Gravitational Waves from Inflation

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- General properties and importance for cosmology
- Current bounds and detectability
- Particle sources during inflation
- Tensor fossils
- Polarized Sunyaev–Zeldovich tomography

- General properties and importance for cosmology
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- Particle sources during inflation

1806.05474 - ED, Fasiello, Hardwick, Koyama, Wands 1608.04216 - ED, Fasiello, Fujita 1411.3029 - Biagetti, ED, Fasiello, Peloso

• Tensor fossils

1708.01587 - **Biagetti**, ED, **Fasiello** 1407.8204 - ED, **Fasiello**, Jeong, Kamionkowski 1504.05993 - ED, **Fasiello**, Kamionkowski

• Polarized Sunyaev–Zeldovich tomography

1810.09463 - Deutsch, ED, **Fasiello**, Johnson, **Muenchmeyer** 1707.08129 - Deutsch, ED, Johnson, **Muenchmeyer**, Terrana

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The universe over time



Cosmic Microwave Background

decoupling of radiation from matter occurs at T ~ 3000 K (today: T ~ 2.7 K)

photons propagate freely after decoupling

fossil radiation, providing a snapshot of the early universe



Primordial Gravitational waves

also a fossil radiation

GW carry direct information about their sources and retain memory of the universe history!

Possible GW production mechanisms in the early universe

- Inflation: amplification of vacuum fluctuations
- Inflation: particle production
- Preheating
- Alternatives to inflation
- Phase transitions
- Cosmic strings
- ...

GW: great potential for discovery of new physics!

Possible GW production mechanisms in the early universe

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GW: great potential for discovery of new physics!

Inflation

- postulated era of accelerated expansion in the very early universe
- explains why CMB is <u>nearly perfectly uniform</u> across scales that were super horizon at decoupling
- explains how those tiny fluctuations were generated



Inflation

Simplest realization: single-scalar field in slow-roll (SFSR)



Inflation

Simplest realization: single-scalar field in slow-roll (SFSR)





Gravitational waves

$$ds^{2} = -dt^{2} + a^{2}(t) \left(\delta_{ij} + \gamma_{ij}\right) dx^{i} dx^{j}$$

 $\gamma^i_i = \partial_i \gamma_{ij} = 0~~{
m two}~{
m polarization}~{
m states}~{
m of}~{
m the}~{
m graviton}$



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Scales — Experiments



Observational bounds/sensitivities



Implications for model building:

$$\frac{\Delta\phi}{M_{\rm pl}} \gtrsim \left(\frac{r_*}{8}\right)^{1/2} \mathcal{N}_* \gtrsim \left(\frac{r_*}{0.01}\right)^{1/2} \qquad \text{threshold for} \\ \text{large field inflation}$$



Observational bounds/sensitivities



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GW background from inflation

$$\ddot{\gamma}_{ij} + 3H\dot{\gamma}_{ij} + k^2\gamma_{ij} = 16\pi G \Pi_{ij}^{TT} \qquad \begin{array}{l} \text{anisotropic} \\ \text{stress-energy} \\ \text{tensor} \\ (\text{from } \delta T_{ij}) \end{array}$$

• homogeneous solution: GWs from vacuum fluctuations

• inhomogeneous solution: GWs from sources

$$\Pi_{ij}^{TT} \propto \left\{ \partial_i \phi \, \partial_j \phi \right\}^{TT} \quad \left\{ E_i E_j + B_i B_j \right\}^{TT} \quad \left\{ \sigma_{ij} \right\}^{TT}$$
scalars vectors tensors

GW background from inflation

• homogeneous solution: GWs from vacuum fluctuations

energy scale of inflation

$$\mathcal{P}_{\gamma}^{\text{vacuum}}(k) = \frac{2}{\pi^2} \frac{H^2}{M_{\text{pl}}^2} \left(\frac{k}{k_*}\right)^{n_T} \qquad \text{red tilt:} \\ n_T = -r/8 \quad \text{amplitude decreases} \\ \text{as we go towards} \\ \text{smaller scales} \end{cases}$$

GW background from inflation

$$\ddot{\gamma}_{ij} + 3H\dot{\gamma}_{ij} + k^2\gamma_{ij} = 16\pi G \Pi_{ij}^{TT}$$

• **inhomogeneous** solution: GWs from **sources**



Why additional fields?

 Natural from a top-down perspective: plenty of candidates from string theory (e.g. moduli fields, axions, Kaluza-Klein modes, gauge fields...)

 Interesting for phenomenology: qualitatively different signatures w.r.t. basic single-field inflation — testable!

