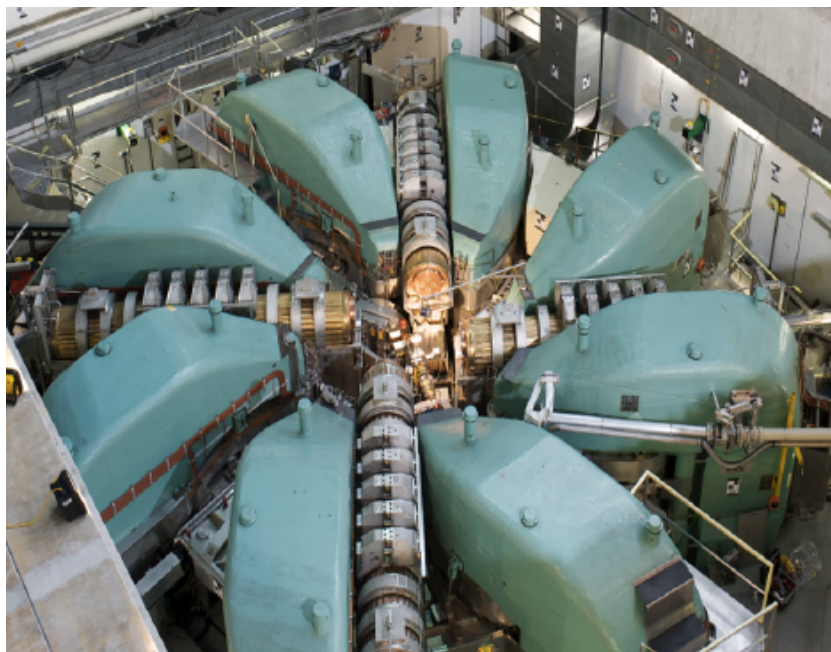
@ PSI



@ JPARC,  
FERMILAB

# The world's most intense continuous muon beam

- PSI delivers the most intense continuous low momentum muon beam in the world (**Intensity Frontiers**)
  - Intensity =  $5 \times 10^8$  muon/s, low momentum  $p = 28$  MeV/c



590 MeV proton ring cyclotron  
Time structure: 50 MHz/20 ns  
**Power: 1.4 MW**

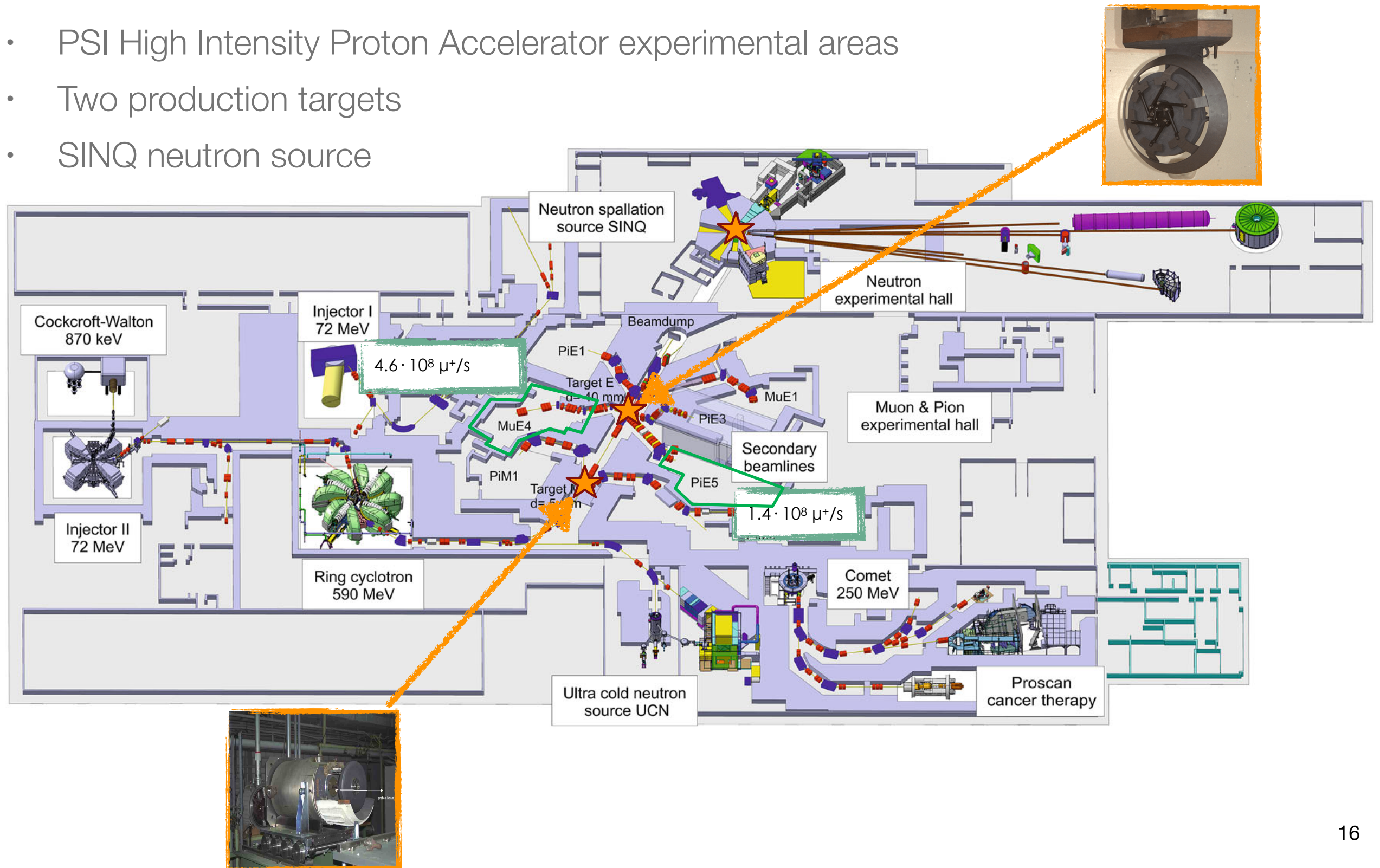
**PSI landscape**





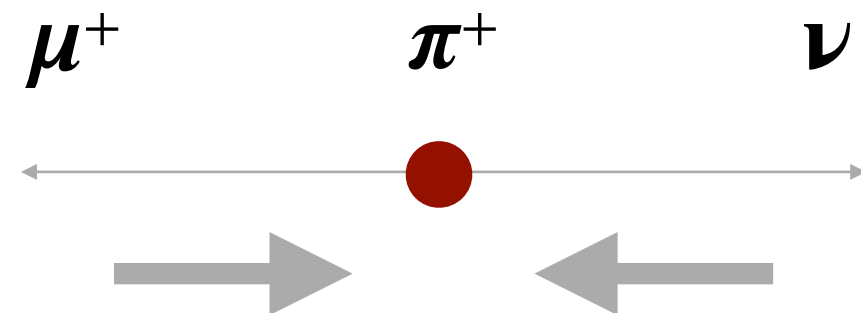
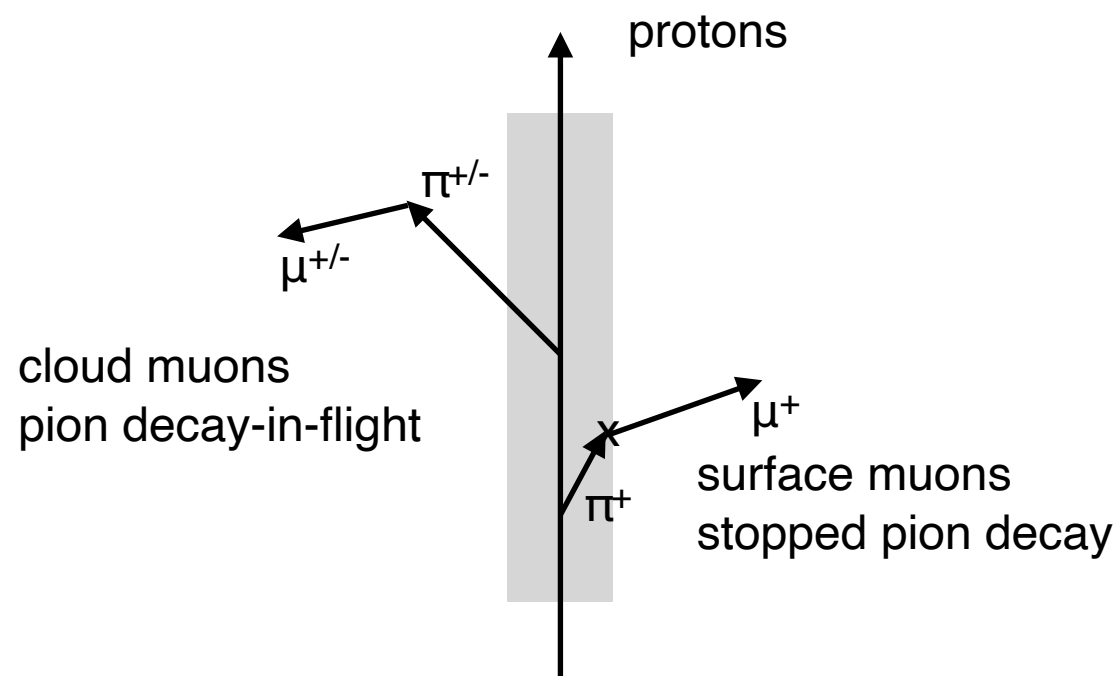
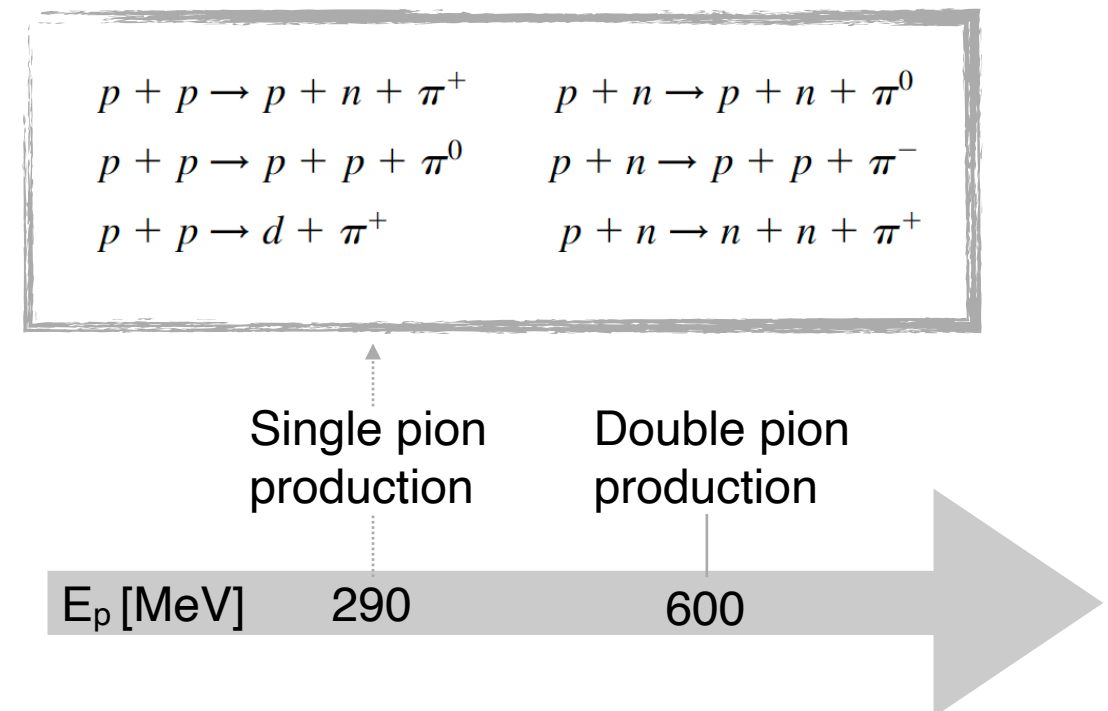
# The world's most intense continuous muon beam

- PSI High Intensity Proton Accelerator experimental areas
- Two production targets
- SINQ neutron source



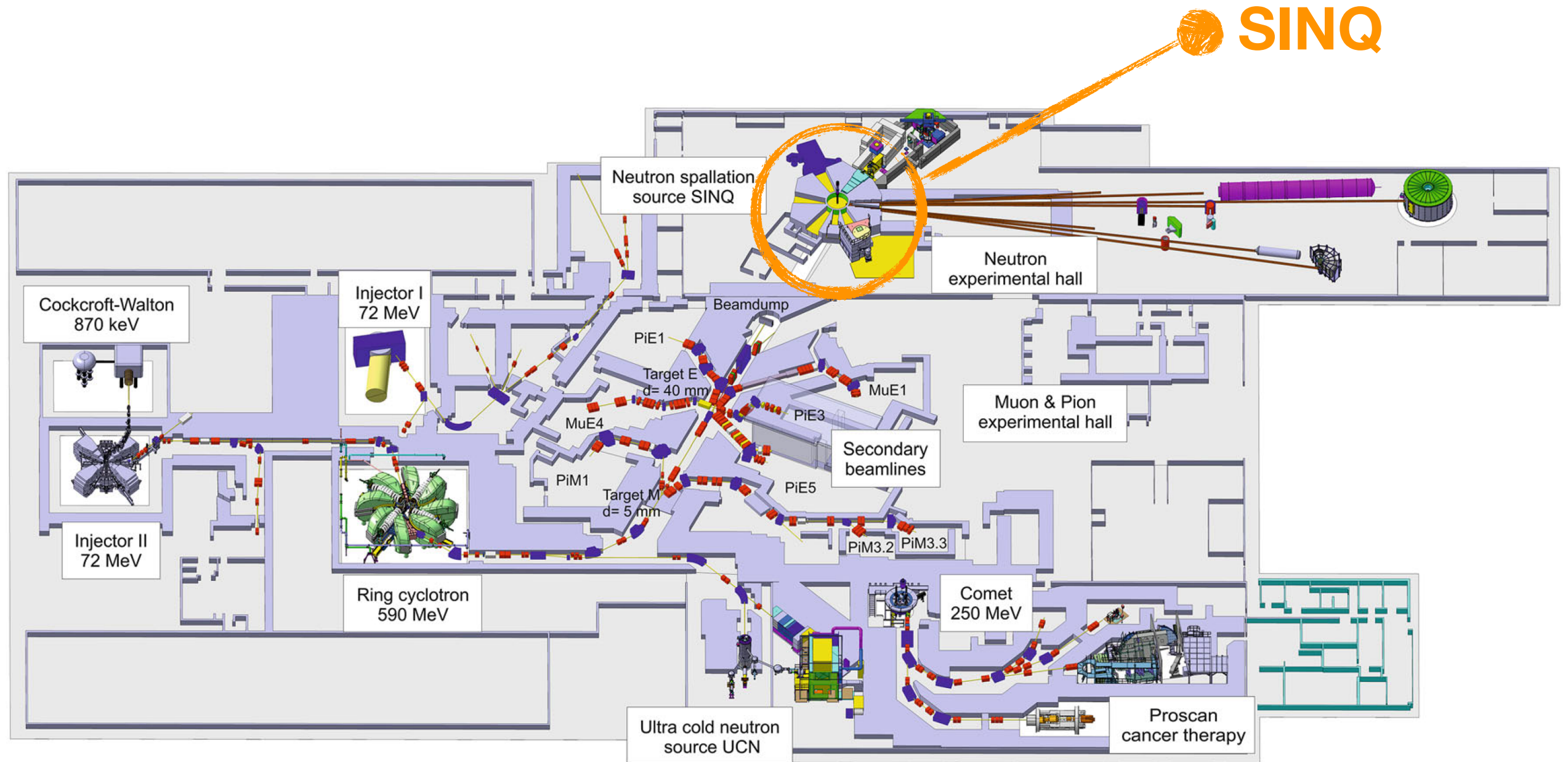
# Muon production via pion decay

- Single pion production at 290 MeV proton energy (LAB)
- Low-energy muon beam lines typically tuned to surface- $\mu^+$  at  $\sim 28 \text{ MeV}/c$
- Note: surface- $\mu \rightarrow$  polarized positively charged muons (spin antiparallel to the momentum)
- Contribution from cloud muons at similar momentum about 100x smaller
- Negative muons only available as cloud muons





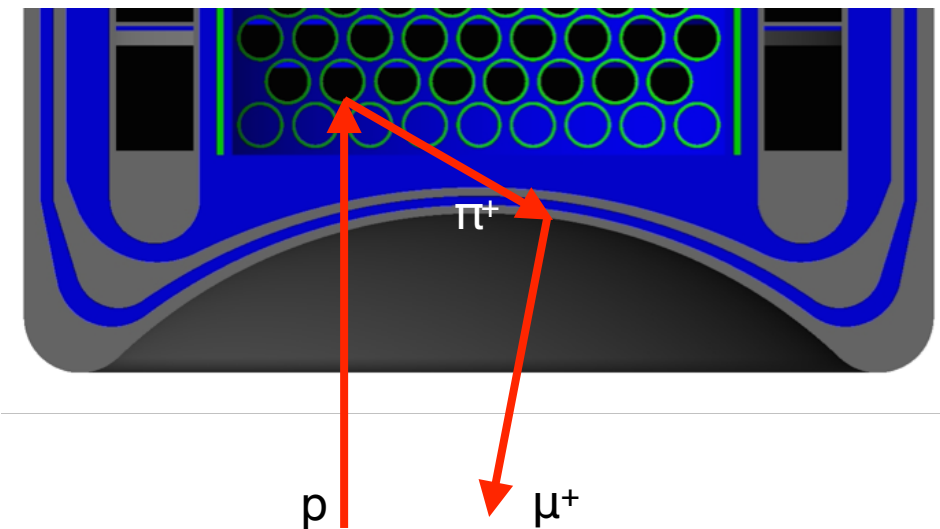
# Initial HiMB concept: @SINQ



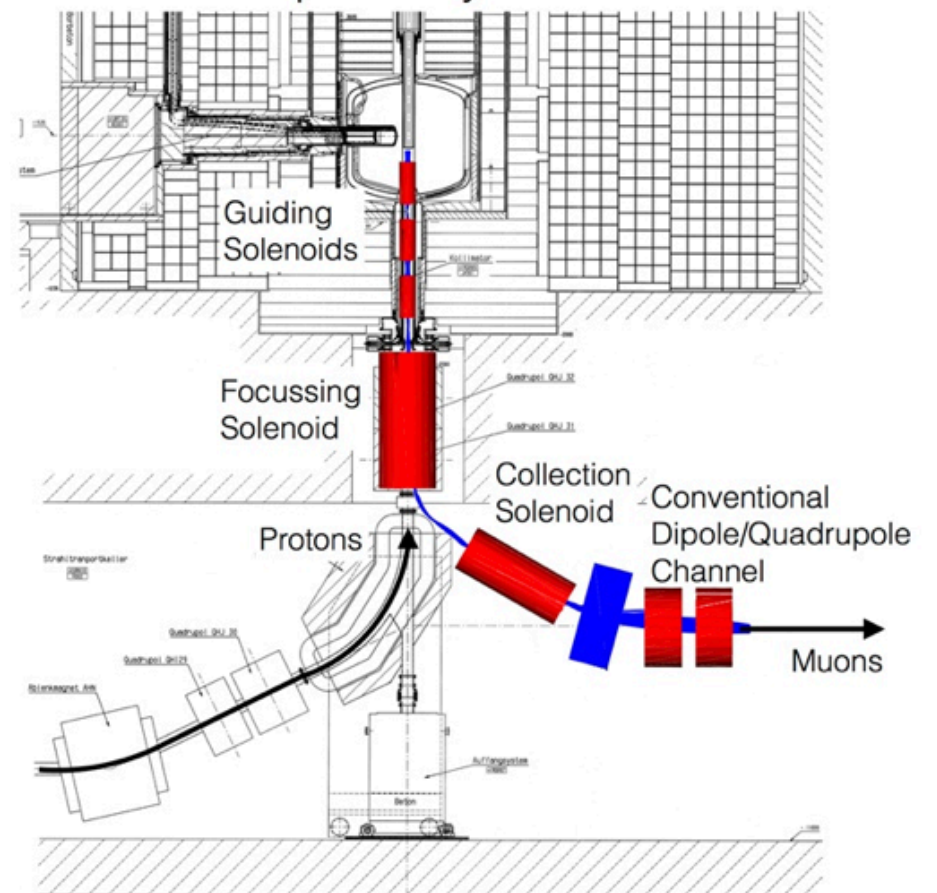
# Initial HiMB concept: @SINQ

- Source simulation (below safety window):  
 **$9 \times 10^{10}$  surface- $\mu^+$ /s @ 1.7 mA  $I_p$**
- Profit from stopping of full beam
- Residual proton beam ( $\sim 1$  MW) dumped on SINQ
- Replace existing quadrupoles with solenoids:
  - Preserve proton beam footprint
  - Capture backward travelling surface muons
- Extract muons in Dipole fringe field
- Backward travelling pions stopped in beam window
- Capturing turned out to be difficult :
  - Large phase space (divergence & 'source' extent)
  - Capture solenoid aperture needed to be increased, but constrained by moderator tank
- High radiation level close to target
- Due these constraints and after several iterations with different capturing elements:
  - **Not enough captures muons to make an high intensity beam**
  - **Alternative solution: HiMB @ EH**

