

^{15}C STRUCTURE AND DYNAMICS: COUPLING HALO EFT TO REACTION MODELS FOR TRANSFER, BREAKUP AND RADIATIVE-CAPTURE

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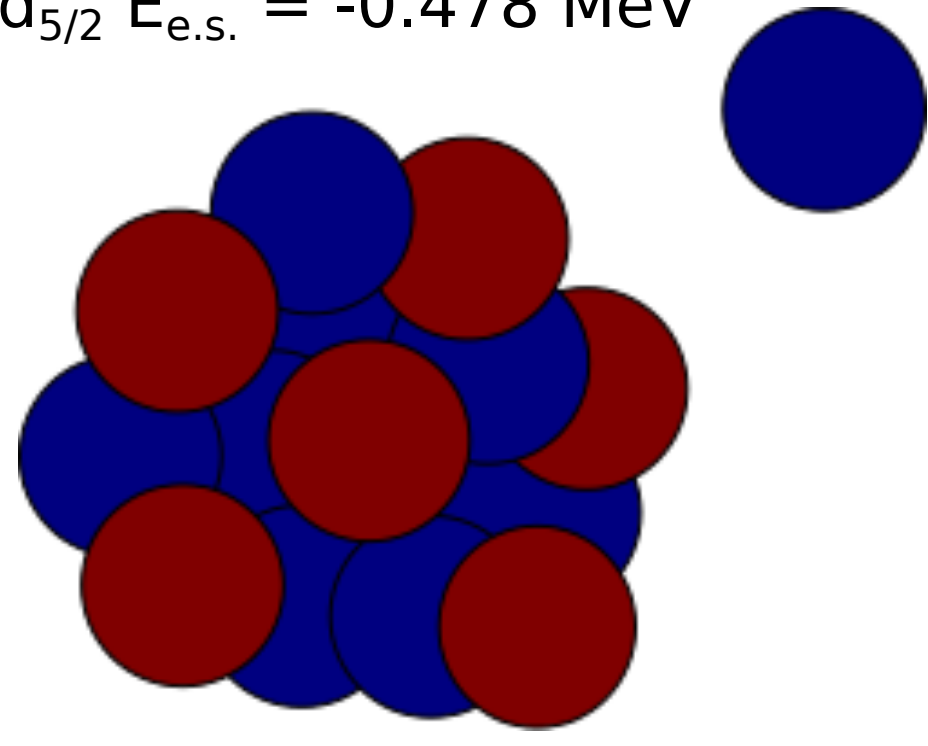
DESCRIPTION OF ^{15}C STRUCTURE WITHIN HALO EFT

$^{15}\text{C} = ^{14}\text{C}(0^+) + n$

^{15}C is a one-neutron halo nucleus modeled as a compact ^{14}C core with one loosely bound neutron

> $1s_{1/2}$ $E_{g.s.} = -1.218$ MeV

> $0d_{5/2}$ $E_{e.s.} = -0.478$ MeV



Effective 1-body Hamiltonian

$$H_0 = -\frac{\hbar^2}{2\mu_{^{14}\text{C}n}}\Delta + V_{^{14}\text{C}n}(\mathbf{r})$$

V_{cn} effective potential simulating core-neutron interaction

Eigenvalue problem

$$H_0\varphi_{n'l_j}(E, \mathbf{r}) = E\varphi_{n'l_j}(E, \mathbf{r})$$

Bound states wavefunctions radial behaviour

$$u_{n'l_j}(r) \xrightarrow{r \rightarrow \infty} C_{n'l_j} e^{-k_{n'l_j}r}$$

$C_{n'l_j}$ is the ANC, associated to the WF tail strength

V_{cn} IN HALO EFT

Hammer, Ji, Phillips JPG 44, 103002 (2017)

$$\text{@NLO } V_{^{14}\text{C}n}(r) = V_0 e^{-\frac{r}{2r_0}} + V_2 r^2 e^{-\frac{r}{2r_0}}$$

V_2 and V_0 adjusted to fit

> in s wave:

binding energy (known experimentally)

ANCs (extracted from peripheral transfer reaction, see below)

> in p wave: δ_p (assumed nil)

