

Studies of the $^{16}\text{O}(\gamma^*, \alpha)^{12}\text{C}$ reaction
for astrophysical relevance at
MAGIX/MESA

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Institute for Nuclear Physics – Johannes Gutenberg University Mainz
SFB School – Boppard – October 23, 2019

Topics

MAGIX@MESA

S-Factor of $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$

Feasibility Studies

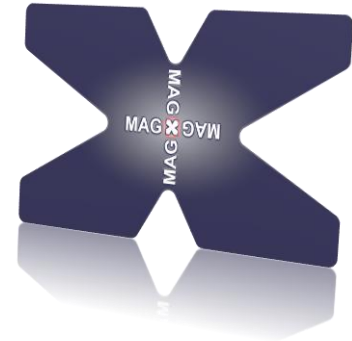
Summary/Outlook





MAGIX@MESA

Mainz Energy-Recovering Superconducting Accelerator



Energy Recovery Linac (ERL) Mode

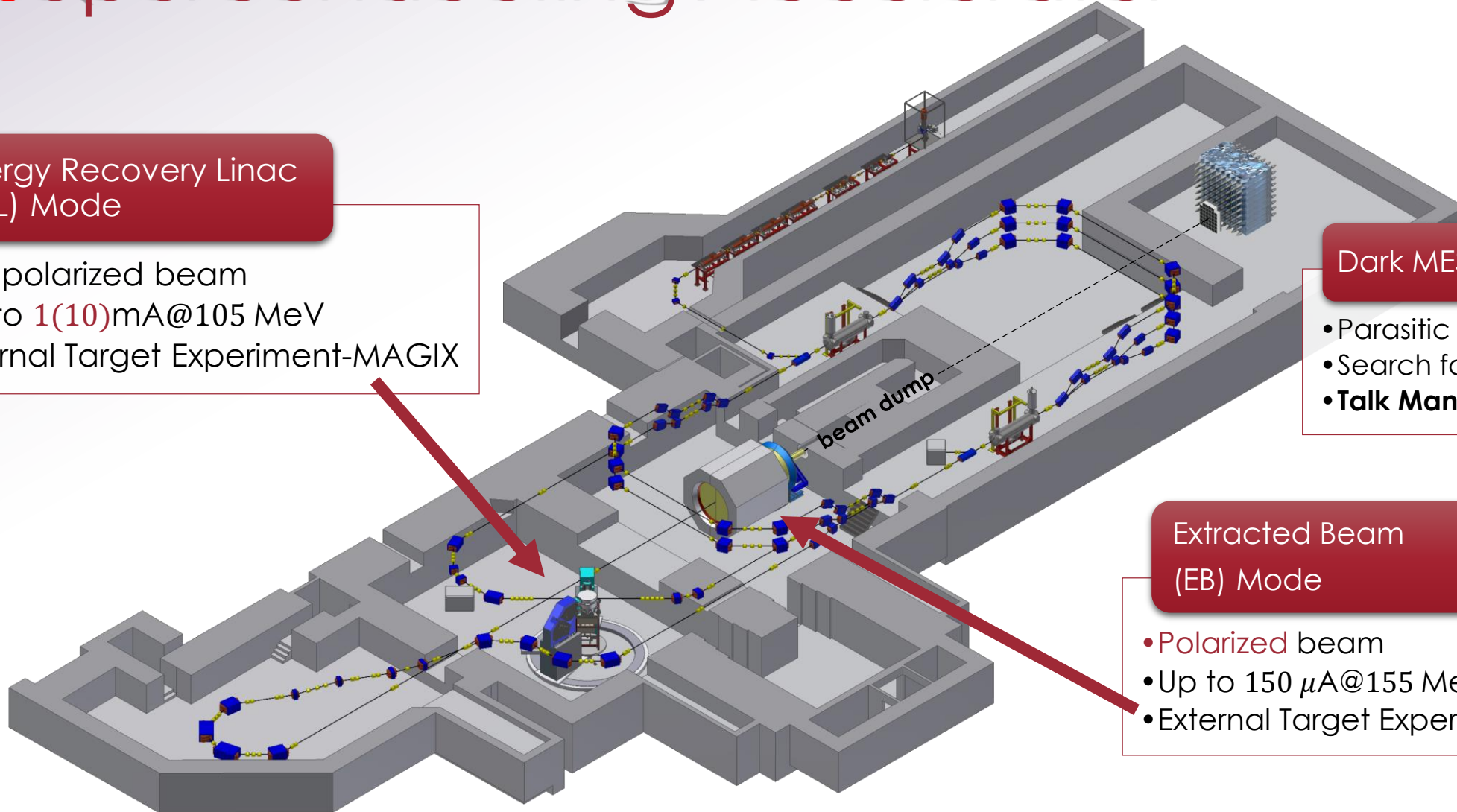
- (un)polarized beam
- Up to **1(10)mA@105 MeV**
- Internal Target Experiment-MAGIX

Dark MESA

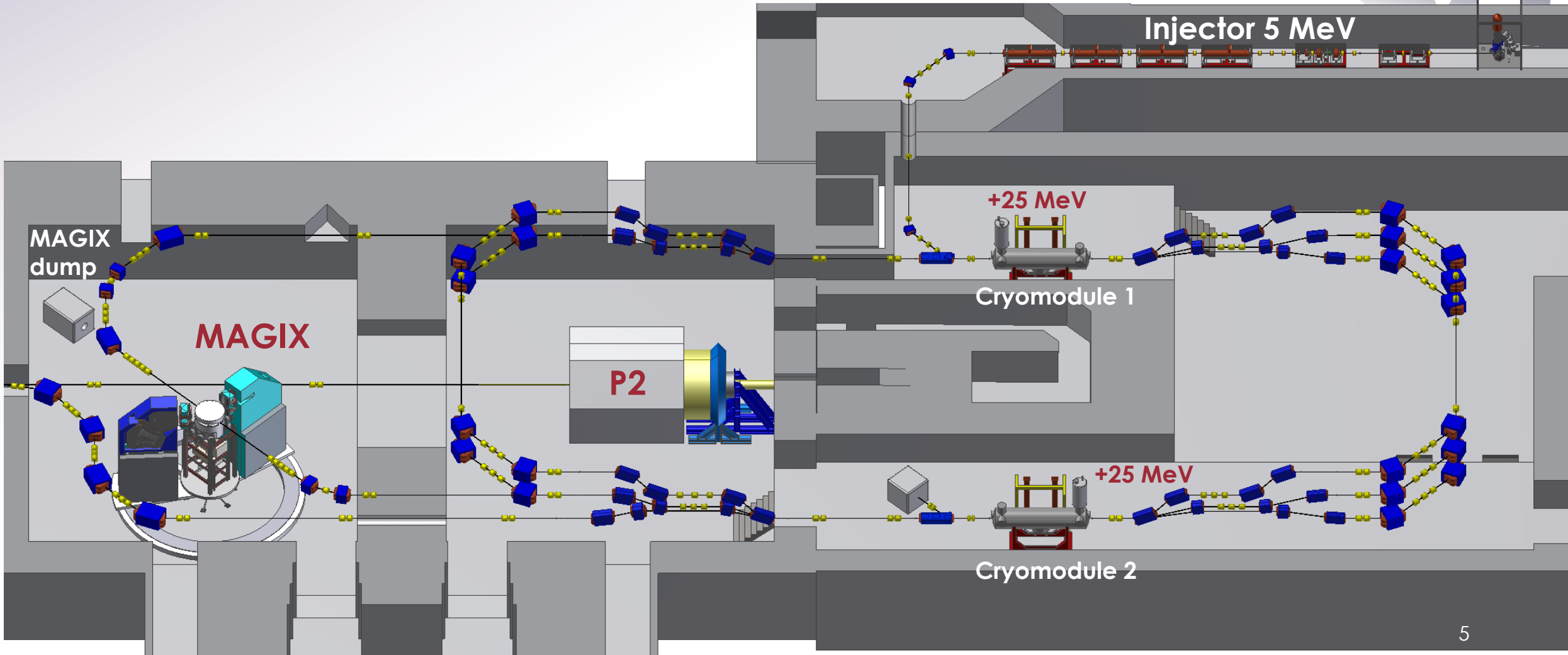
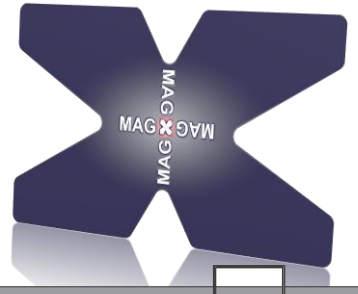
- Parasitic Experiment
- Search for Dark Matter
- **Talk Manuel Mauch**

Extracted Beam (EB) Mode

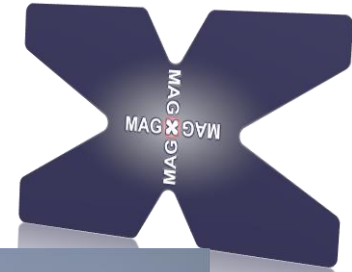
- **Polarized** beam
- Up to $150 \mu\text{A}@155 \text{ MeV}$
- External Target Experiment – P2



Mainz Energy-Recovering Superconducting Accelerator



Mesa Gas Internal target eXperiment - MAGIX



Internal Gas-Target

- Low energy high precision electron scattering
- Different gas types possible

Spectrometer

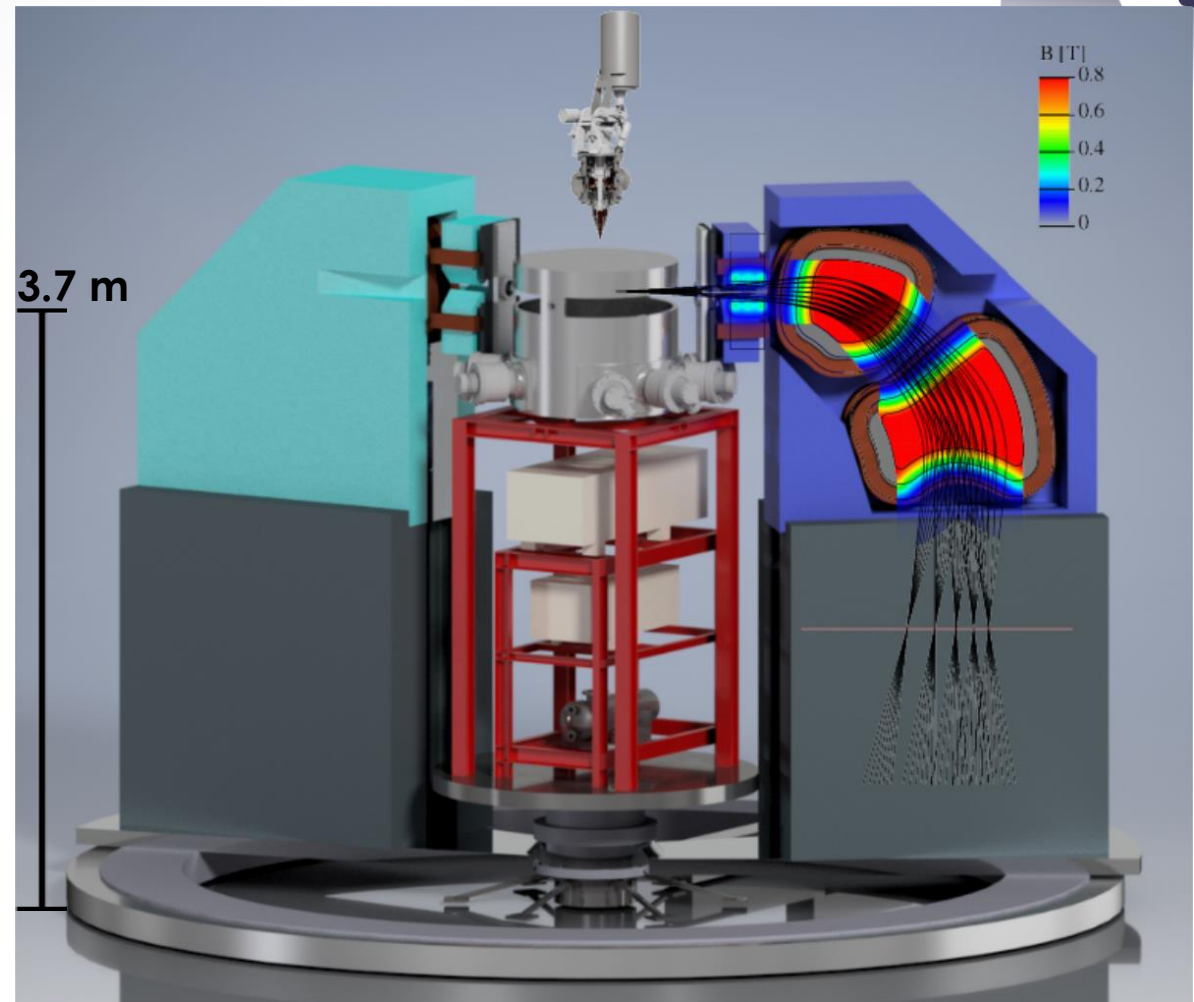
- High momentum resolution $\frac{\Delta p}{p} < 10^{-4}$
- Angular resolution $\Delta\theta < 0.05^\circ$

