

– HADRON PHYSICS –

LECTURE ON SELECTED TOPICS OF THE CONFERENCE

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59th International Winter Meeting on Nuclear Physics
Bormio, January 19th, 2020

- From Hadrons to QCD → brief motivation of the fundamental theory
 - ▶ Quarks as building blocks → QCD Lagrangian
- From QCD to Hadrons → deriving expectations from QCD Lagrangian
 - ▶ e.g. Symmetries of QCD → potential models, Effective theories, Lattice
- Determination of Hadron properties
 - ▶ Methods: e^+e^- Annihilation, γ +Baryon, Hadron-Hadron Collisions, Electron Scattering
 - ▶ ⇒ Mass, Width, Decays, Quantum Numbers,
Wave-Function (Form-Factor, Polarizabilities, ...)
- Compare experiments with expectations: Exotics, ...

Invited Speakers (Hadron Physics only) Bormio 2020:

- *Christoph Blume* (University of Frankfurt)
Recent Results from HADES
- *David Hornidge* (University of Mount Allison)
Hadron polarizability measurements
- *Stefano Spatricko* (University of Torino)
Exotic results from BESIII
- *Wolfram Weise* (TU-München)
Hyperon-nuclear interactions and strangeness in neutron stars
- *Hartmut Wittig* (University of Mainz)
A glimpse of the H dibaryon from a lattice QCD perspective

The Standard Model of Elementary Particles

	mass $\approx 2.2 \text{ MeV}/c^2$	mass $\approx 1.28 \text{ GeV}/c^2$	mass $\approx 173.1 \text{ GeV}/c^2$	mass $\approx 125.09 \text{ GeV}/c^2$
charge $\frac{2}{3}$	u	c	t	H
spin $\frac{1}{2}$	up	charm	top	higgs
	$\approx 4.7 \text{ MeV}/c^2$	$\approx 96 \text{ MeV}/c^2$	$\approx 4.18 \text{ GeV}/c^2$	
charge $-\frac{1}{3}$	d	s	b	
spin $\frac{1}{2}$	down	strange	bottom	
	$\approx 0.511 \text{ MeV}/c^2$	$\approx 105.66 \text{ MeV}/c^2$	$\approx 1.7768 \text{ GeV}/c^2$	
charge -1	e	μ	τ	
spin $\frac{1}{2}$	electron	muon	tau	
	$< 2.2 \text{ eV}/c^2$	$< 1.7 \text{ MeV}/c^2$	$< 15.5 \text{ MeV}/c^2$	
charge 0	ν_e	ν_μ	ν_τ	
spin $\frac{1}{2}$	electron neutrino	muon neutrino	tau neutrino	
				GAUGE BOSONS
				SCALAR BOSONS
				VECTOR BOSONS

Quark Model

Introduced 1964 by Gell-Mann/Zweig to clean up “particle zoo”

Mesons as Quark-Antiquark Pair:

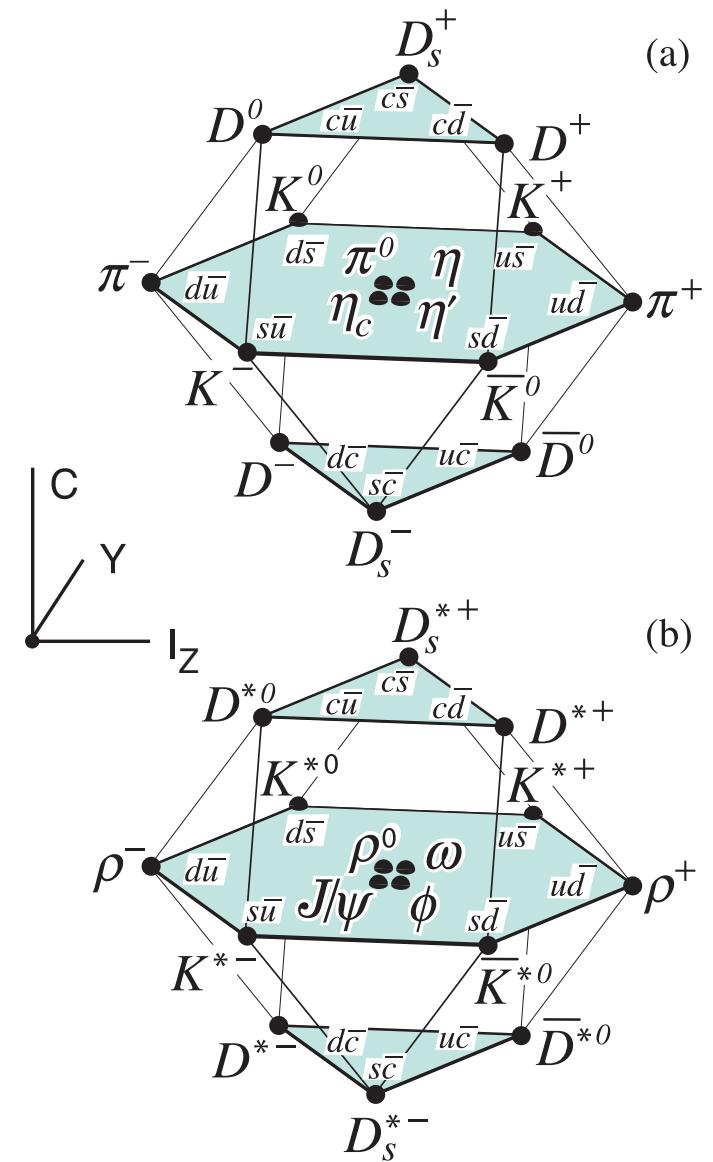
Pions:

π^+	π^0	π^-	η_1
$ u\bar{d}\rangle$	$\frac{1}{\sqrt{2}}(u\bar{u}\rangle - d\bar{d}\rangle)$	$ d\bar{u}\rangle$	$\frac{1}{\sqrt{2}}(u\bar{u}\rangle + d\bar{d}\rangle)$

Kaons:

K^+	K^0	\bar{K}^0	K^-
$ u\bar{s}\rangle$	$ s\bar{u}\rangle$	$ u\bar{s}\rangle$	$ s\bar{u}\rangle$

... 6 flavours \rightarrow 36 Mesons?



C: Charm, Y: Hypercharge, I_z : Isospin

Baryons

Baryons as three quark states

Examples:

$$p : |u \uparrow u \downarrow d \uparrow\rangle$$

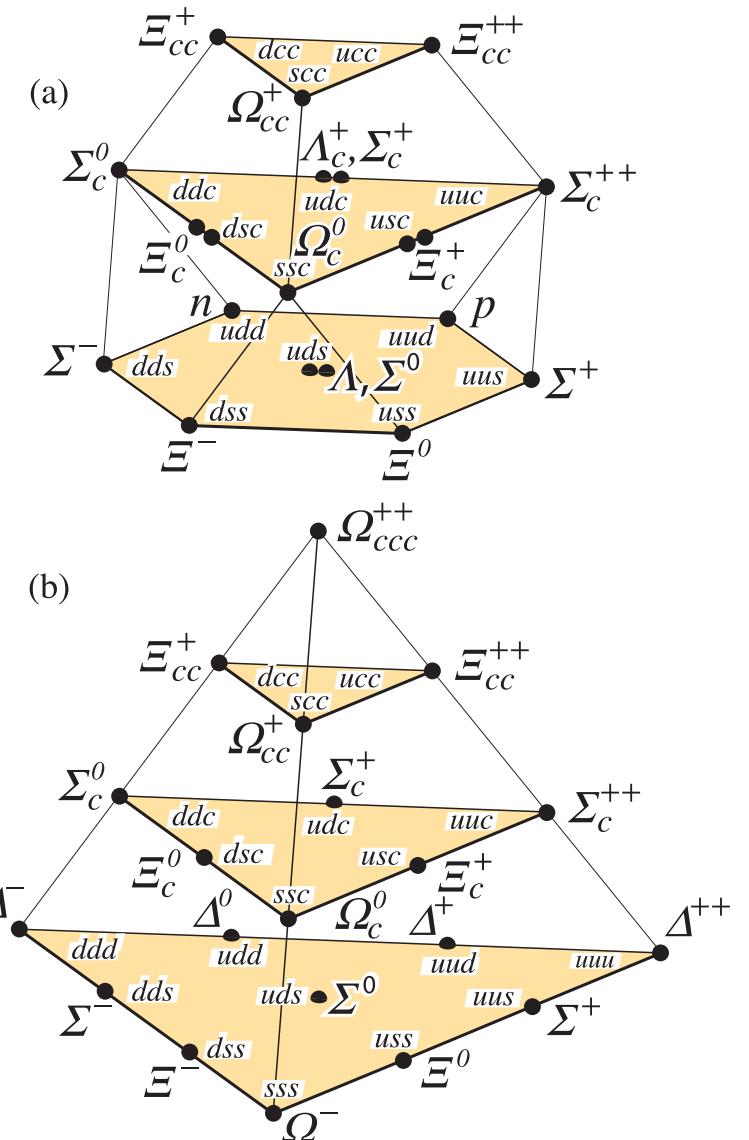
$$n : |u \uparrow d \downarrow d \uparrow\rangle$$

$$\Delta(1232) : |u \uparrow u \uparrow d \uparrow\rangle$$

$$\Lambda : |u \uparrow d \downarrow s \uparrow\rangle$$

...

Ground states are OK, excited states?



Color

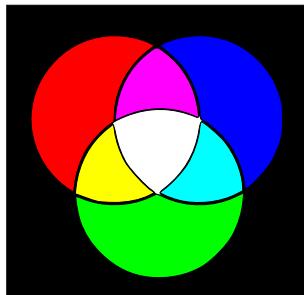
Problem: Δ^{++} with angular momentum $J = \frac{3}{2}$:

$$\Delta^{++} = \underbrace{|uuu\rangle}_{\text{flavour}} \cdot \underbrace{|\uparrow\uparrow\uparrow\rangle}_{\text{spin}} \cdot \underbrace{|l=0\rangle}_{\text{orbital } l}$$

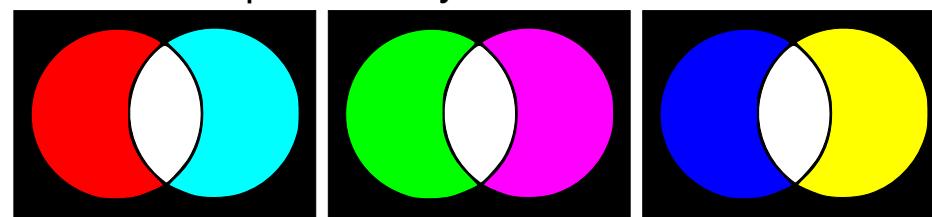
- Not possible for Fermions \rightarrow additional antisymmetric charge necessary
- Not visible for three- and two-quark states

Color Analogy:

Three colors:
Primary Colors



Two Colors:
Color – complementary Color



Physical objects are colorless (*i.e.* $SU(3)$ Color-Singulets):

Baryons: red–green–blue triplets

$$|qqq\rangle = \sqrt{\frac{1}{6}}(|RGB\rangle - |RBG\rangle + |BRG\rangle - |BGR\rangle + |GBR\rangle - |GRB\rangle)$$

Mesons: color–anti-color pairs

$$|q\bar{q}\rangle = |R\bar{R}\rangle + |G\bar{G}\rangle + |B\bar{B}\rangle$$

$\Rightarrow SU(3)$ Symmetry of Gluons

QCD Lagrangian

Lagrangian field theory:

$$L = T - V \quad \text{and} \quad \text{Lagrange's Equation} \quad \frac{d}{dt} \left(\frac{\partial L}{\partial \dot{q}_i} \right) - \frac{\partial L}{\partial q_i} = 0$$

$$\text{or with continuous field } \phi(x_\mu) \quad \frac{\partial}{\partial x_\mu} \left(\frac{\partial \mathcal{L}}{\partial (\partial \phi / \partial x_\mu)} \right) - \frac{\partial \mathcal{L}}{\partial \phi} = 0$$

Only two ingredients for \mathcal{L}_{QCD} :

- Quarks are massive spin $\frac{1}{2}$ particles \Rightarrow Dirac equation for free lagrangian

$$\mathcal{L}_0 = \bar{q}_j (i\gamma^\mu \partial_\mu - m) q_j$$

- Gauge invariant under $SU(3)$ color symmetry

i.e. invariant under local phase rotation: $q(x) \rightarrow e^{i\alpha_a(x)T_a} q(x)$ with eight 3×3 matrices T_a

$$\mathcal{L}_{\text{QCD}} = \bar{q}(i\gamma^\mu \partial_\mu - m)q - g(\bar{q}\gamma^\mu T_a q) G_\mu^a - \frac{1}{4}G_{\mu\nu}^a G_a^{\mu\nu}$$

with 8 massless vector gauge fields transforming like

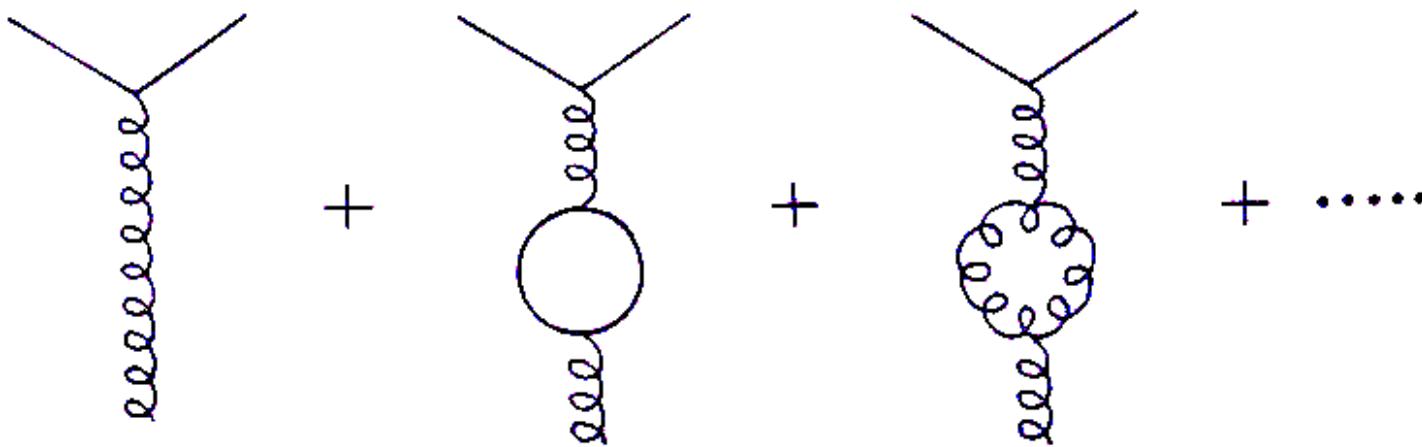
$$G_\mu^a \rightarrow G_\mu^a - \frac{1}{g} \partial_\mu \alpha_a - f_{abc} \alpha_b G_\mu^c$$

gauge field strength tensor

$$G_{\mu\nu}^a = \partial_\mu G_\nu^a - \partial_\nu G_\mu^a - g f_{abc} G_\mu^b G_\nu^c$$

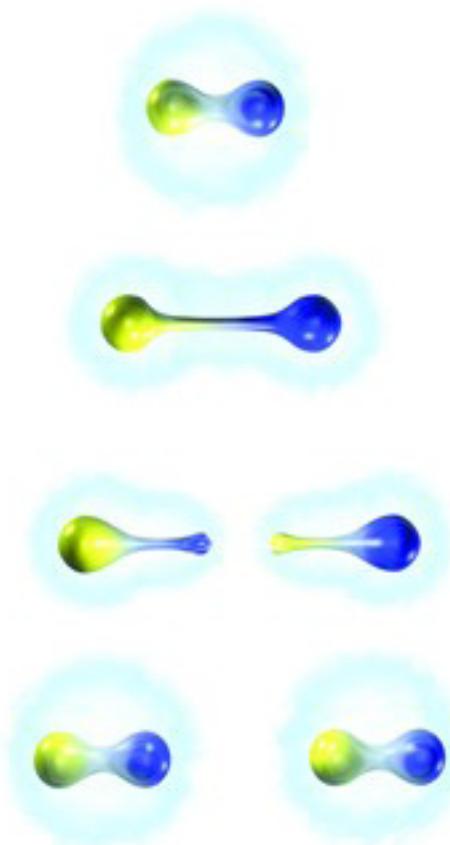
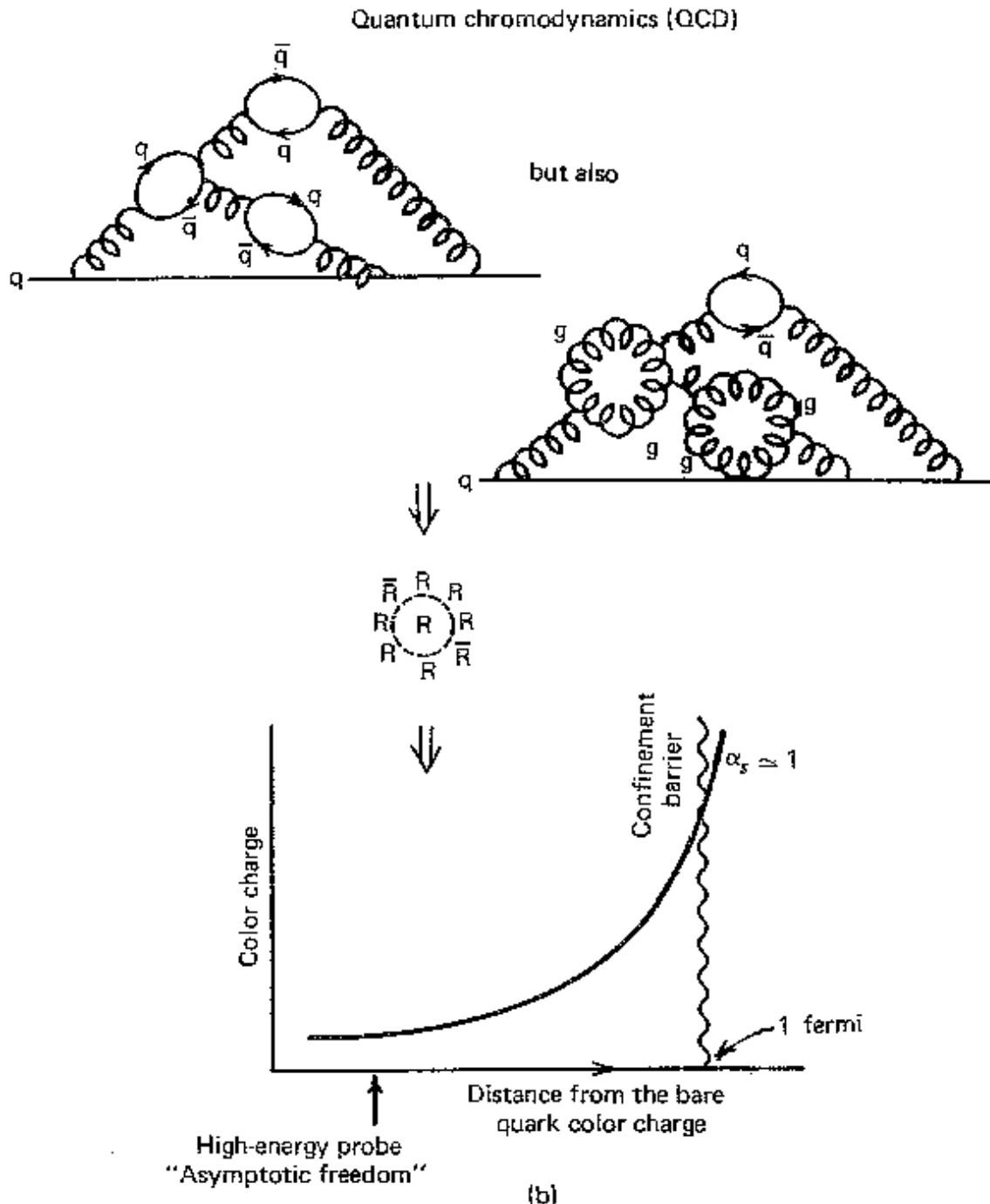
$SU(3)$ structure constants given by $[T_a, T_b] = i f_{abc} T_c \Rightarrow$ “non abelian”

Charge Screening

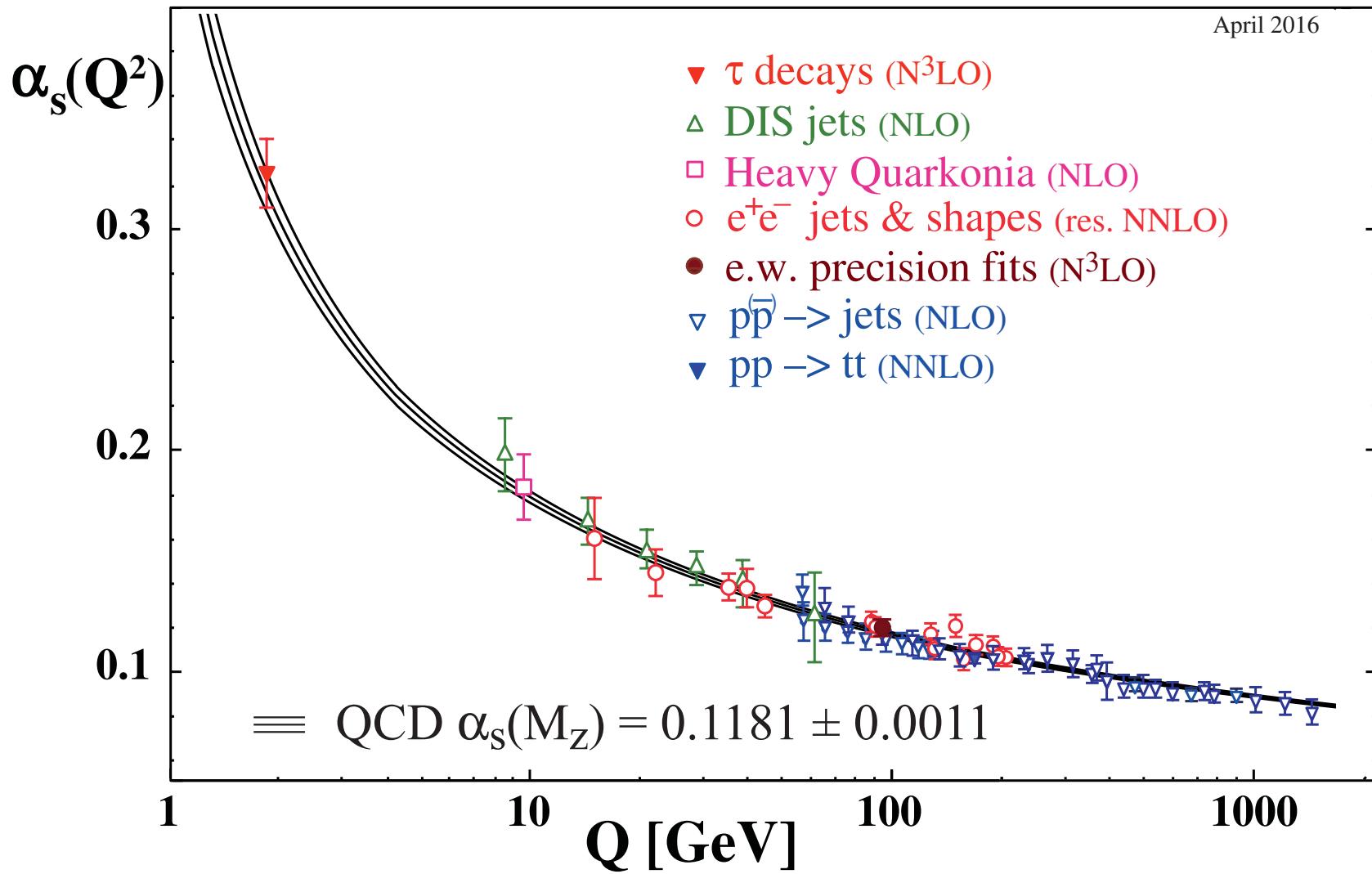


- Quark loops like lepton loops in QED
- For each flavour, large mass suppressed
- Additional:
 - ▶ Gluon Loops
 - ▶ Large contribution: 8 gluons
 - ▶ opposite sign!

Strong Coupling Constant

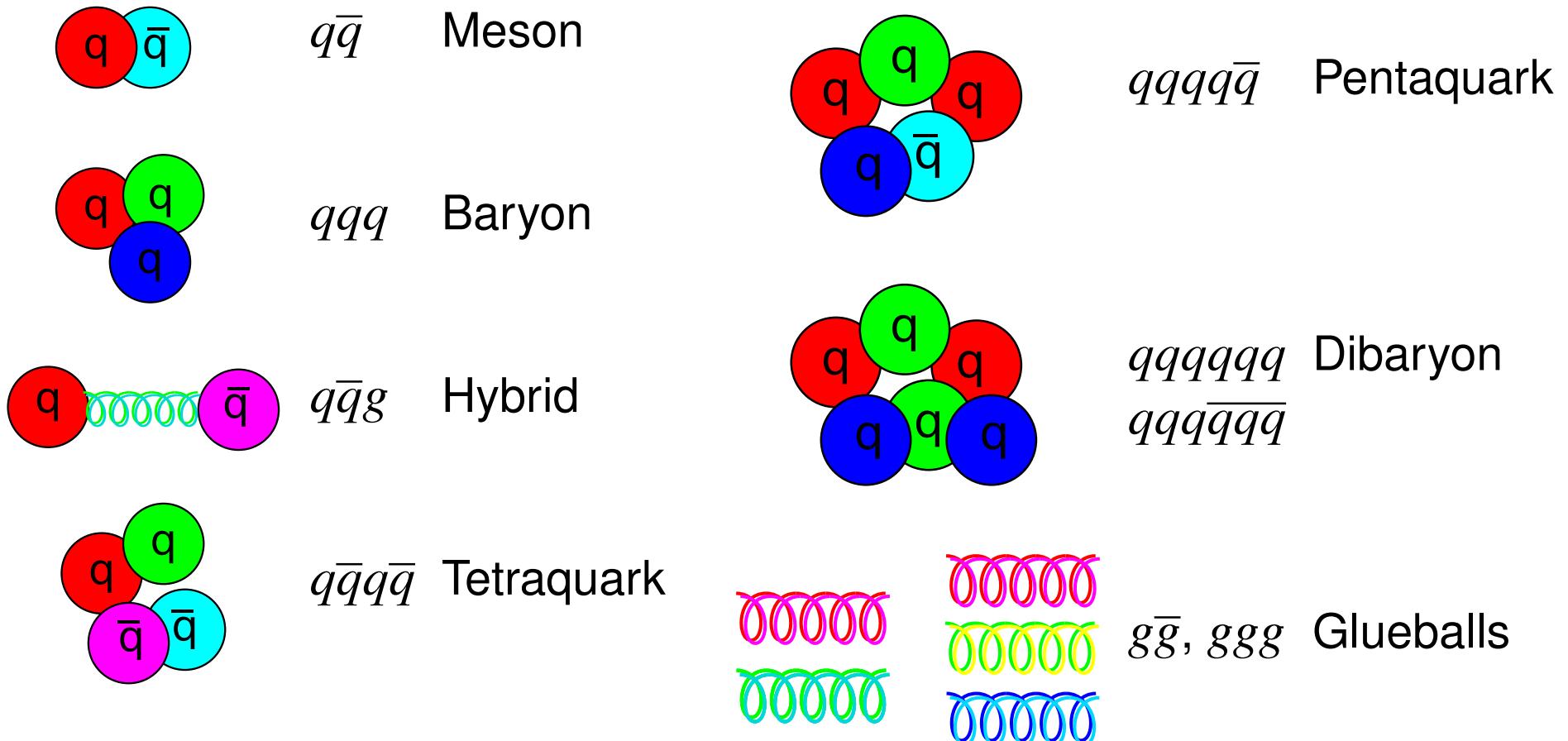


Strong Coupling Constant



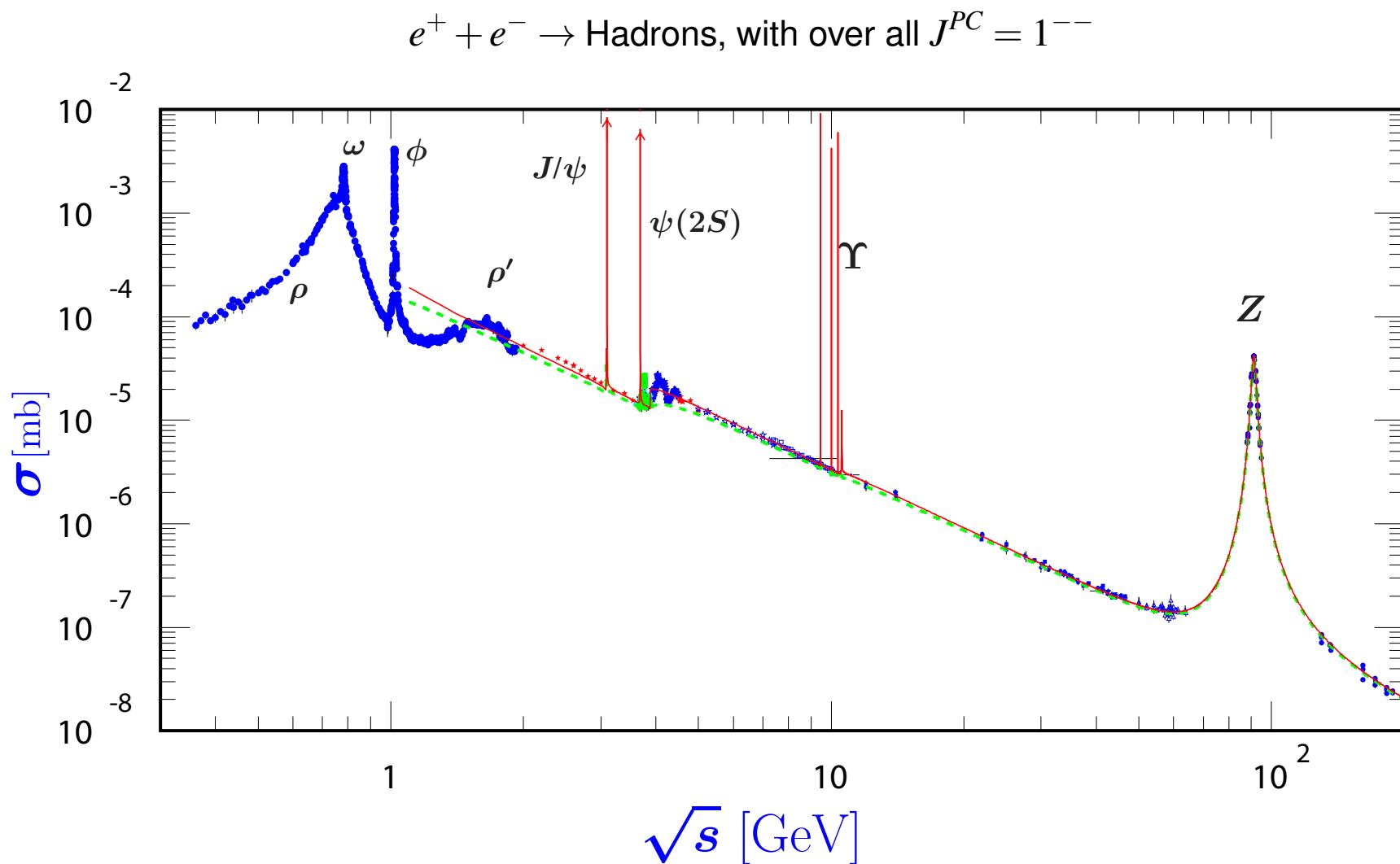
⇒ running of α_s ⇒ non-abelian structure of QCD!

