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# The electron screening effect with a magnetic field on the massive stars

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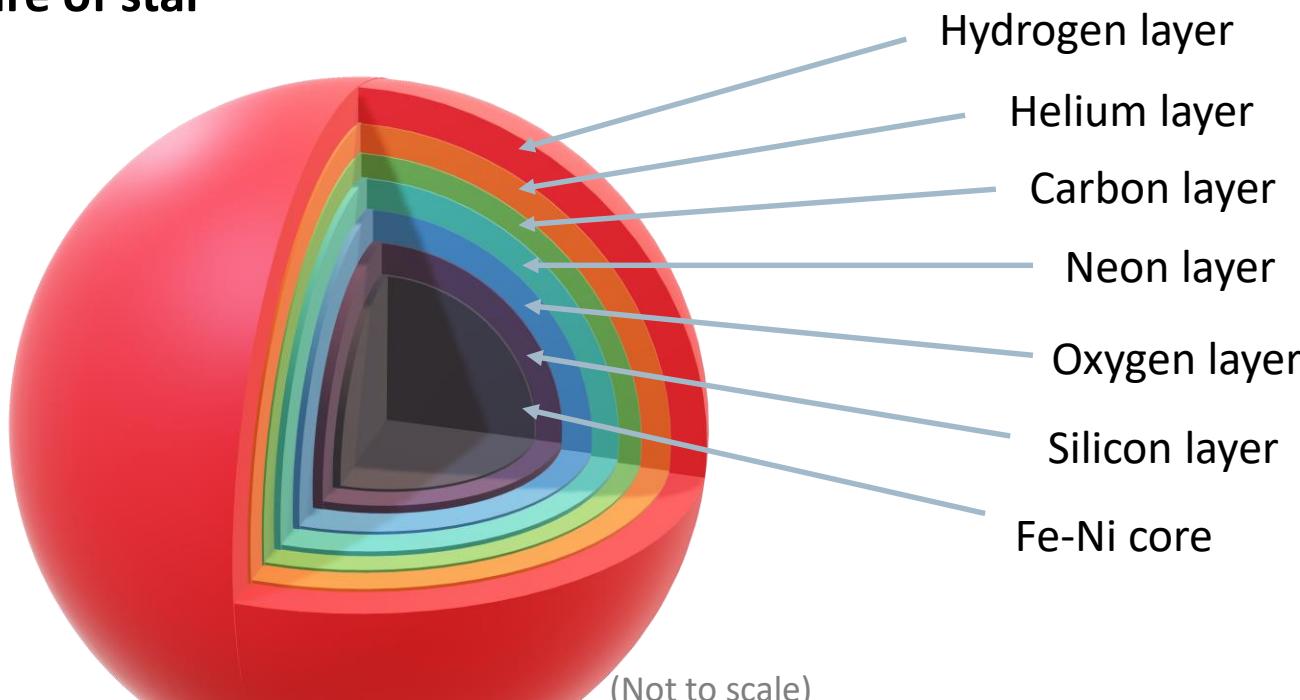
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# Introduction