SINQ spallation target

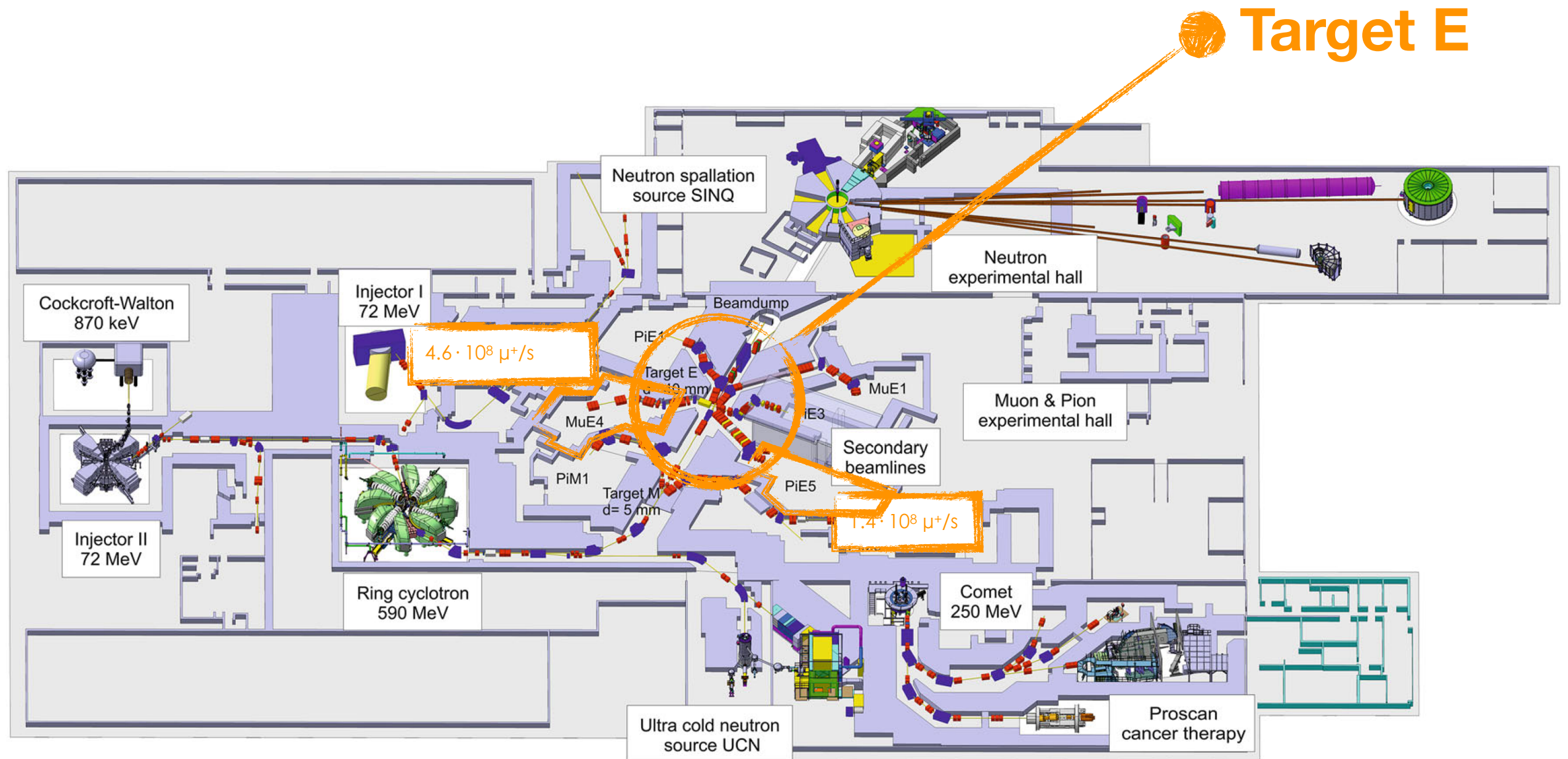


HiMB Conceptual Layout



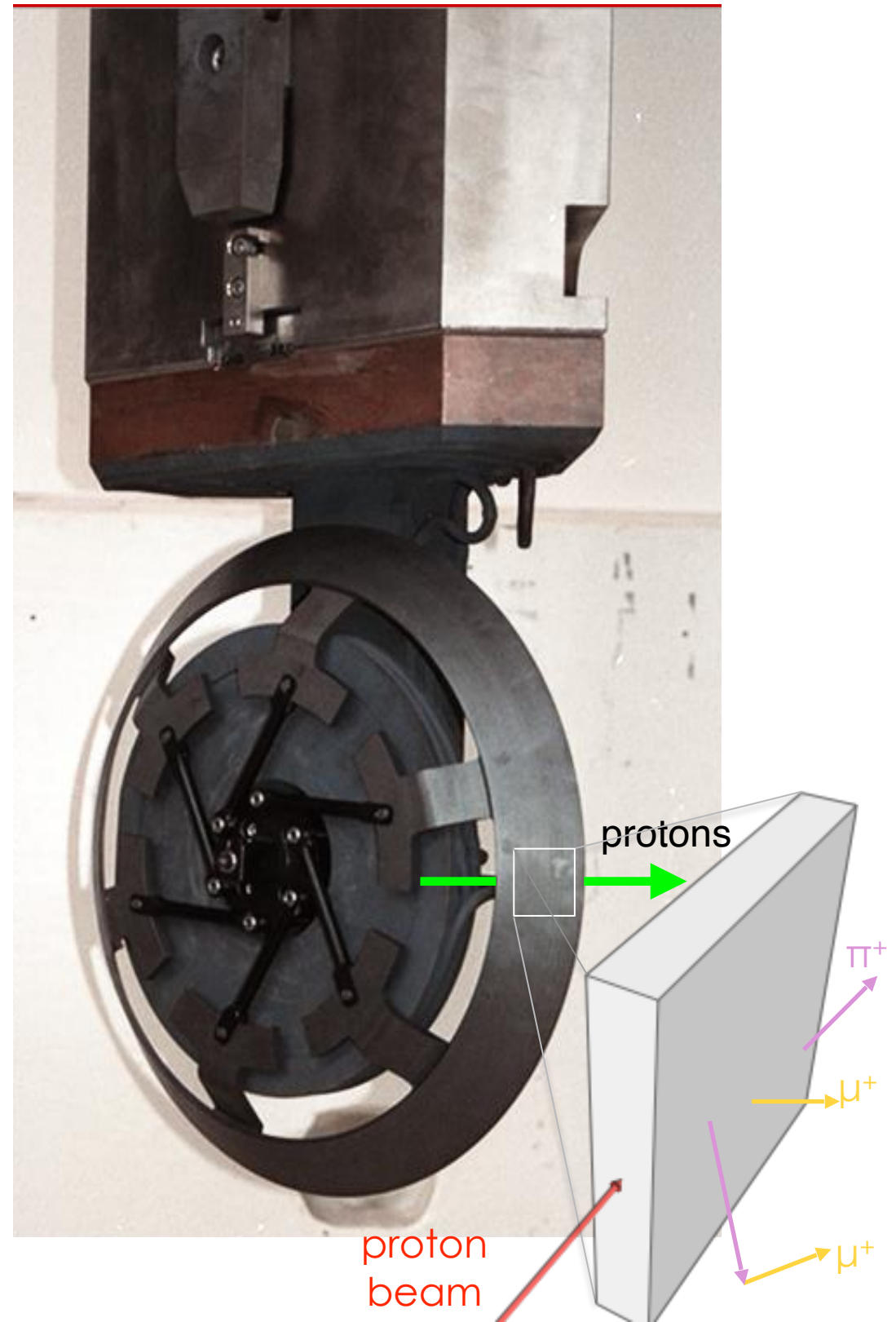


# High Muon Beam Intensity: @Main Experimental Hall



# Target E

- Rotating target (1 Hz)
- Polycrystalline graphite
- 40 mm length in beam direction
- 50 kW proton beam energy deposit
- 1700 K radiation cooled
- 30 % loss of protons
- Delivers world most intense surface muon beams



# HiMB @ HE

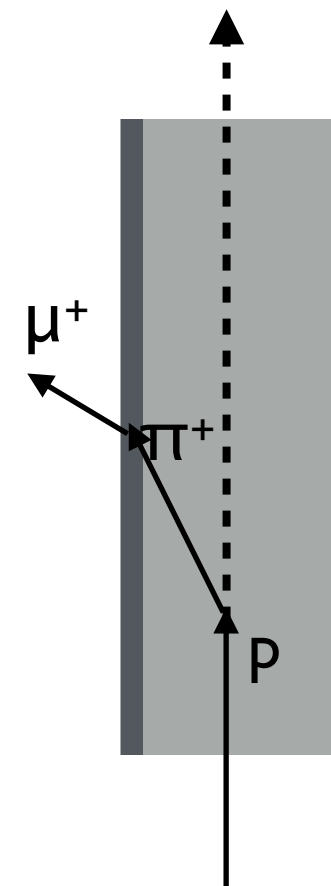
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- Back to standard target to exploit possible improvements towards high intensity beams:
  - Target
    - alternate materials
    - geometry
- Beam line
  - high capture efficiency
  - large phase space acceptance transport channel



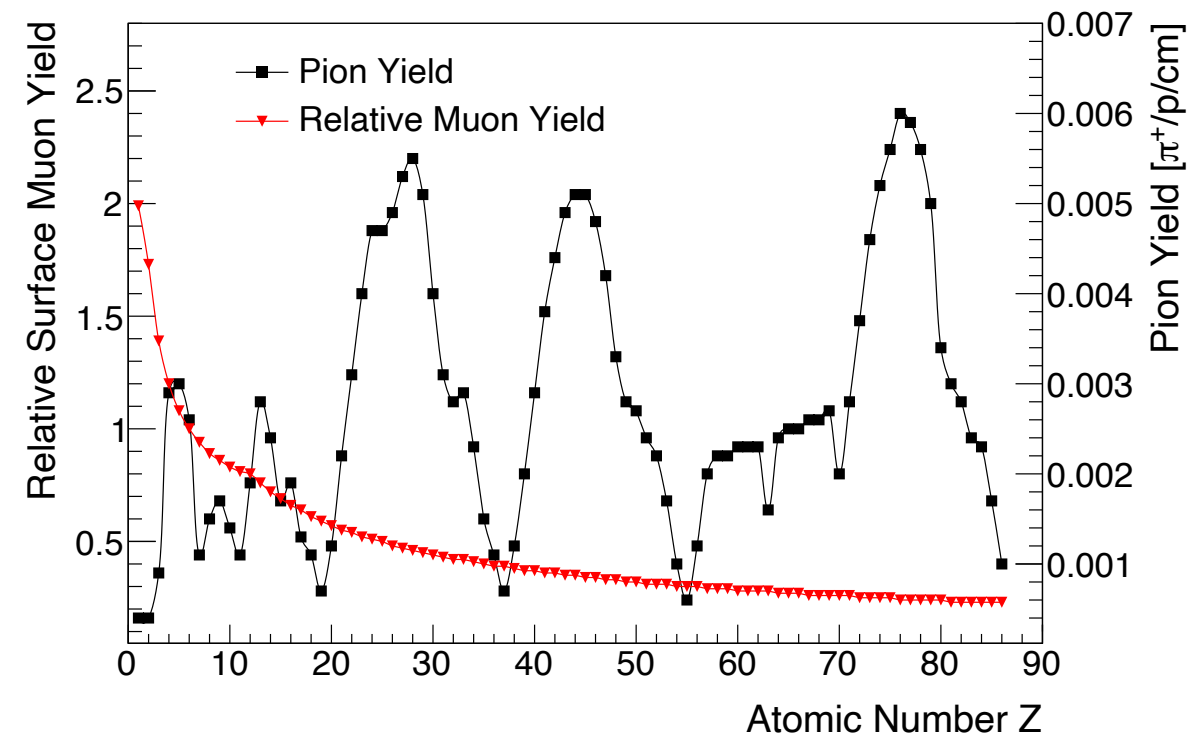
# Optimization of standard production targets

- Back to standard target to exploit possible improvements towards high intensity beams
- **Target alternate materials**
  - Search for high pion yield materials -> higher muon yield
  - Several materials have pion yields > 2x Carbon
  - Relative muon yield favours low-Z materials, but difficult to construct as a target
  - B<sub>4</sub>C and Be<sub>2</sub>C show 10-15% gain



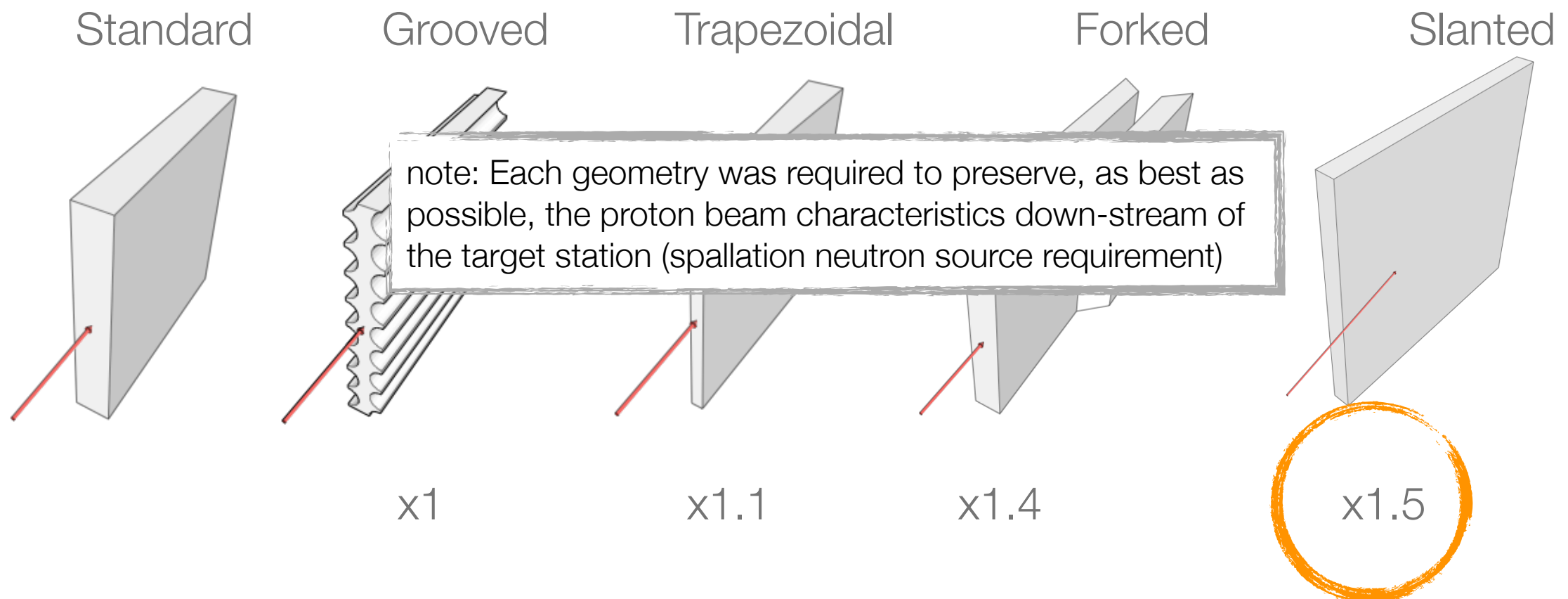
$$\text{relative } \mu^+ \text{ yield} \propto \pi^+ \text{ stop density} \cdot \mu^+ \text{ Range} \cdot \text{length}$$

$$\begin{aligned} &\propto n \cdot \sigma_{\pi^+} \cdot SP_{\pi^+} \cdot \frac{1}{SP_{\mu^+}} \cdot \frac{\rho_c(6/12)_c}{\rho_x(Z/A)_x} \\ &\propto Z^{1/3} \cdot Z \cdot \left(\frac{1}{Z}\right) \cdot \left(\frac{1}{Z}\right) \\ &\propto \frac{1}{Z^{2/3}} \end{aligned}$$



# Optimization of standard production targets

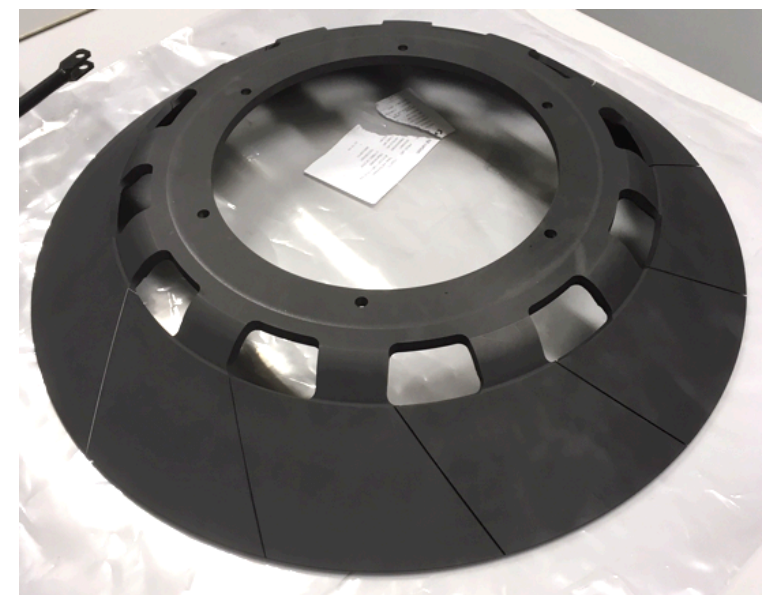
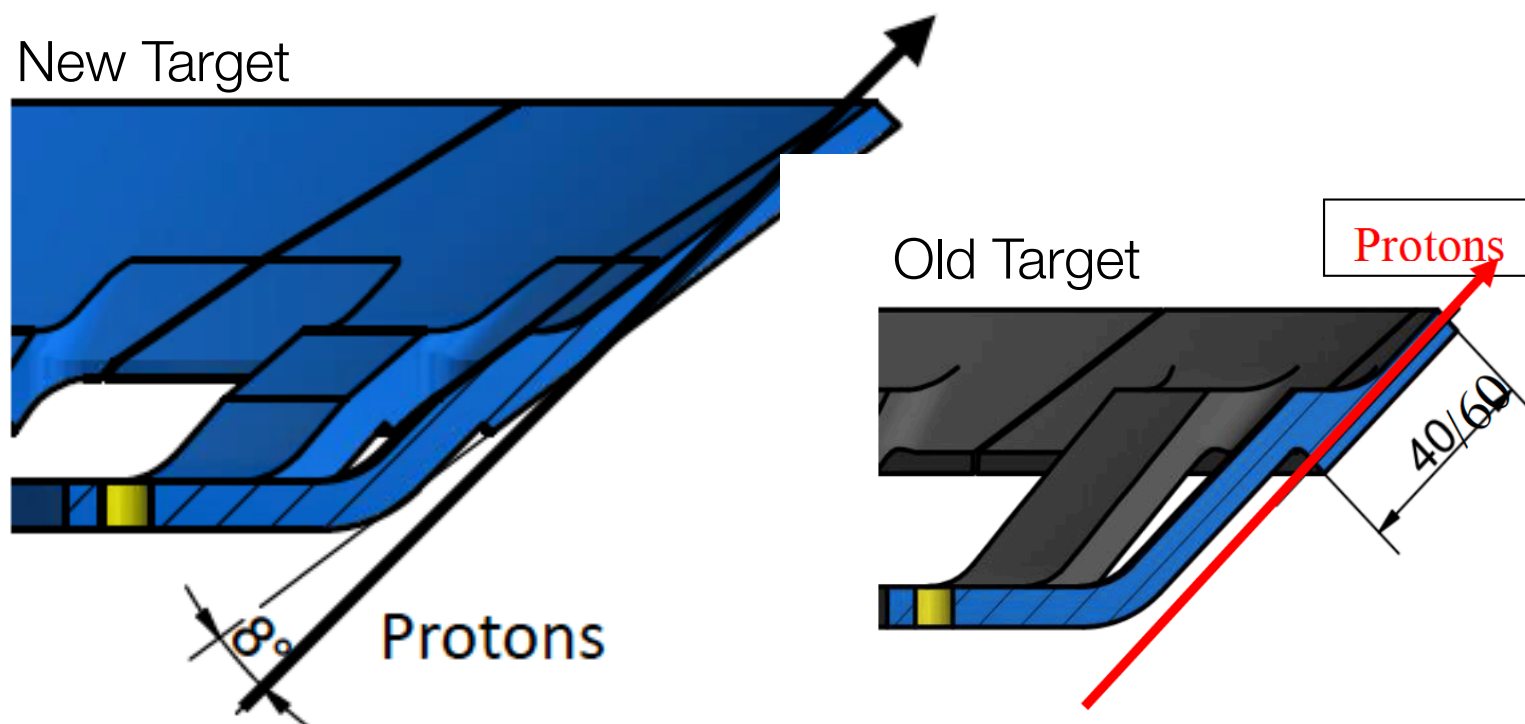
- Strategy: either increasing the surface volume (surface area times acceptance depth) or the pion stop density near the surface
- **Target geometry**
  - Comparison studies of different target geometries: **Different shapes and rotation angles**
  - Enhancements normalised to standard target



# Slanted target: towards the test

Prototype for the New Target E

- Upgrade existing graphite production target E 40 mm
  - 8° slanting angle: Measurement in forward / backward / sideways direction
  - Production and implementation feasible
  - Mechanical and thermal simulations completed and no show-stopper found
  - **Installed in week 48 (Nov. 25th, 2019)**
- **Goals**
  - **Increase surface muon rates for all connected beam lines**
  - **Increase safety margin for “missing” target with the proton beam**