Possible Quark States



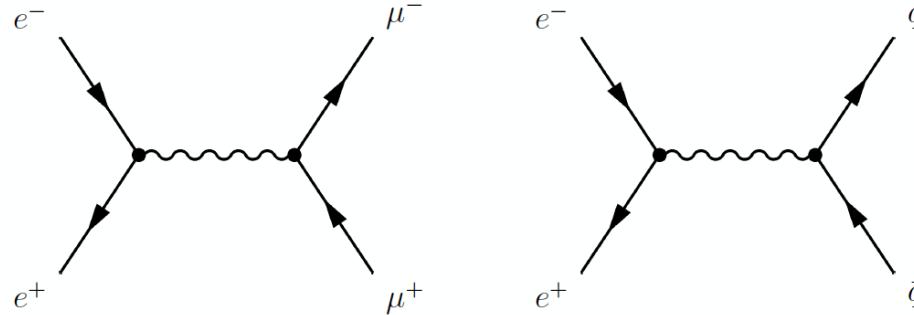
- Not only $q\bar{q}$ and qqq states \Rightarrow a new zoo of “Exotics” is expected!
- Important for most of them: “Color-Singulet” does not mean “white”!
Two singulets are always decoupled \rightarrow non-trivial binding (e.g. “white” exchange) necessary

e^+e^- Annihilation: Cross Section



e^+e^- Annihilation: general features

Idea: Relate $q\bar{q}$ cross section to known (i.e. QED) cross section (μ to be distinguishable from e):



$\mu^+\mu^-$ cross section from QED:

$$\sigma(e^+e^- \rightarrow \mu^+\mu^-) = \frac{4\pi\alpha^2}{3s}$$

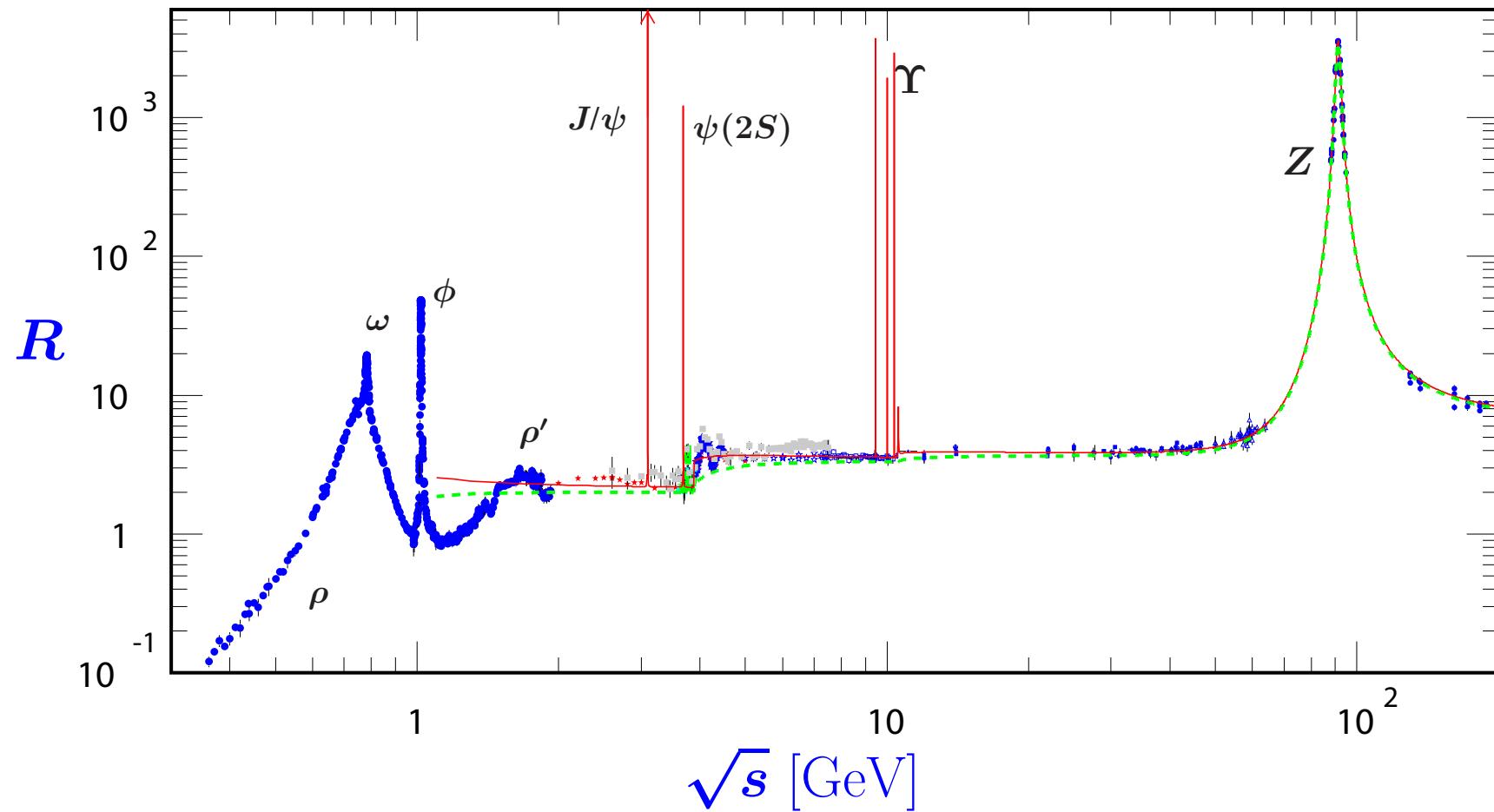
$q\bar{q}$ cross section (also only QED!):

$$\sigma(e^+e^- \rightarrow q\bar{q}) = N_c e_q^2 \sigma(e^+e^- \rightarrow \mu^+\mu^-)$$

$$\text{with } e_q = \begin{cases} -\frac{1}{3} & \text{for } q = d, s, b \\ +\frac{2}{3} & u, c, t \end{cases}$$

and $N_c = 3$ number of colors.

$$R = \frac{\sigma(e^+e^- \rightarrow \text{Hadrons})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)} = \sum_q 3e_q^2$$

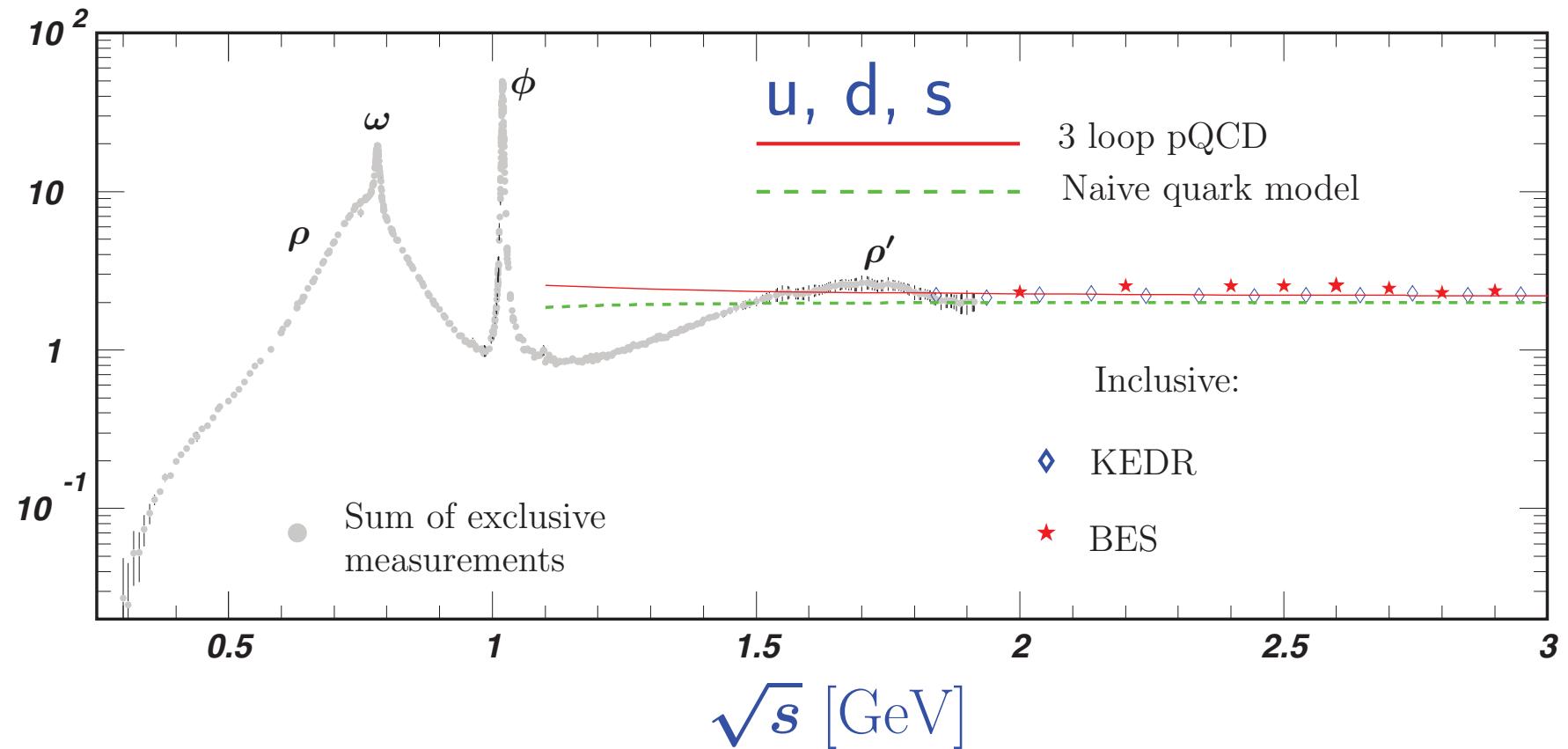


- with QCD corrections: $R = \sum_q 3e_q^2 \left(1 + \frac{\alpha_s(Q^2)}{\pi}\right)$

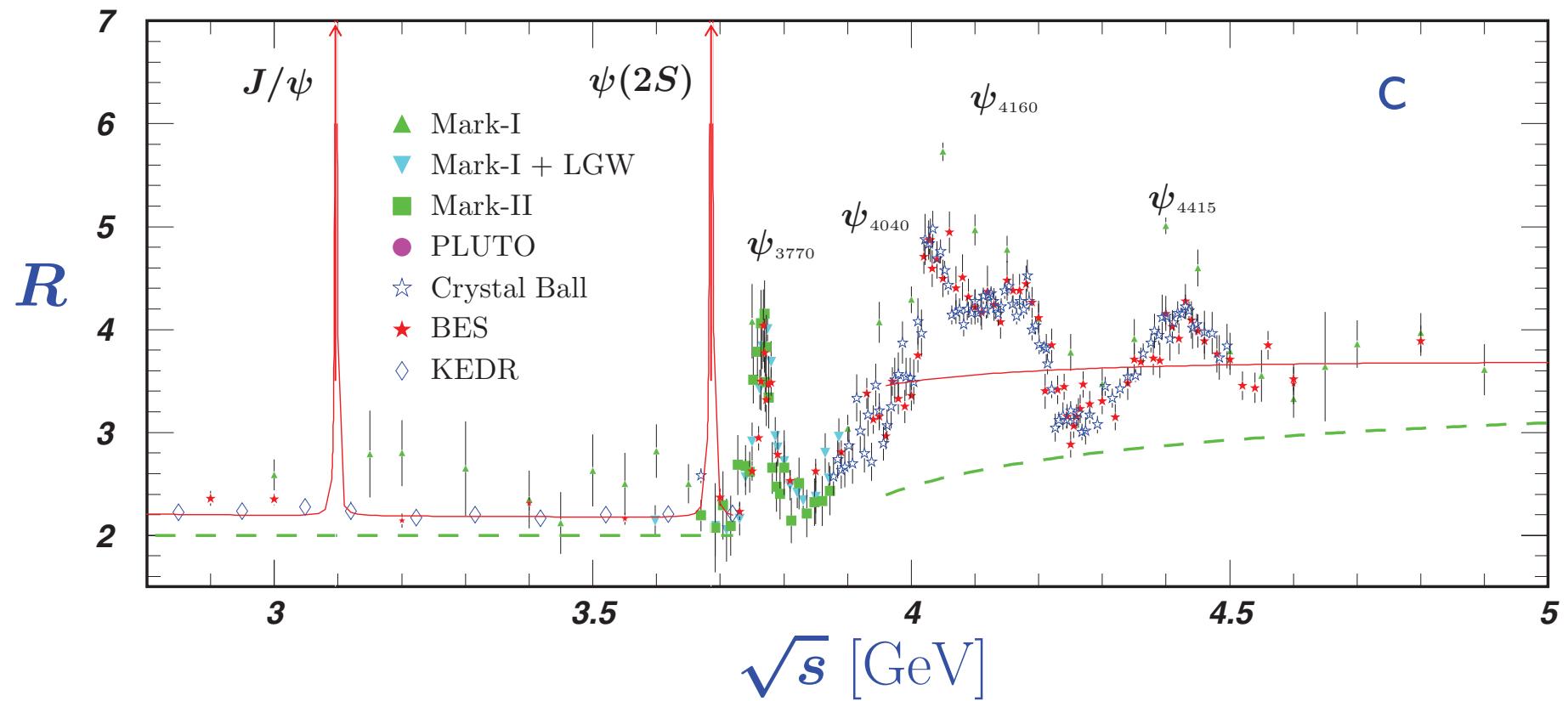
- confirms quark charge

- confirms (again) $N_c = 3$ colors

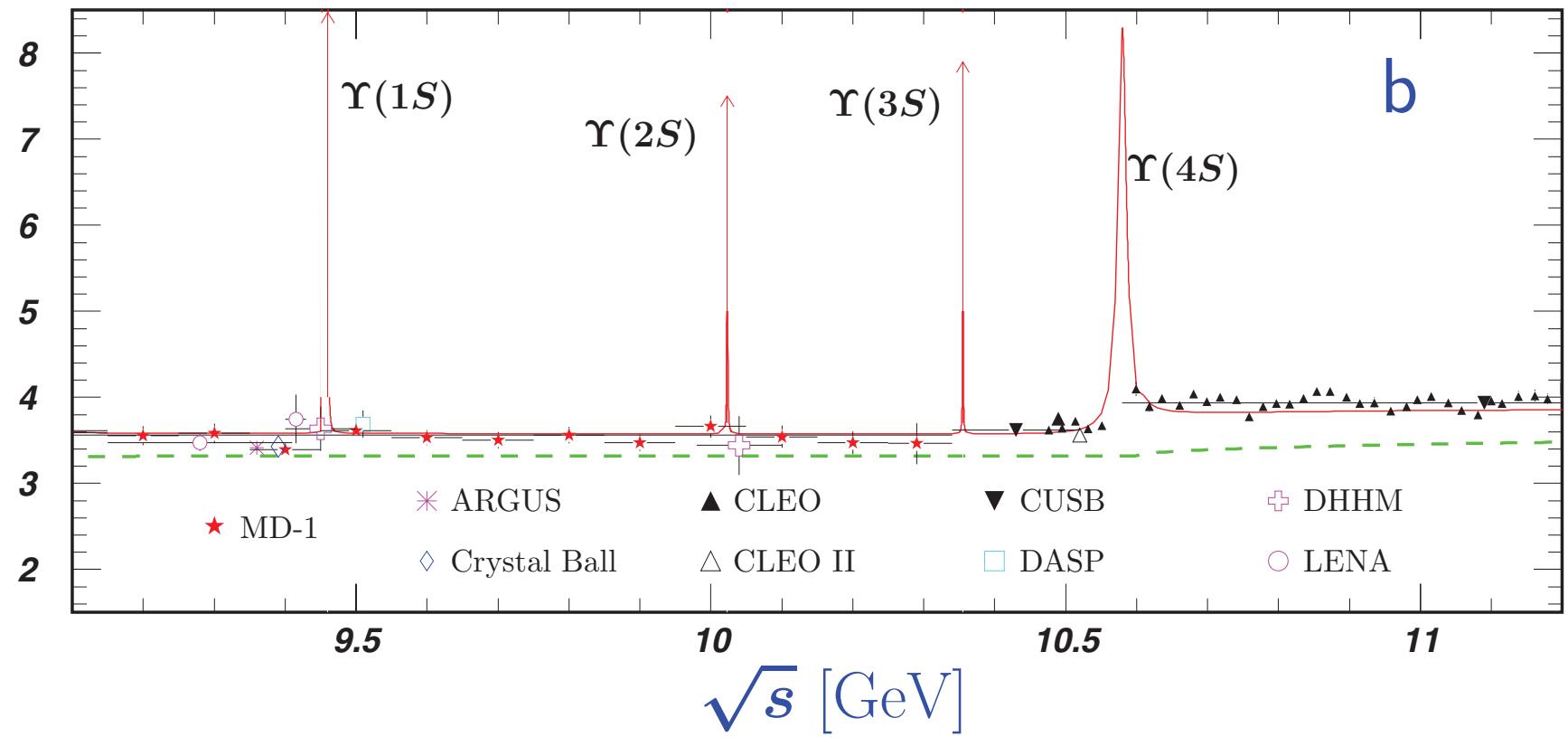
R-Ratio: u, d, s



$$R = \sum_q 3e_q^2 = 3 \left(\left(\frac{2}{3}\right)^2 + 1 \left(-\frac{1}{3}\right)^2 + \left(-\frac{1}{3}\right)^2 \right) = 2$$



$$R = \sum_q 3e_q^2 = 3 \left(\left(\frac{2}{3}\right)^2 + \left(-\frac{1}{3}\right)^2 + \left(-\frac{1}{3}\right)^2 + \left(\frac{2}{3}\right)^2 \right) = \frac{10}{3}$$



$$R = \sum_q 3e_q^2 = 3 \left(\left(\frac{2}{3}\right)^2 + \left(-\frac{1}{3}\right)^2 + \left(-\frac{1}{3}\right)^2 + \left(\frac{2}{3}\right)^2 + \left(-\frac{1}{3}\right)^2 \right) = \frac{11}{3}$$

Consequences from QCD for Hadron Properties

Symmetries of the QCD Lagrangian: Parity

\mathcal{L}_{QCD} is invariant under parity transformation (*i.e.* point reflection)

$$\hat{P} : (t, \vec{x}) \rightarrow (t, -\vec{x})$$

Eigenvalues:

$$\begin{aligned}\hat{P}^2(\phi(t, \vec{x})) &= \hat{P}(\hat{P}(\phi(t, \vec{x}))) = \hat{P}(\phi(t, -\vec{x})) = \phi(t, \vec{x}) \\ \Rightarrow \hat{P}(\phi(t, \vec{x})) &= P\phi(t, \vec{x}) \quad \text{with Eigenvalues} \quad P = \pm 1 \quad (\text{actually } \pm e^{i\Phi}, \text{ but we can redefine } \hat{P})\end{aligned}$$

Consequences for Hadrons:

- All states can be decomposed into states with $P = +1$ or $P = -1$
 - ▶ Might be degenerated?
- System of Hadrons

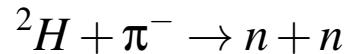
$$\hat{P}(\phi_1(t, \vec{x}) \otimes \phi_2(t, \vec{x}) \otimes \cdots \otimes \phi_N(t, \vec{x})) = P_1(\phi_1(t, \vec{x})) \times P_2(\phi_2(t, \vec{x})) \times \cdots \times P_N(\phi_N(t, \vec{x}))$$

Parity is a “multiplicative” quantum number

- Hadrons produced via QED/QCD from a state with defined total parity have same total parity
- Additional $U(1)$ Symmetries for Baryon-Number, Charge, Lepton Number \Rightarrow combined parity operators
- Define intrinsic parity $P_{\text{Proton}} = P_{\text{Neutron}} = P_{\text{Electron}} = +1$:

Symmetries of the QCD Lagrangian: Experimental determination of Parity

Example: Parity of the pion



- measure angular momentum (i.e. angular distribution)

- intrinsic parity $P(p) = P(n) = 1$

- Deuteron has Spin $S_d = 1$
Pion has Spin $S_\pi = 0$
 s -Wave $L = 0$

\Rightarrow total orbital momentum of final state $L = 1 \Rightarrow P = (-1)^L$

- Sum

$$\underbrace{(1)}_{p\uparrow} \underbrace{(1)}_{n\uparrow} \underbrace{(P_\pi)}_{\text{Pion}} = \underbrace{(-1)}_{L=1} \underbrace{(1)}_{n\uparrow} \underbrace{(1)}_{n\uparrow}$$

\Rightarrow Pion has parity $P_\pi = -1$, it is a “pseudoscalar” particle

General approach:

- calculate parity of initial state
- examine strong and electromagnetic (not weak!!!) decays, determine angular momenta
- tie to defined intrinsic parity

Symmetries of the QCD Lagrangian: Charge Conjugation

\mathcal{L}_{QCD} is invariant under Charge Conjugation (i.e. exchange particle \rightarrow antiparticle)

$$\hat{C} : |\phi\rangle \rightarrow |\bar{\phi}\rangle$$

Same properties as a parity operator

- Eigenvalues $C = \pm 1$
- Multiplicative quantum number for a system
- **New:** only neutral particles can be eigenstates!

Experimental determination: e.g. C-Parity of the pion from decay:

$$\pi^0 \rightarrow \gamma + \gamma$$

- C-Parity of photon $C(\gamma) = -1$ from QED
- Multiplicative $\Rightarrow C(\pi^0) = (-1)_\gamma(-1)_\gamma = 1$

Quantum numbers of the Pion: $J^{PC} = 0^{-+}$

C-Parity only for neutral particles

- Combination with Isospin Rotation $\hat{R} : |I, I_z\rangle \rightarrow |I, -I_z\rangle$
- Define G-Parity: $\hat{G} = \hat{C}\hat{R}$ for charged mesons

Natural Quantum numbers

- “Natural” quantum numbers for mesons: J^{PC} with $|L - S| \leq J \leq |L + S|$

$$\left. \begin{aligned} \hat{P}(Y_{lm}(\theta, \phi)) &= Y_{lm}(\pi - \theta, \phi + \pi) = (-1)^l Y_{lm}(\theta, \phi) \\ \text{intrinsic parity from Dirac Equation: } P(q) &\neq P(\bar{q}) \end{aligned} \right\} \Rightarrow \hat{P}|q\bar{q}\rangle = (-1)^{L+1}|q\bar{q}\rangle$$

- Charge Parity of a Meson as a Quark-Antiquark pair:

$$\hat{C}(|q\bar{q}\rangle) = C|q\bar{q}\rangle$$

► Charge Conjugation corresponds to exchange of quark/antiquark

$$\left. \begin{aligned} \text{Exchange of Wavefunctions (see above)} \quad C &= (-1)^{L+1} \\ \text{Spin flip/No Spin flip for } S = 0/S = 1 \quad C &= (-1)^{S+1} \end{aligned} \right\} \Rightarrow \hat{C}(|q\bar{q}\rangle) = (-1)^{L+S}|q\bar{q}\rangle$$

- Allowed: $0^{-+}, 0^{++}, 1^{--}, 1^{+-}, 1^{++}, 2^{--}, 2^{-+}, 2^{++}, 3^{--}, 3^{+-}, 3^{++}, \dots$
Not allowed: $0^{--}, 0^{+-}, 1^{-+}, 2^{+-}, 3^{-+}, \dots \Rightarrow \text{Exotic Mesons}$

$2S+1L_J$	S	L	J	P	C	J^{PC}	Mesons				Name
1S_0	0	0	0	—	+	0^{-+}	π	η	η'	K	pseudo-scalar
3S_1	1	0	0	—	—	1^{--}	ρ	ω	ϕ	K^*	vector
1P_1	0	1	1	+	—	1^{+-}	b_1	h_1	h'_1	K_1	pseudo-vector
3P_0	1	1	0	+	+	0^{++}	a_0	f_0	f'_0	K_0^*	scalar
3P_1	1	1	1	+	+	1^{++}	a_1	f_1	f'_1	K_1	axial vector
3P_2	1	1	2	+	+	2^{++}	a_2	f_2	f'_2	K_2^*	tensor

Theoretical Approaches

The “brute force” approach: Lattice QCD

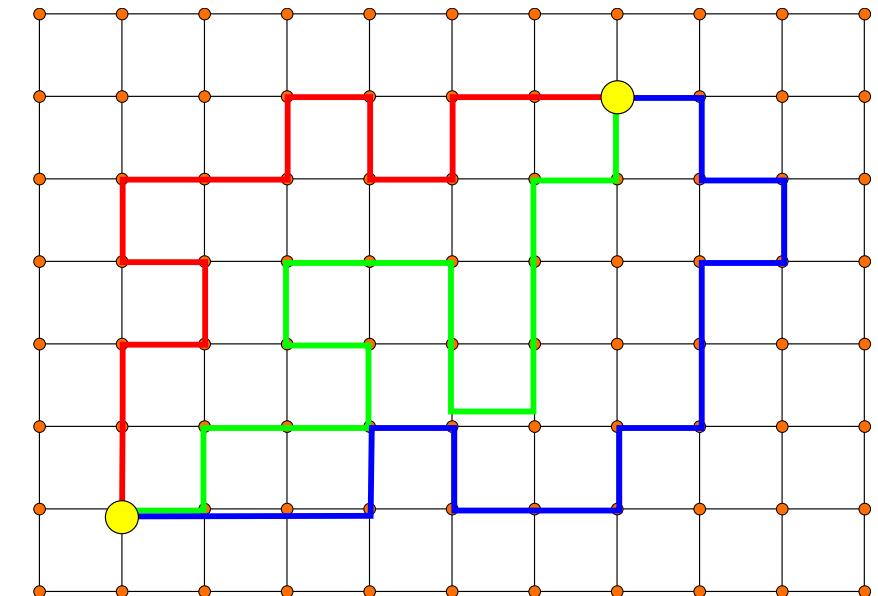
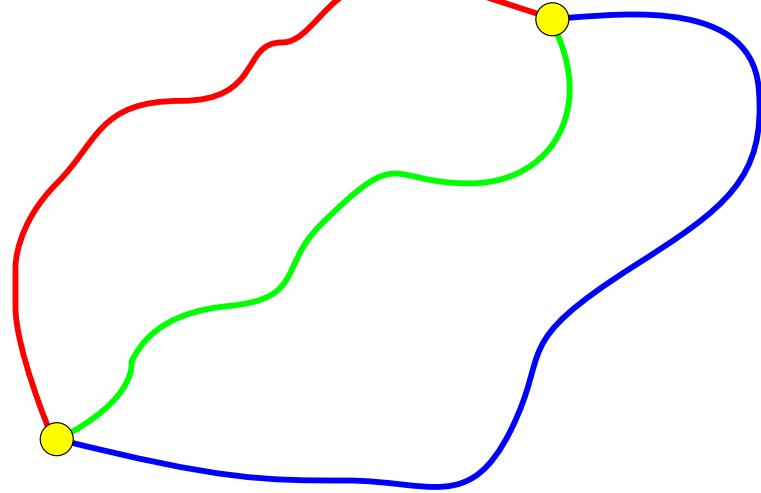
Starting point: Feynman’s Path Integral formulation of Quantum Mechanics:

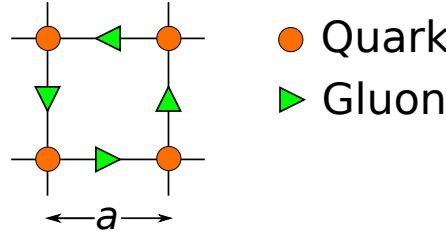
$$\Psi(x_2, t_2) = \frac{1}{Z} \int e^{iS} \Psi(x_1, t_1) \mathcal{D}x$$

with $\int \mathcal{D}x$: Integration over *all* paths $x(t)$ with $x(0) = x_1$

and the action $S = \int_{t_1}^{t_2} L(x, \dot{x}, t) dt$

(a.k.a. Fermat’s principle, Hamilton’s principle, principle of least action)





- Transform to Euclidean Space (necessary to use Monte-Carlo-Methods):

$$t \rightarrow i\tau$$

$$-(dt^2) + dx^2 + dy^2 + dz^2 \rightarrow d\tau^2 + dx^2 + dy^2 + dz^2$$

- Define Link Variables for gluonic field

$$U_\mu = \exp \left(ia G_\mu \left(n + \frac{\hat{\mu}}{2} \right) \right)$$

$U_{\mu\nu}(n)$: closed loop around one tile, “plaquette”

- Fermion action bei discretizing derivatives $\partial\phi_t \approx \frac{\phi(t+a) - \phi(t-a)}{2a}$

$$S = \int \bar{u}(iD_\mu \gamma_\mu + m)u d^4x \quad \rightarrow \quad D_\mu = \frac{1}{2a} [U_\mu(x)q(x + a\hat{\mu}) - U_\mu(x - a\hat{\mu})^\dagger q(x - a\hat{\mu})]$$

- Gluonic action:

$$S = -\frac{1}{2g^2} \text{Tr} \int G_{\mu\nu} G^{\mu\nu} d^4x \quad \rightarrow \quad S_L = -\frac{1}{2g^2} \sum a^4 \text{Tr} (1 - U_{\mu\nu}(n))$$

Final Step: Numeric solution via Markov-chain Monte-Carlo:

- Choose a start-configuration C_0
- Accept a random next configuration C_{n+1} with probability

$$P = \min\left(1, \frac{W(C_{n+1})}{W(C_n)}\right)$$

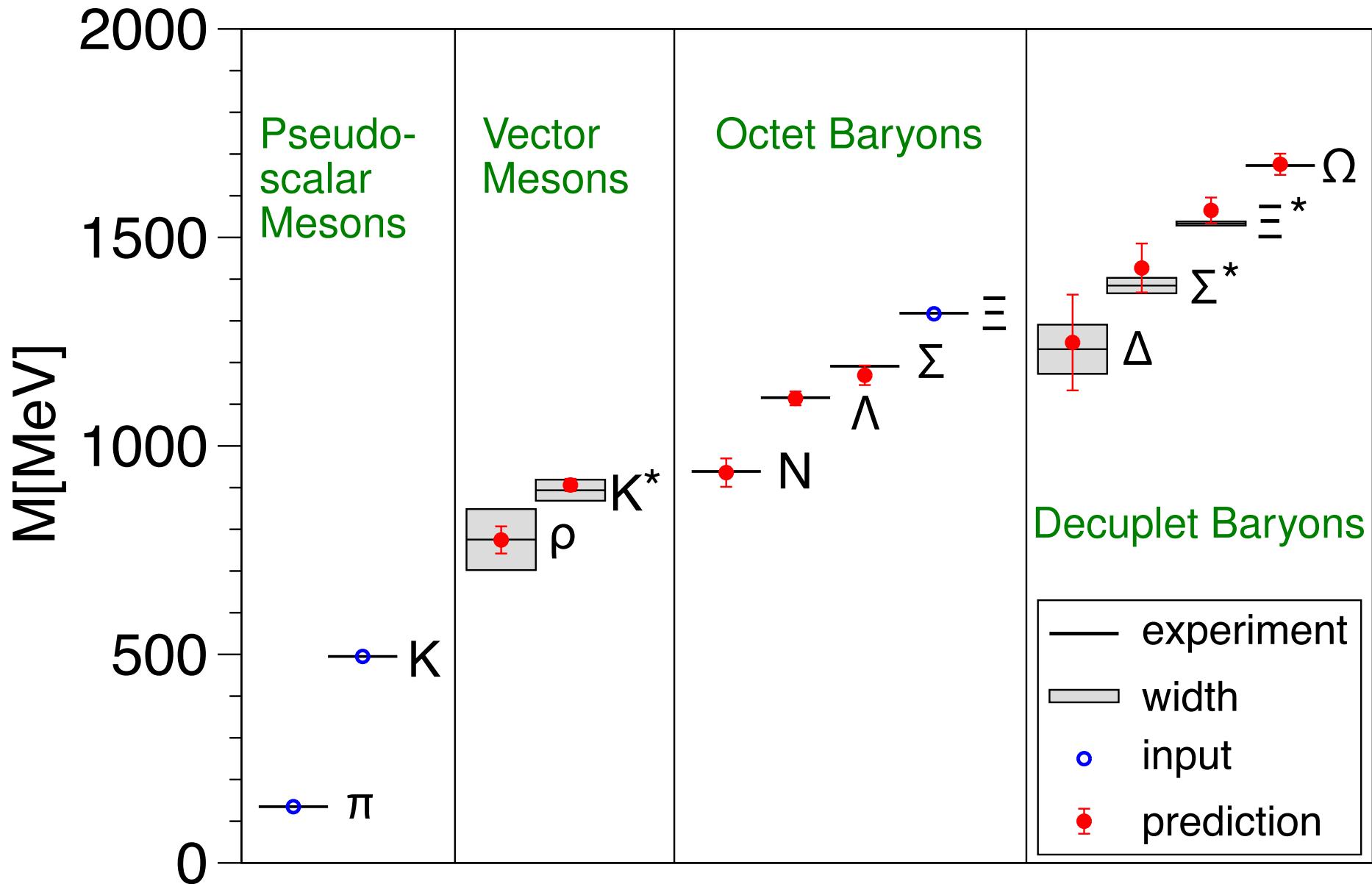
⇒ We don't need to know the probability density function,
we need only the *relative* weight $W(C)$,
calculated by discretized path integral!