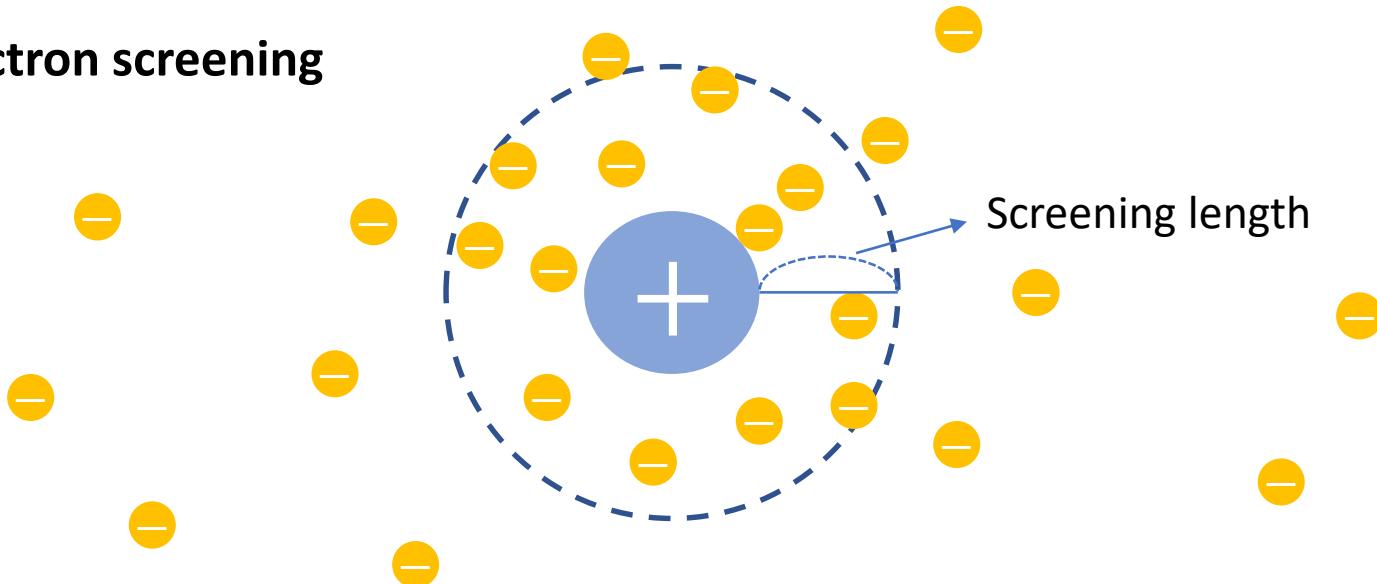
- **Structure of star**



- Stars generate the energy through the thermonuclear reactions
- Stellar evolution occurs through various burning stage depending on their total mass.

# Introduction

- **Electron screening**



- In the environment of ionized stellar plasma, nuclei are surrounded by electron cloud.
- The Coulomb barrier of screened nuclei is decreased.
- The electron screening effect gives a correction to the network calculation.

# Formalism : Classical screening

- Thermonuclear reaction rate

$$\langle \sigma v \rangle \propto \int_0^\infty S(E) P(E) e^{-E/T} dE$$

$S(E)$ : The astrophysical S-factor

$Z_t$ : atomic number of target nucleus

$Z_p$ : atomic number of projectile nucleus

$$P(E) = \exp\left(-\frac{2}{\hbar}\sqrt{2m} \int_{R_0}^{R_c} \sqrt{\frac{Z_t Z_p e^2}{r} - E} dr\right) \equiv e^{-2\pi\eta}$$

- Classical screening

$Z_i$ : atomic number of projectile i nucleus

$n_{z_i}$ : number density of  $z_i$  nuclear

$$\nabla^2 \phi = -4\pi Z_t e^2 \delta(\vec{r}^3) - 4\pi \sum_{z_i \geq -1} z_i e n_{z_i} \exp\left[\frac{z_i e \phi}{T}\right]$$