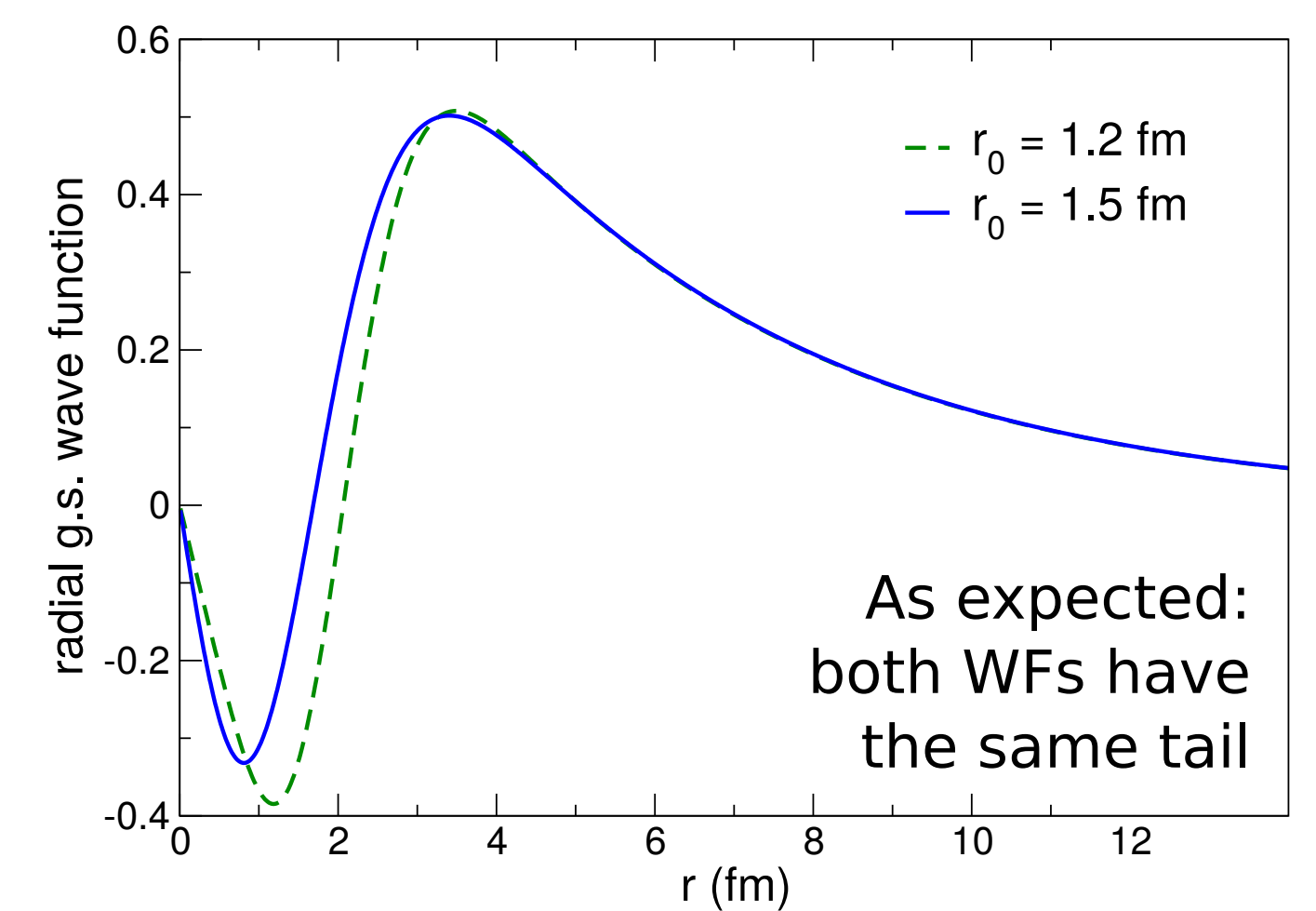
$V_{cn} = 0$ for $l > 1$

r_0 to evaluate sensitivity to short range physics

We consider:

> two $^{14}\text{C}+n$ potentials at NLO with $r_0 = 1.2$ and 1.5 fm

> two potentials for the excited state to see if we have to go beyond NLO



As expected: both WFs have the same tail

ANC EXTRACTION FROM TRANSFER REACTION

Yang and Capel PRC98,054602(2018)

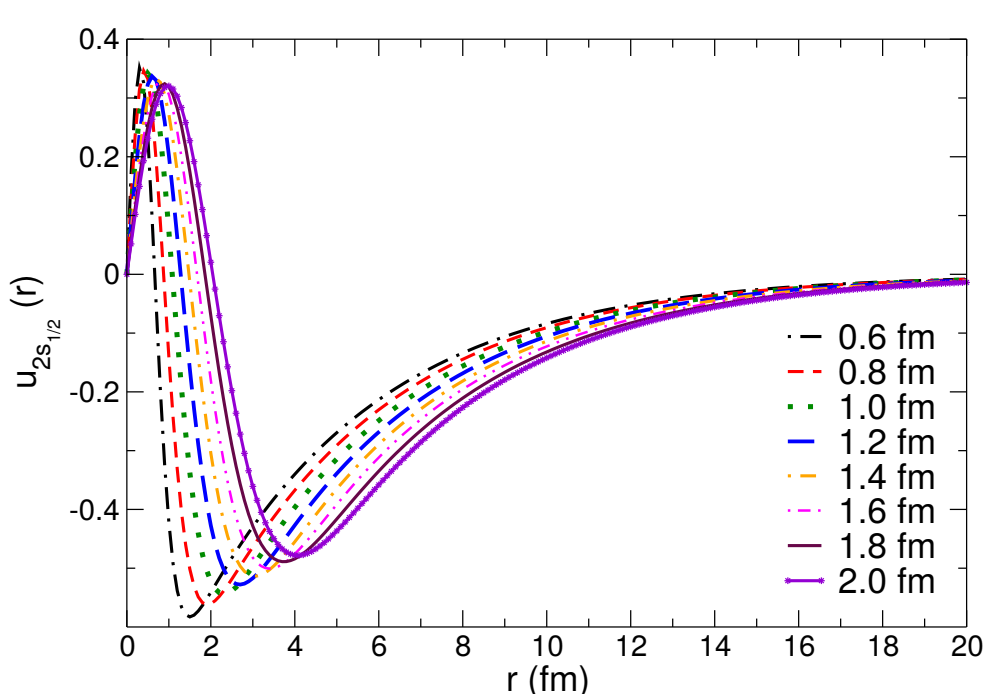
1. Determination of different potentials V_{cn} @LO

