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# SMEFT@NLO in QCD: Top/Higgs/EW sector

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[arXiv:1804.xxxxx](https://arxiv.org/abs/1804.xxxxx)

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# Outline

- Update on status & progress in SMEFT at NLO in QCD
  - Towards complete public Monte Carlo tool
- **Top/Higgs/EW** SMEFT @ the LHC
  - Interactions with Higgs, gauge bosons & top quark
  - Model implementation in leading MFV expansion
- Showcase study
  - Single **top** production in association with a **Z** or **Higgs** at the LHC
  - Investigate energy growth in helicity sub amplitudes
  - Current & future LHC sensitivity study vs. existing constraints
- Motivate & facilitate global LHC analyses of top/Higgs/EW sector at NLO in QCD

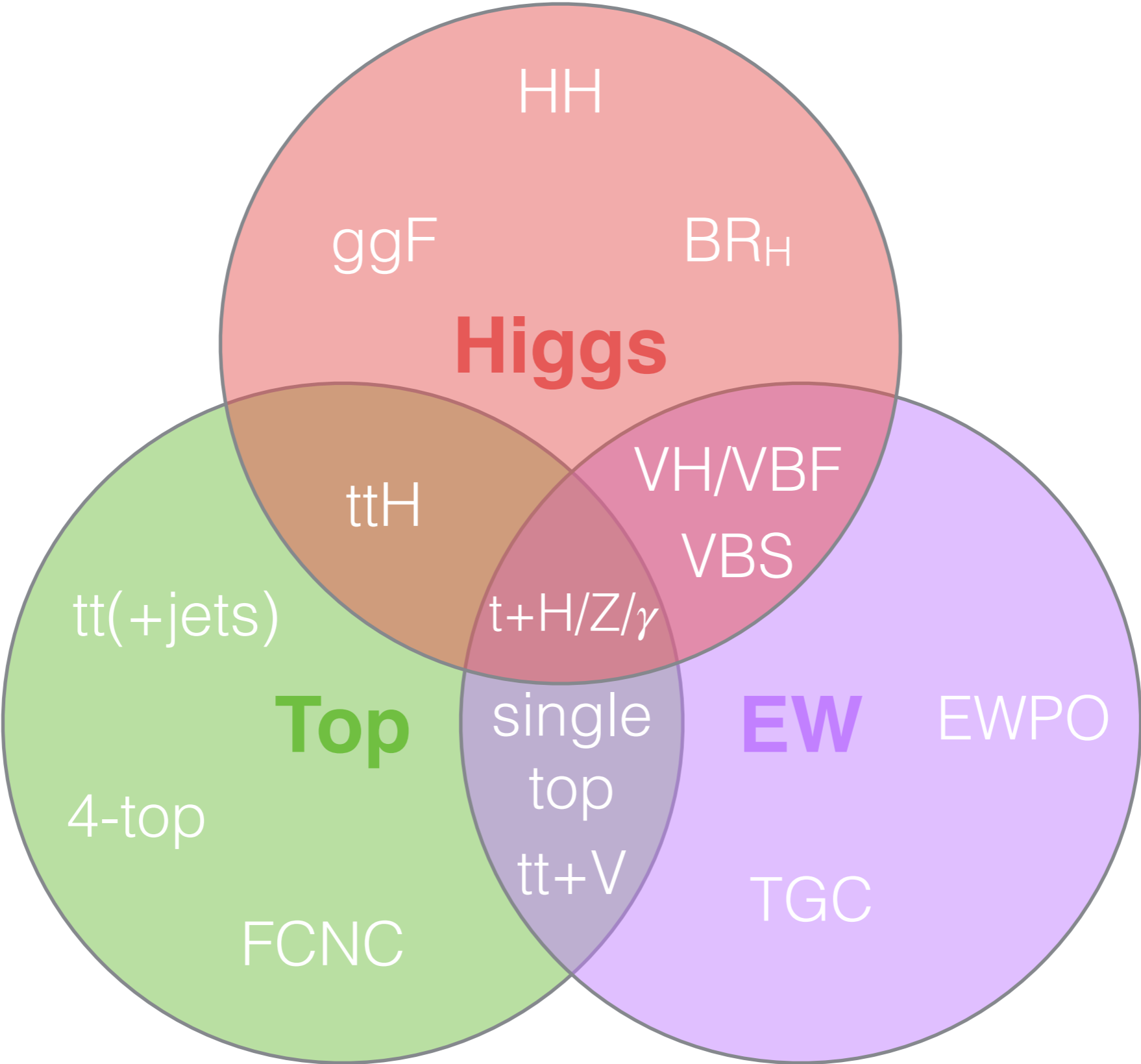
# Introduction

- The LHC is entering a “precision era”
  - No clear evidence for new physics from direct searches
  - We are approaching the limits of the ‘energy frontier’
  - Higgs boson discovery has completed the picture of the Standard Model (SM) Electroweak (EW) sector
  - Properties consistent with SM expectations
  - Complementary approach: SMEFT
- Many channels are becoming systematics dominated
  - Requires high precision theory input: higher order predictions
  - Fixed order (FO) & interfaced with parton shower (PS)
  - Standard for SM, also useful for BSM effects

# SMEFT at the LHC: EWSB sector

Jets

Decays



Flavor

CPV

# Status: LO

- Increasing number of EFT interpretations in experimental analyses
- Several MC implementations of SMEFT at LO
  - HEL, SMEFTsim, dim6top,... *[Alloul et al.; JHEP 1404 (2014) 110]*  
*[Brivio et al.; JHEP 1712 (2017) 070]*
  - Higgs Characterisation, BSMC, HiggsPO,... *[Aguilar Saavedra et al.; arXiv:1802.07237]*  
*[Artoisenet et al.; JHEP 1311 (2013) 043]*  
*[Falkowski et al.; EPJC 75 (2015) 12, 583]*  
*[Greljo et al.; EPJC 77 (2017) 12, 838]*
- Many phenomenological analyses and global fits performed for SMEFT at LHC+... *[Falkowski & Riva; JHEP 1502 (2015) 039]*  
*[Berthier & Trott; JHEP 1505 (2015) 024]*  
*[Corbett et al.; JHEP 1508 (2015) 156]*  
*[Buckley et al.; JHEP 1604 (2016) 015]*  
*[Englert et al.; EPJC 76 (2016) 7, 393]*  
*[Butter et al.; JHEP 1607 (2016) 152]*  
*[Ellis et al.; arXiv:1803.03252]*
  - Separate Higgs/Gauge and top sector
  - LO accuracy