$$\phi_{screen}(r) = \frac{Z_t e}{r} \exp\left(-\frac{r}{\lambda_D}\right)$$

$$\lambda_D = \sqrt{\frac{T}{4\pi e^2 \rho N_A \zeta^2}}$$

$$\zeta \equiv \left( \sum_i \frac{(z_i^2 + Z_i) X_i}{A_i} \right)^{1/2}$$

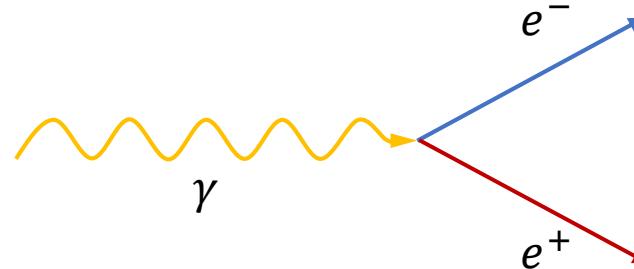
$N_A$ : Avogadro number

$X_i$ : mass fraction of nucleus i

# Formalism : Relativistic screening

- Electron-positron plasma

$$T \gtrsim m_e \approx 0.5 \text{ MeV}$$



- Net electron number density

$$n_e \equiv n_{e^-} - n_{e^+} = 2 \int \frac{d^3 p}{(2\pi)^3} \left[ \frac{1}{\exp \left[ \frac{\sqrt{p^2 + m_e^2} - \mu}{T} \right] + 1} - \frac{1}{\exp \left[ \frac{\sqrt{p^2 + m_e^2} + \mu}{T} \right] + 1} \right]$$

- Screening length

$n_e$ : electron mass  
 $\mu$ : chemical potential

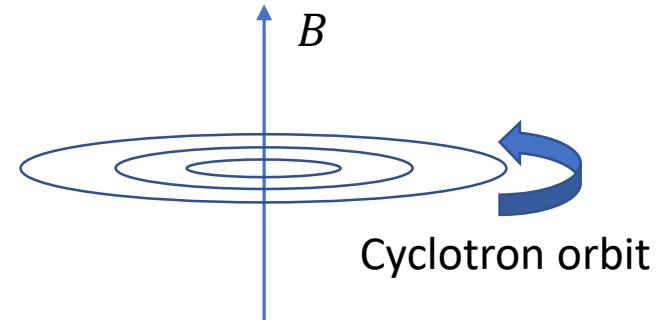
$$\frac{1}{\lambda_{TF}^2} = 4\pi e^2 \frac{\partial n_e}{\partial \mu}^{[1]} \quad \longrightarrow \quad \lambda_{TF} = \left[ \frac{e^2}{\pi^2} \frac{\partial}{\partial \mu} \int_0^\infty dp p^2 f_{FD}(p, \mu, T) \right]^{-1/2}$$

[1] M.A. Famiano et al., Phys. Rev. C 93, 045804(2006)

# Formalism : Magnetic field effect

- **Landau quantization**

$$\sqrt{eB_c} \gtrsim m_e \longrightarrow B_c \approx 4.4 \times 10^{13} \text{ G} \quad [1,2]$$



$$E^2 = \vec{p}^2 + m_e^2 \longrightarrow E^2 = p_{\parallel}^2 + eB(2n + s + 1) + m_e^2$$

n : Landau level

s = ±1 (the electron spin is along or opposed to the B-field respectively)

- **Electron number density**

$$n_e = \frac{1}{\pi^2} \int_0^\infty dp p^2 f_{FD}(p, \mu, T) \longrightarrow n_e = \sum_{n=0}^{\infty} (2 - \delta_{n0}) \int_{-\infty}^{\infty} \frac{dp_{\parallel}}{2\pi} \frac{eB}{2\pi} f_{FD}(E_B, \mu, T) \quad [2]$$

[1] Masahiro Kawasaki and Motohiko Kusakabe. Phys. Rev. D, 86(6):063003, Sep 2012.

[2] D. Grasso and H. R. Rubinstei. Phys. Rep., 348(3):163–266, Jul 2001.

# Formalism : Enhancement factor

- Screening enhancement factor

$$\phi_{screen}(r) = \frac{Z_t e}{r} \exp\left(-\frac{r}{\lambda_{TF}}\right) \quad \frac{1}{\lambda_{TF}^2} = 4\pi e^2 \frac{\partial n_e}{\partial \mu}$$

$$P_{screen} = \exp\left(-2\sqrt{2m} \int_{R_0}^{R_c} \sqrt{\frac{Z_t z_p e^2}{r} e^{-r/\lambda_{TF}} - E} dr\right) = e^{x\pi\eta - 2\pi\eta}$$
$$e^{x\pi\eta} \approx e^{(x\pi\eta)_{E_0}} = e^{\frac{Z_t z_p e^2}{\lambda_{TF} T}} \equiv f_s \quad E_0: \text{Gamow energy}$$