Scalar field (I)



[Biagetti, Fasiello, Riotto 2012, Biagetti, ED, Fasiello, Peloso 2014, Fujita, Yokoyama, Yokoyama, 2014]

Scalar field (II)

Auxiliary scalars with time-varying mass



[Chung et al., 2000, Senatore et al, 2011, Pearce et al, 2017]

Axion-Gauge fields models: genesis

• Generic requirement for inflation: nearly flat potential:

$$\epsilon \equiv \frac{M_p^2}{2} \left(\frac{V'}{V}\right)^2, \ \eta \equiv M_p^2 \frac{V''}{V}$$

... but flatness may be spoiled by radiative corrections!



- Flatness protected by axionic shift symmetry $\phi \rightarrow \phi + c$
 - Natural Inflation [Freese, Frieman, Olinto 1990] $V(\varphi) = \Lambda^4 \left[1 - \cos(\varphi/f)\right]$

• Agreement with observations requires:

$$f \gtrsim M_P$$

undesirable constraint on the theory [Kallosh, Linde, Susskind, 1995, Banks et al, 2003]

Axion-Gauge fields models: motivation

 $\frac{\lambda\chi}{4f}F\tilde{F}$

- naturally light inflaton
- sub-Planckian axion decay constant
- support reheating

Axion-Gauge fields models: SU(2)

$$\mathcal{L} = \mathcal{L}_{\text{inflaton}} - \frac{1}{2} \left(\partial \chi \right)^2 - U(\chi) - \frac{1}{4} FF + \frac{\lambda \chi}{4f} F\tilde{F}$$

$$P_{\gamma, \text{vacuum}} \qquad \qquad \mathcal{L}_{\text{spectator}} \longrightarrow P_{\gamma, \text{sourced}}$$

- Inflaton field dominates energy density of the universe
- Spectator sector contribution to curvature fluctuations negligible



[ED-Fasiello-Fujita 2016]

Axion-Gauge fields models: SU(2)

One helicity of the gauge field fluctuations is amplified from coupling with axion \longrightarrow the same helicity of the tensor mode is amplified



[ED-Fasiello-Fujita 2016]

Axion-Gauge fields models: signatures

• Scale dependence

Chirality

Non-Gaussianity

Scale-dependence

basic single-field inflation

$$n_T \simeq -r/8$$

(nearly flat spectrum)

axion-gauge fields models



- detectably large and running n_T
- bump may occur at small scales

[ED-Fasiello-Fujita 2016, Thorne et al, 2017]

Chirality

basic single-field inflation $\gamma_L = \gamma_R$ non-chiral $\langle TB \rangle, \langle EB \rangle = 0$ (parity conservation)

axion-gauge fields models



Detectable at 2σ by LiteBIRD for r > 0.03 [Thorne et al, 2017]

Chirality

basic single-field inflation

 $\gamma_L = \gamma_R$
non-chiral

axion-gauge fields models

$$\gamma_L \neq \gamma_R$$

chiral

Interferometers: need advanced design with multiple (non co-planar) detectors [Thorne et al. 2017, Smith-Caldwell 2016]

Non-Gaussianity: beyond the power spectrum





Tensor non-Gaussianity



from interactions of the tensors with other fields or from self-interactions



Tensor non-Gaussianity

basic single-field inflation



$$f_{NL} = \mathcal{O}(r^2)$$

too small for detection

axion-gauge fields models



detectable by upcoming CMB space missions
 [Agrawal - Fujita - Komatsu 2017]

Mixed (scalar-tensor) non-Gaussianity

testing interactions of tensors and matter fields



potentially observable!

[ED - Fasiello - Hardwick - Koyama - Wands 2018, Fujita - Namba - Obata 2018]

Inflationary GWs from vacuum fluctuations

- Energy scale of inflation: $V_{\text{infl}}^{1/4} \approx 10^{16} \text{GeV} (r/0.01)^{1/4}$ $H \approx 2 \times 10^{13} \sqrt{r/0.01} \text{ GeV}$
- Scalar field excursion (Lyth bound): $\Delta \phi / M_P \gtrsim (r/0.01)^{1/2}$
- Red tilt: $n_T \simeq -2\epsilon = -r/8$
- Non-chiral: $P_L = P_R$
- Nearly Gaussian: $f_{NL} \ll 1$

One or more of these predictions may be easily violated beyond the minimal set-up!

so far ...



Einstein Telescope, LISA, BBO, DECIGO, ...]



[advanced LIGO/VIRGO, KAGRA, LIGO India, Einstein Telescope, LISA, BBO, DECIGO, ...]