$$V_{^{14}\text{C}n}(r) = V_0 e^{-\frac{r}{2r_0}}$$

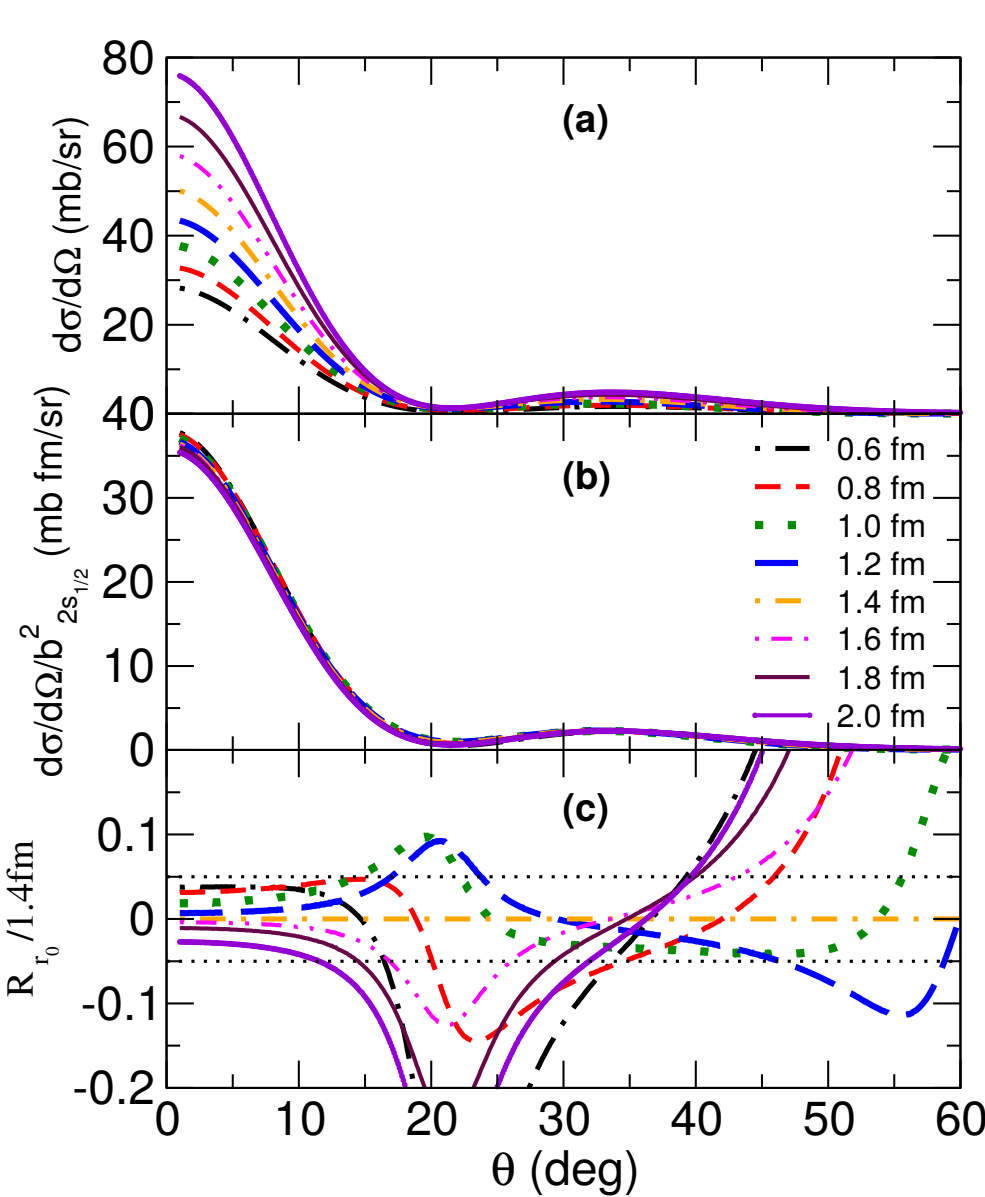
with different $r_0 \Rightarrow V_0$ adjusted neutron binding energy

