

Development of an accurate DWIA model of coherent π^0 -photoproduction to study neutron skins in medium heavy nuclei

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The symmetry energy

- neutron-rich nuclei
 - neutron stars
- } properties strongly dependent on symmetry energy

Equation of state (EOS) of asymmetric matter

$$\mathcal{E}(\rho, \alpha) = \mathcal{E}(\rho, \alpha = 0) + S(\rho) \alpha^2 + \dots \quad \alpha = \frac{N - Z}{A}$$

where α is the neutron-proton asymmetry.

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Taylor expansion around nuclear saturation density ρ_0 ($\simeq 0.15 \text{ fm}^{-3}$):

$$S(\rho) = J + L \left(\frac{\rho - \rho_0}{3\rho_0} \right) + \frac{1}{2} K_{\text{sym}} \left(\frac{\rho - \rho_0}{3\rho_0} \right)^2 + \dots$$

We can constrain L with the neutron skin.

What is the neutron skin?

The symmetry energy

Where do the extra neutrons in n-rich systems (^{208}Pb : $N=126$, $Z=82$)?

- Symmetry energy favors to move them to the surface
- Surface tension favors spherical drop of *uniform* equilibrium density

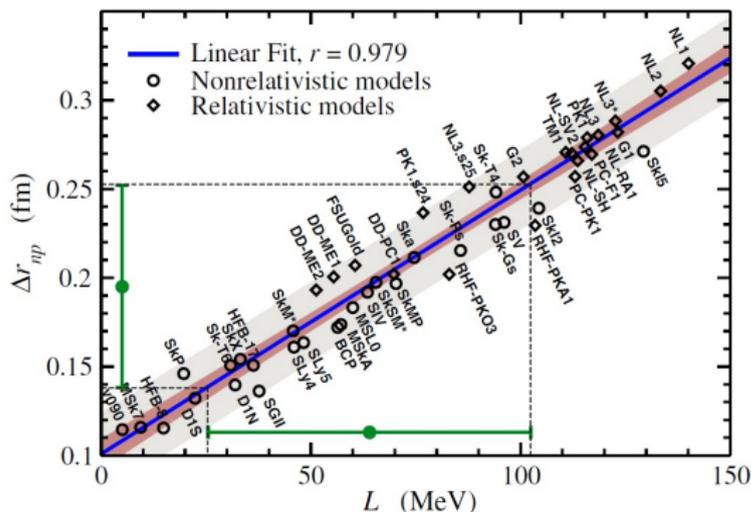
⇒ formation of a neutron skin Δr_{np} , larger as A increases

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PRL 106, (2011) 252501

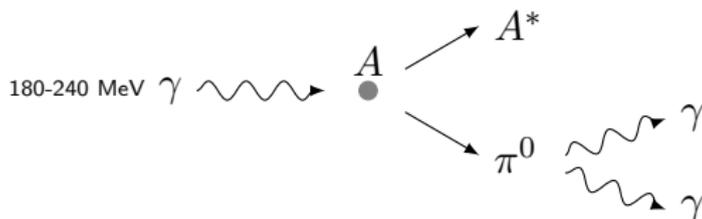
L strongly correlated to Δr_{np}
 \rightarrow need to measure accurately

How can we measure it?

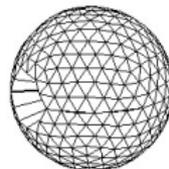
The coherent π^0 photoproduction

In Mainz, at MaMi:

π^0 -photoproduction (on $^{116,120,124}\text{Sn}$)



Crystal Ball



TAPS

Advantages:

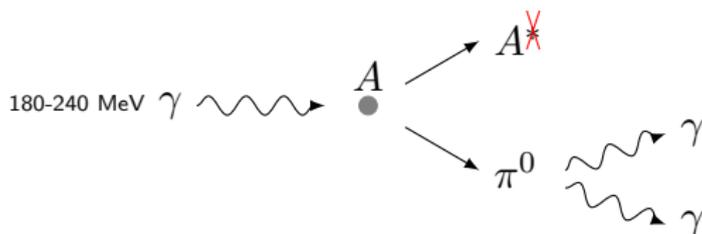
- Same amplitude for n and p
 \rightarrow Sensitivity to nucleon dist.
- Photon is neutral
 \rightarrow Whole volume is probed

Drawbacks:

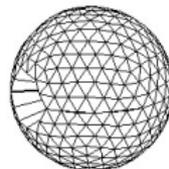
- Final state interactions
 \rightarrow Model dependence
- Delta resonance region
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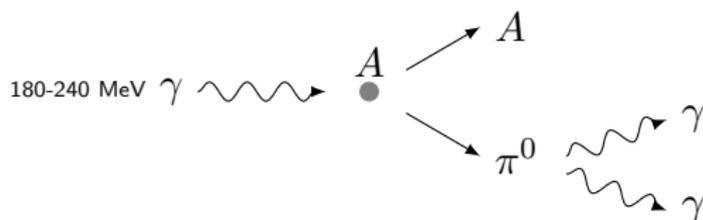
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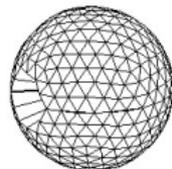
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- Final state interactions
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→ Model dependence

PRL 112, 242502 (2014): skin of 0.15 ± 0.05 fm on ^{208}Pb

- ◇ Choice of density
- ◇ Errors due to model dependencies

Plane wave impulse approximation (PWIA)

- Plane wave: no final state interactions of the pion with nucleus.
- Impulse approximation: only one nucleon interacts with the photon.