- Repeat until “thermalization”, i.e. distribution of configurations corresponds to $W(C)$
- Repeat everything with different Lattice spacing a
- Extrapolation $a \rightarrow 0$

Summary:

- Gauge invariant
- Works in the non-perturbative regime
- Finite volume, finite momentum

Hadron Spectrum from Lattice QCD

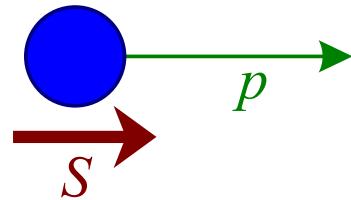


Still one symmetry of QCD not used...

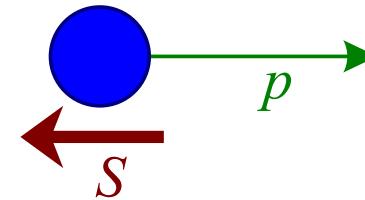
Chirality

Helicity: Spin projection in direction of motion

Right-handed:



Left-handed:



Not a good quantum number: inversion by “overtaking” reference frame!

Better: **Chirality**

$$\gamma^5 = i\gamma^0\gamma^1\gamma^2\gamma^3 = \begin{pmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{pmatrix}$$

For massless particles:

$$\gamma^5 \cdot u_+ = \gamma^5 \cdot \begin{pmatrix} \chi \\ \frac{\vec{\sigma} \cdot \vec{p}}{E+m} \end{pmatrix} = \gamma^5 \cdot \begin{pmatrix} 1 \\ 0 \\ 1 \\ 0 \end{pmatrix} = +u_+ \quad \text{and} \quad \gamma^5 \cdot u_- = \gamma^5 \cdot \begin{pmatrix} 0 \\ 1 \\ 0 \\ -1 \end{pmatrix} = -u_-$$

Eigenvalues of γ^5 are the eigenvalues of helicity for particles with $m \rightarrow 0$

Chirality \approx Lorentz invariant version of Helicity

Chiral Symmetry

Projection Operator

$$\frac{1}{2}(1 + \gamma^5)u = u_R \quad \frac{1}{2}(1 - \gamma^5)u = u_L$$

Consequences for *Dirac Equation* $(i\gamma^\mu p_\mu - m)u = 0$:

$$\bar{u}\gamma^\mu u = (\bar{u}_R + \bar{u}_L)\gamma^\mu(u_R + u_L) = \bar{u}_R\gamma^\mu u_R + \bar{u}_L\gamma^\mu u_L$$

for $m \rightarrow 0$: left-/right-handed particles interact only with left-/right-handed particles

Def.: Chiral Symmetry: invariant under separate rotations

$$\Psi_L \rightarrow e^{-i\theta_L} \Psi_L \quad \text{and} \quad \Psi_R \rightarrow \Psi_R$$

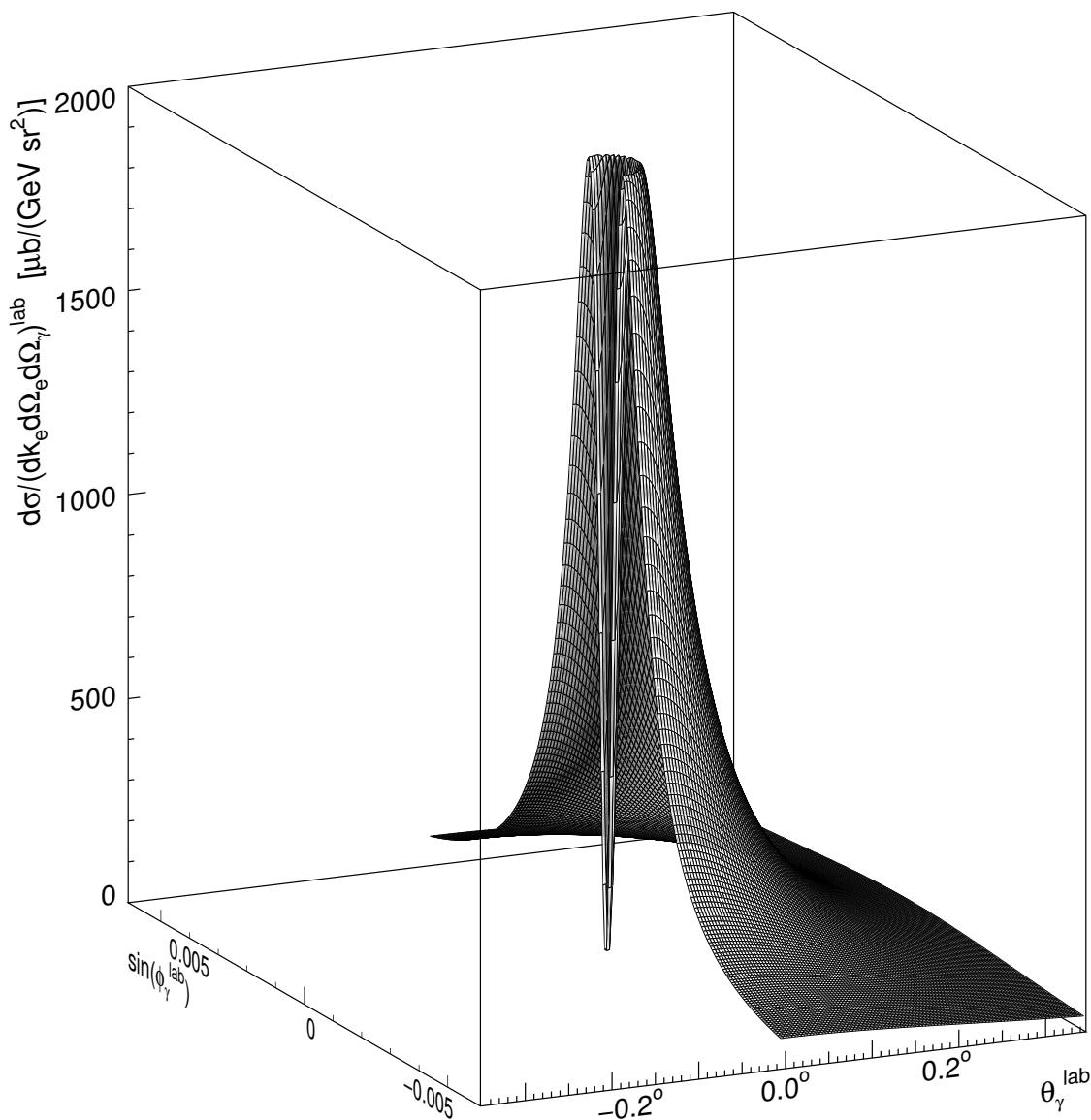
$$\text{or} \quad \Psi_R \rightarrow e^{-i\theta_R} \Psi_R \quad \text{and} \quad \Psi_L \rightarrow \Psi_L$$

Chiral Symmetry in QCD: combination with Isospin rotation of $q = \begin{pmatrix} u \\ d \end{pmatrix}$:

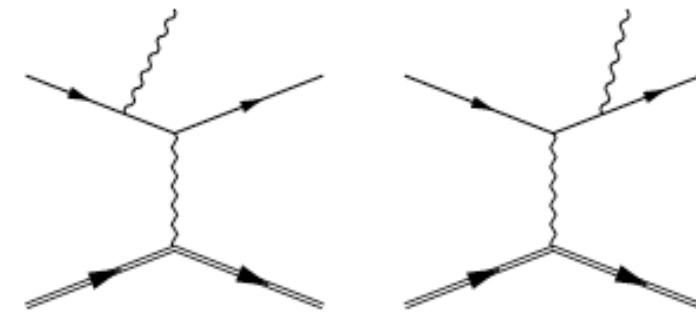
$$U(2)_L \times U(2)_R = \underbrace{SU(2)_L \times SU(2)_R}_{\text{Chiral Symmetry}} \times \underbrace{U(1)_V \times U(1)_A}_{\text{Baryon number, Quan. anomaly}}$$

Chiral Symmetry: QCD invariant under separate isospin rotation for left- and right-handed quarks in the limit of massless quarks

The Power of Chiral Symmetry...



QED Example: Bremsstrahlung



- Virtual intermediate electron
- $\frac{1}{p-m} \rightarrow 0$ Peak in electron direction
- Exactly at $\theta_{\gamma e} = 0$:
 - ▶ Emission of Spin 1 Photon
 - ▶ No orbital angular momentum
 - ▶ ⇒ Spin Flip of electron breaks Chiral Symmetry
 - ▶ Cross section $\rightarrow 0$
- ⇒ Chiral symmetry is powerful

Expectations from Chiral Symmetry for Hadron Physics

Mass of light quarks:

$$m_u = 2.2 \text{ MeV} \quad m_d = 4.7 \text{ MeV}$$

$$m_q \ll m_{\text{Hadrons}}$$

Chiral symmetry $SU(2)_R \times SU(2)_L$ should be conserved at least at 1% level!

Expectations:

- Parity doublets: all light quark states have partner with opposite parity

Observation:

- No parity doublets in baryon or meson spectrum seen! e.g. $\rho(770) < a_1(1200)$
- Three ridiculous light mesons π^0, π^+, π^- with $m_\pi \ll \frac{2}{3}m_p$

Hypothesis:

- Chiral Symmetry is spontaneously broken
- $SU(2)_L \times SU(2)_R \rightarrow SU(2)_V \times SU(2)_A$
of standard vector $SU(2)_V$ and rest ($SU(2)_A \equiv SU(2)_L \times SU(2)_R / SU(2)_V$ is not a group!)

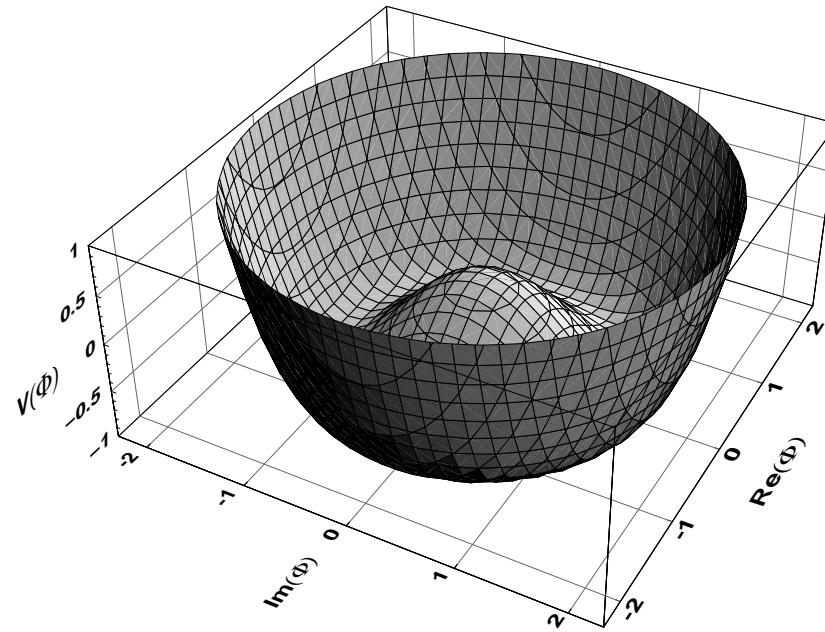
Spontaneous Symmetry Breaking and Goldstone-Theoreme

2-dimensional Example:

$$\mathcal{L} = \frac{1}{2}\partial^\mu\phi\partial_\mu\phi - \frac{1}{2}m^2\phi^*\phi - \frac{\lambda}{4}(\phi^*\phi)^2$$

Minimum at

$$|\phi| = k = \sqrt{-m^2/\lambda}$$



Replace complex scalar field $\phi = ke^{i\theta/k}, \quad \theta \in \mathbb{R}$

$$\Rightarrow \mathcal{L} = \frac{1}{2}(-ie^{-i\theta/k}\partial^\mu\theta)(ie^{i\theta/k}\partial_\mu\theta) - \frac{1}{2}m^2k^2 - \frac{\lambda}{4}k^4 = \frac{1}{2}\partial^\mu\theta\partial_\mu\theta - \underbrace{\frac{1}{2}m^2k^2 - \frac{\lambda}{4}k^4}_{\text{const. in } \theta}$$

\Rightarrow Real scalar field θ ist massless!

Spontaneous Symmetry Breaking \Rightarrow massless Goldstone-Bosons. \Rightarrow QCD: Pions

Chiral Effective Field Theories

What are the relevant degrees of freedom? \Rightarrow e.g. pions as Goldstone-Bosons

Ingredients for an effective field theory:

- Choose degrees of freedom: \Rightarrow Pions
- Most general Lagrangian in these DoF respecting the Symmetries of \mathcal{L}_{QCD}
 - \Rightarrow series in terms of derivatives, fields
 - \Rightarrow this is a perturbative theory!
- Most important: sort these terms!
 - \triangleright Expansion in mass terms (explicit symmetry breaking by $-\bar{q}_f M q_f$)
 - \triangleright Simultaneously expansion in p
 - \triangleright Order Scheme \rightarrow define what is LO, NLO, NNLO!
- Derive Feynman rules, calculate observables order by order, ...

To deal with:

- Regularization \Rightarrow Low Energy Constants Fit to experiment, limits predictive power
- Degrees of freedom: e.g. better to include resonances?
- Convergence of series
- ...

Systematic expansion, not a Model!

N.B.: Theorists' "Slang"

If a theorist uses the word

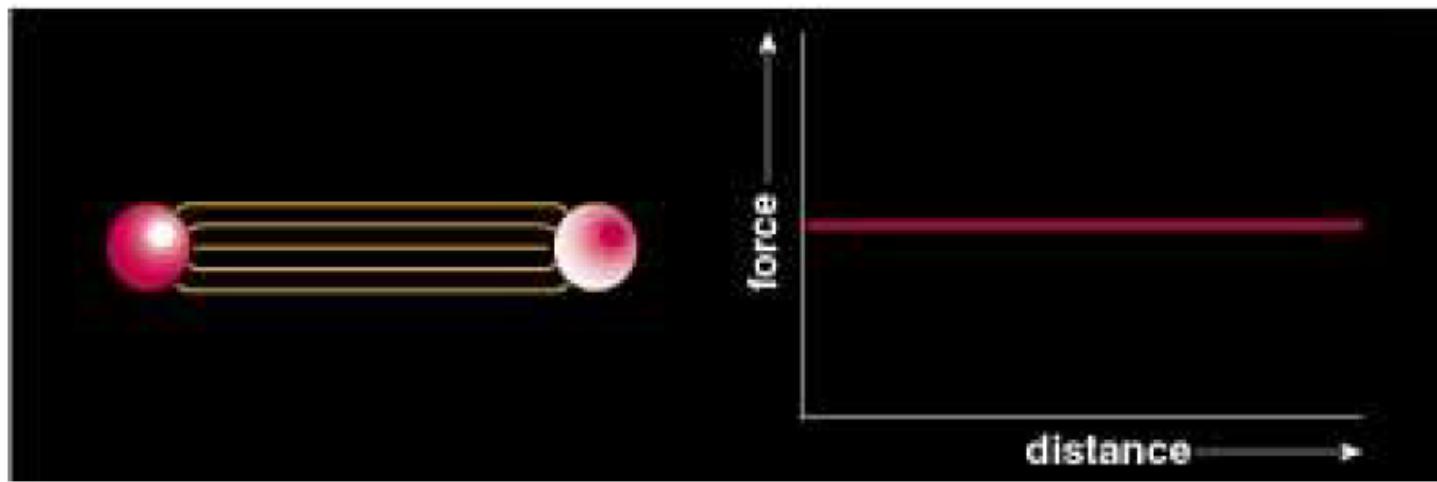
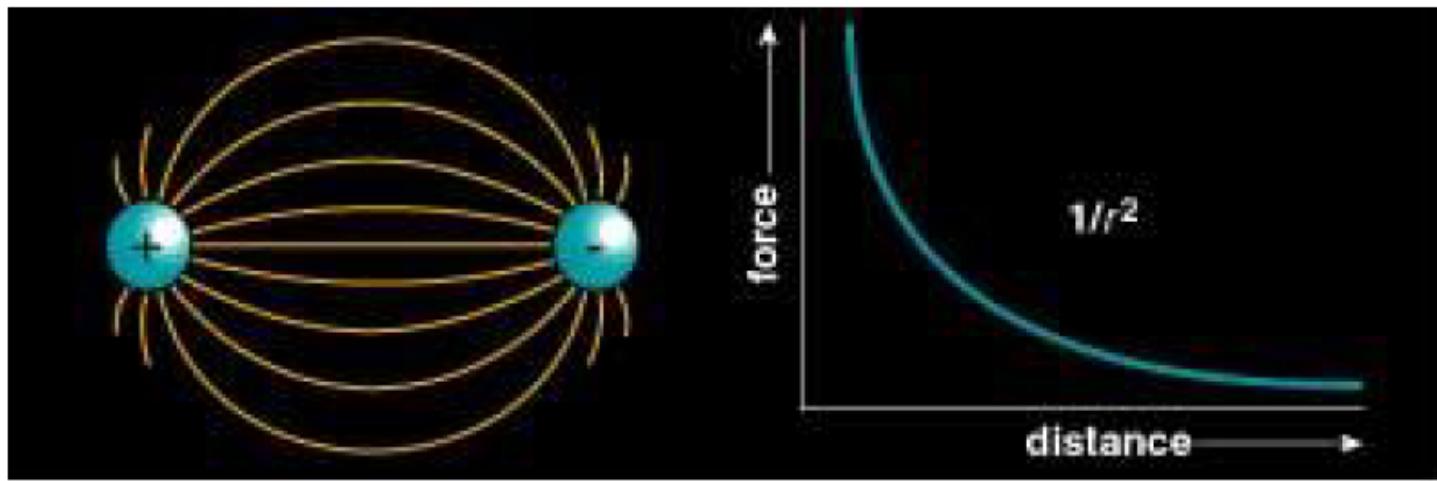
"chiral"

like e.g. in "Chiral Extrapolation of Lattice QCD" this usually means

"Using methodes from Effective Field Theories
using the Chiral Symmetry of QCD"

Potential Models

The $q\bar{q}$ Force of QCD



- Idea: heavy quarks \rightarrow non-relativistic
- A quark in the potential of a mean field

Simple Model: Non-relativistic Potential Model

Model: quarks in the potential of the rest of the meson/baryon

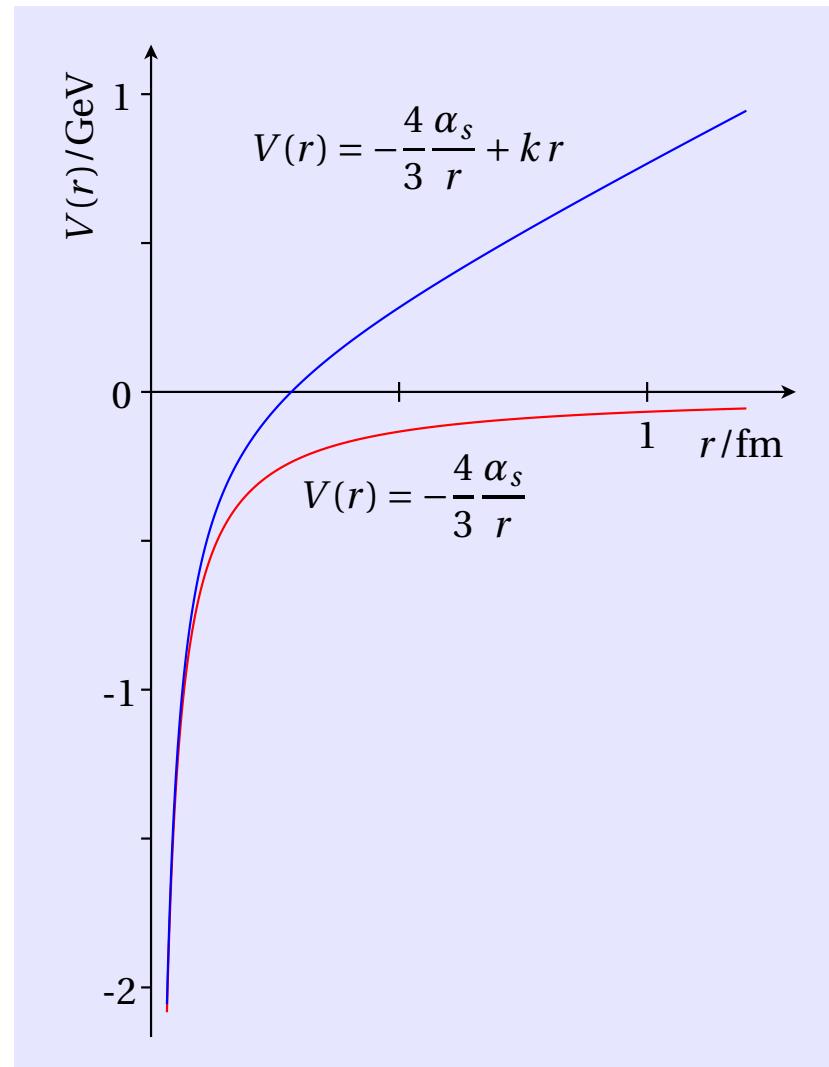
- $V(r \rightarrow 0)$

- ▶ Asymptotic freedom
- ▶ Massless gluons
→ infinite range Coulomb like potential $\frac{1}{r}$

- $V(r \rightarrow \infty)$

- ▶ Confinement potential $k \cdot r$
- ▶ Running coupling constant

$$V(\vec{r}) = -\frac{4 \alpha_s}{3} \frac{1}{r} + k \cdot r$$



Simple Model: Non-relativistic Potential Model

Non-relativistic $q\bar{q}$ potential:

$$V(\vec{r}) = -\frac{4 \alpha_s}{3} \frac{1}{r} + k \cdot r$$

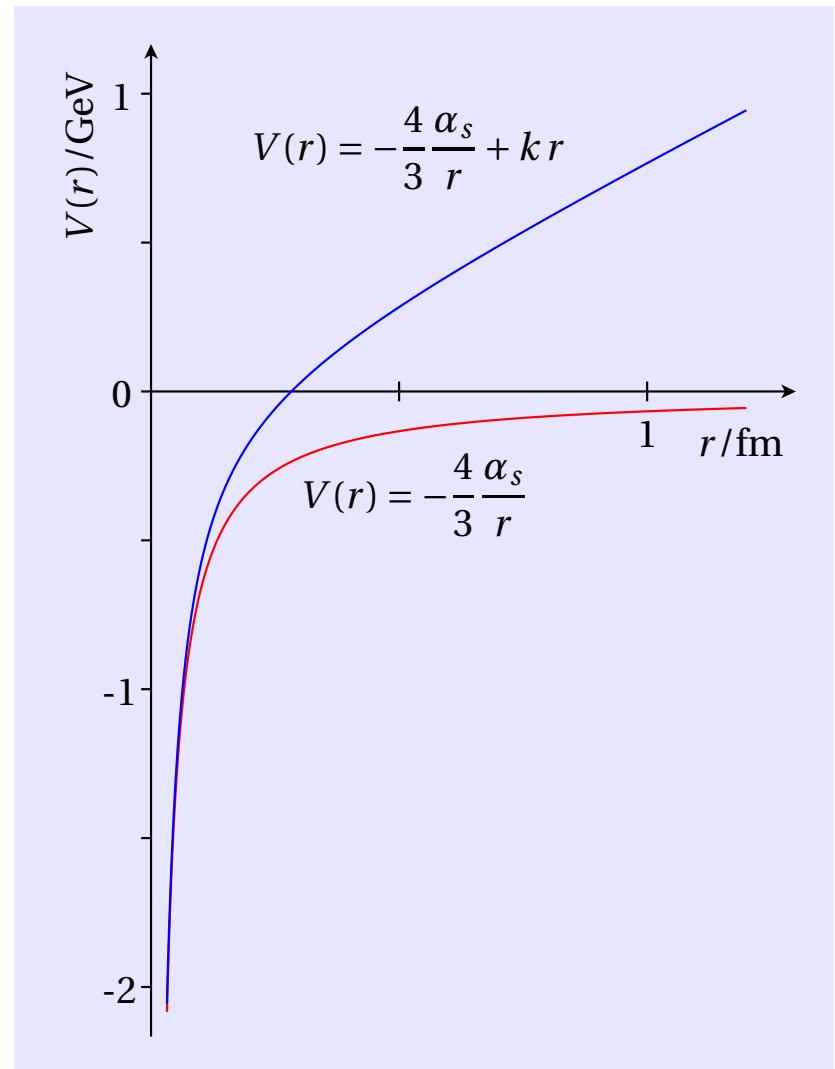
Running Coupling constant:

$$\alpha_s(Q^2) = \frac{12\pi}{(33 - n_f) \log \left(\frac{Q^2}{\Lambda^2} \right)}$$

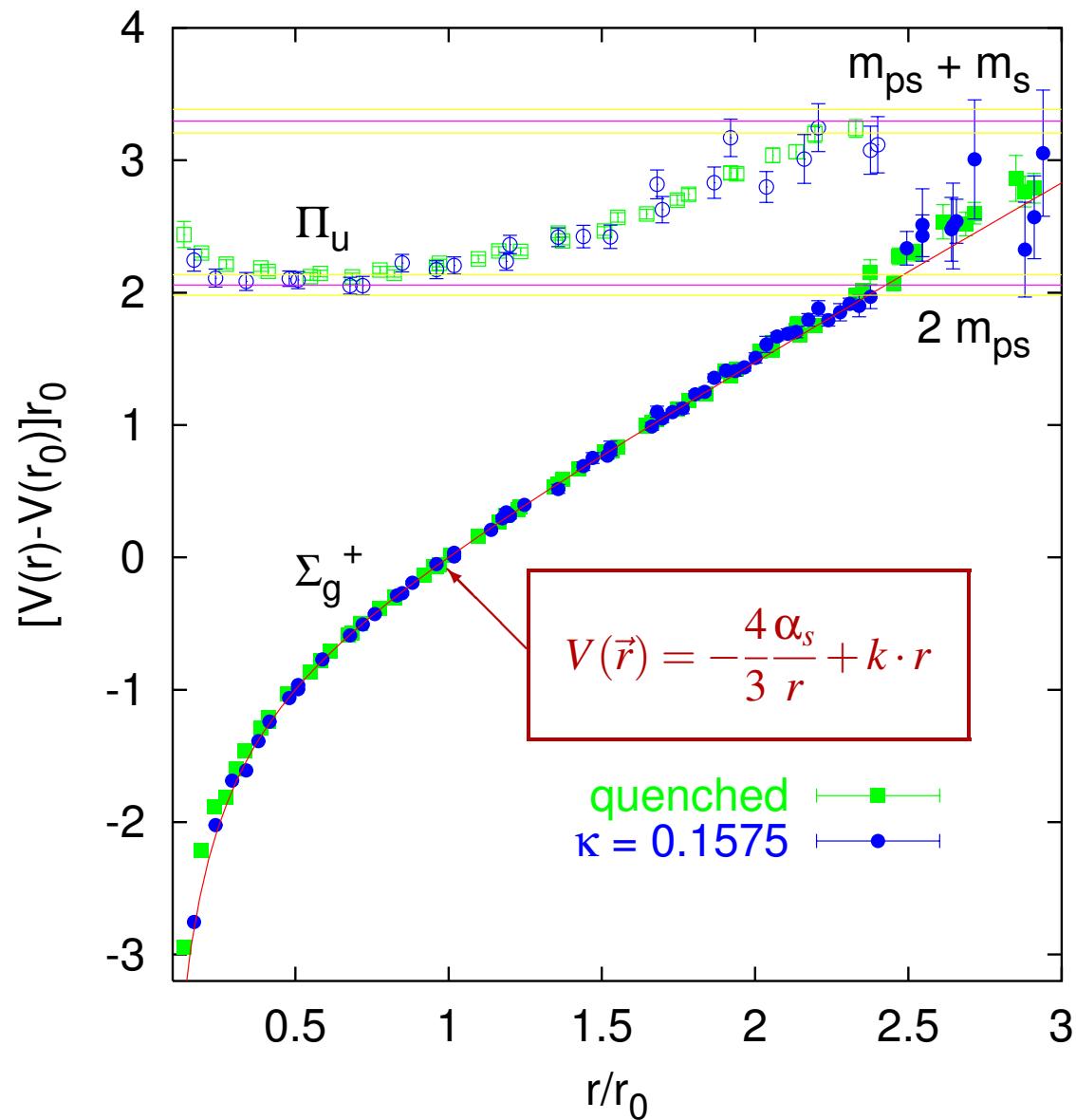
n_f : number of flavours

$\Lambda \approx 0.2 \text{ GeV}$: QCD Scale parameter

$k \approx 1 \frac{\text{GeV}}{\text{fm}}$: QCD String constant



qq Potential from Lattice calculation



Quenched approximation, *i.e.* no disconnected quark loops

Other useful Ingredients: Spin Dependent Potential

Necessary extensions of potential model:

- Spin-Orbit (fine structure)

$$V_{LS} = \frac{1}{2m_c^2 r} (\vec{L} \cdot \vec{S}) \left(3 \frac{dV_V}{dr} - \frac{d^2 V_V}{dr^2} \right)$$

- Spin-Spin (hyperfine structure)

$$V_{SS} = \frac{2}{3m_c^2 r} (\vec{S}_1 \cdot \vec{S}_2) \nabla^2 V_V(r)$$

- Tensor force

$$V_T = \frac{2}{12m_c^2} (3(\vec{S} \cdot \hat{r})(\vec{S} \cdot \hat{r}) - S^2) \left(\frac{1}{r} \frac{dV_V}{dr} - \frac{d^2 V_V}{dr^2} \right)$$

with V_V , V_S vector and scalar part of the previous potential

Finding Hadrons

⇒ Just looking for Bumps?