2. Generation of different wave functions $\varphi_{n'l_j}$

with different ANCs



3. Computation of corresponding $d\sigma_{th}/d\Omega$ for the transfer to ^{15}C g.s. at $E_d = 17$ MeV

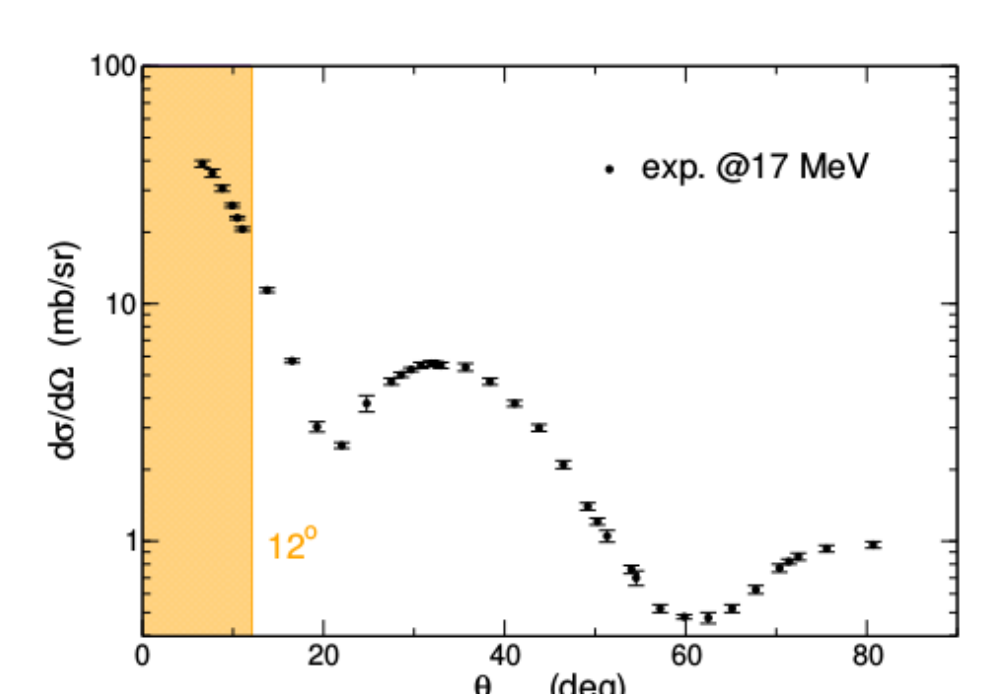


(a) FR-ADWA calculation Johnson and Tandy NPA235, 56 (1974)

(b) spread reduced at forward angle scaling by ANC^2

(c) $\frac{R_{r_0/1.4\text{fm}}(\theta)}{\left(\frac{\text{ANC}(1.4\text{fm})}{\text{ANC}(r_0)}\right)^2 \frac{d\sigma_{th}^{(r_0)}/d\Omega}{d\sigma_{th}^{(1.4\text{fm})}/d\Omega}} - 1$ reaction assumed peripheral if spread lower than 5% $\Rightarrow \theta < 12^\circ$

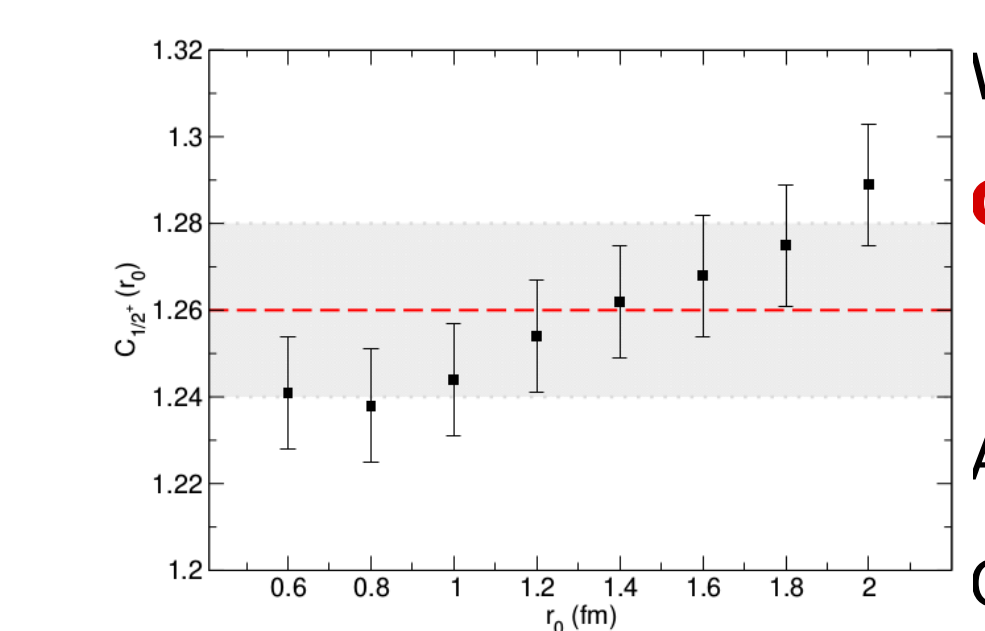
4. Comparison with the experimental cross section