Thin Target - High Beam Current

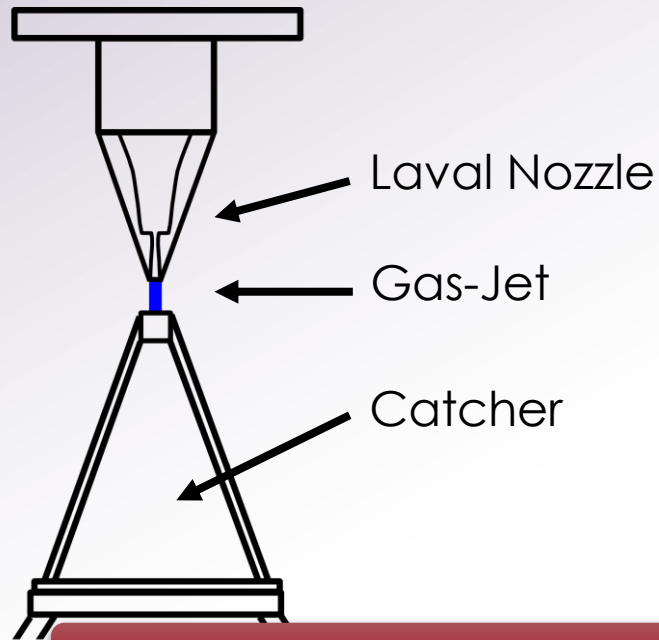
- High luminosity $\mathcal{L} \sim 10^{35} \text{ cm}^{-2} \text{ s}^{-1}$

Physics

- e.-m. form factor measurements
- Search for messenger particles of the dark sector
- Reaction studies of astrophysical relevance
- Few Body reactions
- ...



Jet-Target

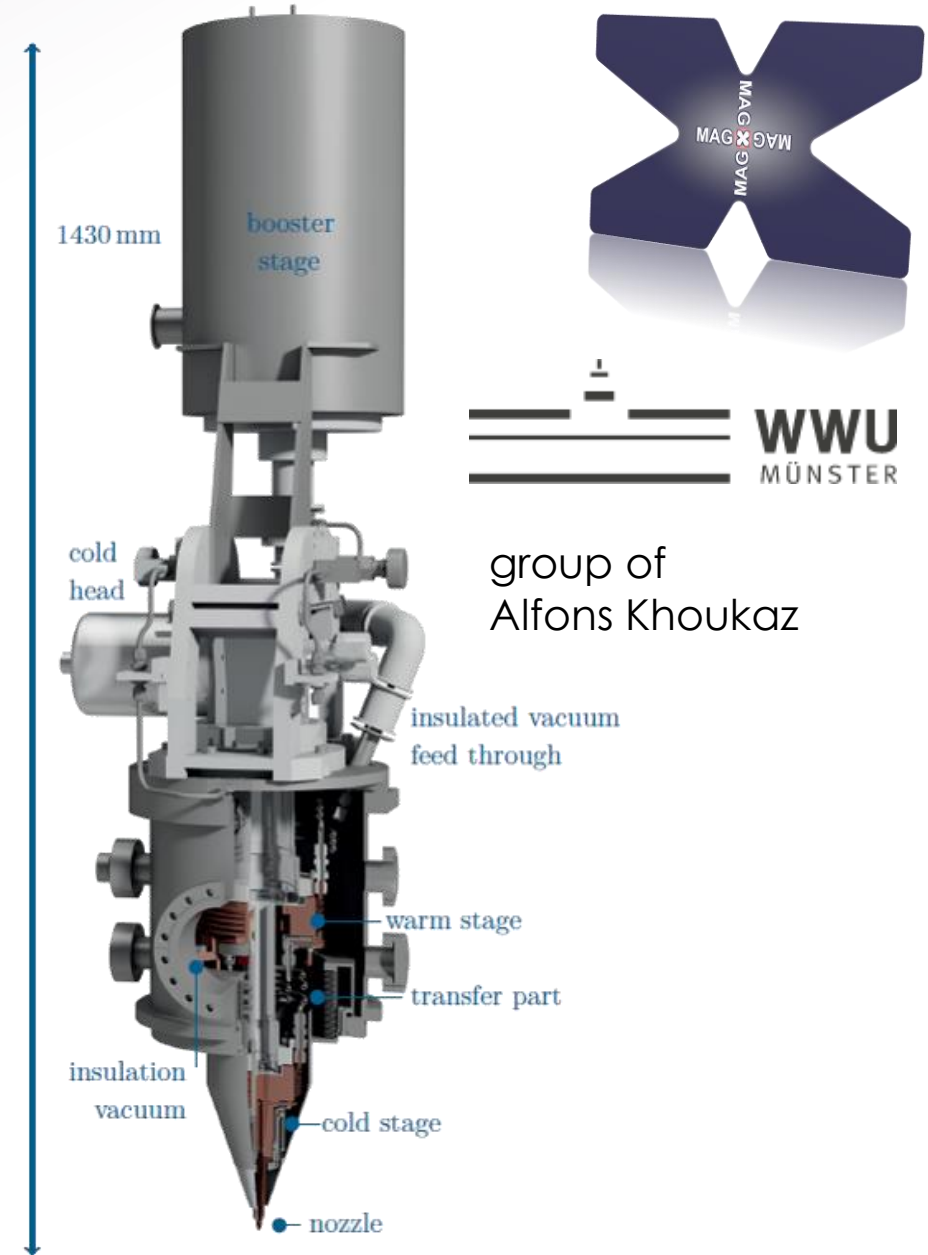
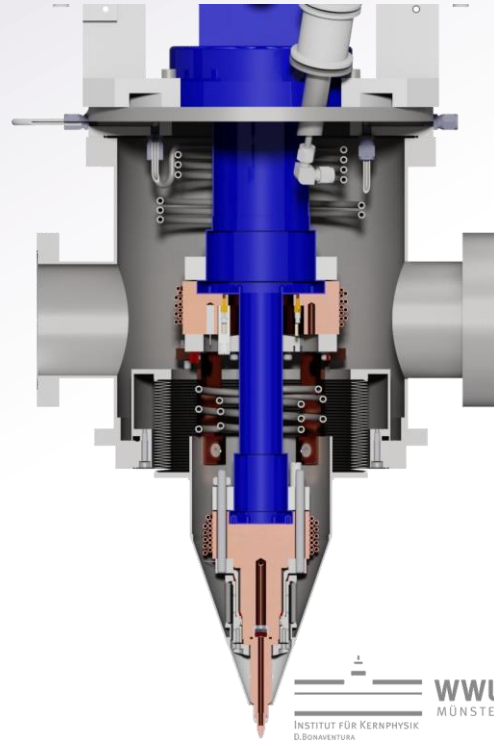


Gas-Jet

- Directive gas beam in vacuum
- ~Point-like (Diameter ~3 mm)
- $>10^{18}$ atoms / cm²

Three stages of cooling

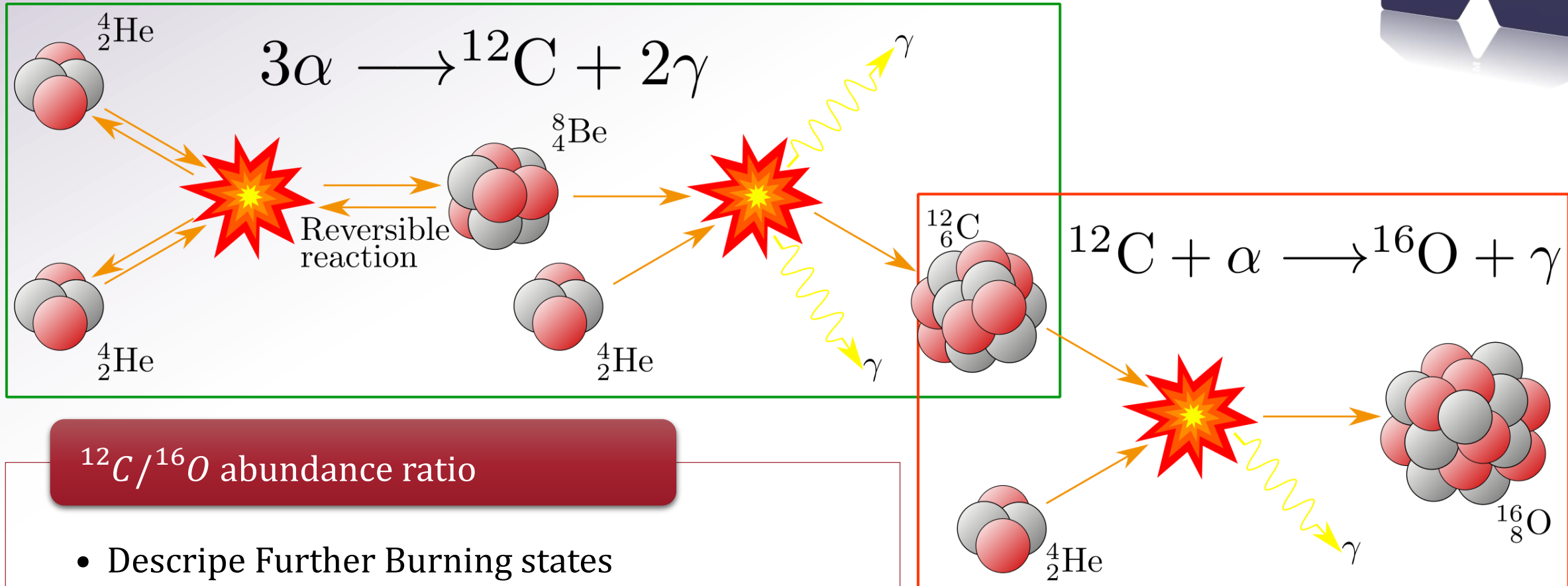
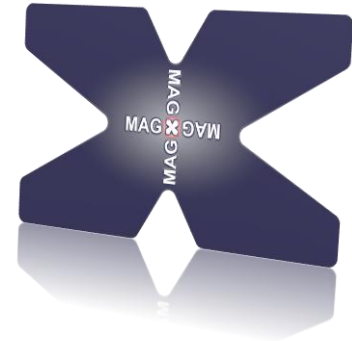
- Precooling (Booster)
- 1st main stage: down to 28 K
- 2nd main stage: down to 8 K