- Thermonuclear reaction rate with screening effect

$$\langle\sigma v\rangle_{screen} = \left(\frac{8}{\pi\mu_{pt}}\right)^{1/2} \frac{N_A}{T^{3/2}} \int_0^\infty S(E) f_s e^{-2\pi\eta} e^{-E/T} dE$$
$$= f_s \langle\sigma v\rangle_{unscreen}$$


$\mu_{pt}$ : reduced mass

# Result

- **Baryon number density**

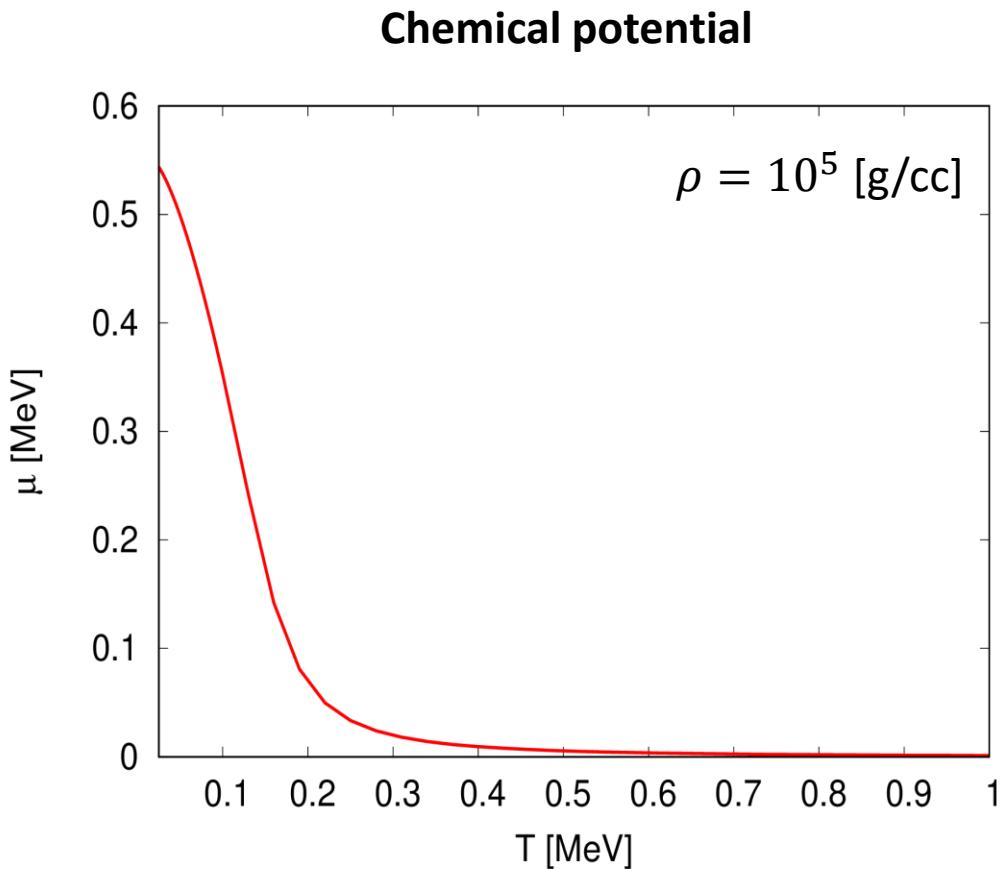
$$n_b = \rho N_A \sum Y_i$$

- **Net electron number density**

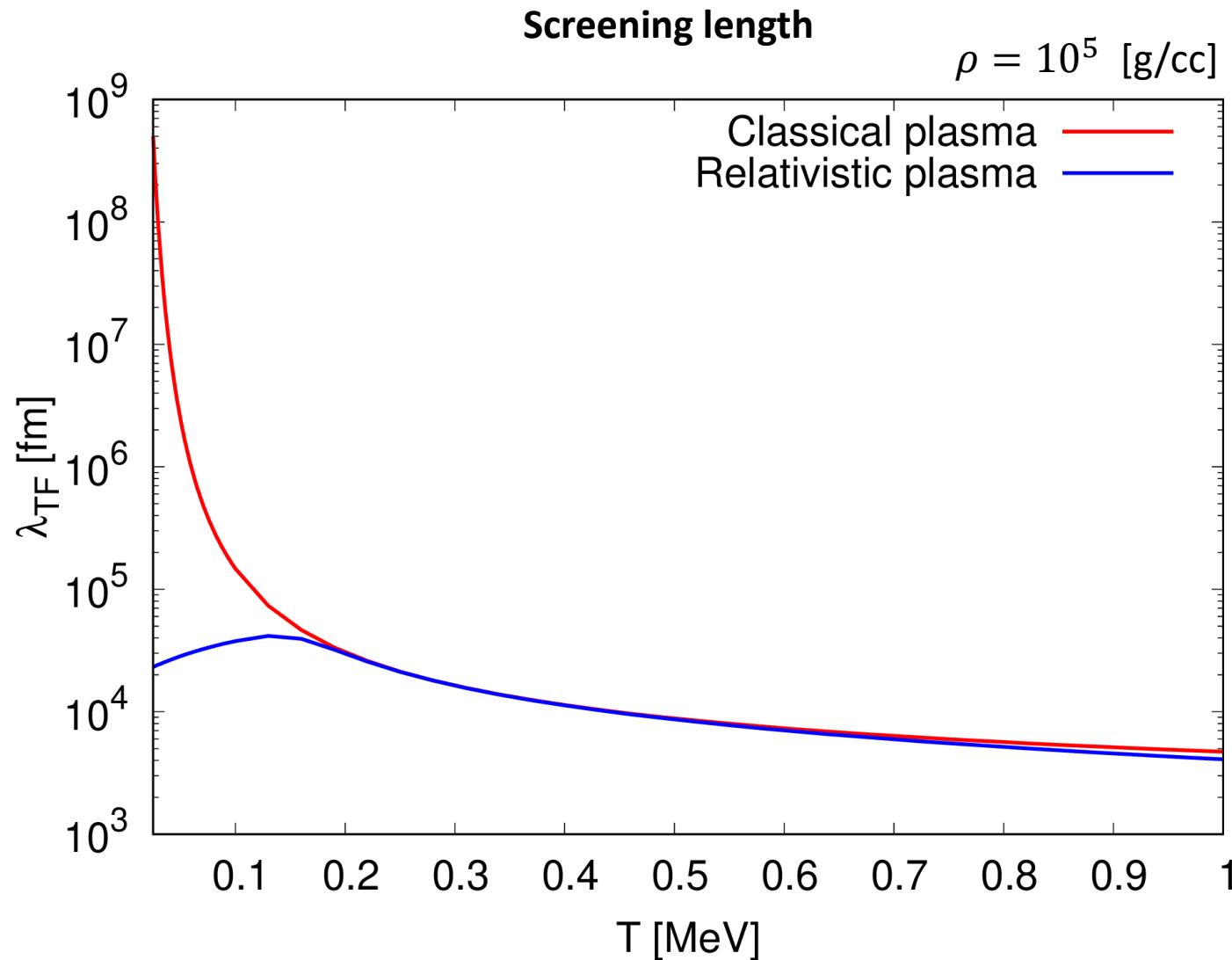
$$n_e = \sum_{n=0}^{\infty} (2 - \delta_{n0}) \int_{-\infty}^{\infty} \frac{dp_{\parallel}}{2\pi} \frac{eB}{2\pi} f_{FD}(E_B, \mu, T)$$