Cross section (Drechsel, Tiator, Kamalov and Yang in NPA 660, 423):

$$\frac{d\sigma_{\text{PWIA}}^{\gamma \rightarrow \pi}}{d\Omega_{\text{CM}}} \propto |f_2(\vec{k}_\pi, \vec{k}_\gamma) \rho_A(q)|^2$$

photo-production elementary amplitude (on one nucleon)

Nucleon density

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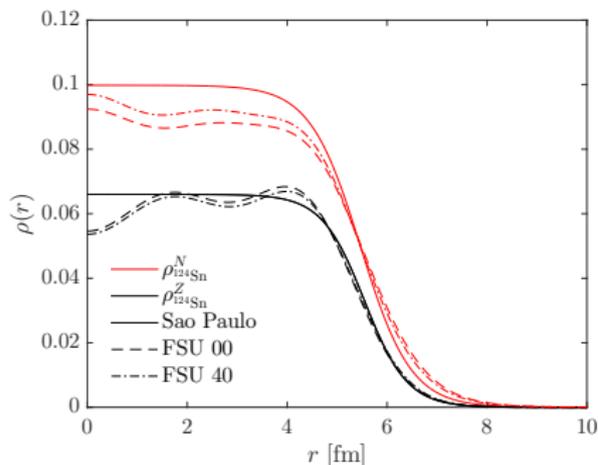
photo-production
elementary amplitude
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Nucleon density

CGLN amplitudes taken from MAID (<https://maid.kph.uni-mainz.de/maid2007/helic.html>)

Densities used for the calculations

Densities of ^{124}Sn

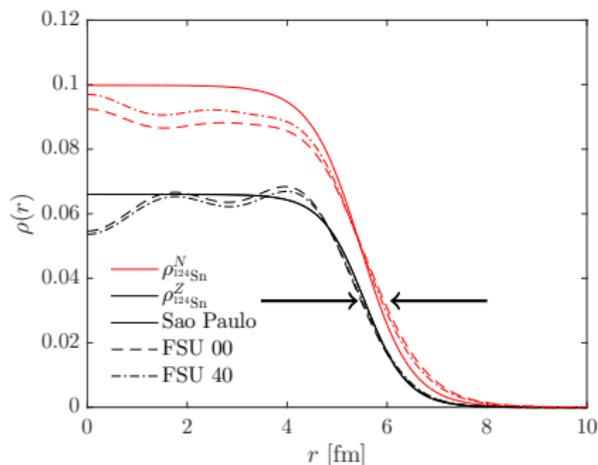


- Sao Paulo (Phenomenological)
→ Fermi-Dirac
- FSU model (courtesy of J. Piekarewicz)
→ Microscopic MF model

Can we differentiate them on a photo-production cross section?

Densities used for the calculations

Densities of ^{124}Sn



\neq skins

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$$\Delta r_{np} = 0.05 \text{ fm}$$

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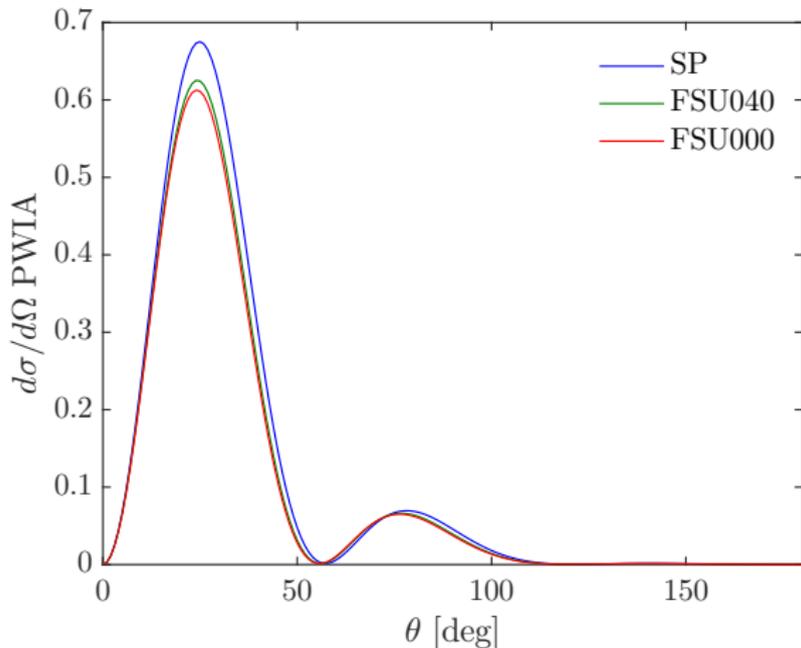
$$\Delta r_{np}^{\text{FSU00}} = 0.28 \text{ fm}$$

$$\Delta r_{np}^{\text{FSU40}} = 0.19 \text{ fm}$$

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Photo-production cross section in PWIA

For these densities, photo-production in PWIA (^{124}Sn , 180-190 MeV):