S-Factor of $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$

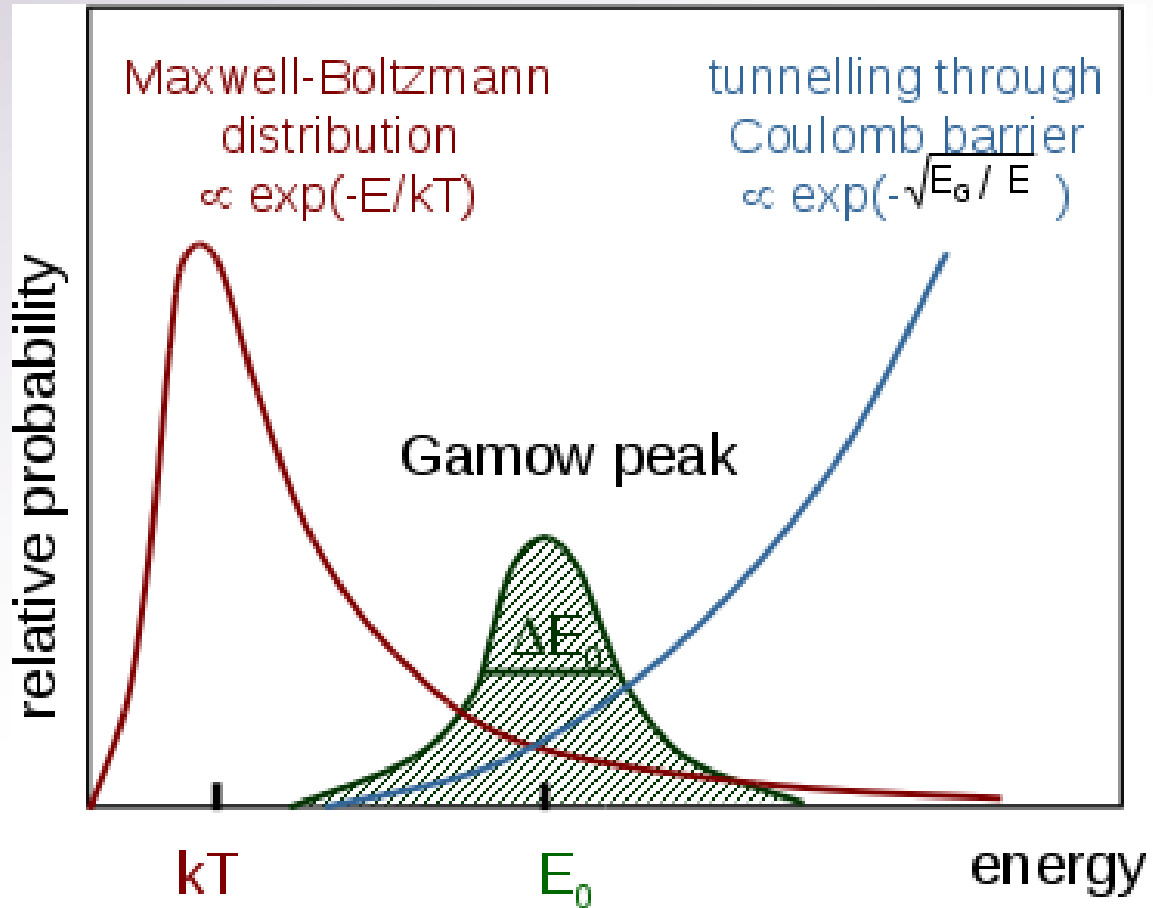
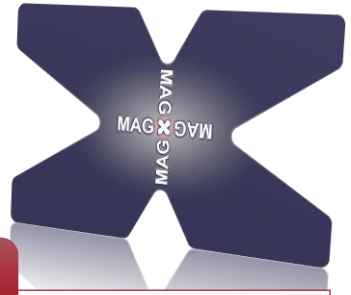
Helium Burning in Red Giants



${}^{12}\text{C}/{}^{16}\text{O}$ abundance ratio

- Describe Further Burning states
- Nucleosynthesis in massive stars

Gamow-Peak



Maxwell-Boltzmann distribution

- Energy distribution in hot gas
 $\propto \exp\left(-\frac{E}{kT}\right)$
- $kT \sim 15 \text{ keV} @ T = 2 \cdot 10^8 \text{ K}$

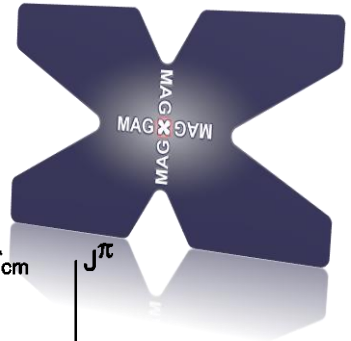
Coulomb penetration factor

- Tunnelling probability
- $\propto \exp(-\sqrt{E_0/E})$

Gamow-Peak

- $E_0 = \left(\frac{1}{2} b \cdot k \cdot T\right)^{\frac{2}{3}} \approx 300 \text{ keV} @ T \approx 2 \cdot 10^8 \text{ K}$
 $b = \pi \alpha Z_1 Z_2 \sqrt{2\mu c^2}$ with $\mu =$ reduced mass

S-Factor of $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$



$$\sigma(E) = \frac{1}{E} e^{-\frac{2\pi Z_1 Z_2 \alpha c}{v}} \cdot S(E)$$

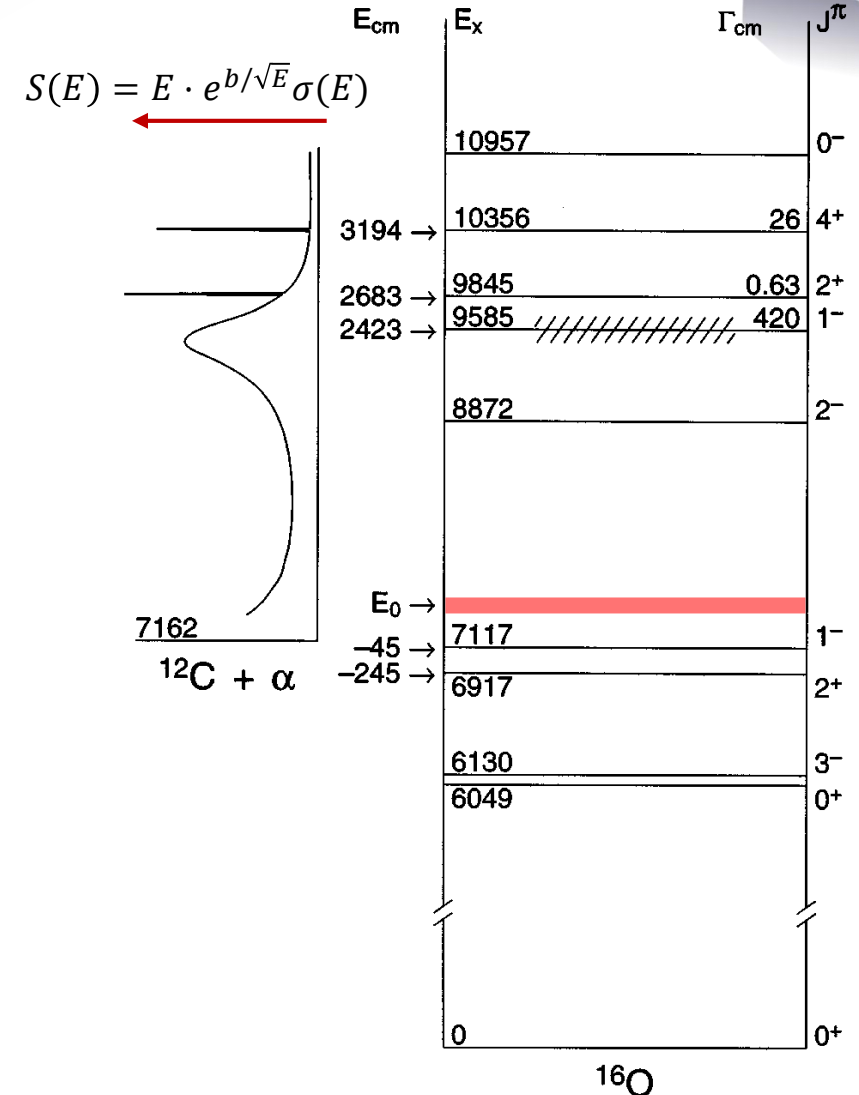
• S-Factor $S(E)$

- Deviation factor from trivial model
- Represents any effect of nuclear structure
- Close to the Gamow-Peak the cross section is dominated by subthreshold resonances

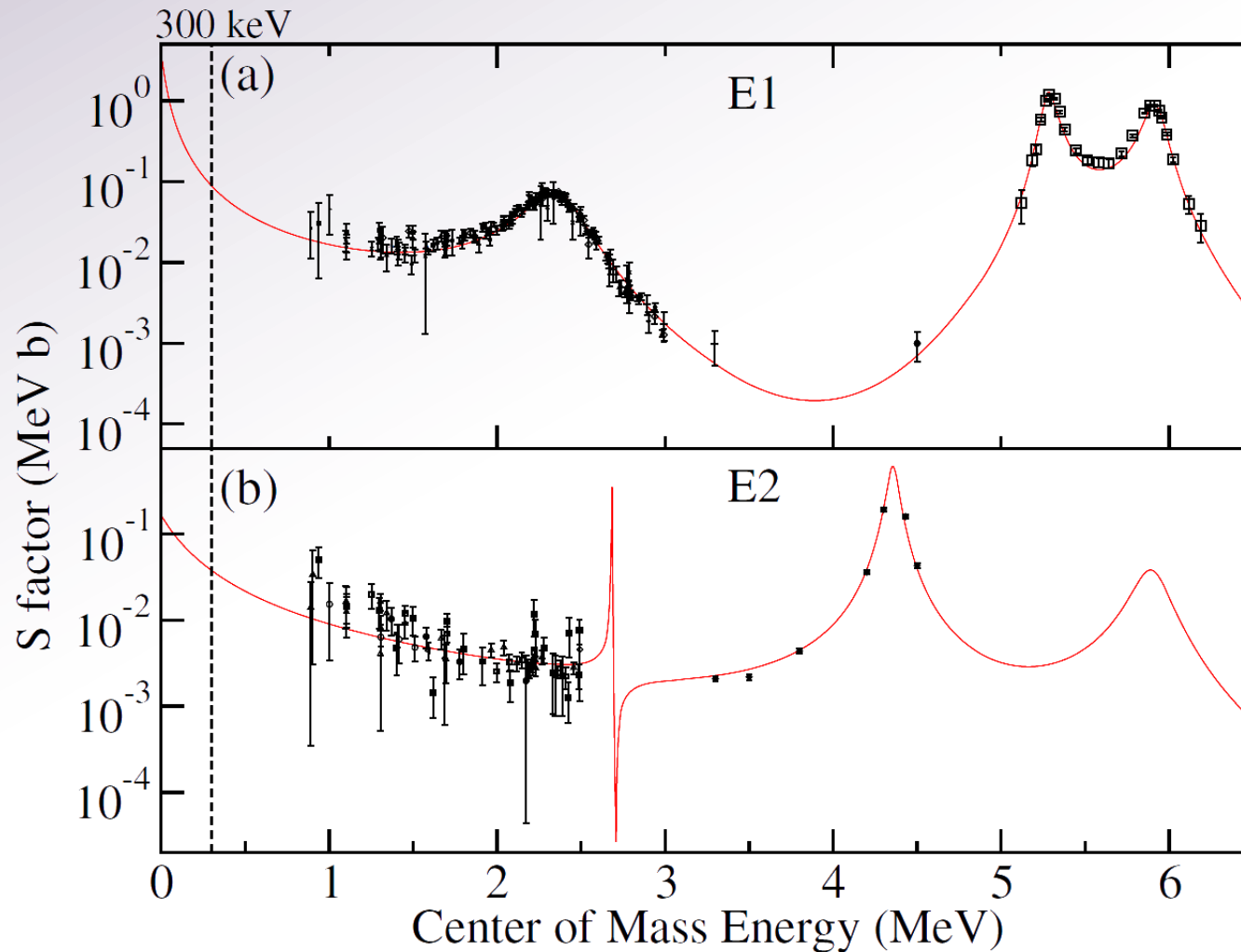
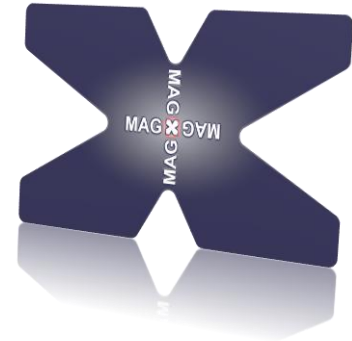
$$\sigma_{l=1} \text{ and } \sigma_{l=2}$$