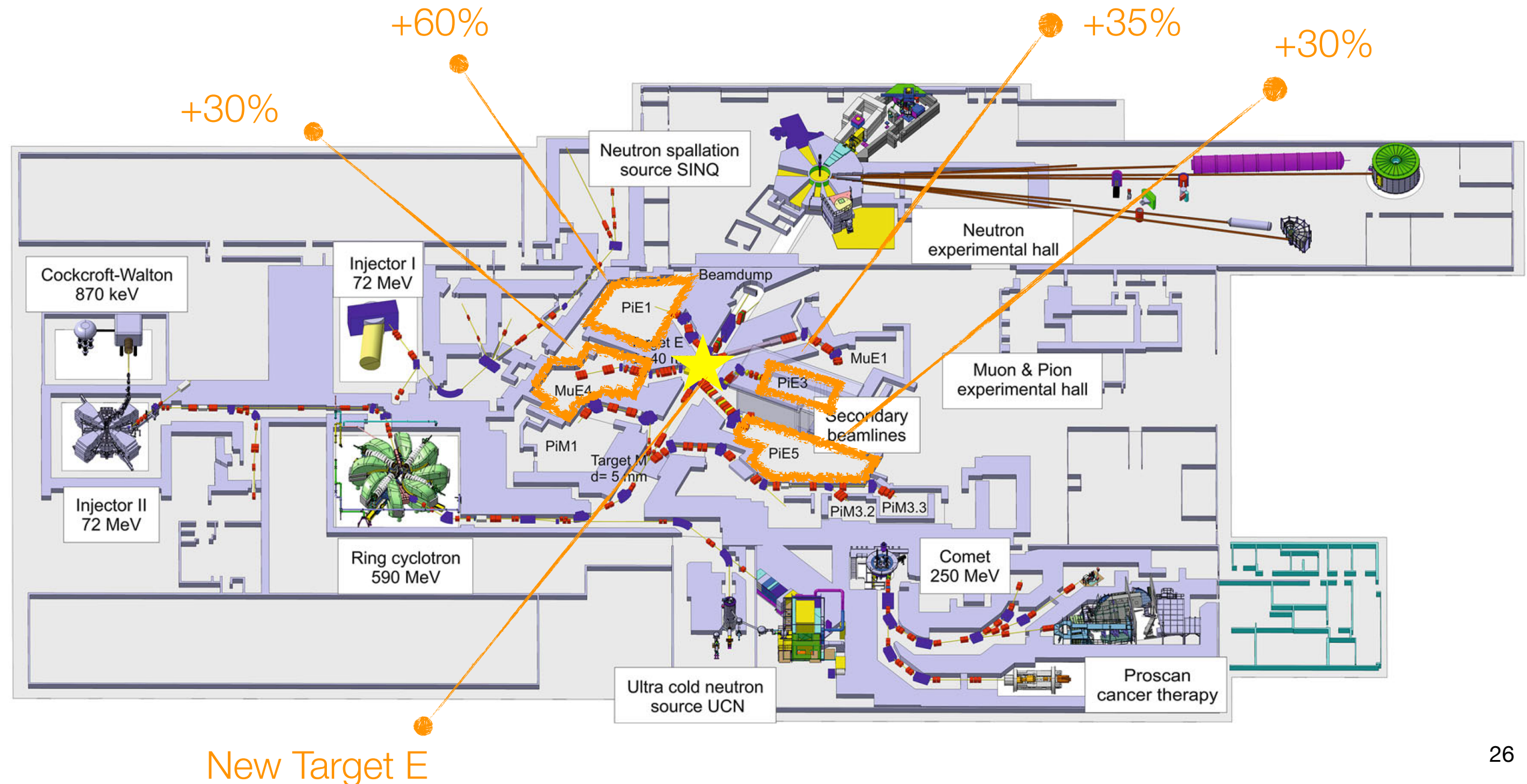


New Target E



# Slanted target: 2019 test Results

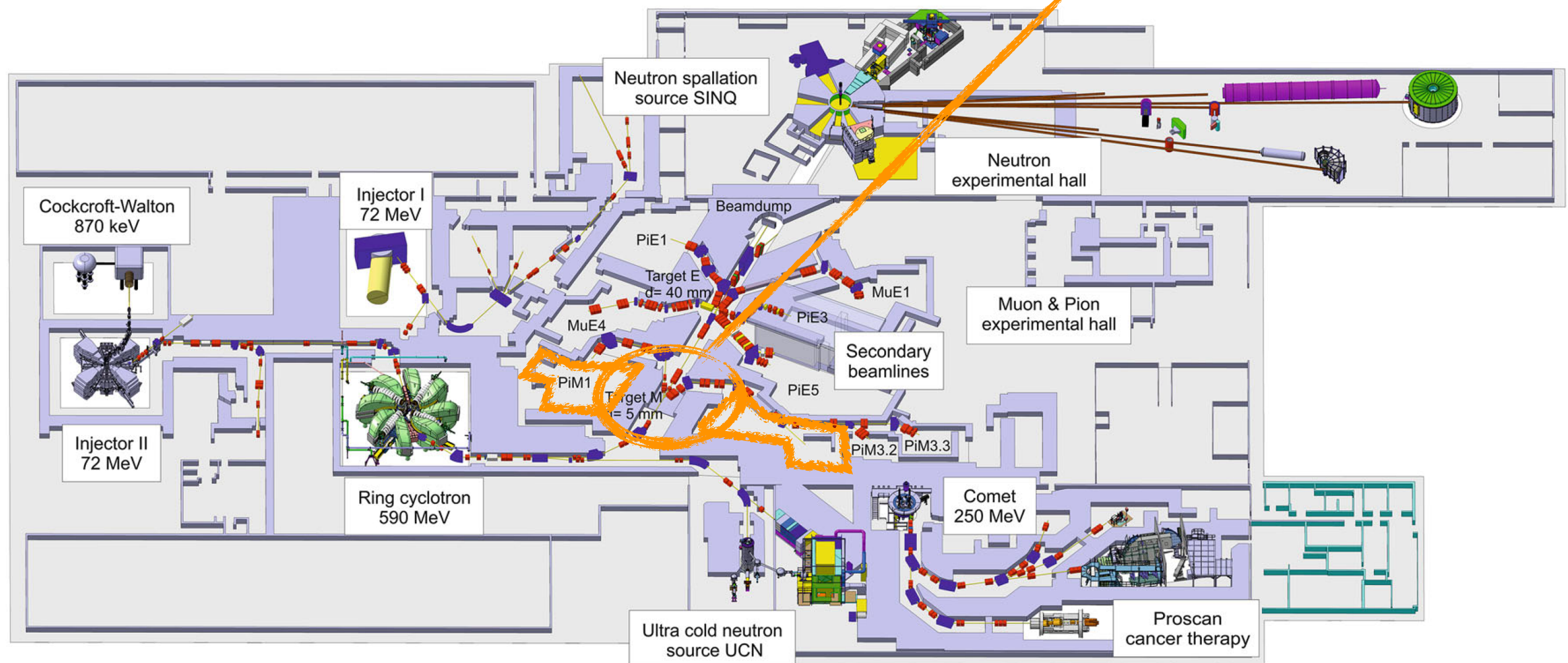
- Expect ~30-60 % enhancement
- Measurements successfully done in different experimental areas in fall 2019
- Analysis still undergoing: **increased muon yield CONFIRMED!**
- To be seen: **impact of higher thermal stress on long term stability of target wheel**



# Towards the HiMB project @ PSI

- Final position for the HiMB target: "Present" TgM location
- $\sim 90^\circ$  extraction to existing experimental areas
- Large phase space acceptance solenoidal channel

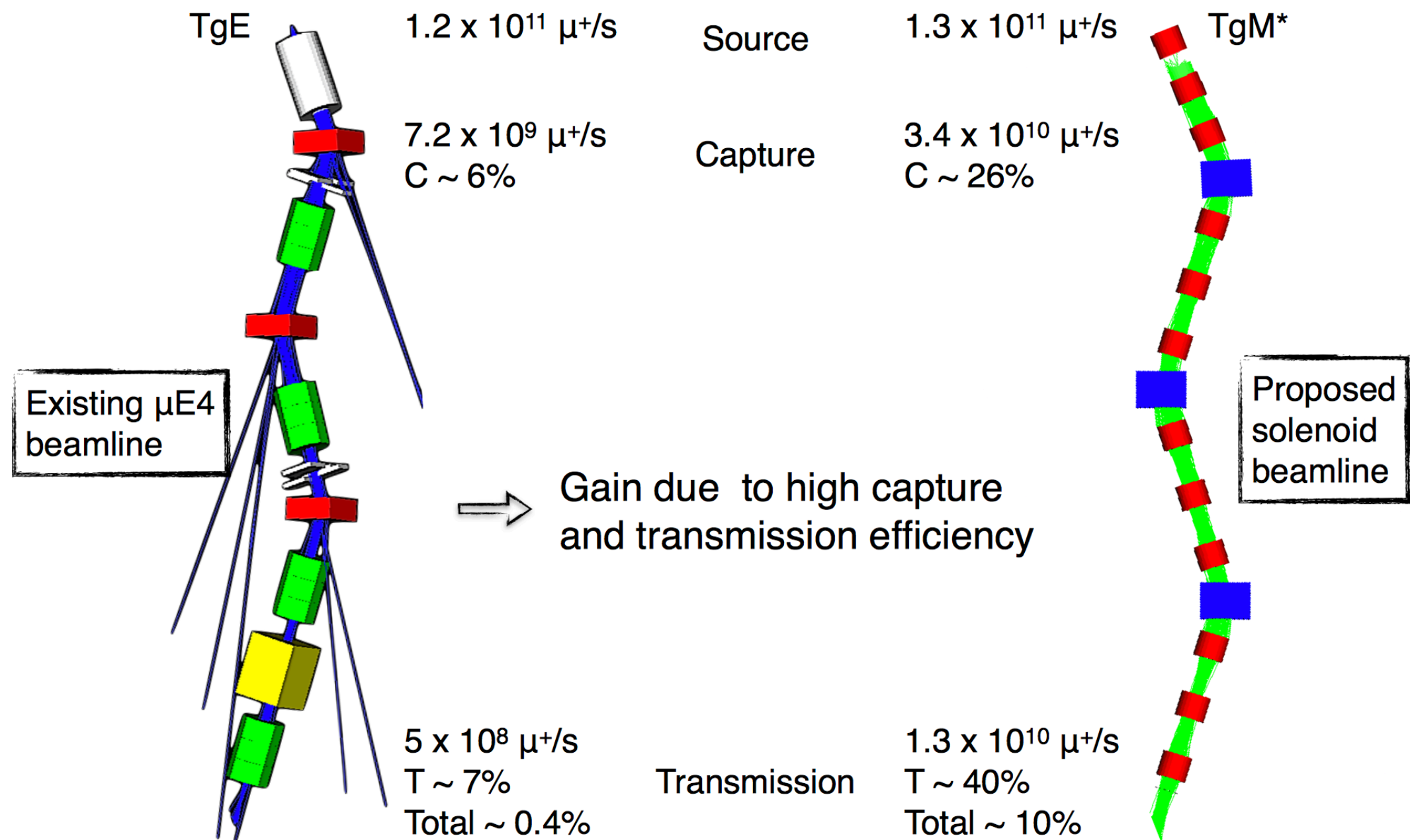
**Target M**





# Prospects

- Aim:  $O(10^{10})$  muon/s; Surface (positive) muon beam ( $p = 28 \text{ MeV/c}$ ); **DC** beam
- Time schedule: **O(2025)**



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# The muCool project at PSI

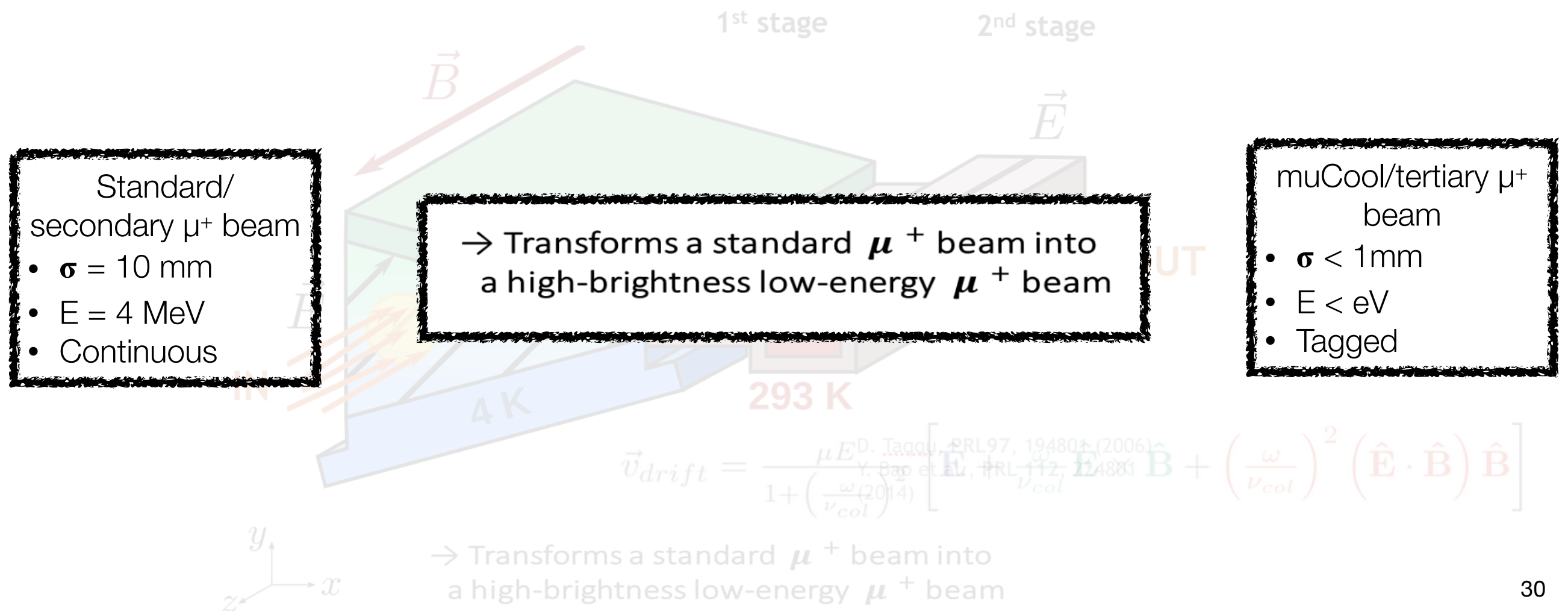
- Aim: High-brightness low energy muon beam
- Phase space reduction based on: dissipative energy loss in matter (He gas) and position dependent drift of muon swarm
- Increase in brightness by a factor  $10^{10}$  with an efficiency of  $10^{-3}$

for:

$\mu$ SR (solid state physics)

muonium (spectroscopy, gravitational interaction...)

muon experiments ( $\mu$ EDM, g-2...)



# The muCool project at PSI

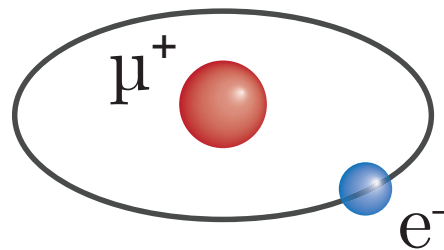
- Aim: low energy high-brightness muon beam
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for:

**$\mu$ SR (solid state physics)**

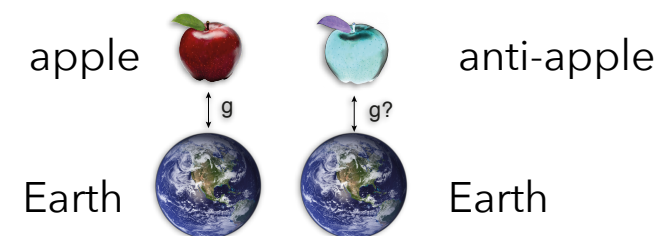
**muonium (spectroscopy, gravitational interaction...)**

**muon experiments ( $\mu$ EDM, g-2...)**



- ▶ hydrogen-like exotic atom
- ▶ pure leptonic system (1st and 2nd gen.)
- ▶ no finite size / nuclear effects
- ▶ ... but, short lifetime  $\sim 2.2$   $\mu$ s
- ▶ **Precision spectroscopy**: test of bound-state QED, fundamental constants:  $m_\mu$ ,  $R_\infty$ ,  $m_\mu/m_p$ ,  $q_\mu/q_e$  ...

## Muonium gravity experiment?



test of weak equivalence principle on  $\mu^+$  :