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Squeezed non-Gaussianity



amplitude of long-wavelength modes coupled with amplitude of short-wavelength modes



Soft limits and fossils



Soft limits and fossils



[ED, Fasiello, Jeong, Kamionkowski - 2014, ED, Fasiello, Kamionkowski - 2015, Biagetti, ED, Fasiello - 2017]

Why is squeezed non-Gaussianity so important?

Soft limits in inflation

SINGLE-FIELD (single-clock) inflation: soft-limits not observable



Intuitive understanding :

Super-horizon modes freeze-out

• Standard initial conditions

Soft mode rescales background for hard modes Effect can be gauged away!

[Maldacena 2003, Creminelli, Zaldarriaga 2004]

Soft limits in inflation





Soft limits reveal (extra) fields mediating inflaton or graviton interactions

squeezed bispectrum delivers info on mass spectrum!!!



Soft limits in inflation

- Extra fields [Chen - Wang 2009, ED - Fasiello - Kamionkowski 2015, ED - Emami 2016, Biagetti - ED - Fasiello 2017, ...]
- Non-Bunch Davies initial states

[Holman - Tolley 2007, Ganc - Komatsu 2012, Brahma - Nelson - Shandera 2013, ...]

Broken space diffs

(e.g. space-dependent background)

[Endlich et al. 2013, ED - Fasiello - Jeong - Kamionkowski 2014, ...]

probe for (extra) fields, pre-inflationary dynamics, (non-standard) symmetry patterns

Tensor fossils

• Learning about primordial gravitational waves through non-Gaussian effects

Local observables affected by long modes (anisotropic effects / off-diagonal correlations)

• Effects from "squeezed" tensor-scalar-scalar bispectrum particularly effective at constraining inflation!

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Polarized Sunyaev–Zeldovich tomography



Polarized Sunyaev-Zel'dovich effect



- Polarization from Thomson scattering of (quadrupolar) radiation by free electrons
- Used to obtain a map of the remote (= locally observed)
 CMB quadrupole
- Additional information w.r.t. primary CMB (scattered photons from off our past light cone)

Polarized Sunyaev-Zel'dovich effect

$$(Q \pm iU)(\hat{n}_e)\big|_{pSZ} = -\frac{\sqrt{6}}{10}\sigma_T \int d\chi_e \ a(\chi_e) \ n_e(\hat{n}_e, \chi_e) \underbrace{\tilde{q}_{eff}^{\pm}(\hat{n}_e, \chi_e)}_{(qeff)}$$

$$\tilde{q}_{\text{eff}}^{\pm}(\hat{n}_{e},\chi) = \sum_{m=-2}^{2} q_{\text{eff}}^{m}(\hat{n}_{e},\chi_{e}) \pm 2Y_{2m}(\hat{n}_{e})$$

$$q_{\text{eff}}^{m}(\hat{n}_{e},\chi_{e}) = \int d^{2}\hat{n} \left[\Theta(\hat{n}_{e},\chi_{e},\hat{n}) + \Theta^{T}(\hat{n}_{e},\chi_{e},\hat{n})\right] Y_{2m}^{*}(\hat{n})$$
"Denote" (choose used at the location of the secttorer) CMD subdrupple

"Remote" (observed at the location of the scatterer) CMB quadrupole

<u>Notice</u>: $q_{\text{eff}}^m(\mathbf{\hat{n}_e}, \chi_e \to 0) = a_{2m}^T$



pSZ tomography

Reconstructing the remote quadrupole field from CMB-LSS cross-correlation:

$$\left\langle \begin{array}{l} (Q \pm iU) \Big|_{pSZ} \left(\delta(\bar{\chi}_e) \right) \right\rangle \sim \left\langle \delta q^{\pm} \delta \right\rangle \sim q^{\pm}(\hat{n}_e, \bar{\chi}_e) \left\langle \delta \delta \right\rangle(\bar{\chi}_e)$$

tracer of electron
number density ensemble average
over small-scales
(q treated as a fixed
deterministic field) long-wavelength
modulation of
small-scale power