Gamow-Peak

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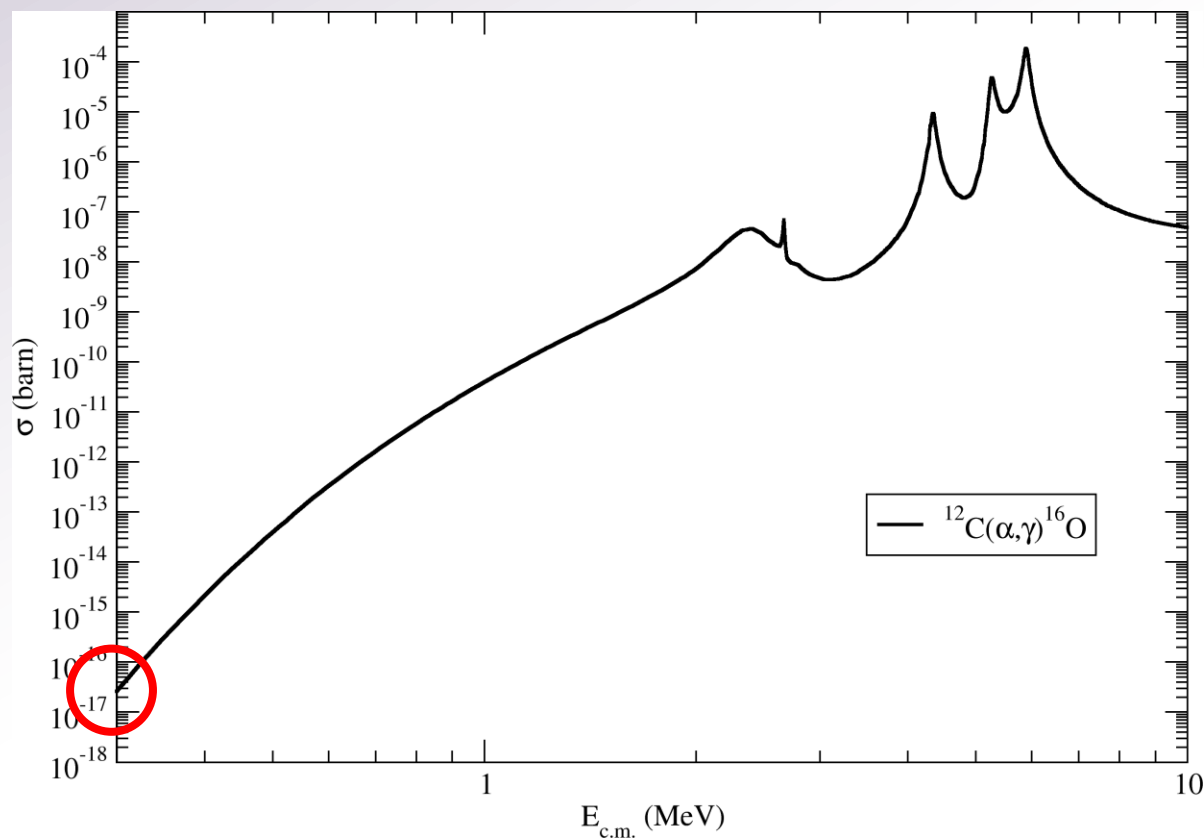
Measurement of S-Factor



Extrapolate $S(300 \text{ keV})$

- Kunz et al. (2001)
 $165 \pm 50 \text{ keV} \cdot \text{b}$
- Hammer (2005)
 $162 \pm 39 \text{ keV} \cdot \text{b}$
- Schürmann (2012)
 $161 \pm 19_{\text{stat}}^{+8}_{-2_{\text{sys}}} \text{ keV} \cdot \text{b}$

Cross Section



Measurement

- Cross section drops rapidly for $E < 1$ MeV
- $\sigma(E_0) \sim 10^{-17}$ barn
→ High luminosity necessary
- Precise low-energy measurements required

Motivation

- Direct measurements never done @ $E_{\text{cm}} < 0.9$ MeV



Feasibility Studies

Feasibility Studies at MAGIX@MESA

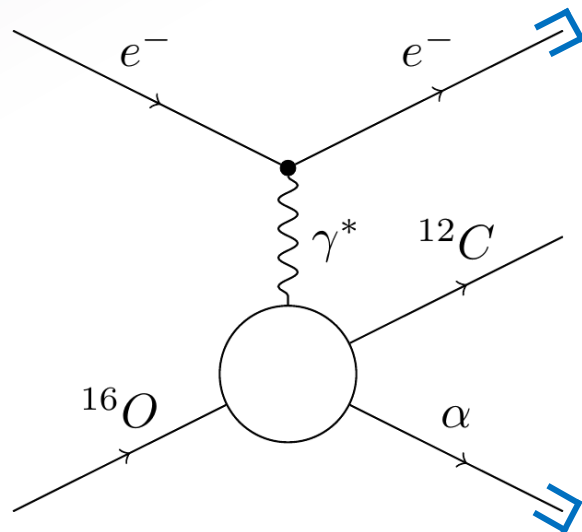


Experimental Setup

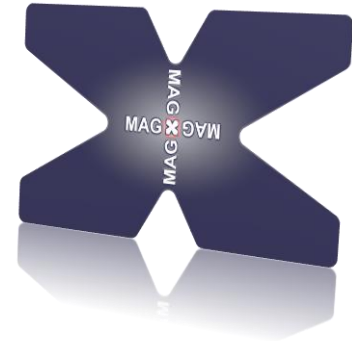
- Inelastic e^- scattering on oxygen gas with low $|q|^2$ (quasi real photons)

Measurement of Coincidence (e^-, α)

- Suppress background
- Determine α -particle angular distribution



Feasibility Studies at MAGIX@MESA

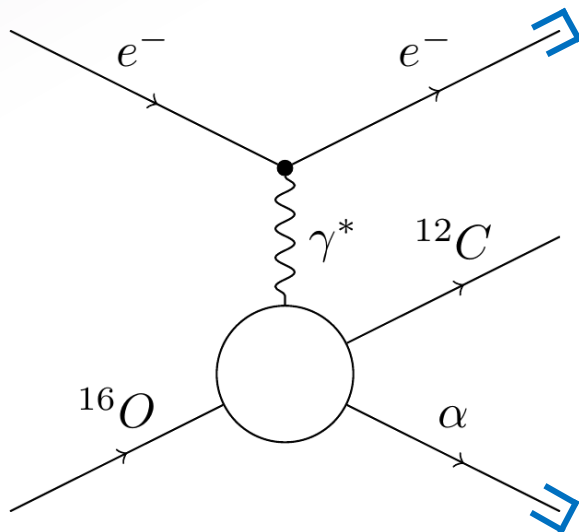


Experimental Setup

- Inelastic e^- scattering on oxygen gas with low $|q|^2$ (quasi real photons)

Measurement of Coincidence (e^-, α)

- Suppress background
- Determine α -particle angular distribution



Inelastic scattering cross section

$$\frac{d^2\sigma}{d\Omega dE'} = \frac{4\alpha^2 E'^2}{q^4} \left[W_2(q^2, \nu) \cdot \cos^2\left(\frac{\theta}{2}\right) + 2W_1(q^2, \nu) \cdot \sin^2\left(\frac{\theta}{2}\right) \right]$$

Relation between structural functions and the transversal / longitudinal part of the virtual photon cross section σ_T, σ_L

$$W_1 = \frac{\kappa}{4\pi^2\alpha} \sigma_T \quad W_2 = \frac{\kappa}{4\pi^2\alpha} \left(1 - \frac{\nu^2}{q^2}\right)^{-1} (\sigma_L + \sigma_T)$$

with
$$\kappa = \frac{W^2 - M^2}{2M}$$

For $|q^2| \rightarrow 0$: σ_L vanishes and $\sigma_T \rightarrow \sigma^{\text{tot}}(\gamma + {}^{16}\text{O} \rightarrow X)$

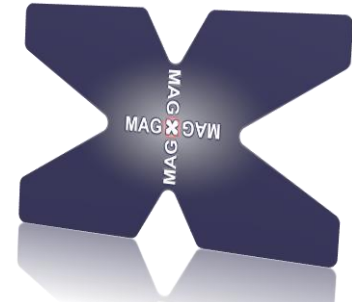
$$\frac{d^5\sigma}{d\Omega_e dE' d\Omega^*} = \Gamma \frac{d\sigma_v}{d\Omega^*}$$

with

$$\Gamma = \frac{\alpha\kappa}{2\pi^2|q^2|} \cdot \frac{E'}{E} \cdot \frac{1}{1-\varepsilon}$$

$$\varepsilon = \left(1 - 2 \frac{\nu^2 - q^2}{q^2} \tan^2\left(\frac{\theta}{2}\right)\right)^{-1}$$

Time Reversal Factor

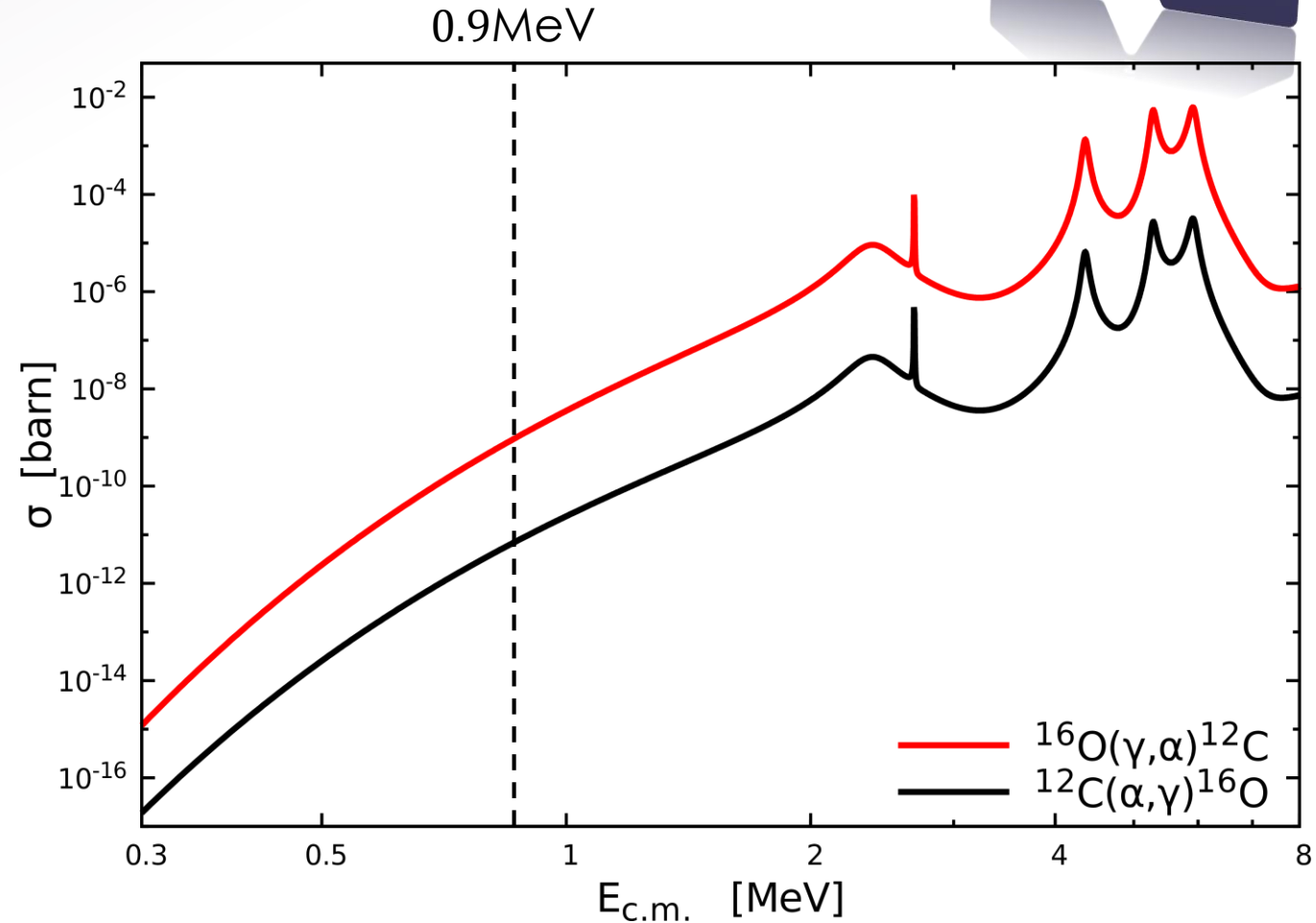
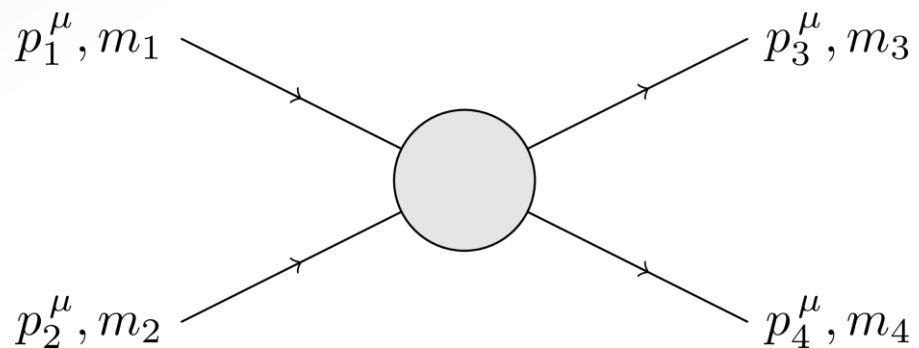