- ▶ **elementary** antiparticle
- ▶ second generation lepton

# The muCool project at PSI

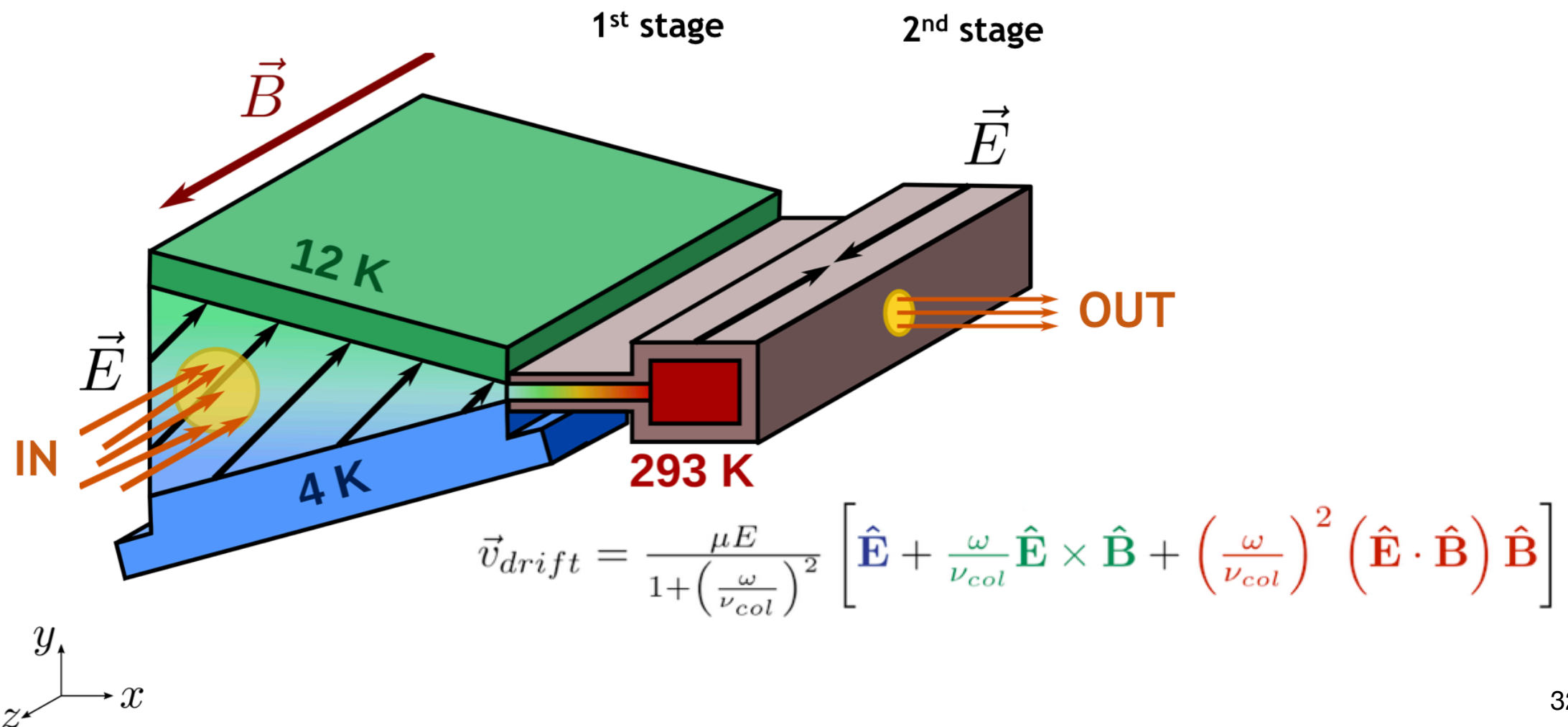
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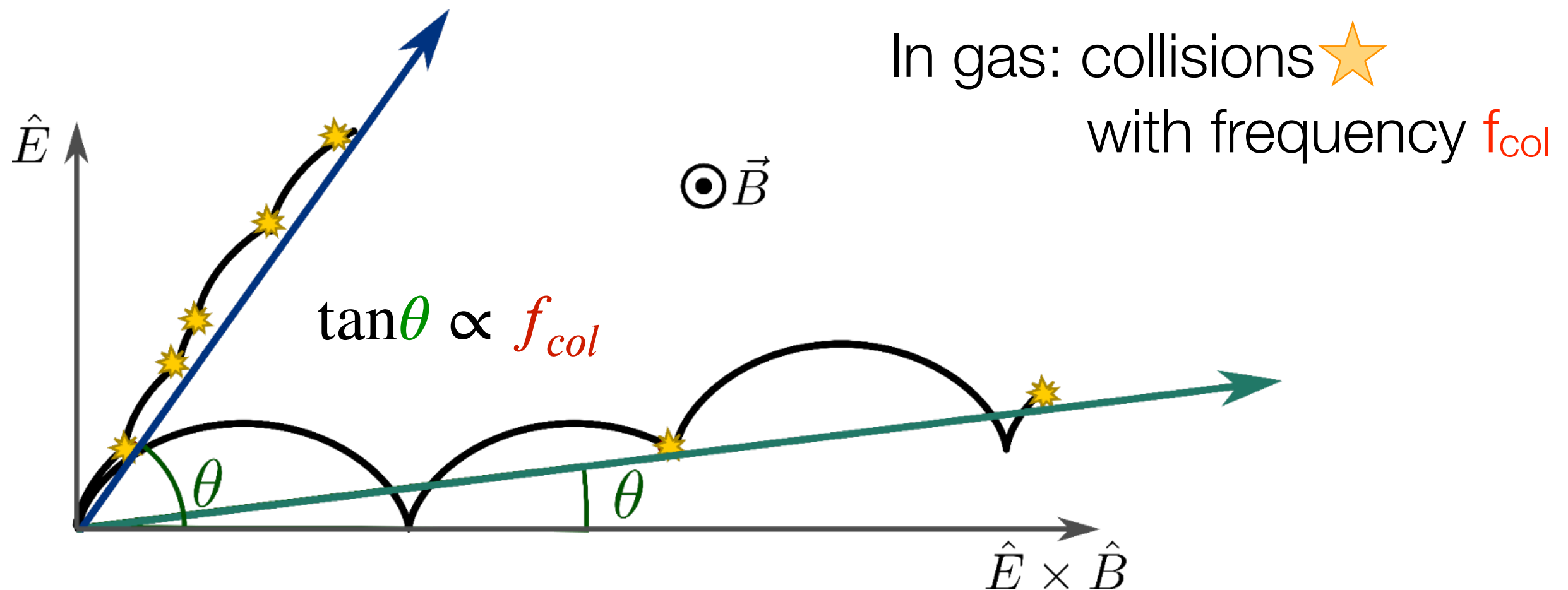
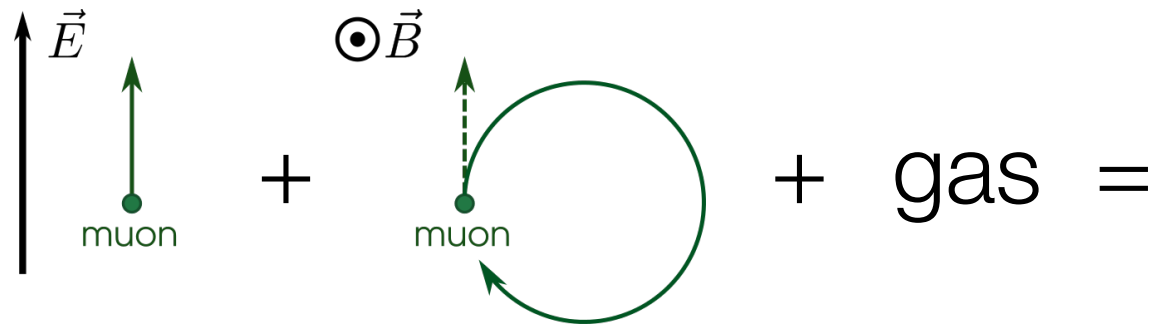
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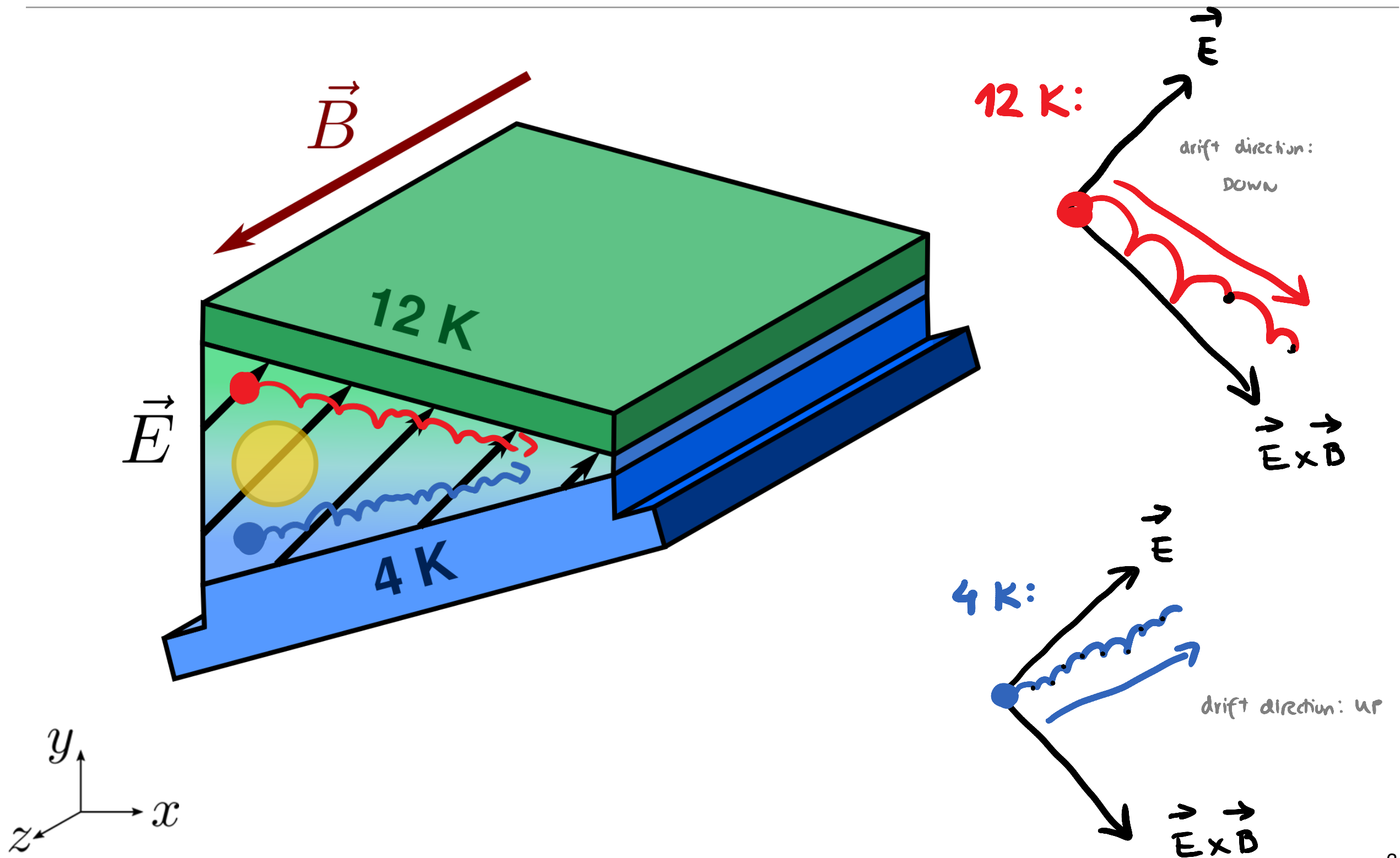




# Trajectories in E and B field + gas

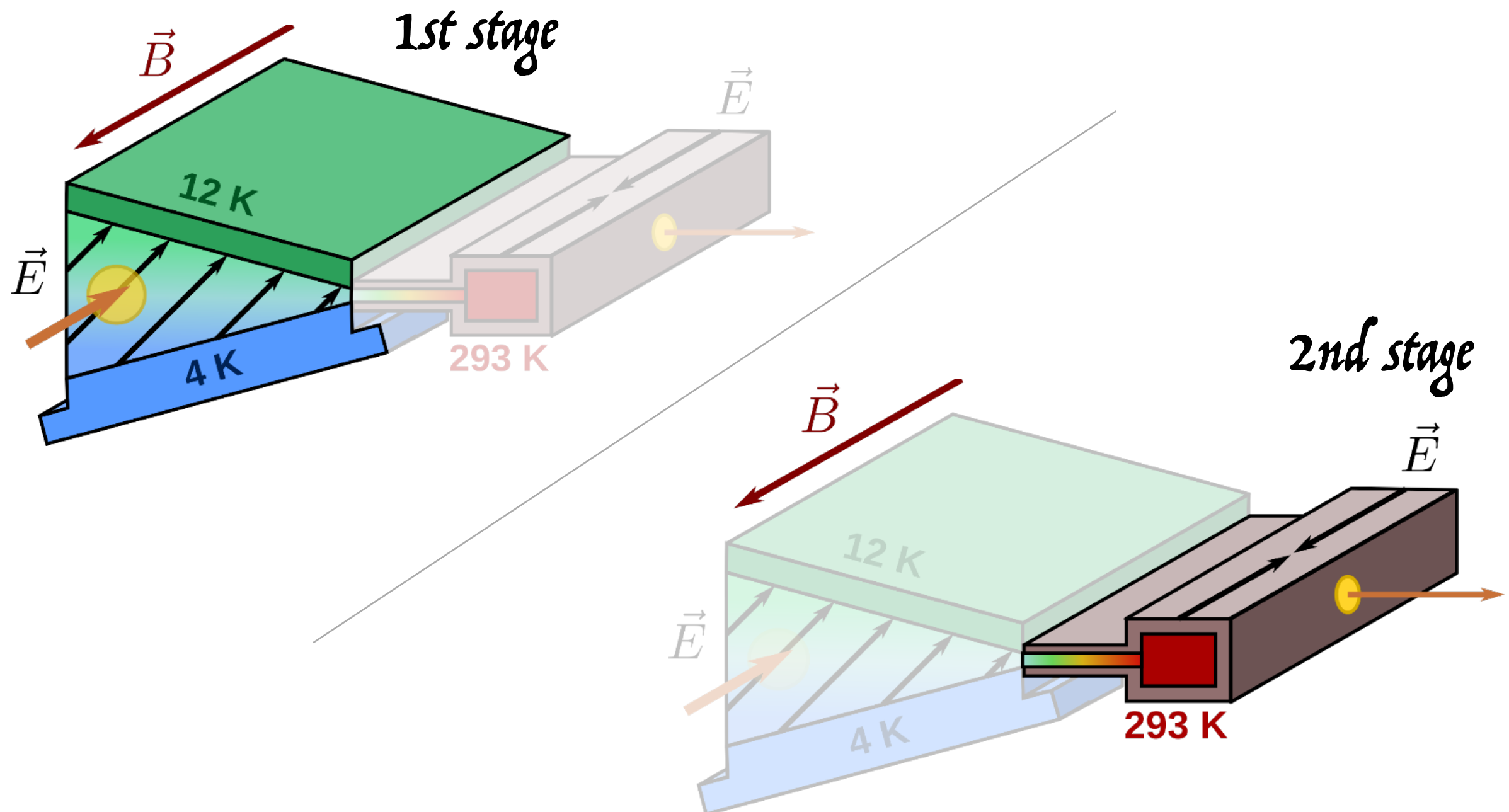


# Working principle: 1st Stage



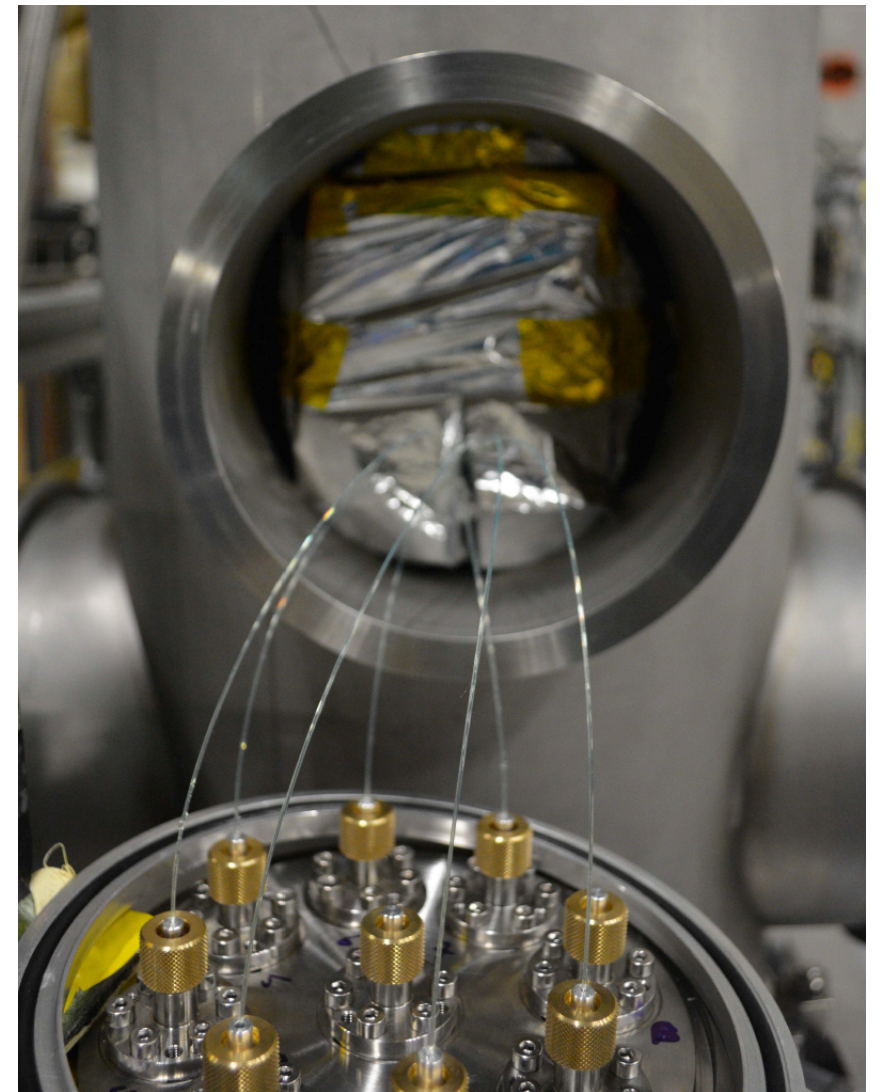
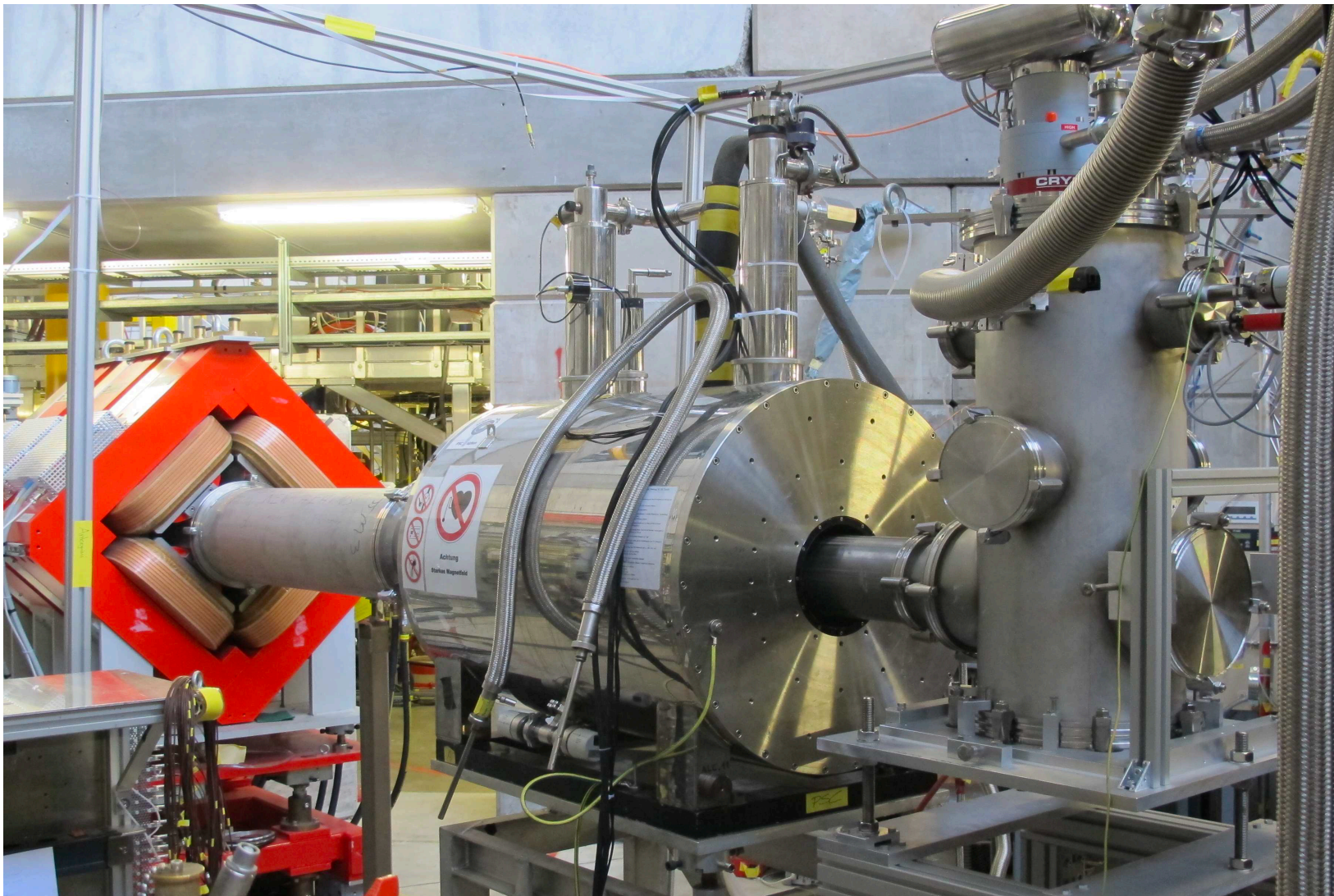
# Experimental setup and results: 1st stage and 2 stage

- Separately longitudinal and transverse compression: **PROVED**
- **Very good agreement between data and simulations**





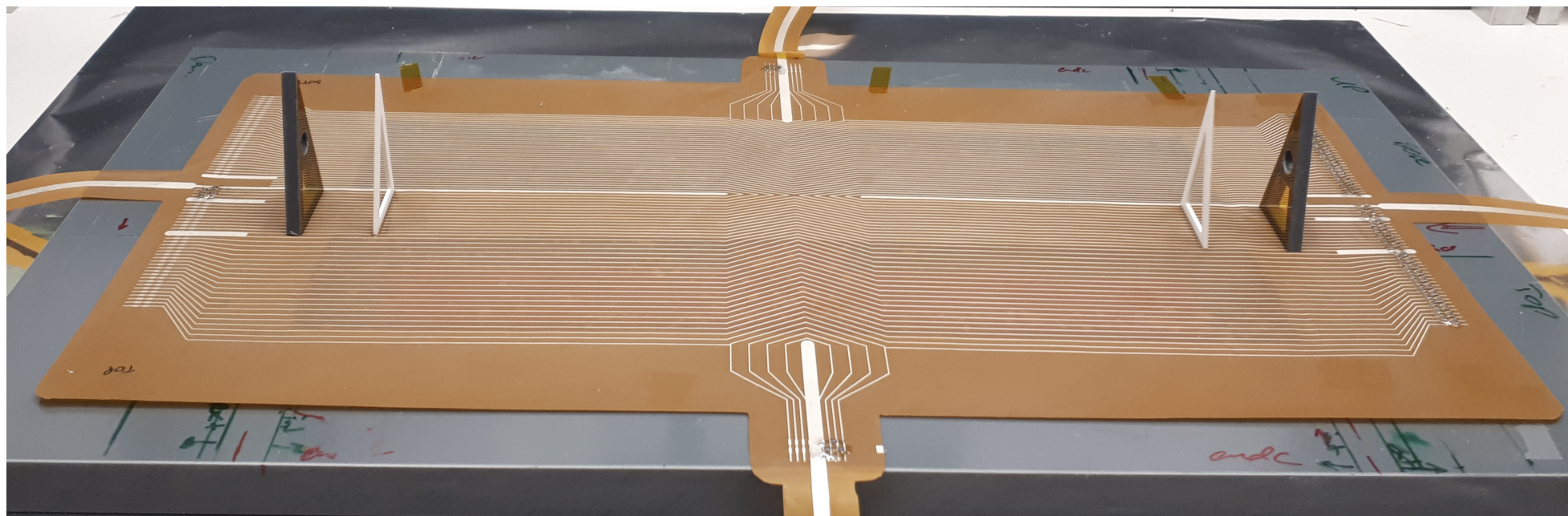
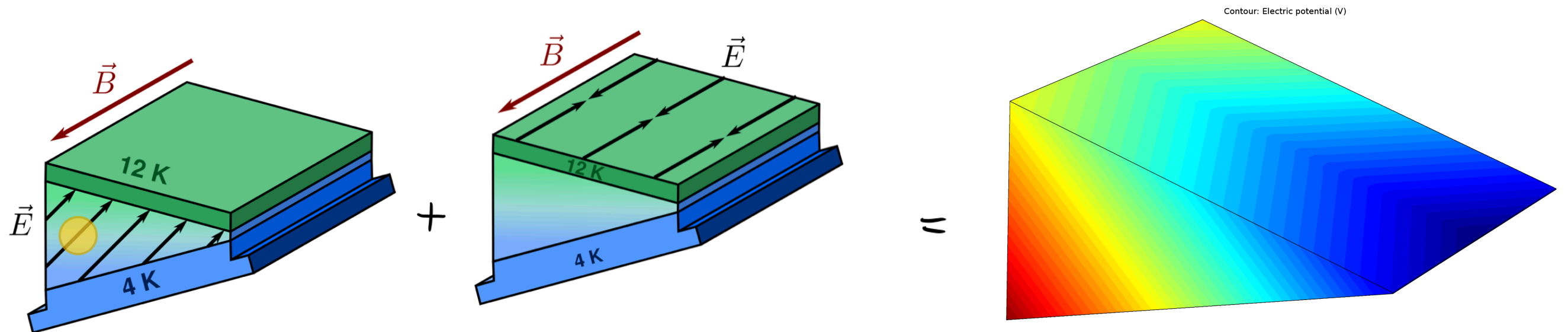
# Experimental setup and results: 1st stage