# Going NLO

- Ultimate goal: a **precision global fit** of full SMEFT including LHC observables at HL-LHC
- Step 1: **NLO QCD(+PS)** predictions
  - K-factors/shapes & control over PDF + scale uncertainties
- **NLO EW** corrections
  - Potentially important but much harder
  - Automation on the way with SHERPA, Madgraph5\_aMC@NLO
- **RG-improved** predictions & **operator mixing**
  - Very helpful for cross checking NLO implementations
  - Compare to full NLO calculations, assess the importance of finite terms

*[Alonso\*, Jenkins, Manohar & Trott; JHEP 1310 (2013) 087, JHEP 1401 (2014) 035 & JHEP 1404 (2014) 159\*]*

# Status: Higgs

- **Single Higgs** state of the art @ fixed order:
  - Yukawa & HGG ops. (NNLO+NNLL) *[Grazzini et al.; arXiv:1705.05143]*
  - Top chromomagnetic op. (NLO) *[Deutschmann et al.; JHEP 1712 (2017) 063]*
- Public codes with partial SMEFT contributions @ NLO
  - HiGlu *[Spira; arXiv:hep-ph/9510347]*
  - SusHi (aMC-SusHi) *[Harlander, Liebler & Mantler; arXiv:1605.03190]*
- Double Higgs
  - HPAIR *[Dawson, Dittmaier & Spira; Phys. Rev. D58:115012]*
  - HiggsPair (HERWIG++) *[Goertz et al.; JHEP 1504 (2015) 167]*
- eHDECAY for BR *[Contino et al.; Comp. Phys. Comm. 185 (2014) 3412-3423]*
- Full 1-loop  $H \rightarrow \gamma\gamma$  and  $H \rightarrow bb$  *[Hartmann & Trott; PRL 115 (2015) 191801]*  
*[Gauld, Scott & Pecjak; PRD94 (2016) 074045]*

# Status: Higgs & EW

*[Denner et al.; JHEP 1203 (2012) 075]*

- HAWK <http://omnibus.uni-freiburg.de/~sd565/programs/hawk/hawk>
  - VBF and VH @ NLO in QCD & EW for SM
  - 2 anomalous couplings parameters at NLO in QCD

*[Baglio et al.; arXiv:1404.3940]*

- VBFNLO <https://www.itp.kit.edu/vbfnlo>
  - General tool for Higgs/weak boson production @ NLO in QCD
  - LO event generation & general L3 anomalous coupling parametrisation

*[KM, Sanz & Williams.; JHEP 1608 (2016) 039]*

- WH & ZH via POWHEG-BOX/MCFM <http://powhegbox.mib.infn.it>
  - NLO QCD +PS event generation for Higgs/EW operators (SILH)

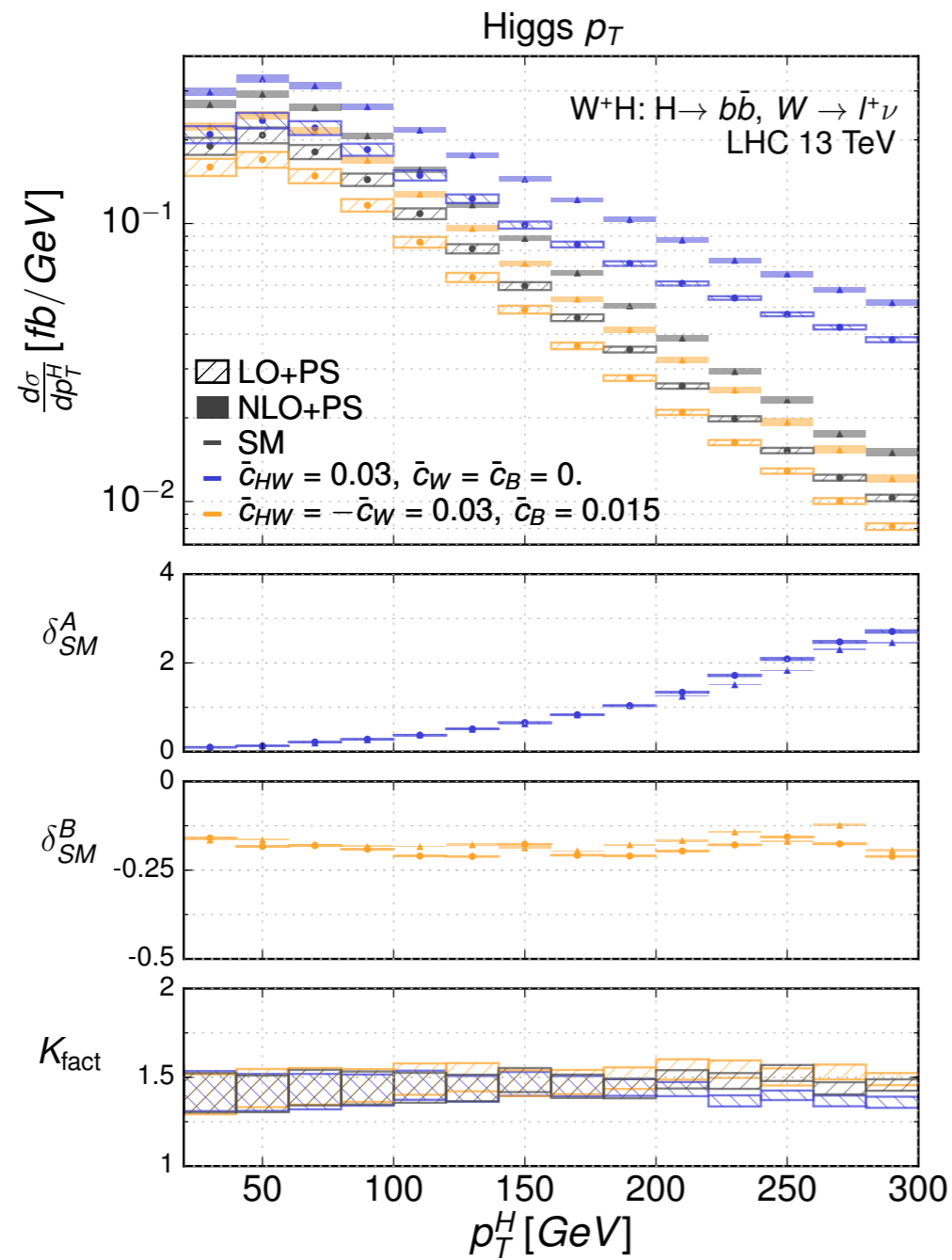
*[Degrande, et al.; EPJC 77 (2017) 4, 262]*

