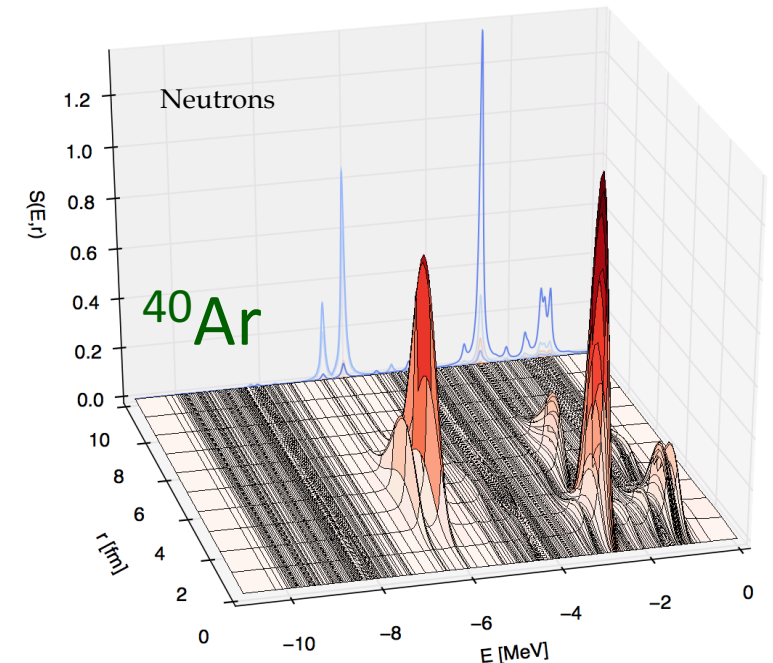
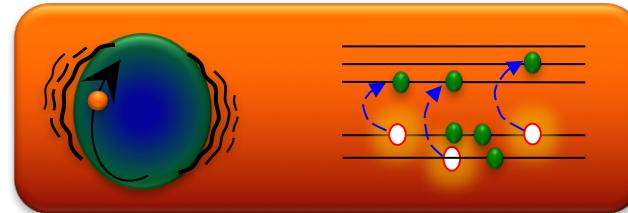
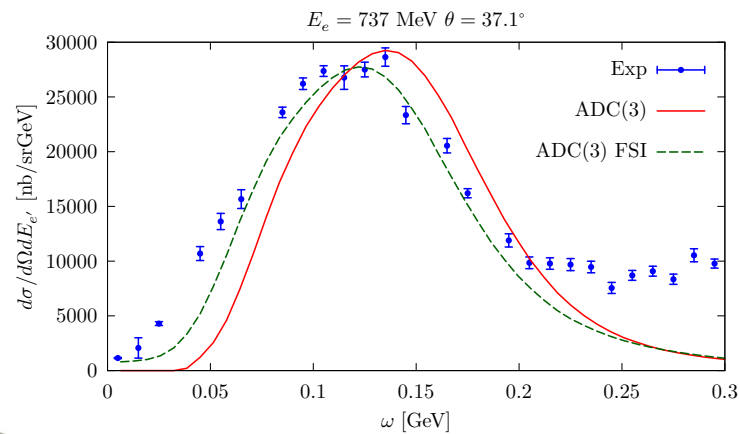


Neutrino and Electron Scattering off Nuclei with SCGF

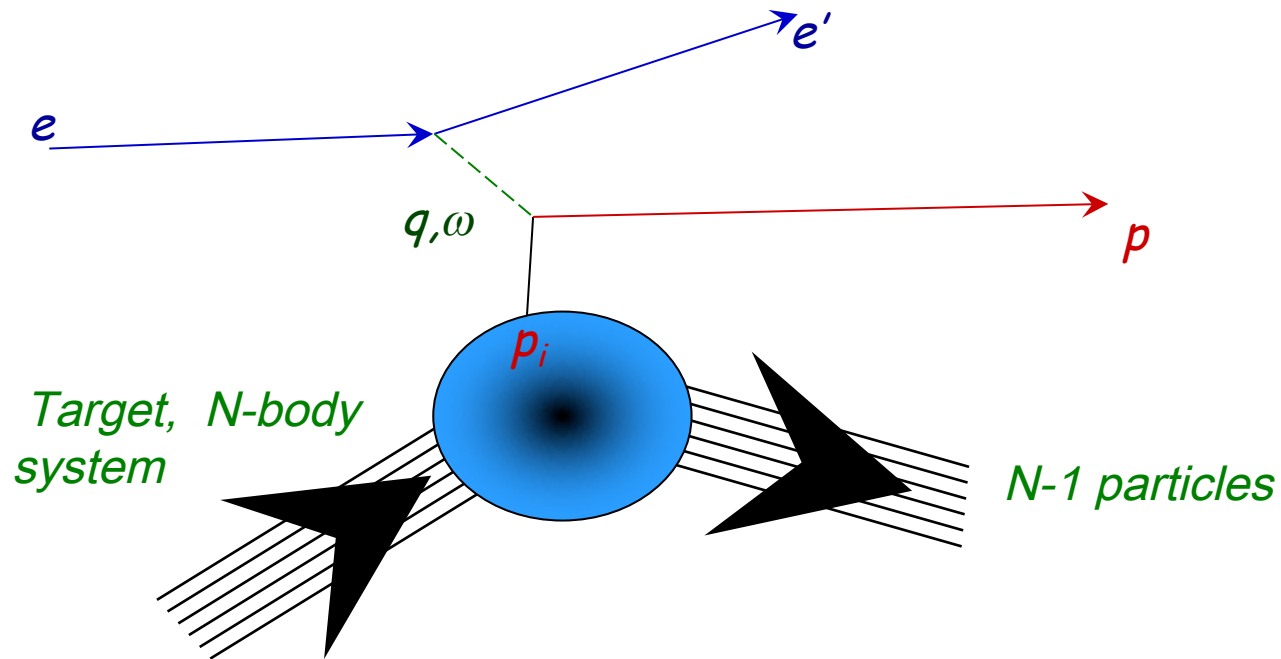
Carlo Barbieri — University of Surrey

2 October 2018



Spectroscopy via knock out reactions – *basic idea*

Use a probe (ANY probe) to eject the particle we are interested to:



In plane wave impulse approximation (PWIA):

$$\frac{d\sigma_{(e,e'p)}}{dE_{e'} d\Omega_{e'} d\Omega_p} = \sigma_{ep} \times S^h(p_m, E_m)$$

- Spectral distribution is crucial (in spite of “non observability”...)
- Targets are low-energy (ground) states

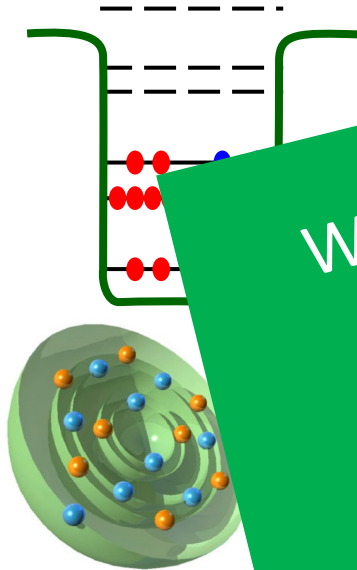
Basic idea:

- we know, e , e' and p
- “get” *energy and momentum of p_i* : $p_i = k_e' + k_p - k_e$
 $E_i = E_e' + E_p - E_e$

Better to choose *large transferred momentum and weak probes!!!* Energy and momentum transfer can be high. What about currents? Breaking of EFT? Use e⁻ scattering to constrain electroweak

Concept of correlations

independent
particle picture



Spectral function: distribution of
momentum (p_m) and energy (E_m)

Want to understand structure and nuclear forces
directly from first principles (ab initio).
So far, fully characterised only for closed-shell and
stable isotopes... (!)

[W. Dickhoff, CB, Prog. Part. Nucl. Phys. **52**, 377 (2004)]

E_m [MeV]

Saclay data for $^{16}\text{O}(e, e'p)$

[Mougey et al., Nucl. Phys. A335, 35 (1980)]

Understand a few stable closed shells:

[CB and W. H. Dickhoff, Prog. Part. Nucl. Phys **52**, 377 (2004)]

Current Status of low-energy nuclear physics

Composite system of interacting fermions

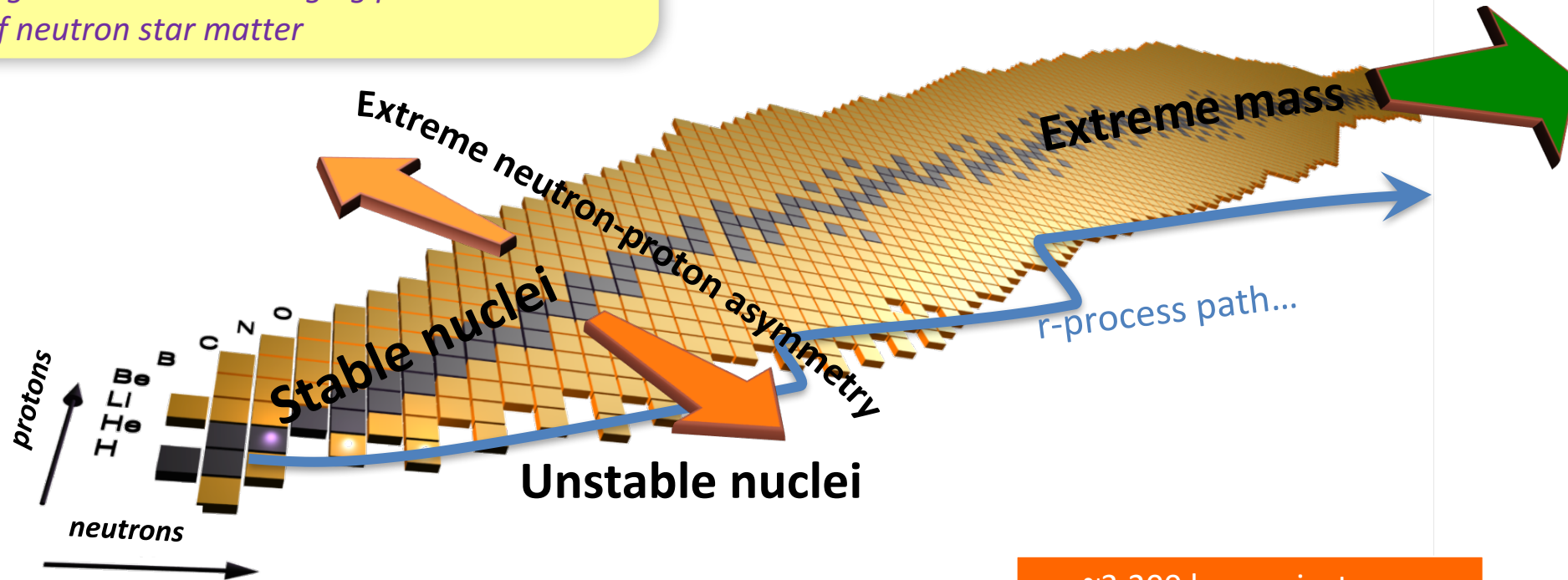
Binding and limits of stability

Coexistence of individual and collective behaviors

Self-organization and emerging phenomena

EOS of neutron star matter

Experimental
programs
RIKEN, FAIR, FRIB...



- ~3,200 known isotopes
- ~7,000 predicted to exist
- Correlation characterised in full for ~283 stable

Nature **473**, 25 (2011); **486**, 509 (2012)

Current Status of low-energy nuclear physics

Composite system of interacting fermions

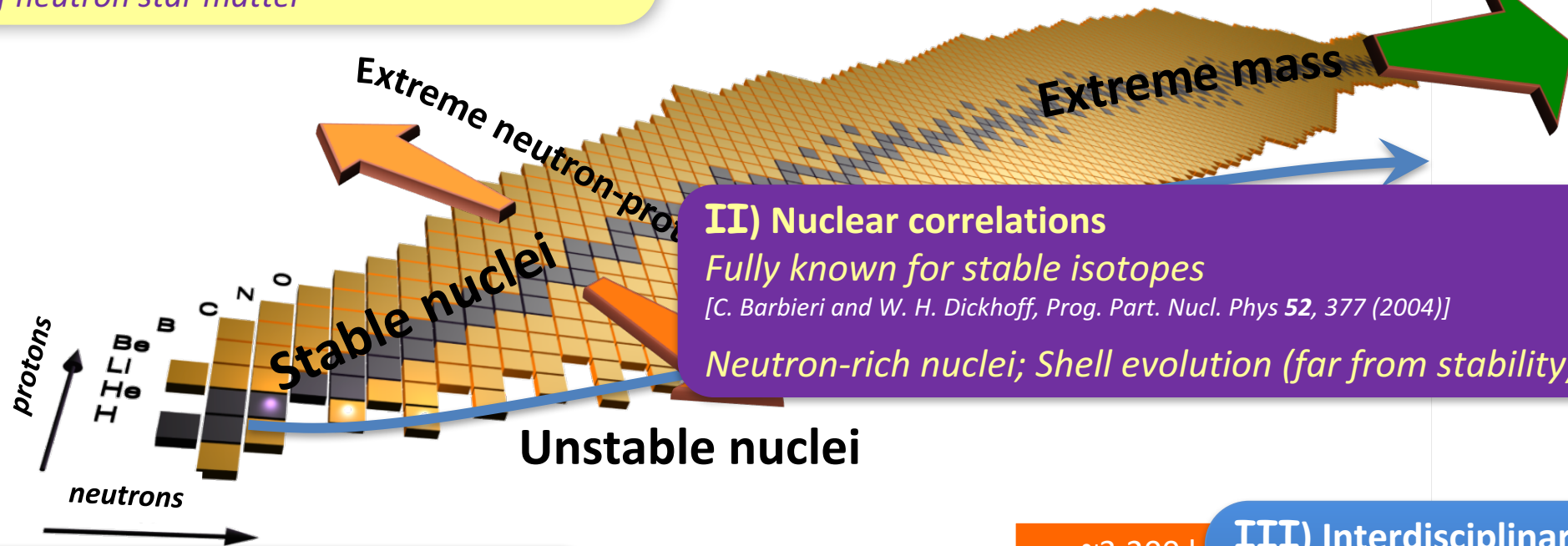
Binding and limits of stability

Coexistence of individual and collective behaviors

Self-organization and emerging phenomena

EOS of neutron star matter

Experimental
programs
RIKEN, FAIR, FRIB...



II) Nuclear correlations

Fully known for stable isotopes

[C. Barbieri and W. H. Dickhoff, Prog. Part. Nucl. Phys 52, 377 (2004)]

Neutron-rich nuclei; Shell evolution (far from stability)

I) Understanding the nuclear force

QCD-derived; 3-nucleon forces (3NFs)

First principle (ab-initio) predictions

III) Interdisciplinary character

Astrophysics

Tests of the standard model

Other fermionic systems:

ultracold gasses; molecules;

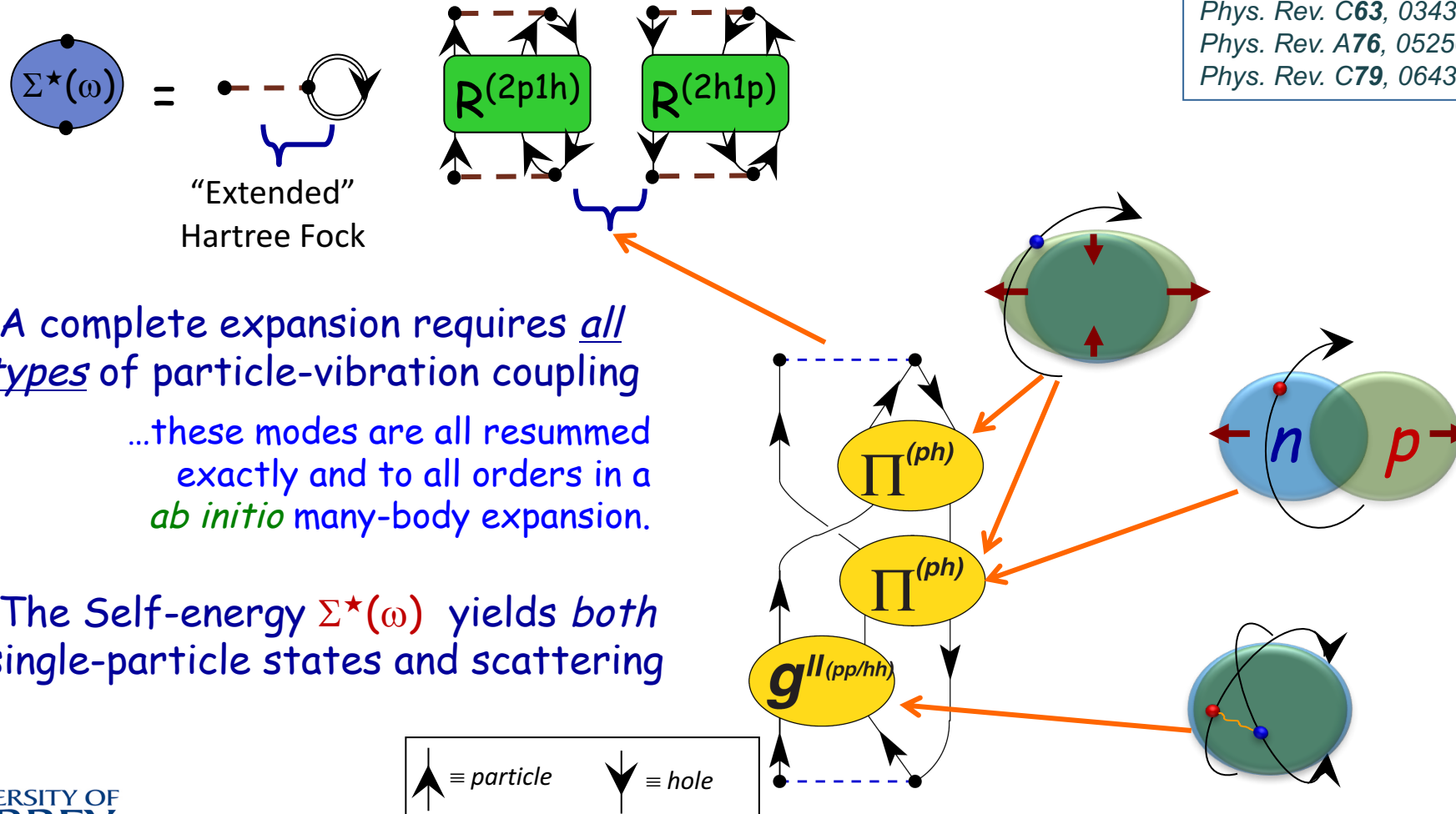
- ~3,200 k
- ~7,000 p
- Correlati
- in full fo

Nature **473**, 25

The FRPA Method in Two Words

Particle vibration coupling is the main mechanism driving the redistribution and fragmentation of particle strength—especially in the quasielastic regions around the Fermi surface...