Time Reversed Reaction

- Phase space examination under T-symmetry invariance

$$\frac{\sigma_{i \rightarrow f}}{\sigma_{f \rightarrow i}} = \frac{(2I_3 + 1)(2I_4 + 1)}{(2I_1 + 1)(2I_2 + 1)} \cdot \frac{|\vec{p}|_f^2}{|\vec{p}|_i^2}$$

- Cross section gains a factor of $\times 50$



Simulation – General Setup



Spectrometer

- Minimum angular $\theta \sim 13^\circ$

α –Detector

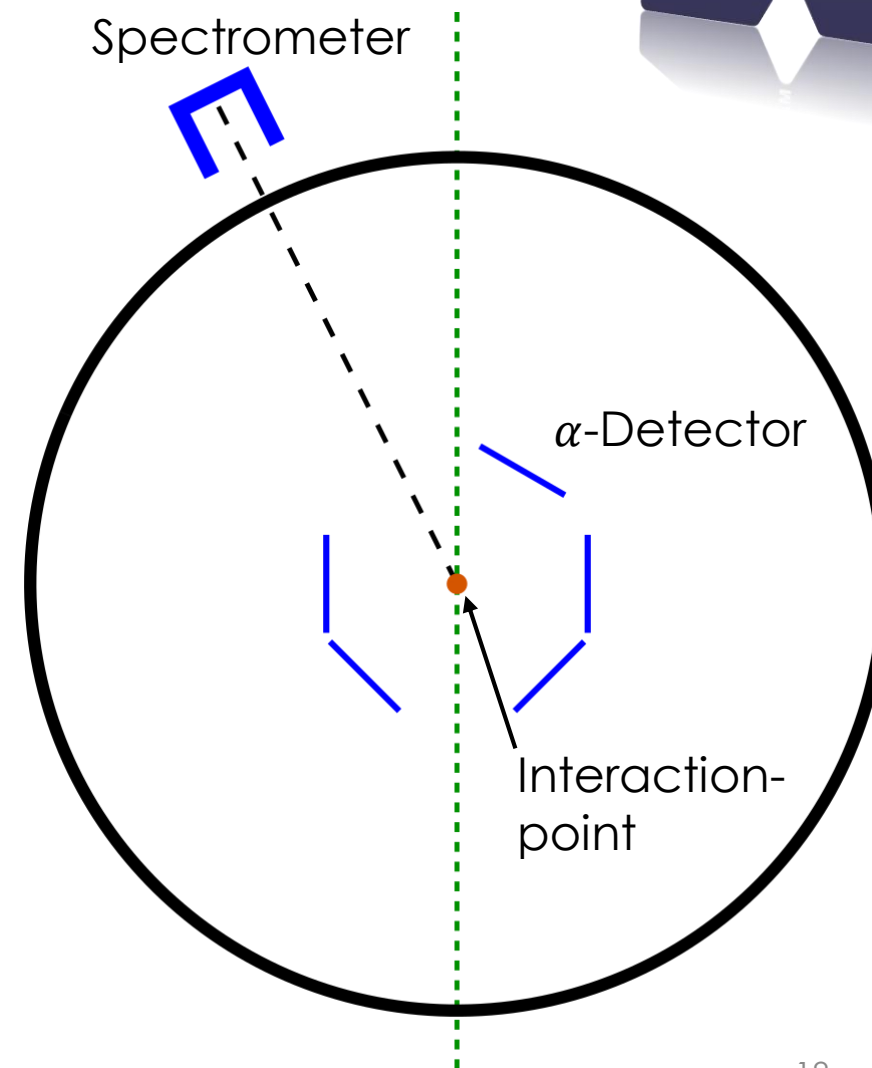
- Segmented Silicon-Detector
- $50 \times 50 \text{ mm}^2$
- 5 Detectors with $d = 10\text{cm}$
- Different angular $\theta = 30^\circ, \pm 90^\circ, \pm 120^\circ$

Oxygen Gas-Jet

- $2 \cdot 10^{18} \text{ at/cm}^2$
- Diameter = 3 mm

Parameters

- Luminosity $L \sim 10^{34} \text{ cm}^{-2}\text{s}^{-1}$
- Time $T = 4 \text{ weeks}$
- S-Factor from AZURE2 (JINA)



Phase 1 – MAGIX@MAMI

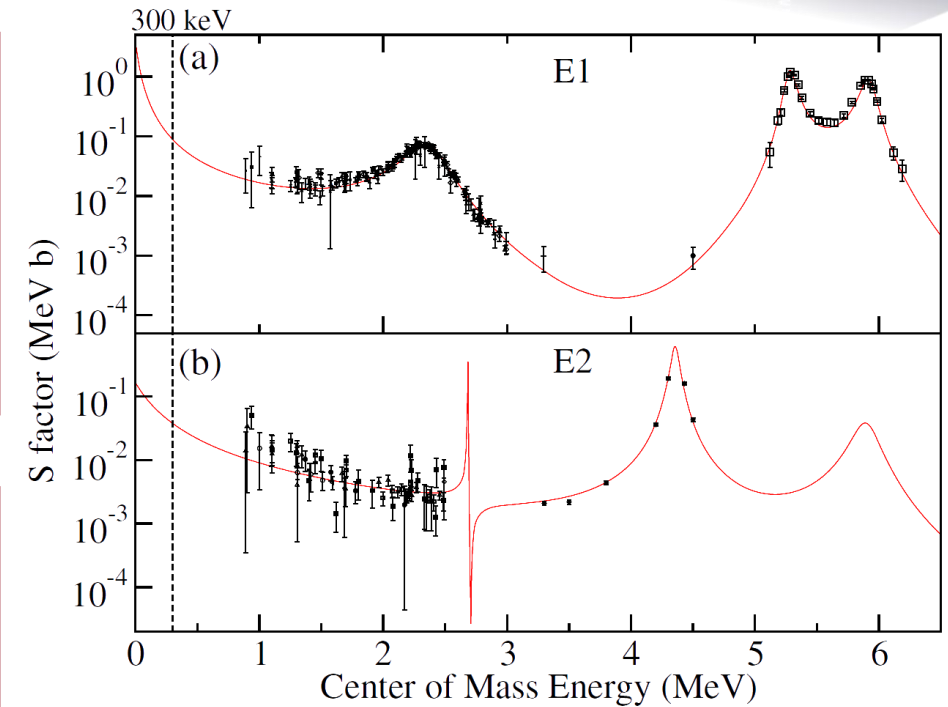


MAGIX@MAMI

- MAMI (Mainzer Microtron) is a running accelerator in Mainz
- $E = 195\text{MeV}@100\mu\text{A}$
- First experiment expected in **2020**
- **Talks: Philipp Eckert and Edoardo Mornacchi**

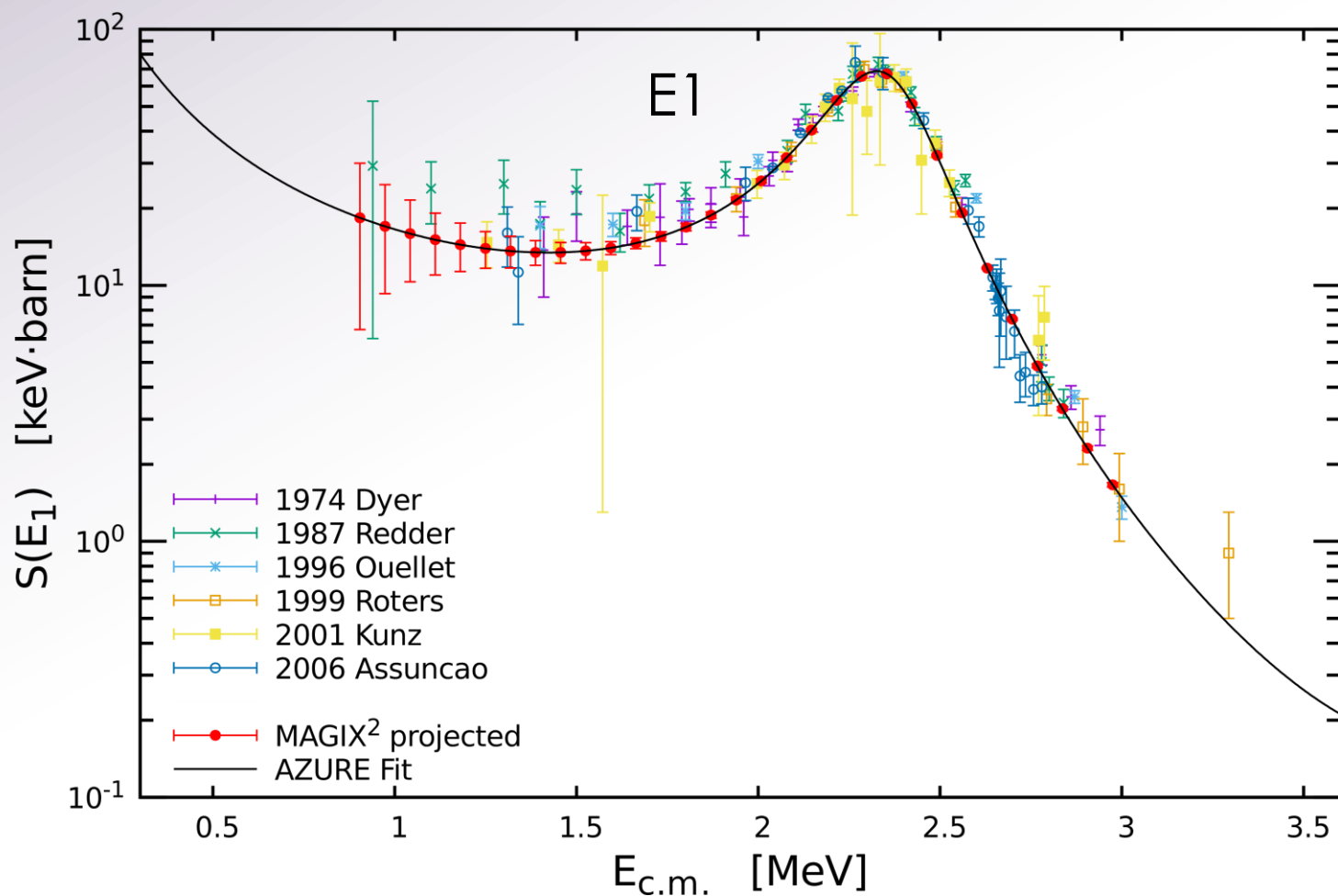
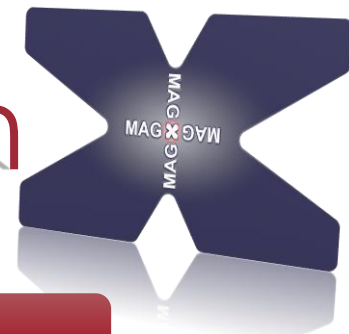
The goal

- Test Silicon-Strip Detectors for the α – particles detection
- Measurement of the cross section in the well known area of $E_{cm} > 1.8\text{ MeV}$
- Compare results with existing data
- Determine the unknown longitudinal parameter



Cp. R. deBoer et al. „The $^{12}\text{C}(\alpha; \gamma)^{16}\text{O}$ reaction and its implications for stellar helium burning”