- HELatNLO <http://feynrules.irmp.ucl.ac.be/wiki/HELatNLO>
  - FeynRules/NLOCT/UFO implementation of Higgs/EW operators
  - VH, VBF & any other process of interest (CPV operators also on the way)

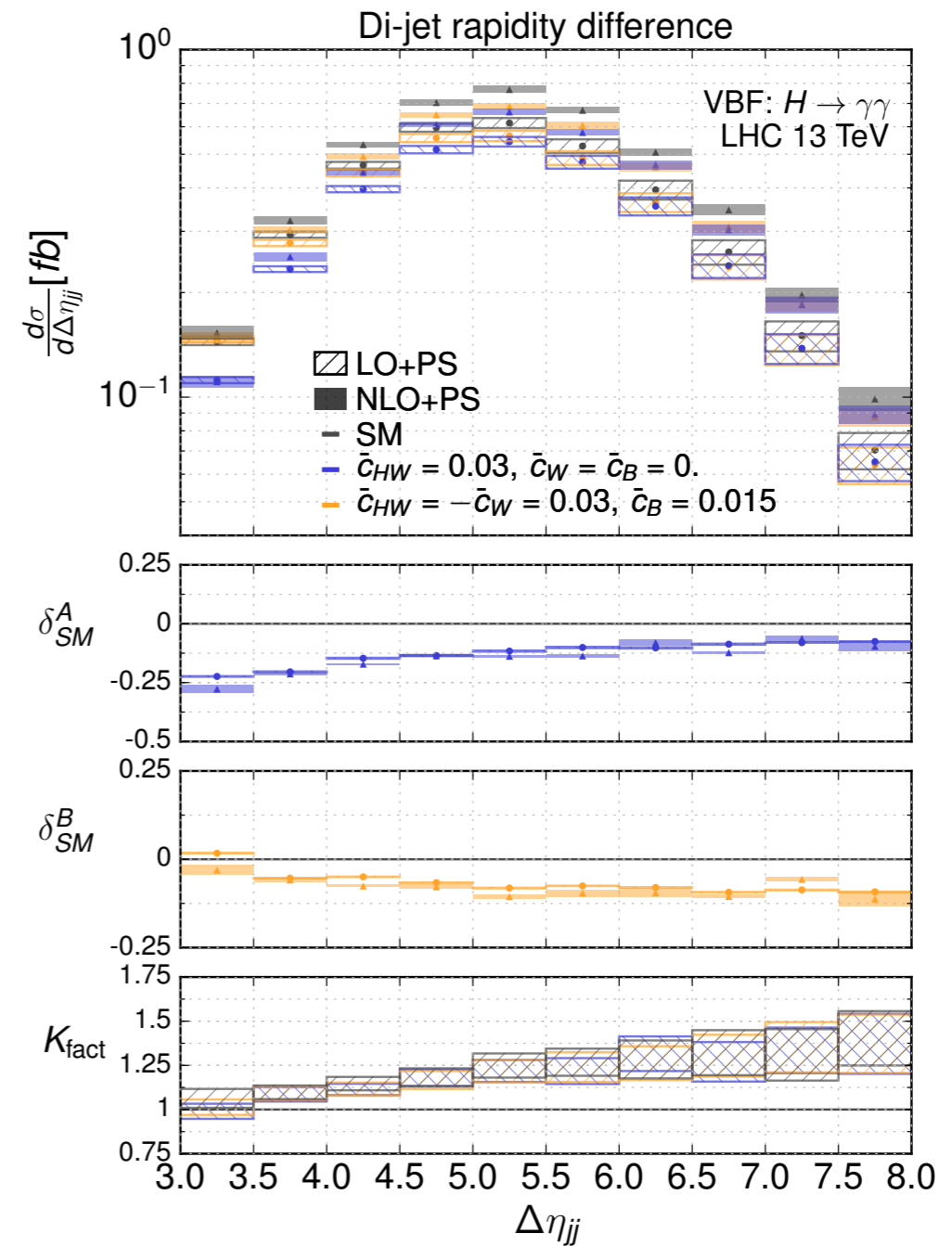


# SMEFT@NLO QCD+PS

WH



VBF



# Status: Top

- Currently no public SMEFT tool for top sector at NLO
- Several works on specific processes based on private implementations
- Single top *[Zhang; PRL 116 (2016) 162002]*
- ttH *[Maltoni, Vryonidou & Zhang; JHEP 1610 (2016) 123]*
- tt+Z/ $\gamma$  *[Bylund et al.; JHEP 1605 (2016) 052]*
- top FCNC *[Degrande et al.; PRD 91 (2015) 034024]*  
*[Durieux, Maltoni & Zhang; PRD 91 (2015) 074017]*
- Our work: bring all previous implementations together into a public model for top/Higgs/EW SMEFT at NLO in QCD

# FeynRules/NLOCT/UFO

- **FeynRules** *[Christensen & Duhr; Comp. Phys. Comm. 180 (2009) 1614]*  
*[Alloul et al.; Comp. Phys. Comm. 185 (2014) 2250]*
  - Framework: Lagrangian → Feynman rules → UFO model → MC events
- **Universal FeynRules Output (UFO)** *[Degrande et al.; Comp. Phys. Comm. 183 (2012) 1201]*
  - Model file with particle content, internal/external parameters, Feynman rules, Lorentz structures, counter-terms,...
  - Compatible with many MC event generators (MG5, Sherpa, Whizard,...)
- **NLOCT** *[Degrande; Comp. Phys. Comm. 197 (2015) 239]*  
*[Hahn; Comp. Phys. Comm. 140 (2001) 415]*
  - Automatic calculation of UV and  $R_2$  counter-terms from FeynRules model
  - Implemented as additional Feynman rules in the UFO format
  - UV: on-shell renormalisation procedure for masses/wavefunction,  $\overline{\text{MS}}$  for higher point functions
  - $R_2$ : numerical artefacts of dimensional regularisation

# Top/Higgs/EW SMEFT

- **Top quark** is a crucial ingredient of the EW sector
  - Top-Higgs-W/Z couplings/masses are related in SM: **unitarity cancellations**
  - May reveal hints about the underlying nature of EWSB
- **Coloured** sector, strongly coupled to the Higgs
  - Large corrections to inclusive rates ( $\sim 1$  **K-factors**)
  - Non-trivial **shape corrections** at differential level
  - Non-trivial **renormalisation/operator mixing** from QCD
- Active research topic in SMEFT at NLO in QCD
- Many measurements at the LHC
  - Total, differential & boosted
  - Access **rare** processes *e.g.*  $tt+Z/W/\gamma$ ,  $tZj$