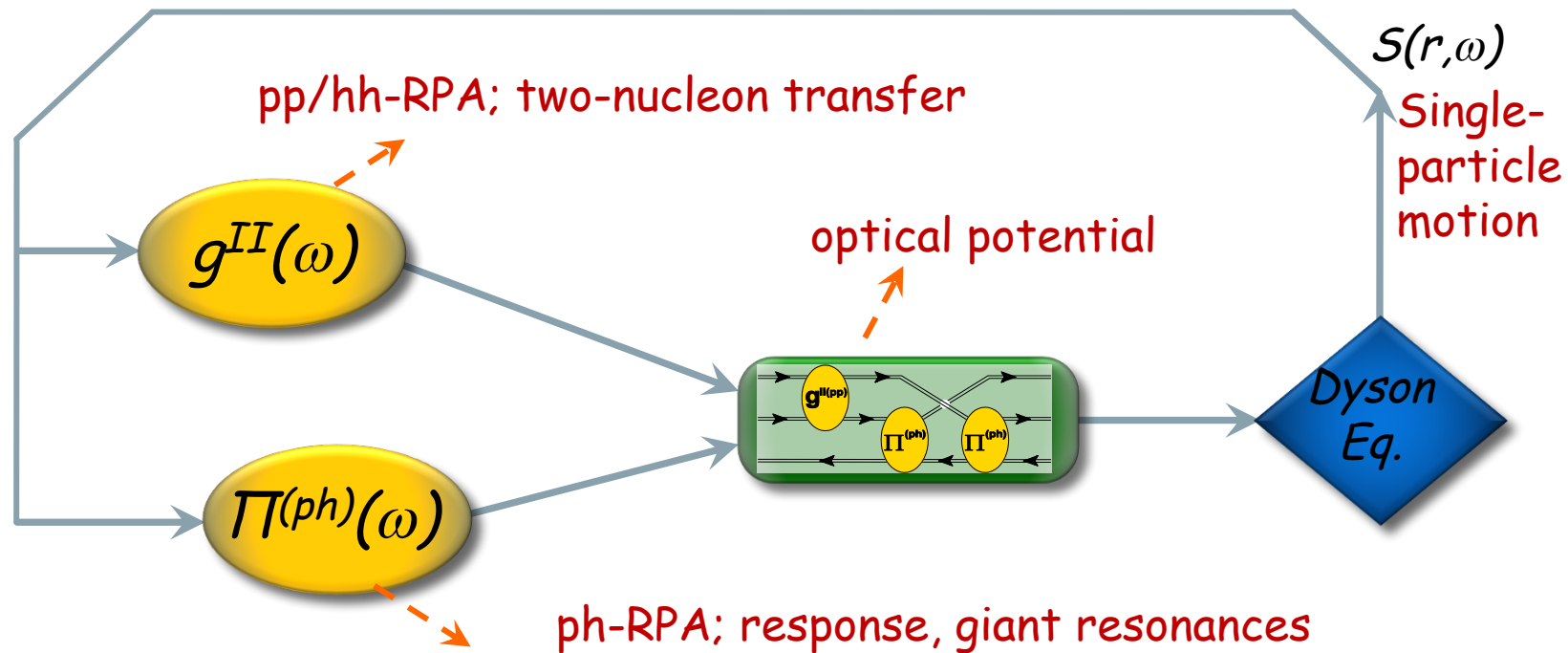
CB et al.,
 Phys. Rev. C **63**, 034313 (2001)
 Phys. Rev. A **76**, 052503 (2007)
 Phys. Rev. C **79**, 064313 (2009)



- A complete expansion requires all types of particle-vibration coupling
 ...these modes are all resummed exactly and to all orders in a *ab initio* many-body expansion.

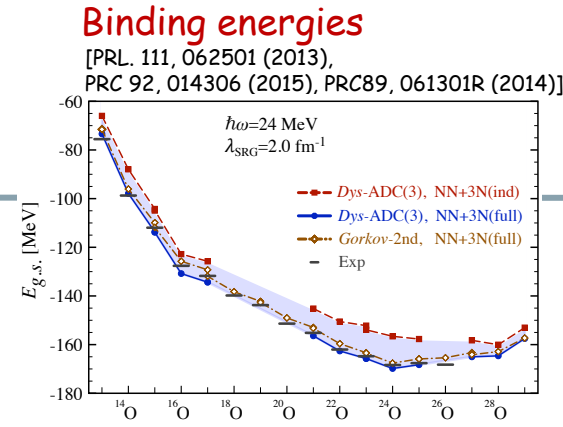
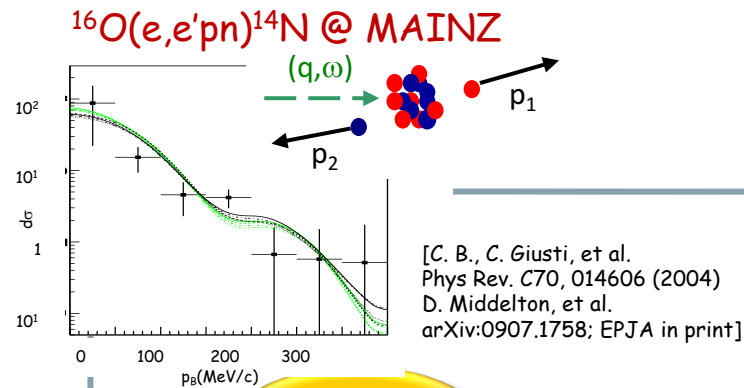
- The Self-energy $\Sigma^*(\omega)$ yields *both* single-particle states and scattering

Self-Consistent Green's Function Approach



- Global picture of nuclear dynamics
- Reciprocal correlations among effective modes
- Guaranties *macroscopic conservation laws*

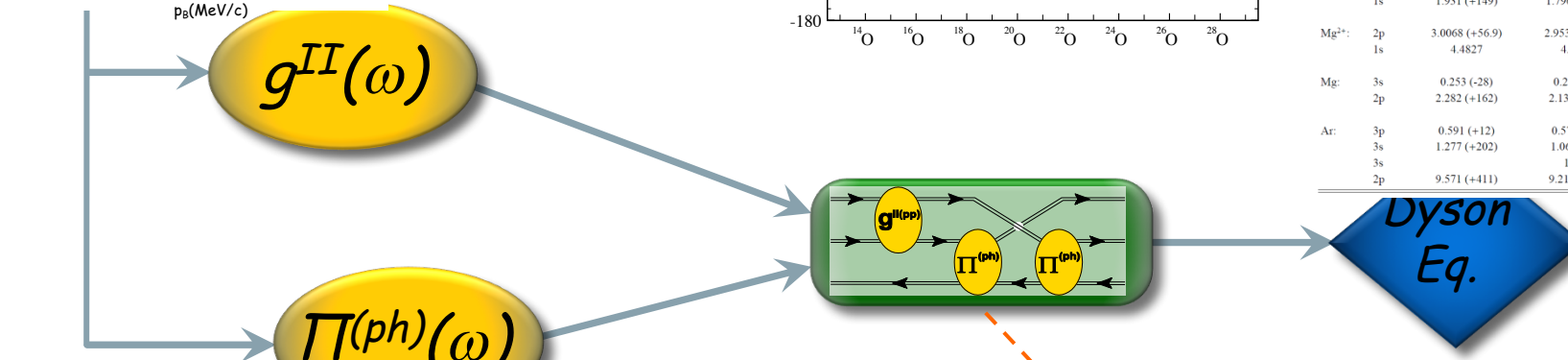
Self-Consistent Green's Function Approach



Ionization energies/affinities, in atoms

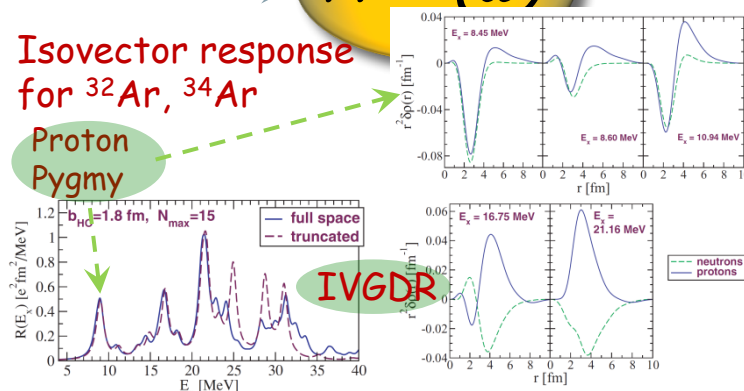
[CB, D. Van Neck,
AIP Conf. Proc. 1120, 104 ('09) & in prep]

		Hartree-Fock	FRPAc	Experiment [16, 17]
He:	1s	0.918 (+14)	0.9008 (-2.9)	0.9037
Be ²⁺ :	1s	5.6672 (+116)	5.6551 (-0.5)	5.6556
Be:	2s	0.3093 (-34)	0.3224 (-20.2)	0.3426
	1s	4.733 (+200)	4.5405 (+8)	4.533
Ne:	2p	0.852 (+57)	0.8037 (+11)	0.793
	1s	1.931 (+149)	1.7967 (+15)	1.782
Mg ²⁺ :	2p	3.0068 (+56.9)	2.9537 (+3.8)	2.9499
	1s	4.4827	4.3589	
Mg:	3s	0.253 (-28)	0.280 (-1)	0.281
	2p	2.282 (+162)	2.137 (+17)	2.12
Ar:	3p	0.591 (+12)	0.579 (±0)	0.579
	3s	1.277 (+202)	1.065 (-10)	1.075
	3s		1.544	
	2p	9.571 (+411)	9.219 (+59)	9.160



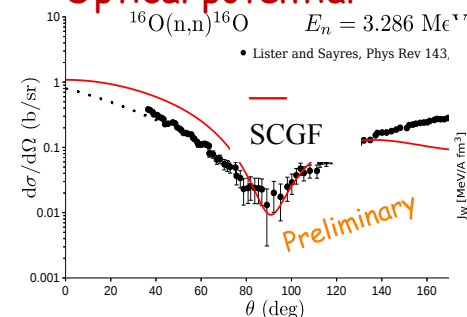
Isovector response for ^{32}Ar , ^{34}Ar

Proton
Pygmy

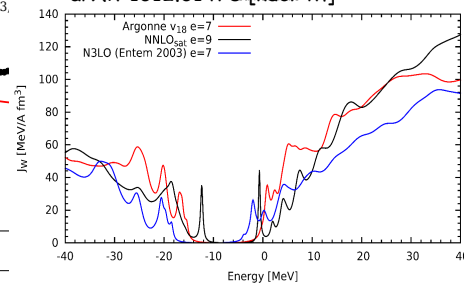


[C. B., K. Langanke, et al., Phys. Rev. C77, 024304 (2008)]

Optical potential

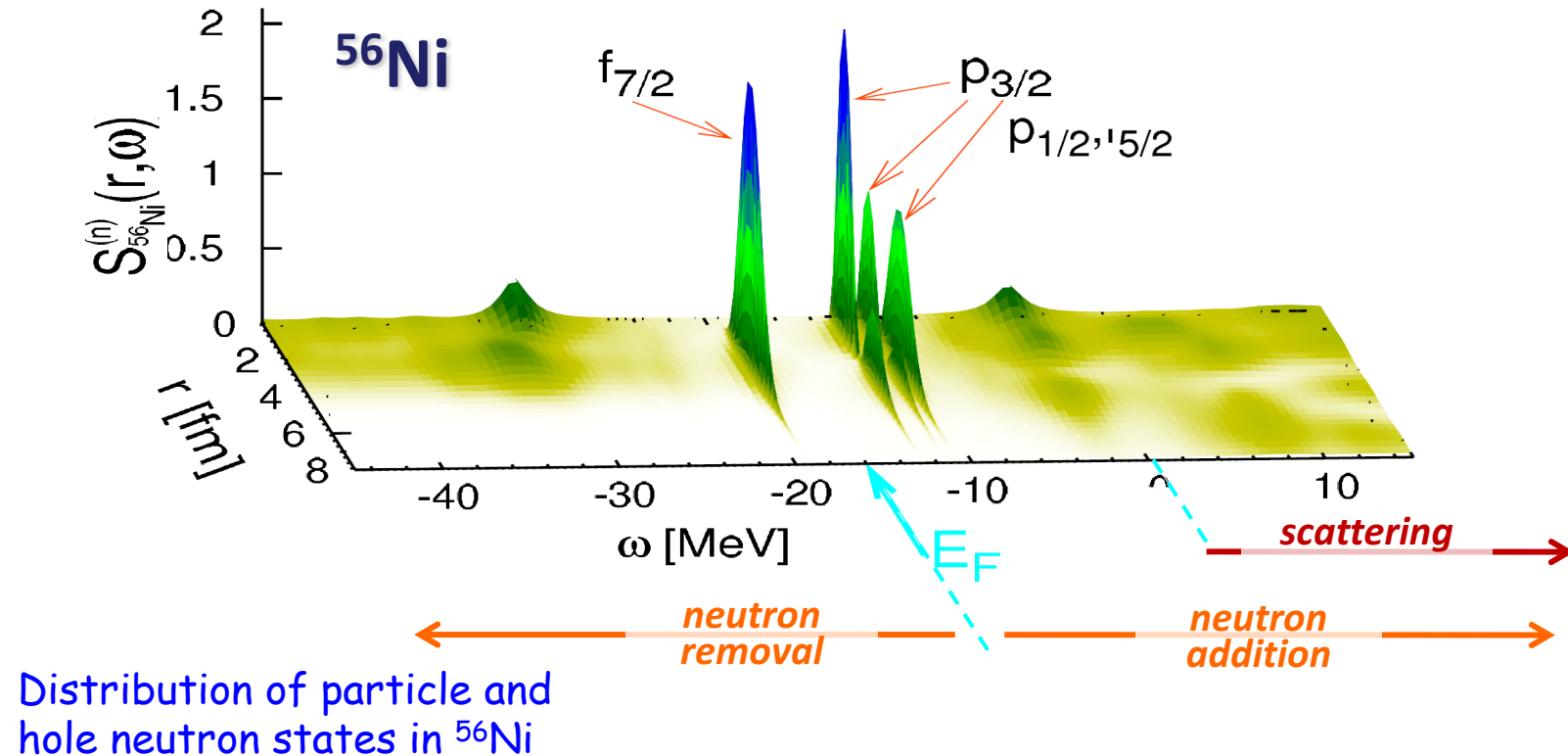


arXiv:1612.01478 [nucl-th]



One-nucleon spectral function

$$S^{p,h}(r, \omega) = \mp \frac{1}{\pi} \text{Im} g(r = r'; \omega)$$



W. Dickhoff, CB, Prog. Part. Nucl. Phys. 53, 377 (2004)
CB, M.Hjorth-Jensen, Pys. Rev. C79, 064313 (2009)

Reach of *ab initio* methods across the nuclear chart

Approximate approaches for closed-shell nuclei

- Since 2000's
- SCGF, CC, IMSRG
- Polynomial scaling

Approximate approaches for open-shells

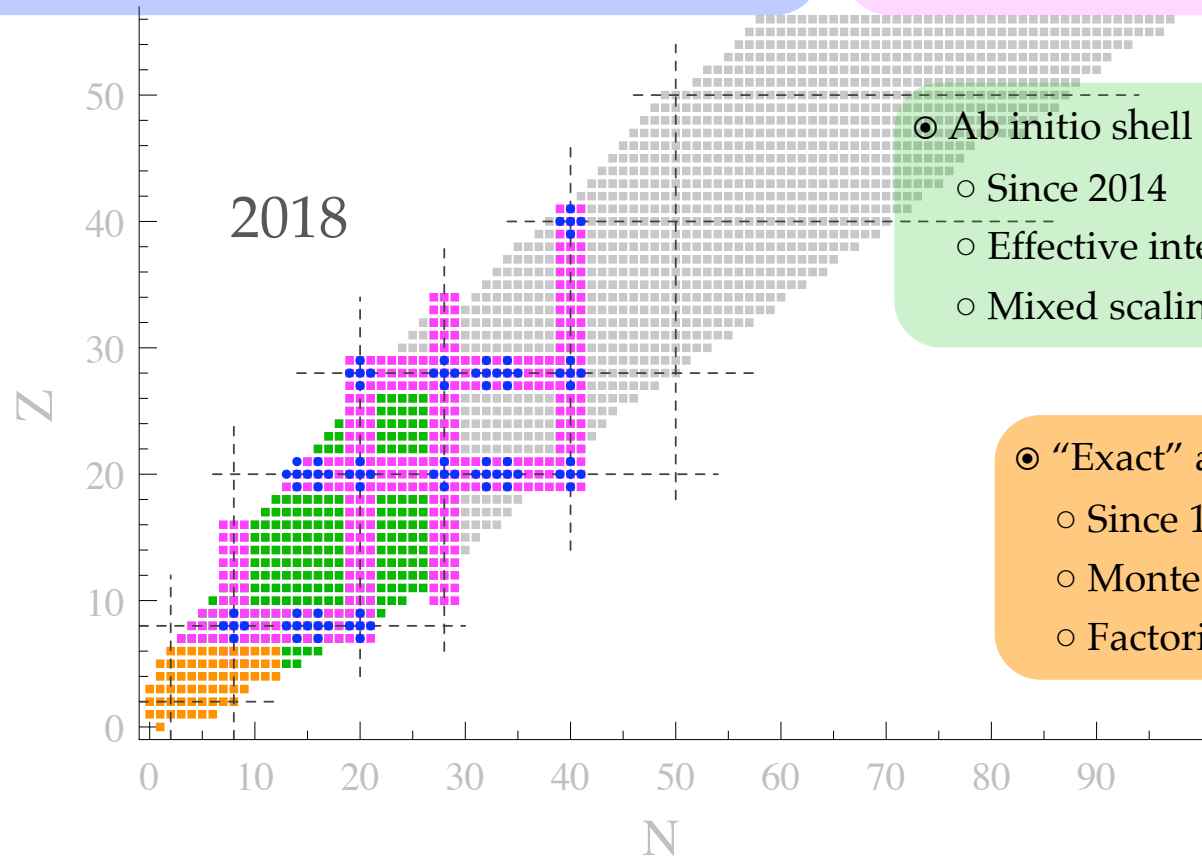
- Since 2010's
- GGF, BCC, MR-IMSRG
- Polynomial scaling

Ab initio shell model

- Since 2014
- Effective interaction via CC/IMSRG
- Mixed scaling

"Exact" approaches

- Since 1980's
- Monte Carlo, CI, ...
- Factorial scaling



Chiral EFT interactions
and
3-nucleon forces

in mid-mass isotopes

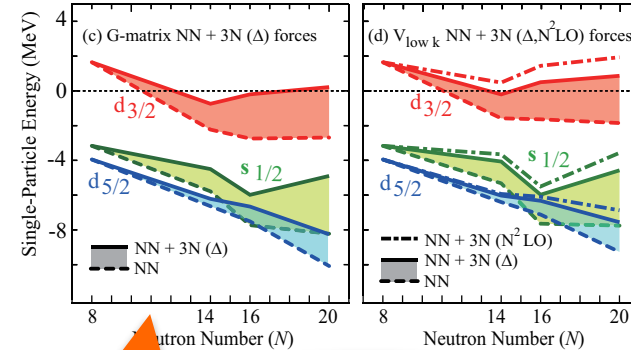
Realistic nuclear forces form Chiral EFT

Chiral EFT for nuclear forces:

	2N forces	3N forces	4N forces
LO $\mathcal{O}\left(\frac{Q^0}{\Lambda^0}\right)$			
NLO $\mathcal{O}\left(\frac{Q^2}{\Lambda^2}\right)$			
N ² LO $\mathcal{O}\left(\frac{Q^3}{\Lambda^3}\right)$			
N ³ LO $\mathcal{O}\left(\frac{Q^4}{\Lambda^4}\right)$			

(3NFs arise naturally at N2LO)

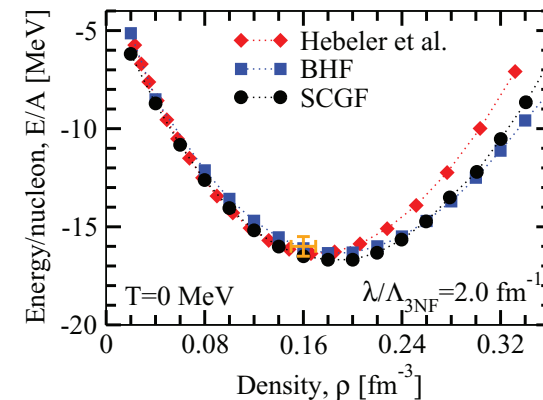
Single particle spectrum at E_{fermi} :



[T. Otsuka et al.,
Phys. Rev. Lett. **105**,
032501 (2010)]

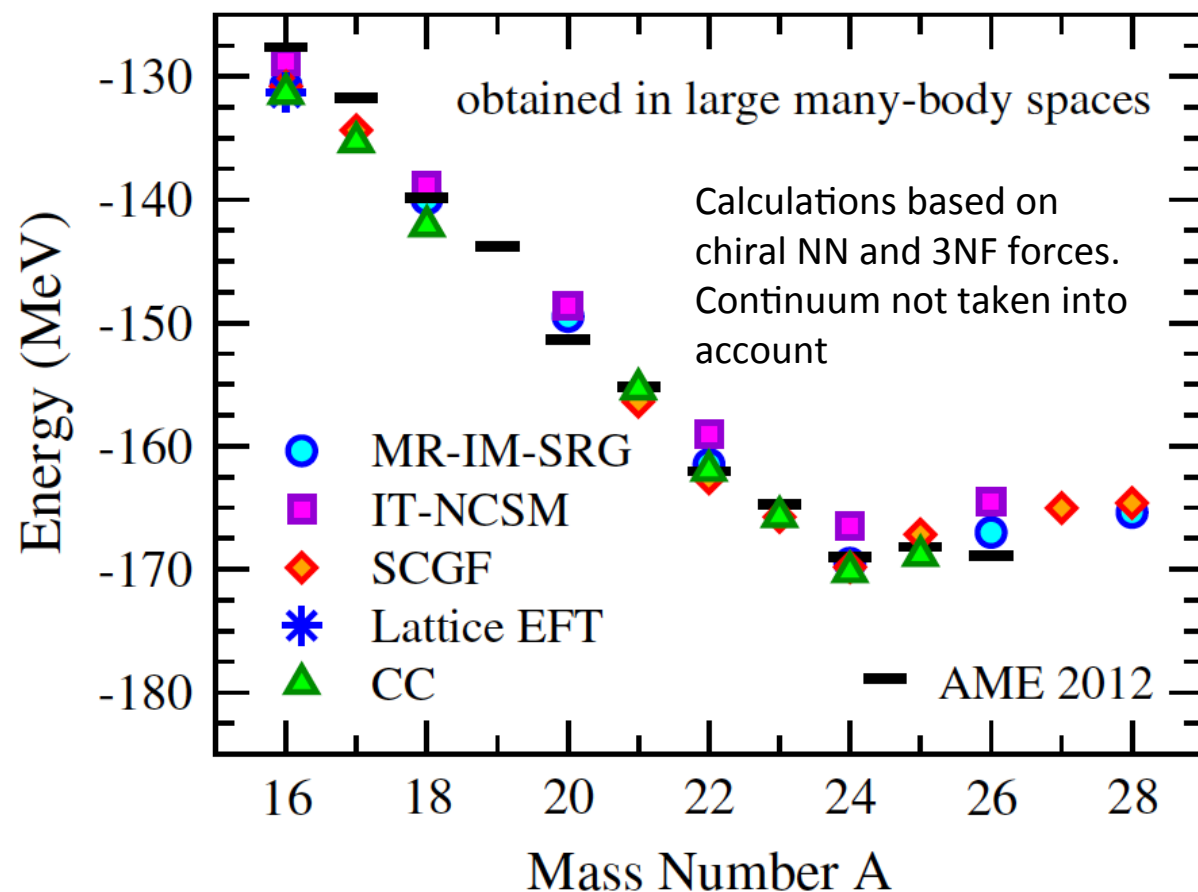
Need at LEAST 3NF!!!
("cannot" do RNB physics without...)