# The muCool project at PSI: Status

- 1st stage + 2nd stage
- **Next Step:** Extraction into vacuum





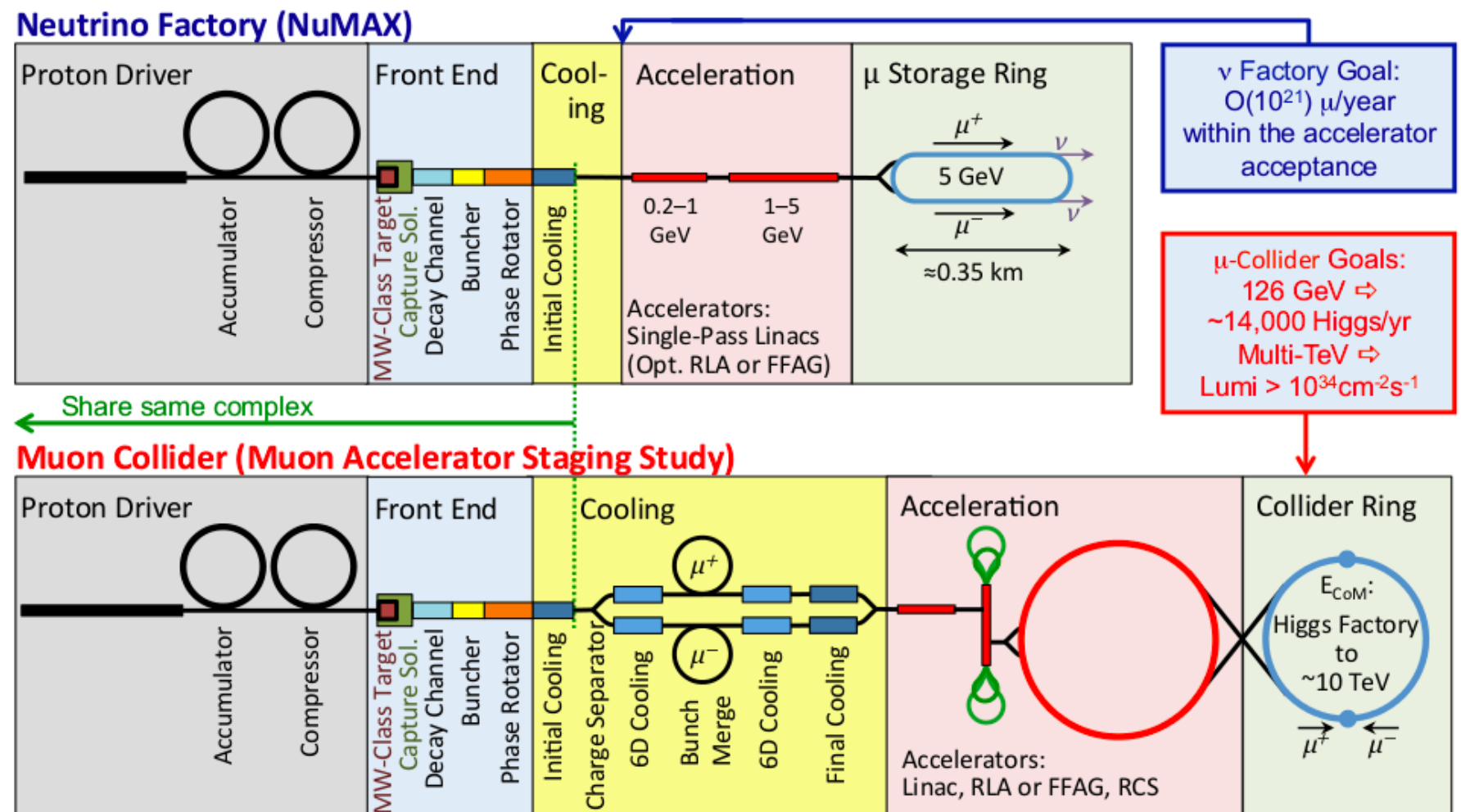
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# Muon Collider & Neutrino Factory (very short intro!)

- Neutrino factory is also a muon factory and viceversa
- In both facilities:
  - High power protons
  - Target  $\rightarrow$  pions
  - Capture  $\rightarrow$  **muons**
  - **Cooling**
  - Rapid acceleration
  - Storage ring



## Challenges:

- Muon beam: **tertiary** ( $p \rightarrow \pi \rightarrow \mu$ ) and **unstable** (muon life time  $\sim 2.2 \mu\text{s}$ )
  - Use high power proton driver
  - Use fast cooling (ionisation cooling  $\rightarrow$  MICE)
  - Develop rapid accelerators

# What is Muon Ionization cooling? (MICE)

- Energy loss in the absorbers reduces  $p_L$  and  $p_T$
- Scattering **heats** the beam
- RF cavity restore  $p_L$  only
- The net effect is the reduction of the beam emittance: **cooling**
  - Strong focusing, low-Z absorber material and high RF cavity are required



$$\frac{d\epsilon_n}{ds} \sim -\frac{1}{\beta^2} \left\langle \frac{dE_\mu}{ds} \right\rangle \frac{\epsilon_n}{E_\mu} + \frac{1}{\beta^3} \frac{\beta_\perp (0.014 \text{ GeV})^2}{2E_\mu m_\mu L_R}$$

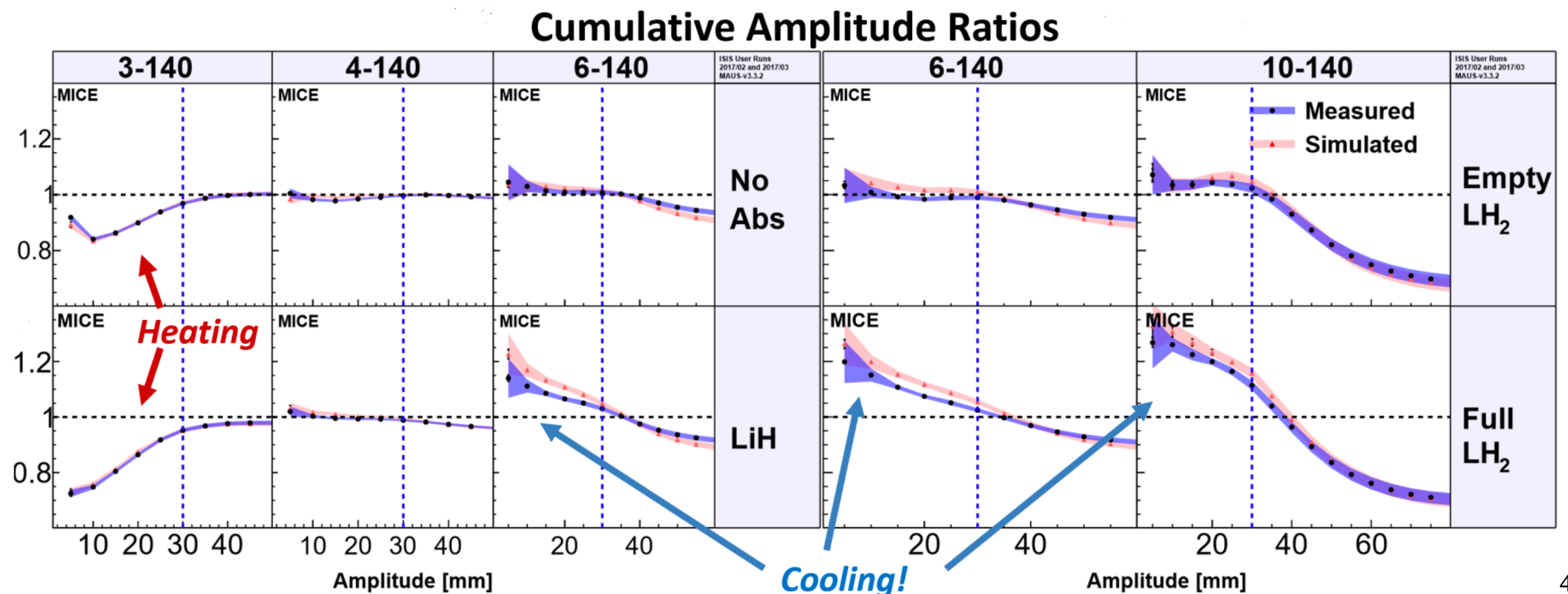
Cooling

Heating

$d\epsilon_n/ds$  is the rate of change of normalised-emittance within the absorber;  
 $\beta$ ,  $E_\mu$  and  $m_\mu$  the muon velocity, energy, and mass, respectively;  
 $\beta_\perp$  is the lattice betatron function at the absorber;  
 $L_R$  is the radiation length of the absorber material.

# MICE results

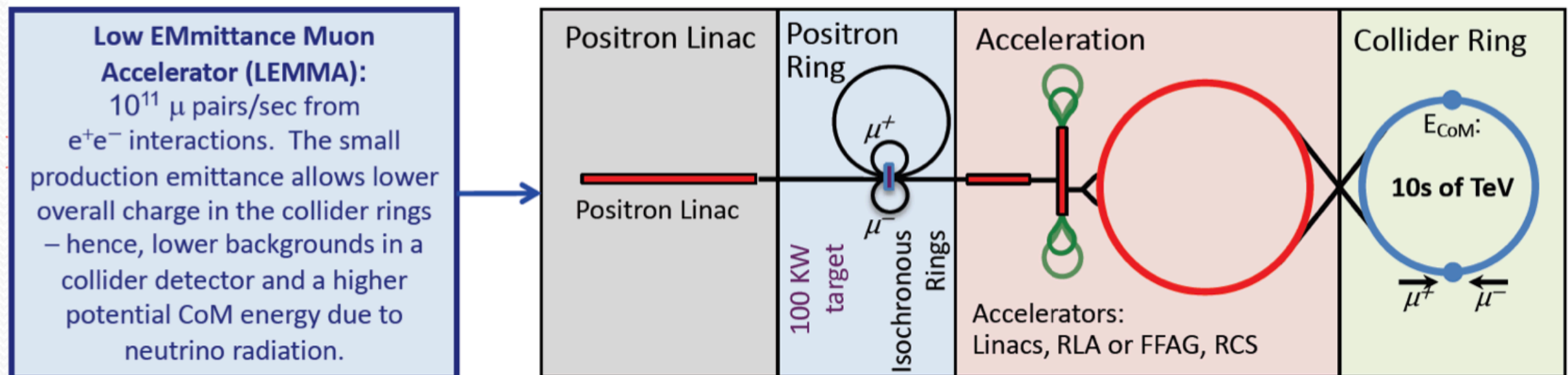
- Muon cooling is last “in principle” challenge for muon collider and neutrino factory R&D.
- MICE:
  - measured the underlying physics processes that govern cooling
  - made an unprecedented single particle measurement of the particle trajectories in an accelerator lattice
  - first observation of ionisation cooling





# LEMMA concept

- LEMMA: Low EMittance Muon Accelerator
- Positron driver muon source
- Muons produced from  $e^- e^+ \rightarrow \mu^- \mu^+$ 
  - 45 GeV positron beam impinging on a target ( $e^-$  at rest)
  - $\mu^- \mu^+$  produced @ ~22 GeV with low transverse emittance with  $\gamma(\mu) \approx 200$  and  $\mu$  laboratory **lifetime** of about **500  $\mu\text{s}$**
  - Aimed at obtaining high luminosity with relatively small  $\mu^\pm$  fluxes thus reducing background rates and activation problems due to high energy  $\mu^\pm$  decays



# European Strategy

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From the deliberation document of the European Strategy Update:

## High-priority future initiatives

[..]In addition to the high field magnets the accelerator R&D roadmap could contain:

[..] an international design study for a muon collider, as it represents a unique opportunity to achieve a multi-TeV energy domain beyond the reach of  $e^+e^-$ -colliders, and potentially within a more compact circular tunnel than for a hadron collider. The biggest challenge remains to produce an intense beam of cooled muons, **but novel ideas are being explored**;

For the European Strategy the Laboratory Directors Group (LDG) established a muon collider working group to provide input on the muon collider

- LDG represents: CERN, DESY, INFN, STFC, IRFU (CEA), CIEMAT, NIKHEF, LNGS, IJCLab(CNRS), PSI
- Proposed to the European Strategy Process to form an international collaboration to study the muon collider

Open questions - We have asked ourself about (discussion just started):

Can muCool&HiMB contribute on this program?

Can a low energy high-brightness negative muon beam be produced?

What about a muon collider/accelerator concept based on low energy high-brightness muon beams subsequently re-accelerated?

# Outlook

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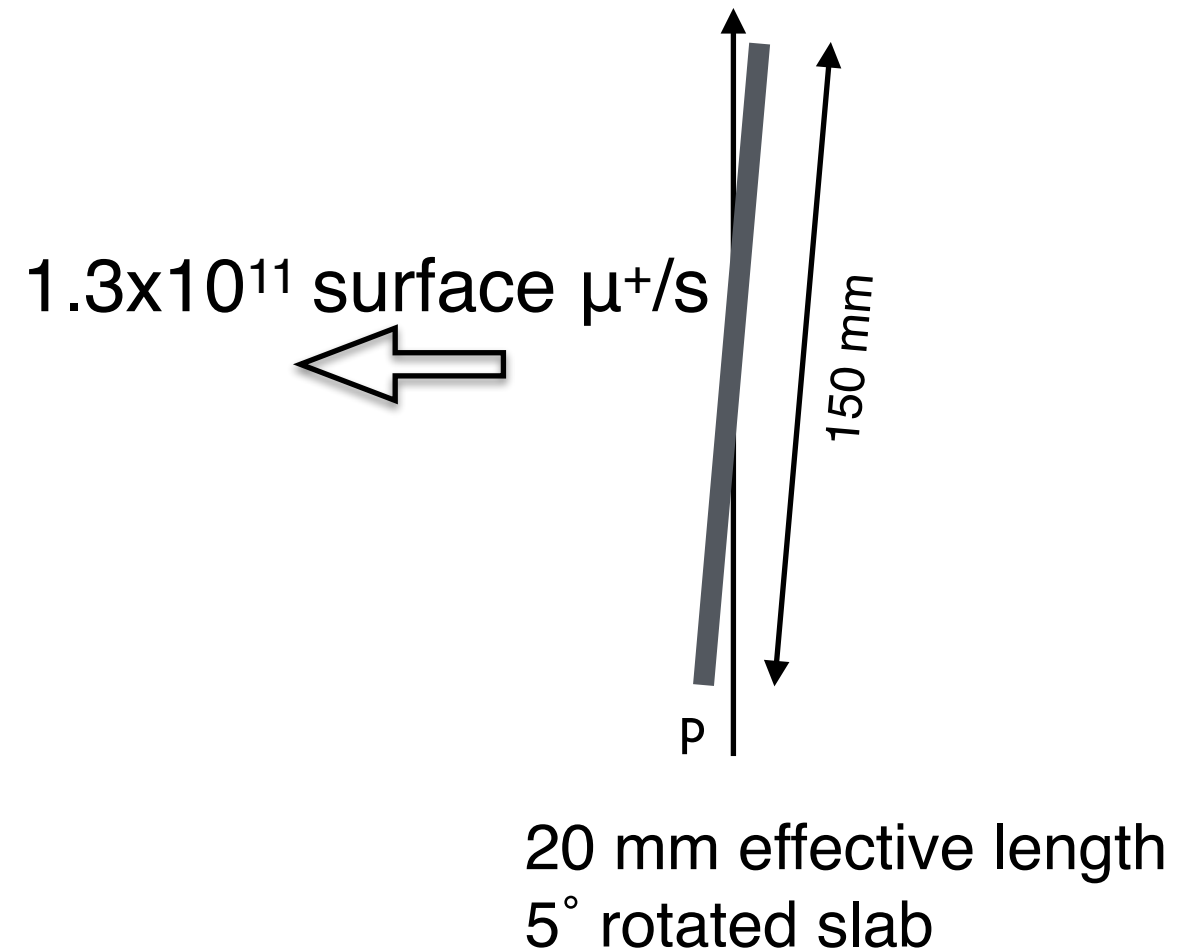
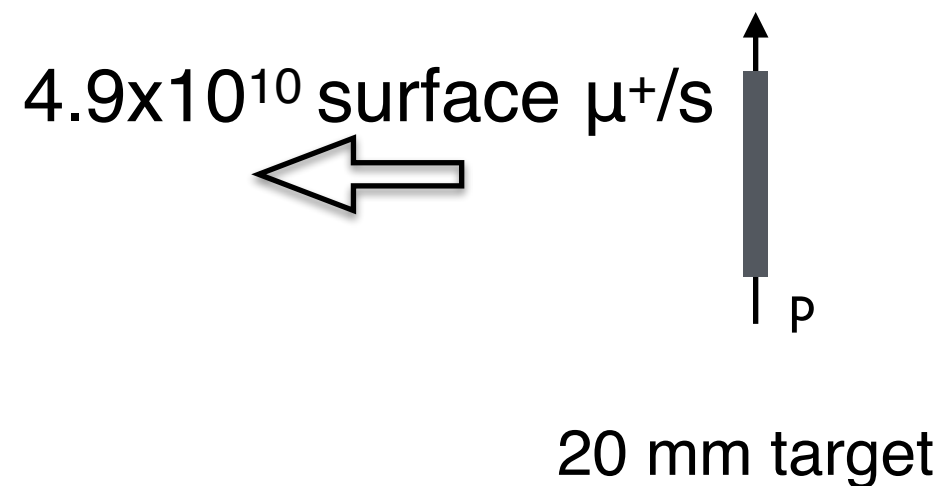
- Precision physics is a very sensitive tool to explore and unveil new physics
- HiMB aims at surface high intensity muon beam **O(10<sup>10</sup> muon/s)**
  - Initial simulations show that such rates are feasible; Target optimisation test: successfully done. Increase muon rate as expected. Beam optics and investigations on proton beam modifications underway
  - Put into perspective the target optimisation only, corresponding to **50%** of muon beam intensity gain, would corresponds to effectively raising the proton beam power at PSI by **650 kW**, equivalent to a beam power of almost **2 MW**. If the same exercise is repeated put into perspective the beam line optimisation the equivalent beam power would be of the order of **several tens of MW**
- muCool aims at low energy high-brightness muon beam
  - Increase in brightness by a factor **10<sup>10</sup>** with an efficiency of **10<sup>-3</sup>**
  - First two stages demonstrated independently. Measurements and simulations agree. Current development: combining two stages and extraction into the vacuum
- Future accelerator concepts based on muons are part of the European Strategy recommendations
- Ongoing efforts (Muon collider&Neutrino Factory&New Ideas) open the doors for high energy muon accelerators as a probe of fundamental physics



# Target geometry for new target M\*

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- Change current 5 mm TgM for 20 mm TgM\*
- 20 mm rotated slab target as efficient as Target E