What is a Bump? The Line Shape:

- Strong Decay \Rightarrow Lifetime $\tau \approx 10^{-23} \text{ s}$
 \Rightarrow Width $\Gamma_0 \approx 100 \frac{\text{MeV}}{c}$

- Breit-Wigner Amplitude (complex mass in Dirac-propagator)

$$BW(m) = \frac{\Gamma_0/2}{m_0 - m - i\Gamma_0/2}$$

valid for $\Gamma_0 \ll m_0$
 $m_0 \gg$ Threshold Energy

- Better (relativistic, orbital momentum, phase space included):

$$BW(m) = \frac{m_0 \Gamma(m)}{m_0^2 - m^2 - im_0 \Gamma(m)}$$

with $\Gamma(m) = \Gamma_0 \frac{m_0}{m} \frac{p}{p_0} \frac{F_l^2(p)}{F_l^2(p_0)}$

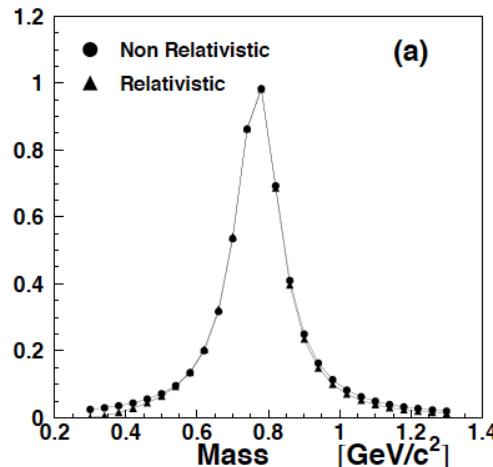
angular momentum barrier: $F_0(p) = 1$

$$F_1(p) = \sqrt{2z/(z+1)} \quad \text{with } z = (p/p_R)^2$$

$$F_2(p) = \sqrt{13z^2/((z-3)^2 + 9z)}$$

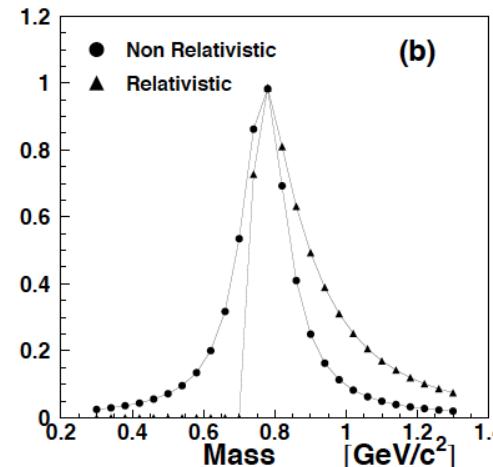
...

Example $\rho(770)$



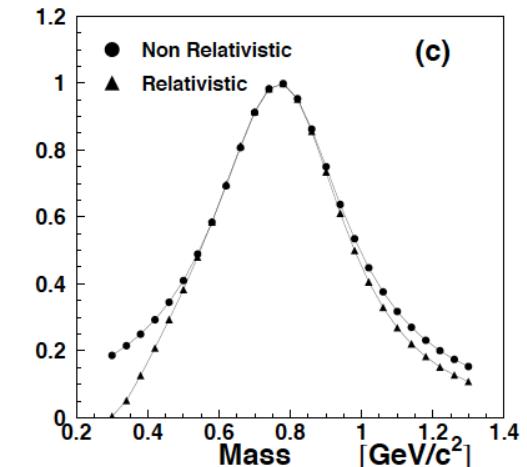
$$\Gamma_0 = 150 \text{ MeV}$$

$$m_1 = m_2 = 140 \text{ MeV}$$



$$150 \text{ MeV}$$

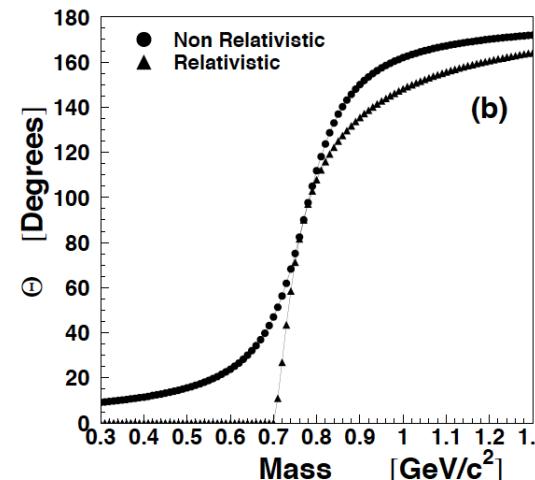
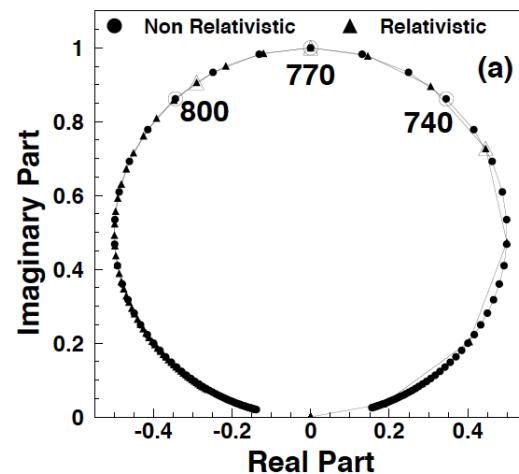
$$350 \text{ MeV}$$



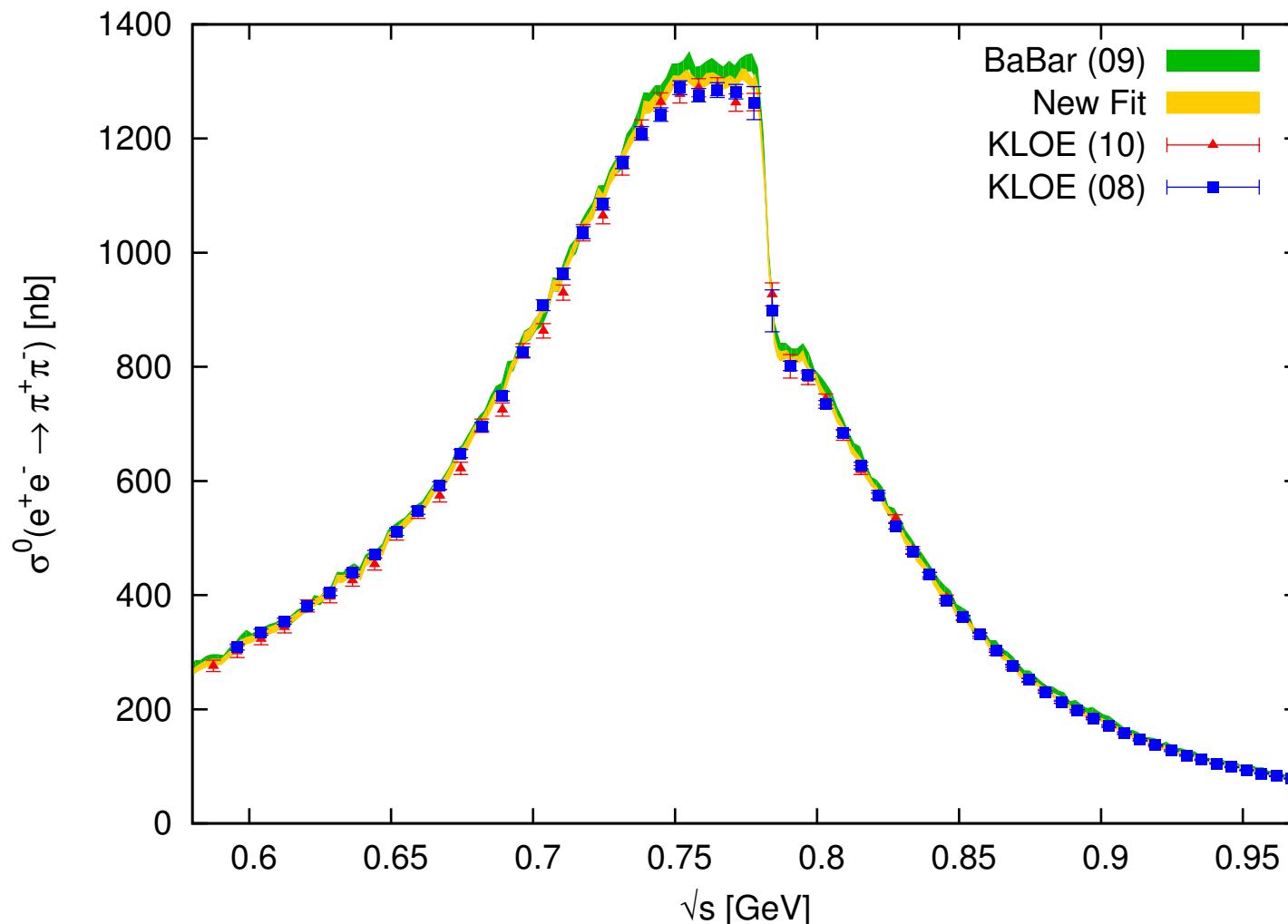
$$350 \text{ MeV}$$

$$140 \text{ MeV}$$

Argand-Diagramm:



Reality Check: $\rho \rightarrow \pi^+ \pi^-$



no clean Breit-Wigner $\rightarrow \rho - \omega$ interference at the position of the ω mass
 \rightarrow amplitude and phase changed
 \Rightarrow all open channels have to be considered on complex amplitude level!

Coupled channels

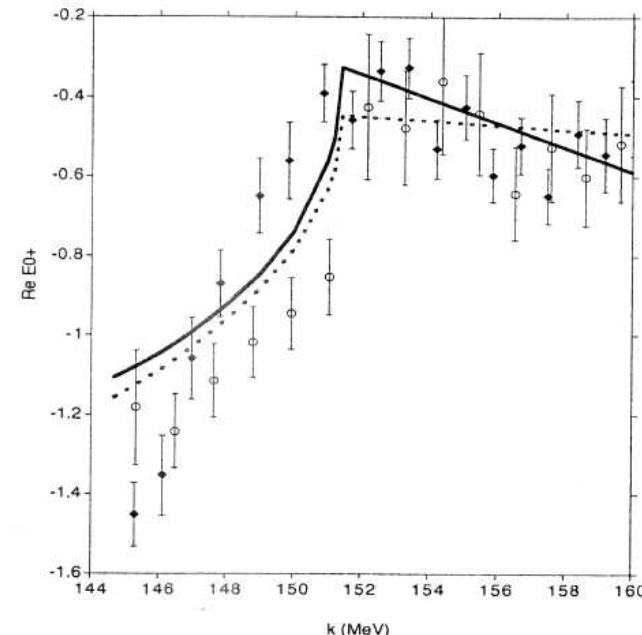
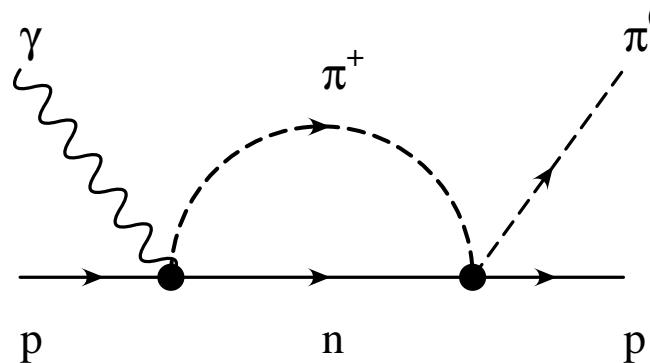
Simplest Example: proton around the pion production threshold

three open channels: $\gamma + p$, $n + \pi^+$, $p + \pi^0$

- Scattering matrix (S-Matrix) of complex transition amplitudes:

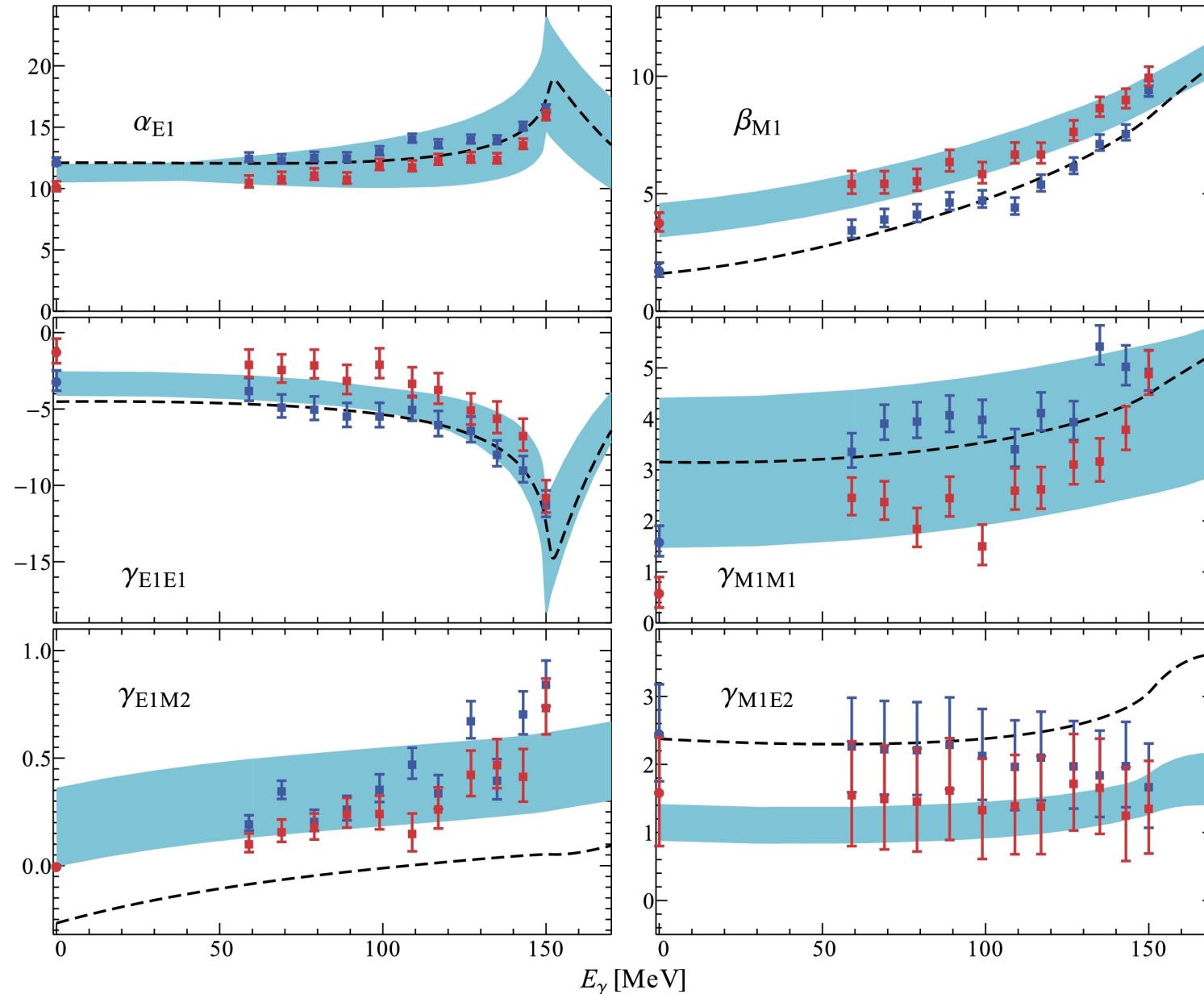
$$\begin{pmatrix} p + \gamma \\ n + \pi^+ \\ p + \pi^0 \end{pmatrix}_{\text{final}} = \begin{pmatrix} A_{\gamma\gamma} & A_{\gamma\pi} & A_{\gamma\pi} \\ A_{\gamma\pi} & A_{\pi\pi} & A_{\pi^+\pi^0} \\ A_{\gamma\pi} & A_{\pi^+\pi^0} & A_{\pi\pi} \end{pmatrix} \cdot \begin{pmatrix} p + \gamma \\ n + \pi^+ \\ p + \pi^0 \end{pmatrix}_{\text{initial}}$$

- Conservation of Probability \Leftrightarrow Unitarity of S-matrix
- All channels are seen in all other channels
- $\gamma + p \rightarrow p + \pi^0$, s-wave:



Compton-Scattering

Polarizabilities in Compton Scattering (partial waves):



Is the Scattering Phase an Observable?

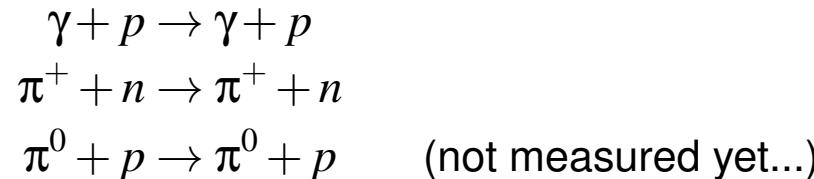
Quantum-mechanics: An absolute phase is not measurable!

But:

- Elastic scattering: optical Theorem

$$\sigma = \frac{4\pi}{k} \text{Im} \{f(\theta = 0)\}$$

- Elastic phase is a *transition phase*
- Direct measurable at forward direction ($\theta = 0$) in

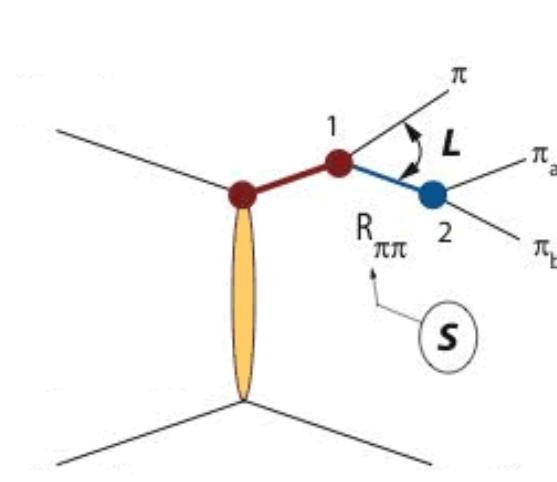


- Unitarity of S-matrix fixes phase of *all scattering amplitudes*

⇒ Scattering amplitudes have relative phases (initial state → final state)!

⇒ Production amplitudes are also **Observables** (but in reality hard to determine absolute)

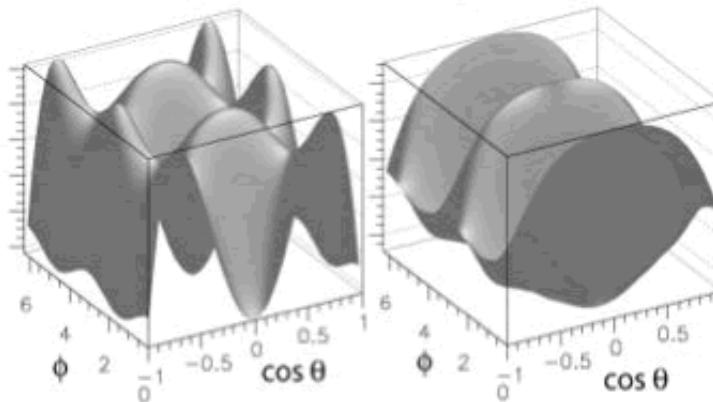
The Art of Partial Wave Analysis



(a) resonance: X decay (b) isobar: $R_{\pi\pi}$ decay

$$X(2^{++}) \rightarrow f_2(1275)\pi$$

$$f_2(1275) \rightarrow \pi\pi$$



- Limited significance of single channels (even if this presentation is “standard” in talks...)
- All open channels have to be fitted simultaneously
- Separate for every angular momentum (Partial Wave)
- Fit on *Amplitude* level (not cross section!)
- Polarization degrees of freedom
- Resonances: Breit-Wigner width (line shape, pole position), mass
- Background contributions
- Combinatorial background
- ...

Hundreds of parameters, most determined with limited significance

...choose wisely

I only believe in peaks seen

... in several channels

... by different groups,

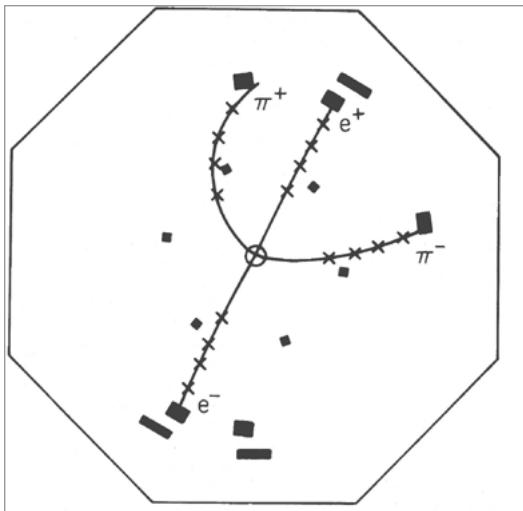
... measured with different apparatus,

... with different analysis

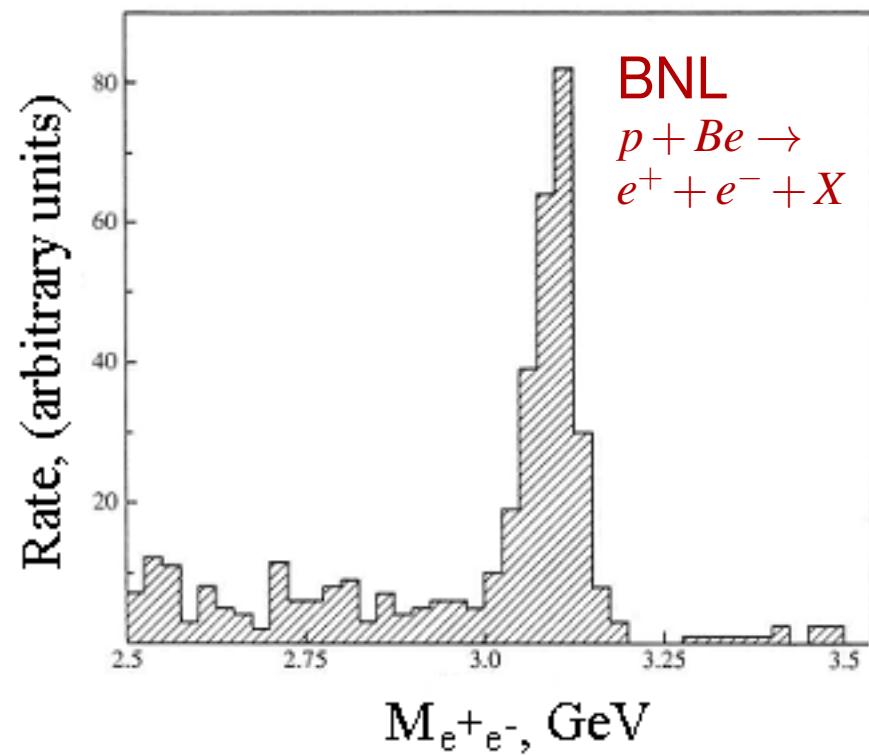
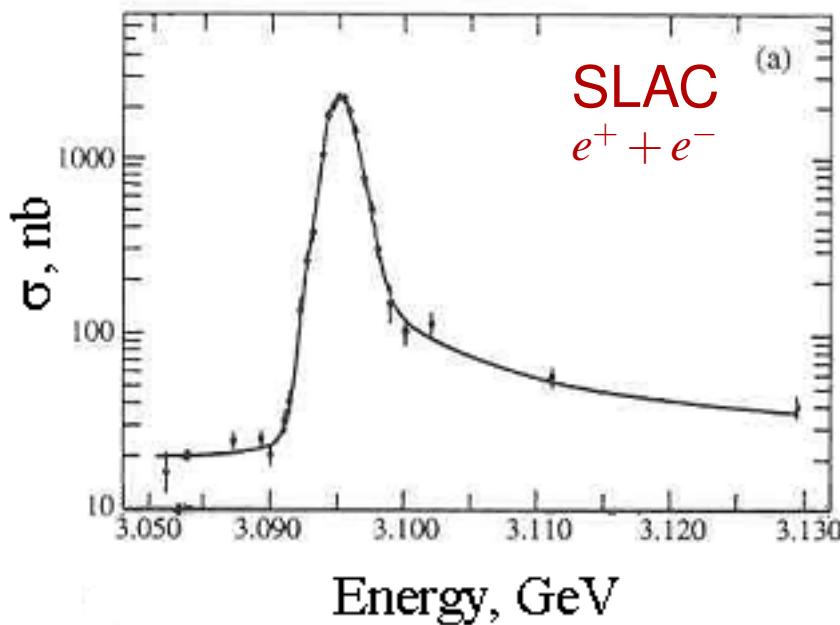
and still I have doubts...

Heavy Quark Mesons

The J/ψ discovery

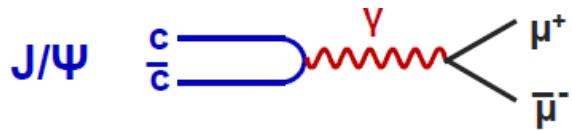


- Simultaneous discovery 1974 in BNL and SLAC
 - First evidence of a new quark: charm
 - Confirmation of quark model (c missing partner of s)
 - Bound state of $c\bar{c}$ quarks
- ⇒ new era of heavy quark physics

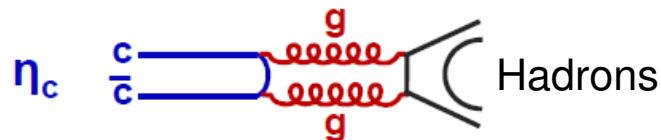


J/ψ -Decays

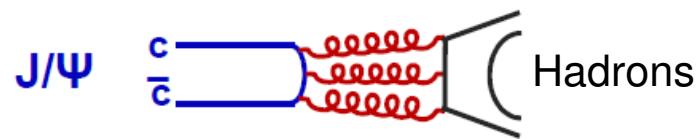
Below open charm threshold:



$J^{--} \Rightarrow$ electromagnetic decay possible



States with $C = +1$ can decay via two gluons

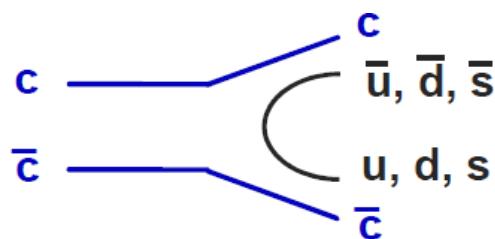


States with $C = -1$ can only decay via three gluons

⇒ electro-magnetic decay of same order of magnitude as strong decay

⇒ J/ψ is a very small resonance

Above open charm threshold:



⇒ broad resonances

Heavy Quark Systems

Heavy Quarks:

$$m_c = 1.3 \text{ GeV}$$

$$m_b = 4.2 \text{ GeV}$$

$$m_t = 170 \text{ GeV}$$

- ## Heavy Quark Systems are *non-relativistic*:

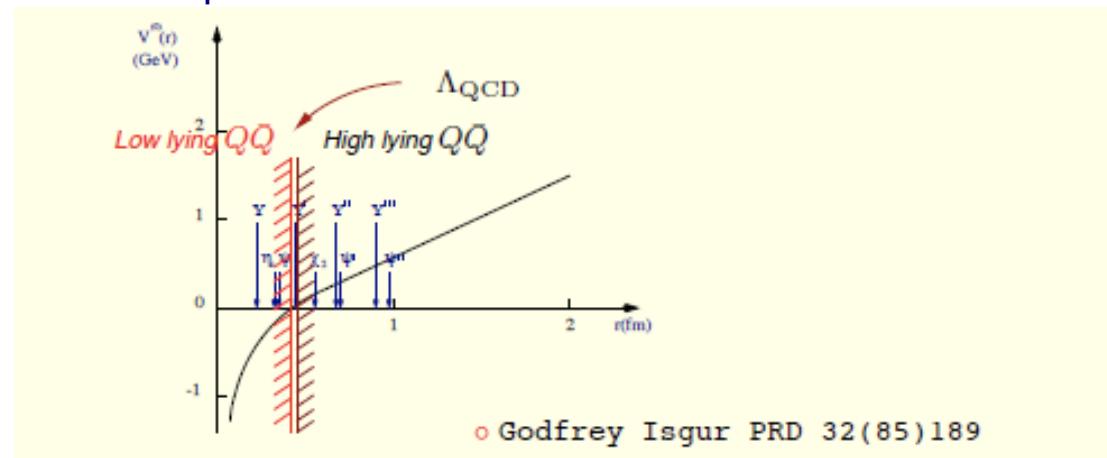
$$m_{J/\Psi} = 3.1 \text{ GeV} = 2 \times m_c + 2 \times 0.25 \text{ GeV}$$

$$\Rightarrow \beta = \frac{p}{E} \approx \frac{0.25 \text{ GeV}}{1.3 \text{ GeV}} = 0.2$$

- The mass scale is *perturbative*:

$$m_Q \gg \Lambda_{QCD}$$

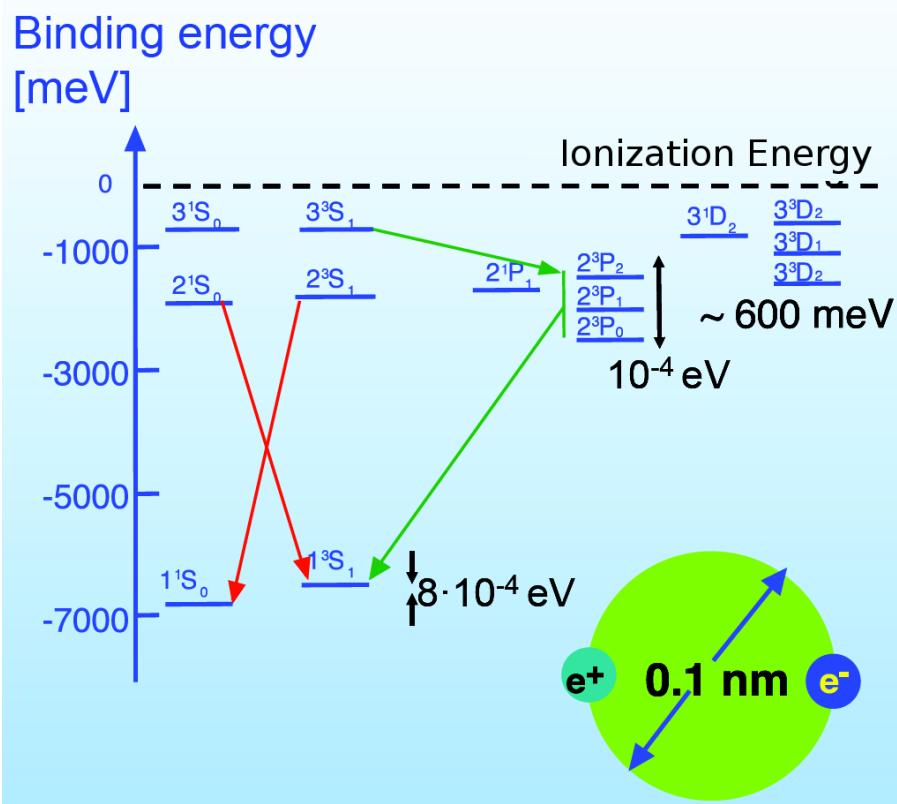
- Potential model for description well suited



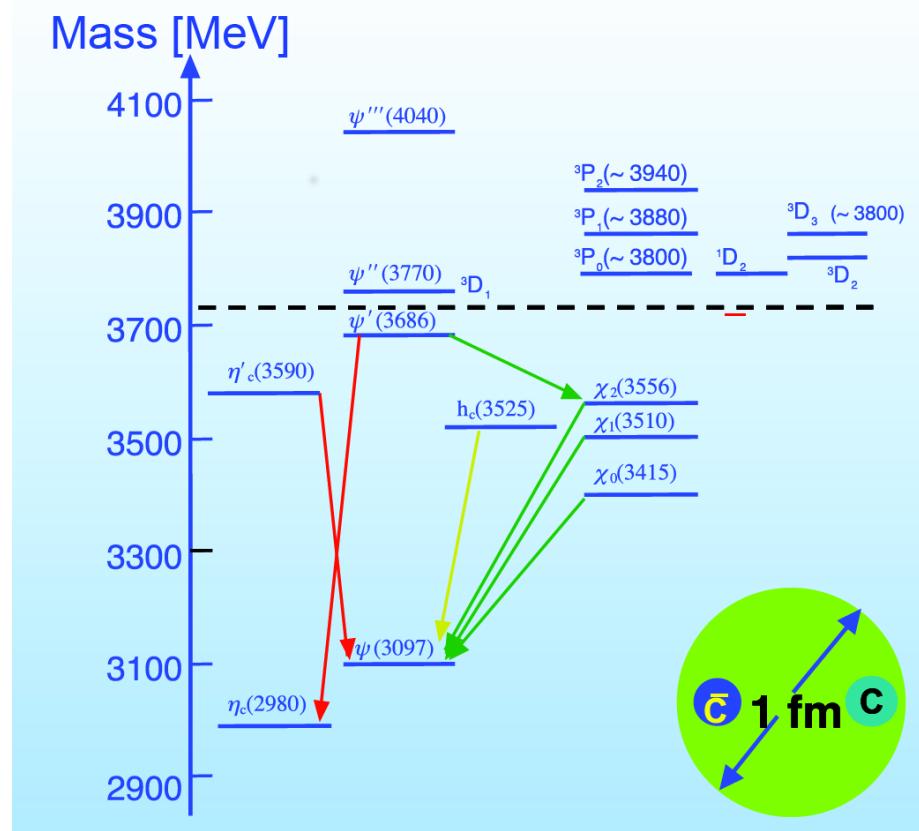
non-perturbativ – transition – perturbative regime