Saturation of nuclear matter:



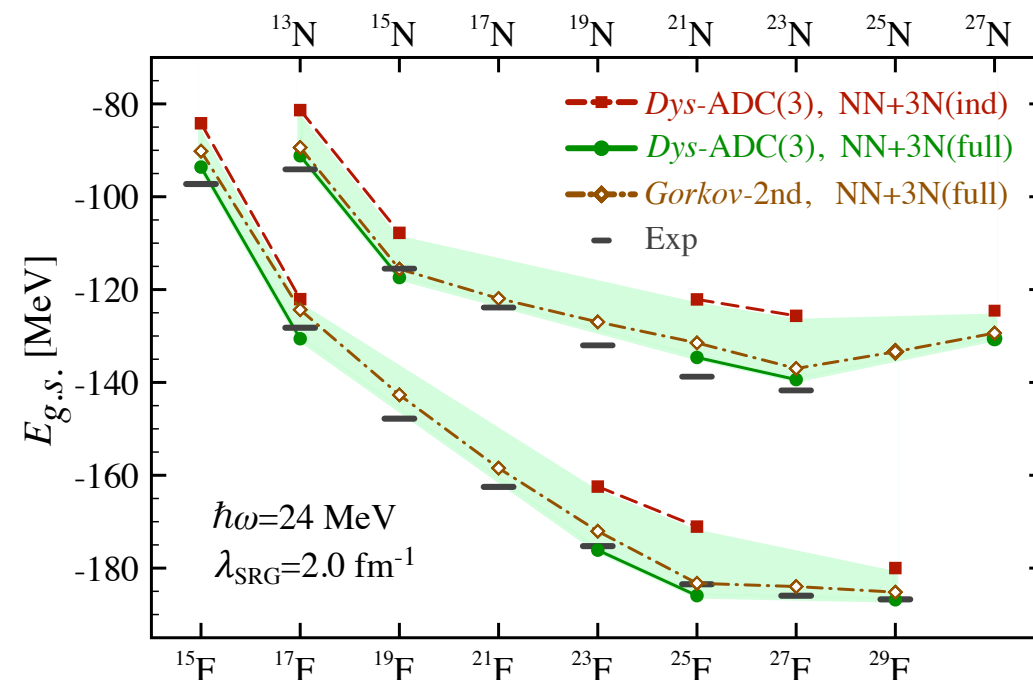
[A. Carbone et al.,
Phys. Rev. C **88**, 044302 (2013)]

Benchmark of *ab-initio* methods in the oxygen isotopic chain



Hebeler, Holt, Menendez, Schwenk, Ann. Rev. Nucl. Part. Sci. in press (2015)

A. Cipollone, CB, P. Navrátil, Phys. Rev. Lett. **111**, 062501 (2013)
and Phys. Rev. C **92**, 014306 (2015)



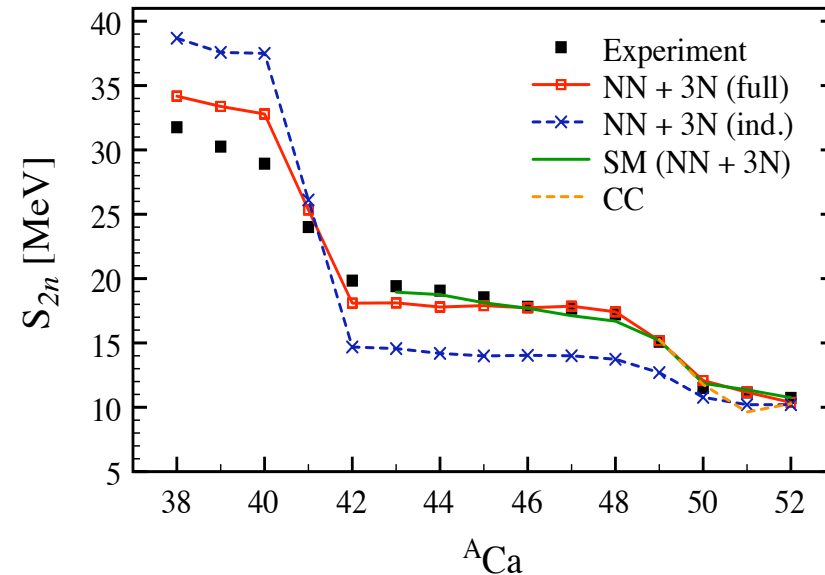
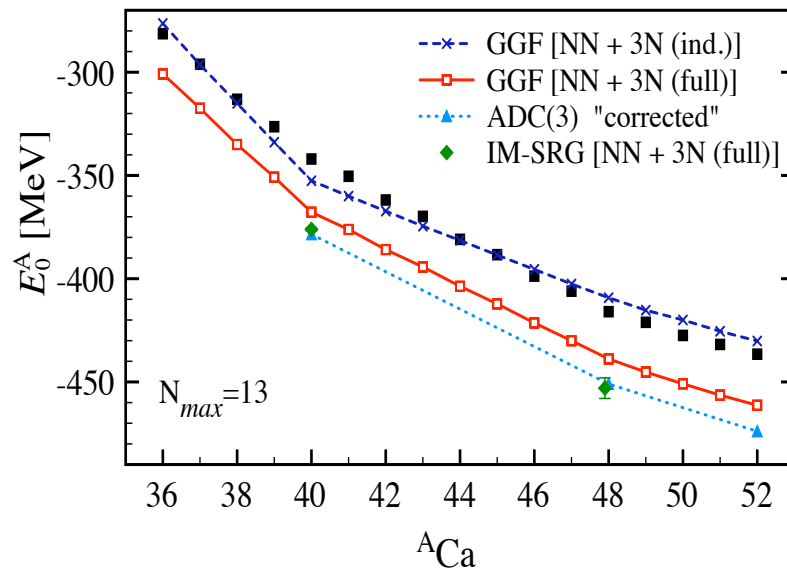
→ 3NF tensor and 3NF near fluorine's dripline

N3LO ($\Lambda = 500$ MeV/c) chiral NN interaction evolved to 2N + 3N forces (2.0 fm $^{-1}$)

N2LO ($\Lambda = 400$ MeV/c) chiral 3N interaction evolved (2.0 fm $^{-1}$)

Calcium isotopic chain

Ab-initio calculation of the whole Ca: *induced* and *full* 3NF investigated



- *induced* and *full* 3NF investigated
- *genuine* (N2LO) 3NF needed to reproduce the energy curvature and S_{2n}
- N=20 and Z=20 gaps *overestimated!*
- Full 3NF give a *correct trend* but *over bind!*



Radii and Binding Energies in Oxygen Isotopes: A Challenge for Nuclear Forces

V. Lapoux,^{1,*} V. Somà,¹ C. Barbieri,² H. Hergert,³ J. D. Holt,⁴ and S. R. Stroberg⁴

- New fits of chiral interactions (NNLO_{sat}) highly improve comparison to data

- Deficiencies remain for neutron rich isotopes

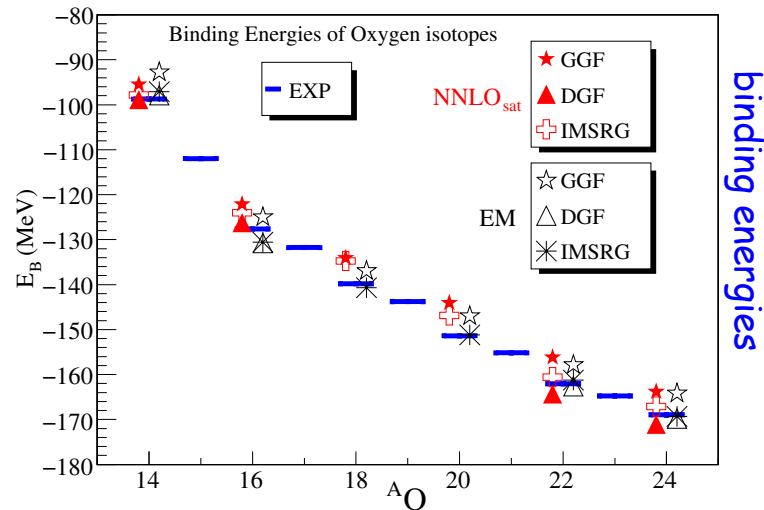
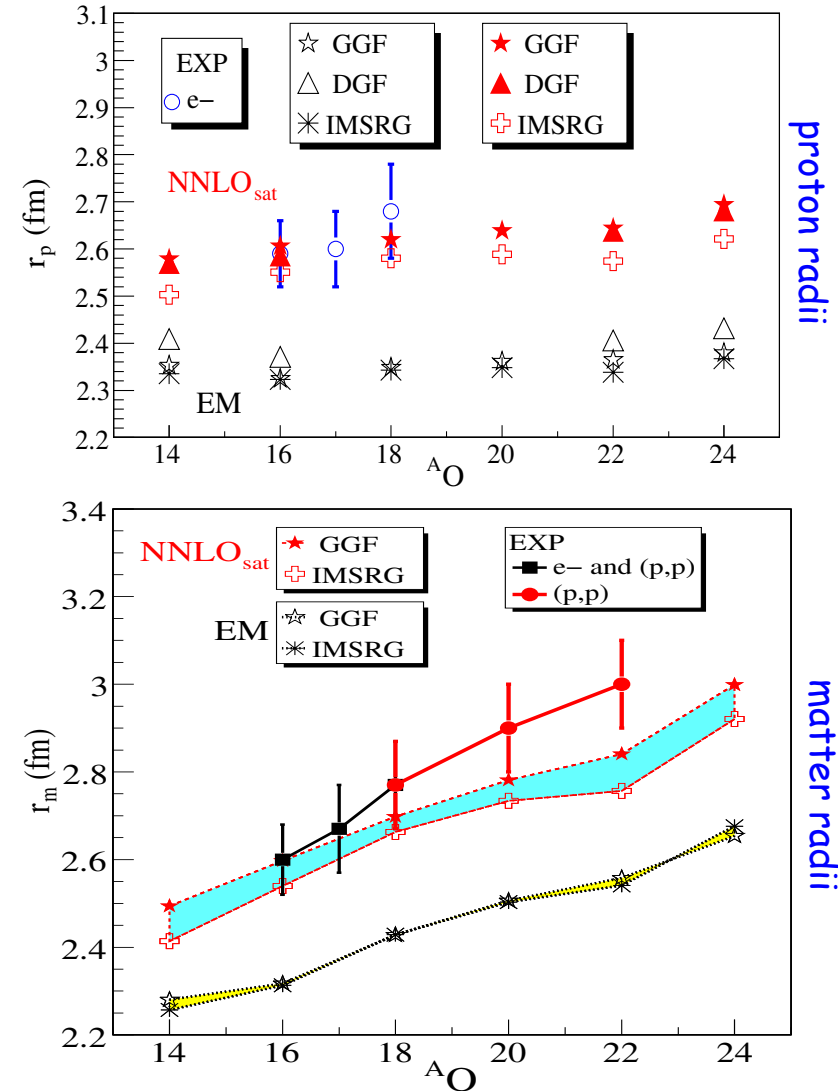
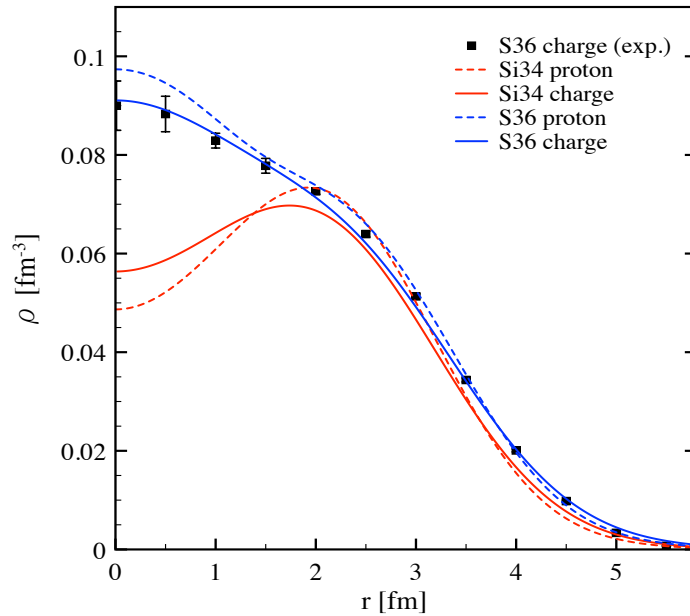


FIG. 1. Oxygen binding energies. Results from SCGF and IMSRG calculations performed with EM [20–22] and NNLO_{sat} [26] interactions are displayed along with available experimental data.



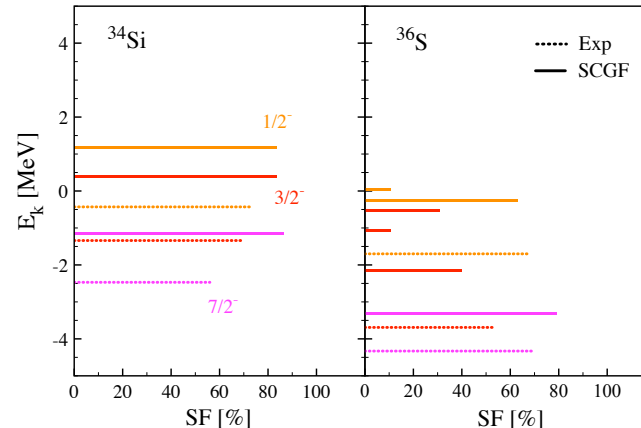
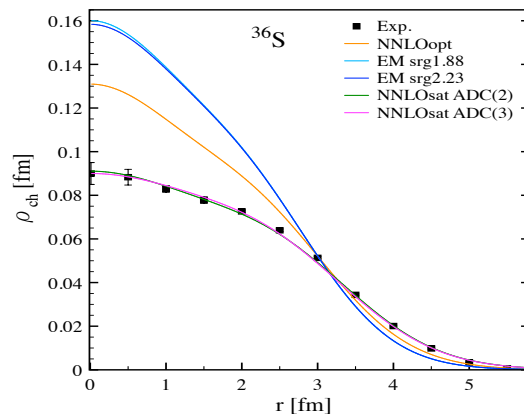
Bubble nuclei... ^{34}Si prediction



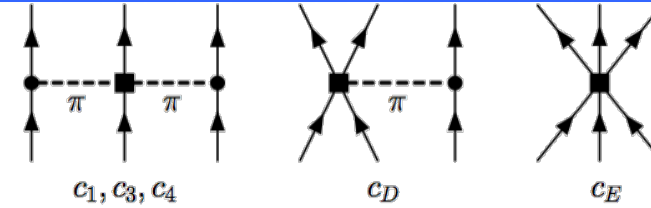
Duguet, Somà, Lecuse, CB, Navrátil,
Phys.Rev. **C95**, 034319 (2017)

- ^{34}Si is unstable, charge distribution is still unknown
- Suggested central depletion from mean-field simulations
- *Ab-initio* theory confirms predictions
- Other theoretical and experimental evidence:
Phys. Rev. **C 79**, 034318 (2009),
Nature Physics **13**, 152–156 (2017).