- **Charge neutrality**

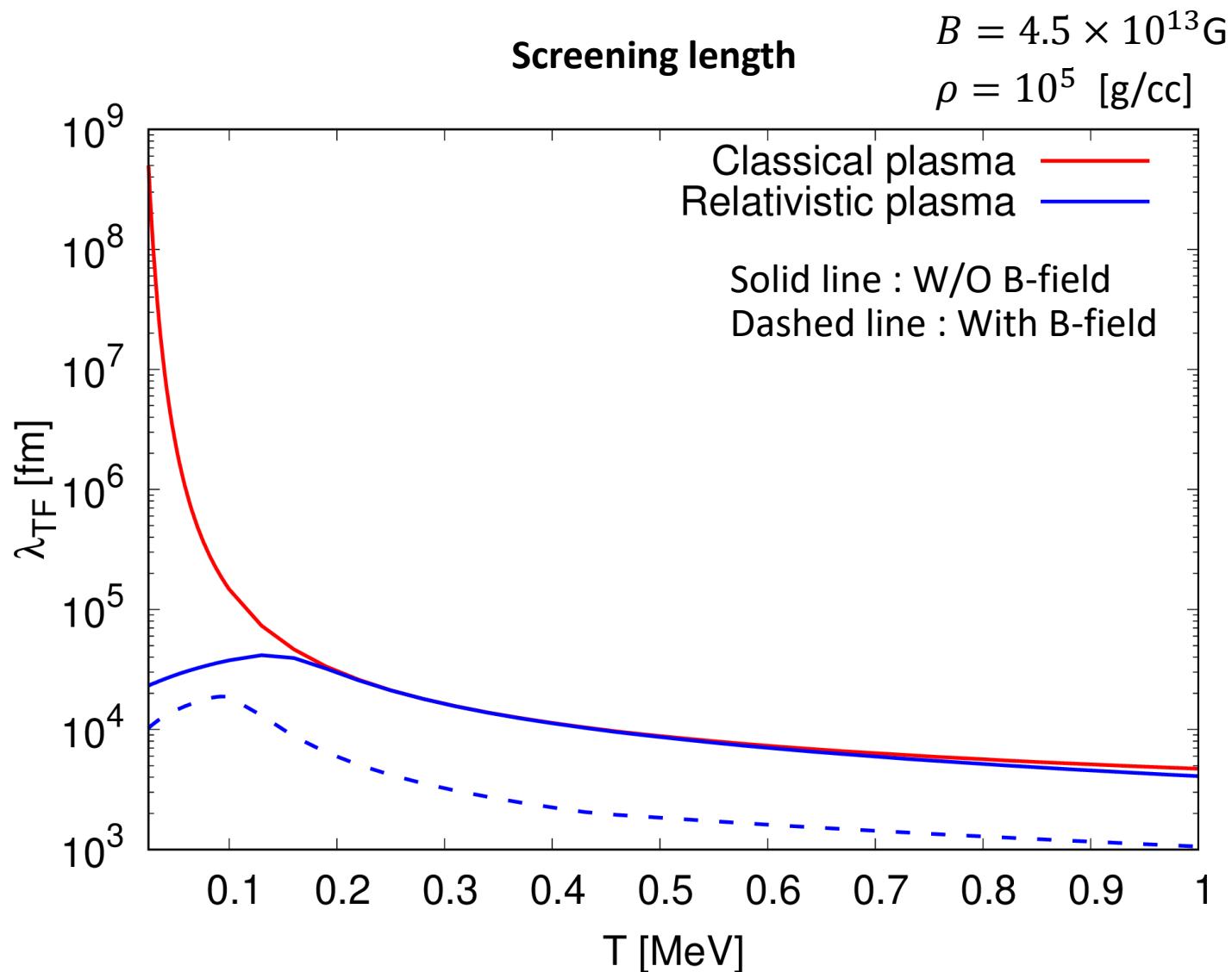
$$\rho N_A \sum Y_i = \sum_{n=0}^{\infty} (2 - \delta_{n0}) \int_{-\infty}^{\infty} \frac{dp_{\parallel}}{2\pi} \frac{eB}{2\pi} f_{FD}(E_B, \mu, T)$$