# Minimal Flavor Violation

[D'Ambrosio et al.; Nucl. Phys. B645 (2002) 155]

- Building SMEFT for top/Higgs/EW sector:
  - Fermion operators singling out **top/3rd generation** fermion fields
  - Go **beyond flavor universal** scenario in a controlled way

$$q^i \rightarrow U_q^{ij} q^j, \quad u^i \rightarrow U_u^{ij} u^j, \quad d^i \rightarrow U_d^{ij} d^j, \quad l^i \rightarrow U_l^{ij} l^j, \quad e^i \rightarrow U_e^{ij} e^j$$

- SM possesses a large  $U(1)^5$  flavor symmetry
  - Only **broken** by Yukawa couplings
  - Restore symmetry by promoting Yukawa matrices to spurions
  - Apply principle to higher dim. operators

$$Y_u \rightarrow U_q Y_u U_u^\dagger, \quad Y_d \rightarrow U_q Y_d U_d^\dagger, \quad Y_e \rightarrow U_L Y_e U_e^\dagger$$

$$\mathcal{L}_{\text{Yuk.}} = Y_d^{ij} (\bar{q}_i \varphi) d_j + Y_u^{ij} (\bar{q}_i \tilde{\varphi}) u_j + Y_e^{ij} (\bar{l}_i \varphi) e_j + \text{h.c.}$$

$$\langle Y_d \rangle^{ij} = y_d^{ij} \propto m_d^{ij}, \quad \langle Y_e \rangle^{ij} = y_e^{ij} \propto m_e^{ij}, \quad \langle Y_u \rangle^{ij} = (V^\dagger y_u)^{ij} \propto (V^\dagger)^{ik} m_u^{kj}$$

# Classification in SMEFT

- Operators that **break**  $U(1)^5$ : spurion insertion

- Yukawa

$$a_{u\varphi} [V^\dagger y_u]^{ij} (\varphi^\dagger \varphi) (\bar{q}_i \tilde{\varphi}) u_j$$

- Dipoles

$$a_{uW} [V^\dagger y_u]^{ij} (\bar{q}_i \tilde{\varphi}) \sigma^{\mu\nu} \tau_I u_j W_{\mu\nu}^I$$

- Right handed charged current

$$i a_{\varphi ud} [y_u V y_d]^{ij} (\tilde{\varphi}^\dagger D_\mu \varphi) (\bar{u}_i \gamma^\mu d_j)$$

- Operators that **preserve**  $U(1)^5$ : spurions parametrise departures from symmetric limit

- All other fermion currents
- 3rd generation quarks **preferentially selected** due to large Yukawas
- SMEFT  $\rightarrow$  **Flavor symmetric** + **3rd generation only** operators

$$(\bar{q}^i q^j) [\mathbb{I} + Y_u Y_u^\dagger + Y_d Y_d^\dagger + \dots]^{ij} \rightarrow (\bar{q}^i q^j) [\mathbb{I} + V^\dagger (y_u)^2 V + (y_d)^2 + \dots]^{ij}$$

$$(\bar{u}^i u^j) [\mathbb{I} + Y_u^\dagger Y_u + \dots]^{ij} \rightarrow (\bar{u}^i u^j) [\mathbb{I} + (y_u)^2 + \dots]^{ij},$$

$$(\bar{d}^i d^j) [\mathbb{I} + Y_d^\dagger Y_d + \dots]^{ij} \rightarrow (\bar{d}^i d^j) [\mathbb{I} + (y_d)^2 + \dots]^{ij},$$

# SMEFT@NLO in QCD

- MC tool for all **top/EW/Higgs** operators
- Use Warsaw basis for definiteness
  - Tools for translation between bases *[Falkowski et al.; EPJC 75 (12) 1-14]*  
[rosetta.hepforge.org](http://rosetta.hepforge.org)

## Gauge/Higgs

Higgs vev & kinetic term	$\mathcal{O}_\varphi$	$(\varphi^\dagger \varphi)^3$	–	–	
	$\mathcal{O}_{\varphi\Box}$	$(\varphi^\dagger \varphi)\Box(\varphi^\dagger \varphi)$	–	–	
$m_z$ (cust. sym.)	$\mathcal{O}_{\varphi D}$	$(\varphi^\dagger D_\mu \varphi)^\dagger (\varphi^\dagger D_\mu \varphi)$	–	–	
Gauge/Higgs & gauge kinetic terms/mixing	$\mathcal{O}_{\varphi G}$	$\varphi^\dagger \varphi G_A^{\mu\nu} G_{\mu\nu}^A$	$\mathcal{O}_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi G_A^{\mu\nu} \tilde{G}_{\mu\nu}^A$	CP violation in v2
	$\mathcal{O}_{\varphi W}$	$\varphi^\dagger \varphi W_i^{\mu\nu} W_{\mu\nu}^i$	$\mathcal{O}_{\varphi \tilde{W}}$	$\varphi^\dagger \varphi W_i^{\mu\nu} \tilde{W}_{\mu\nu}^i$	
	$\mathcal{O}_{\varphi B}$	$\varphi^\dagger \varphi B^{\mu\nu} B_{\mu\nu}$	$\mathcal{O}_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi B^{\mu\nu} \tilde{B}_{\mu\nu}$	
	$\mathcal{O}_{\varphi WB}$	$\varphi^\dagger \sigma^i \varphi W_i^{\mu\nu} B_{\mu\nu}$	$\mathcal{O}_{\varphi W \tilde{B}}$	$\varphi^\dagger \sigma^i \varphi W_i^{\mu\nu} \tilde{B}_{\mu\nu}$	
Triple gauge, ...	$\mathcal{O}_{3W}$	$\epsilon^{ijk} W_{i,\mu\nu} W_j^{\nu\rho} W_{k,\rho}^\mu$	$\mathcal{O}_{3\tilde{W}}$	$\epsilon^{ijk} \tilde{W}_{i,\mu\nu} W_j^{\nu\rho} W_{k,\rho}^\mu$	

# SMEFT@NLO in QCD

- Work in MFV hypothesis, keeping only  $y_t$  non-zero
- Validate with existing implementations where available