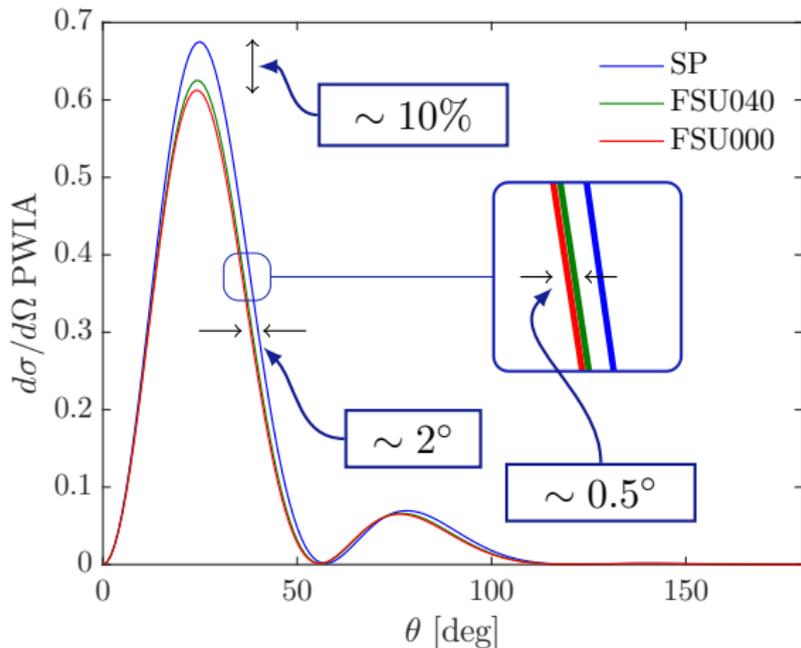
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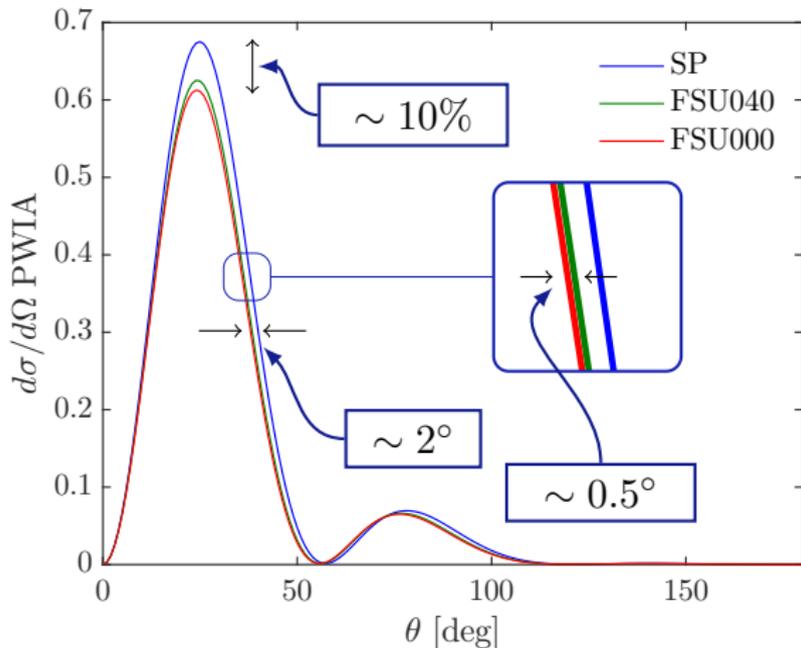
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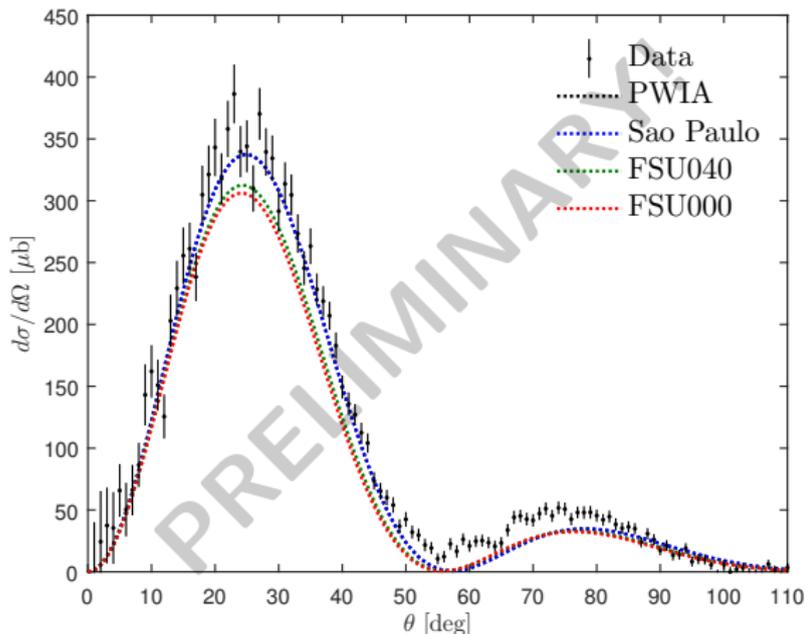
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How does that compare with experimental data?

