

# LCSRs Discussion

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## LCSRs for $B \rightarrow \{P, V\}$ Form Factors

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# Shameless Self Advertisement



- ▶ C++ implementation of the LCSRs publicly available
- ▶ uses numerical integration so that  $B$ -LCDAs can be swapped
- ▶ results of recent analysis are contained in the EOS release and as separate machine-readable ancillary files

[Gubernari,Kokulu,DvD 1811.00983]

[EOS homepage](#)

[GitHub repository](#)

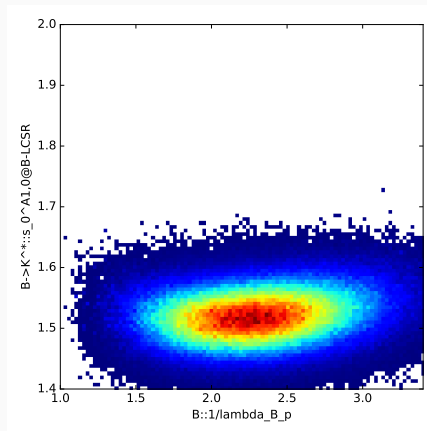
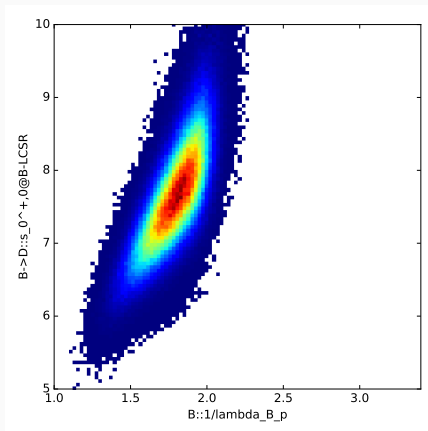
- ▶ we are happy to adapt / extend EOS for your needs  
please contact us

## Interesting observation

when determining the threshold parameters for all  $\bar{B} \rightarrow D$ ,  $\bar{B} \rightarrow D^*$ , and  $B \rightarrow K^*$  form factors

- ▶ each form factor has an independent threshold parameter
- ▶ posteriors show weak correlation between threshold parameter and LCDA input  $\lambda_B^+$
- ▶ in combination posterior contains surprising amount of information on  $\lambda_B^+$
- ▶ take with a grain of salt: this is probably highly model dependent, still investigating

# Interesting observation



LCSR Input:  $1/\lambda_B^+$  from  $B^- \rightarrow \gamma \ell^- \bar{\nu}$

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# $B^- \rightarrow \gamma \ell^- \bar{\nu}$ : Belle 2 back-of-an-envelope projections

Assuming a lower cut  $E_\gamma \leq 1 \text{ GeV}$

[B2TIP Report 1808.10567]

Table 46: Expected statistical error in  $10^{-6}$  for Belle and Belle II for a simulated partial branching fraction of  $\Delta\mathcal{B}(B^+ \rightarrow \ell^+ \nu_\ell \gamma) = 5.0 \times 10^{-6}$ .

	Belle	Belle II	Belle II
New analysis		5 ab <sup>-1</sup>	50 ab <sup>-1</sup>
	+1.48	+0.56	+0.18
	-1.39	-0.53	-0.17

- ▶ projected central value larger than existing Belle upper bound

$$\mathcal{B}(B^- \rightarrow \gamma \ell^- \bar{\nu})|_{E_\gamma \leq 1 \text{ GeV}} < 3.5 \cdot 10^{-6} \quad @ \quad 90\% \text{CL} \quad \text{[Belle 1810.12976]}$$

- ▶ present central value

$$\mathcal{B}(B^- \rightarrow \gamma \ell^- \bar{\nu})|_{E_\gamma \leq 1 \text{ GeV}} = (1.4 \pm 1 \pm 0.4) \cdot 10^{-6} \quad \text{[Belle 1810.12976]}$$