Phase 2 – MAGIX@MESA Simulation



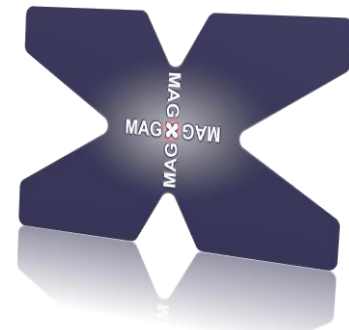
Setup

- MAGIX@MESA (expected in **2023**)
- $E = 105$ MeV@1 mA
- Spectrometer $\theta \sim 13^\circ$

Result

- We can measure the S-Factor for $E_{c.m.} > 0.9$ MeV
- Compatible precision to existing measurements
- Expected statistical errors increase significantly for $E_{c.m.} < 0.9$ MeV

How to improve this result



Increase cross section

- $$\sigma \propto \frac{E'}{E|q^2|} = \frac{1}{E^2 \sin^2 \frac{\theta}{2}}$$

Modify Parameters

- Decrease energy:

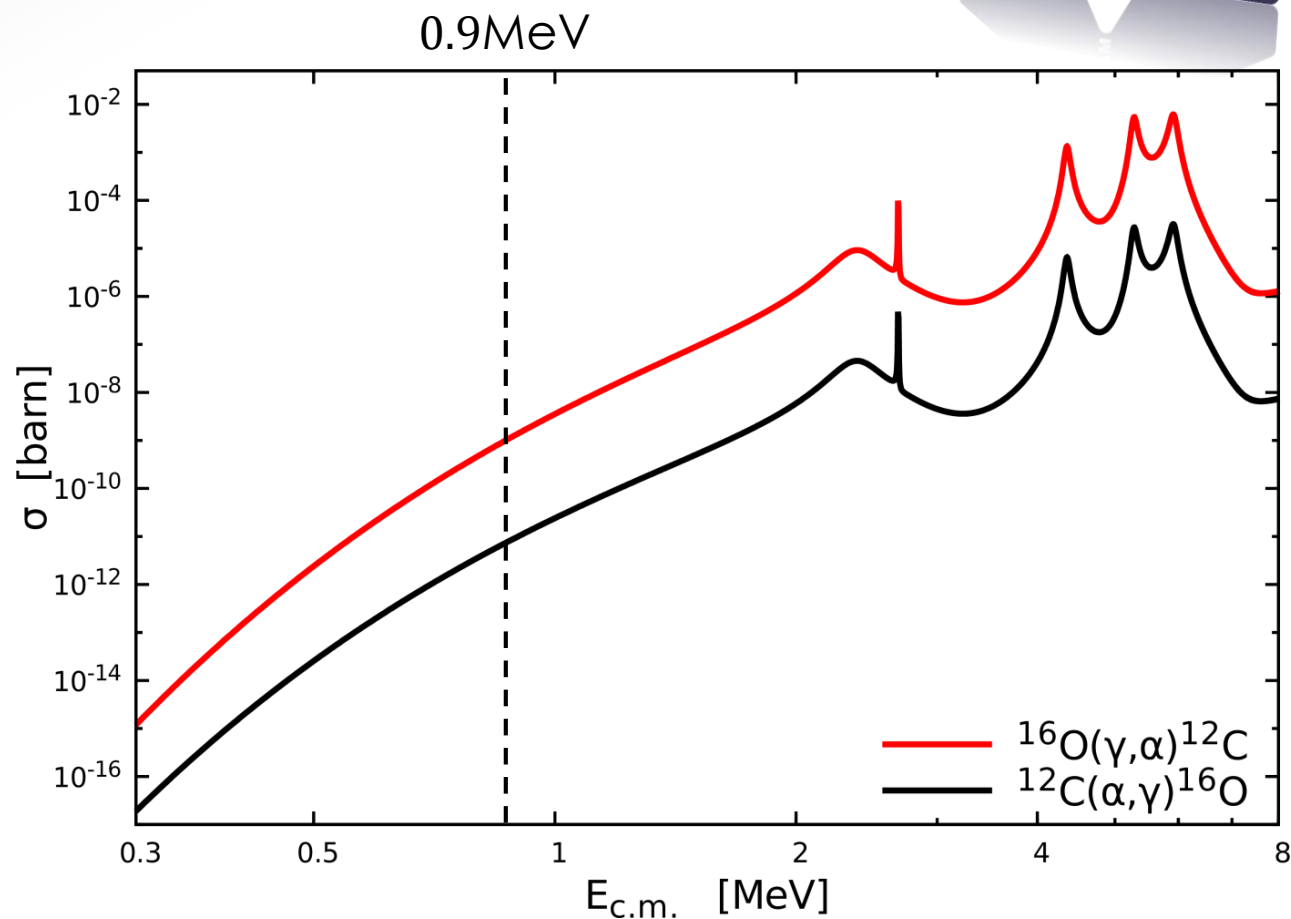
$$E = 105 \text{ MeV to } 10 \text{ MeV} \Rightarrow \sigma \times 100$$

(maximum factor)

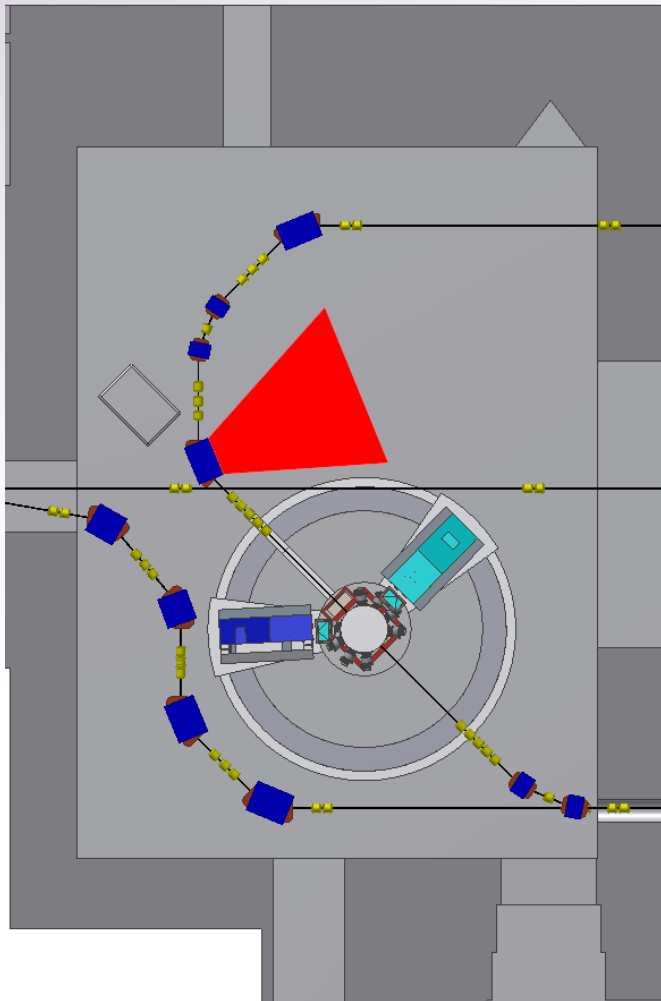
- Decrease angle:

$$\theta = 10^\circ \text{ to } 1^\circ \Rightarrow \sigma \times 100$$

$$\theta = 10^\circ \text{ to } 0.1^\circ \Rightarrow \sigma \times 1000$$



Phase 3 – Zero Degree Tagger



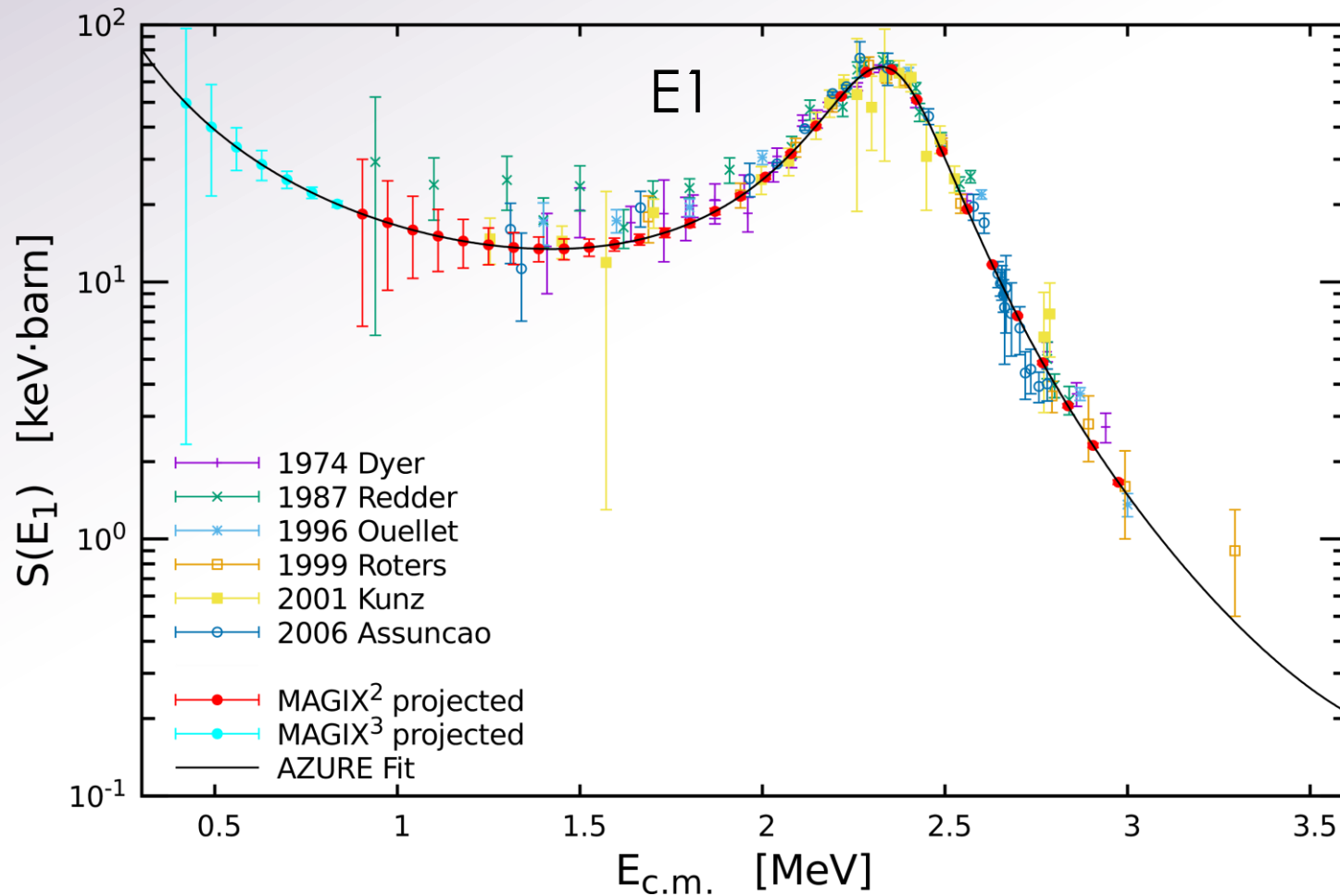
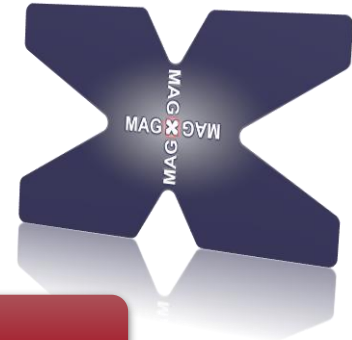
ERL Mode Integrated Tagger

- Use first deflection magnet to separate scattered electrons from beam
- Minimum Energy loss
- Theta-Acceptance $\theta_e = 0 - 0.5^\circ$

Tagger Design

- Under progress
- Special design for deflection magnet
- Deflection angle 45°
- Distance $\sim 1\text{m}$
- Width $\sim 80\text{cm}$

Phase 3 – Simulation of Zero Degree Tagger



Setup

- MAGIX@MESA
- $E = 105 \text{ MeV@1 mA}$

Zero-Degree Tagger

- Simulation uses Ideal detector
- Theta-Range $\theta_e = 0 - 0.5^\circ$

Result

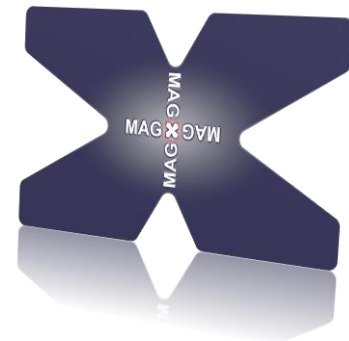
- Statistical errors much smaller for

$$E_{c.m.} > 0.5 \text{ MeV}$$



Summary/Outlook

Summary / Outlook



S-Factor of $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$

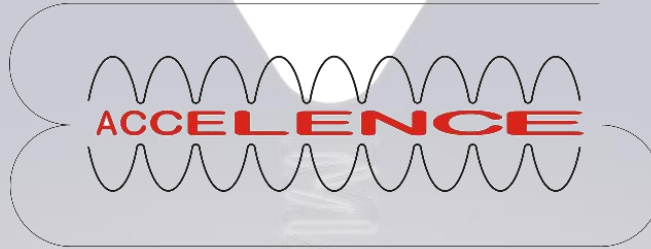
- Inelastic electron scattering on oxygen gas
- Detection of the scattered electron and the α – particle in coincidence

MAGIX²

- Spectrometer at minimum angular $\theta \sim 13^\circ$
- We can measure the S-Factor for $E_{\text{c.m.}} > 0.9 \text{ MeV}$
- Compatible precision to existing measurements

MAGIX³

- Zero Degree Tagger will improve the results
- Simulation predicts: We can measure the S-Factor for $E_{\text{c.m.}} > 0.5 \text{ MeV}$

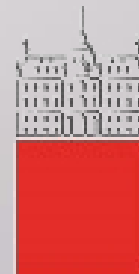


THANK YOU FOR YOUR ATTENTION!