Comparison with experiment at $T_\gamma = 180\text{-}190$ MeV



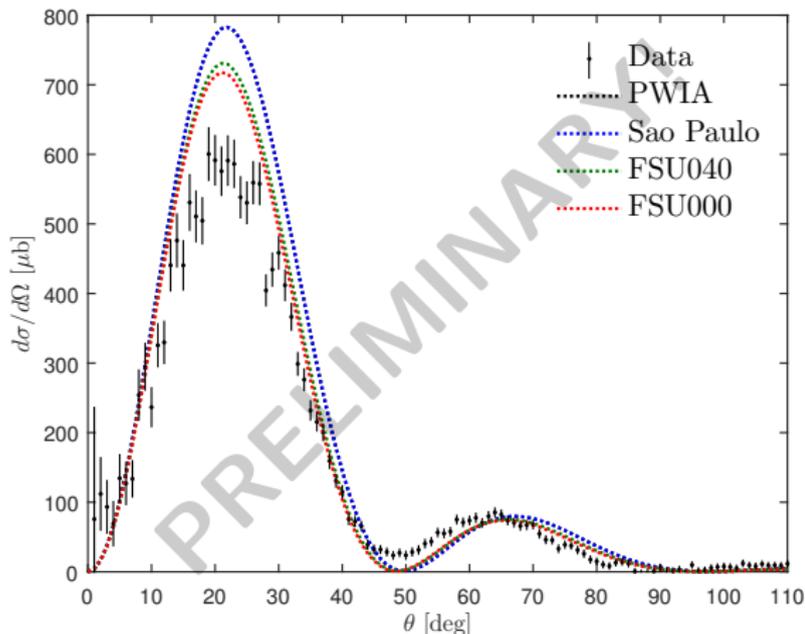
θ precision $\sim 1^\circ$

Fair agreement

Shift of second peak

Data courtesy of M. Ferretti (PRELIMINARY)

Comparison with experiment at $T_\gamma = 200-210$ MeV



θ precision $\sim 1^\circ$

Less good agreement

Shift of second peak

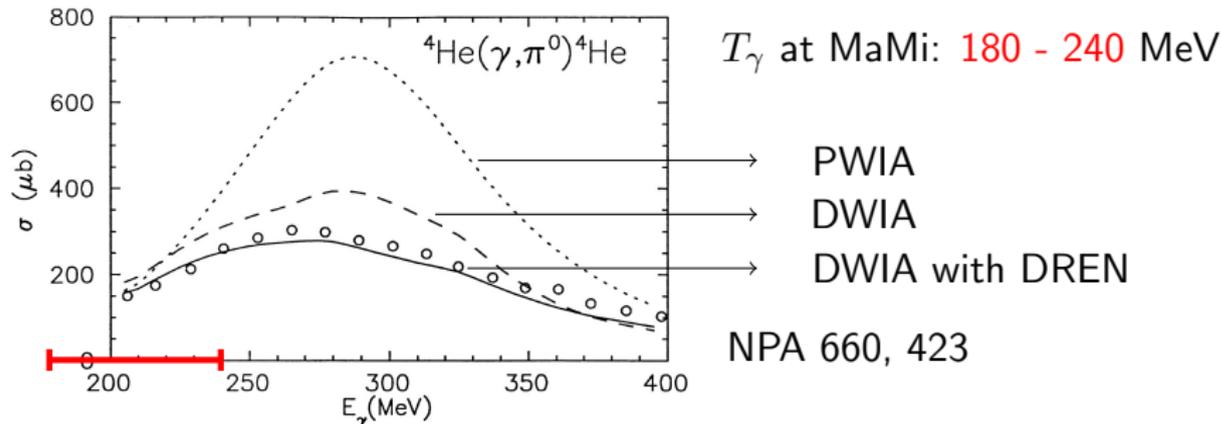
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Distorted wave impulse approximation (DWIA)

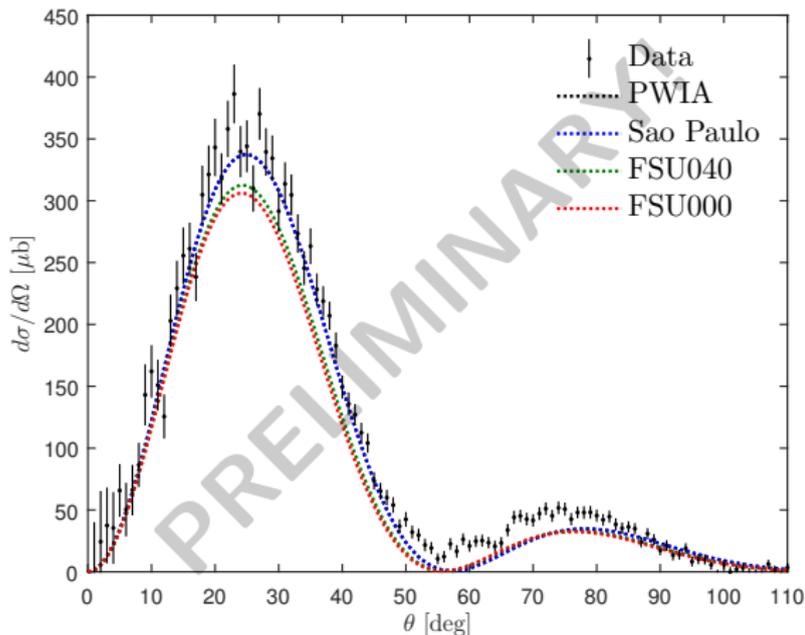
Cross section of photoproduction in DWIA

→ Final state interactions taken into account

$$\frac{d\sigma_{\text{DWIA}}^{\gamma \rightarrow \pi}}{d\Omega_{\text{CM}}} \text{ loses its proportionality to } \rho(q)$$