Experiment: Mukhamedzhanov et al. PRC84, 024616 (2011)

We infer an ANC for each potential from a χ^2 analysis in the peripheral region

5. Extracted ^{15}C ANC



We obtain a final ANC for g.s.

$$C_{1/2^+} = 1.26 \pm 0.02 \text{ fm}^{-1/2}$$

Analogously for the e.s.

$$C_{5/2^+} = 0.056 \pm 0.001 \text{ fm}^{-1/2}$$

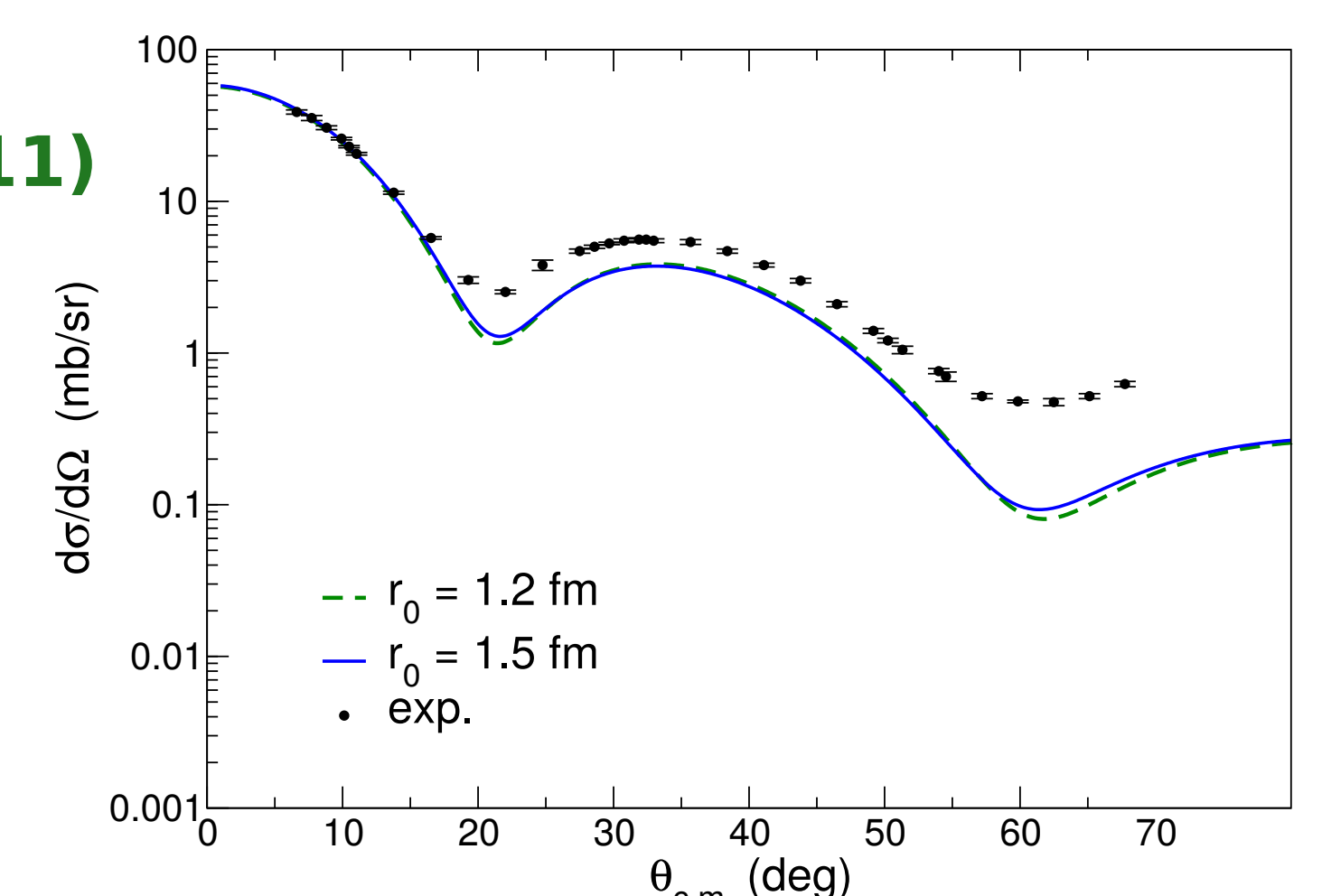
TRANSFER $^{14}\text{C}(d,p)^{15}\text{C}$

Experiment: Mukhamedzhanov et al. PRC84, 024616 (2011)

FR-ADWA calculation Johnson and Tandy NPA235, 56 (1974)