Validated by charge distributions and neutron quasiparticle spectra:



- Local: chiral N³LO NN+ N²LO 3N500
 - $c_D = -0.2$ $c_E = -0.205$ (${}^3\text{H}$ $E_{\text{gs}} = -8.48$ MeV)
 - ${}^4\text{He}$



$$\langle H \rangle = -28.4939 \quad \langle V_{3b_2\pi} \rangle = -5.8819 \quad \langle V_{3b_D} \rangle = -0.2206 \quad \langle V_{3b_E} \rangle = 1.2665$$

- Non-local: chiral N²LO_{sat} NN+3N
 - $c_D = +0.8168$ $c_E = -0.0396$ (${}^3\text{H}$ $E_{\text{gs}} = -8.53$ MeV)
 - ${}^4\text{He}$

$$\langle H \rangle = -28.4596 \quad \langle V_{3b_2\pi} \rangle = -4.7260 \quad \langle V_{3b_D} \rangle = 1.3897 \quad \langle V_{3b_E} \rangle = 0.4174$$

- Local/Non-local: chiral N³LO NN+ N²LO

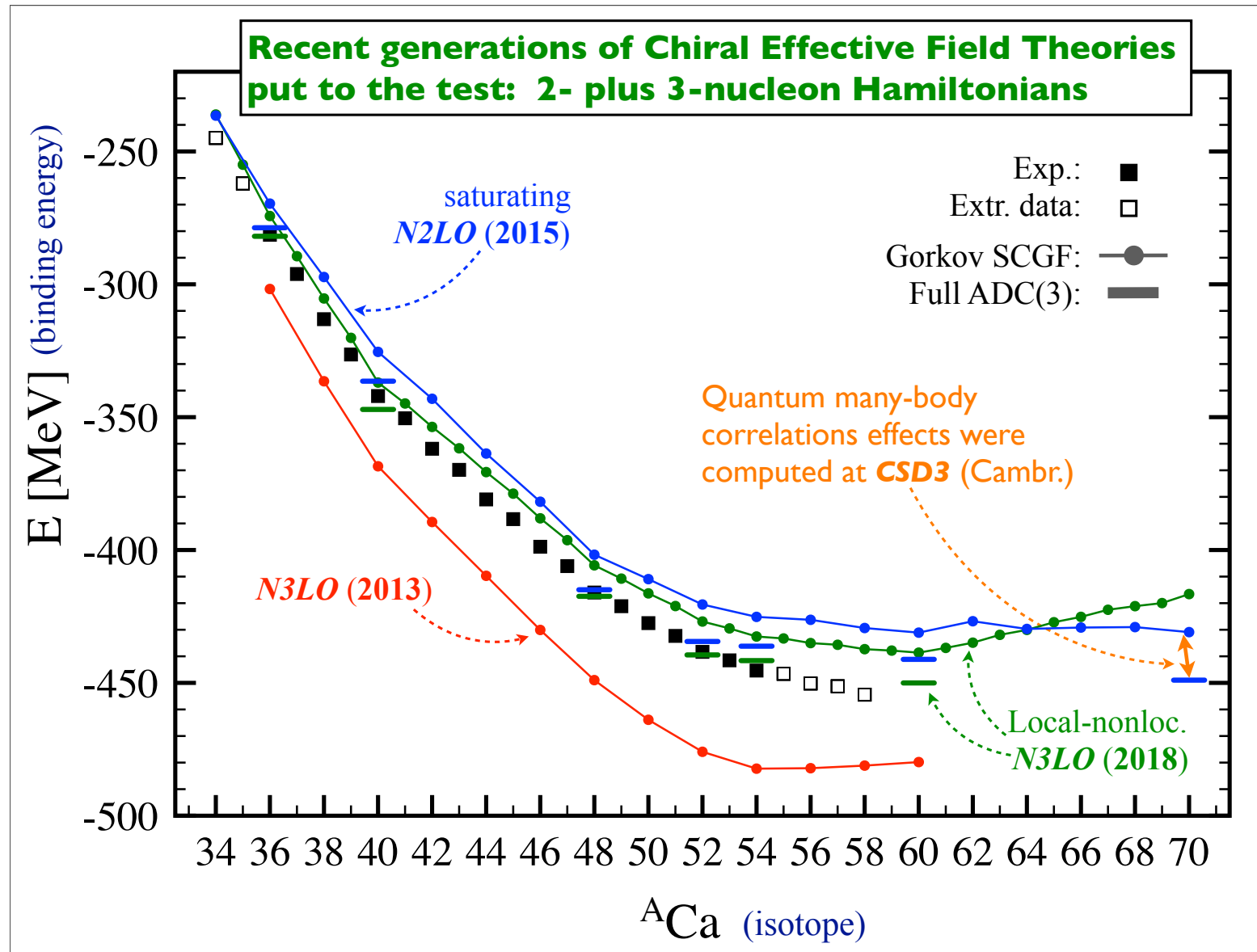
$$F\left(\frac{1}{2}(\pi_1^2 + \pi_2^2); \Lambda_{\text{nonloc}}\right) W_1^Q(\Lambda_{\text{loc}}) F\left(\frac{1}{2}(\pi_1^2 + \pi_2^2); \Lambda_{\text{nonloc}}\right)$$

Use completeness
in HO basis to calculate
products of $F W F$

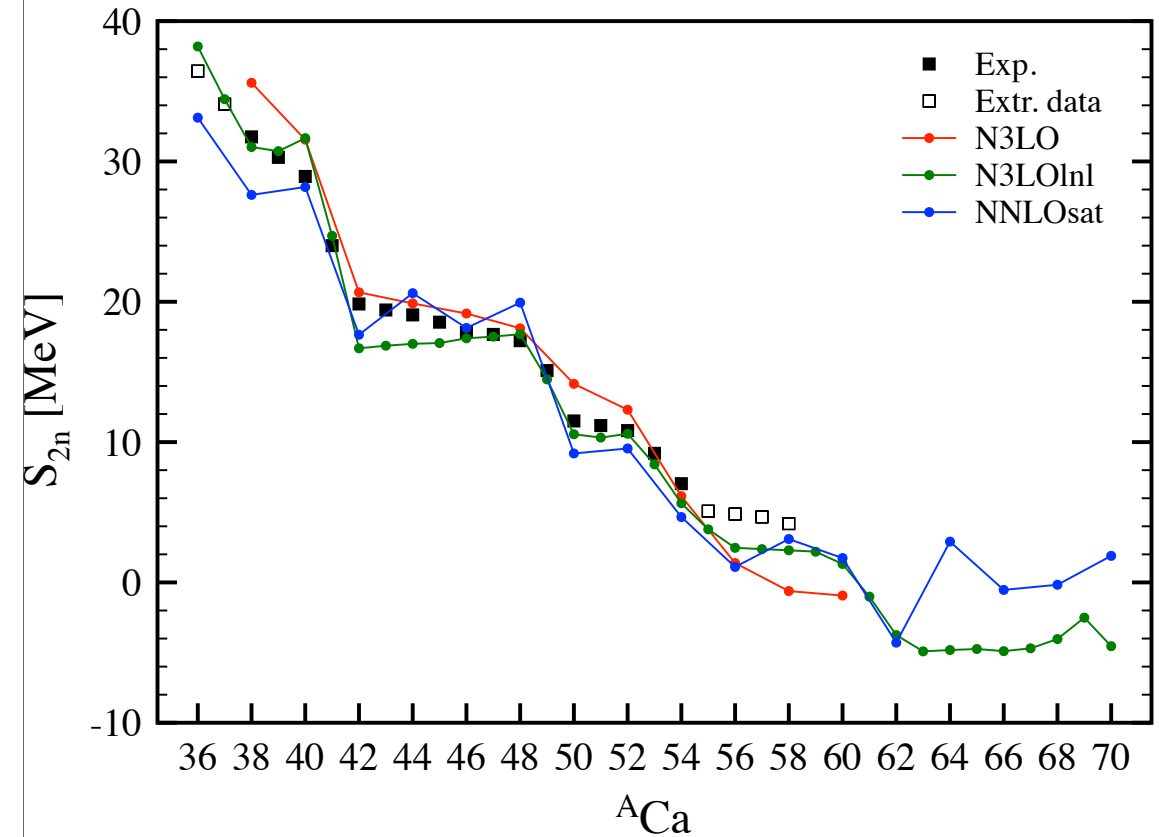
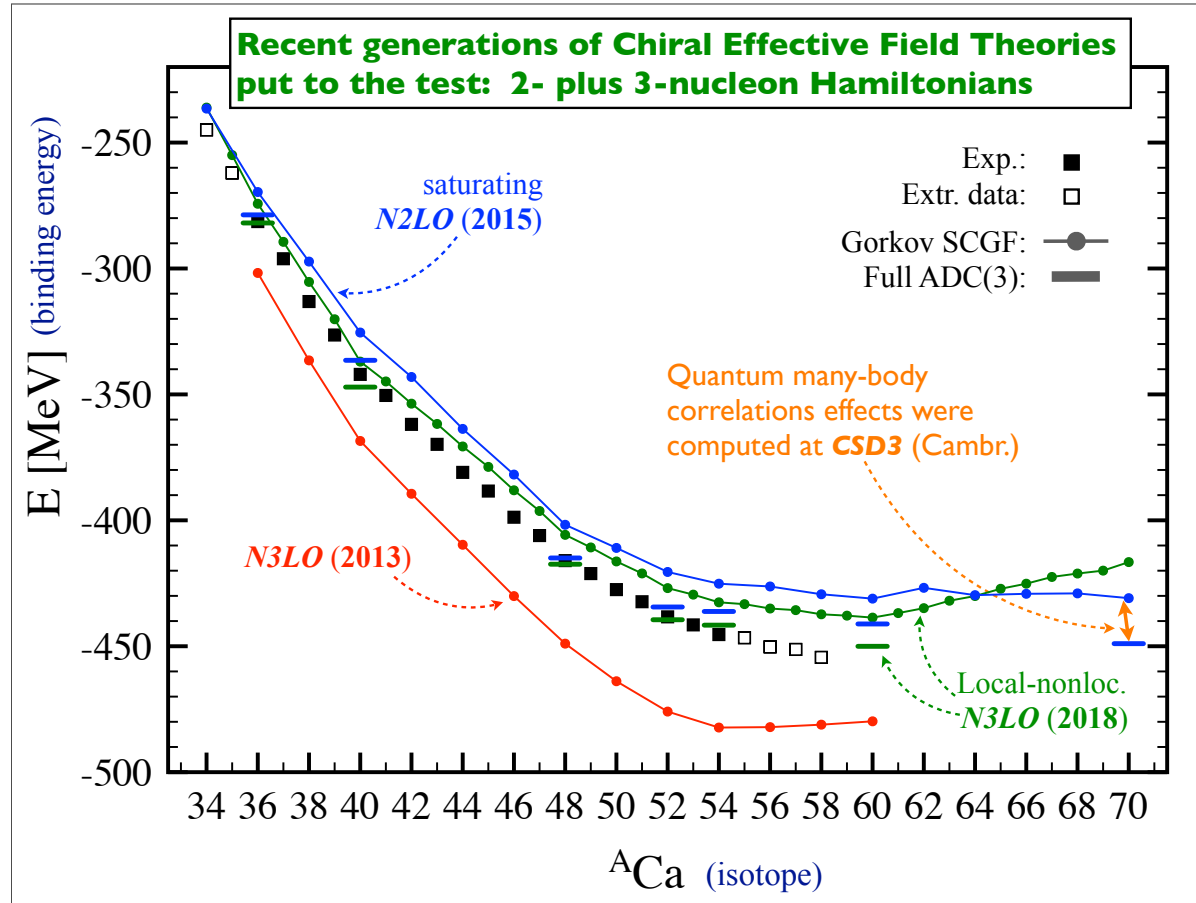
- $c_D = +0.7$ $c_E = -0.06$ (${}^3\text{H}$ $E_{\text{gs}} = -8.44$ MeV)
- ${}^4\text{He}$

$$\langle H \rangle = -28.2530 \quad \langle V_{3b_2\pi} \rangle = -4.8124 \quad \langle V_{3b_D} \rangle = 0.7414 \quad \langle V_{3b_E} \rangle = 0.4255$$

Comparison of nuclear forces - ^ACa



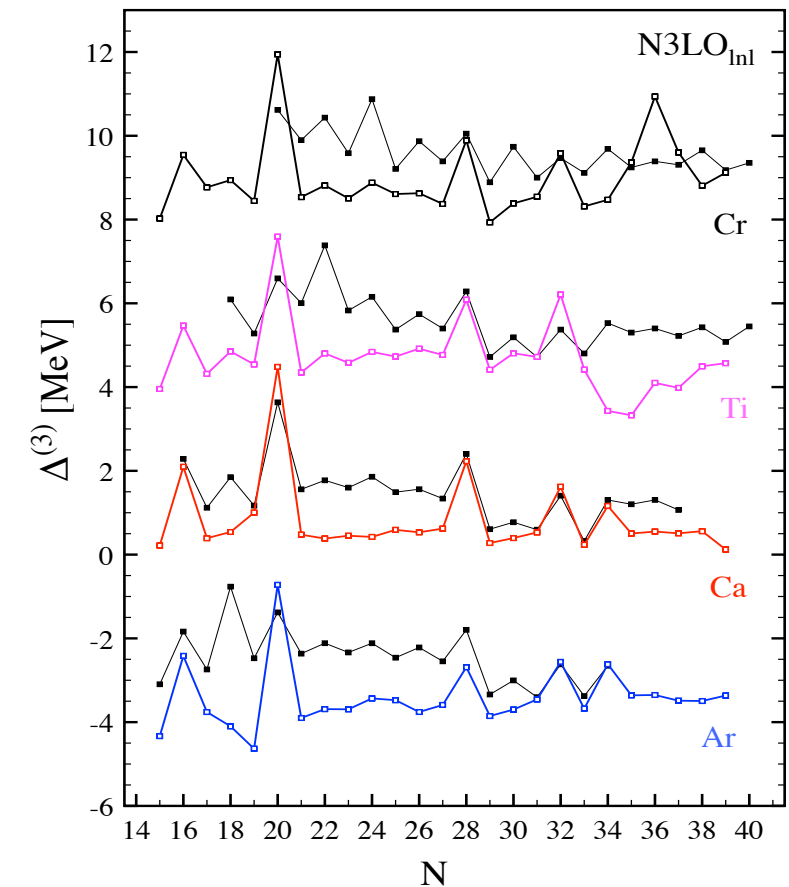
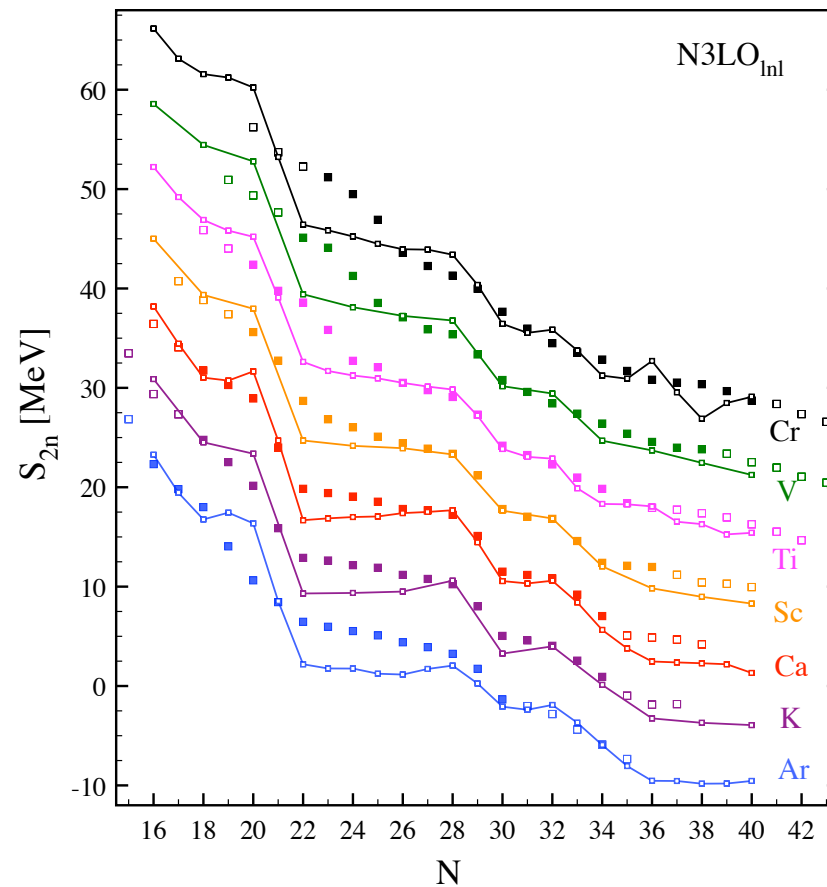
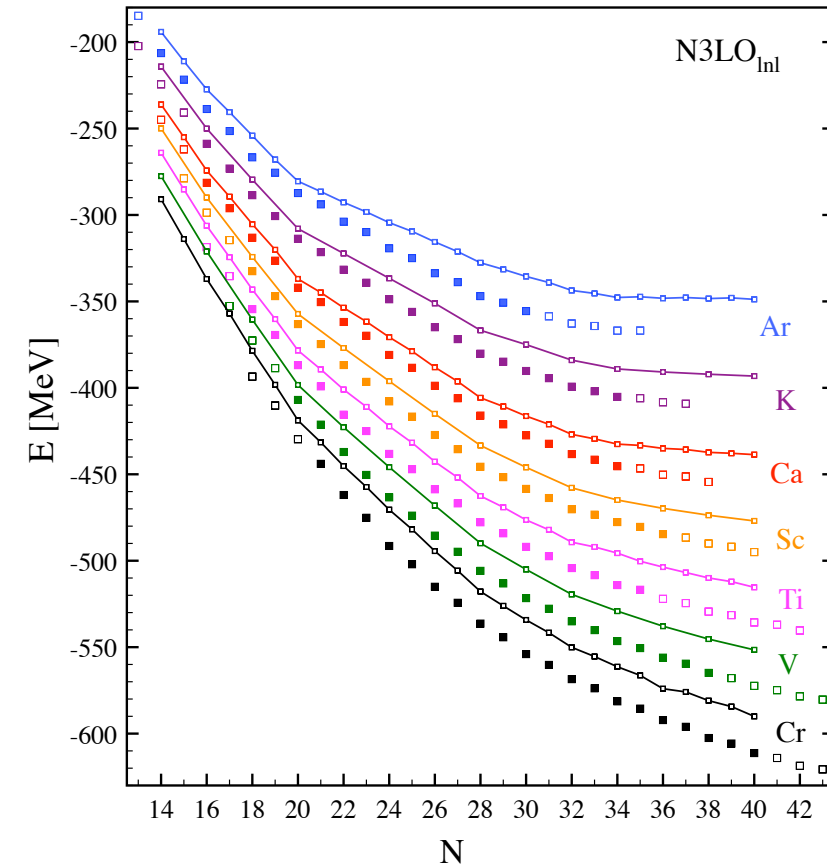
Comparison of nuclear forces - ^ACa



$N3LO(500) + nln\ 3NF$

SCGF – Gorkov-ADC(2)

PRELIMINARY



Masses in the Ti isotopic chain

- High precision measurements at TITAN (TRIUMF):
Newly developed Multiple-Reflection Time-of-Flight
Mass Spectrometer (MR-TOF-MS)
- Weak shell closure at N=32 (quenched w.r.t. ^{52}Ca)

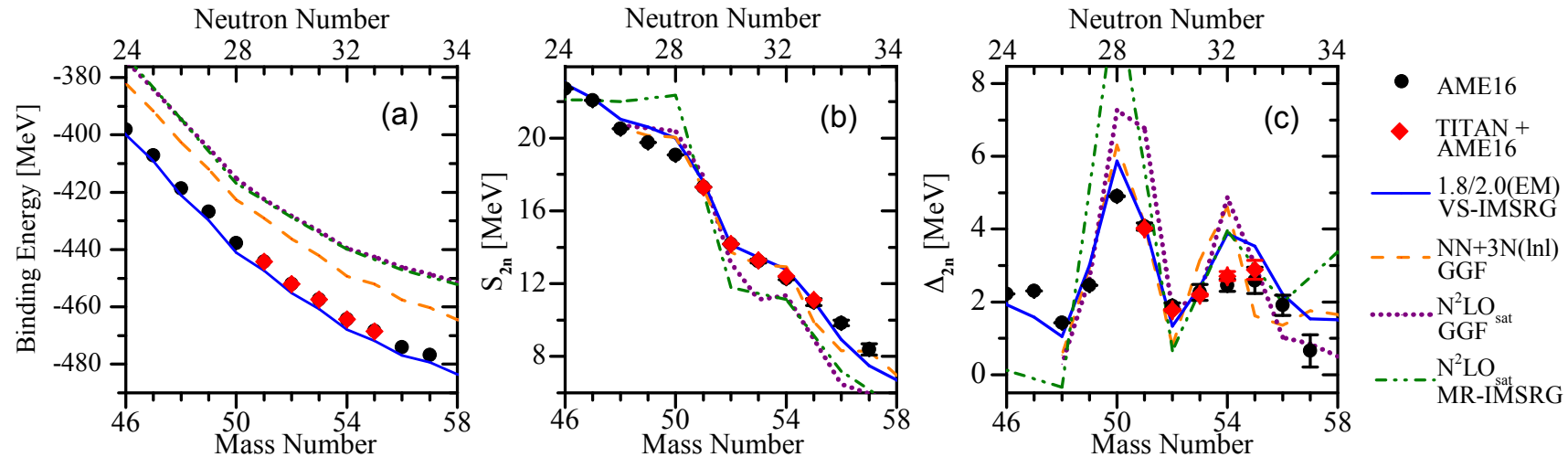


FIG. 4. The mass landscape of titanium isotopes is shown from three perspectives: (a) absolute masses (shown in binding energy format), (b) its first “derivative” as two-neutron separation energies (S_{2n}), and (c) its second “derivative” as empirical neutron-shell gaps (Δ_{2n}). Both theoretical *ab-initio* calculations (lines) and experimental values (points) are shown.