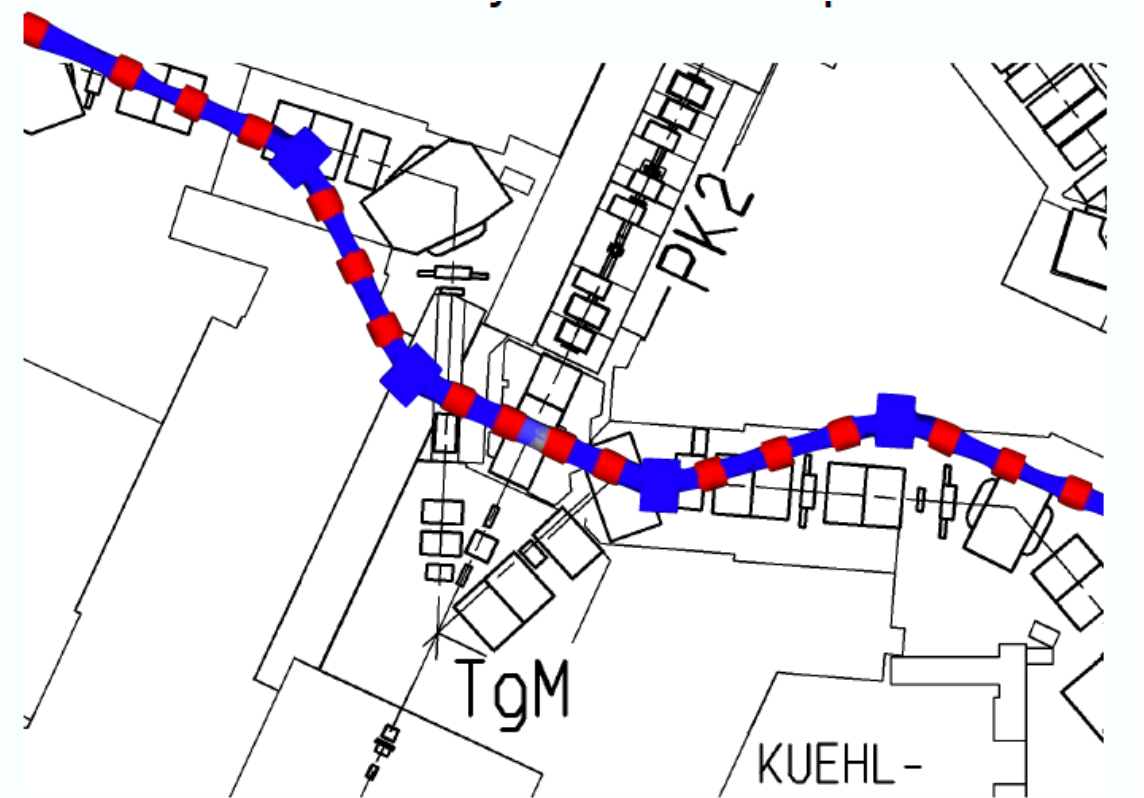




# ToDo

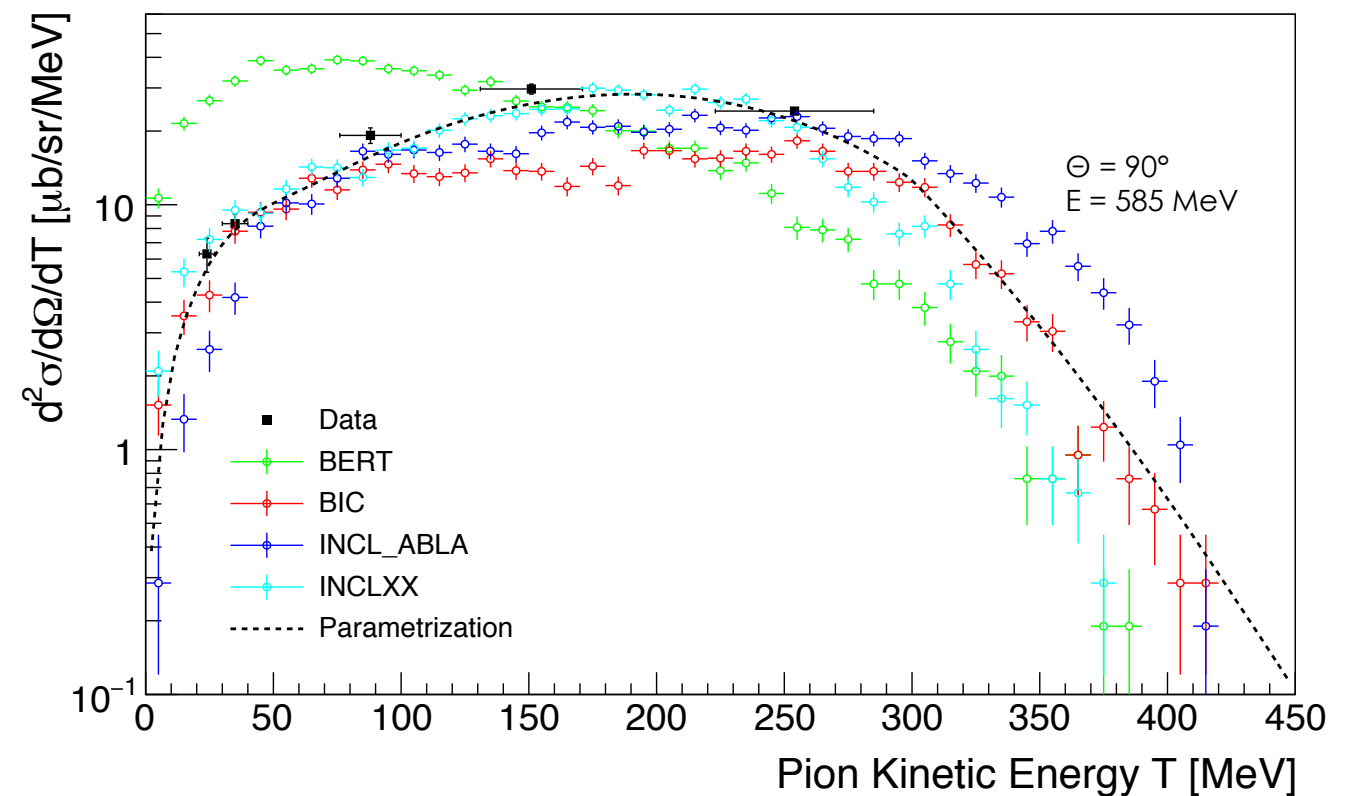
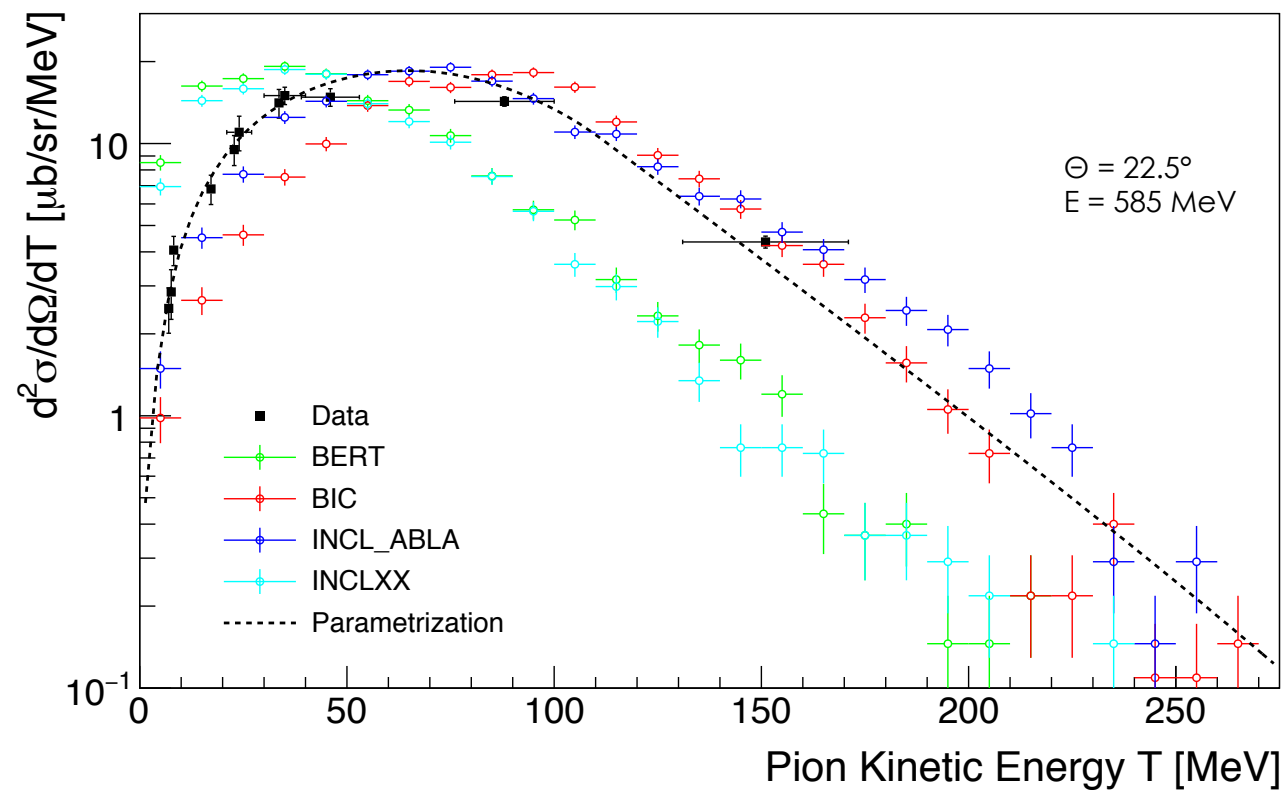
- Optimization of capturing
- Optimize final focussing
- Iterative Beam line optimization and implementation of beam monitoring and particle separator locations with max. transmission
- Minimize shielding modifications
- Particle separation
- Investigate impact on proton beam properties
- Study extraction angle
- Determine new target location
- Disposal of highly radioactive waste
- Study Mu3e setup phase space acceptance and optimize final focus properties
- Find solution with current users of Target M

Schematic of the layout in the experimental hall



# HiMB Simulation

- Geant4 pion production cross sections not optimised for low energies
- Implemented our own pion production cross section into Geant4/G4beamline based on measured data and two available parametrizations (**HiMB model**)
- Valid for all pion energies, proton energies < 1000 MeV, all angles and all materials
- Reliable results at 10% level



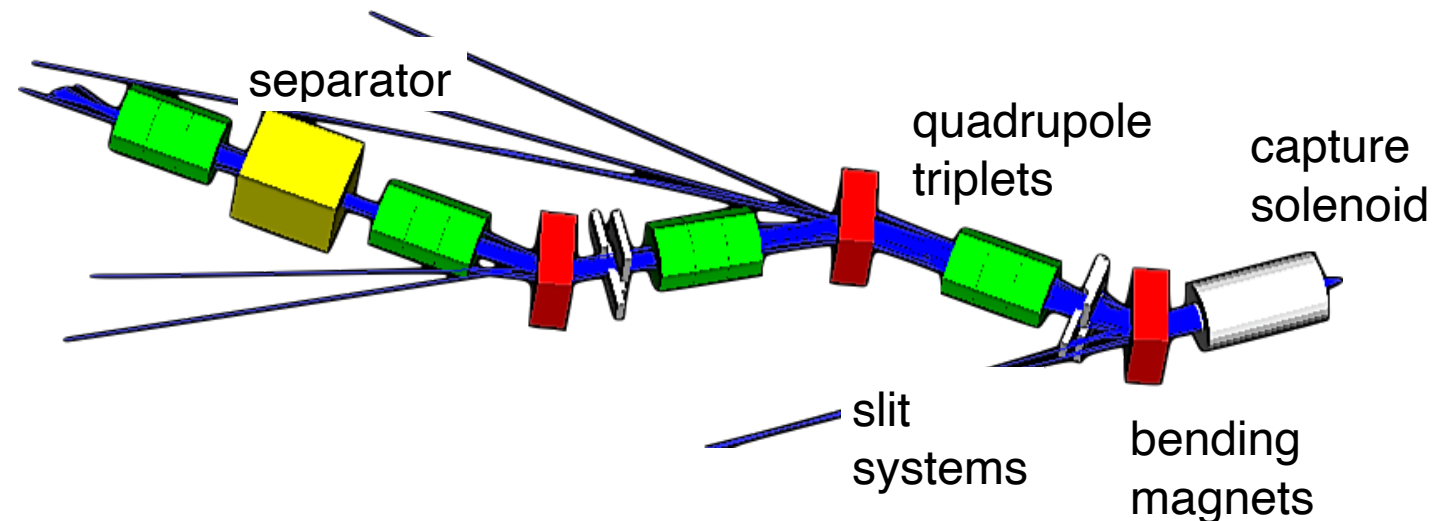
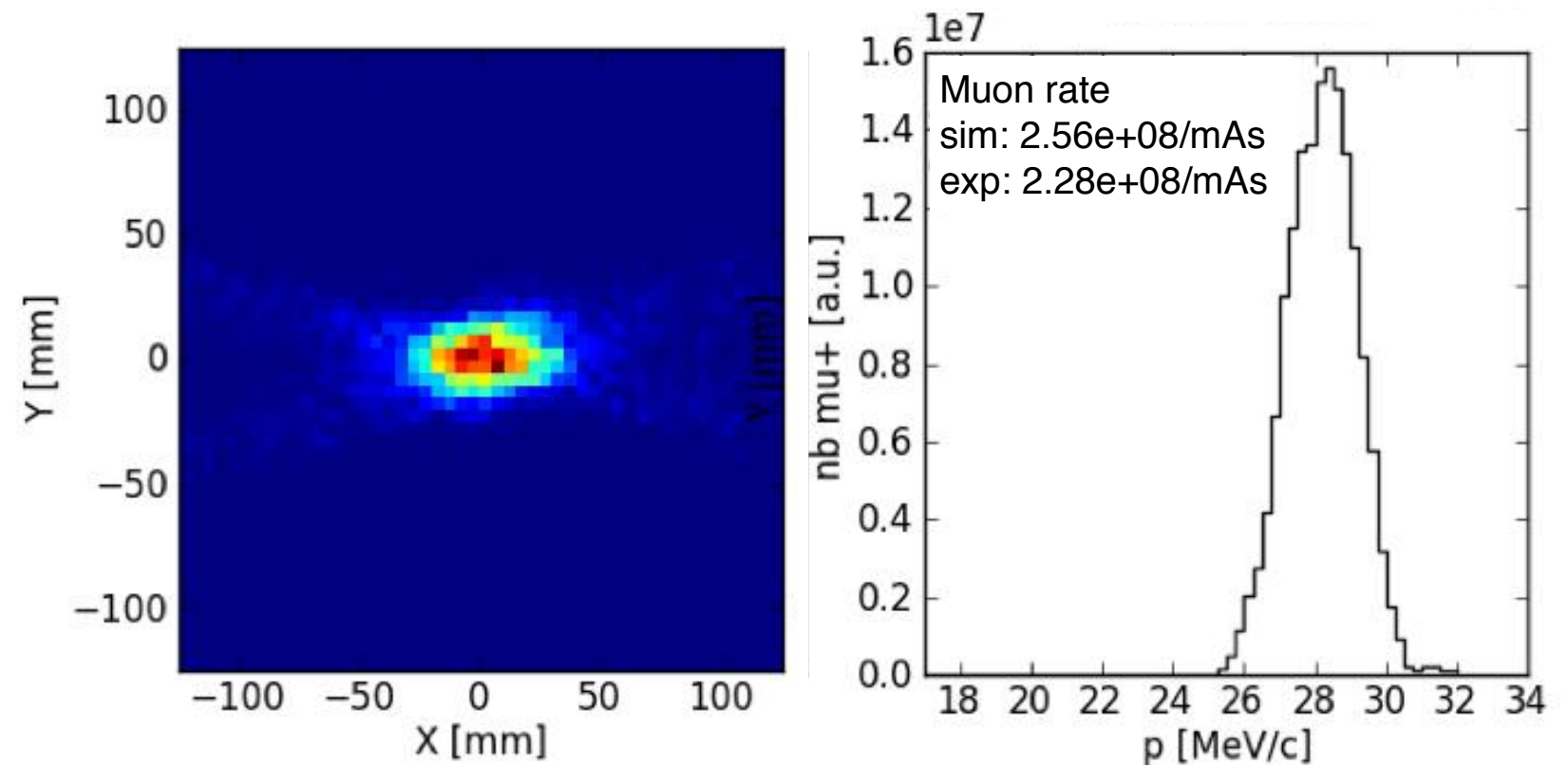
R. L. Burman and E. S. Smith, Los Alamos Tech. Report LA-11502-MS (1989)

R. Frosch, J. Löffler, and C. Wigger, PSI Tech. Report TM-11-92-01 (1992)

F. Berg et al., Phys. Rev. Accel. Beams **19**, 024701 (2016)

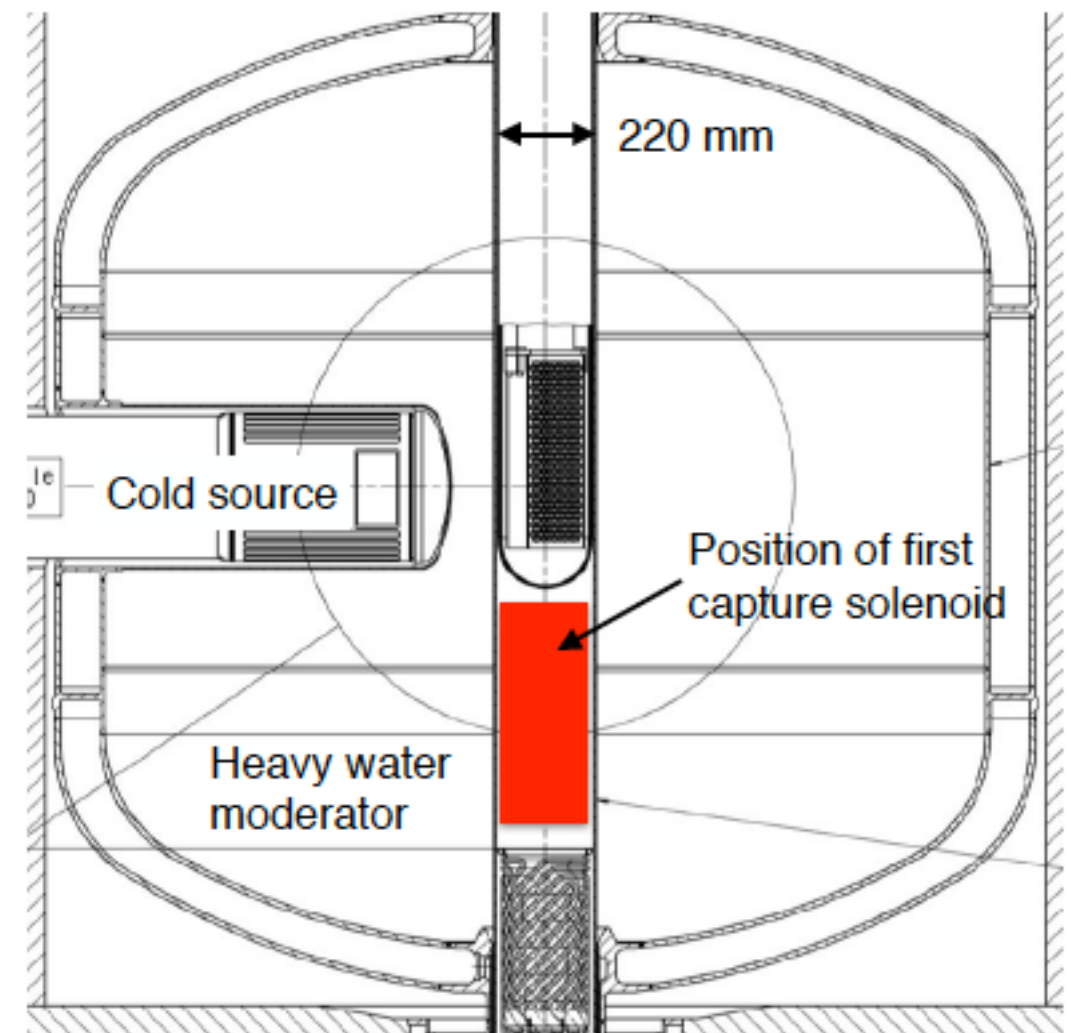
# HiMB model validation

- Full simulation of  $\mu$ E4 and  $\pi$ E5 beam lines starting from proton beam
- Detailed field maps available for all elements
- Very good agreement between simulation and measurements



# Initial HiMB concept: @SINQ

- Source simulation (below safety window):  
 **$9 \times 10^{10}$  surface- $\mu^+$ /s @ 1.7 mA  $I_p$**
- Profit from stopping of full beam
- Residual proton beam ( $\sim 1$  MW) dumped on SINQ
- Replace existing quadrupoles with solenoids:
  - Preserve proton beam footprint
  - Capture backward travelling surface muons
- Extract muons in Dipole fringe field
- Backward travelling pions stopped in beam window
- Capturing turned out to be difficult :
  - Large phase space (divergence & 'source' extent)
  - Capture solenoid aperture needed to be increased, but constrained by moderator tank
- High radiation level close to target
- Due these constraints and after several iterations with different capturing elements:
  - **Not enough captures muons to make an high intensity beam**
  - **Alternative solution: HiMB @ EH**