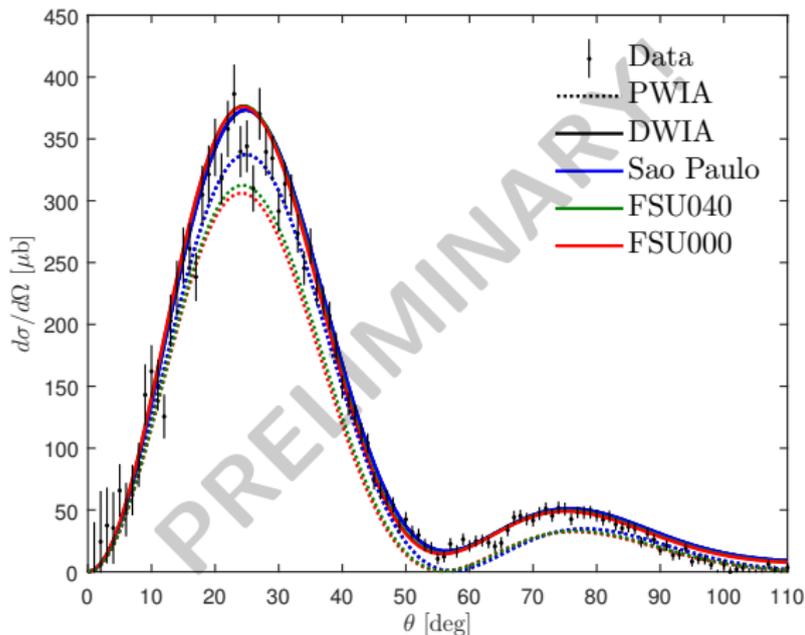


Comparison with experiment at $T_\gamma = 180\text{-}190$ MeV



Data courtesy of M. Ferretti (PRELIMINARY)

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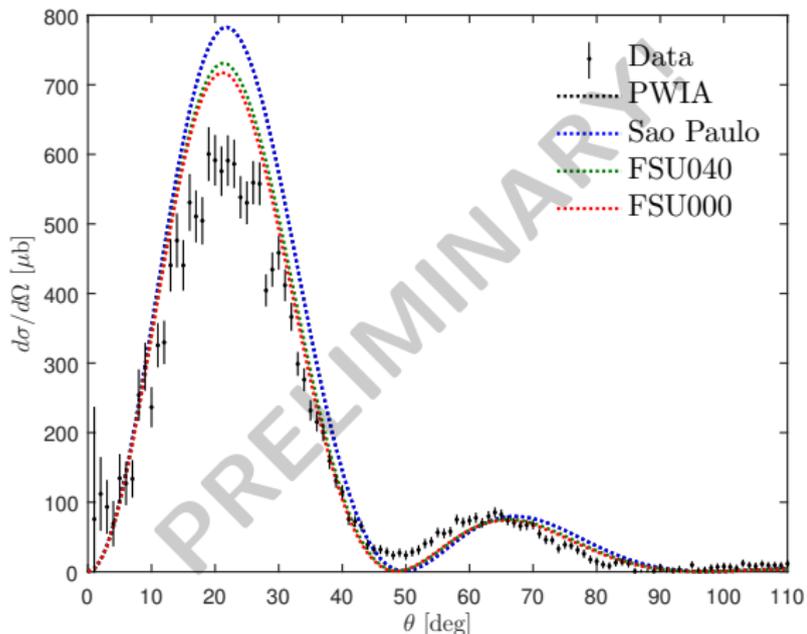
Good agreement

2nd peak reproduced

No $\rho(q)$ dependence

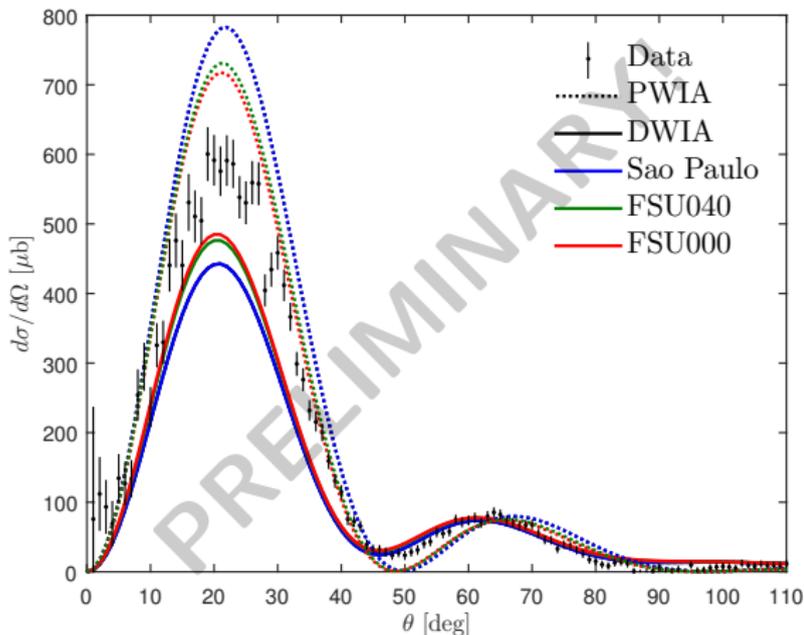
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Comparison with experiment at $T_\gamma = 200\text{-}210$ MeV



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Comparison with experiment at $T_\gamma = 200-210$ MeV



Data courtesy of M. Ferretti (PRELIMINARY)

Less good agreement

1st peak suppressed

2nd peak reproduced

$\rho(q)$ dependence

potential needs to be adjusted

Conclusion, prospects and thanks

- New reaction model implemented
 - ◇ PWIA has dependence when differences of skins ~ 0.10 fm (but little)
 - ◇ DWIA $\pi - A$ potential needs adjustments in range of energies
- What remains to be done
 - ◇ Can we infer information about skin from comparing different isotopes?
 - ◇ Constraints on DWIA $\pi - A$ potential
 - ◇ Analysis of the dependence to $\pi - A$ potential (DWIA)
 - ◇ DREN (Δ resonance) to be studied and adjusted