Results

- Good agreement with data for $\theta < 12^\circ$
- The reaction does not depend on WF inner part $r_0 = 1.2 \text{ fm} \sim r_0 = 1.5 \text{ fm}$ for $\theta < 12^\circ$
- For $\theta > 12^\circ$ short range physics shows up



COULOMB BREAKUP OF ^{15}C ON Pb

Experiments: > GSI E_{LAB} = 605 AMeV Datta Pramanik et al., PLB551 (2003) 63 > RIKEN E_{LAB} = 68 AMeV Nakamura et al., PRC79 (2009) 035805

The relativistic Eikonal model

Klein-Gordon equation in the T-P CM frame $[(\hbar c)^2 \nabla^2 + (\hbar c k)^2 - 2E V_{PT}] \Psi = 0$ Satchler, Nucl. Phys. A 540 (1992) 533

Adiabatic and eikonal approximations neglecting core excitations, to obtain the eikonal expression

$$\hat{\Psi}(\mathbf{b}, z, r) = e^{i\chi(\mathbf{b}, s)} \Phi_{l_0 j_0 m_0}(E_0, \mathbf{r}) \text{ where } \chi(\mathbf{b}, s) = \chi^N(\mathbf{b}, s) + \chi^C(\mathbf{b}, s) + \chi_{PT}^C(\mathbf{b}, s)$$

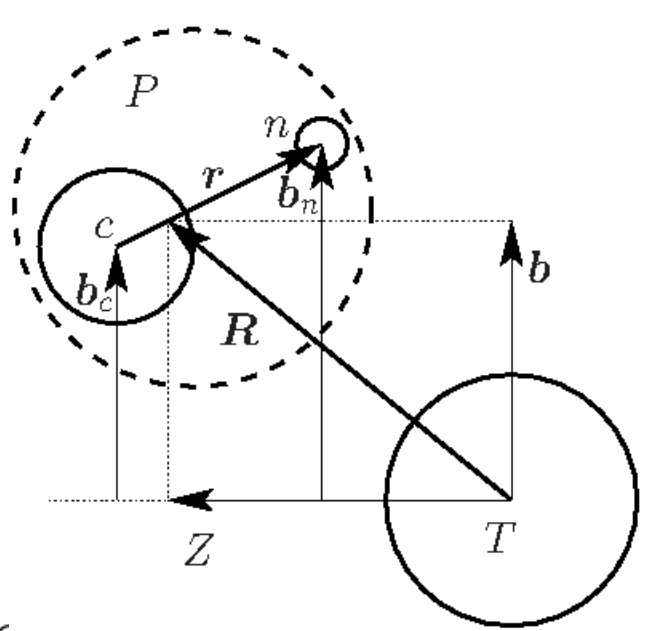
Nuclear phase: optical limit approximation Horiuchi, Suzuki, Capel and Baye, PRC 81 (2010)

Coulomb phase: correction to avoid divergence Margueron, Bonaccorso and Brink, Nucl. Phys. A720 (2003)

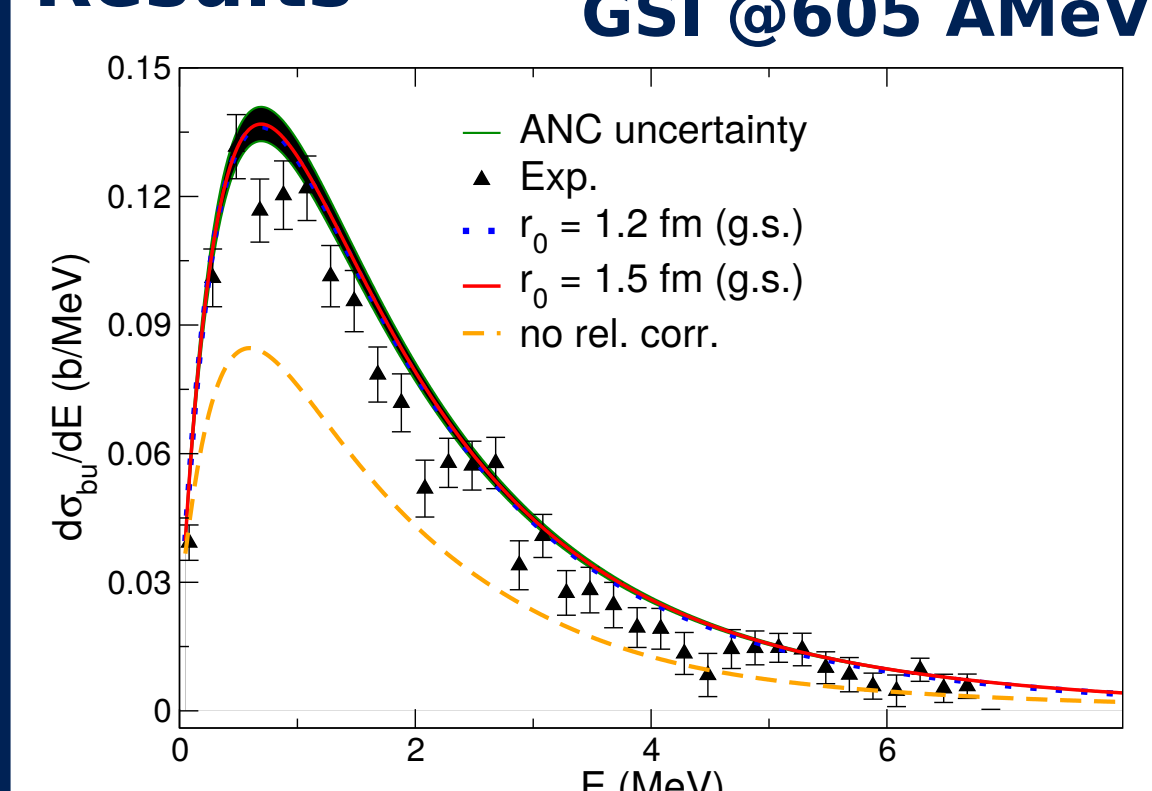
Lorentz boost $\mathbf{V}_{PT}(\mathbf{b}, z, r) \rightarrow \gamma \mathbf{V}_{PT}(\mathbf{b}, \mathbf{y}, r)$ to express breakup cross section in P rest frame