Positronium as Model for Quarkonium (Charmonium or Bottomonium)

Positronium

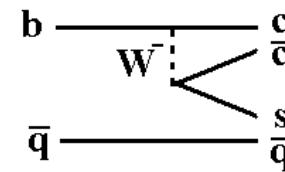


Charmonium



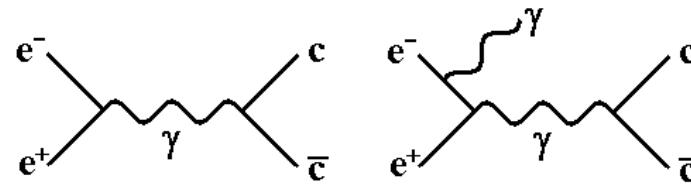
Production channels

- Weak decay

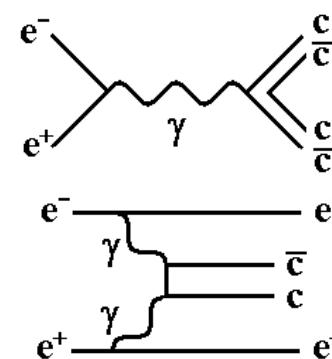


Belle

- e^+e^- annihilation and initial state radiation
 - only $J^{PC} = 1^{--}$
 - $0 < E <$ c.m. energy

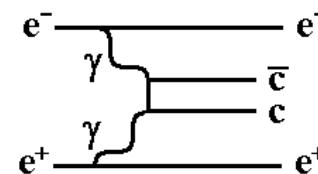


- Double Charmonium
 - $J/\psi + c\bar{c}$

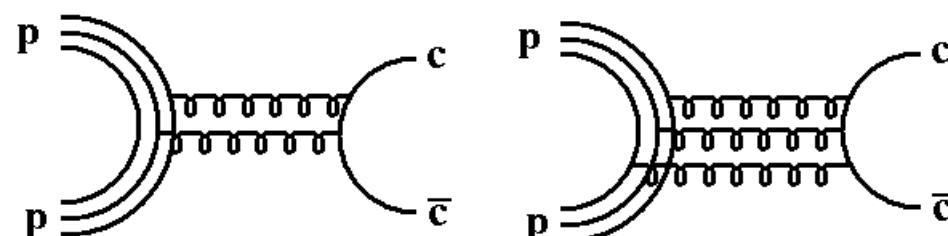


BES III

- Two-photon production
 - $C = +1$



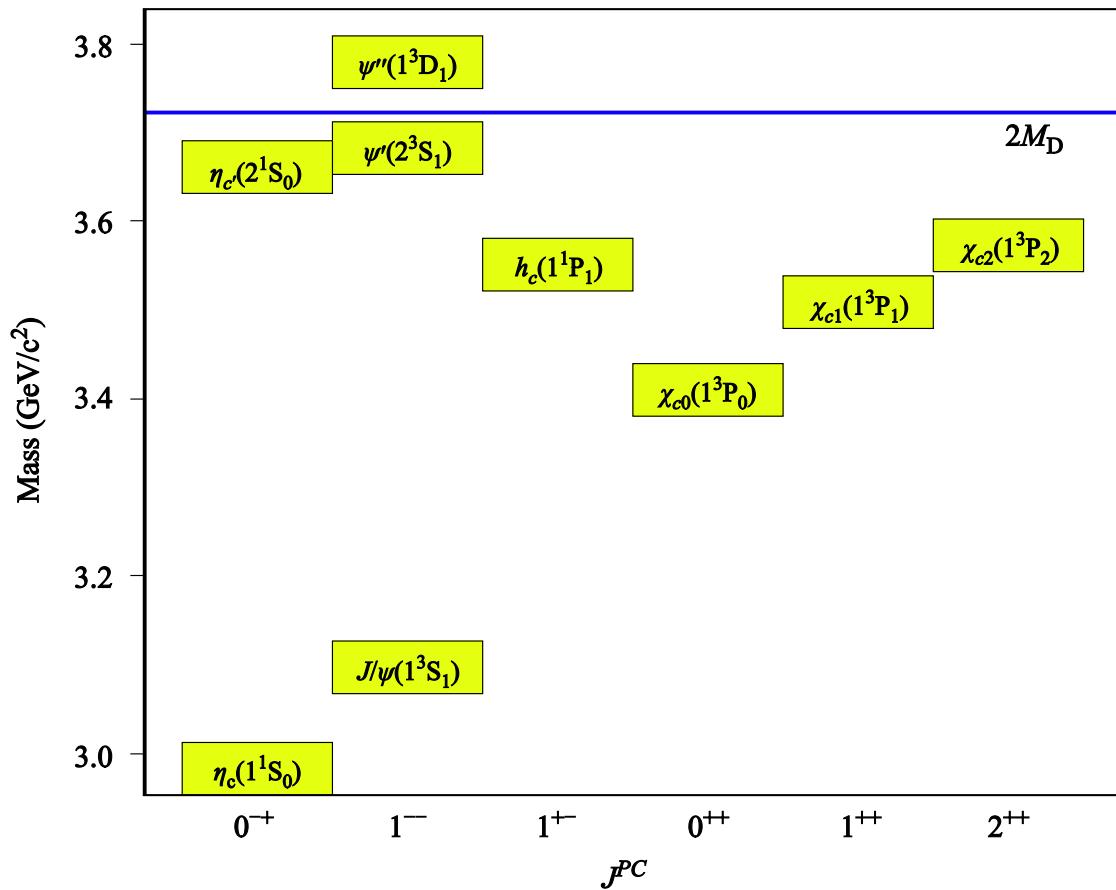
- $p\bar{p}$ annihilation
 - 2 gluons: $0^{-+}, 0^{++}, 2^{++}$
 - 3 gluons: $1^{--}, 1^{-+}$



PANDA

Charmonium States below open charm threshold

Discovered Charmonium States:



- Solution of non rel. Schrödinger-Equation

- Notation:

0^{-+}	1^{--}	1^{+-}	J^{++}
η_c	Ψ	h_c	$\chi_{1,2,3}$

- 8 States well established

- Hyperfine splitting to adjust spin dependent potential V_{SS}

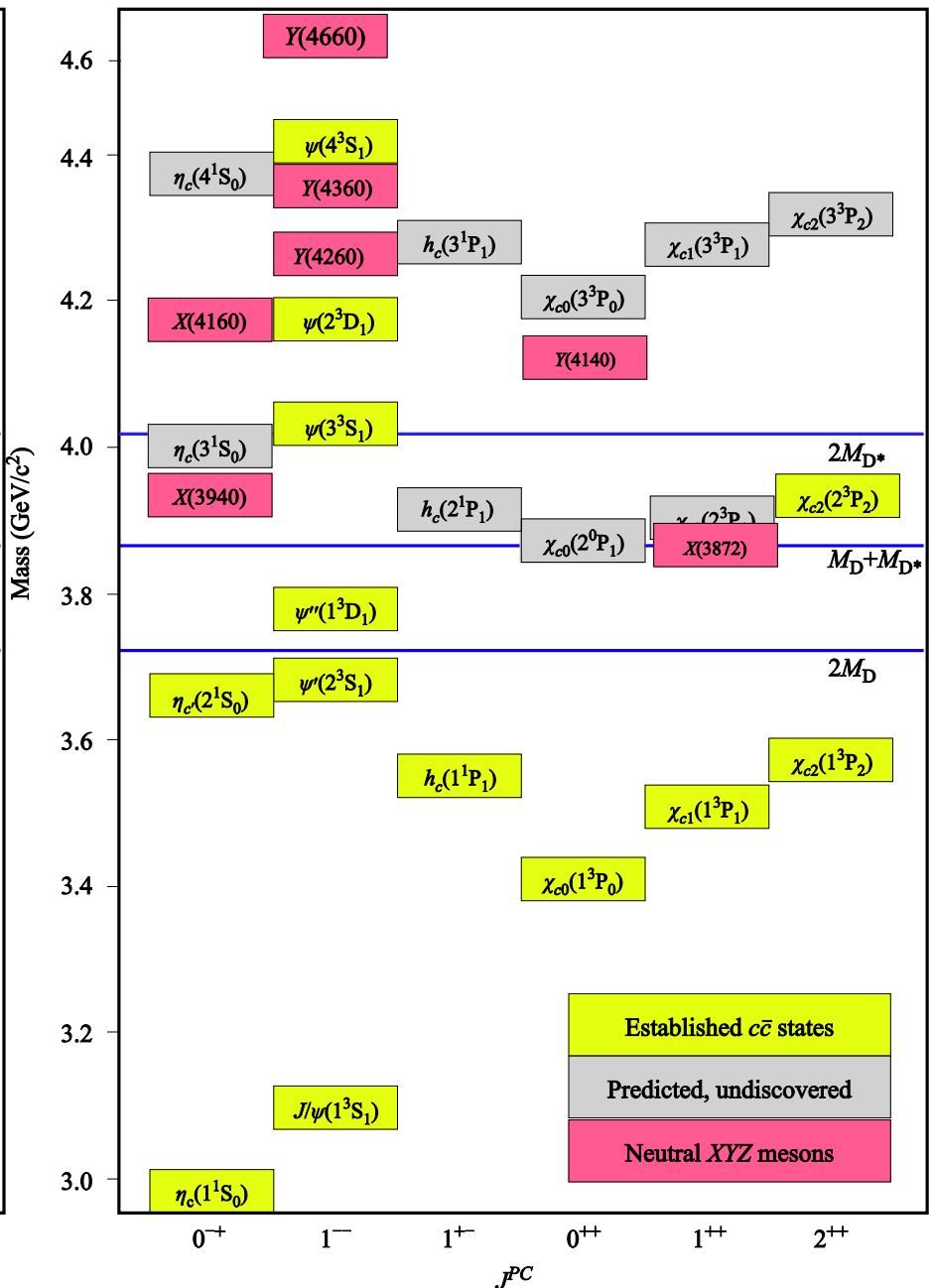
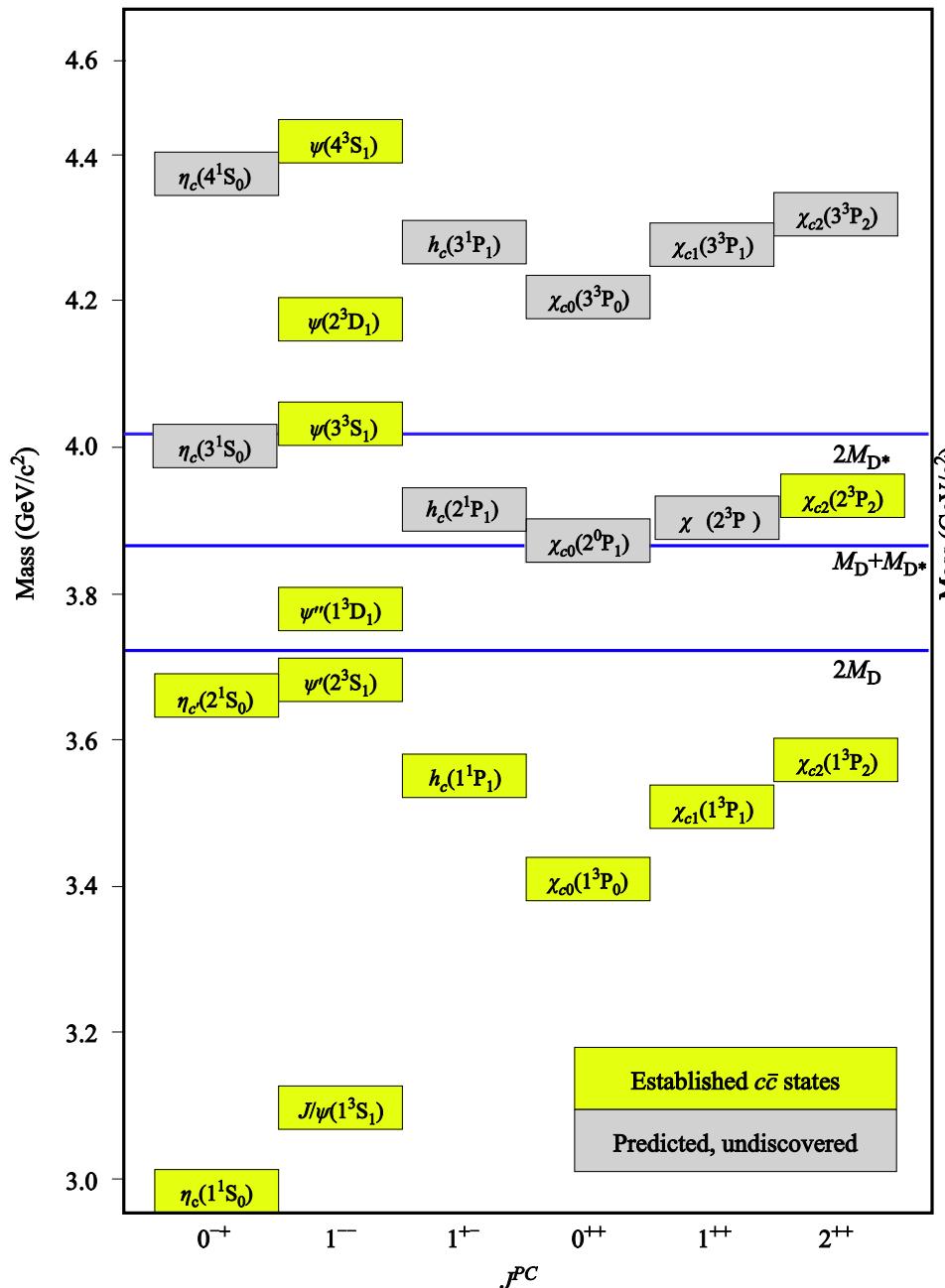
$$\Delta m_{hf}(1S) = m(J/\Psi) - m(\eta_c) = 116 \text{ MeV}$$

- Look for

► Missing States

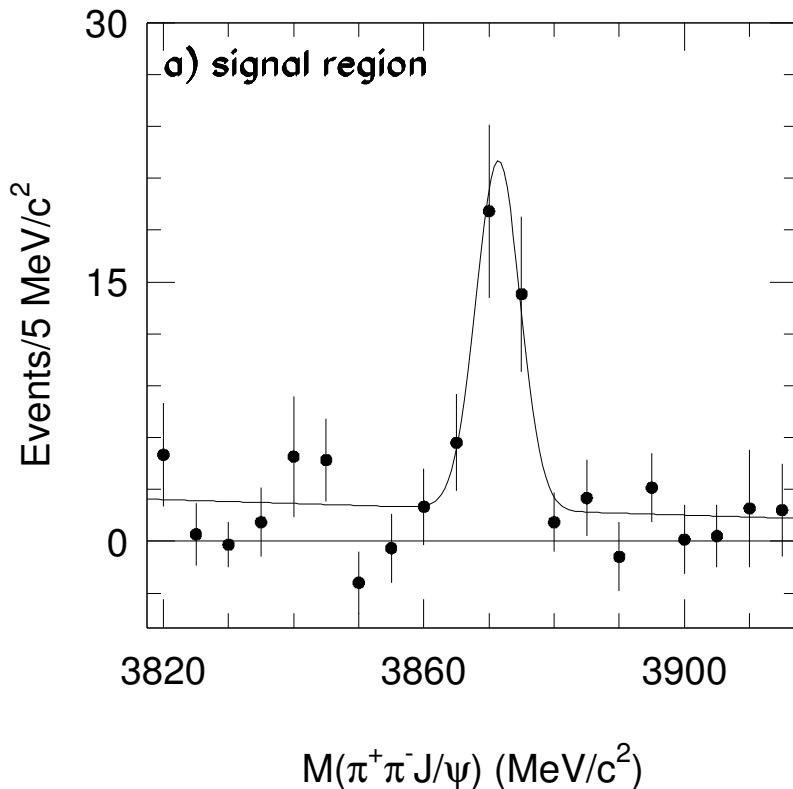
► Additional States

Charmonium Spectrum



The $X(3872)$ (new PDG2018 naming scheme: $\chi_{c1}(3872)$)

Belle (2013): A new state, not quite fitting into spectrum:



Discovery channel:

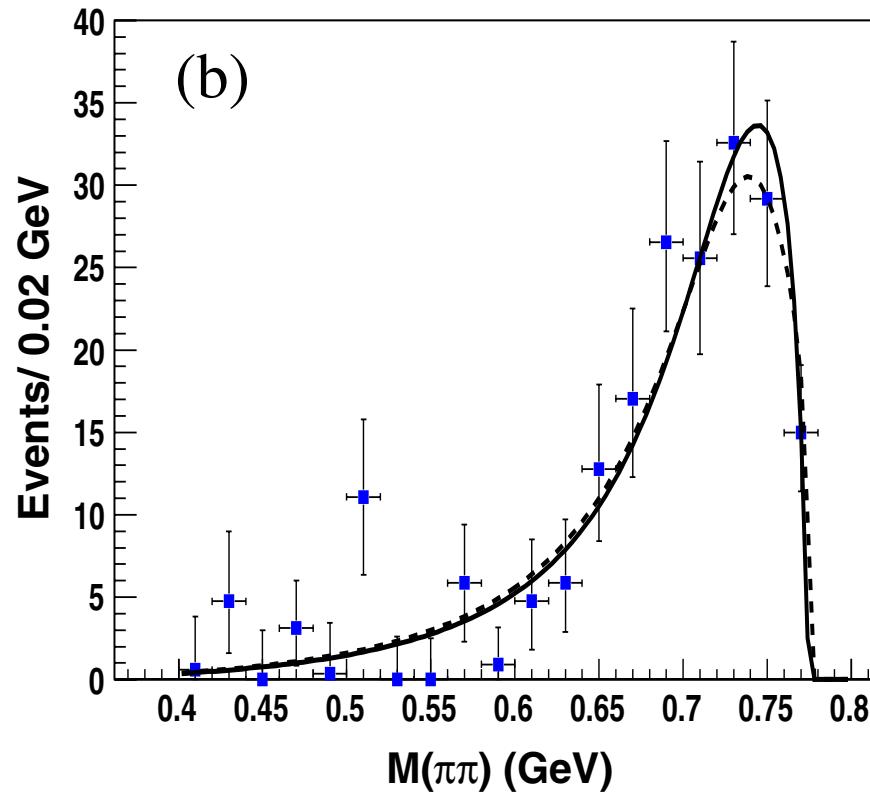
$$e^+ e^- \rightarrow \Upsilon(4S) \rightarrow B^+ B^-$$
$$B^+ \rightarrow K^+ \underbrace{\pi^+ \pi^-}_{\text{subsystem}} J/\psi$$

- Decay to J/ψ : $c\bar{c}$ content necessary
- Isospin: Decay via $\rho \rightarrow \pi^+ \pi^-$ or $\omega \rightarrow \pi^+ \pi^-$
- ρ decay is isospin violating \rightarrow suppressed
- Both channels are of same order
 \Rightarrow additional u and d content?

- Resonance confirmed by BaBar, BES, CDF, D0, LHCb, ...
- LHCb: Quantum Numbers $J^{PC} = 1^{++}$, $I = 0$ (these are not exotic!)

$X(3872)$ Decay to $\rho J/\psi$

$$X(3872) \rightarrow \rho + J/\psi$$
$$\rho \rightarrow \pi^+ + \pi^-$$



- Two Pion distribution described by Breit-Wigner with known $\rho(770)$ width
- Violates Isospin conservation \Rightarrow at least two gluons
- Should be suppressed compared to decay via $\omega \rightarrow \pi^+ \pi^- \pi^0$

Interpretations of the $X(3872)$

$X(3872)$ Properties

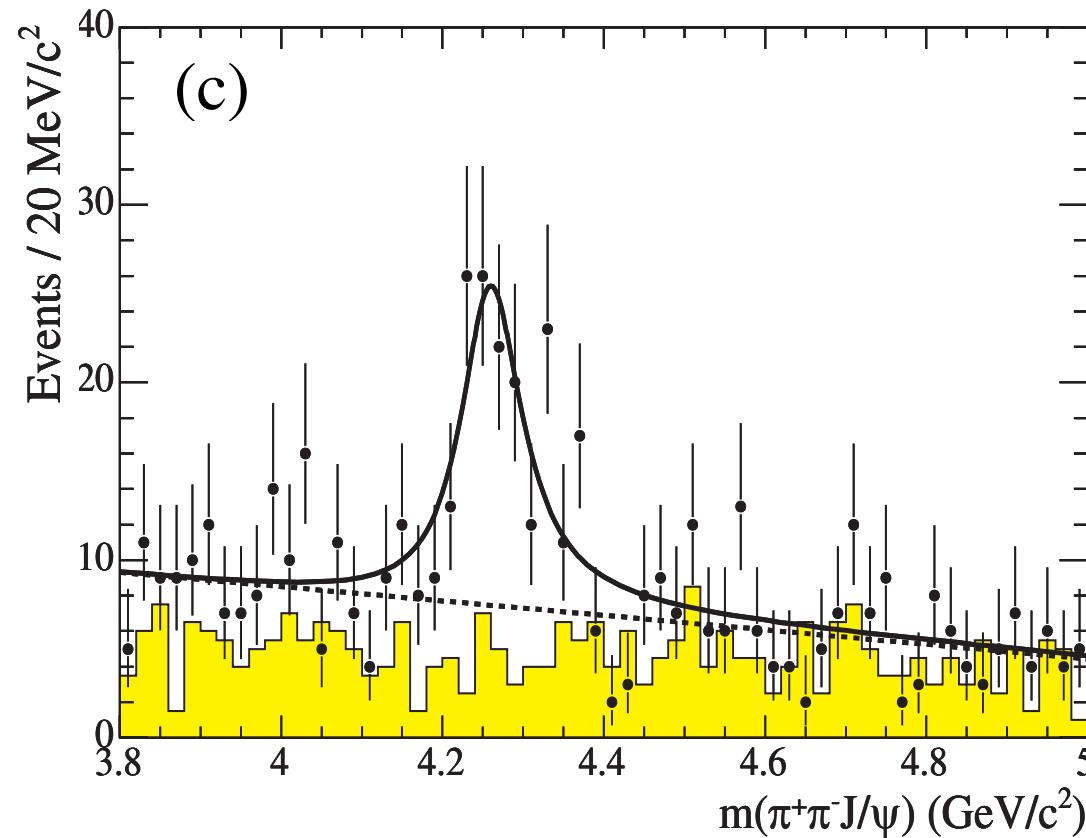
- Mass is very close to open charm threshold $\bar{D}_0 D_0^*$
- Width is very narrow $< 1.2 \text{ MeV}$
- small binding \Rightarrow huge separation
- Decays to $\rho J/\psi$
- Decays to $\omega J/\psi$
- Decays dominant to $\bar{D}_0 D_0^*$

Interpretation:

- Exotic nature? Probably...
- Many interpretations on the market
- Loosely bound $\bar{D}_0 D_0^*$ molecule?

BaBar (2005) via Initial State Radiation

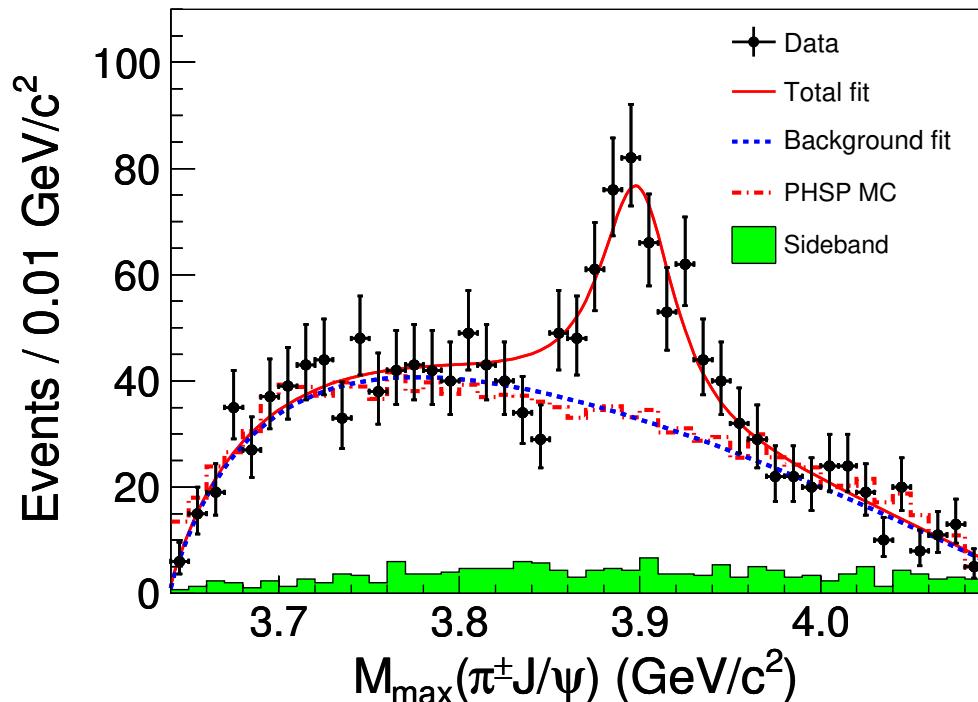
$$e^+ e^- \rightarrow \gamma_{ISR} \pi^+ \pi^- J/\psi$$



- Quantum numbers are now $J^{PC} = 1^{--}$
- Confirmed by CLEO, CLEOIII, Belle, BESIII
- Weak coupling consistent with hybrid meson

$Z_c^+(3900)$

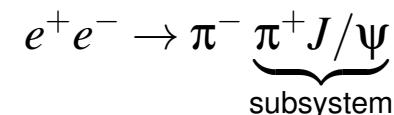
BES III (2013)



Status:

- Confirmed by several experiments
- Several states
- also Z_b^+ states seen
- PDG 2018 naming scheme:

X	now χ	Isospin 0
Y	now ψ	
Z		Isospin 1



- Decay to J/ψ :
 $\Rightarrow c\bar{c}$ content necessary
- Charged!!!!!!
 \Rightarrow at least $c\bar{c}ud\bar{d}$

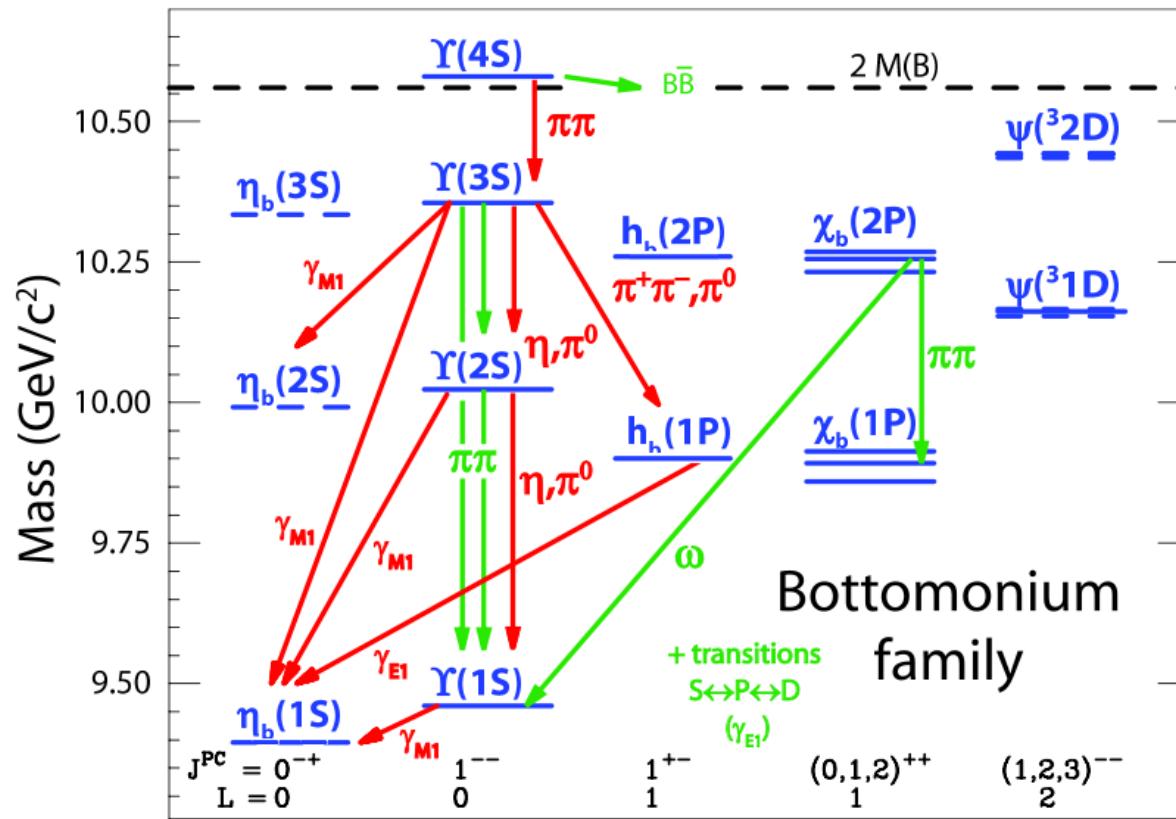
Growing number of states...