		3rd generation	Flavor universal
		Top	Light
Yukawa	$\mathcal{O}_{t\varphi}$	$(\varphi^\dagger \varphi) (\bar{Q} t) \tilde{\varphi}$	$\mathcal{O}_{\varphi l}^{(3)}$ $i(\varphi^\dagger \overleftrightarrow{D}_\mu^i \varphi) (\bar{l} \gamma^\mu \sigma_i l)$
Dipole	$\mathcal{O}_{tG}$	$(\bar{Q} \sigma_{\mu\nu} T^A t) \tilde{\varphi} G_A^{\mu\nu}$	$\mathcal{O}_{\varphi l}^{(1)}$ $i(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi) (\bar{l} \gamma^\mu l)$
	$\mathcal{O}_{tW}$	$(\bar{Q} \sigma_{\mu\nu} \tau^i t) \tilde{\varphi} W_i^{\mu\nu}$	$\mathcal{O}_{\varphi u}$ $i(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi) (\bar{e} \gamma^\mu e)$
	$\mathcal{O}_{tB}$	$(\bar{Q} \sigma_{\mu\nu} t) \tilde{\varphi} B^{\mu\nu}$	$\mathcal{O}_{\varphi q}^{(3)}$ $i(\varphi^\dagger \overleftrightarrow{D}_\mu^i \varphi) (\bar{q} \gamma^\mu \sigma_i q)$
Currents	$\mathcal{O}_{\varphi Q}^{(3)}$	$i(\varphi^\dagger \overleftrightarrow{D}_\mu^i \varphi) (\bar{Q} \gamma^\mu \sigma_i Q)$	$\mathcal{O}_{\varphi q}^{(1)}$ $i(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi) (\bar{q} \gamma^\mu q)$
	$\mathcal{O}_{\varphi Q}^{(1)}$	$i(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi) (\bar{Q} \gamma^\mu Q)$	$\mathcal{O}_{\varphi u}$ $i(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi) (\bar{u} \gamma^\mu u)$
	$\mathcal{O}_{\varphi t}$	$i(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi) (\bar{t} \gamma^\mu t)$	$\mathcal{O}_{\varphi d}$ $i(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi) (\bar{d} \gamma^\mu d)$
RHCC	$\mathcal{O}_{\varphi b}$	$i(\tilde{\varphi} D_\mu \varphi) (\bar{b} \gamma^\mu t)$	

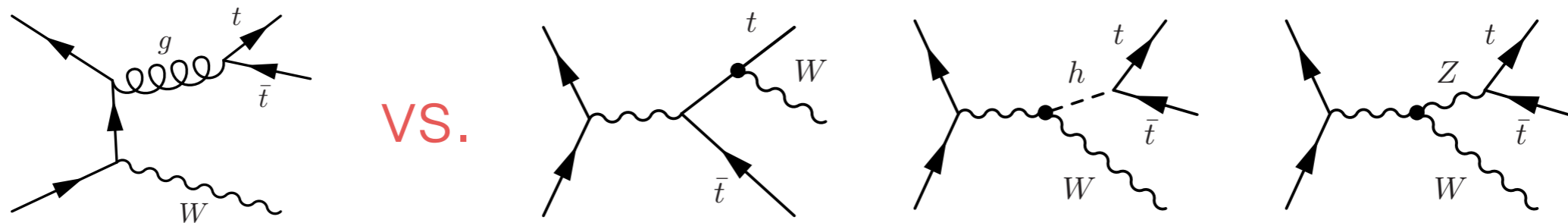


# The model

- FeynRules/NLOCT UFO implementation of above operators from Warsaw basis
- Leading MFV expansion *[Aguilar-Saavedra et al.; arXiv:1802.07237]*
  - U(2) flavor symmetry in the light quarks
  - Flavor universal 1st and 2nd gen. & no chirality flipping or RHCC bilinears
  - 3rd generation bilinears associated to the Top Yukawa
  - No CPV operators
- Omit gauge/Yukawa coupling normalisations
- Include field redefinitions needed for canonical EW sector
- 4-fermion operators: in progress

# Case study

- Processes involving top/Higgs/W/Z
  - Unitarity cancellations  $\leftrightarrow$  top mass generation mechanism
- Previous  $t\bar{t}+(W/Z/H/\gamma)$  EFT studies
  - Considered effects on dominant QCD-induced production
  - In the SM, pure EW contributions 2 orders of magnitude smaller
  - EFT effects can enhance these due to strong energy growth



- Challenging to access top/EW operators in top processes with a QCD counterpart

# Case study: $tZj/tHj$

- Alternative: require presence of a **single top** quark
  - Eliminates QCD contribution
- Single top rate at 13 TeV LHC  $\sim 200$  pb (1/4 of QCD  $tt$ )
  - Sensitive to **2 four-fermion** and **3 top/EW** operators that modify  $tbW$  vertex
- Require the presence of an additional **Z** or **Higgs**
  - Unique possibility of probing full set of top/Higgs/EW operators at once
  - Processes at the heart of EWSB sector
  - **Higher thresholds** may enhance EFT effects
- Recent LHC measurement of  $tZj$  cross section at  $4.2\sigma$ 
  - [ATLAS; arXiv:1710.03659], [CMS-PAS-TOP-16-020 & arXiv:1712.02825]*
- Timely moment to perform EFT sensitivity study in this pair of challenging processes & showcase model implementation