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Thank you for your attention

Many thanks to my collaborators

(P. Capel, C. Sfienti, M. Vanderhaeghen
M. Thiel, M. Ferretti, V. Tsaran)



Backup

The symmetry energy

Bethe-Weizsäcker: incompressible quantum liquid-drop binding energy

$$B(Z, N) = a_V A - a_S A^{2/3} - a_C \frac{Z^2}{A^{1/3}} - a_A \frac{(N - Z)^2}{A} + \dots$$

In the limit where volume V and $A \rightarrow \infty$ but $A/V = \rho_0$ constant

$$\epsilon(\alpha) \equiv -\frac{B(Z, N)}{A} = -a_V + J\alpha^2, \quad \alpha = \frac{N - Z}{A}$$

α neutron-proton asymmetry.

Incompressible \rightarrow fails to reproduce response to density fluctuations
 \Rightarrow Equation of state (EOS) of asymmetric matter

$$\mathcal{E}(\rho, \alpha) = \mathcal{E}(\rho, \alpha = 0) + S(\rho) \alpha^2 + \dots \quad \alpha = \frac{N - Z}{A}$$

$\pi - A$ potential used

We currently use the potential (Phys. Rev. C25, 952 (1982))

$$U(\vec{k}', \vec{k}) \propto \left[(\hat{b}_0 + \hat{c}_0 q^2) \rho_A(q) + (\hat{B}_0 + \hat{C}_0 q^2) \rho_{A,2}(q) + (\vec{k} \cdot \vec{k}') \mathcal{L}(q) \right]$$
$$\left\{ \begin{array}{l} \mathcal{L}(q) = FT(\mathcal{L}(r)) = FT \left(\frac{L(r)}{1 + (4\pi/3)\lambda L(r)} \right) \\ L(r) = \hat{c}_0 \rho_A(r) + \hat{C}_0 \rho_{A,2}(r) \end{array} \right.$$

Derived from most general $\pi - N$ potential (for spin 0 nucleus!) + Abs.

$$f^{\pi N}(\vec{k}'_{\pi}, \vec{k}_{\pi}) = b_0 + b_1 \hat{\mathbf{t}}_{\pi} \cdot \hat{\mathbf{r}}_N + (c_0 + c_1 \hat{\mathbf{t}}_{\pi} \cdot \hat{\mathbf{r}}_N) \vec{k}_{\pi} \cdot \vec{k}'_{\pi}$$

\hat{b}_0, \dots fitted on C, O, Ca, Zr, Pb ($T_{\pi}^{\text{lab}} = 50 \text{ MeV} \rightarrow T_{\gamma}^{\text{lab}} \sim 180 \text{ MeV}$)

E dep. shaped like b_0, \dots from SAID (http://gwddac.phys.gwu.edu/analysis/pin_analysis.html)

Derivation of new potential ongoing (with V. Tsaran, M. Vanderhaeghen)

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b_0 , b_1 , c_0 and c_1 taken from SAID (http://gwdac.phys.gwu.edu/analysis/pin_analysis.html)

- + Impulse approximation (other nucleons of nucleus are spectators)
- + Folding with density of nucleus
- + Kinematic corrections ($\pi - N$ to $\pi - A$ cm. frame)
- + Adding absorption (B_0 and C_0 parameters from NPA329, 429 (1979))

Derivation has been done for ^{12}C (V. Tsaran):

$$\begin{aligned} U(\vec{k}', \vec{k}) &\propto U^{1\text{st}} + U^{2\text{nd}} + U^{\text{abs}} \\ &= \left\{ [b_0 + c_0(\vec{k} \cdot \vec{k}' + q^2)] \rho_A(q) + c_0 K(q) \right\} \\ &\quad + \left\{ \tilde{b}_0^2 Z_{ss}(\vec{k}', \vec{k}) + \tilde{b}c Z_{sp}(\vec{k}', \vec{k}) + \tilde{c}_0 Z_{pp}(\vec{k}', \vec{k}) \right\} \\ &\quad + \left\{ B_0 + C_0[\vec{k} \cdot \vec{k}' + q^2] \right\} \rho_{A,2}(q) \end{aligned}$$