E. Leistenschneider *et al.*, *CB*, [Phy. Rev. Lett.](#), 0 (2018) – **TITAN** coll. @
TRIUMF

Electron and neutrino scattering off nuclei

N. Rocco, CB, Phys. Rev. C**98**, 025501 (2018).

N. Rocco, CB, O. Benhar, A. De Pace, A. Lovato, arXiv:1810.0wxyz (in prep)

Lepton-nucleon cross section

$$\left(\frac{d\sigma}{dT'd\cos\theta'}\right)_{\nu/\bar{\nu}} = \frac{G^2}{2\pi} \frac{k'}{2E_\nu} \left[\hat{L}_{CC}R_{CC} + 2\hat{L}_{CL}R_{CL} + \hat{L}_{LL}R_{LL} + \hat{L}_T R_T \pm 2\hat{L}_{T'}R_{T'} \right],$$

Nuclear structure is in the
hadronic tensor:

$$R_{CC} = W^{00}$$

$$R_{CL} = -\frac{1}{2}(W^{03} + W^{30})$$

$$R_{LL} = W^{33}$$

$$R_T = W^{11} + W^{22}$$

$$R_{T'} = -\frac{i}{2}(W^{12} - W^{21}),$$

$$W^{\mu\nu} = \sum_f \langle 0 | j^\mu | f \rangle \langle f | j^\nu | 0 \rangle \delta(E_0 + \omega - E_f)$$

Lepton-nucleon cross section

$$\left(\frac{d\sigma}{dT' d\cos\theta'} \right)_{\nu/\bar{\nu}} = \frac{G^2}{2\pi} \frac{k'}{2E_\nu} \left[\hat{L}_{CC} R_{CC} + 2\hat{L}_{CL} R_{CL} + \hat{L}_{LL} R_{LL} + \hat{L}_T R_T \pm 2\hat{L}_{T'} R_{T'} \right],$$

Nuclear structure is in the hadronic tensor:

Two models of the Spectral function

$$W^{\mu\nu}(\mathbf{q}, \omega) = \int \frac{d^3k}{(2\pi)^3} dE P_h(\mathbf{k}, E) \frac{m^2}{e(\mathbf{k})e(\mathbf{k}+\mathbf{q})} \\ \times \sum_i \langle k | j_i^{\mu\dagger} | k+q \rangle \langle k+q | j_i^\nu | k \rangle \\ \times \delta(\omega + E - e(\mathbf{k} + \mathbf{q})),$$

$$P_h(\mathbf{k}, E) = \frac{1}{\pi} \sum_{\alpha\beta} \tilde{\Phi}_\beta^*(\mathbf{k}) \tilde{\Phi}_\alpha(\mathbf{k}) \\ \times \text{Im} \langle \psi_0^A | a_\beta^\dagger \frac{1}{E + (H - E_0^A) - i\epsilon} a_\alpha | \psi_0^A \rangle$$

SCGF/ADC(3)
using chiral NNLOsat

$$W_{2b}^{\mu\nu}(\mathbf{q}, \omega) = \frac{V}{2} \int d\tilde{E} \frac{d^3k}{(2\pi)^3} d\tilde{E}' \frac{d^3k'}{(2\pi)^3} \frac{d^3p}{(2\pi)^3} \\ \times \frac{m^4}{e(\mathbf{k})e(\mathbf{k}')e(\mathbf{p})e(\mathbf{p}')} P_h^{\text{NM}}(\mathbf{k}, \tilde{E}) P_h^{\text{NM}}(\mathbf{k}', \tilde{E}') \\ \times \sum_{ij} \langle k k' | j_{ij}^{\mu\dagger} | p p' \rangle \langle p p' | j_{ij}^\nu | k k' \rangle \\ \times \delta(\omega + \tilde{E} + \tilde{E}' - e(\mathbf{p}) - e(\mathbf{p}')). \quad (41)$$

$$P_h(\mathbf{k}, E) = P_h^{1h}(\mathbf{k}, E) + P_h^{\text{corr}}(\mathbf{k}, E).$$

$$P_h^{1h}(\mathbf{k}, E) = \sum_{\alpha \in \{\text{F}\}} Z_\alpha |\phi_\alpha(\mathbf{k})|^2 F_\alpha(E - e_\alpha)$$

CBF using AV18+UIX
(see Benhar's talk)

$$P_h^{\text{corr}}(\mathbf{k}, E) = \int d^3R \rho_A(\mathbf{R}) P_{h, \text{NM}}^{\text{corr}}(\mathbf{k}, E; \rho_A(\mathbf{R}))$$

Lepton-nucleon cross section

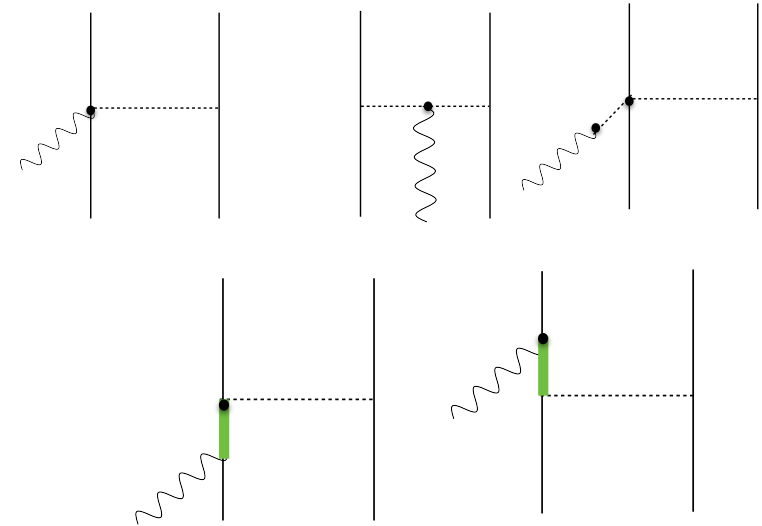
$$\left(\frac{d\sigma}{dT' d\cos\theta'} \right)_{\nu/\bar{\nu}} = \frac{G^2}{2\pi} \frac{k'}{2E_\nu} \left[\hat{L}_{CC} R_{CC} + 2\hat{L}_{CL} R_{CL} + \hat{L}_{LL} R_{LL} + \hat{L}_T R_T \pm 2\hat{L}_{T'} R_{T'} \right],$$

Nuclear structure is in the hadronic tensor:

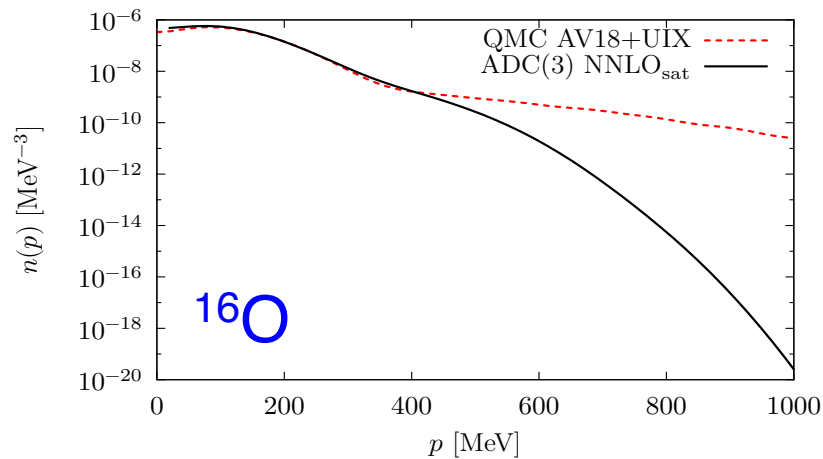
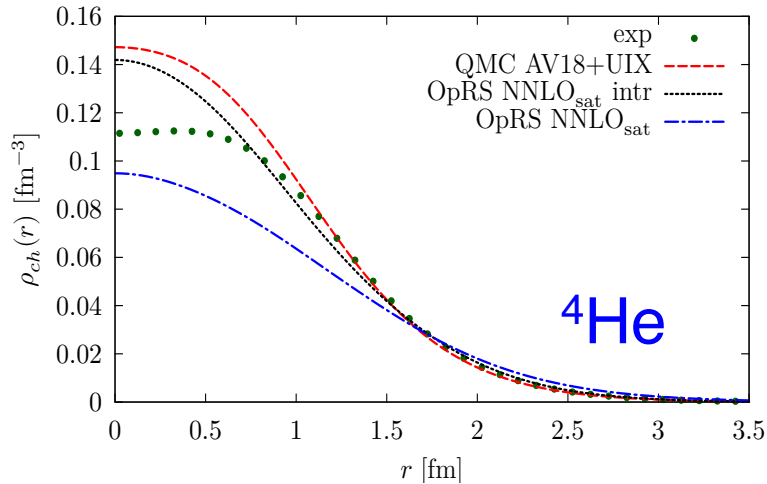
- Two-body diagrams contributing to the axial and vector responses

$$W^{\mu\nu}(\mathbf{q}, \omega) = \int \frac{d^3k}{(2\pi)^3} dE P_h(\mathbf{k}, E) \frac{m^2}{e(\mathbf{k})e(\mathbf{k}+\mathbf{q})} \\ \times \sum_i \langle k | j_i^{\mu\dagger} | k+q \rangle \langle k+q | j_i^\nu | k \rangle \\ \times \delta(\omega + E - e(\mathbf{k}+\mathbf{q})),$$

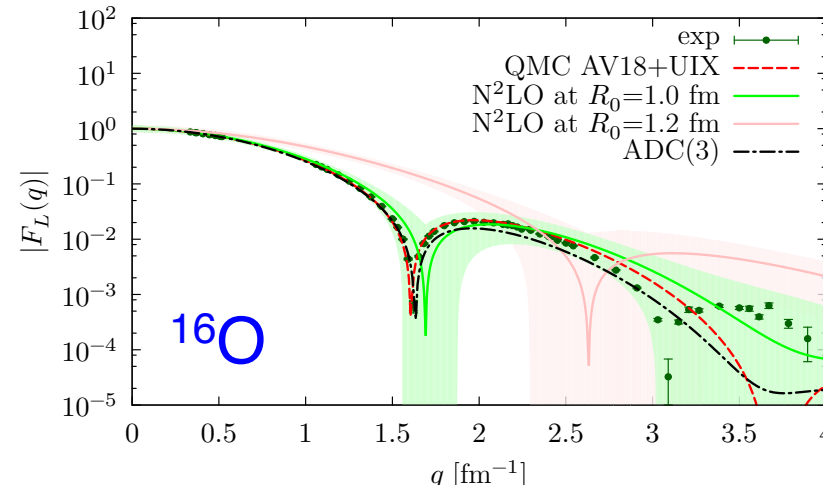
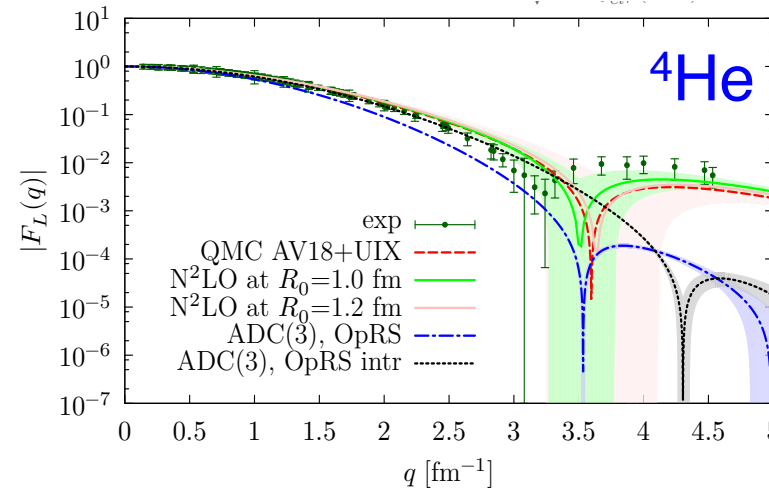
$$W_{2b}^{\mu\nu}(\mathbf{q}, \omega) = \frac{V}{2} \int d\tilde{E} \frac{d^3k}{(2\pi)^3} d\tilde{E}' \frac{d^3k'}{(2\pi)^3} \frac{d^3p}{(2\pi)^3} \\ \times \frac{m^4}{e(\mathbf{k})e(\mathbf{k}')e(\mathbf{p})e(\mathbf{p}')} P_h^{\text{NM}}(\mathbf{k}, \tilde{E}) P_h^{\text{NM}}(\mathbf{k}', \tilde{E}') \\ \times \sum_{ij} \langle k k' | j_{ij}^{\mu\dagger} | p p' \rangle \langle p p' | j_{ij}^\nu | k k' \rangle \\ \times \delta(\omega + \tilde{E} + \tilde{E}' - e(\mathbf{p}) - e(\mathbf{p}')). \quad (41)$$



Prediction for chrg./mom. distributions and form factors



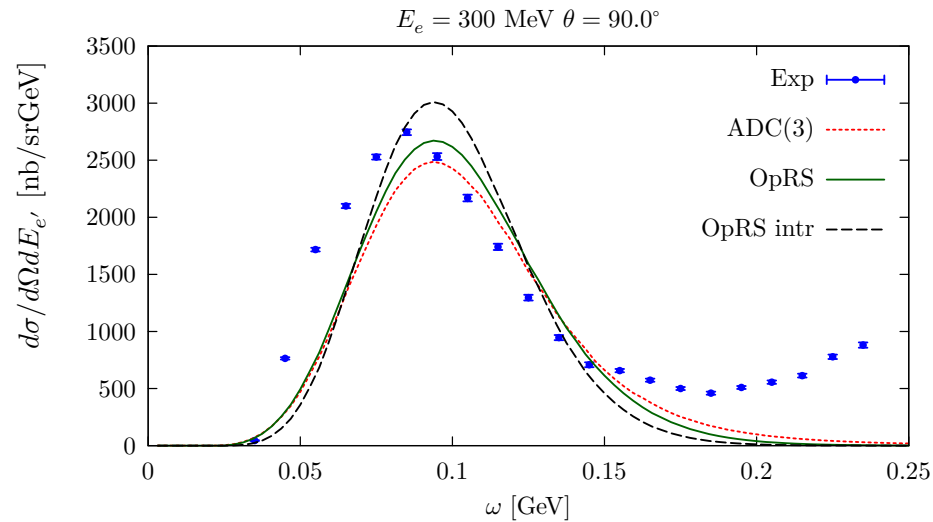
$$F_L(\mathbf{q}) = \frac{1}{Z} \frac{G_E^p(Q_{el}^2) \tilde{\rho}_p(q) + G_E^n(Q_{el}^2) \tilde{\rho}_n(q)}{\sqrt{1 + Q_{el}^2/(4m^2)}}$$



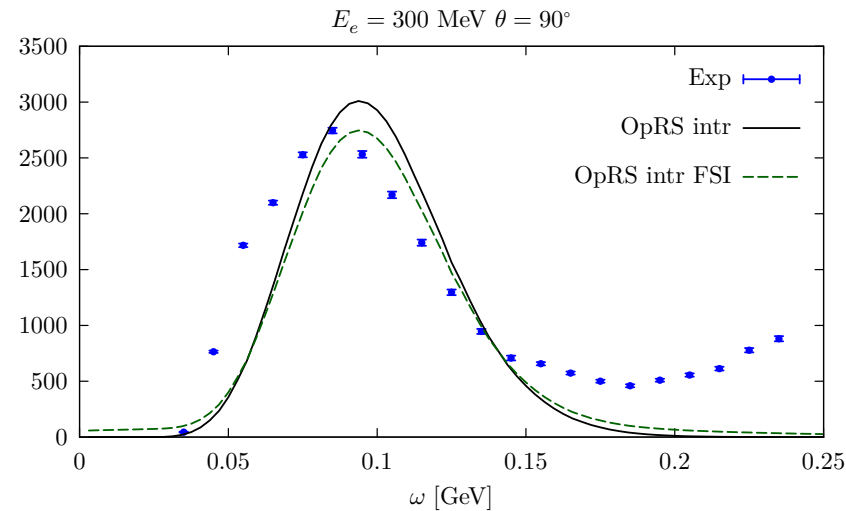
- Calculations from the spectral functions obtained using SCGF
- Based on the saturating chiral N2LO-sat nuclear force
- Comparison to QMC calculations based on **local chiral forces** and/or **AV18+UIX** [PRC96, 024326 ('17), PRC96, 054007 ('17), PRC97, 044318 ('18)]

$^4\text{He}-e^-$ cross sections from the SCGF Spect. Fnct.

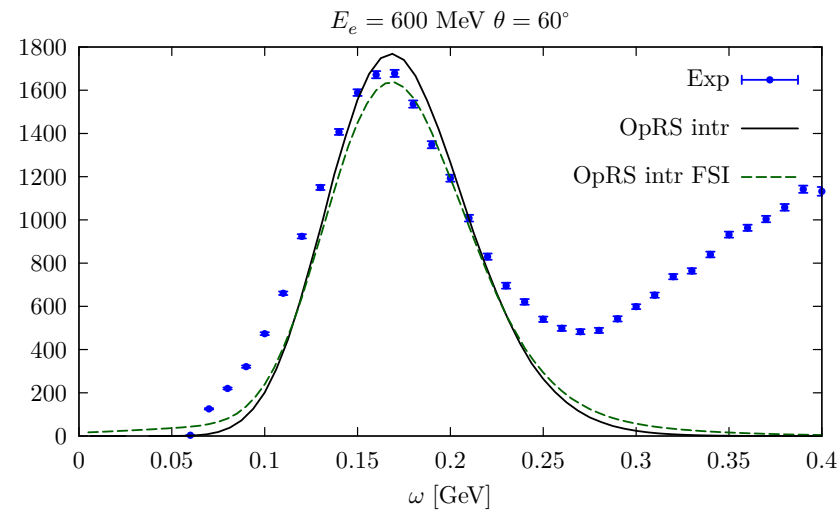
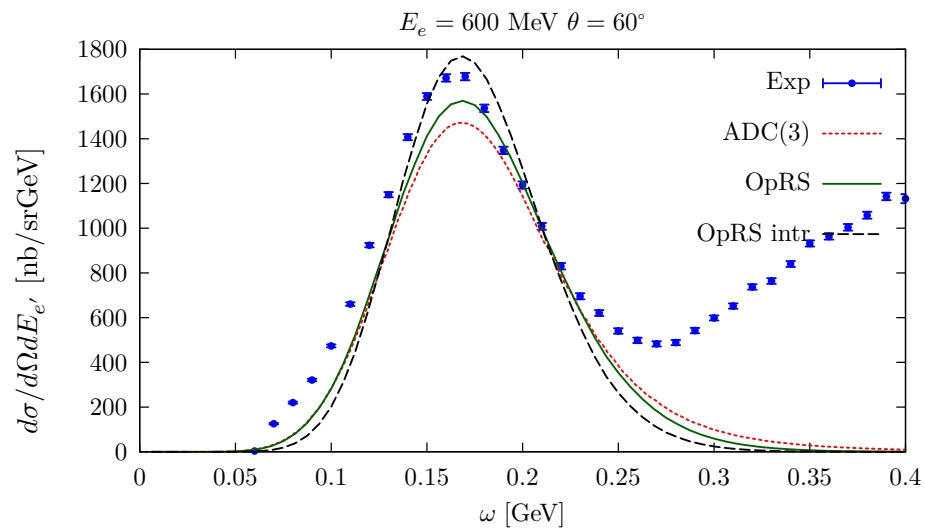
PW Impulse approximation:



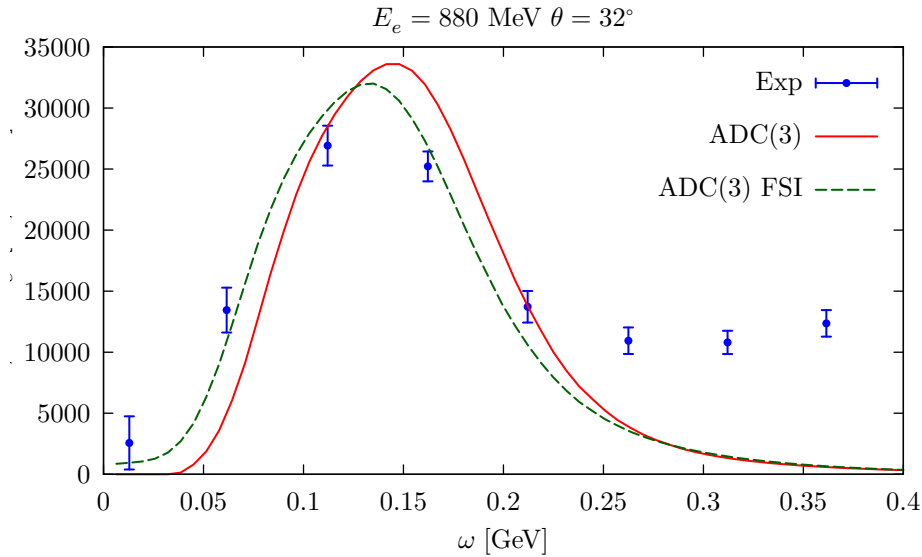
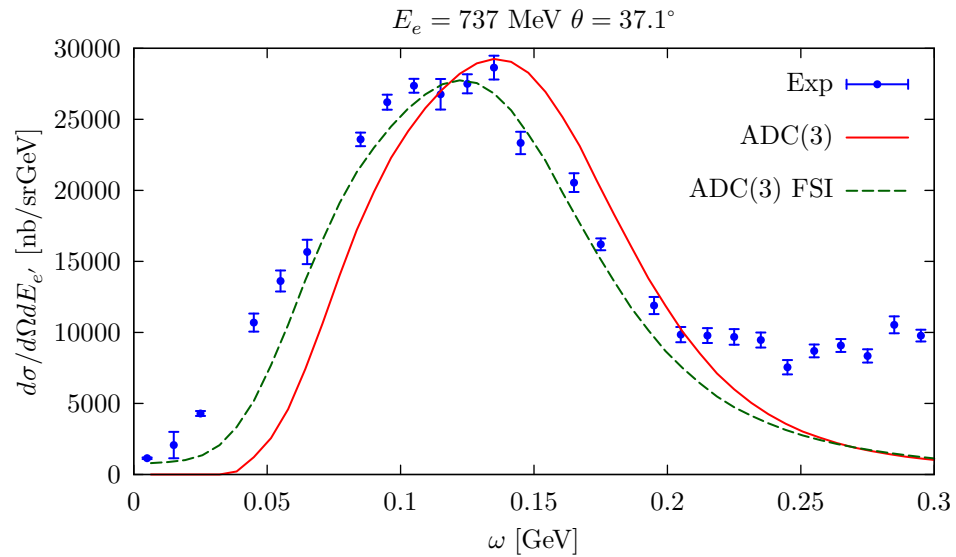
Adding FSI:



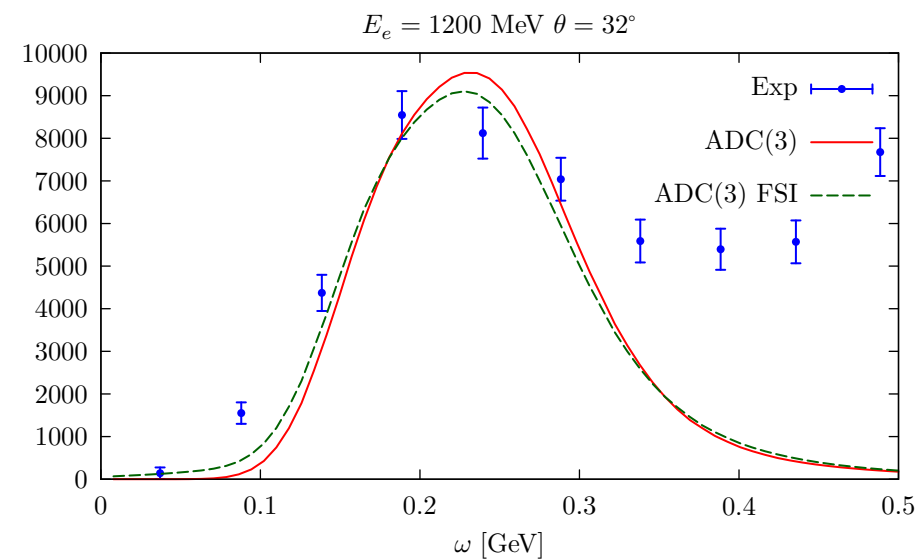
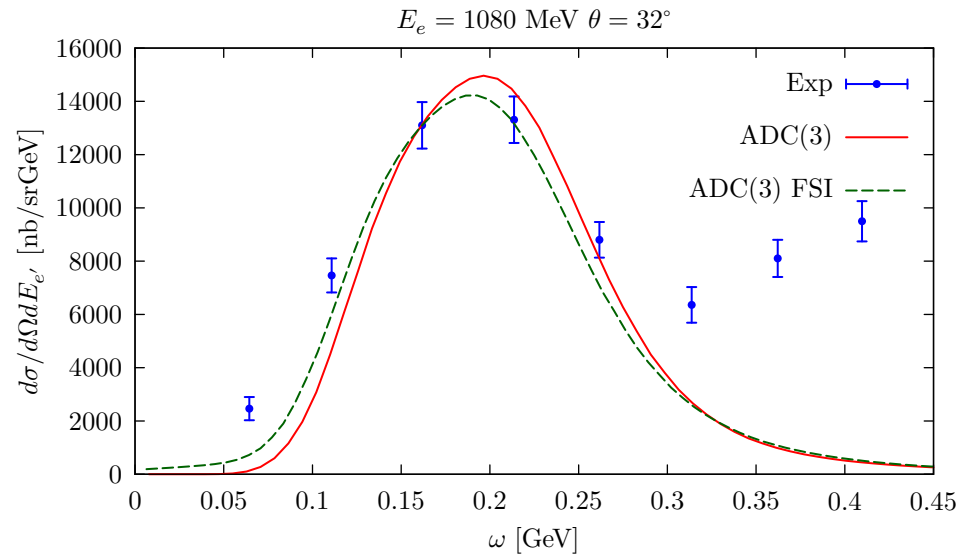
Based on the saturating chiral N2LO-sat nuclear force



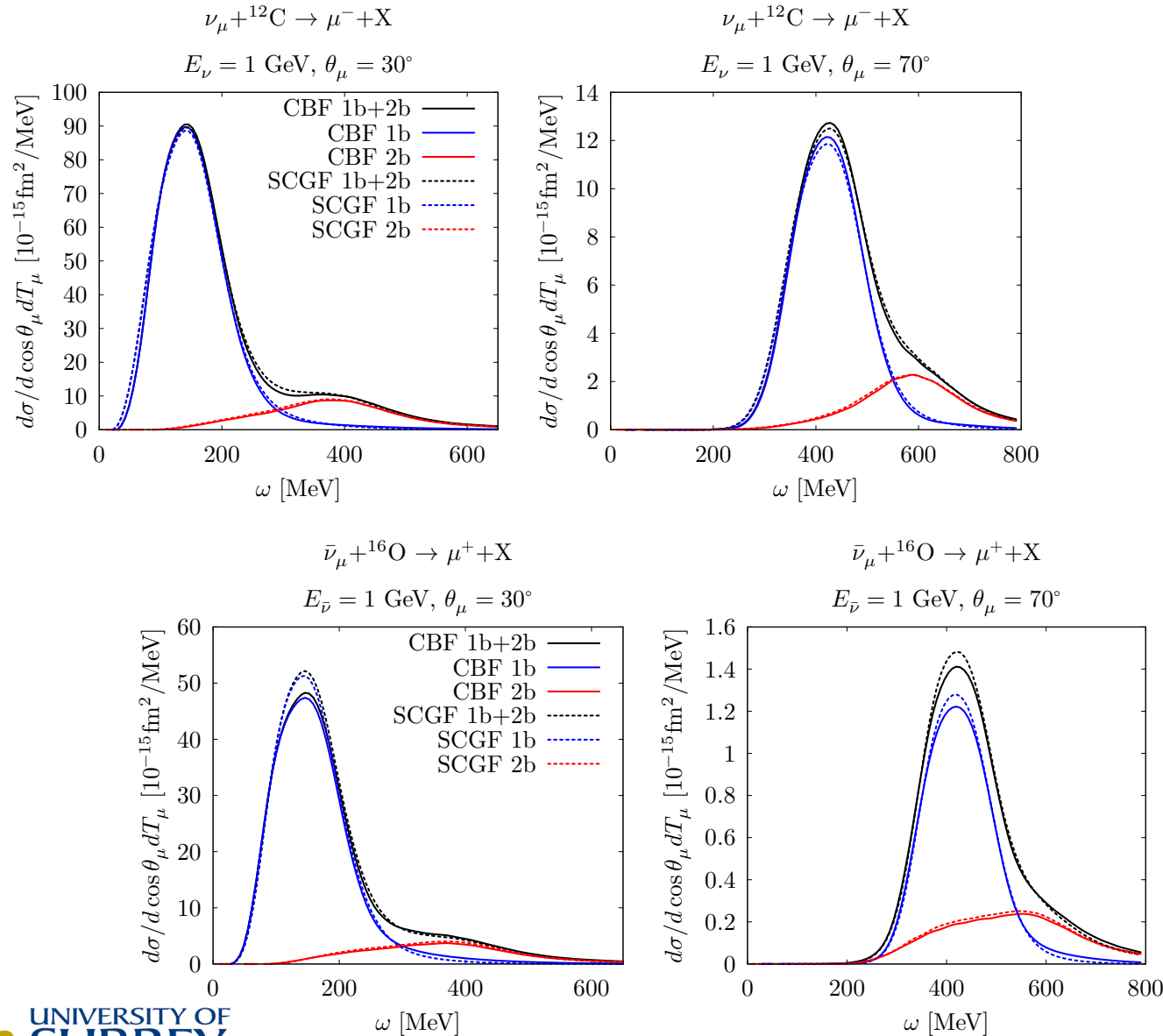
$^{16}\text{O}-e^-$ cross sections from the SCGF Spect. Fnct.



Based on the
saturating chiral
N2LO-sat
nuclear force



Charged-current reaction for 1 GeV neutrinos



One-body current describe quasi elastic peak

Difference between CBF(AV18) and SCGF(NNLOsat) from 1-b terms

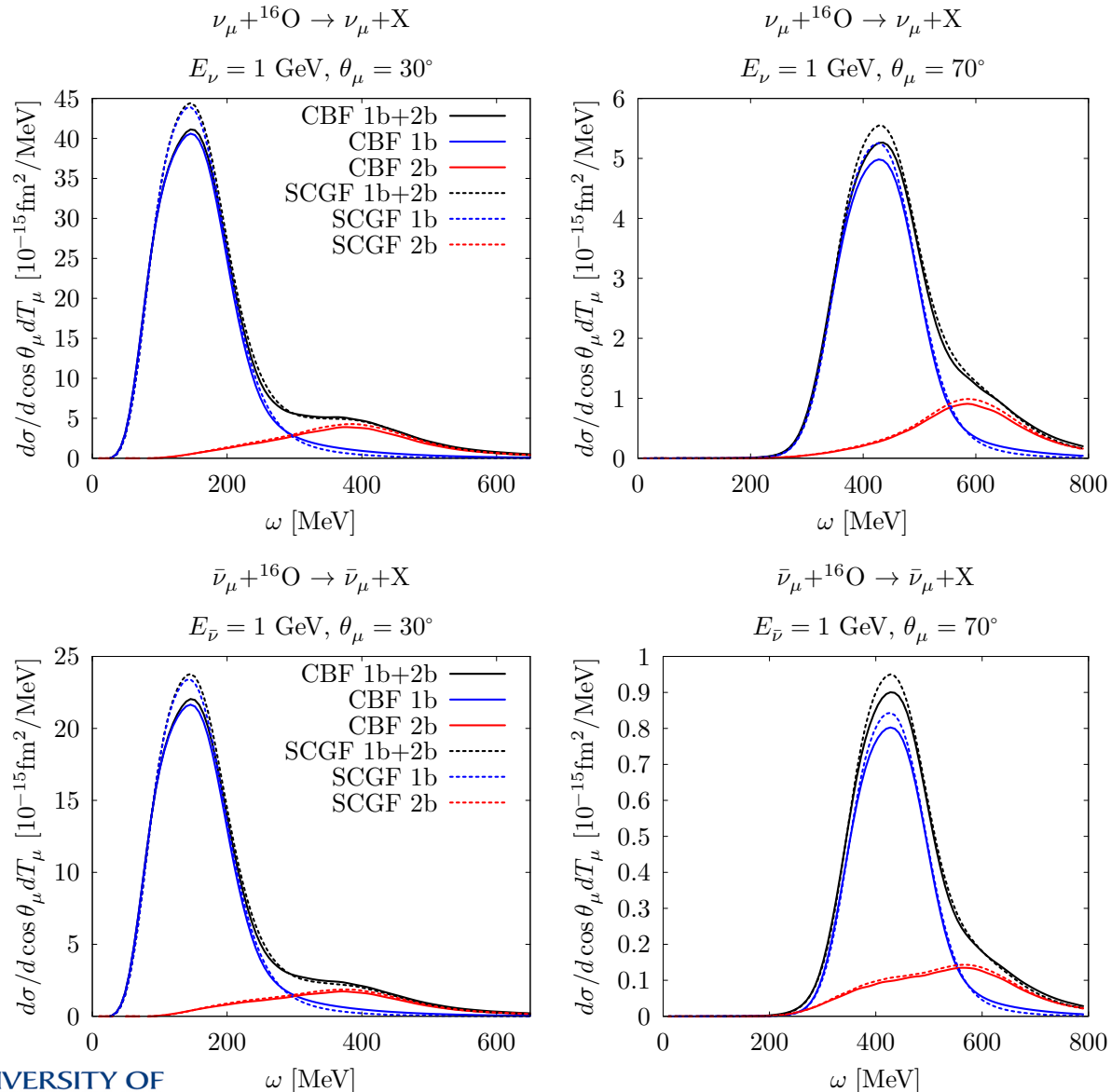
Two-body currents fill up dip region

Missing Delta and meson emission contributions

X-sec. droppin with scattering angle

N. Rocco, CB, O. Benhar, A. De Pace, A. Lovato, arXiv:1810.0wxyz (in preparation)

Neutral-current reaction for 1 GeV neutrinos



One-body current describe quasi elastic peak

Difference between CBF(AV18) and SCGF(NNLOsat) from 1-b terms

Two-body currents fill up dip region

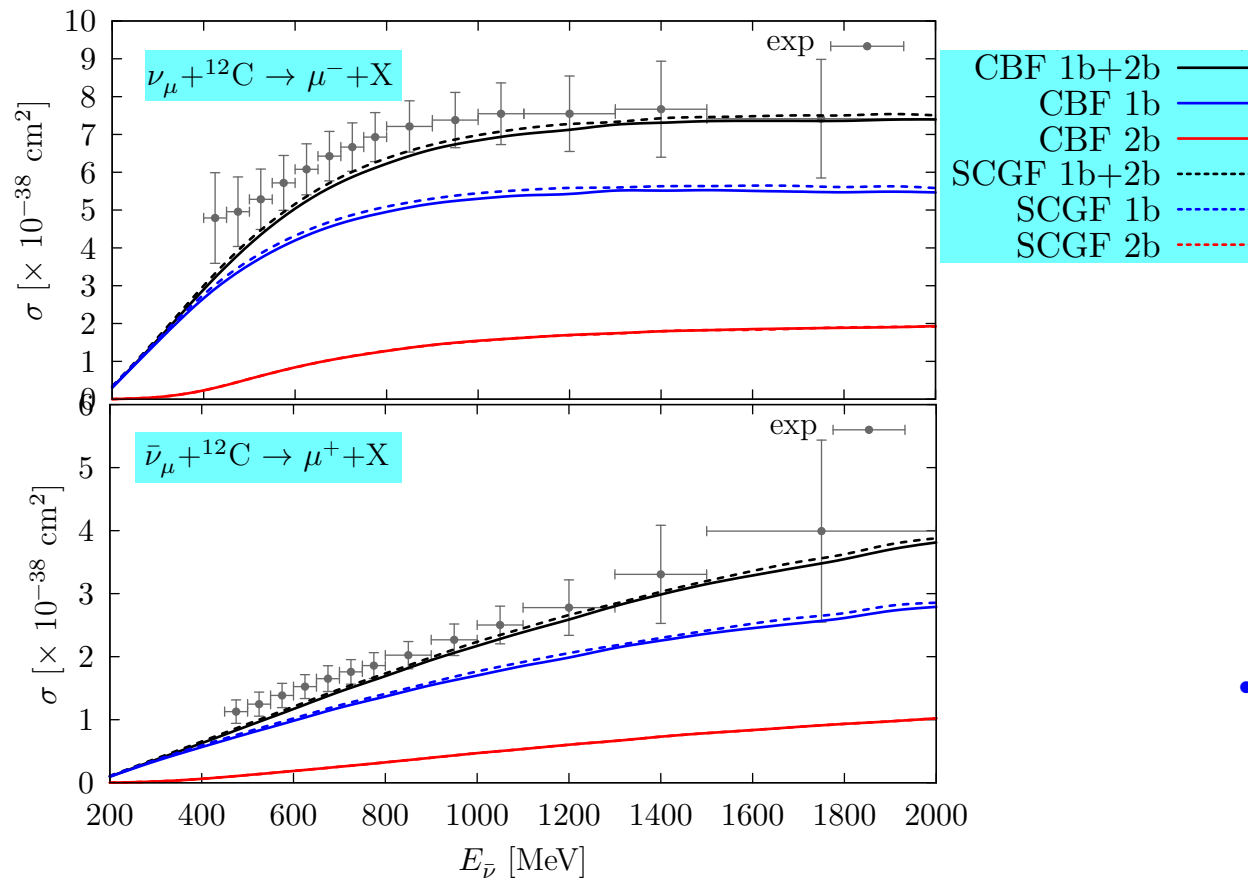
Missing Delta and meson emission contributions

X-sec. droppin with scattering angle

N. Rocco, CB, O. Benhar, A. De Pace, A. Lovato,
arXiv:1810.0wxyz (in preparation)

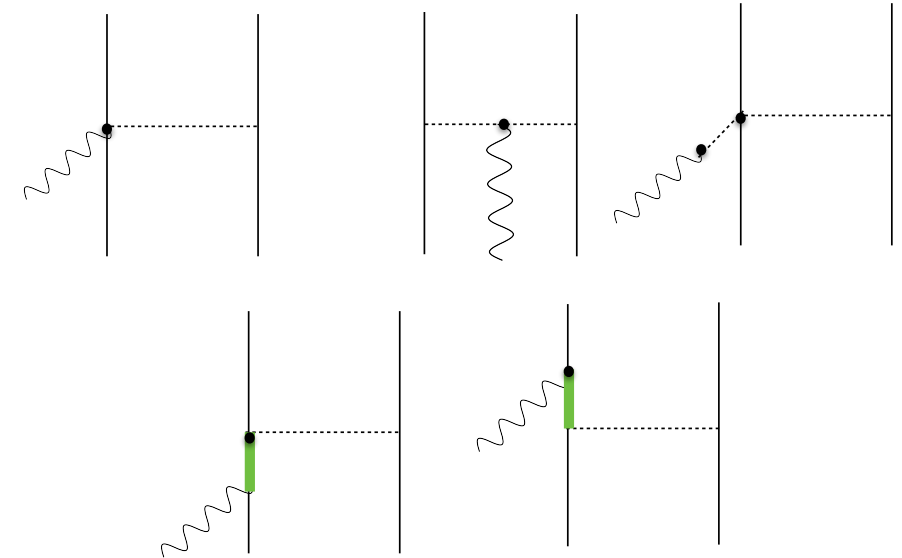
Role of two-body (meson exchange) currents in ν -A

CC0 π total cross section: MiniBooNE data



The 2p2h contribution is needed to explain the magnitude of the total cross section

- Two-body diagrams contributing to the axial and vector responses

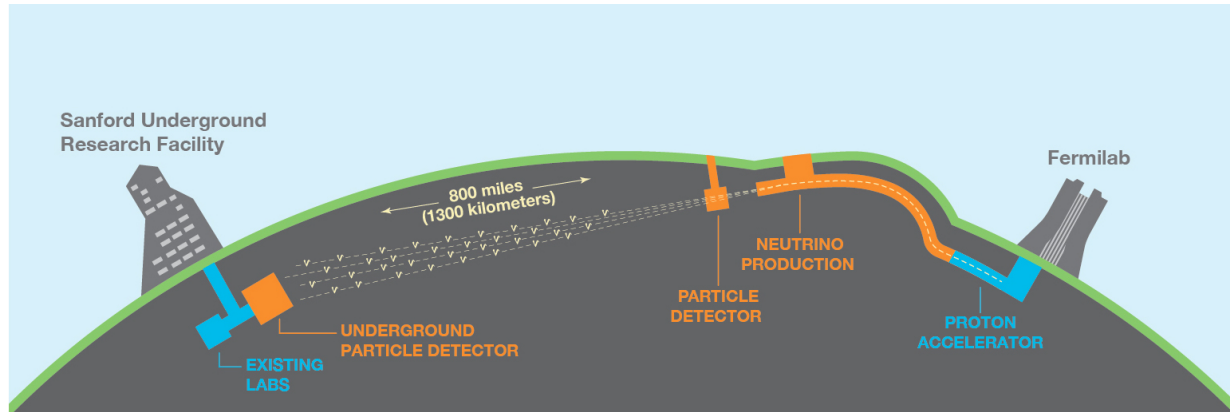


- Preliminary implementation discards 1b-2b interference:

$$W_{2p2h}^{\mu\nu} = W_{ISC}^{\mu\nu} + W_{MEC}^{\mu\nu} + \cancel{W_{int}^{\mu\nu}}$$

N. Rocco, CB, O. Benhar, A. De Pace, A. Lovato,
arXiv:1810.0wxyz (in preparation)

Neutrino Oscillations – next generation experiments



DUNE experiment will measure long base line neutrino oscillations to:

- Resolve neutrino mass hierarchy
- Search for CP violation in weak interaction
- Search for other physics beyond SM



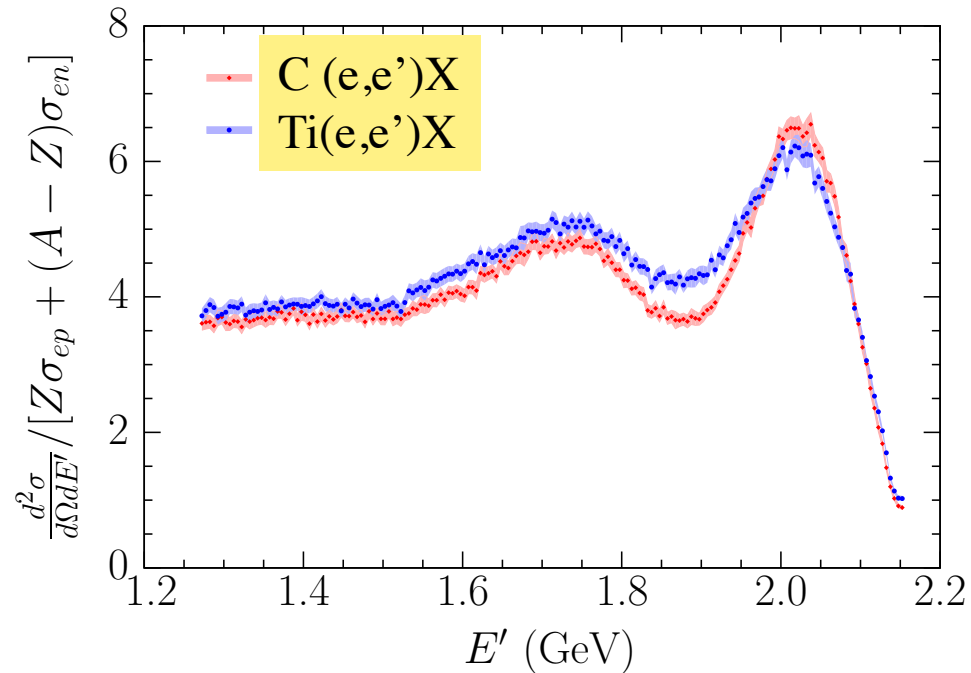
Liquid Argon projection chamber is being used. It will require **one order of magnitude** (20% → 2%) improvement in theoretical prediction for ν - ^{40}Ar cross sections to achieve proper event reconstruction.