# Operators

tHj

tZj

both

Rescaling of  
h couplings

NLO

• $\mathcal{O}_W$	$\varepsilon_{IJK} W_{\mu\nu}^I W^{J,\nu\rho} W_{\rho}^{K,\mu}$	• $\mathcal{O}_{\varphi Q}^{(3)}$	$i(\varphi^\dagger \overleftrightarrow{D}_\mu \tau_I \varphi) (\bar{Q} \gamma^\mu \tau^I Q) + \text{h.c.}$
• $\mathcal{O}_{\varphi W}$	$(\varphi^\dagger \varphi - \frac{v^2}{2}) W_I^{\mu\nu} W_{\mu\nu}^I$	• $\mathcal{O}_{\varphi Q}^{(1)}$	$i(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi) (\bar{Q} \gamma^\mu Q) + \text{h.c.}$
• $\mathcal{O}_{\varphi WB}$	$(\varphi^\dagger \tau_I \varphi) B^{\mu\nu} W_{\mu\nu}^I$	• $\mathcal{O}_{\varphi t}$	$i(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi) (\bar{t} \gamma^\mu t) + \text{h.c.}$
• $\mathcal{O}_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^\dagger (\varphi^\dagger D_\mu \varphi)$	• $\mathcal{O}_{\varphi tb}$	$i(\tilde{\varphi} D_\mu \varphi) (\bar{t} \gamma^\mu b) + \text{h.c.}$
• $\mathcal{O}_{\varphi \square}$	$(\varphi^\dagger \varphi) \square (\varphi^\dagger \varphi)$	• $\mathcal{O}_{\varphi q}^{(1)}$	$i(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi) (\bar{q}_i \gamma^\mu q_i) + \text{h.c.}$
• $\mathcal{O}_{t\varphi}$	$(\varphi^\dagger \varphi - \frac{v^2}{2}) \bar{Q} t \tilde{\varphi} + \text{h.c.}$	• $\mathcal{O}_{\varphi q}^{(3)}$	$i(\varphi^\dagger \overleftrightarrow{D}_\mu \tau_I \varphi) (\bar{q}_i \gamma^\mu \tau^I q_i) + \text{h.c.}$
• $\mathcal{O}_{tW}$	$i(\bar{Q} \sigma^{\mu\nu} \tau_I t) \tilde{\varphi} W_{\mu\nu}^I + \text{h.c.}$	• $\mathcal{O}_{\varphi u}$	$i(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi) (\bar{u}_i \gamma^\mu u_i) + \text{h.c.}$
• $\mathcal{O}_{tB}$	$i(\bar{Q} \sigma^{\mu\nu} t) \tilde{\varphi} B_{\mu\nu} + \text{h.c.}$	• $\mathcal{O}_{Qq}^{(3,1)}$	$(\bar{q}_i \gamma_\mu \tau_I q_i) (\bar{Q} \gamma^\mu \tau^I Q)$
• $\mathcal{O}_{tG}^*$	$i(\bar{Q} \sigma^{\mu\nu} T_A t) \tilde{\varphi} G_{\mu\nu}^A + \text{h.c.}$	• $\mathcal{O}_{Qq}^{(3,8)}$	$(\bar{q}_i \gamma_\mu \tau_I T_A q_i) (\bar{Q} \gamma^\mu \tau^I T^A Q)$

Constrained by electroweak precision tests (LEP)

Two blind directions in Warsaw basis:

$$\mathcal{O}_{HW} = (D^\mu \varphi)^\dagger \tau_I (D^\nu \varphi) W_{\mu\nu}^I$$

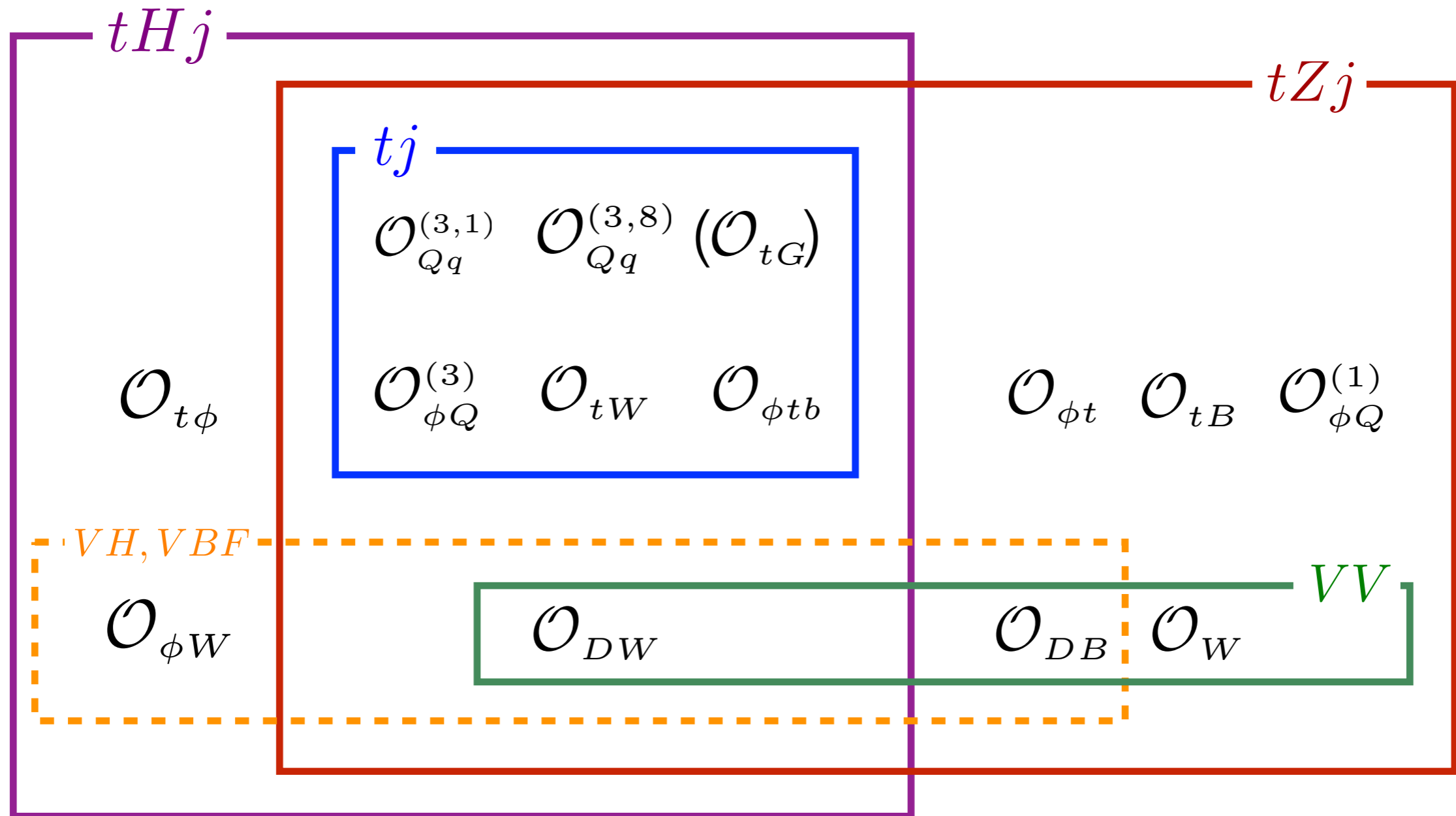
$$\mathcal{O}_{HB} = (D^\mu \varphi)^\dagger (D^\nu \varphi) B_{\mu\nu}.$$

$$\frac{dC_i(\mu)}{d \log \mu} = \frac{\alpha_s}{\pi} \gamma_{ij} C_j(\mu), \quad \gamma = \begin{pmatrix} -2 & 0 & 0 \\ 0 & 2/3 & 0 \\ 0 & 0 & 2/3 \end{pmatrix}$$