# Result

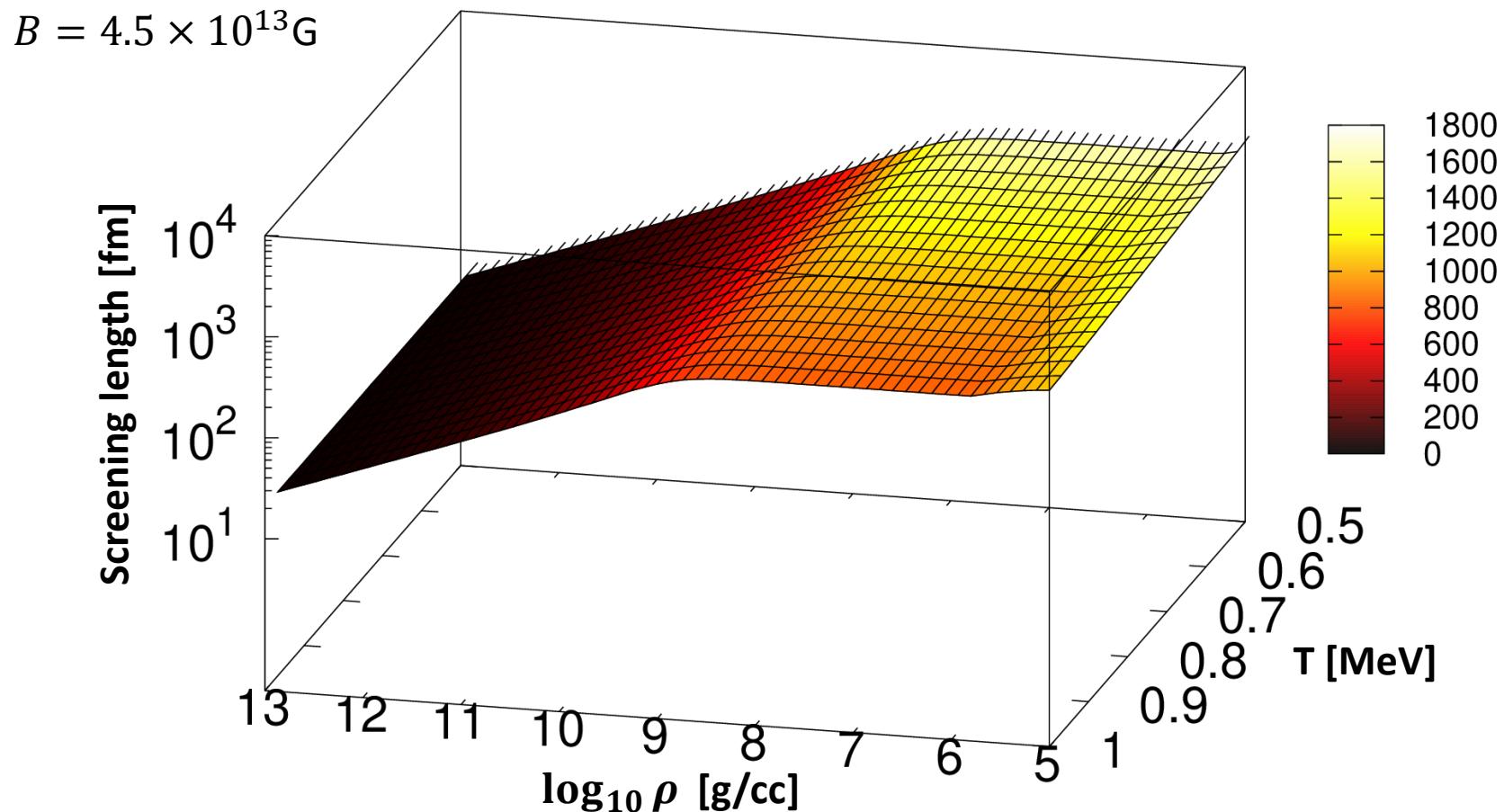


# Result



# Result

## Screening length

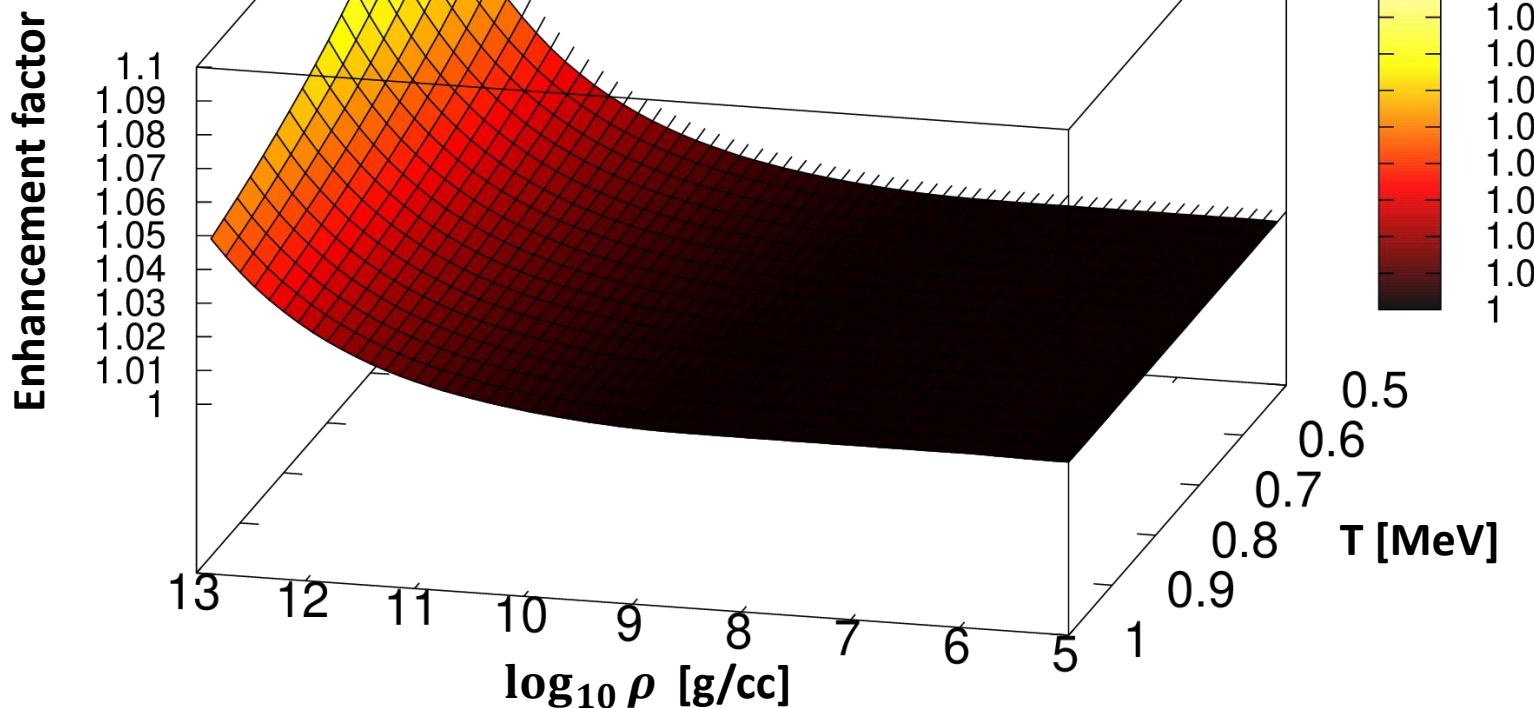


# Result

Screening enhancement factor

$$f_s = e^{\frac{Z_1 Z_2 e^2}{T \lambda_{TF}}}$$

$$B = 4.5 \times 10^{13} \text{ G}$$



# Summary

- We try to modify the reaction rate using the electron screening effect.
- Considering only the effects of pair creation, there is little screening effect occurs in the electron positron plasma.
- Including magnetic field effect, the screening effect is increased.
- As a future work, we will investigate the specific stellar environment where screening effects, including magnetic field effect, may occur.

*Thank you for your attention!*