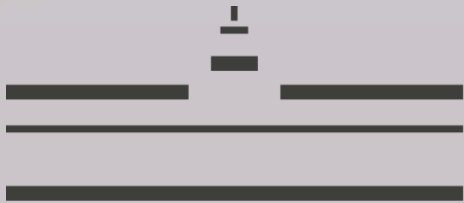
<http://magix.kph.uni-mainz.de>



**Massachusetts
Institute of
Technology**



University of Ljubljana



**WESTFÄLISCHE
WILHELMS-UNIVERSITÄT
MÜNSTER**

**JOHANNES GUTENBERG
UNIVERSITÄT MAINZ**





BACKUP

MAGIX - Spectrometers

Spectrometer

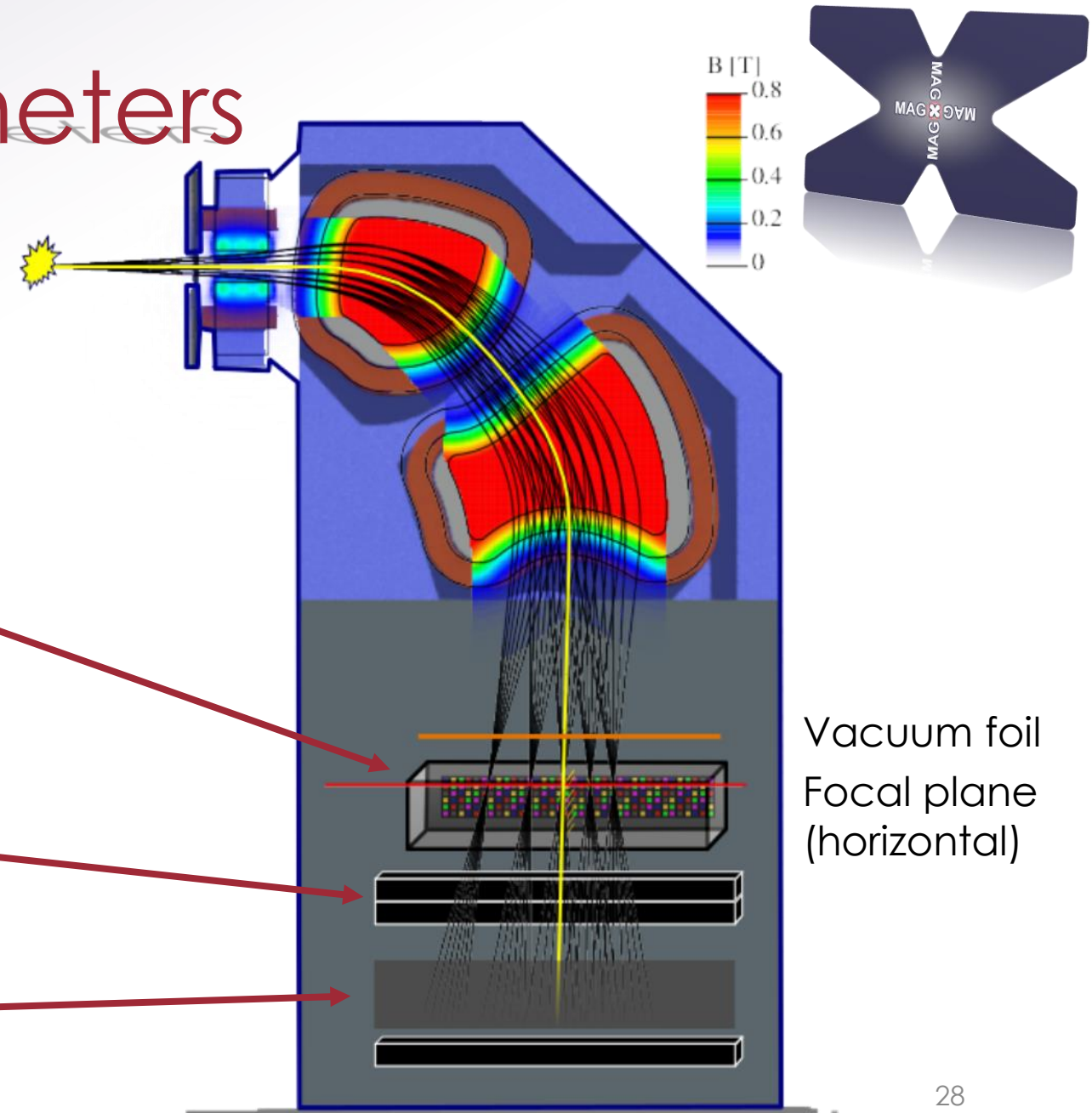
- High momentum resolution $\frac{\Delta p}{p} < 10^{-4}$
- Angular resolution $\Delta\theta < 0.05^\circ$

Time Projection Chamber

- Minimal radiation thickness
- Tracking multiple trace points
-> 5(multiplicities) x 20(rows)

Trigger-System

- Trigger, Timing and PID purposes
- 4 active segmented scintillator layers
- Lead shield in between



Time Projection Chamber

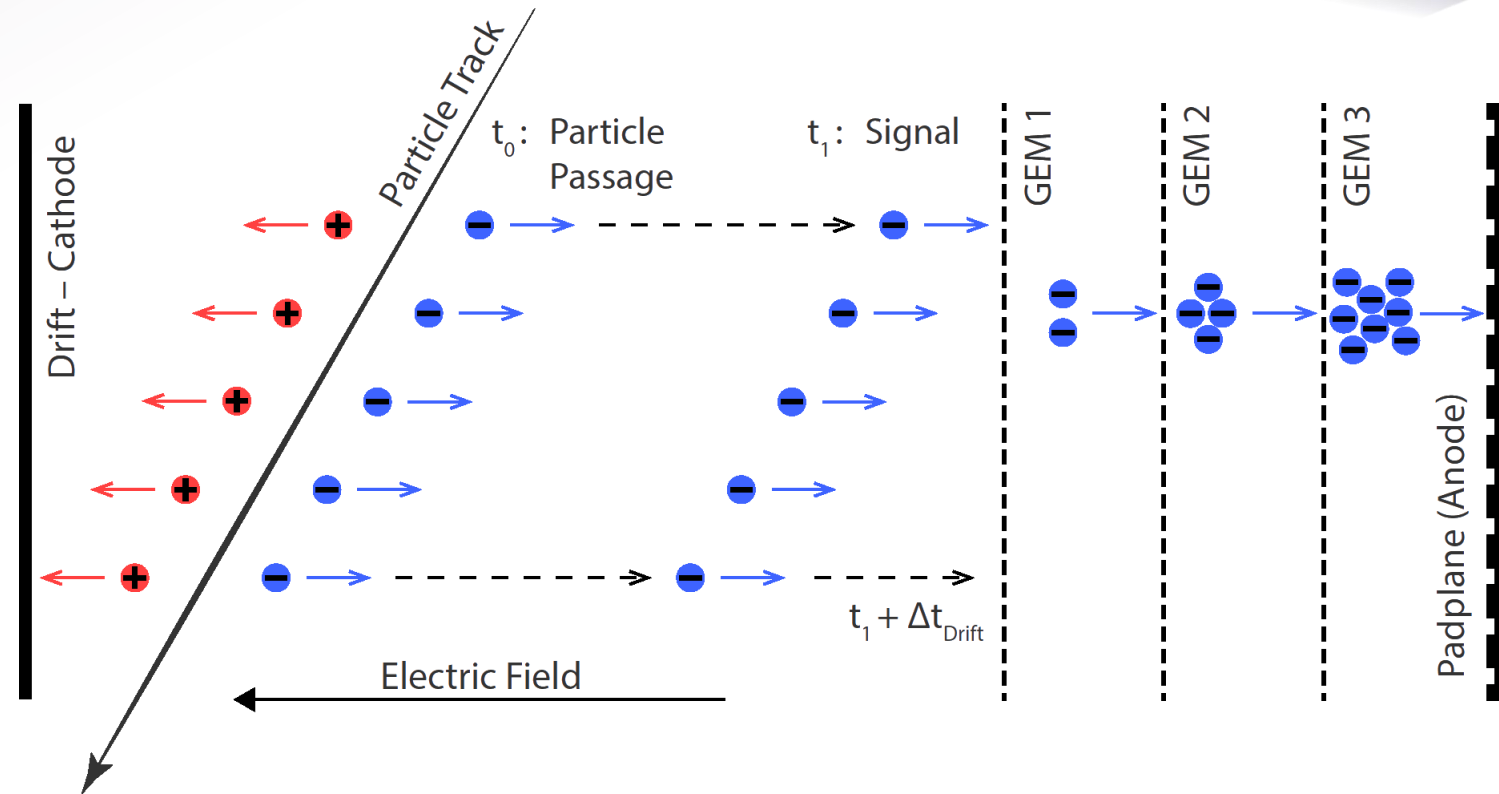


Working principle

- Particle transits active volume
- Ionisation
- Electrons drift along the E-field to readout
- GEMs amplify the electrons