Winther and Alder, Nucl. Phys. A 319 (1979)

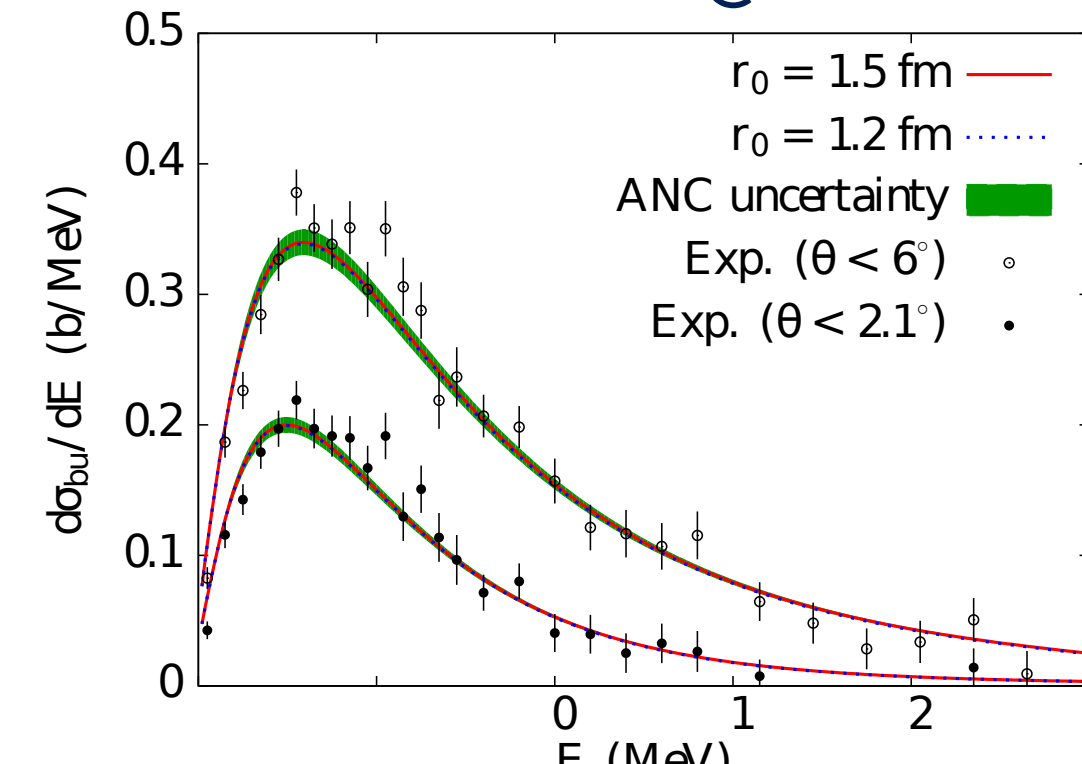
$$\frac{d\sigma_{bu}}{dE} = \frac{4\mu_{cf}}{\hbar^2 K} \frac{1}{2j_0 + 1} \sum_{m_0} \sum_{l_{jm}} \int_0^\infty b db |S_{kljm}^m(b)|^2 \text{ where } S_{kljm}^m(b) \sim \langle \varphi_{l_{jm}}(E) | e^{i\chi^N} (e^{i\chi^C} - i\chi^C + i\chi^{FO}) e^{i\chi_{PT}^C} | \varphi_{l_0 j_0 m_0}(E_0) \rangle$$



Results



RIKEN @68 AMeV



- Relativity is important in the high energy case
- Excellent agreement with data
- Band shows ANC uncertainty
- The reaction does not depend on WF inner part $r_0 = 1.2 \text{ fm} \sim r_0 = 1.5 \text{ fm}$
- No effect for the e.s. inclusion \Rightarrow for Coulomb breakup the Halo EFT expansion works fine at NLO