# Optimization of standard production targets

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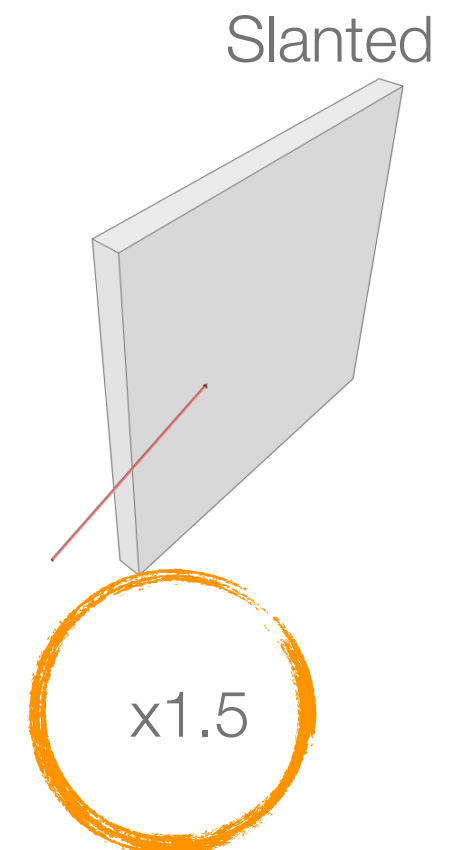
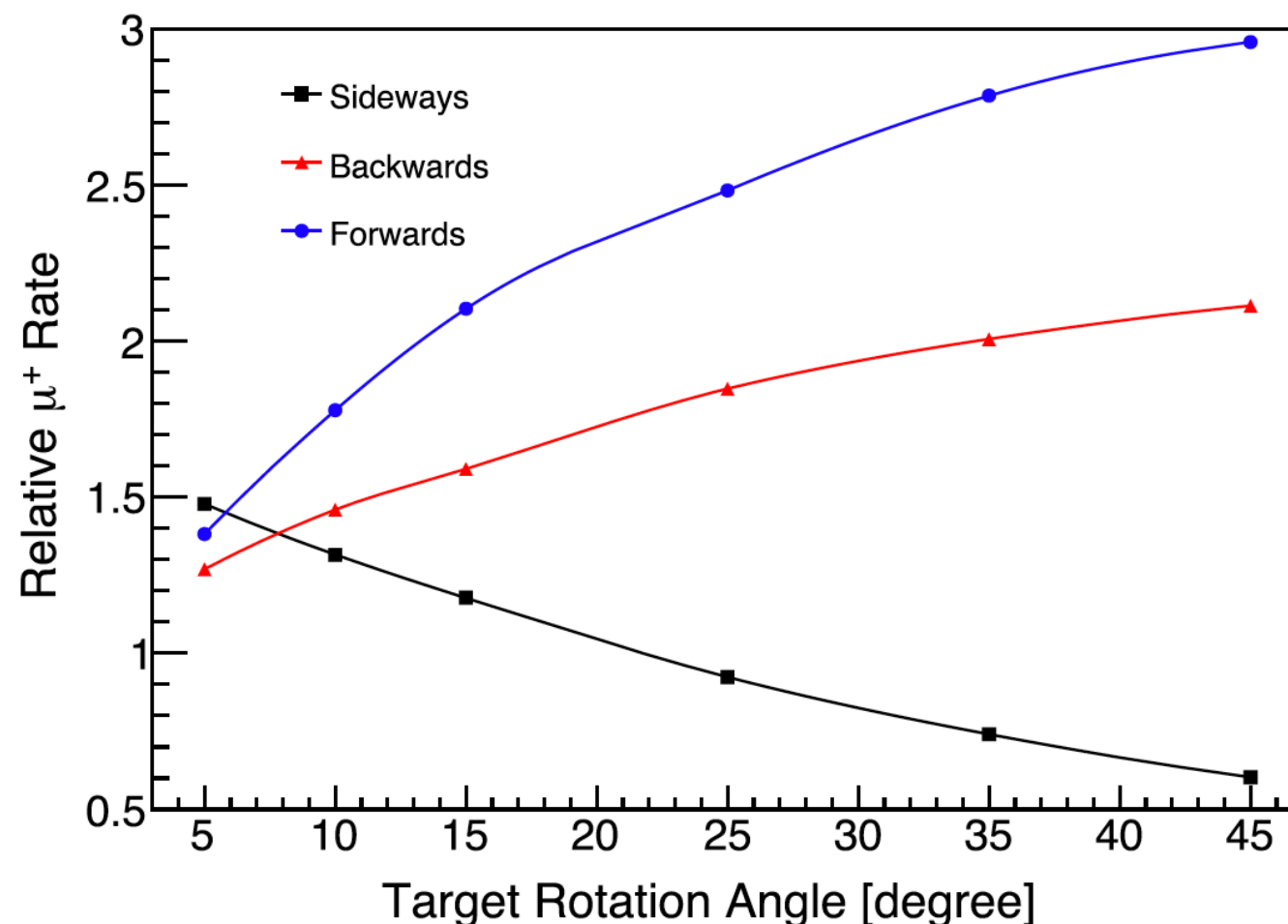
- Strategy: either increasing the surface volume (surface area times acceptance depth) or the pion stop density near the surface
- **Target geometry**
  - Comparison studies of different target geometries: **TgE for different lengths**

Surface muon rate

Length [mm]	Upstream	Downstream	Side
10	$1.4 \times 10^{10}$	$9.0 \times 10^9$	$1.8 \times 10^{10}$
20	$1.6 \times 10^{10}$	$1.2 \times 10^{10}$	$5.1 \times 10^{10}$
30	$1.9 \times 10^{10}$	$1.1 \times 10^{10}$	$8.5 \times 10^{10}$
40	$1.8 \times 10^{10}$	$1.1 \times 10^{10}$	$1.2 \times 10^{11}$
60	$1.8 \times 10^{10}$	$1.2 \times 10^{10}$	$2.1 \times 10^{11}$

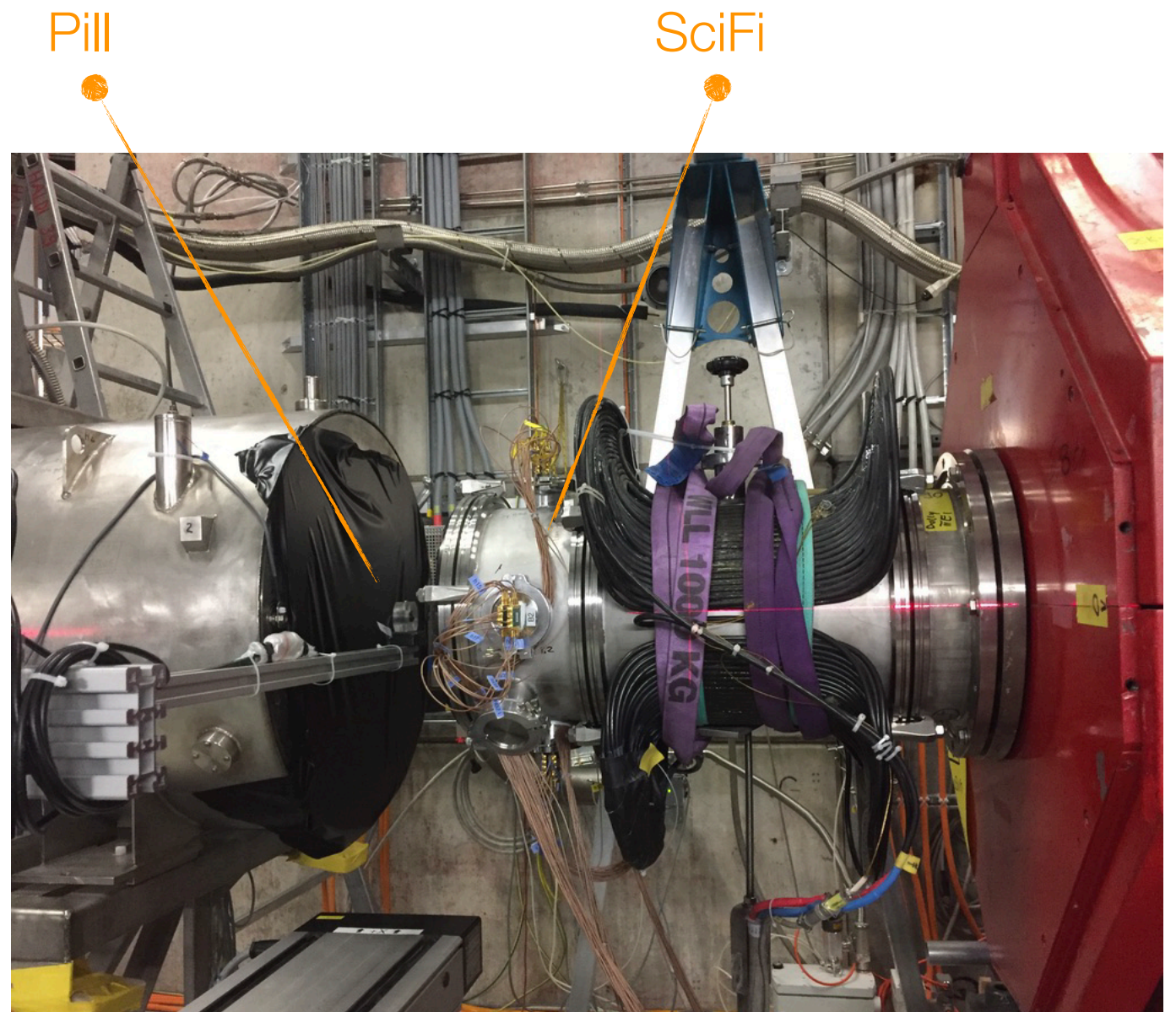
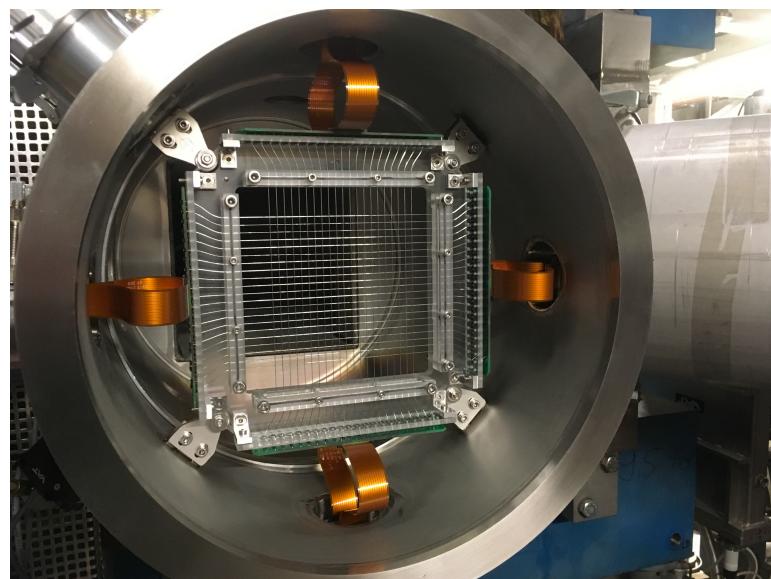
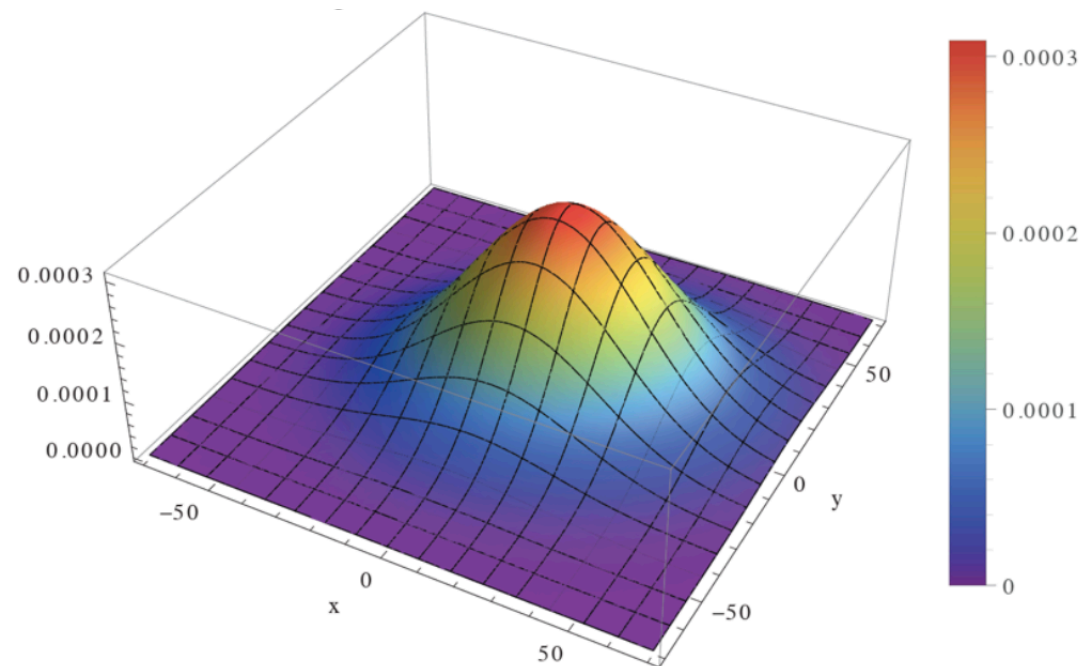
# Optimization of standard production targets

- Strategy: either increasing the surface volume (surface area times acceptance depth) or the pion stop density near the surface
- **Target geometry**
  - Comparison studies of different target geometries: **Different rotation angles**
  - Enhancements normalised to standard target



# Slanted target: 2019 test Results

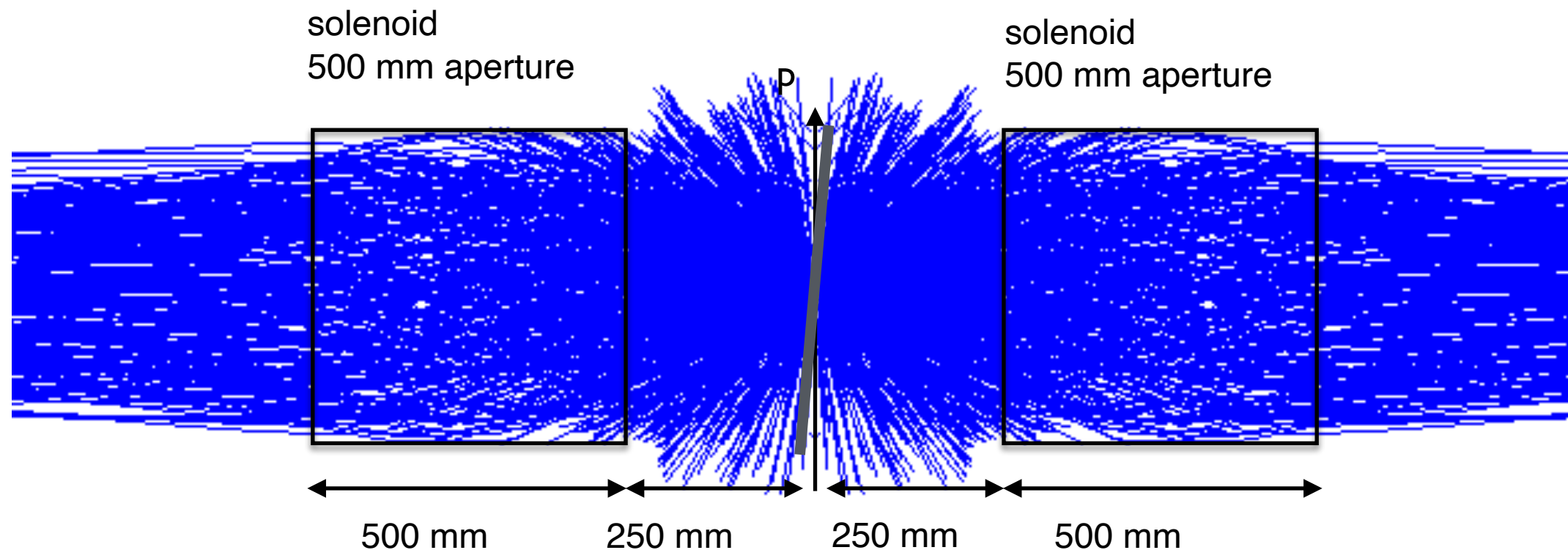
- Two independent detectors
  - SciFi:  $0.5 \times 0.5 \text{ mm}^2$  scintillating fibers coupled to SiPMs to form a grid
  - Pill: (diam.) 2 mm x (length) 2 mm scintillator coupled to Hamamatsu R9880U-110 photomultiplier





# Split capture solenoids

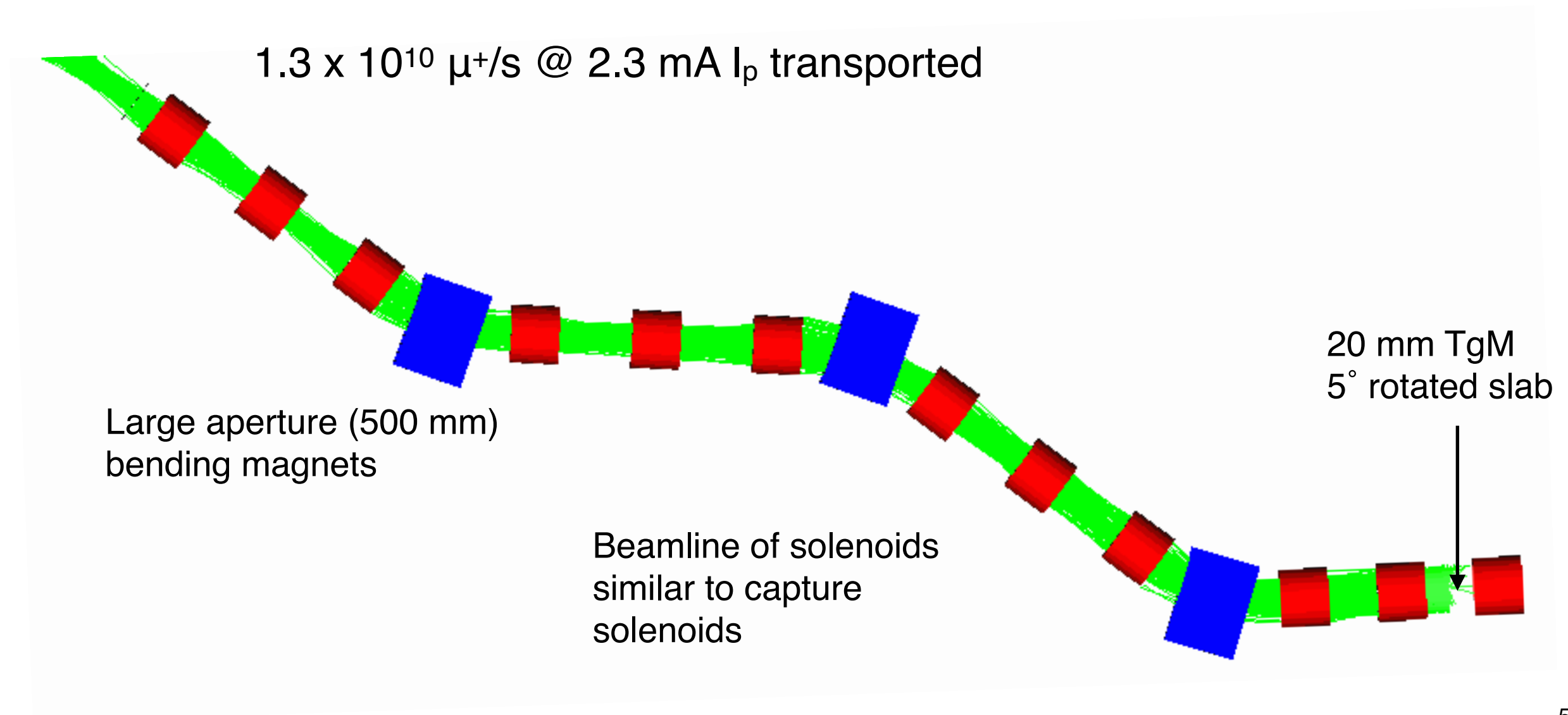
- Two normal-conducting, radiation-hard solenoids close to target to capture surface muons
- Central field of solenoids  $\sim 0.35$  T
- Field at target  $\sim 0.1$  T





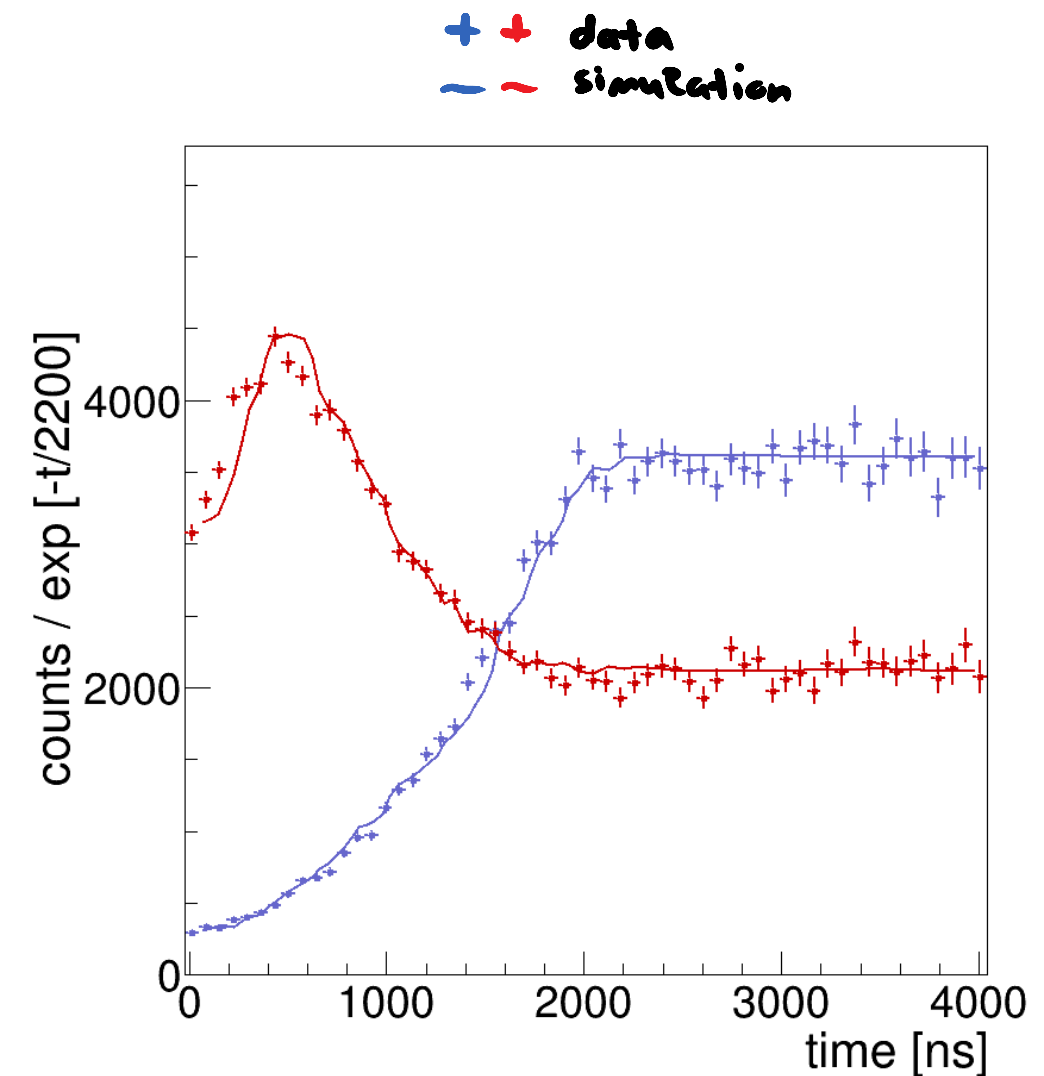
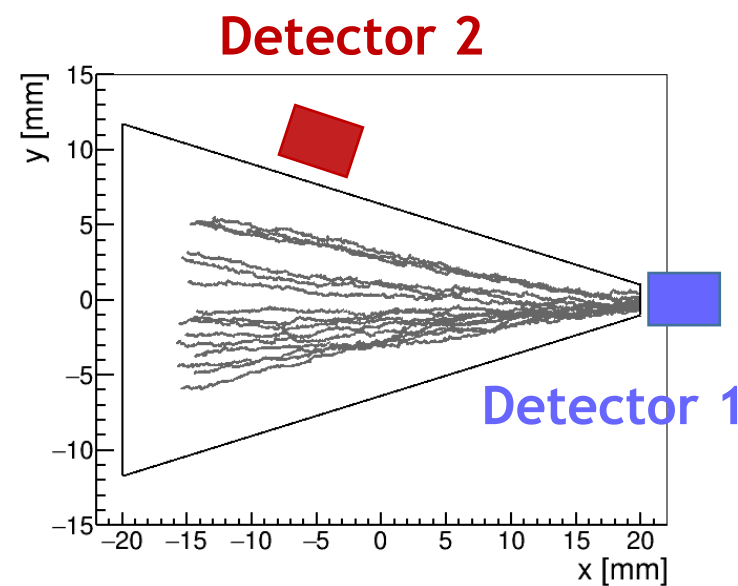
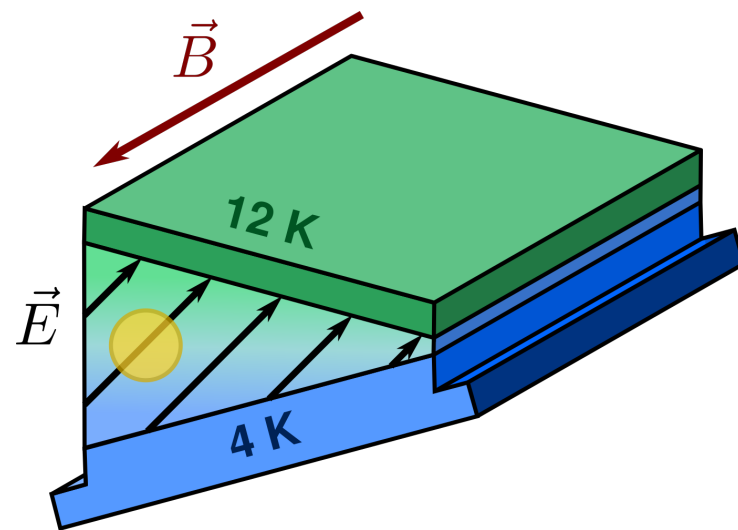
# Solenoid beam line