→ Need good knowledge of ^{40}Ar spectral functions and consistent structure-scattering theories.

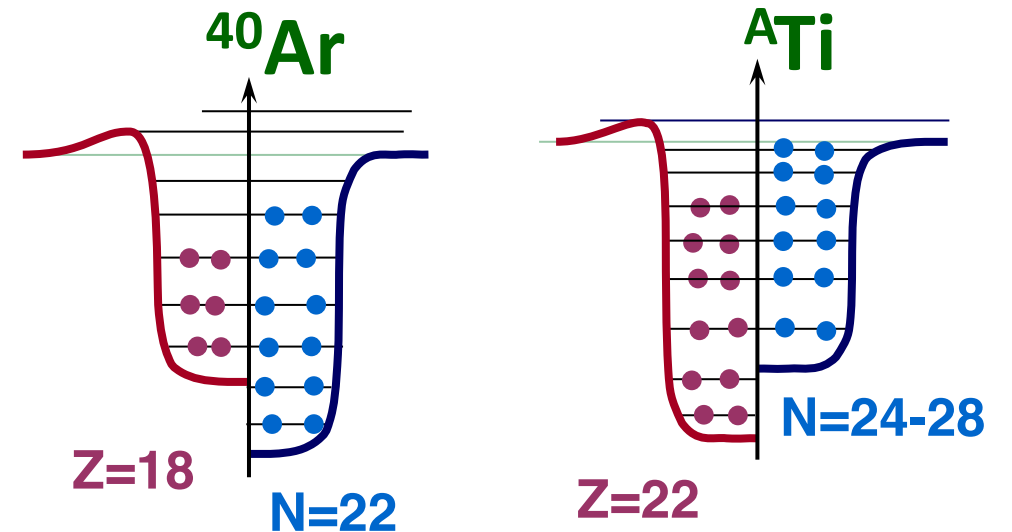
Spectral function for ^{40}Ar and Ti

Jlab experiment E12-14-012 (Hall A)

Phys. Rev. C 98, 014617 (2018)

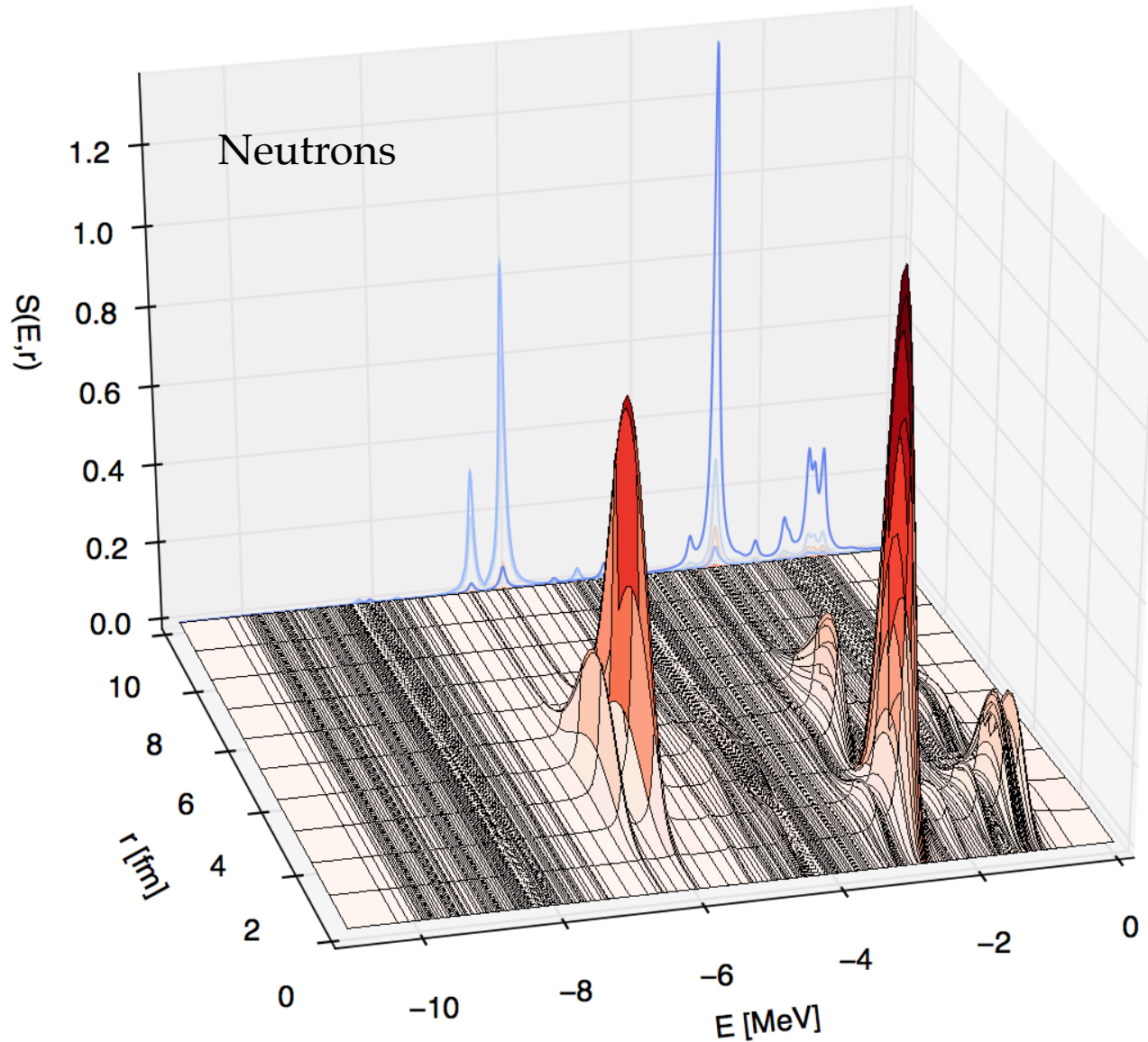


$^{40}\text{Ar}(e,e'p)$ and Ti(e,e'p) data being analyzed



Proton distribution in Ti similar to neutron in ^{40}Ar ??

Spectral function for ^{40}Ar



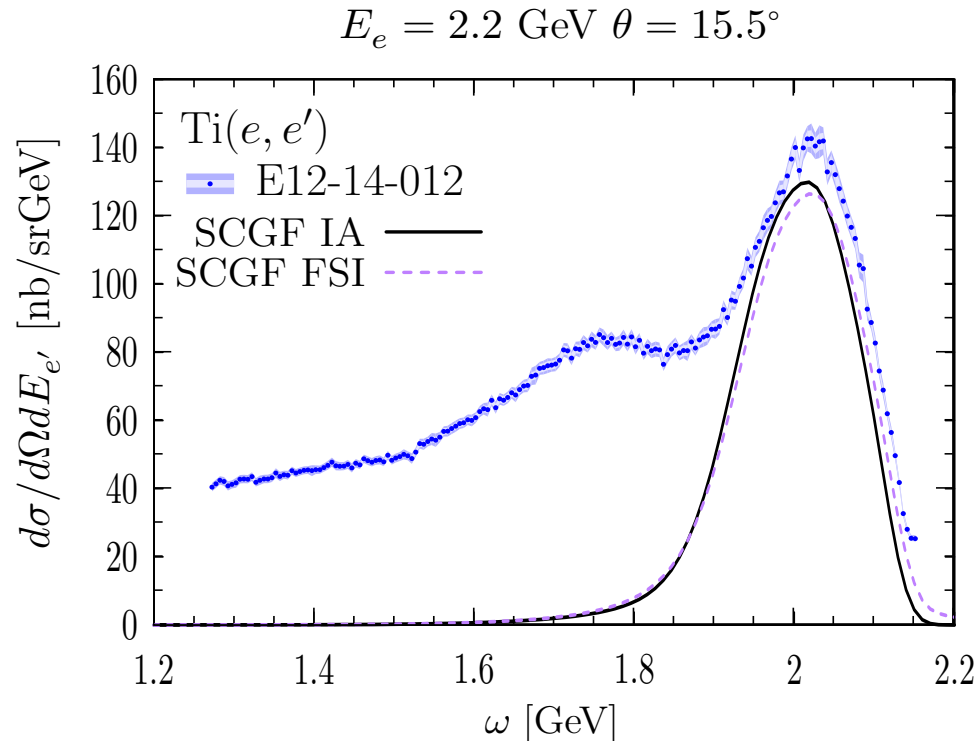
- Experimental data now available for Jlab:
H. Dai et al., arXiv:1803.01910
 - Ab initio simulations based on the ADC(2) truncation of the N2LO-sat Hamiltonian
- Want validation of initial state correlation before they are implemented in neutrino- ^{40}Ar simulations

N. Rocco, V. Somà, CB, in preparation

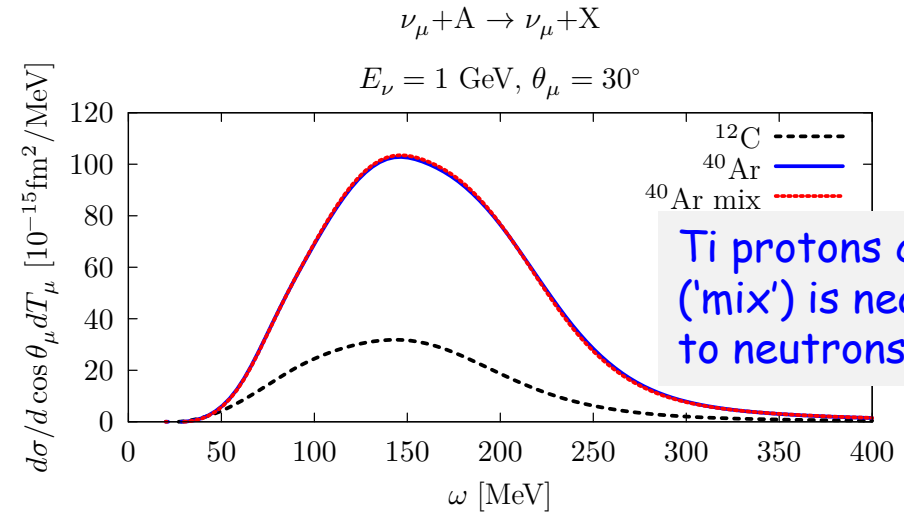
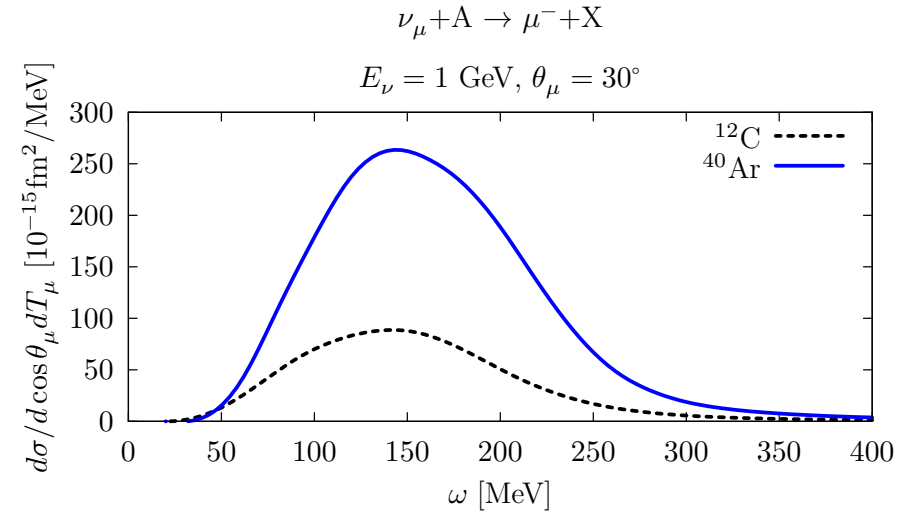
Electron and ν scattering on ^{40}Ar and Ti

Jlab experiment E12-14-012 (Hall A)

Phys. Rev. C 98, 014617 (2018)



$^{40}\text{Ar}(e, e'p)$ and $\text{Ti}(e, e'p)$ data being analyzed



Ti protons contribution ('mix') is nearly identical to neutrons in ^{40}Ar .

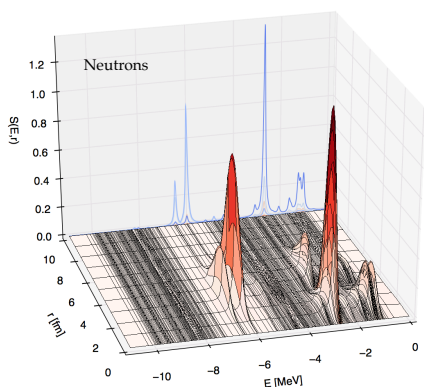
N. Rocco, CB and V. Somà, in preparation.

Summary

Thank you for your attention!!

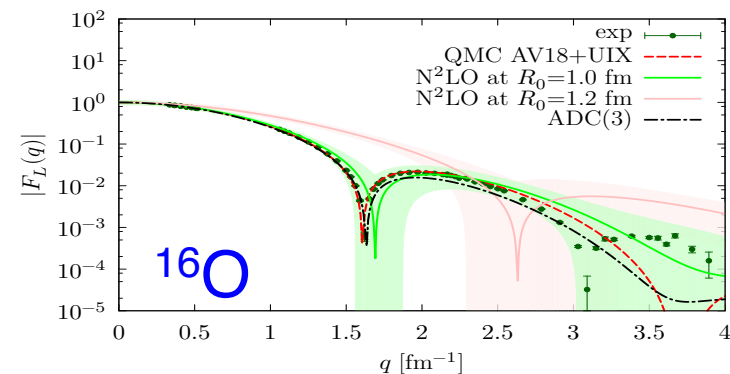
Saturating chiral interactions and 3N forces:

- *Description of nuclear g.s. in the pf shell is improved-especially in the trends w.r.t. iso-sopin asymmetry.*
- *Radii: newer generations of chiral interaction can give satisfactory radii.*



Applications to electron and neutrino scattering:

- *Spectral functions are extracted naturally from the SCGF formalism.*
- *good reproduction of charge/momentum distribution and electron scattering.*
- *Inclusion of electroweak currents (1b and 2b) underway (by N. Rocco).*



**A. Cipollone, A. Rios,
A. Idini, F. Raimondi**



V. Somà, T. Duguet

granite atomica - energie rinnovabili



A. Lovato, N. Rocco

ECT*

A. Carbone



P. Navratil

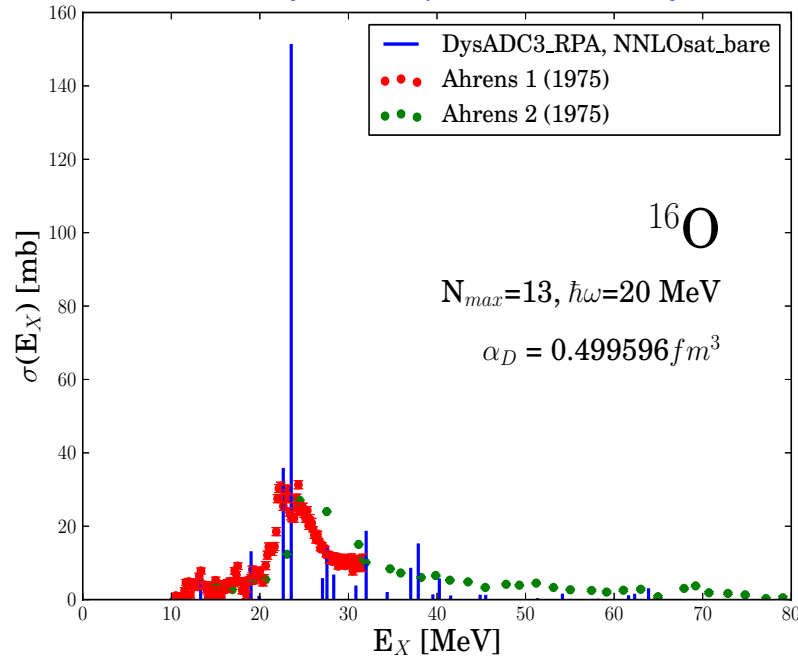


**SAPIENZA
UNIVERSITÀ DI ROMA**

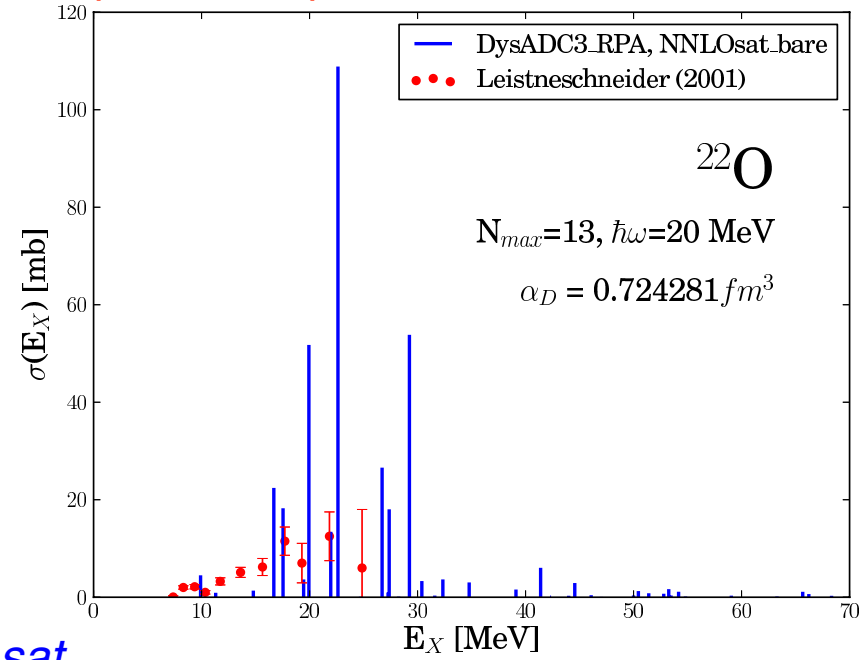
O. Benhar

Results for Oxygen isotopes

σ from RPA response (discretized spectrum) vs σ from photoabsorption and Coulomb excitation