- ▶ assuming the uncertainty to be dominantly statistical in nature for the current central value, the projection reads

$$\frac{\delta\mathcal{B}}{\mathcal{B}} \simeq 3.6\% \times \sqrt{\frac{5.0 \cdot 10^{-6}}{1.4 \cdot 10^{-6}}} \simeq 7\%$$

[adapted from B2TIP Report 1808.10567 & Belle 1810.12976]

# Combining $B \rightarrow \gamma \ell \nu$ with $B \rightarrow \mu \nu$

schematically:  $\frac{\mathcal{B}(B \rightarrow \gamma \ell \nu)}{\mathcal{B}(B \rightarrow \mu \nu)} \propto \frac{1}{\lambda_{B,+}} + \text{three part./soft contributions}$

## theory

$B \rightarrow \tau \nu$

- ▶ removes normalization  $|V_{ub}| f_B$

$B \rightarrow \gamma \ell \nu$

- ▶ hard contrib. known to NLL precision  
[Beneke/Rohrwild 1110.3228]
- ▶ soft contrib. known in disp. approach  
[Braun/Khodjamirian 1210.4454]
- ▶ 3-particle contr.  
[Wang 1609.09813]  
[Braun et al. 1804.04962]

fit yields lower limit on the uncertainty

$$\sigma(\lambda_{B,+}) = 0.035 \text{ GeV} \quad [\text{assuming } \lambda_{B,+} = 0.35 \text{ GeV}]$$

## experiment

- ▶ expected uncertainty on  $B \rightarrow \mu \nu$   
for Belle II  $\sim 7\%$  for  $\mathcal{B} \simeq 3.5 \cdot 10^{-7}$

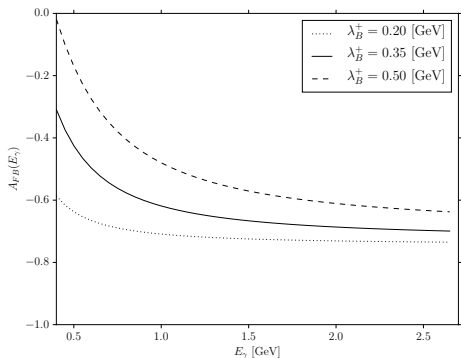
[adapted from B2TIP Report 1810.12976]

- ▶ expected uncertainty on  $B \rightarrow \gamma \ell \nu$   
for Belle II  $\sim 3.5\%$  for  
 $\mathcal{B}|_{E_\gamma > 1.0 \text{ GeV}} \simeq 5 \cdot 10^{-6}$

[adapted from B2TIP Report 1810.12976]



# Angular distribution of $B \rightarrow \gamma l \nu$



- ▶ use hypothetical measurements of binned  $A_{FB}$ 
  - ▶ [1.7 GeV, 2.0 GeV]
  - ▶ [2.0 GeV, 2.3 GeV]
  - ▶ [2.3 GeV,  $M_B/2$ ]
- ▶ assume a lower limit of **5%** on the uncertainty in each bin

scan yields a lower limit on the precision:

$$\sigma(\lambda_{B,+}) = 0.05 \text{ GeV} \quad [\text{assuming } \lambda_{B,+} = 0.35 \text{ GeV}]$$

$D_S$ -meson LCDAs?

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## $D_s^- \rightarrow \gamma l^- \bar{\nu}$ in QCDF ?

- ▶ adapting QCDF results for  $B^- \rightarrow \gamma l^- \bar{\nu}$  seems straightforward
- ▶ convergence doubtful, even for  $E_\gamma \leq 1 \text{ GeV}$
- ▶ no data available yet!
- ▶ however ...

$$\mathcal{B}(D_s^- \rightarrow \mu^- \bar{\nu}) = (5.5 \pm 0.23) \cdot 10^{-3}$$

[Particle Data Group]

- ▶ laboratory for the  $B^- \rightarrow \gamma l^- \bar{\nu}$  interested?
- ▶ potential applications:  $D_s \rightarrow \{K, \phi\} l \bar{\nu}$  LCSRs