- First version of beam optics showing that large number of muons can be transported.
- Almost parallel beam, no focus, no separator, ...
- Final beam optics under development



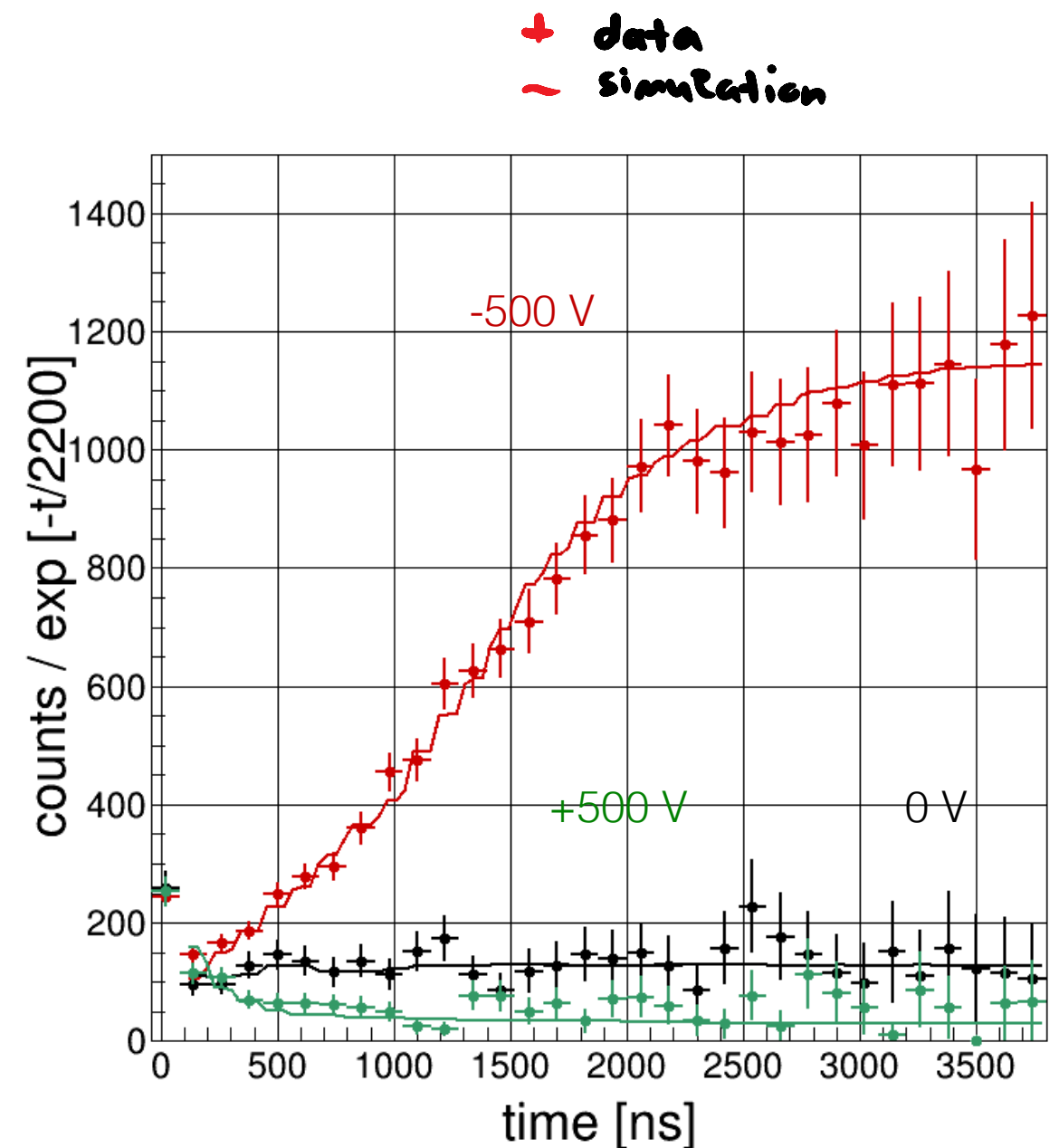
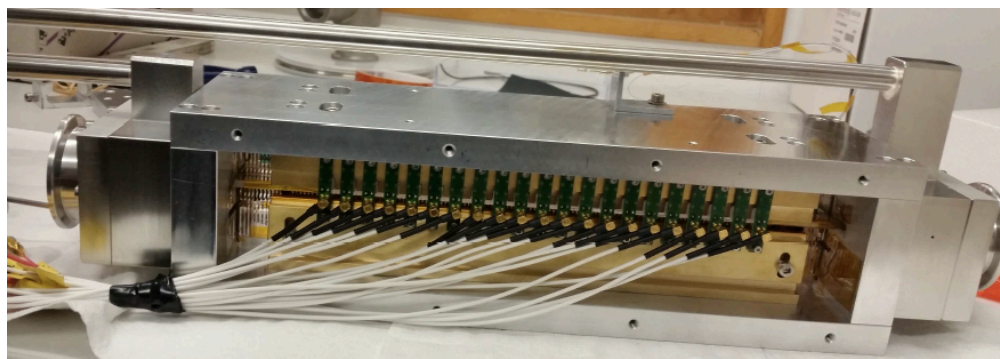
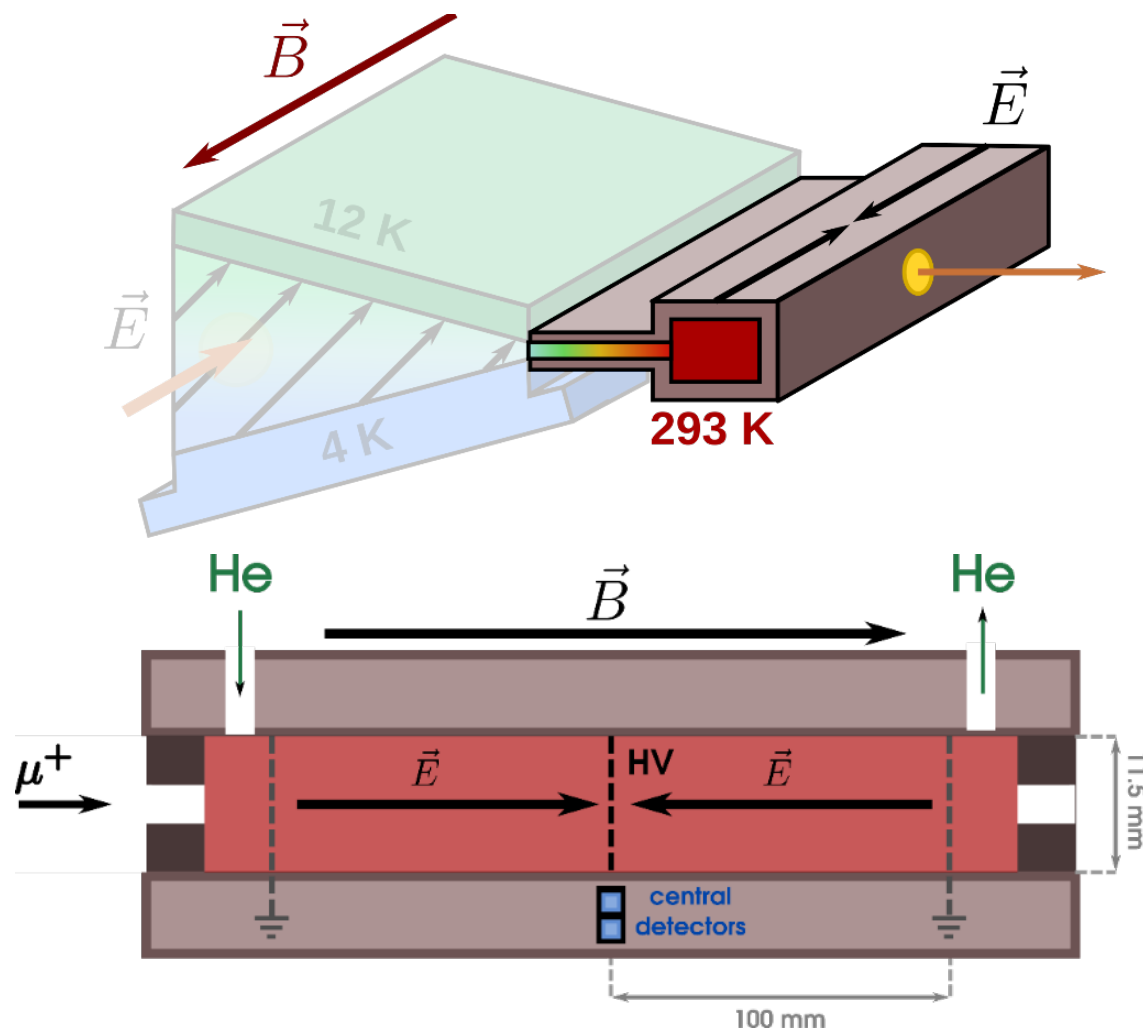
# Experimental setup and results: 1st stage

- Separately longitudinal and transverse compression: **PROVED**
- **Very good agreement between data and simulations**



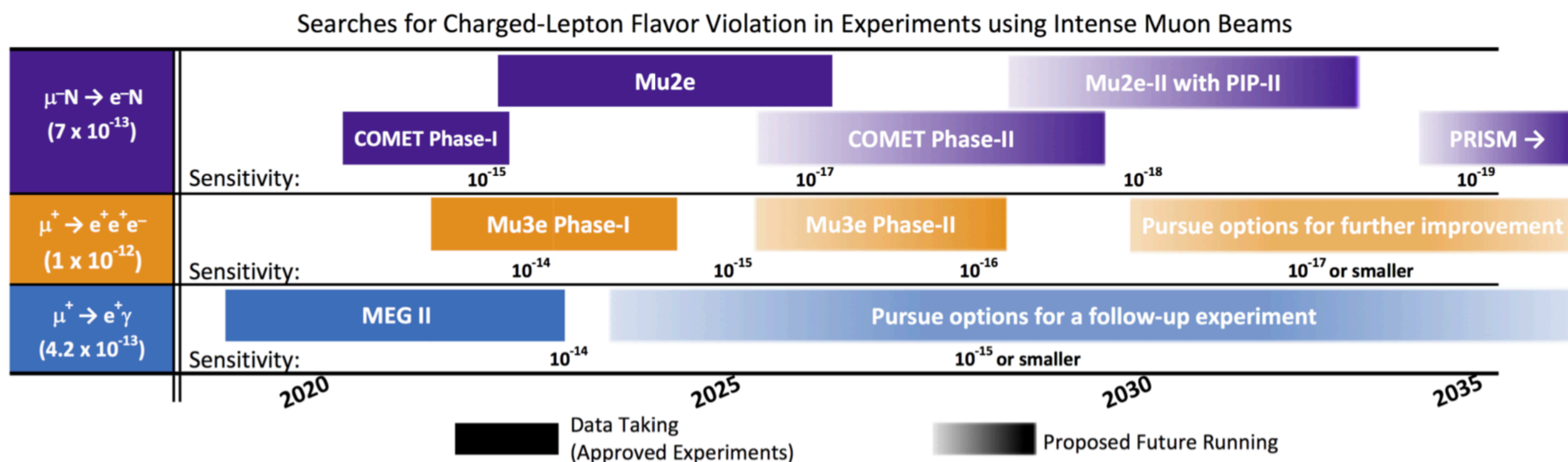
# Experimental setup and results: 2nd stage

- Separately longitudinal and transverse compression: **PROVED**
- **Very good agreement between data and simulations**



# Final remarks

- Astonishing sensitivities in muon cLFV channels are foreseen for the incoming future
- **cLFV remains one of the most exciting place where to search for new physics**
- Submitted inputs to the European Strategy Committee



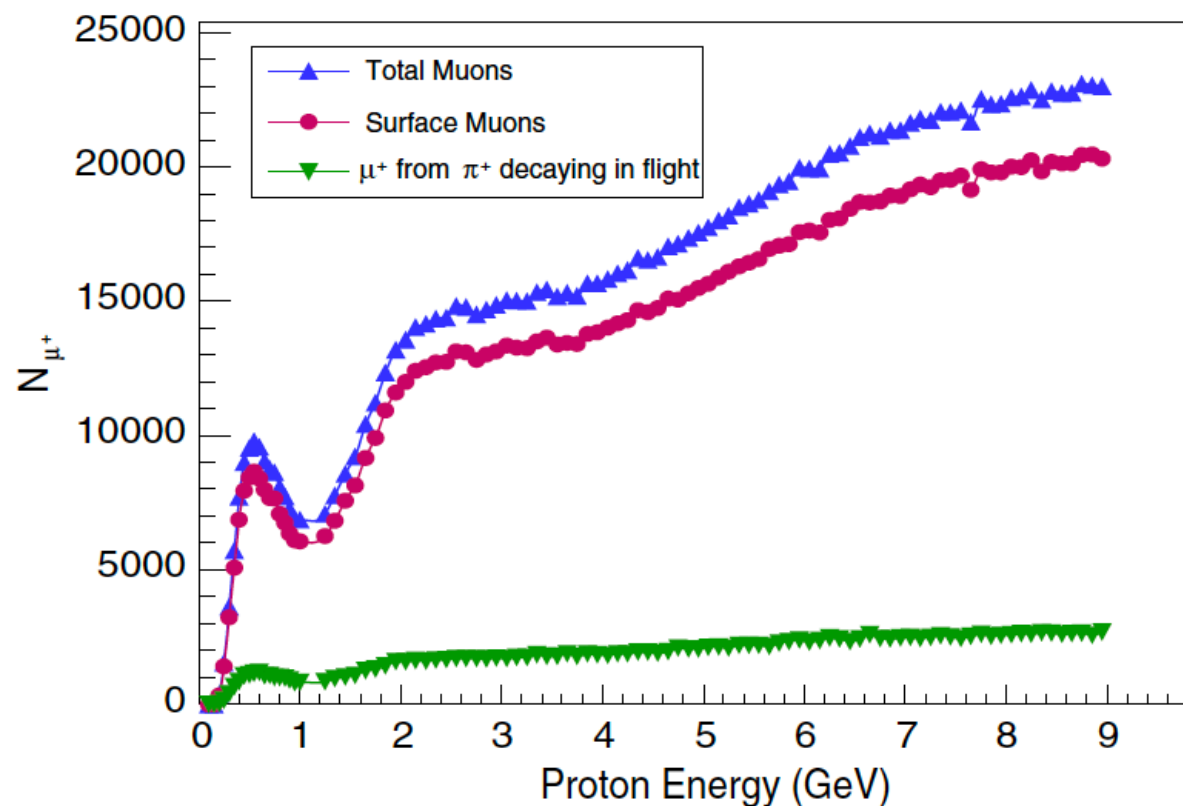
Thanks for your attention!



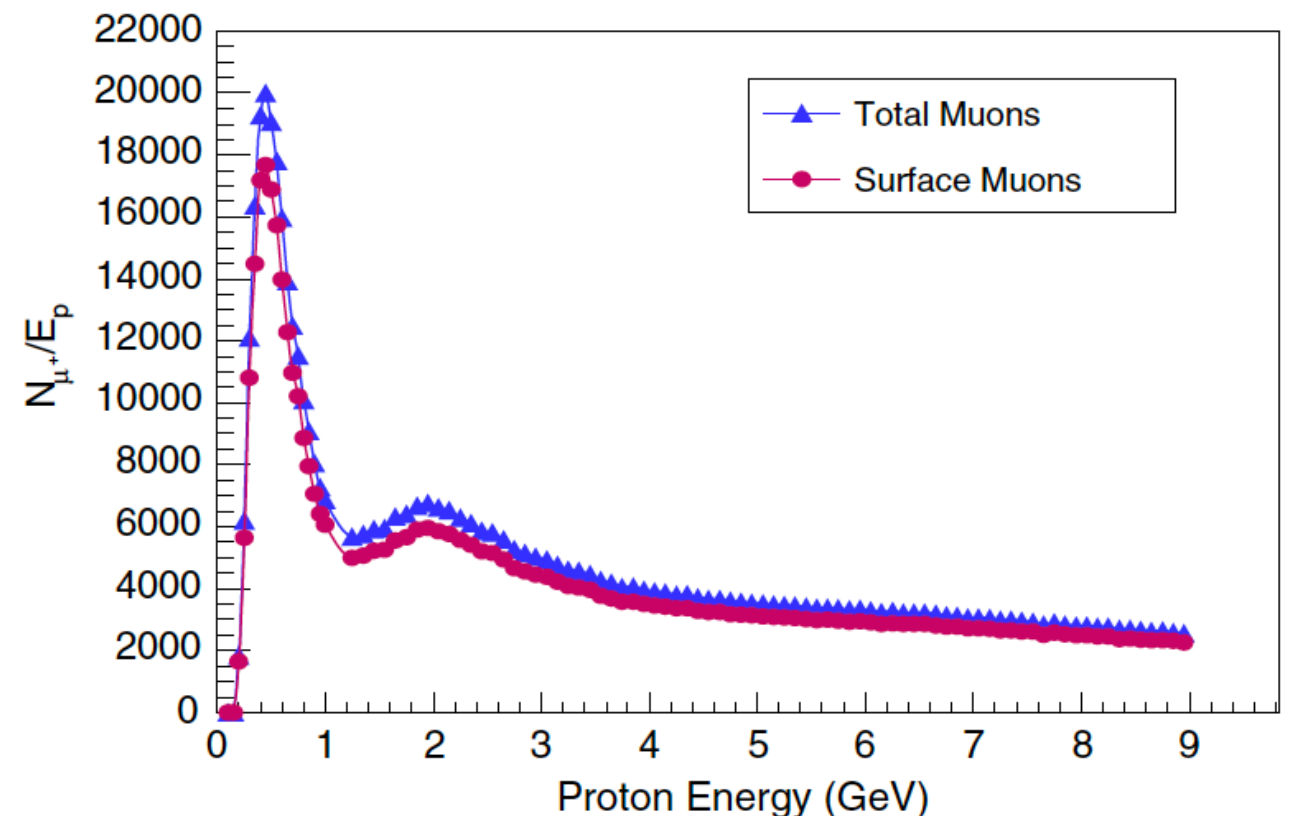
# Optimal surface muon production

- **BUNGAU** et al., Phys. Rev. ST Accel. BEAMS **16**, 014701 (2013)
- Target: graphite
- Simulation validation: ISIS data
- For standalone muon facility: 500 MeV proton energy is the optimal energy

Variation of muon yield with proton energy at higher energies



Normalization of the muon yield to the proton energy



# Muon production via pion decay

- Single pion production at 290 MeV proton energy (LAB)
- Low-energy muon beam lines typically tuned to surface- $\mu^+$  at  $\sim 28$  MeV/c
- Note: surface  $-\mu \rightarrow$  polarized positively charged muons (spin antiparallel to the momentum)
- Contribution from cloud muons at similar momentum about 100x smaller
- Negative muons only available as cloud muons