Particle Data Group (2018): States near open $c\bar{c}$ or $b\bar{b}$ threshold

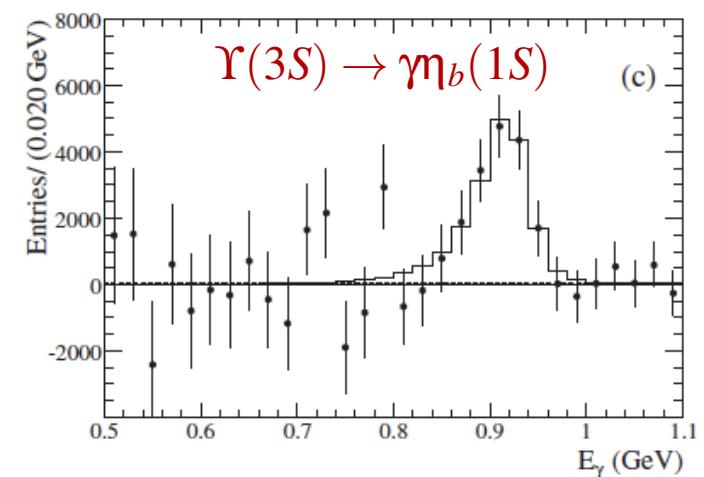
PDG Name	Former/Common Name(s)	m (MeV)	Γ (MeV)	$I^G(J^{PC})$	Production	Decay	Discovery Year	Summary Table
$\chi_{c1}(3872)$	$X(3872)$	3871.69 ± 0.17	< 1.2	$0^+(1^{++})$	$B \rightarrow KX$ $p\bar{p} \rightarrow X\dots$ $pp \rightarrow X\dots$ $e^+e^- \rightarrow \gamma X$	$\pi^+\pi^- J/\psi$ $3\pi J/\psi$ $D^{*0}\overline{D}^0$ $\gamma J/\psi$ $\gamma\psi(2S)$	2003	YES
$Z_c(3900)$		3886.6 ± 2.4	28.2 ± 2.6	$1^+(1^{+-})$	$\psi(4260) \rightarrow \pi^- X$ $\psi(4260) \rightarrow \pi^0 X$	$\pi^+ J/\psi$ $\pi^0 J/\psi$ $(D\bar{D}^*)^+$ $(D\bar{D}^*)^0$	2013	YES
$X(4020)$	$Z_c(4020)$	4024.1 ± 1.9	13 ± 5	$1^+(?^-)$	$\psi(4260, 4360) \rightarrow \pi^- X$ $\psi(4260, 4360) \rightarrow \pi^0 X$	$\pi^+ h_c$ $\pi^0 h_c$ $(D^*\bar{D}^*)^+$ $(D^*\bar{D}^*)^0$	2013	YES
$Z_b(10610)$		10607.2 ± 2.0	18.4 ± 2.4	$1^+(1^{+-})$	$\Upsilon(10860) \rightarrow \pi^- X$ $\Upsilon(10860) \rightarrow \pi^0 X$	$\pi^+ \Upsilon(1S, 2S, 3S)$ $\pi^0 \Upsilon(1S, 2S, 3S)$ $\pi^+ h_b(1P, 2P)$ $(B\bar{B}^*)^+$	2011	YES
$Z_b(10650)$		10652.2 ± 1.5	11.5 ± 2.2	$1^+(1^{+-})$	$\Upsilon(10860) \rightarrow \pi^- X$	$\pi^+ \Upsilon(1S, 2S, 3S)$ $\pi^+ h_b(1P, 2P)$ $(B^*\bar{B}^*)^+$	2011	YES

...and ≈ 25 more unassigned states above threshold

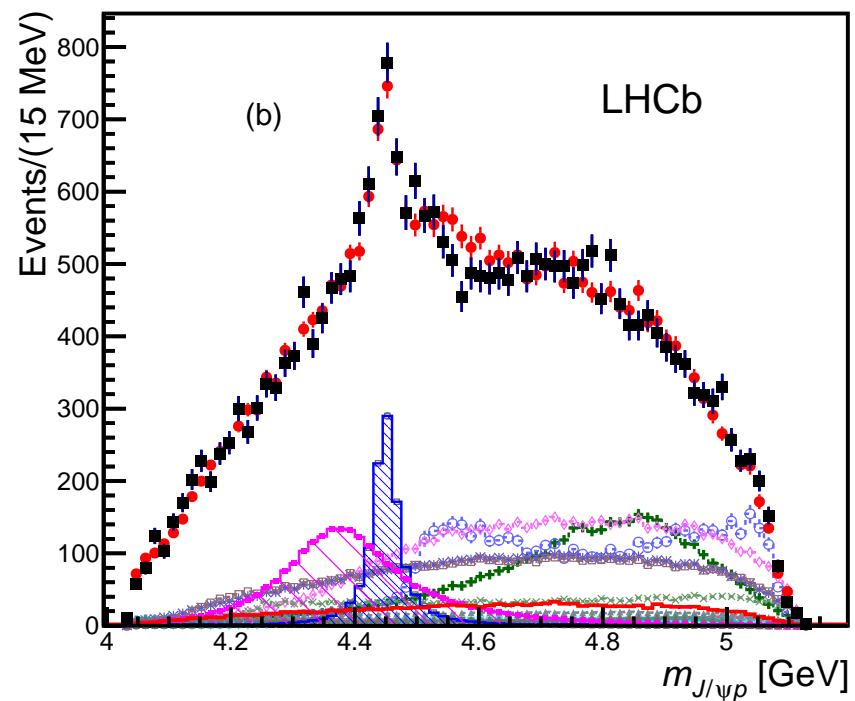
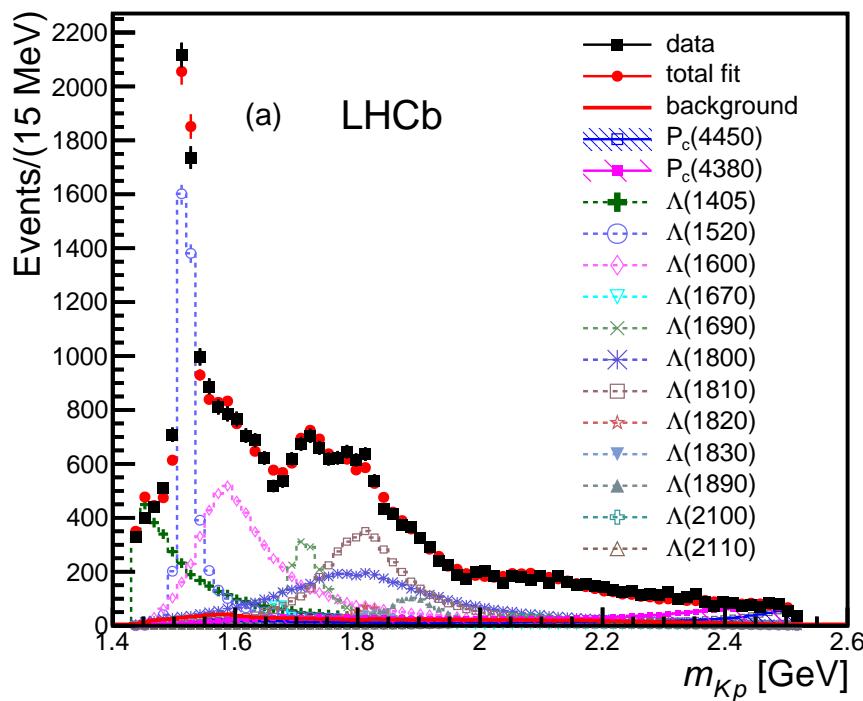
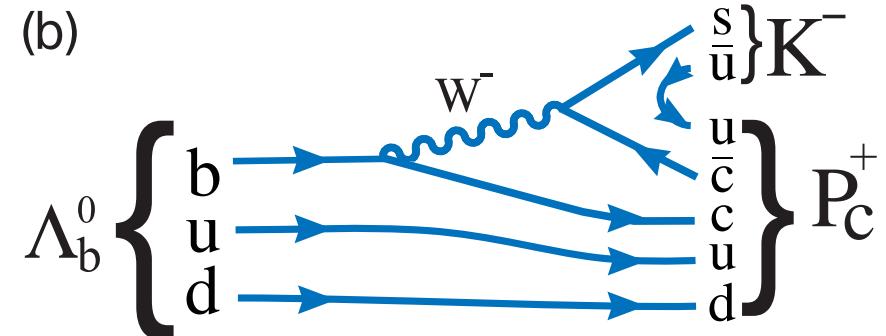
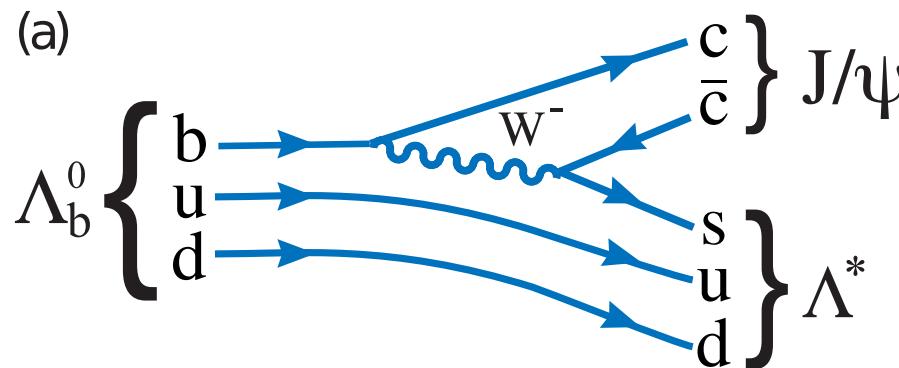
Bottomonium



- higher b -quark mass
- lower coupling $\alpha_s(Q^2)$
- dominated by Coulomb term of the potential
- better description by potential models
- ground state $\eta_b(1S)$ discovered 2008

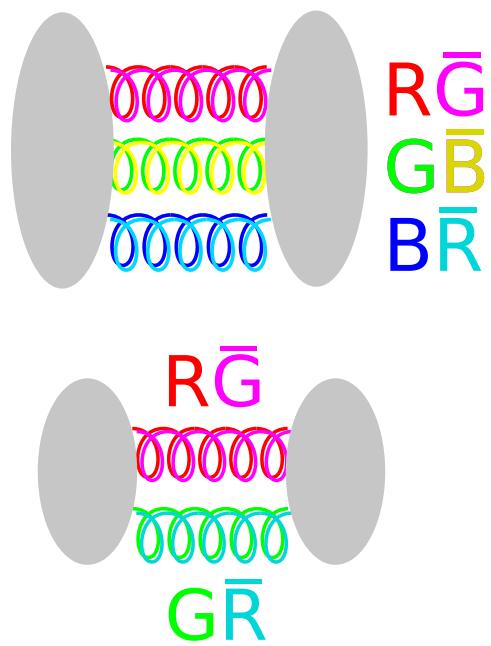
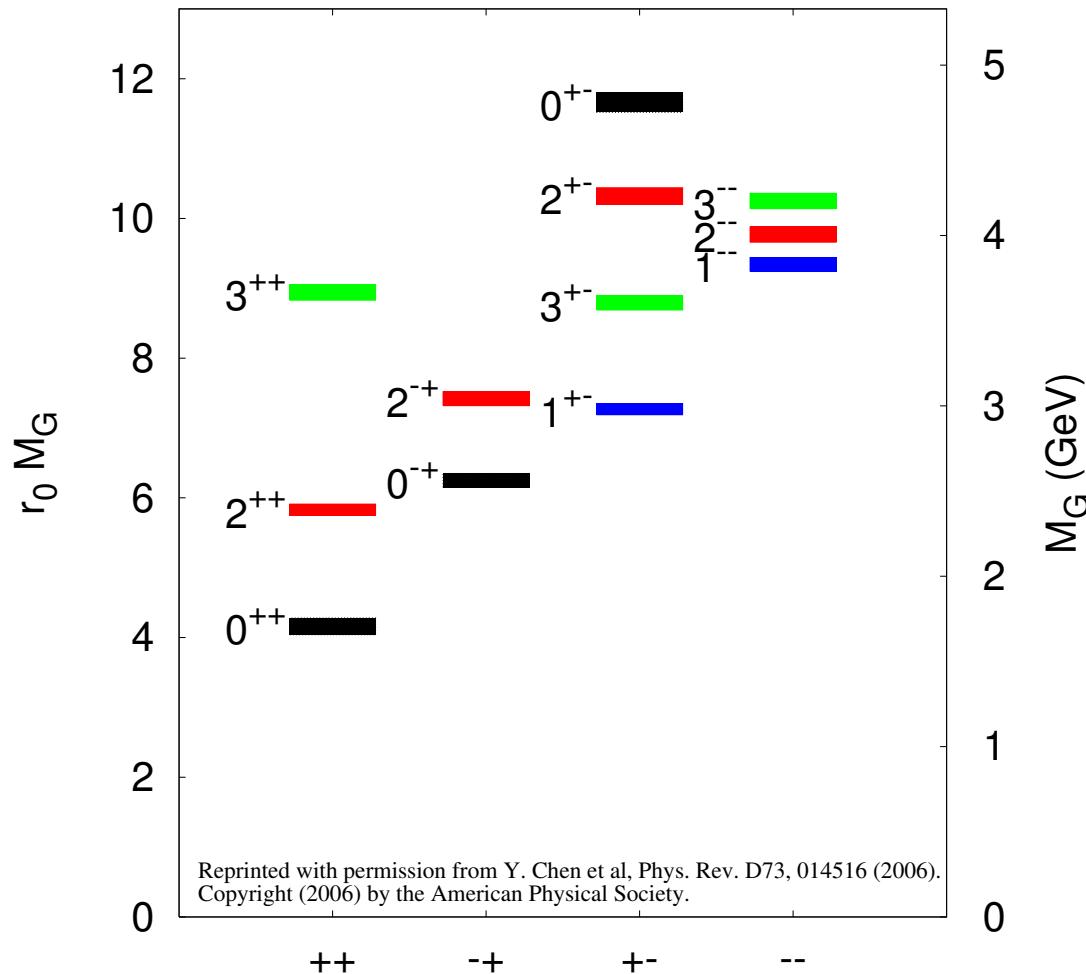


Pentaquark (LHCb 2015)



$$\Lambda_b^0 \rightarrow J/\psi + K^- + p$$

Glueballs



- Calculable in Lattice QCD
- Predictions:

$$J^{PC} = 0^{++}, 2^{++}$$

- Mixing with scalar mesons $f_0(1370)$
- Candidates $f_0(1500)$, $f_0(1710)$, ...
- No clear signature yet

Strangeness

What can we do with the *s*-quark?

Is the *s*-quark a light quark?

- Use $SU(3)$ Chiral Perturbation Theory
- $m_u = 2.2 \text{ MeV}/c \approx m_d = 4.4 \text{ MeV}/c \approx 0$
- $m_s = 96 \text{ MeV}/c$

\Rightarrow ChPT works “fairly well”

Is the *s* quark a heavy quark?

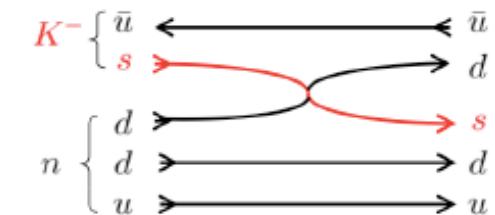
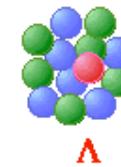
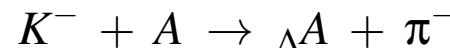
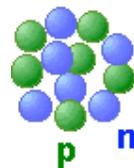
- Use a potential model
- Use constituent quark masses
- $m_\Lambda = 1116 \text{ MeV}/c \Rightarrow m_u = m_d = 300 \text{ MeV}/c; \quad m_s = 500 \text{ MeV}/c \gg 96 \text{ MeV}/c$

\Rightarrow Potential model works “fairly well”

\Rightarrow no precision expected

Hypernuclei

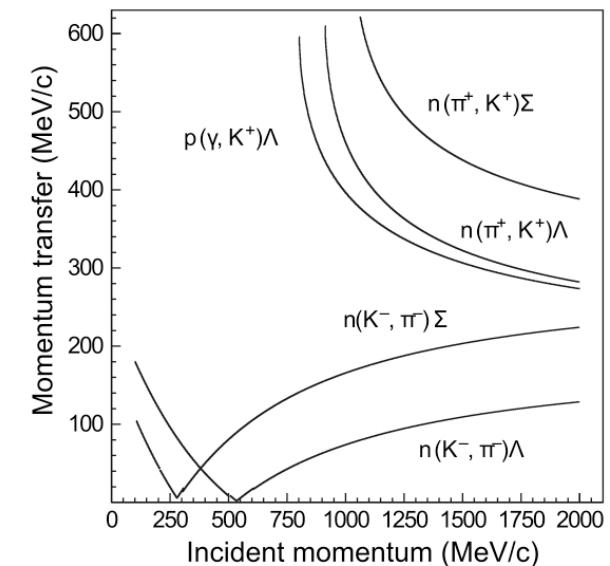
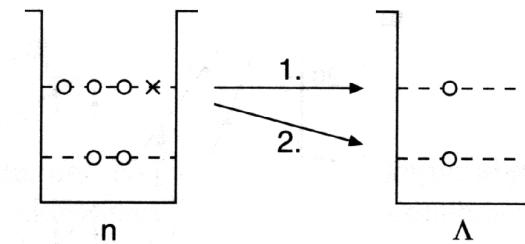
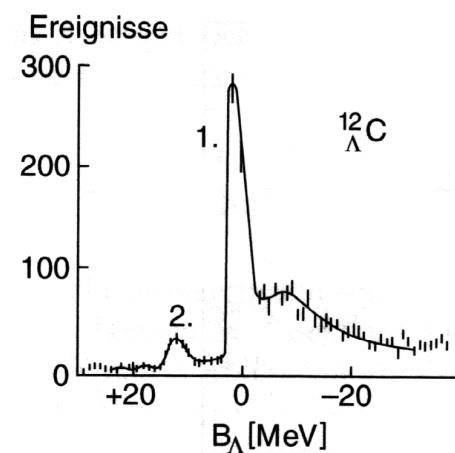
Idea: Use strangeness to mark e.g. a single particle in a nuclei!



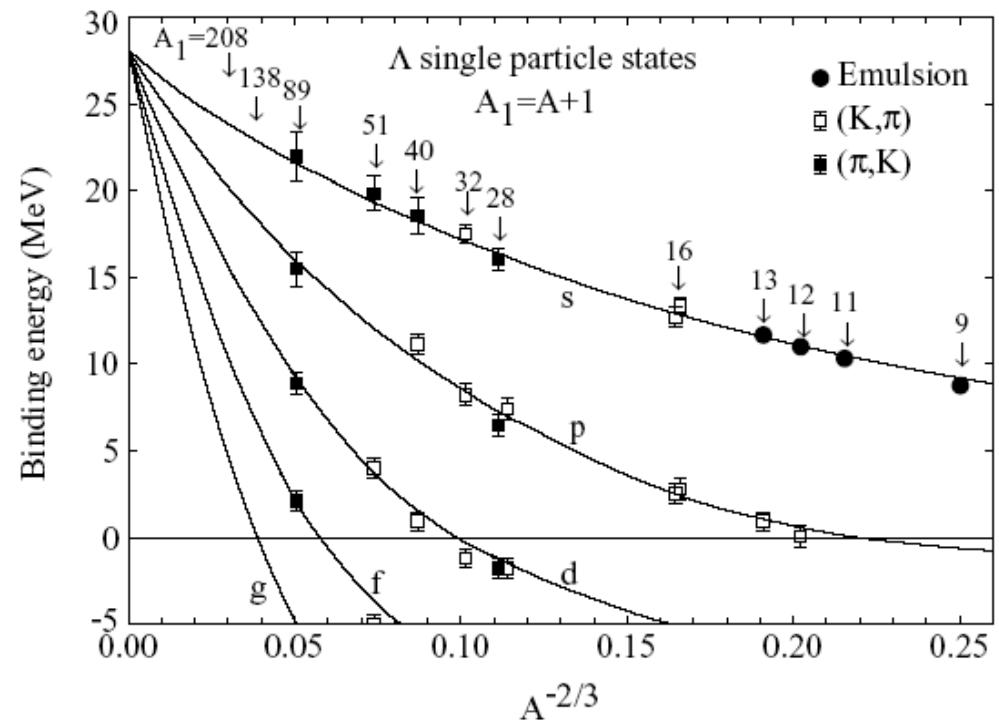
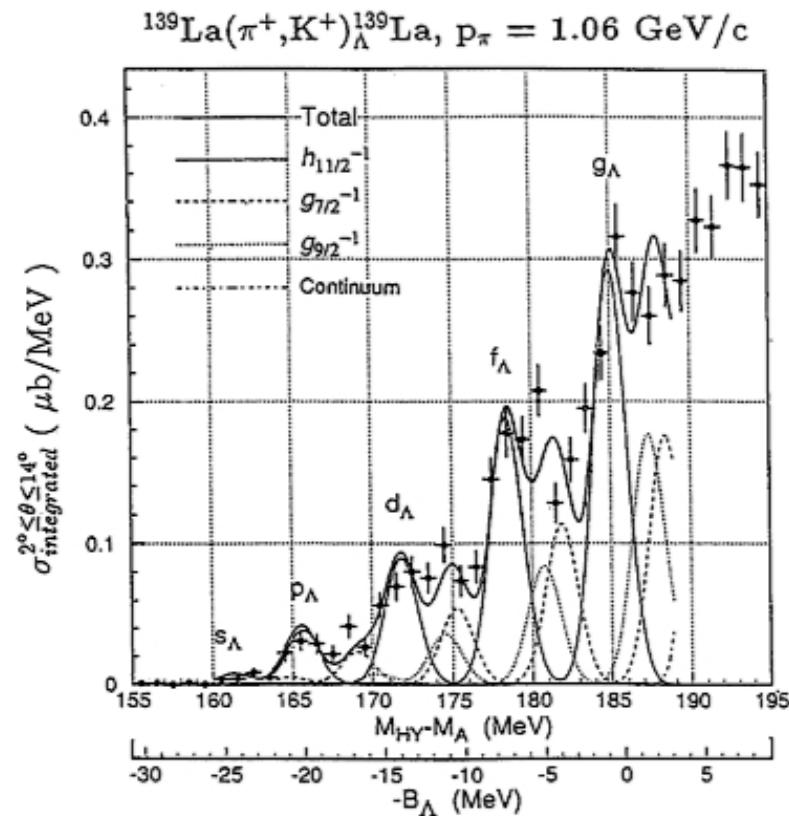
Recoil-less production possible!

⇒ no momentum transfer to the nuclear target

No Pauli-blocking! Hyperons test all states of the potential



Hypernuclei



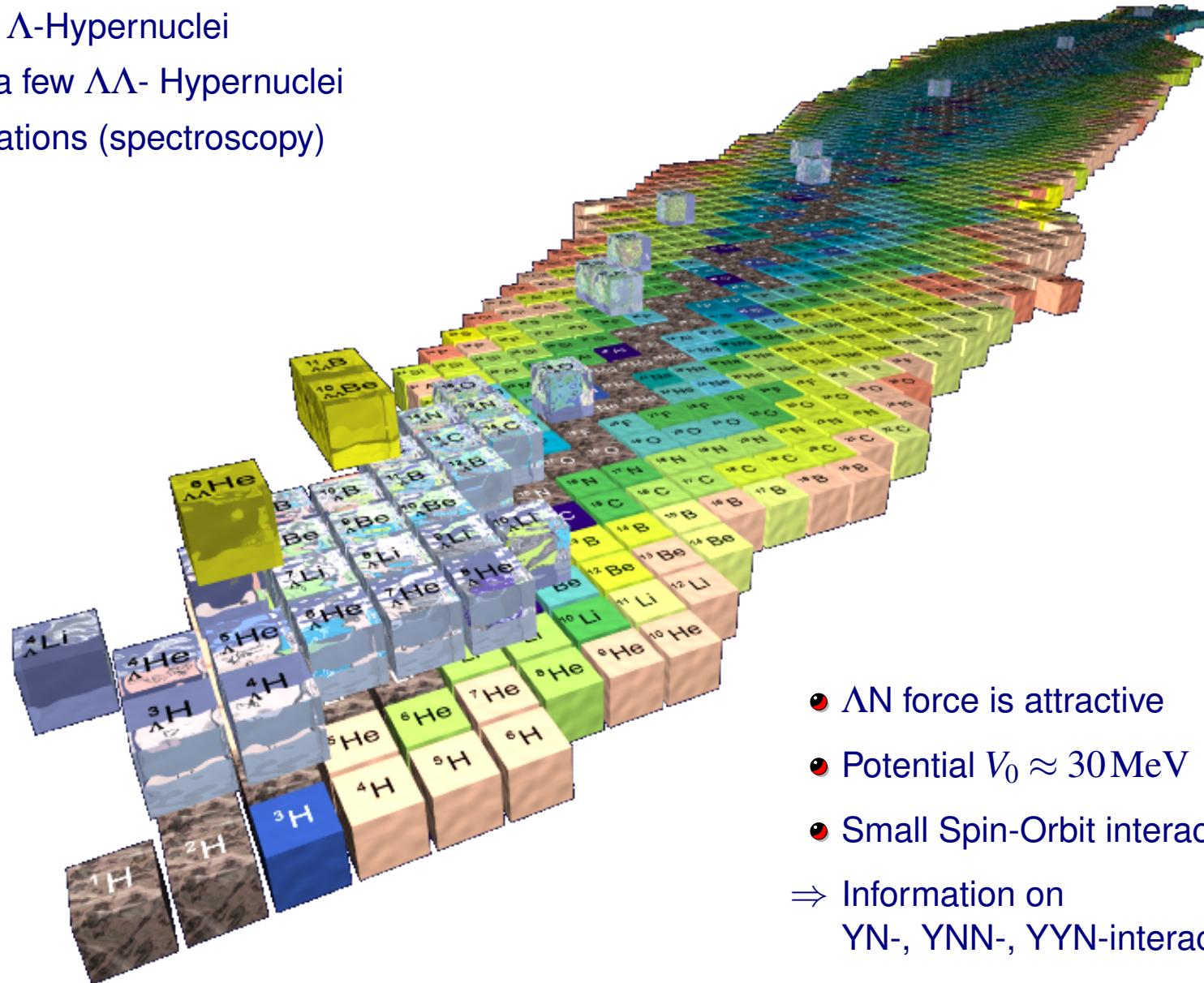
- Complete mapping of the shell structure (single particle states)
- Model potential → deduce hyperon-N interaction
- Excitation spectrum, e.g. via electron scattering

Hypernuclei

$\approx 40 \Lambda$ -Hypernuclei

only a few $\Lambda\Lambda$ - Hypernuclei

Excitations (spectroscopy)



- ΛN force is attractive
 - Potential $V_0 \approx 30 \text{ MeV}$
 - Small Spin-Orbit interaction
- ⇒ Information on
YN-, YNN-, YYN-interaction

Neutron Stars



Neutron Stars

Baronic Number $N_B \sim 10^{57}$

Mass $M \sim 1 - 2 M_\odot$

Radius $R \sim 10 - 12 \text{ km}$

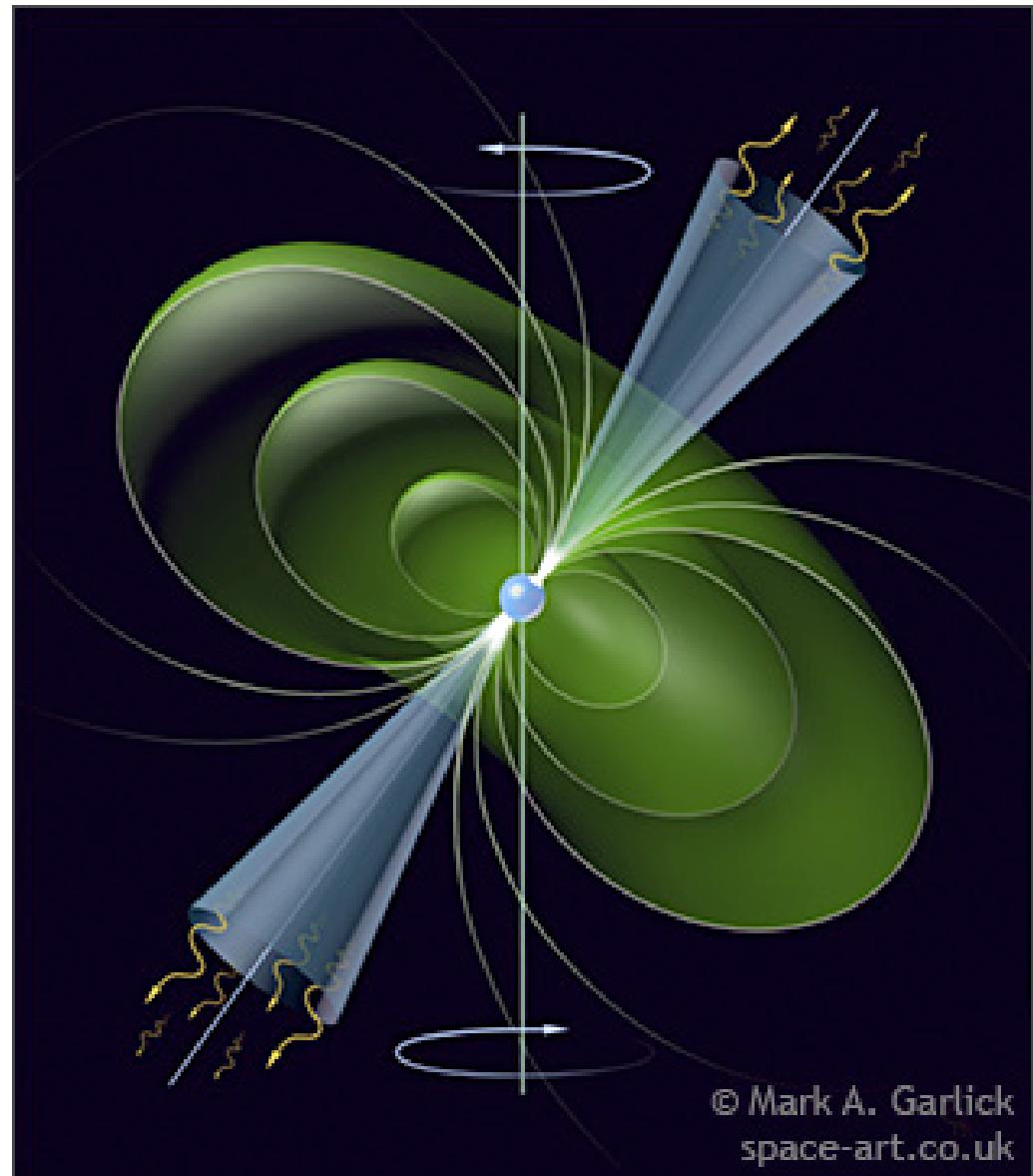
Density $\rho \sim 10^{15} \frac{\text{g}}{\text{cm}^3}$

Magnetic Field $B \sim 10^{8 \dots 16} \text{ G}$

Electric Field $E \sim 10^{18} \frac{\text{V}}{\text{cm}}$

Temperature $T \sim 10^{6 \dots 11} \text{ K}$

shortest Rotation $t \sim 1.58 \text{ ms}$



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Equilibrium of electro-weak force:



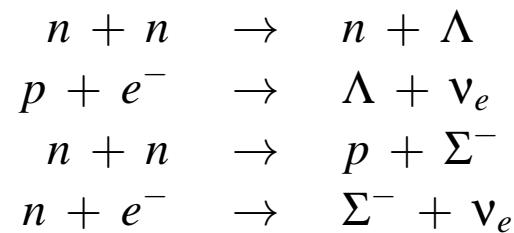
Definition Baryo-Chemical Potential:

$$\mu = \frac{dE}{dn} \quad \text{Change of energy with number}$$

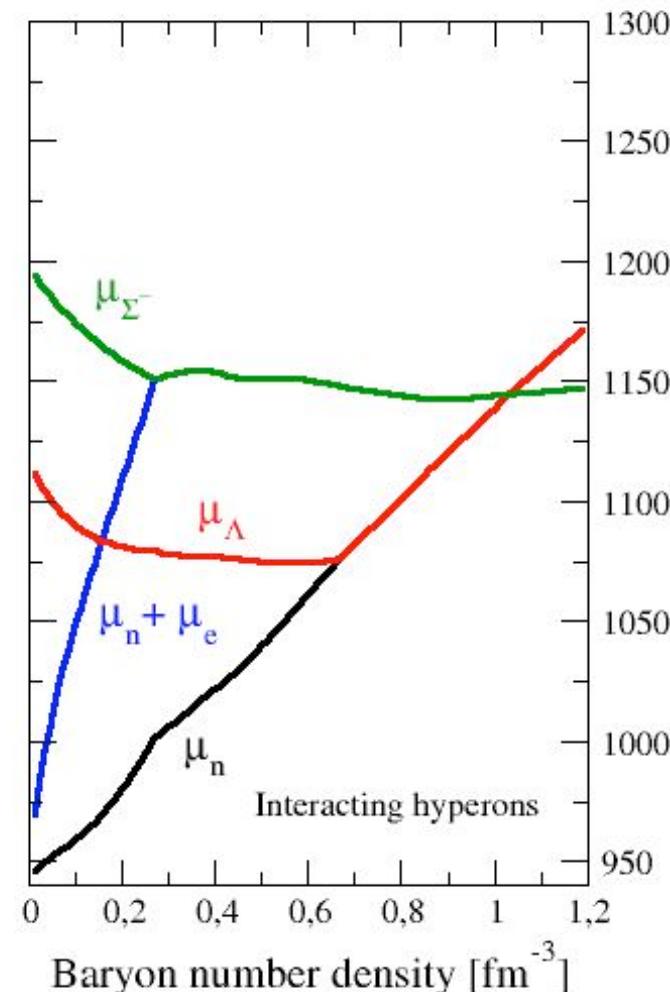
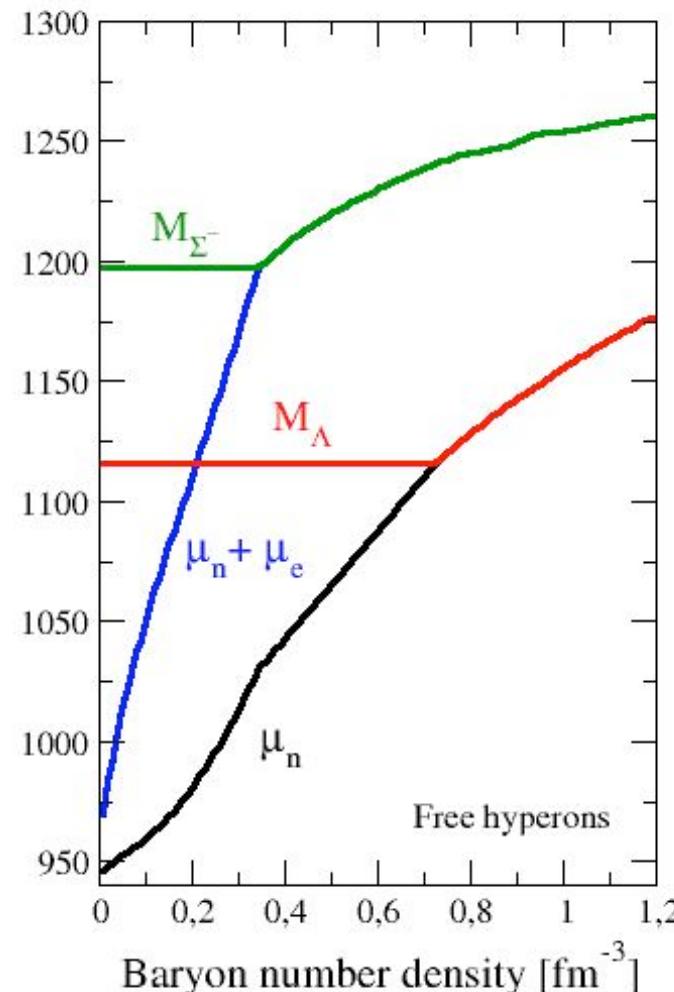
simplifies equilibrium condition for n, p :

$$\mu_n = \mu_p + \mu_e + \mu_{\bar{\nu}}$$

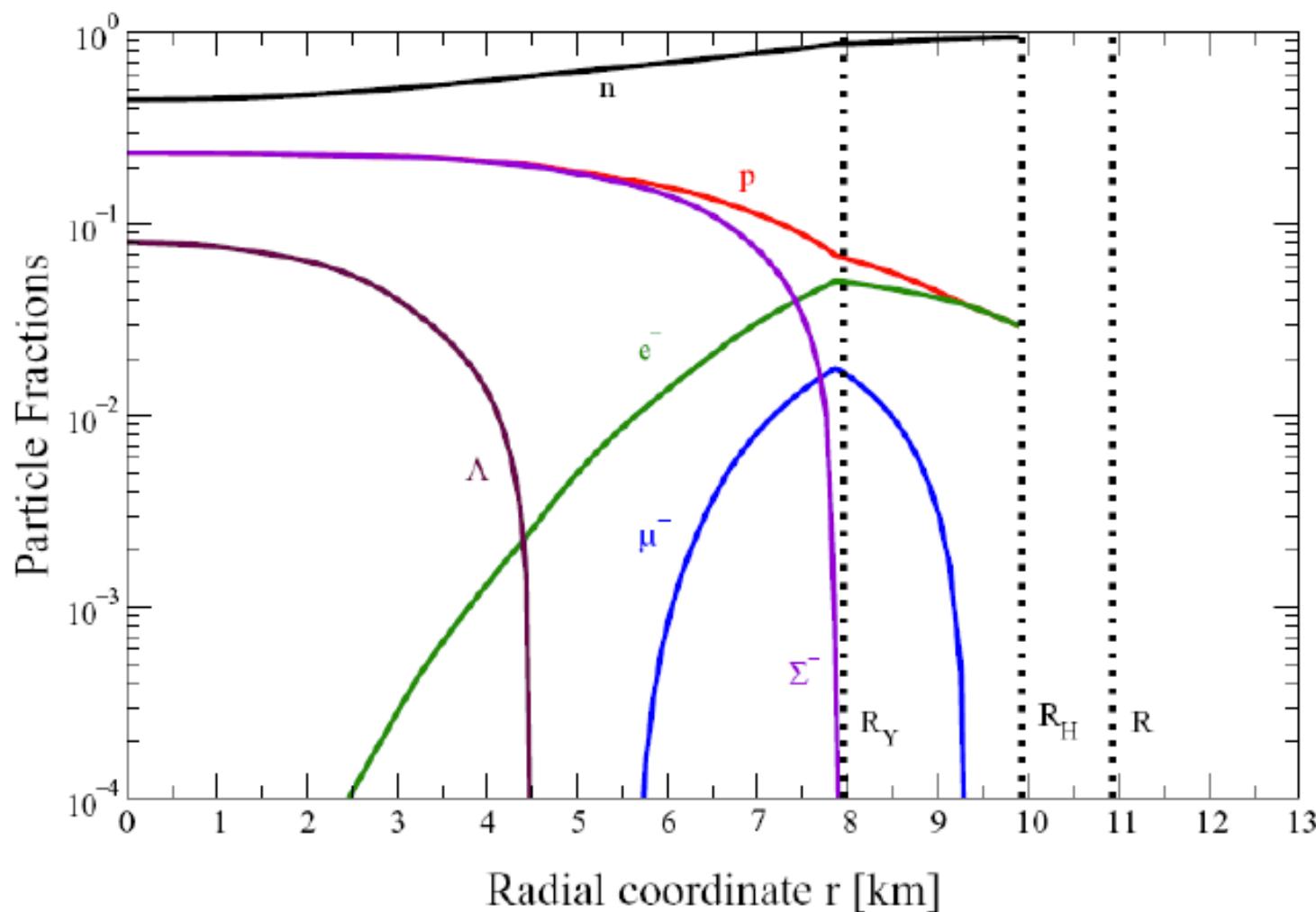
Hyperon content of Neutron Stars



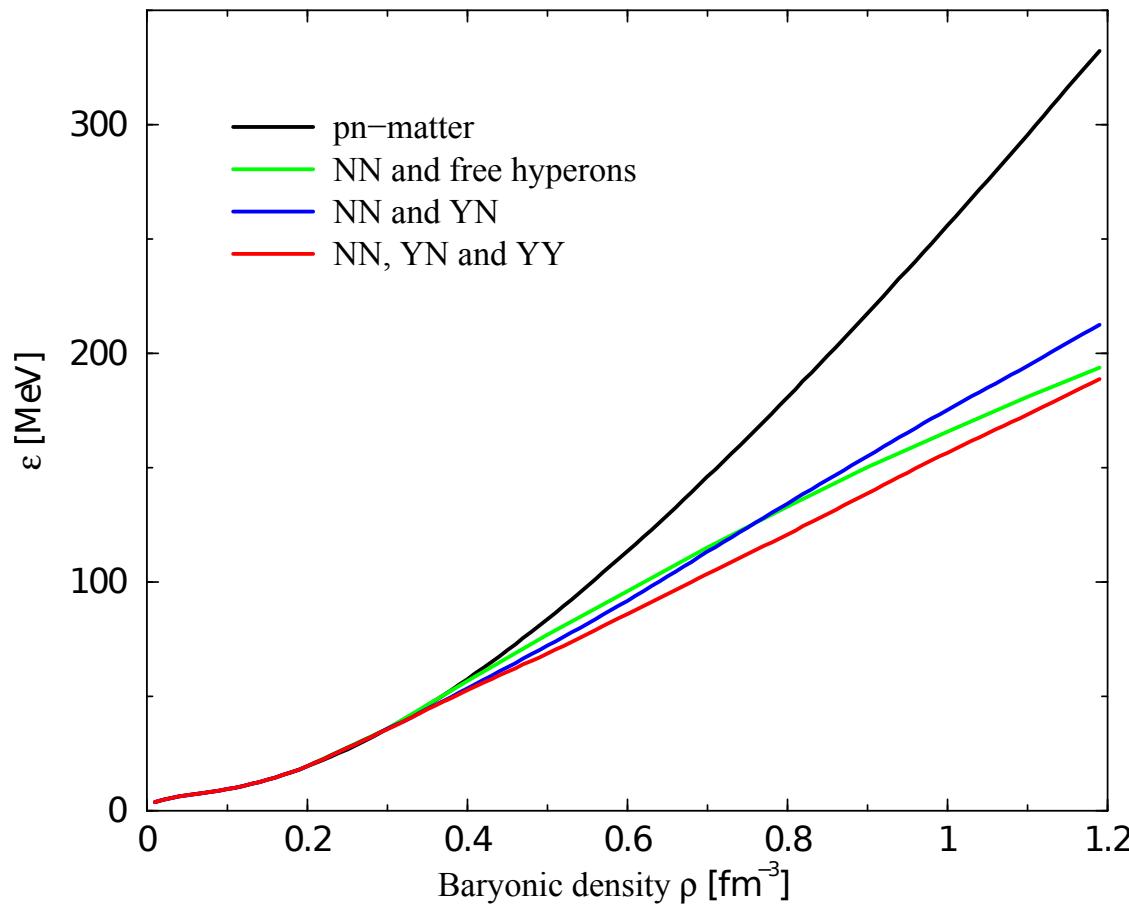
$$\begin{aligned}
 \mu_{\Sigma}^- &= \mu_n + \mu_{e^-} + \mu_{\nu_e} \\
 \mu_{\Lambda} &= \mu_n
 \end{aligned}$$



Hyperon content of Neutron Stars



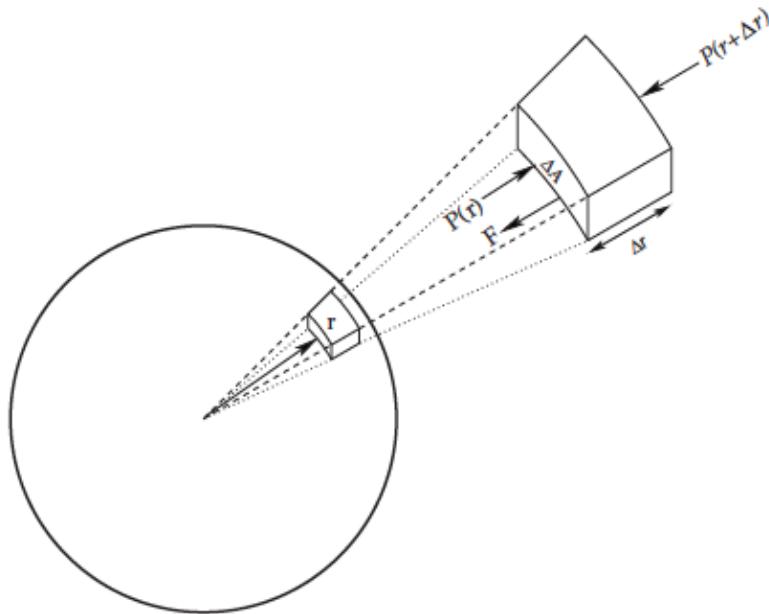
Equation of State



- Equation of State $\varepsilon(\rho)$ (or equivalent $P(\rho) = \rho^2 d(\varepsilon/\rho)/d\rho$) defines hydrostatic properties
- Hyperons “soften” the Equation of State
- What does this mean for a neutron star?

Neutron Star Structure

Newtonian Approach:



Differential Force:

$$F_r = -\frac{GM(r)\Delta m}{r^2} - P(r+\Delta r)\Delta A + P(r)\Delta A = \Delta m \frac{d^2 r}{dt^2}$$

Equilibrium ($\ddot{r} = \dot{r} = 0$) :

$$-\frac{GM(r)\rho(r)}{r^2} - \frac{dP(r)}{dr} = \rho(r) \frac{d^2 r}{dt^2} = 0$$

$$\frac{dP}{dr} = -\frac{GM(r)\rho(r)}{r^2} \quad P(0) = P_c$$

$$\frac{dm}{dr} = 4\pi r^2 \rho(r) \quad m(0) = m_c$$

Neutron star structure

Relativistic Approach:

- Escape velocity

$$\frac{1}{2}mv^2 = \frac{GMm}{R} \Rightarrow v \approx \frac{c}{2}$$

⇒ relativistic effects are important

- Solve Einstein's field Equation with Energy-Density Tensor of stellar matter $T^{\mu\nu}(\varepsilon, P(\varepsilon))$

$$\begin{aligned} G^{\mu\nu} &= 8\pi T^{\mu\nu}(\varepsilon, P(\varepsilon)) \\ \varepsilon &= \rho c^2 \end{aligned}$$

- Solution possible for **symmetric, non-rotating star**:

$$\frac{dP}{dr} = -\frac{Gm\varepsilon}{c^2r^2} \left(1 + \frac{P}{\varepsilon}\right) \left(1 + \frac{4\pi r^3 P}{c^2 m}\right) \left(1 - \frac{2Gm}{c^2 r}\right)^{-1}$$

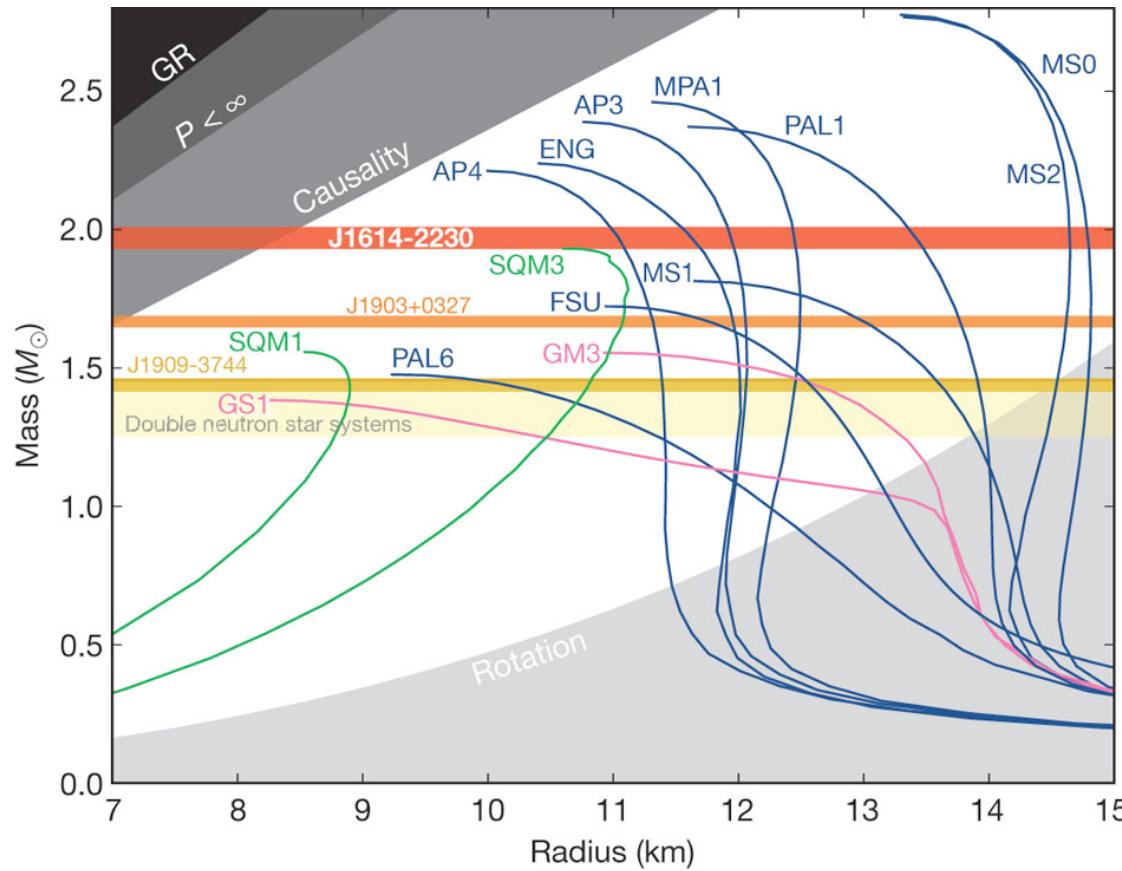
$$\frac{dm}{dr} = \frac{4\pi r^2 \varepsilon}{c^2}$$

$$P(0) = P(\varepsilon_c) \quad P(R) = 0$$

$$m(0) = 0 \quad m(R) = M$$

Tolman-Oppenheimer-Volkoff equations

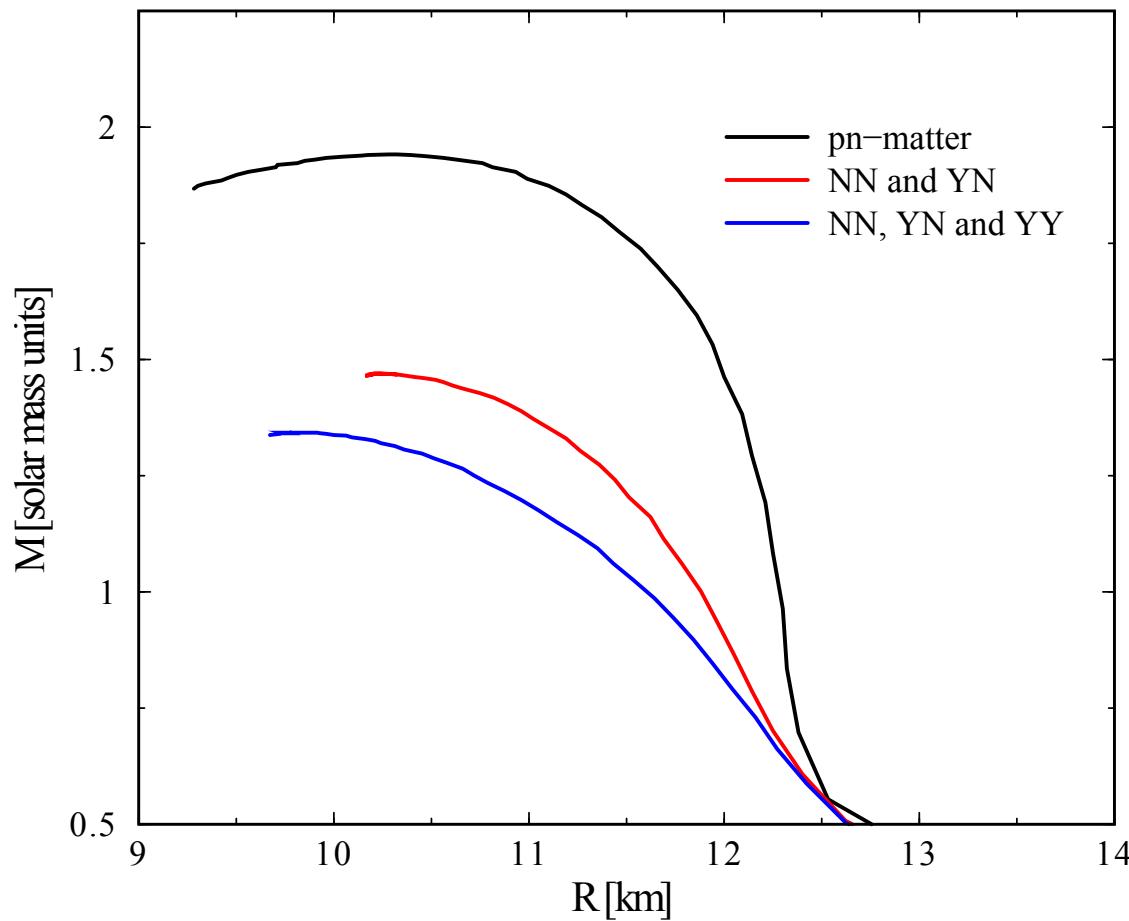
Mass – Radius Plots



Constraints:

- **General Relativity (GR):** Neutron Star is not a black hole $\Rightarrow R > \frac{2GM}{c^2}$
- **Compressibility (Stability):** $dP/d\rho > 0$ $\Rightarrow R > \frac{9}{4} \frac{GM}{c^2}$
- **Causality:** Speed of sound less than speed of light $\Rightarrow R > \frac{9}{4} \frac{GM}{c^2}$
- **Rotation:** Centrifugal force less than gravitational force $\Rightarrow R < \left(\frac{GM}{2\pi}\right)^{1/3} \frac{1}{v^{2/3}}$

Neutron Star with Strangeness



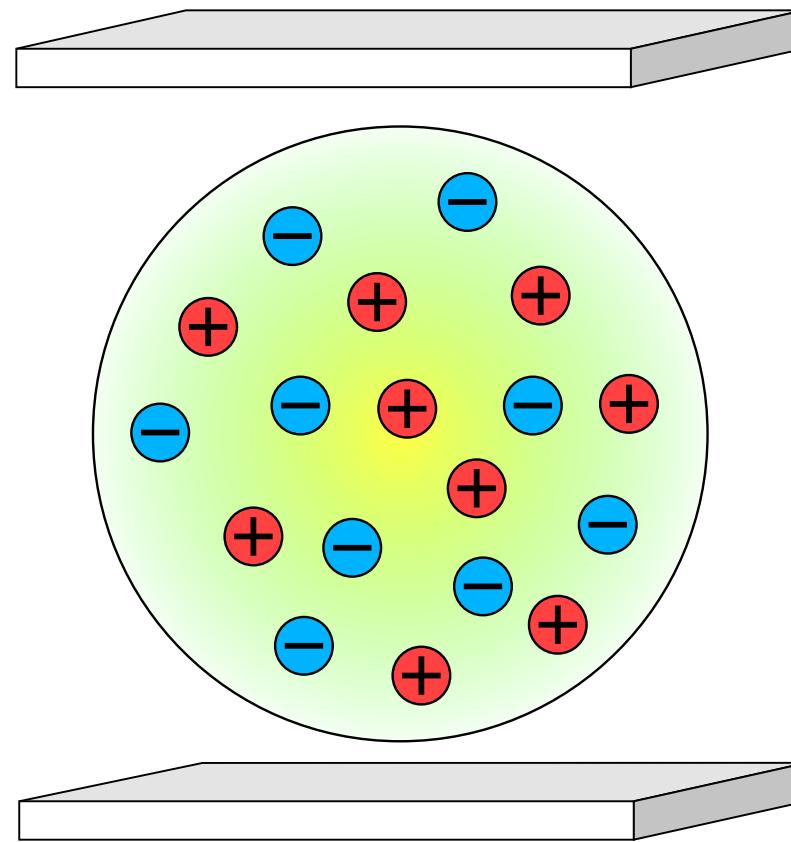
Hyperon Puzzle:

- Softening of Equation of State by Hyperons
- Reduction of maximal Neutron Star Mass by $0.5 M_{\odot}$
- Clear contradiction to observation of $2 M_{\odot}$

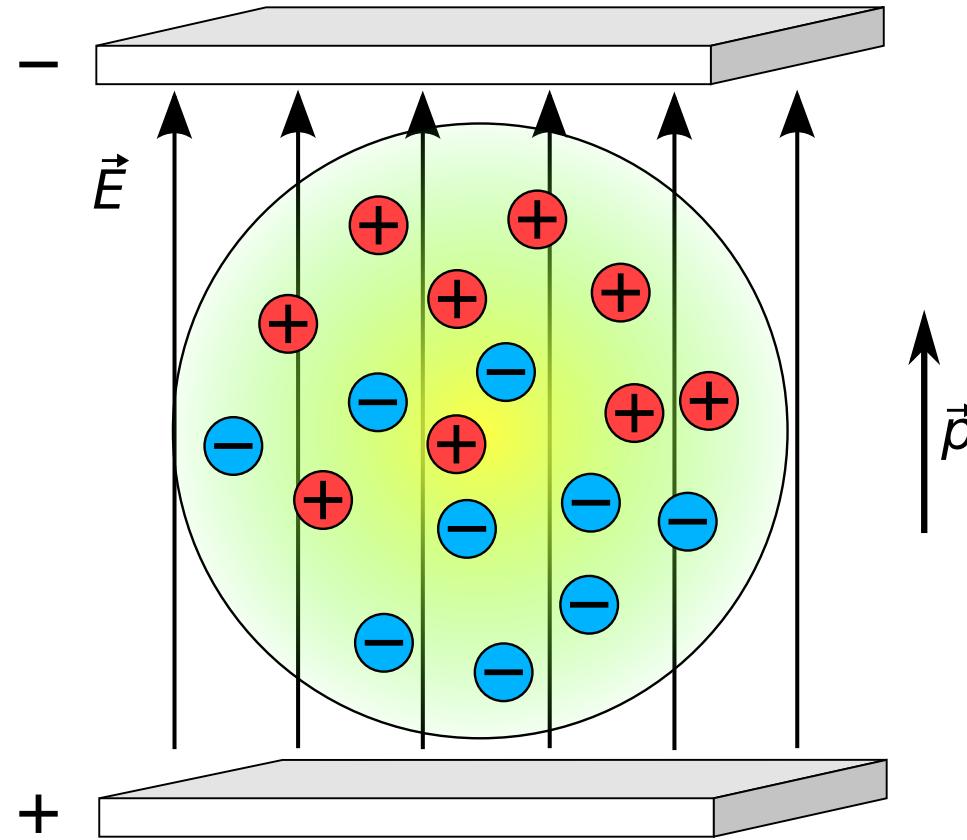
⇒ Study hyperons in medium in Experiment/Theory

Polarizabilities

Electric Polarizability: α



Electric Polarizability: α

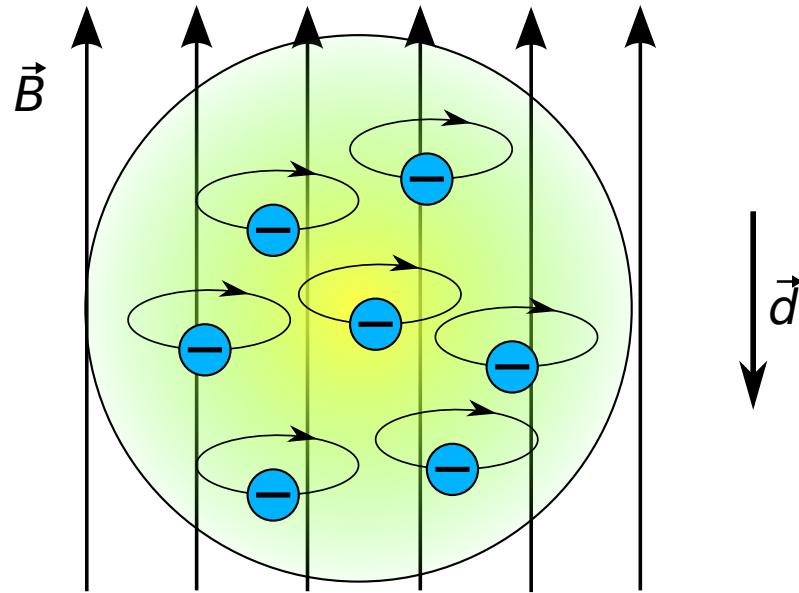


Polarizability α : induced dipole moment $\vec{p} = \alpha \vec{E}$

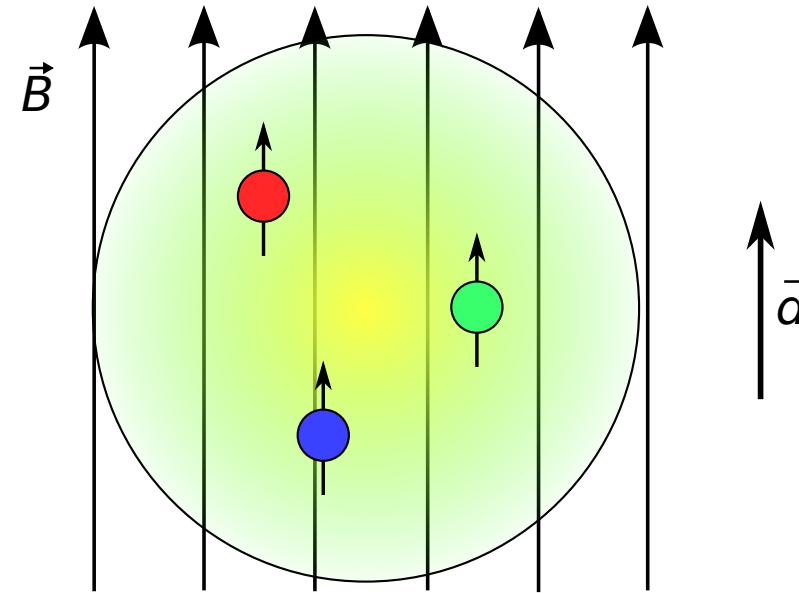
$$\left. \begin{aligned} |\vec{p}| &= e \cdot 1 \text{ fm} \\ \alpha &= 10 \cdot 10^{-4} \text{ fm}^3 \end{aligned} \right\} \Rightarrow |\vec{E}| = 1.4 \frac{\text{GV}}{\text{fm}}$$

Magnetic Polarizability: β

Diamagnetic



Paramagnetic



- Induced circular eddy currents
- \vec{p} opposite to external field \vec{B}
- Polarizability $\beta < 0$

- Alignment of spins
- \vec{p} parallel to external field \vec{B}
- Polarizability $\beta > 0$

What do we expect?