RGE

Consider these two instead to assess orthogonal sensitivity of tZj/tHj

# Interplay



(I) : Individual  
 (M) : Marginalised

[Buckley et al.; JHEP 1604 (2016) 015] [Butter et al.; JHEP 1607 (2016) 152]  
 [Alioli et al.; JHEP 1705 (2017) 086] [Zhang et al.; PRD 86 (2012) 014024]

[TeV<sup>-2</sup>]

# Existing limits

Op.	TF (I)	TF (M)	RHCC (I) tree/loop	SFitter (I)	PEWM <sup>2</sup>
$\mathcal{O}_W$				[-0.18,0.18]	
$\mathcal{O}_{HW}$				[-0.32,1.62]	
$\mathcal{O}_{HB}$				[-2.11,1.57]	
$\mathcal{O}_{\varphi W}$				[-0.39,0.33]	
$\mathcal{O}_{\varphi tb}$			[-5.28,5.28]/[-0.046,0.040]		
$\mathcal{O}_{\varphi Q}^{(3)}$	[-2.59,1.50]	[-4.19,2.00]			$-1.0 \pm 2.7$ <sup>3</sup>
$\mathcal{O}_{\varphi Q}^{(1)}$	[-3.10,3.10]				$1.0 \pm 2.7$
$\mathcal{O}_{\varphi t}$	[-9.78,8.18]				$1.8 \pm 3.8$
$\mathcal{O}_{tW}$	[-2.49,2.49]	[-3.99,3.40]			$-0.4 \pm 2.4$
$\mathcal{O}_{tB}$	[-7.09,4.68]				$4.8 \pm 10.6$
$\mathcal{O}_{tG}$	[-0.24,0.53]	[-1.07,0.99]			
$\mathcal{O}_{t\varphi}$				[-18.2,6.30]	
$\mathcal{O}_{Qq}^{(3,1)}$	[-0.40,0.60]	[0.66,1.24]			
$\mathcal{O}_{Qq}^{(3,8)}$	[-4.90,3.70]	[6.06,6.73]			

$$c_{t\varphi} \subset [-6.5, 1.3]$$

Combination of ttH @ 13 TeV

[CMS; CMS-PAS-HIG-17-003]  
 [CMS; CMS-PAS-HIG-17-004]  
 [ATLAS; CERN-EP-2017-281]

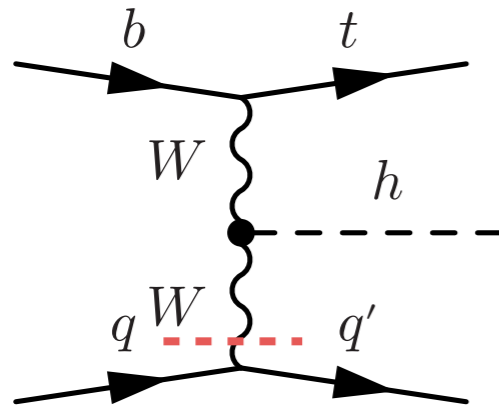
$$c_{Qq}^{(3,8)} \subset [-1.40, 1.20]$$

Combination of LHC single-top

[CMS; JHEP 12 (2012) 035]  
 [ATLAS; PRD 90 (2014) 11, 112006]  
 [CMS; JHEP 09 (2016) 027]  
 [ATLAS; JHEP 04 (2017) 086]  
 [ATLAS; EPJC 77 (2017) 8, 531]  
 [ATLAS; PLB 756 (2016) 228-246]

# SMEFT in tHj/tZj

tHj (tZj = h → Z)

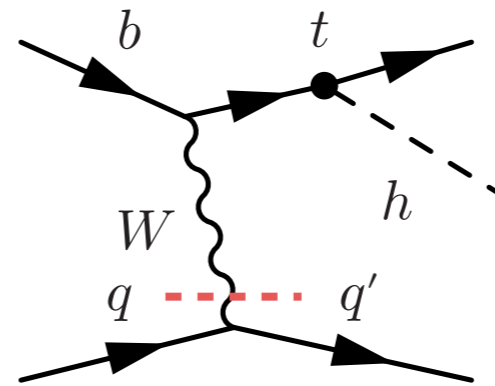


$$\mathcal{O}_{\varphi W} : \varphi^\dagger \varphi W_i^{\mu\nu} W_{\mu\nu}^i$$

HWW

TGC

$$\mathcal{O}_W : \epsilon^{ijk} W_{i,\mu\nu} W_j^{\nu\rho} W_{k,\rho}^\mu$$

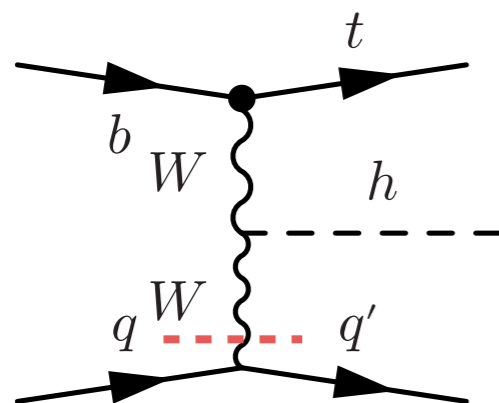


$$\mathcal{O}_{t\varphi} : (\varphi^\dagger \varphi) (\bar{Q} t) \tilde{\varphi}$$

top Yukawa

ttZ coupling

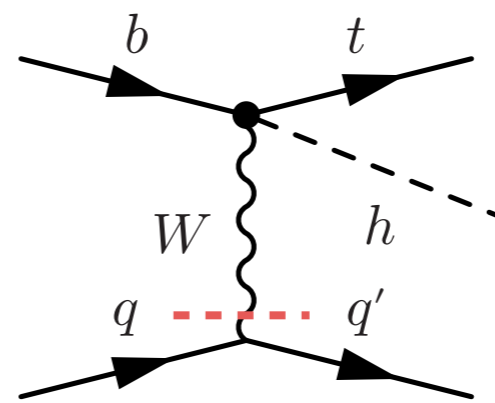
$$\mathcal{O}_{\varphi t} : i(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi) (\bar{t} \gamma^\mu t)$$



$$\mathcal{O}_{\varphi Q}^{(3)} : i(\varphi^\dagger \overleftrightarrow{D}_\mu^i \varphi) (\bar{Q} \gamma^\mu \sigma_i Q)$$