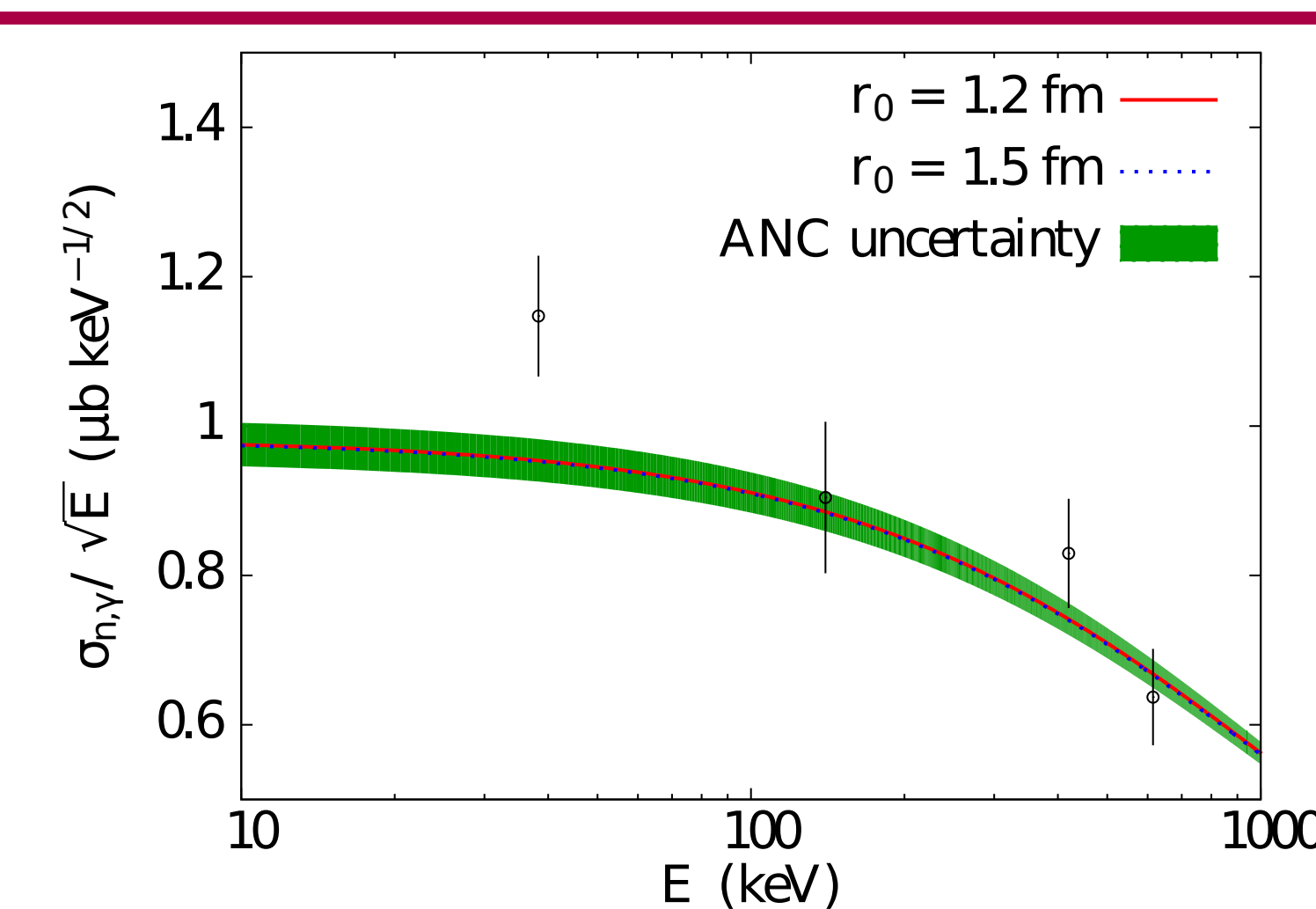
RADIATIVE CAPTURE MODEL $^{14}\text{C}(n,\gamma)^{15}\text{C}$

Experiment: Reifarth et al., PRC77 (2008) 015804

^{14}C and n merge to form ^{15}C by emitting a photon from ^{15}C continuum (E) to one of its bound states (E_{n1})

Results

- Good agreement with data for $E > 100$ keV
- Band related to ANC uncertainty
- Cross section independent on internal wave function
- Problem at low energy \Rightarrow more research on this point is needed!



CONCLUSIONS

Using one single Halo-EFT description of ^{15}C adjusted on

> binding energy \rightarrow known from experiment

> ANC \rightarrow extracted analysing transfer reaction

We reproduce data for different reactions: transfer, breakup (at intermediate and high energy) and radiative capture

In particular:

o Halo-EFT description works well @NLO

o using the r_0 parameter we can test short-range physics (important only in transfer processes at large angles)