Diamagnetic:

- Only a fraction of the charge is carried by valence quarks
- χ PT: Relevant degrees of freedom:

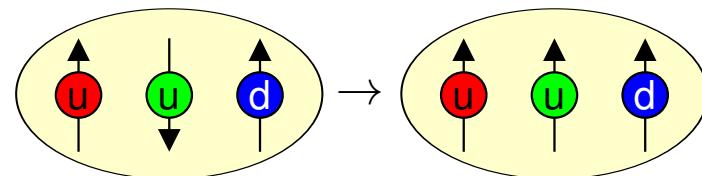
$$\pi^+, \pi^-, \pi^0$$

- Pion cloud

\Rightarrow Currents of spinless charged particles

Paramagnetic:

- Resonance Structure of Nucleons
- Example: $N \rightarrow \Delta(1232)$ excitation:



\Rightarrow Photon induced spin flip $\frac{1}{2} \rightarrow \frac{3}{2}$

Questions:

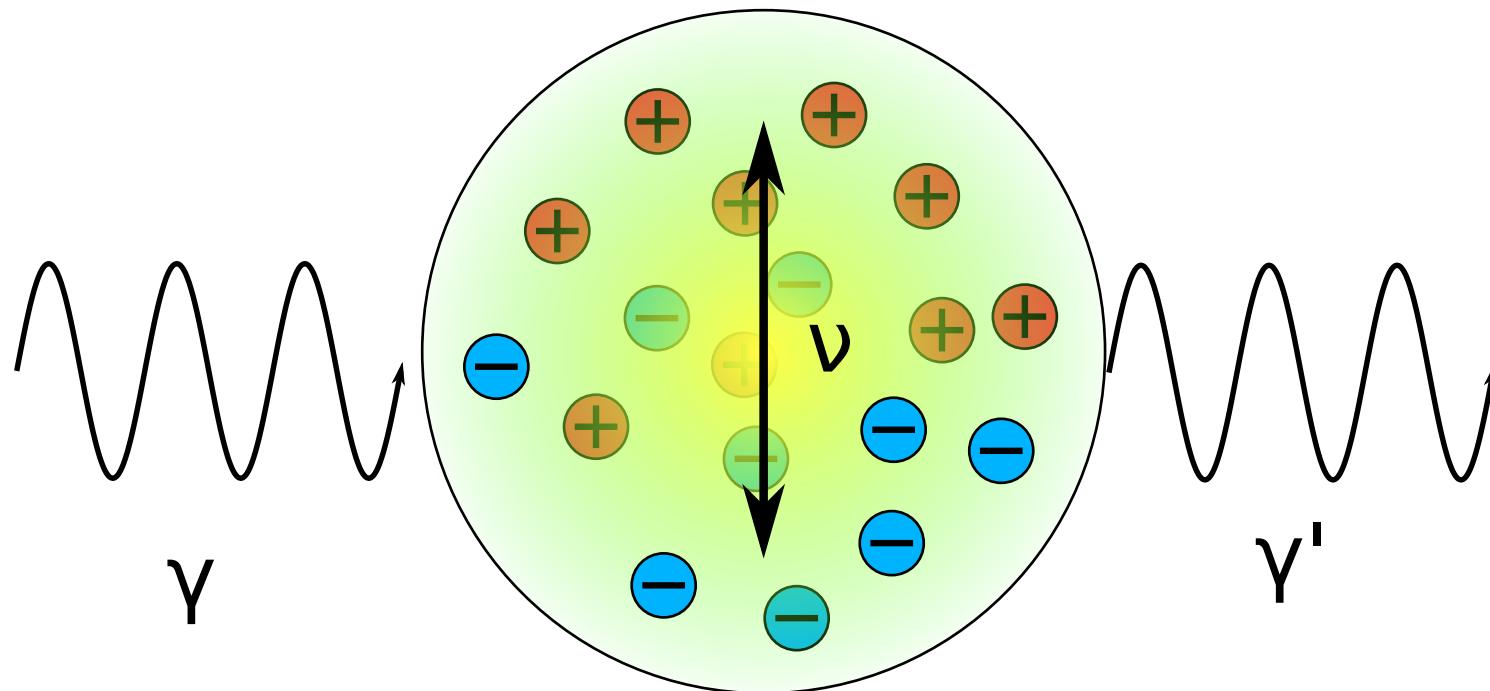
- How to distinguish? \Rightarrow Sign of β
- Transition with energy?
- Transition with resolution (photon virtuality q^2)?

Dynamical Measurement

Huge fields required:

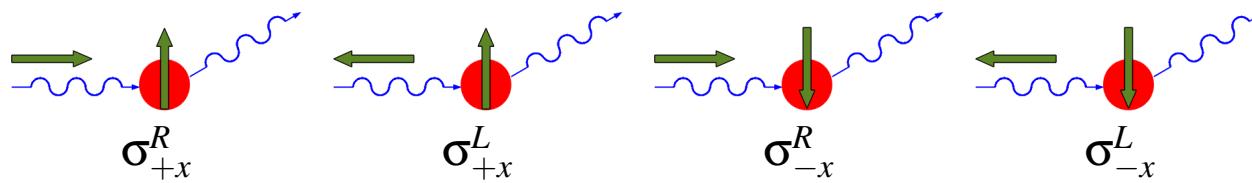
$$\left. \begin{array}{l} |\vec{p}| = e \cdot 1 \text{ fm} \\ \alpha = 10 \cdot 10^{-4} \text{ fm}^3 \end{array} \right\} \Rightarrow |\vec{E}| = 1.4 \frac{\text{GV}}{\text{fm}}$$

Absorption and Emission of photon \Rightarrow COMPTON SCATTERING

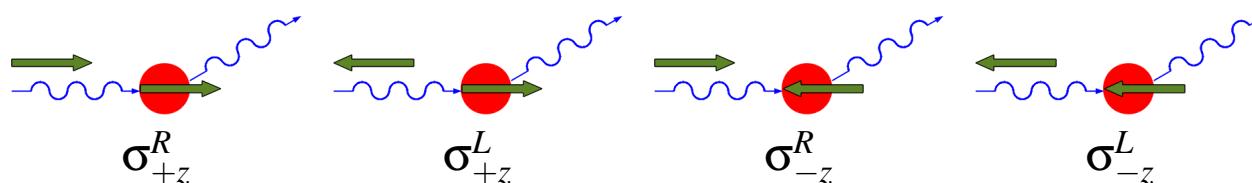


$$\frac{d\sigma}{d\Omega} = \frac{d\sigma_0}{d\Omega} - \frac{e^2}{4\pi m_p} \left(\frac{q'}{q} \right)^2 q q' \left\{ \frac{1}{2} (\bar{\alpha} + \bar{\beta}) (1 + \cos \theta)^2 + \frac{1}{2} (\bar{\alpha} - \bar{\beta}) (1 - \cos \theta)^2 \right\} + \dots$$

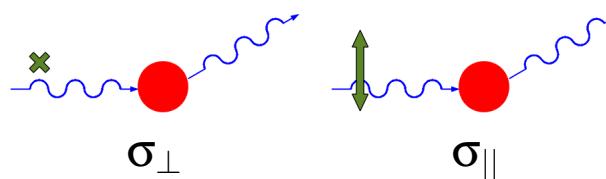
Polarized Target and polarized beam



$$\Sigma_{2x} = \frac{\sigma_{+x}^R - \sigma_{+x}^L}{\sigma_{+x}^R + \sigma_{+x}^L}$$



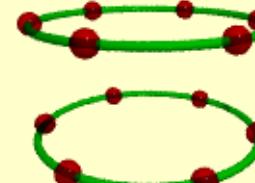
$$\Sigma_{2z} = \frac{\sigma_{+z}^R - \sigma_{+z}^L}{\sigma_{+z}^R + \sigma_{+z}^L}$$



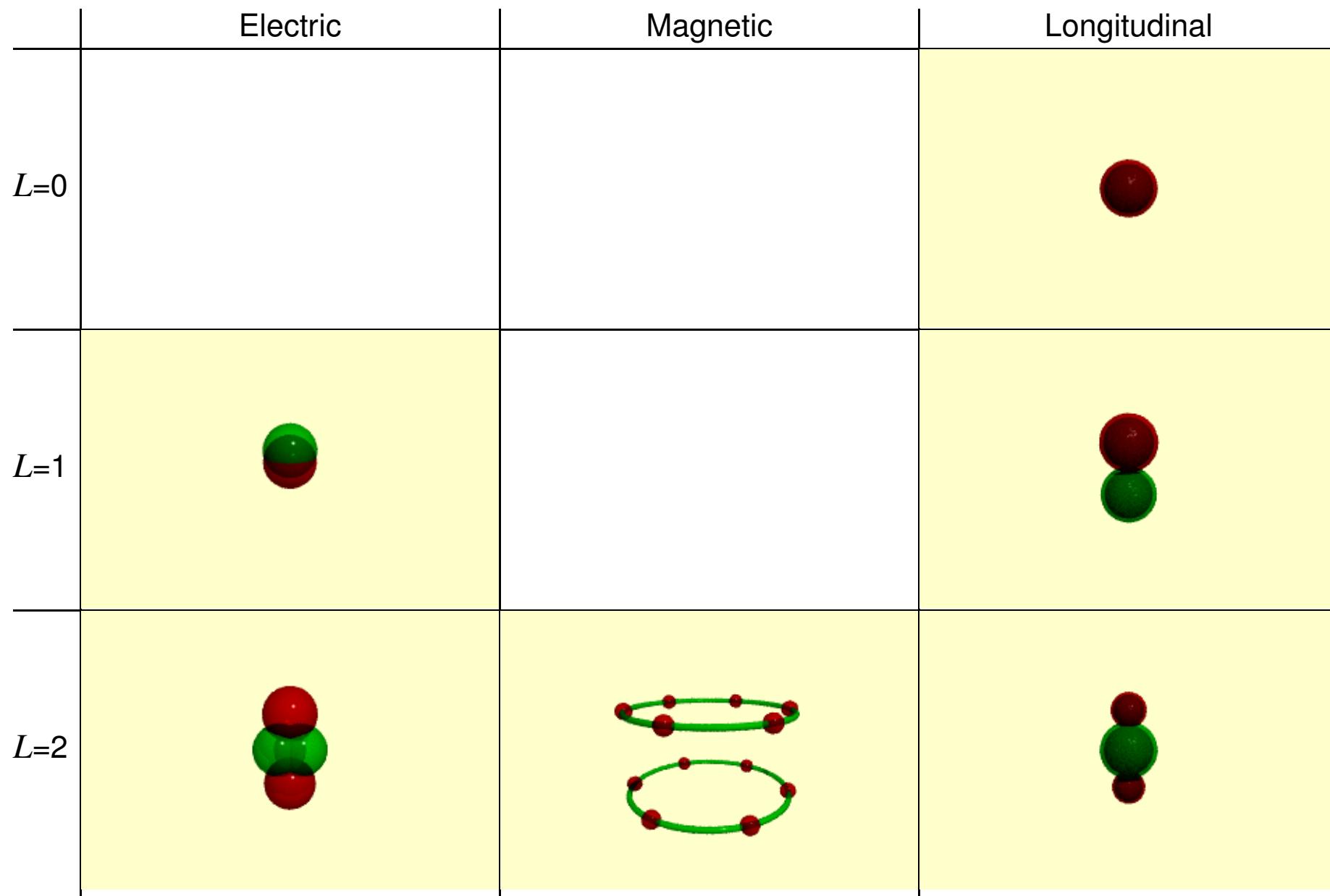
$$\Sigma_3 = \frac{\sigma_\perp - \sigma_\parallel}{\sigma_\perp + \sigma_\parallel}$$

⇒ spin polarizabilities γ_{E1E1} , γ_{M1M1} , γ_{E1M2} , γ_{M1E2}

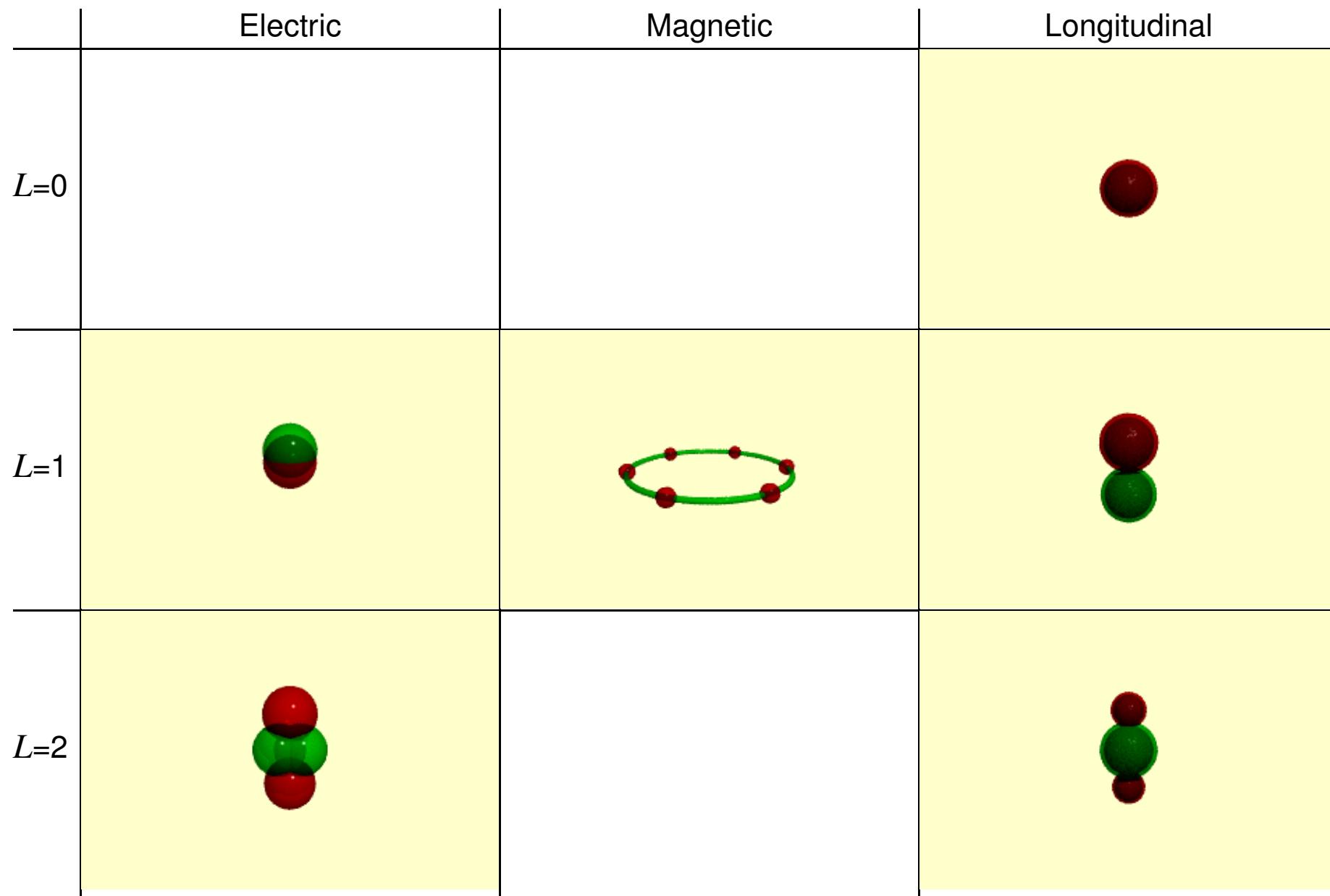
Spin Polarizabilities

	Electric	Magnetic	Longitudinal
$L=0$			
$L=1$			
$L=2$			

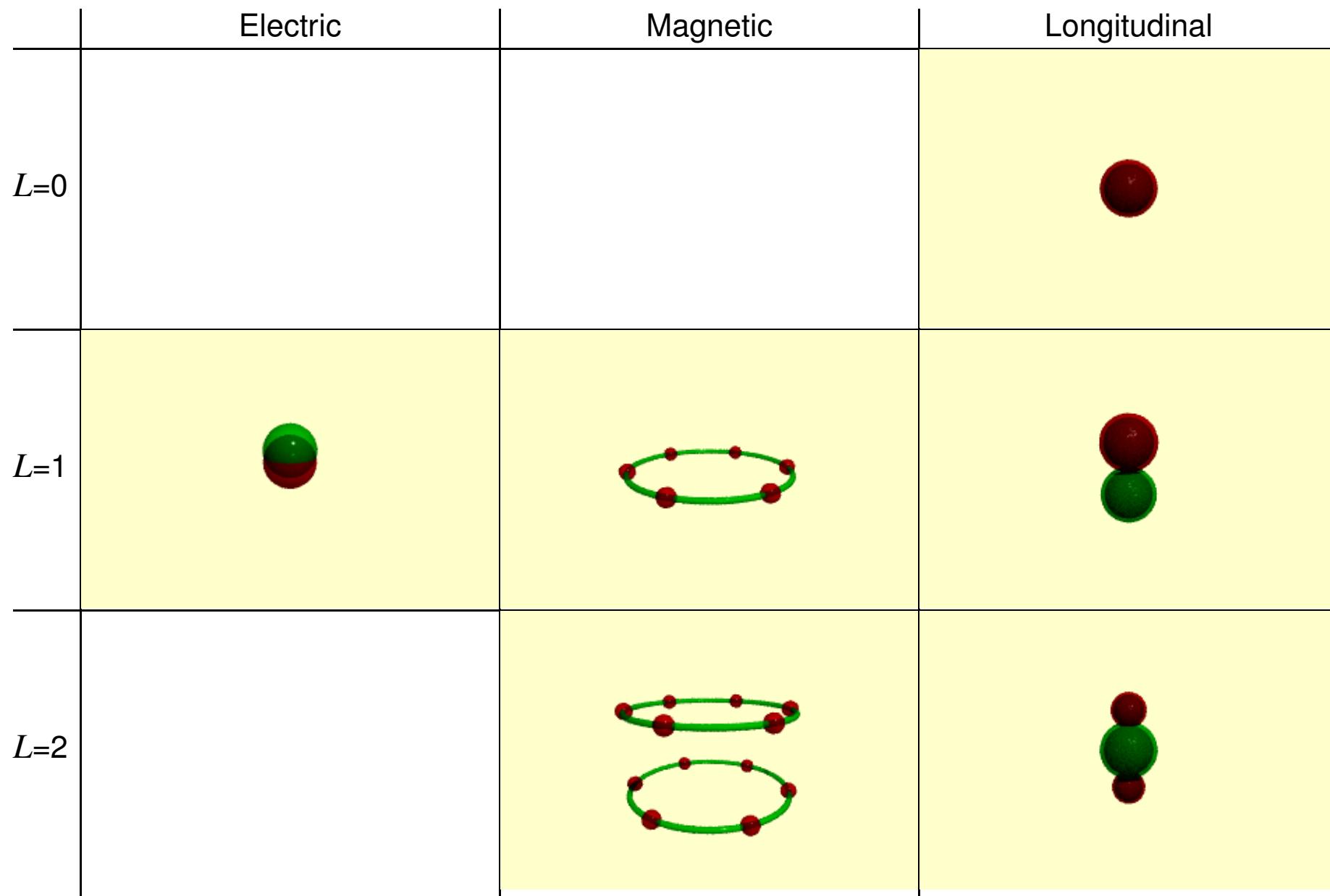
Spin Polarizabilities



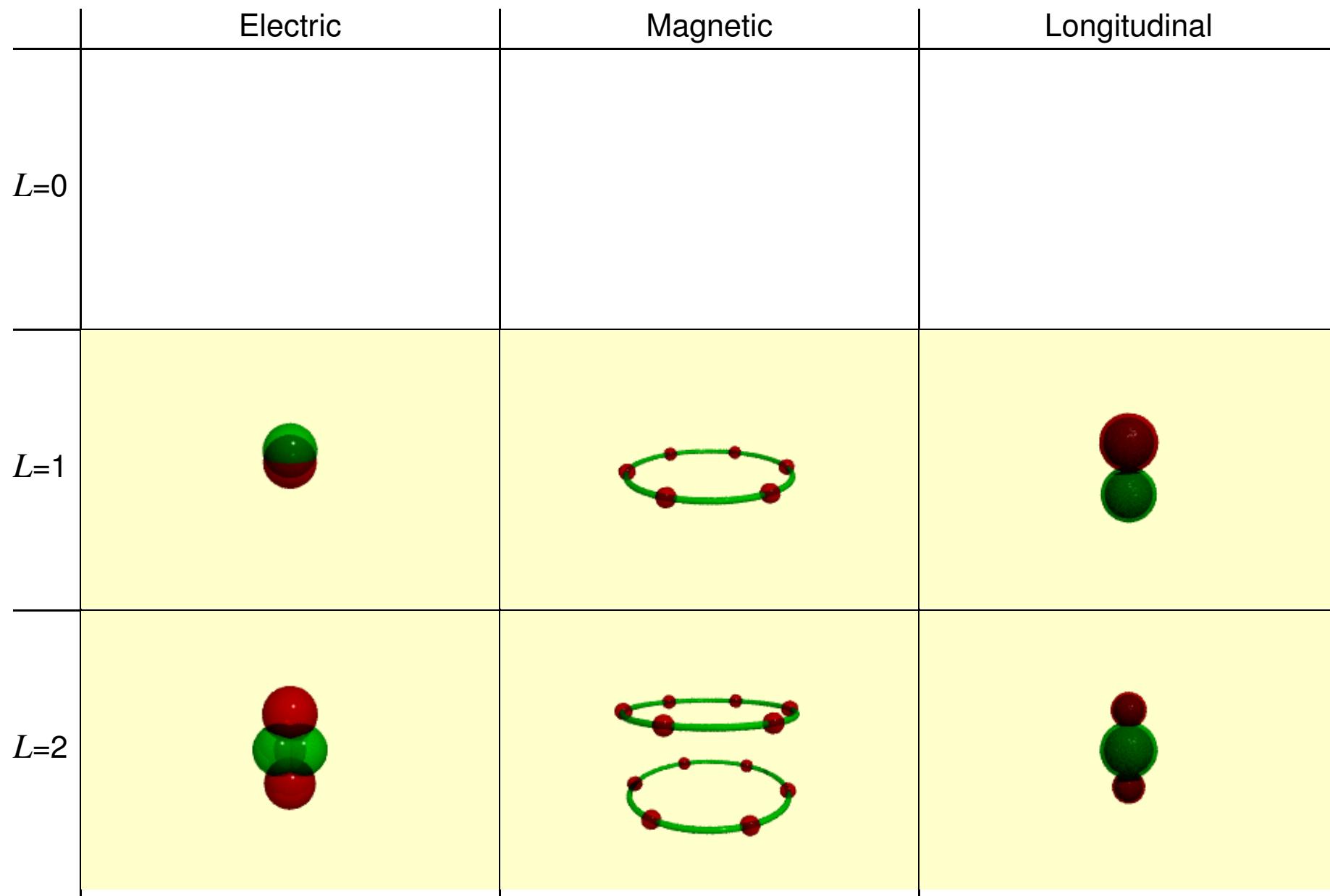
Spin Polarizabilities



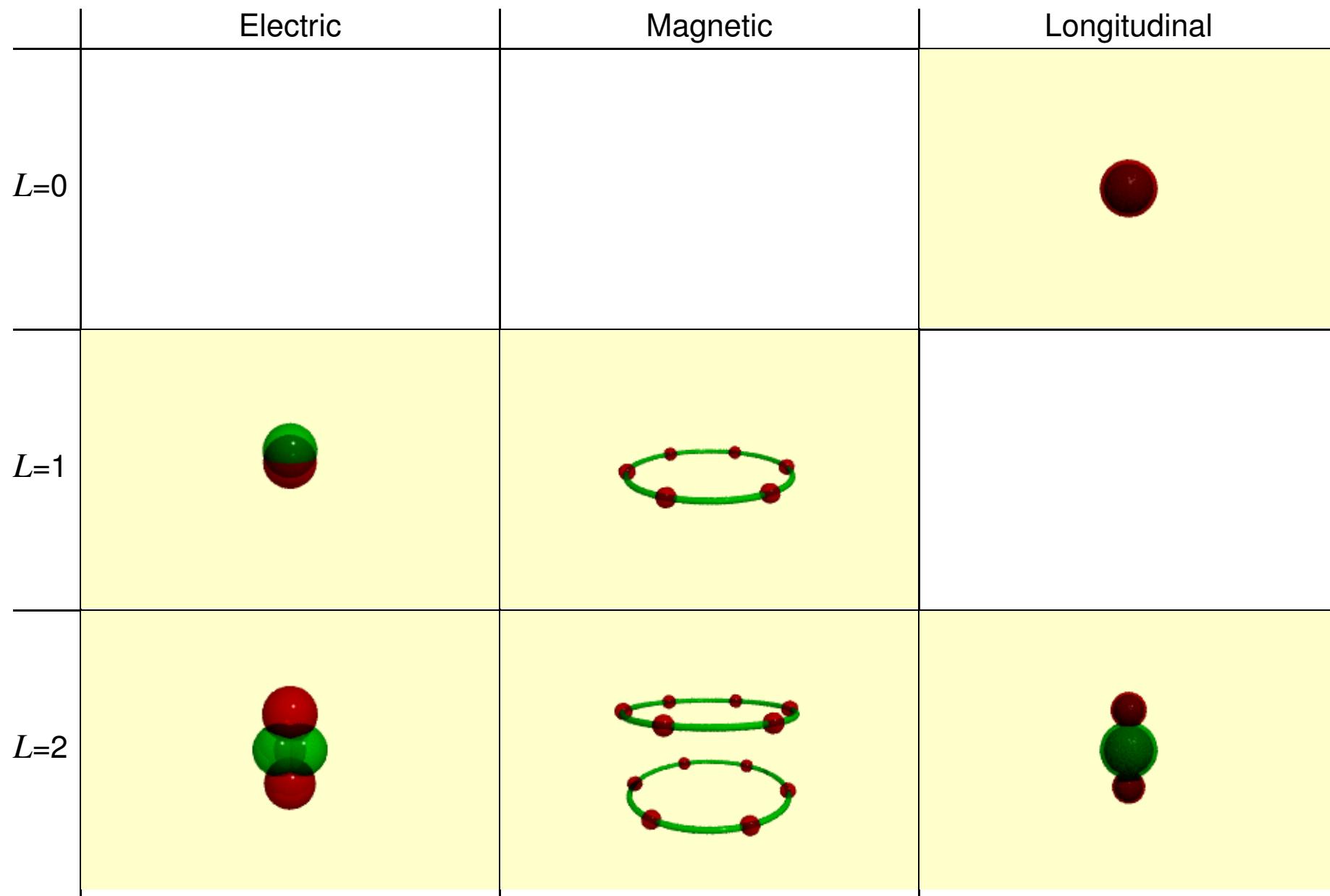
Spin Polarizabilities



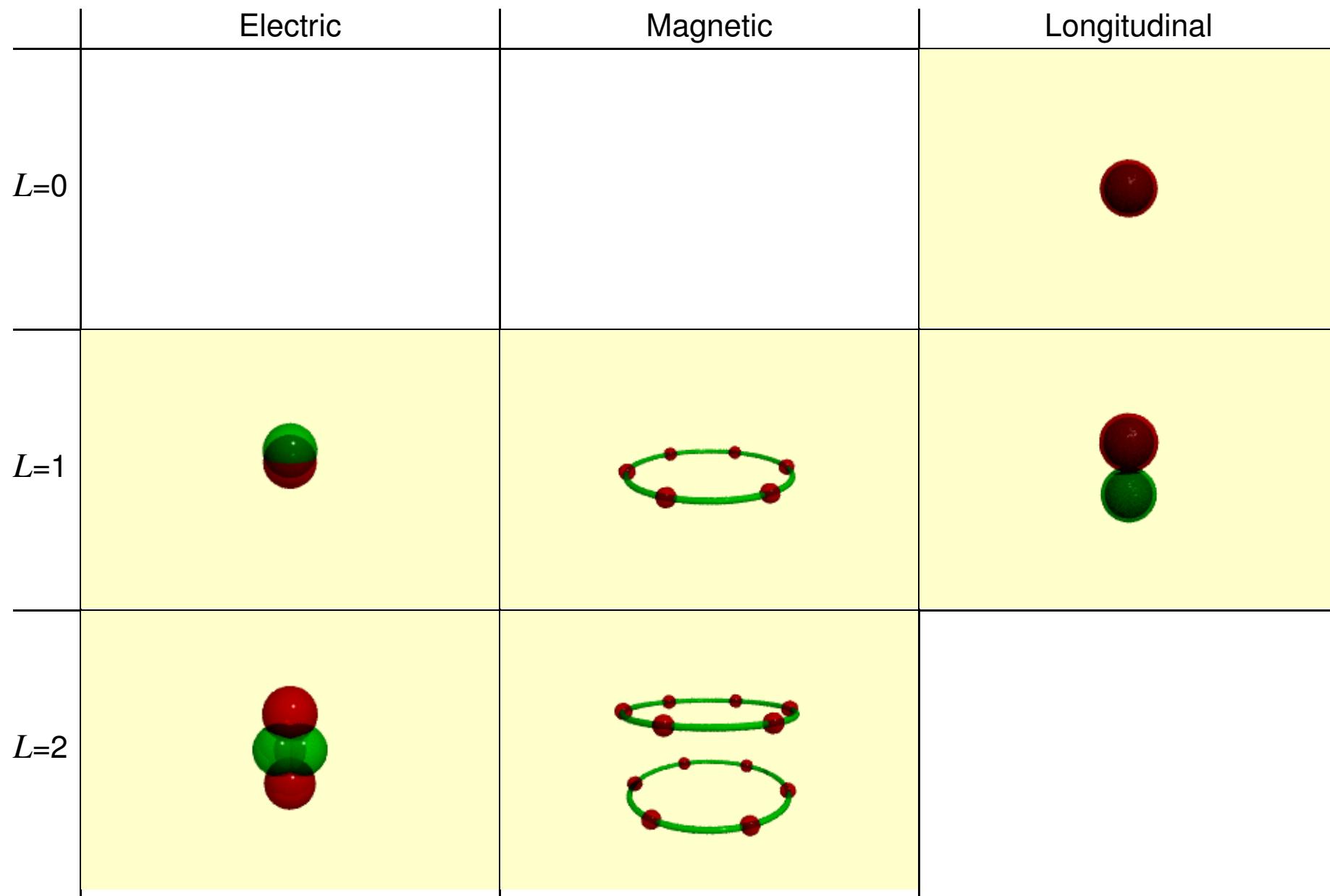
Spin Polarizabilities



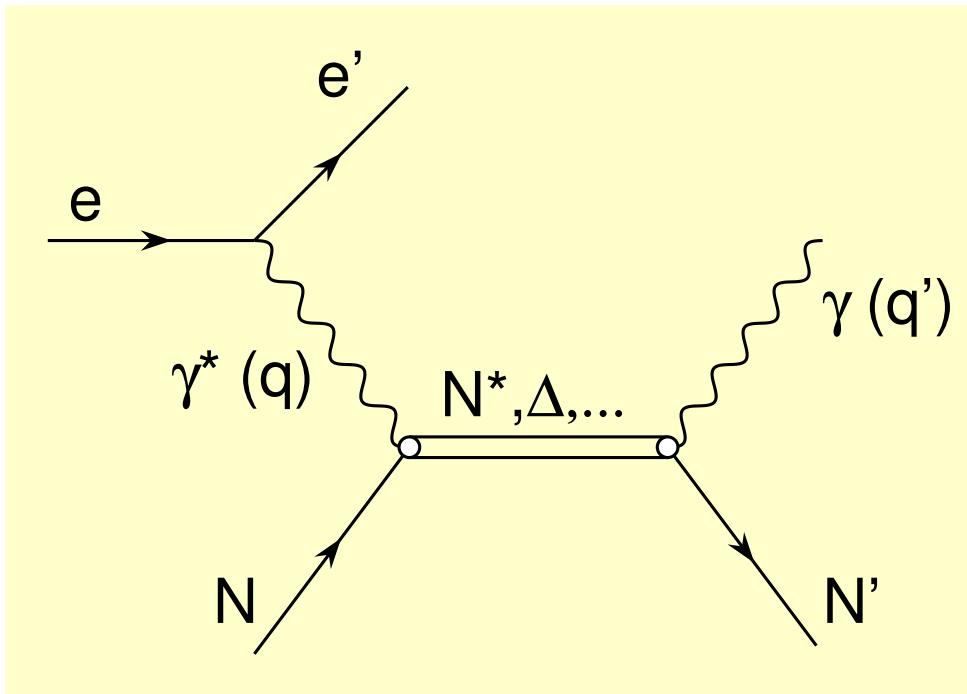
Spin Polarizabilities



Spin Polarizabilities



Virtual Compton Scattering



- Polarizabilities depend on photon virtuality Q^2
 ⇒ Generalized Polarizabilities
- Polarizabilities are defined in static limit $q' \rightarrow 0$
- Interpretation of GP(Q^2):
 ⇒ “Form Factor” measurement in external field
 ⇒ Fouriertransform of local distribution of polarizabilities

Hadron Physics Conclusions

- An invaluable tool for a deep understanding of strong interaction and QCD
- Exciting experimental Results
 - ▶ New discoveries $\approx 1/\text{year}$
 - ▶ XYZ and clear signatures of Exotic States
- Continuing Progress in Theory
 - ▶ Lattice QCD
 - ▶ Modelling of exotic states
- Running and new Facilities for Spectroscopy
 - ▶ LHC, e^+e^- Colliders
 - ▶ JLab 12
 - ▶ PANDA at FAIR
- Connection to Astrophysics
 - ▶ Neutron Stars as dense hadronic matter
- Precision Physics
 - ▶ Determination of Wave Functions
 - ▶ Polarizabilities
- And still a lot to do ...