NNLOsat

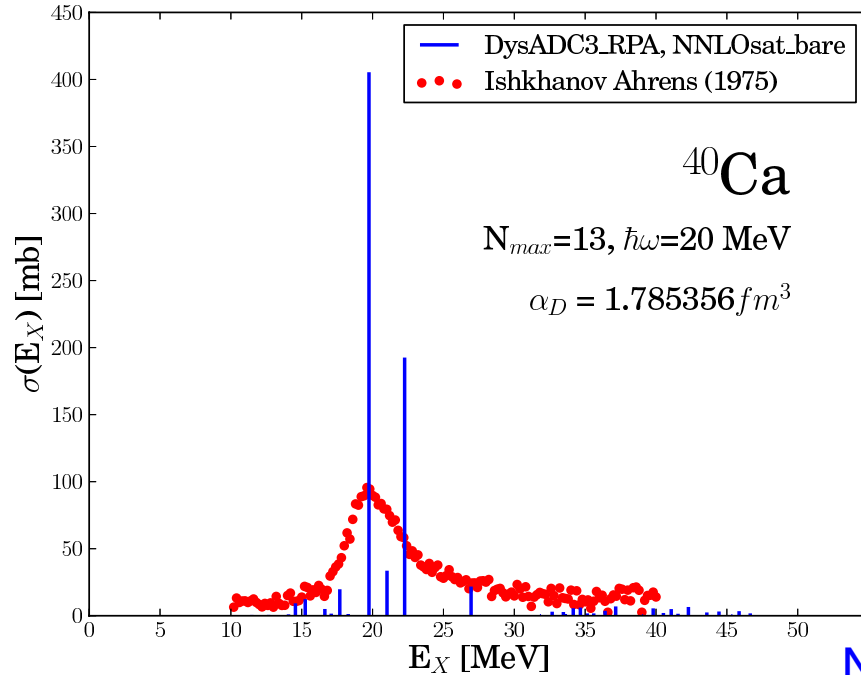


- GDR position of ^{16}O reproduced
- Hint of a soft dipole mode on the neutron-rich isotope

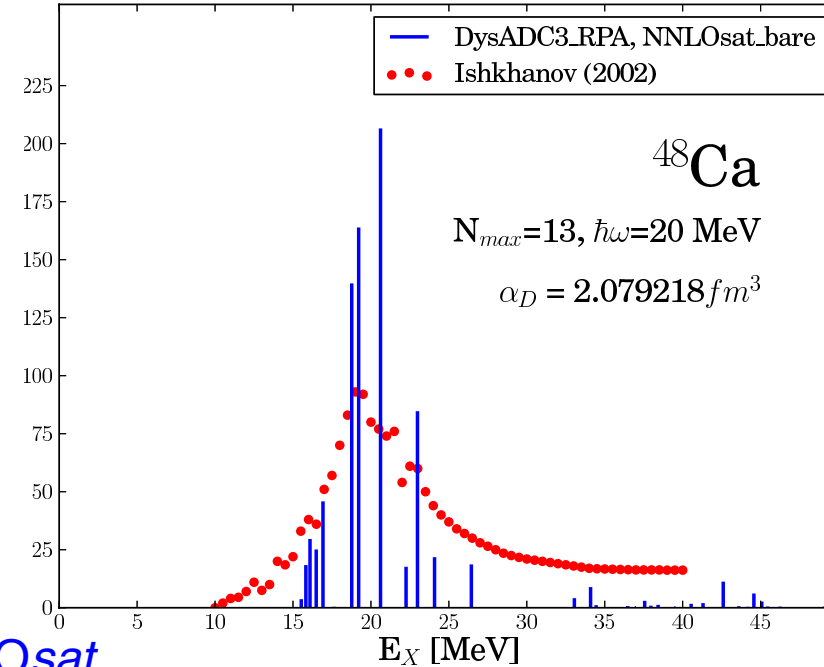
Nucleus	Dipole polarizability α_D (fm ³)		
	SCGF	CC/LIT	Exp
^{16}O	0.50	0.57(1)	0.585(9)
^{22}O	0.72	0.86(4)	0.43(4)

Results for Calcium isotopes

σ from RPA response (discretized spectrum) vs σ from photoabsorption and Coulomb excitation



NNLOsat



- Positions of GDRs reproduced

Nucleus	Dipole polarizability α_D (fm ³)		
	SCGF	CC/LIT	Exp
^{40}Ca	1.79	1.47 (1.87) _{thresh}	1.87(3)
^{48}Ca	2.08	2.45	2.07(22)

Two-nucleon emission

CB, C. Giusti, et al., Phys Rec **C70** , 014606 (2004)

D. Middleton et al.: Eur. Phys. J. A 29, 261-270 (2006)
Eur. Phys. J. A 43, 137-143 (2010)

M. Makek et al.: Eur. Phys. J. A 52, 298 (2016)

Calculating $(e, e'pN)$ cross sections @ low energy

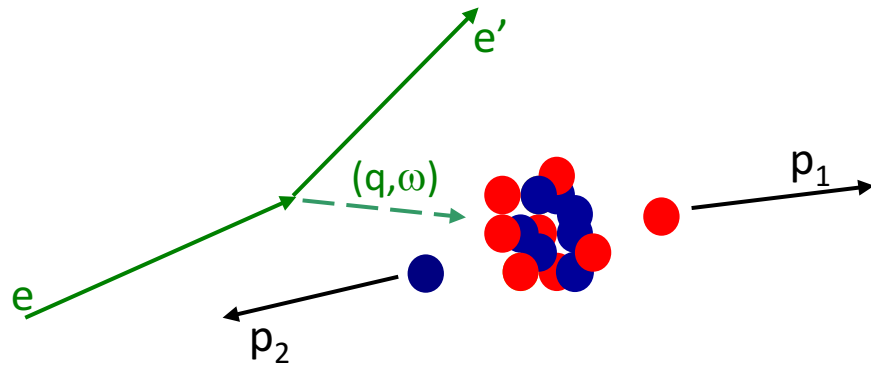
The hadronic current is:

$$J^\mu(q) = \int \langle \Psi_f | \hat{J}^\mu(r) | \Psi_i \rangle e^{iq \cdot r} d\mathbf{r} = \int \Psi_f^*(\mathbf{r}_1 \boldsymbol{\sigma}_1, \mathbf{r}_2 \boldsymbol{\sigma}_2) J^\mu(\mathbf{r}, \mathbf{r}_1 \boldsymbol{\sigma}_1, \mathbf{r}_2 \boldsymbol{\sigma}_2) \\ \times \Psi_i(\mathbf{r}_1 \boldsymbol{\sigma}_1, \mathbf{r}_2 \boldsymbol{\sigma}_2) e^{iq \cdot r} d\mathbf{r} d\mathbf{r}_1 d\mathbf{r}_2 d\boldsymbol{\sigma}_1 d\boldsymbol{\sigma}_2$$

Final state: $\Psi_f^*(\mathbf{r}_1 \boldsymbol{\sigma}_1, \mathbf{r}_2 \boldsymbol{\sigma}_2)$. \rightarrow 3-body scatt.: Opt. pot.

Initial state: $\Psi_i(\mathbf{r}_1 \boldsymbol{\sigma}_1, \mathbf{r}_2 \boldsymbol{\sigma}_2)$. \rightarrow nucl. structure (S^{hh})

Reaction current: $J^\mu(\mathbf{r}, \mathbf{r}_1 \boldsymbol{\sigma}_1, \mathbf{r}_2 \boldsymbol{\sigma}_2) = J^{(1\text{-body})} + J^{(2)}$



The reaction rate is:

$$\frac{d^8 \sigma}{dE'_0 d\Omega dE'_1 d\Omega'_1 d\Omega'_2} = K \Omega_f f_{\text{rec}} |j_\mu J^\mu|^2$$

K , Ω_f , f_{rec}^{-1} and j_μ are known.

The hadronic current J^μ is the non-trivial part

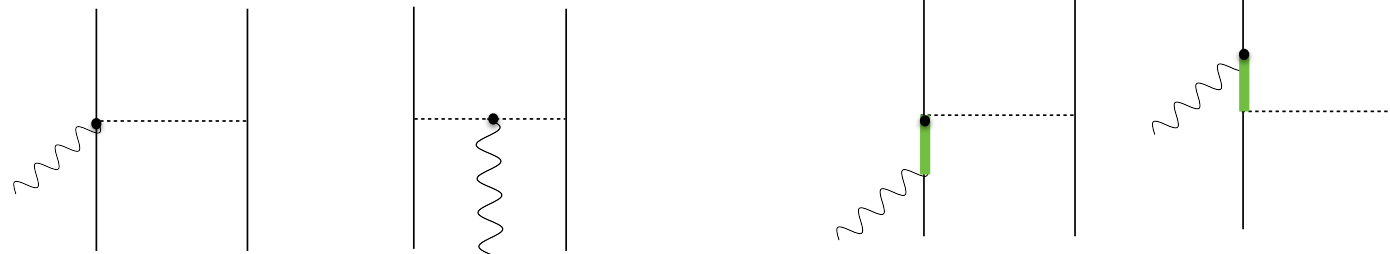
direct

two-body currents

(seagull)

(pion-in-flight)

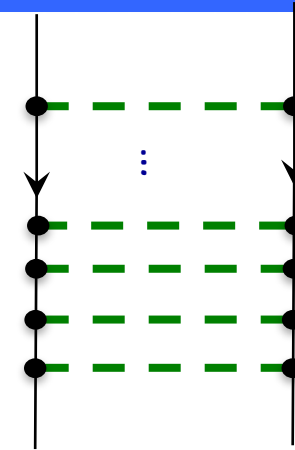
(delta)



Correlated 2-nucleon wave function

$$X_{abJ}^i = \langle \Psi_J^{i,A-2} | (c_{\tilde{\beta}} c_{\bar{\alpha}})_J | \Psi_0^A \rangle$$

Obtained from RPA resummation of ladder diagrams (similarly to shell model configuration mixing between two-nucleon states):



Direct calculations of correlations are possible in a finite space **P** (e.g. 4-10 osc. shells - NO CORE) which is complete for LRC:

$$P \hat{H}_{\text{eff}} P | \Phi_i \rangle = E_i | \Phi_i \rangle$$

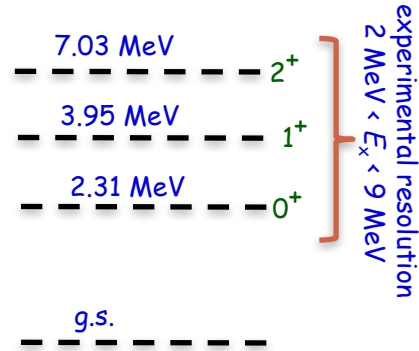
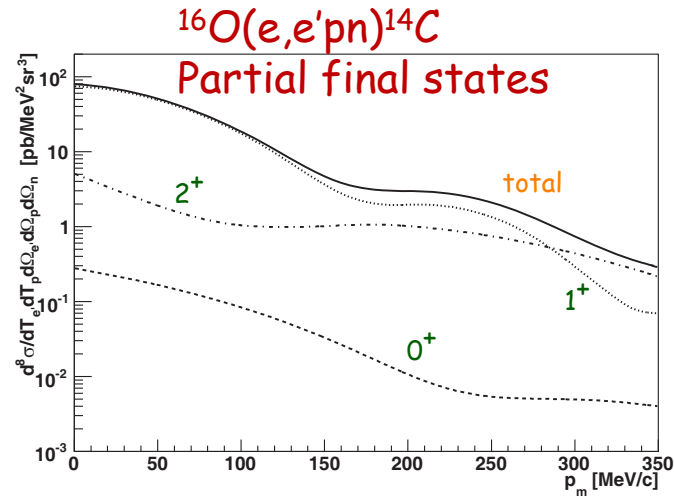
Effects from SRC are then included by calculating ladders in the excluded space **Q**:

$$| \Psi_i \rangle = (1 + \hat{\chi}) | \Phi_i \rangle = | \Phi_i \rangle + | \chi_i \rangle$$

$$| \Psi \rangle = | \Phi \rangle + \frac{Q}{\omega - Q \hat{T} Q + i \eta} \hat{G}(\omega) | \Phi \rangle \quad \hat{G}(\omega) = \hat{V} + \hat{V} \frac{Q}{\omega - Q \hat{T} Q + i \eta} \hat{G}(\omega)$$



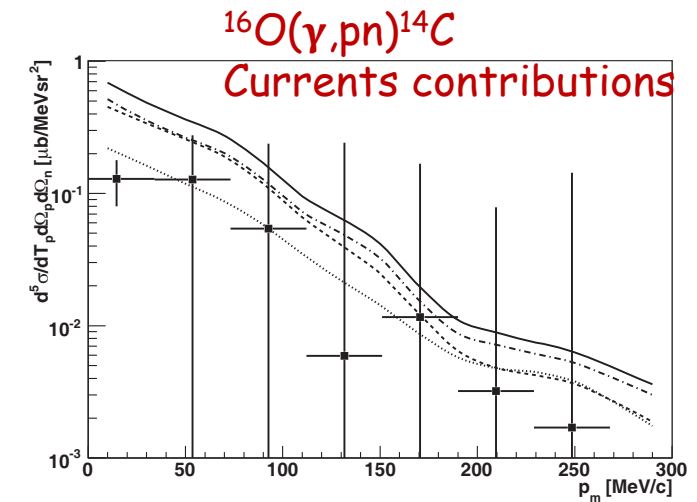
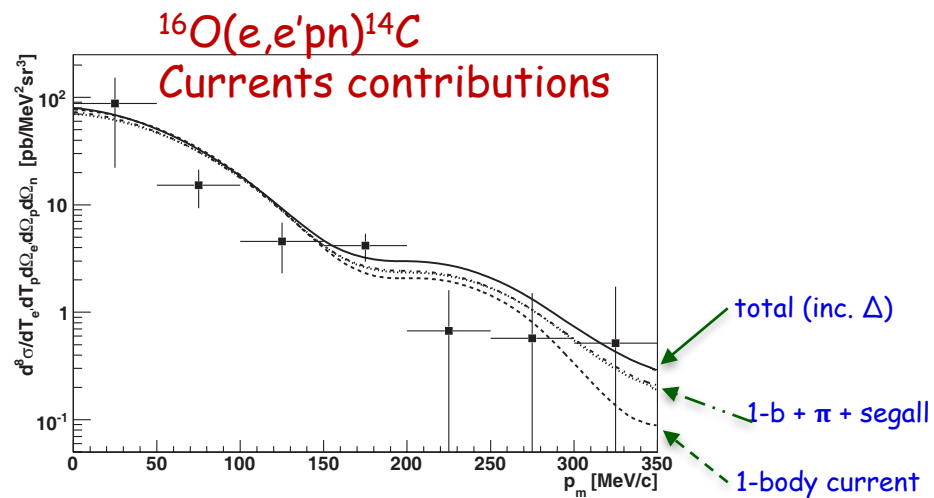
Proton-neutron emission from ^{16}O



Experiments at MAMI

D. Middleton et al., C. Giusti, CB,
Eur. Phys. J. A 29, 261–270 (2006)
Eur. Phys. J. A 43, 137–143 (2010)

Eur. Phys. J. A 52, 298 (2016)



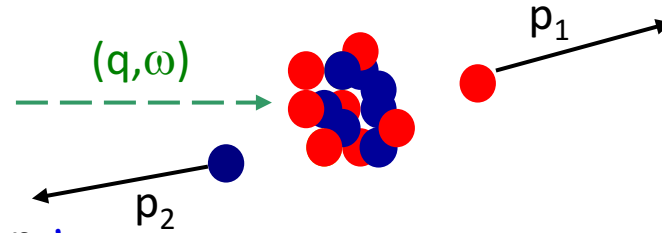
Correlations in proton-neutron knock out

- $^{16}\text{O}(e,e'pn)^{14}\text{N}$

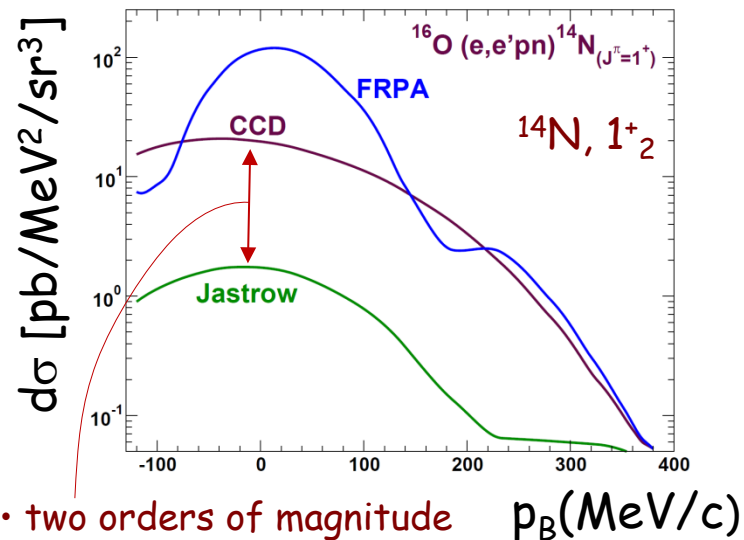
- initial wave function from SCGF or 'CCM'

- Pavia model for final state interactions

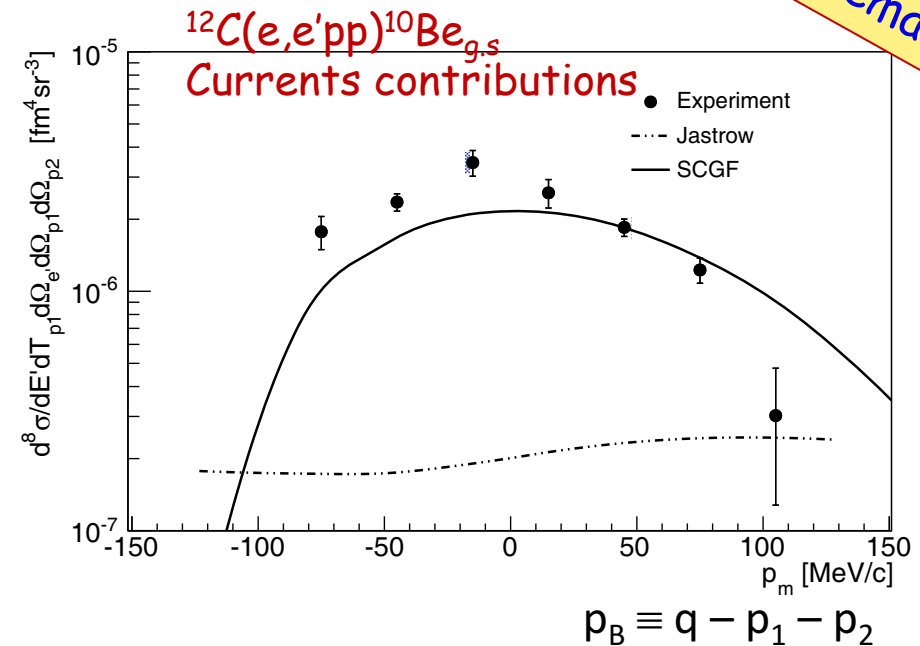
- Integrated x-secs. plotted vs. $p_B \equiv q - p_1 - p_2$:



Long range corrl. effects
may be dominant in
appropriate kinematics



• two orders of magnitude
from long-range correlations.



H. Muether, Giusti et al, Phys Rev C (1999) -- CCD
CB, C. Giusti, et al., Phys Rec C70 , 014606 (2004) -- SCGF

Experiment at MAMI Eur. Phys. J. A 52, 298 (2016)

Can we learn something from $(e, e'pN)$ at MESA ??

- Direct two-nucleon emission directly sensitive to currents (2N currents too!)
- Low-energy correlation effects may be relevant in appropriate kinematics
- Old experiments very difficult and difficult E/p resolution

→ BUT what about MESA??

- Viable way to test currents and interaction theories/models?
- Applications from EFT/ab initio? (though FSI require optical models...)
- Utility to constrain $\beta\beta$ -decay??