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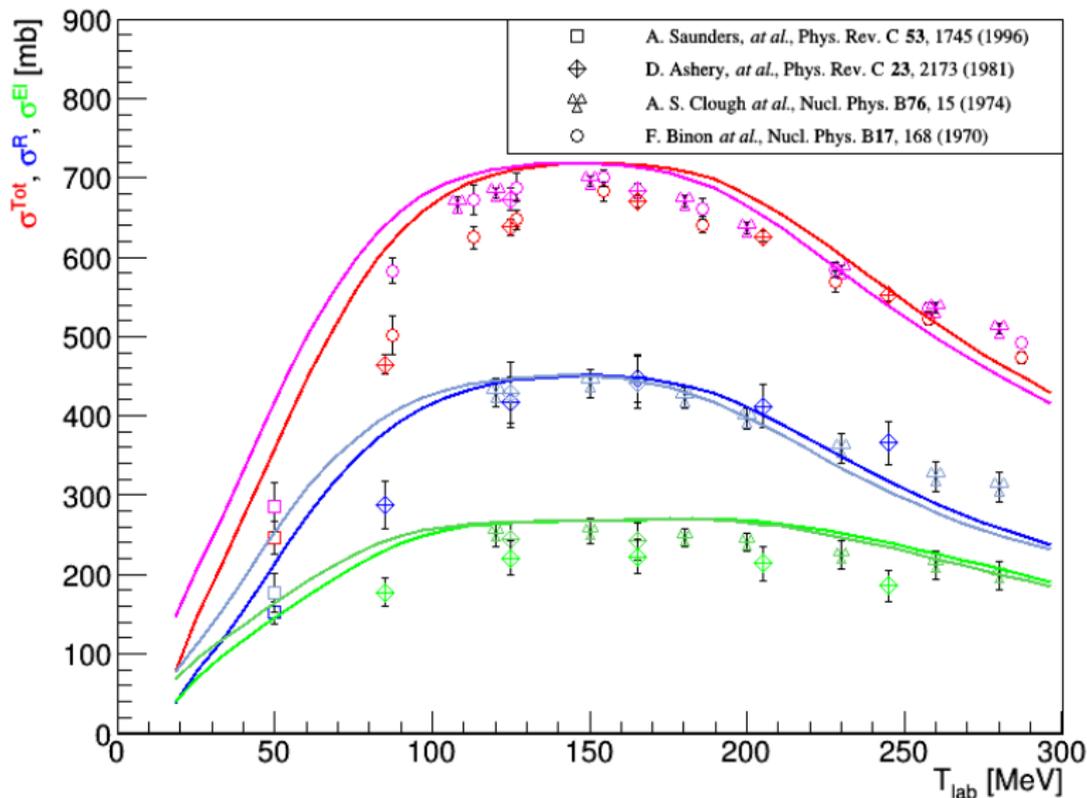
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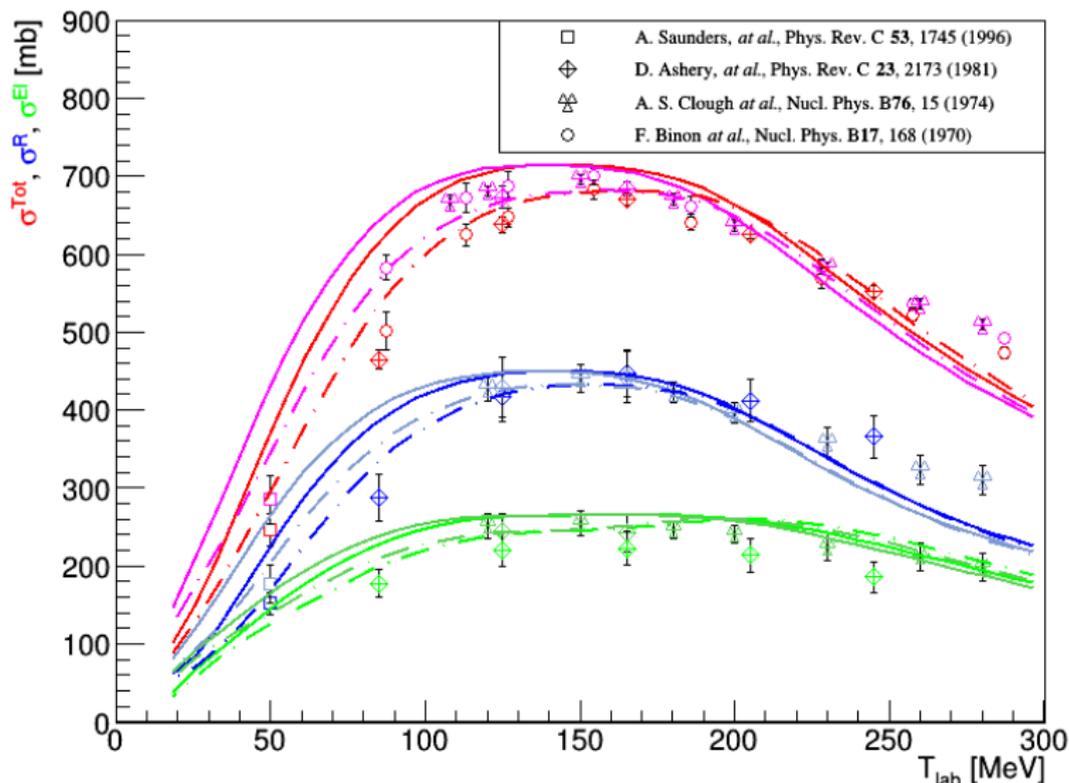
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FT($\rho^2(r)$)

How close to data are we with the potential (on ^{12}C)?

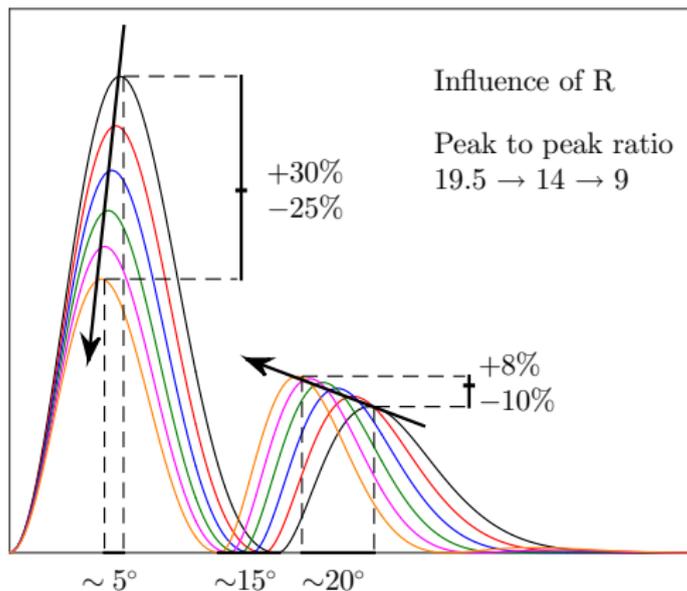


How close to data are we with the potential (on ^{12}C)?