[Kamionkowski, Loeb 1997, Alizadeh, Hirata 2012, Deutsch, ED, Johnson, Muenchmeyer, Terrana - 2017]

pSZ tomography



Bin-averaged quadrupole field moments decomposition:

$$\bar{q}^{\pm \alpha}(\hat{n}_e) = \sum_{\ell m} a_{\ell m}^{q \pm \alpha}{}_{\pm 2} Y_{\ell m}(\hat{n}_e)$$

$$\begin{cases} a_{\ell m}^{q,E\,\alpha} = -\frac{1}{2} \left(a_{\ell m}^{q+\alpha} + a_{\ell m}^{q-\alpha} \right) & \longleftarrow \text{ scalars/}\\ a_{\ell m}^{q,B\,\alpha} = -\frac{1}{2i} \left(a_{\ell m}^{q+\alpha} - a_{\ell m}^{q-\alpha} \right) & \longleftarrow \text{ tensors}\\ \text{only} \end{cases}$$

binned

$$\underbrace{\text{Optimal unbiased estimator}}_{\hat{a}_{\ell m}^{q,X\,\alpha}} : X = E, B$$

$$\hat{a}_{\ell m}^{q,X\,\alpha} = \sum_{\ell_1 m_1 \ell_2 m_2} \left(W_{\ell m \ell_1 m_1 \ell_2 m_2}^{X,E} a_{\ell_1 m_1}^E + W_{\ell m \ell_1 m_1 \ell_2 m_2}^{X,B} a_{\ell_1 m_1}^B \right) \Delta \tau_{\ell_2 m_2}^{\alpha}$$

[A.-S. Deutsch, ED, M.C. Johnson, M. Muenchmeyer, A. Terrana - 2017]

Primordial gravitational wave phenomenology with pSZ tomography

full set of correlations between primary CMB and reconstructed remote quadrupole field



[A.-S. Deutsch, ED, M. Fasiello, M.C. Johnson, M. Muenchmeyer - 2018]

$$C_{\ell,\alpha\alpha'}^{XX} = \int d\ln k \, \Delta_{\ell\alpha}^{X}(k) \Delta_{\ell\alpha'}^{X}(k) \, \mathcal{P}_{h}, \quad X = \{qE, qB\}$$

$$C_{\ell,\alpha}^{qEX} = \int d\ln k \, \Delta_{\ell\alpha}^{qE}(k) \Delta_{\ell}^{X}(k) \, \mathcal{P}_{h}, \quad X = \{T, E\}$$

$$C_{\ell,\alpha}^{qBB} = \int d\ln k \, \Delta_{\ell\alpha}^{qB}(k) \Delta_{\ell}^{B}(k) \, \mathcal{P}_{h}, \quad X, Y = \{T, E\}$$

$$C_{\ell,\alpha\alpha'}^{qEqB} = \Delta_{c} \int d\ln k \, \Delta_{\ell\alpha}^{qE}(k) \Delta_{\ell\alpha'}^{qB}(k) \, \mathcal{P}_{h}, \quad X, Y = \{T, E\}$$

$$C_{\ell,\alpha}^{qEB} = \Delta_{c} \int d\ln k \, \Delta_{\ell\alpha}^{qE}(k) \Delta_{\ell}^{B}(k) \, \mathcal{P}_{h}, \quad X = \{T, E\}$$

$$C_{\ell\alpha}^{qBX} = \Delta_{c} \int d\ln k \, \Delta_{\ell\alpha}^{qB}(k) \Delta_{\ell}^{X}(k) \, \mathcal{P}_{h}, \quad X = \{T, E\}$$

$$C_{\ell}^{XB} = (\Delta_{c}) \int d\ln k \, \Delta_{\ell\alpha}^{qB}(k) \Delta_{\ell}^{B}(k) \, \mathcal{P}_{h}, \quad X = \{T, E\}$$
chirality
primordial tensor power spectrum

[A.-S. Deutsch, ED, M. Fasiello, M.C. Johnson, M. Muenchmeyer - 2018]

Fisher matrix forecast to derive exclusion bounds

• parameters in the primordial tensor power spectrum for the SU(2) model

amplitude *r*

scale-dependence n_T

chirality Δ_c

[A.-S. Deutsch, ED, M. Fasiello, M.C. Johnson, M. Muenchmeyer - 2018]

Forecasted parameter constraints



- green: zero-noise cosmic variance limit using primary CMB T, E, B
- red: T, E, B, qE, qB with instrumental noise $1 \mu K$ arcmin
- blue: T, E, B, qE, qB with instrumental noise $0.1 \,\mu K$ arcmin
- grey: T, E, B, qE, qB with no instrumental noise

pSZ tomography

improvements on constraints on phenomenological models of the tensor sector w.r.t. using the primary CMB (only)

Observers: optimize future missions to go after these signals

Primordial gravitational waves

• an important probe of the early universe and its evolution

• can lead to discovery of new physics

- testable on a vast range of scales (and from cross-correlations of different probes!)
- different observables (not only r and Ω_{GW}) to characterize them and identify their sources