3D track reconstruction

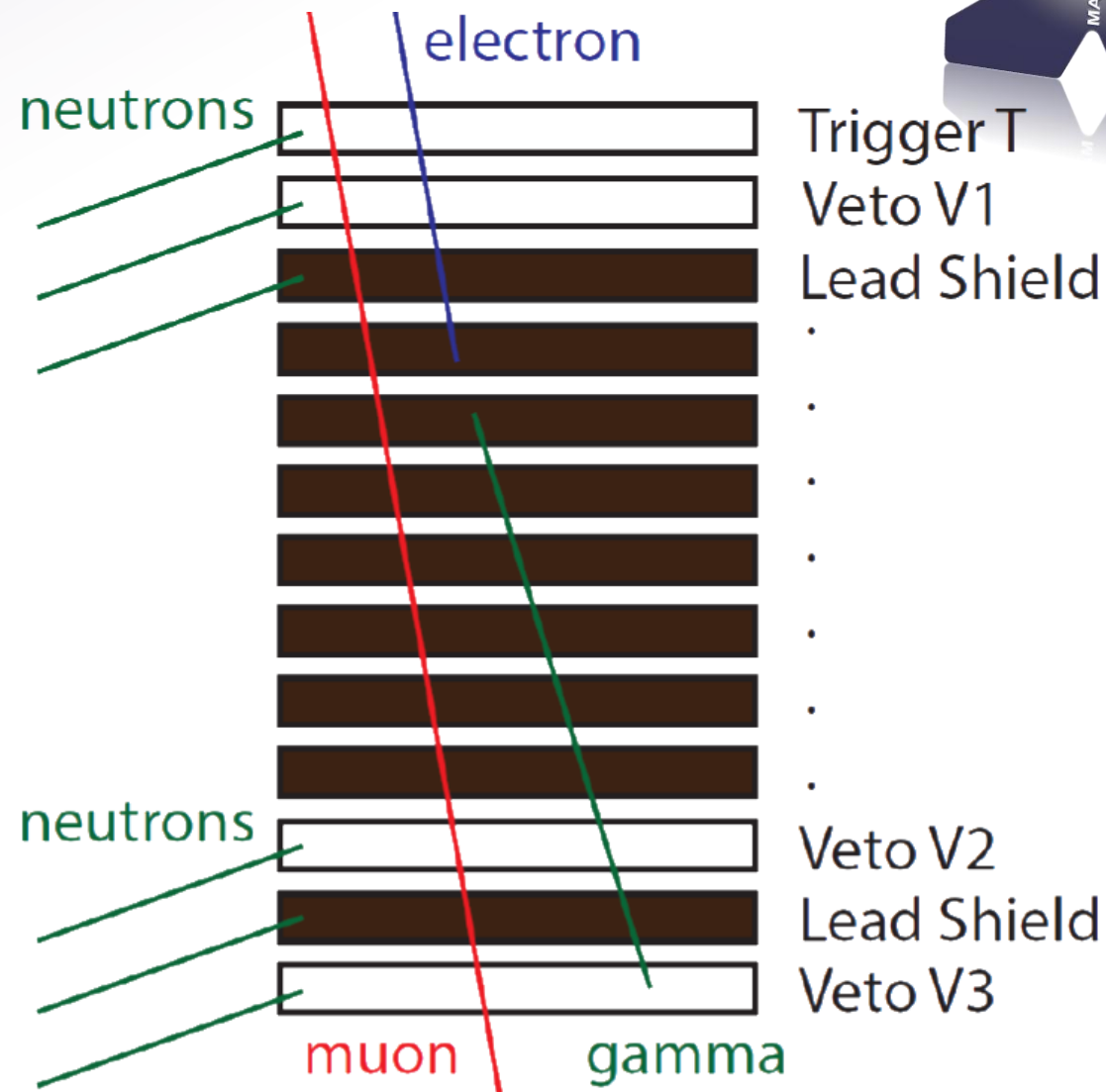
- X and Y component in readout plane
- Z component with drift time



Trigger-System

Trigger and Veto-System

- Electrons and muons point in the same direction
- Beam induced neutrons
- Different particles have different detector signatures



MAMI and MESA at KPH Mainz

MAMI

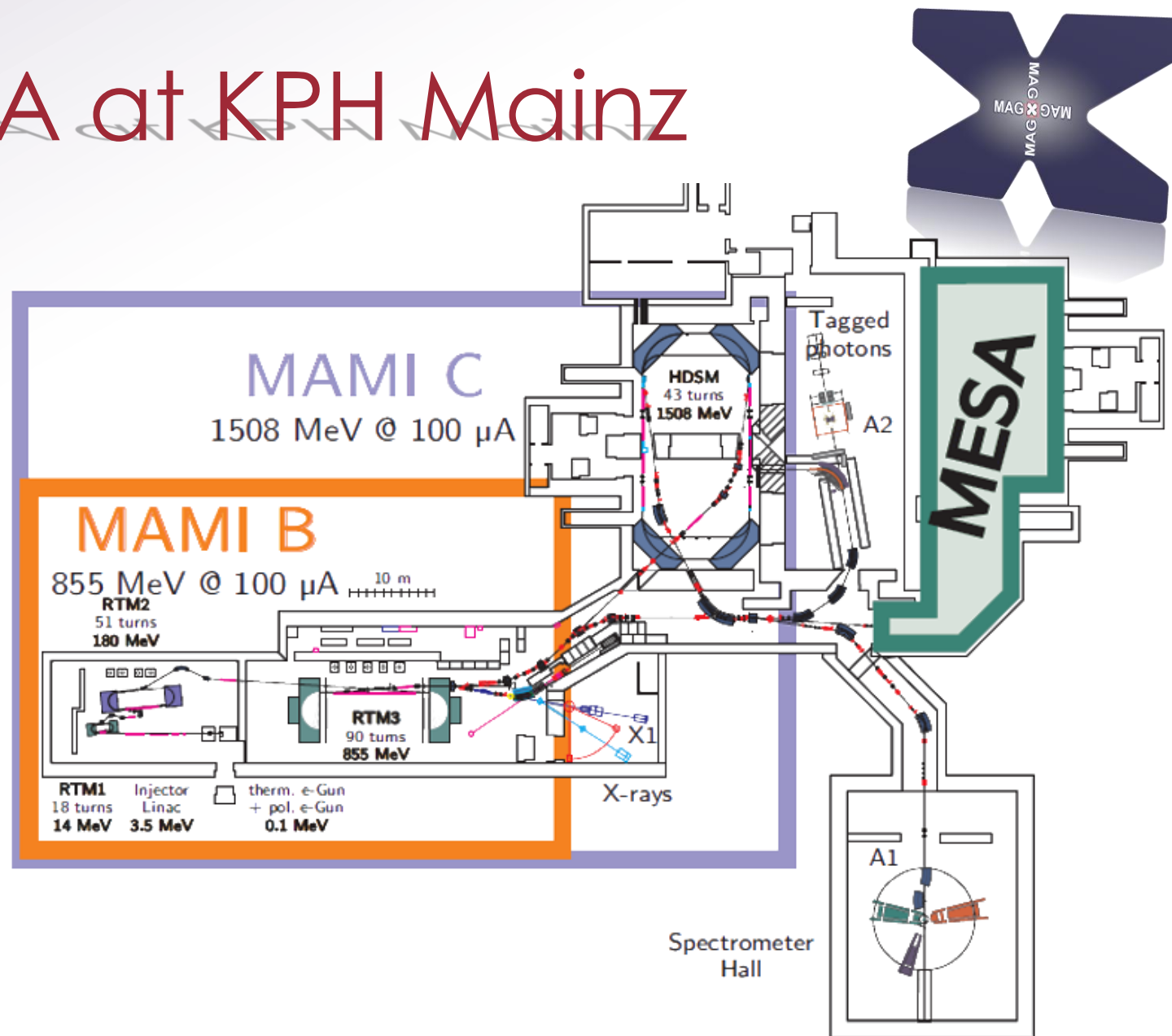
- Electron Accelerator
- Operating since >25 years
- Up to 1508 MeV @ 100 μ A

Physics

- Electron scattering
- Real photons
- X-Ray radiation

MESA

- Build in the existing facility + Extension for MESA halls



Timeline for MESA



Construction

- Construction of the extended MESA hall will delay the construction start of the accelerator and experiments to at least **2021**.

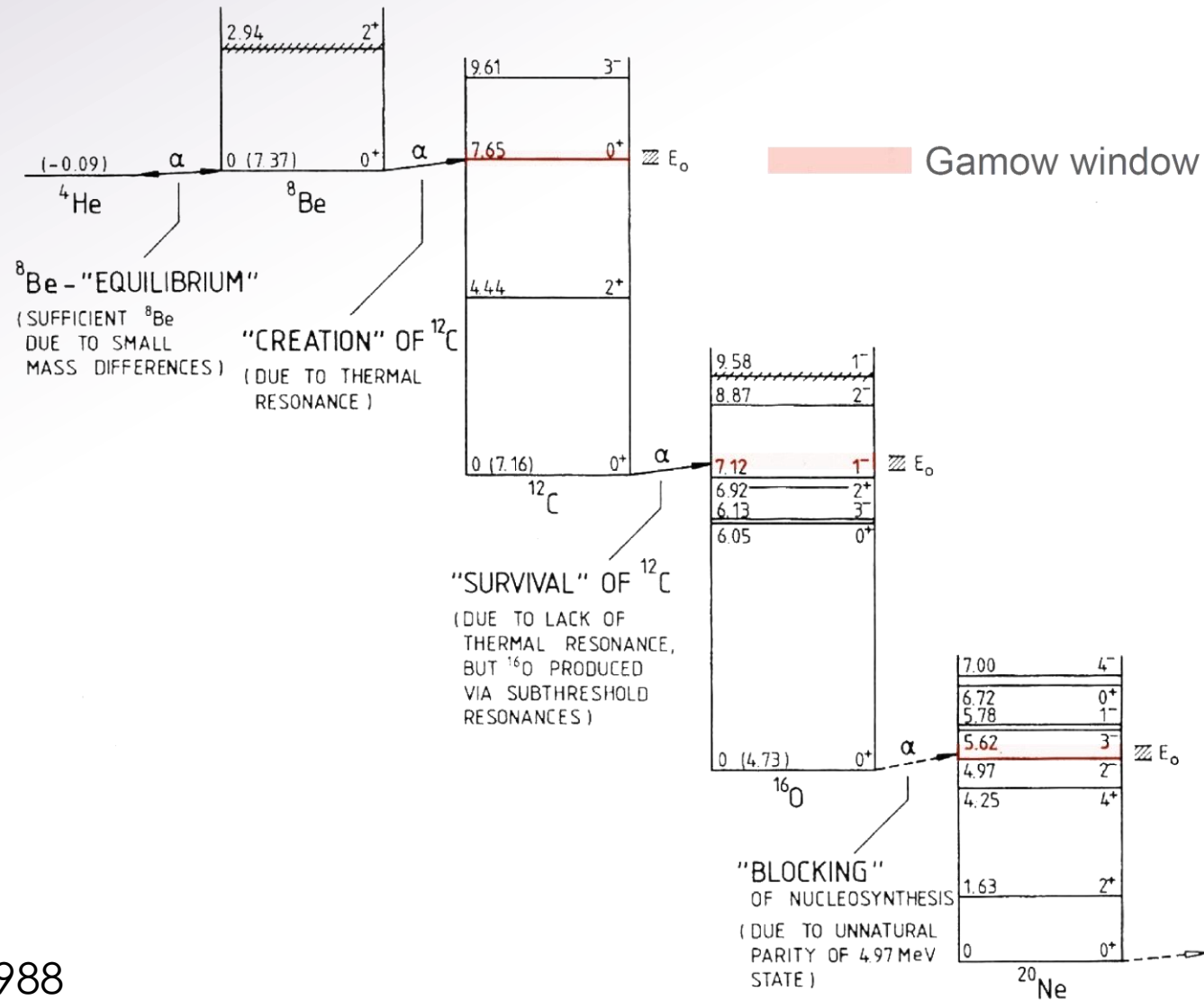
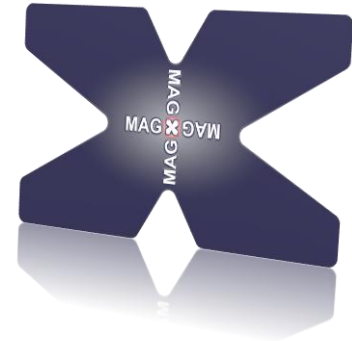
Commissioning

- Commissioning of the accelerator is planned to start in **2022**

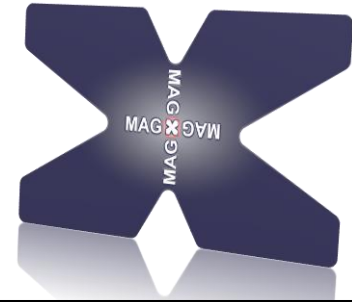
First beam

- First beam to experiments can be expected **in 2023**

Helium Burning in Red Giants



Differential cross section



$$\begin{aligned}
 & 4\pi \left(\frac{d\sigma}{d\Omega} \right)_{(\gamma, \alpha)}(E, \theta) \\
 &= \sigma_{E1}(E) [1 - P_2(\cos \theta)] \\
 &+ \sigma_{E2}(E) \left[1 + \frac{5}{7} P_2(\cos \theta) - \frac{12}{7} P_4(\cos \theta) \right] \\
 &+ 6 \cos \Phi_{12}(E) \sqrt{\frac{\sigma_{E1}(E) \sigma_{E2}(E)}{5}} [P_1(\cos \theta) - P_3(\cos \theta)]
 \end{aligned}$$

With the phase between E1 and E2

$$\Phi_{12} = \delta_d - \delta_p - \arctan \frac{\eta}{2}$$

where $\delta_{p,d}$ are the p- and d-wave phase shifts from elastic α -scattering on carbon

And the Sommerfeld parameter $\eta = \frac{Z_\alpha Z_{12C} \cdot \alpha c}{v}$

Cp. deBoer