Influence of the radius R on PWIA

Influence of radius R on the photo-production cross section



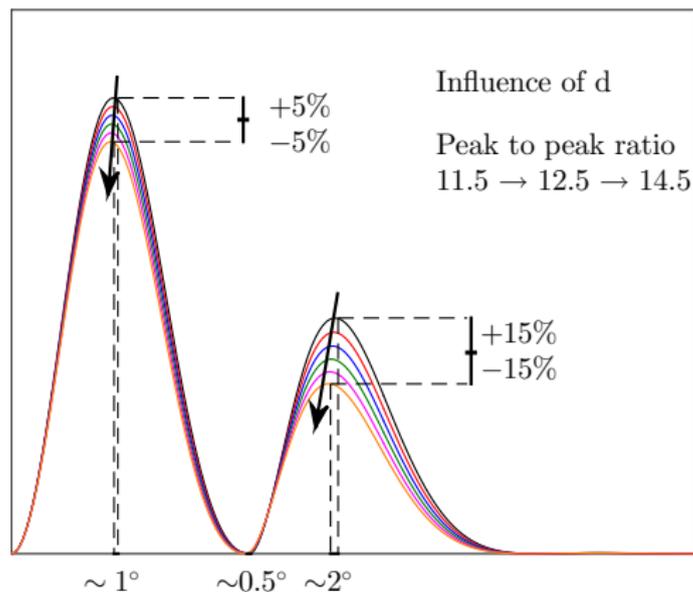
As R increases ($\pm 10\%$),

- First peak \downarrow
- Second peak \uparrow
- Large shift to small ang.

Peak to peak ratio exhibits large variations

Influence of the diffuseness d on PWIA

Influence of diffuseness d on the photo-production cross section



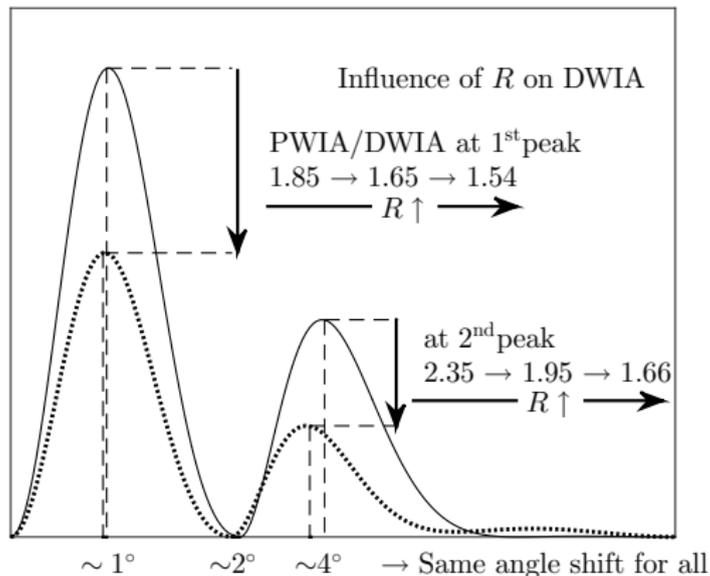
As d increases ($\pm 10\%$),

- First peak \downarrow (like R)
- Second peak \downarrow ($> < R$)
- Small shift to small ang. ($> < R$)

Peak to peak ratio exhibits small variations

Influence of the radius R on DWIA

Influence of radius R on the photo-production cross section with distortion



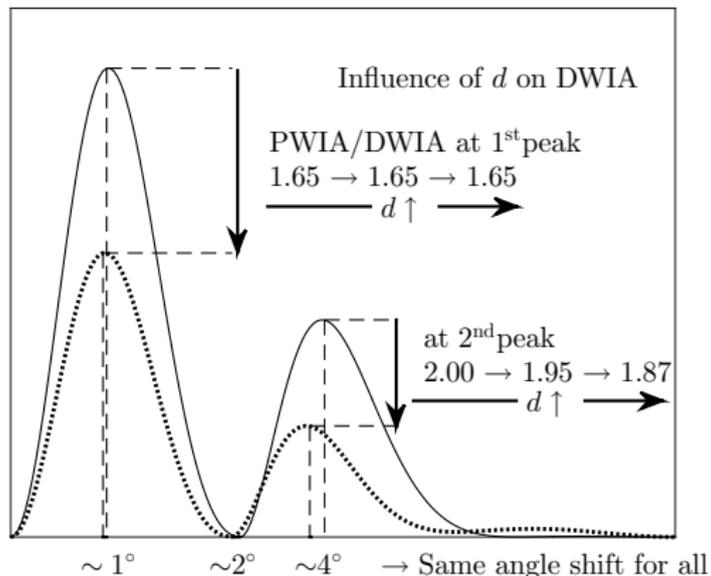
As R increases ($\pm 10\%$), impact of DWIA is

- smaller on first peak
- smaller on second peak
- the same at all angles

Peak to peak ratio exhibits small variations

Influence of the diffuseness d on DWIA

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