Wtb vertex

$$\mathcal{O}_{\varphi tb} : i(\tilde{\varphi} D_\mu \varphi) (\bar{b} \gamma^\mu t)$$



$$\mathcal{O}_{\varphi Q}^{(3)} : i(\varphi^\dagger \overleftrightarrow{D}_\mu^i \varphi) (\bar{Q} \gamma^\mu \sigma_i Q)$$

Contact terms

$$\mathcal{O}_{tB} : (\bar{Q} \sigma_{\mu\nu} t) \tilde{\varphi} B^{\mu\nu}$$

- Accessing the  $bW \rightarrow tH$  &  $bW \rightarrow tZ$  sub-amplitudes
  - Rich interplay between EFT operators from different sectors
  - Different energy growth and interference with the SM

# Anatomy of tHj

bW → tH

- LO helicity amplitudes
  - High energy limit:  $s \sim -t \gg v^2$
- **Maximum** energy growth
  - SU(2) triplet current
  - **Interferes** with leading SM
  - **RHCC**
  - Weak dipole
  - Fields strengths source **transverse gauge bosons**
  - Not captured by Goldstone equiv.
- **Subleading** energy growth
  - $\propto m_t$  & interferes with sub-leading SM amplitude → no growth

$\lambda_b, \lambda_W, \lambda_t$	SM	$\mathcal{O}_{t\varphi}$	$\mathcal{O}_{\varphi Q}^{(3)}$	$\mathcal{O}_{\varphi W}$	$\mathcal{O}_{tW}$	$\mathcal{O}_{HW}$
$-, 0, -$	$s^0$	$s^0$	$\frac{\sqrt{s(s+t)}}{\sqrt{2}}$	$s^0$	$s^0$	$\sqrt{s(s+t)}$
$-, 0, +$	$\frac{1}{\sqrt{s}}$	$m_t\sqrt{-t}$	$m_t\sqrt{-t}$	$\frac{1}{\sqrt{s}}$	$\frac{m_W s}{\sqrt{-t}}$	$\frac{1}{\sqrt{s}}$
$-, -, -$	$\frac{1}{\sqrt{s}}$	$\frac{1}{\sqrt{s}}$	$m_W\sqrt{-t}$	$\frac{m_W s}{\sqrt{-t}}$	$m_t\sqrt{-t}$	$\frac{m_W(s+t)}{\sqrt{-t}}$
$-, -, +$	$\frac{1}{s}$	$s^0$	$s^0$	—	$\sqrt{s(s+t)}$	$\frac{1}{s}$
$-, +, -$	$\frac{1}{\sqrt{s}}$	—	$\frac{1}{\sqrt{s}}$	$\frac{m_W(s+t)}{\sqrt{-t}}$	$\frac{1}{\sqrt{s}}$	$\frac{m_W(s+t)}{\sqrt{-t}}$
$-, +, +$	$s^0$	—	$s^0$	$s^0$	$s^0$	$\frac{1}{s}$

$\mathcal{O}_{\varphi tb}, \lambda_b = +$

$\lambda_t \backslash \lambda_W$	0	+	-
+	$\sqrt{s(s+t)}$	$m_W\sqrt{-t}$	$\frac{1}{\sqrt{s}}$
-	$m_t\sqrt{-t}$	$s^0$	$s^0$



# Anatomy of tZj

bW → tZ

$\lambda_b, \lambda_W, \lambda_t, \lambda_Z$	SM	$\mathcal{O}_{\varphi Q}^{(3)}$	$\mathcal{O}_{\varphi Q}^{(1)}$	$\mathcal{O}_{\varphi t}$	$\mathcal{O}_{tB}$	$\mathcal{O}_{tW}$	$\mathcal{O}_W$	$\mathcal{O}_{HW}$	$\mathcal{O}_{HB}$
- , 0 , - , 0	$s^0$	$\sqrt{s(s+t)}$	-	-	-	$s^0$	$s^0$	$\sqrt{s(s+t)}$	$s^0$
- , 0 , + , 0	$\frac{1}{\sqrt{s}}$	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$	$m_Z \sqrt{-t}$	$\frac{m_W(2s+3t)}{\sqrt{-t}}$	-	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$
- , - , - , 0	$\frac{1}{\sqrt{s}}$	$m_W \sqrt{-t}$	-	-	-	-	$\frac{m_W(s+2t)}{\sqrt{-t}}$	$m_W \sqrt{-t}$	$\frac{1}{\sqrt{s}}$
- , - , + , 0	$\frac{1}{s}$	$s^0$	$s^0$	$s^0$	$s^0$	$\sqrt{s(s+t)}$	$s^0$	$s^0$	$\frac{1}{\sqrt{s}}$
- , 0 , - , -	$\frac{1}{\sqrt{s}}$	$m_W \sqrt{-t}$	-	-	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$	$\frac{m_W(s+2t)}{\sqrt{-t}}$	$\frac{m_W(ss_W^2+2t)}{\sqrt{-t}}$	$\frac{m_W s}{\sqrt{-t}}$
- , 0 , - , +	$\frac{1}{\sqrt{s}}$	-	-	-	-	-	$\frac{m_W(s+t)}{\sqrt{-t}}$	$\frac{m_W(s+t)}{\sqrt{-t}}$	$\frac{m_W(s+t)}{\sqrt{-t}}$
- , 0 , + , -	$s^0$	$s^0$	$s^0$	-	-	$s^0$	$s^0$	$s^0$	$s^0$
- , 0 , + , +	$\frac{1}{s}$	$s^0$	$s^0$	$s^0$	$\sqrt{s(s+t)}$	$\sqrt{s(s+t)}$	-	$s^0$	$s^0$
- , + , - , 0	$\frac{1}{\sqrt{s}}$	-	-	-	-	-	$\frac{m_W(s+t)}{\sqrt{-t}}$	$\frac{1}{\sqrt{s}}$	$\frac{1}{\sqrt{s}}$
- , + , + , 0	$s^0$	$s^0$	-	-	-	$s^0$	-	$s^0$	$\frac{1}{s}$
- , - , - , -	$s^0$	$s^0$	$s^0$	-	$s^0$	$s^0$	$s^0$	$s^0$	$s^0$
- , - , - , +	$\frac{1}{s}$	-	-	-	-	-	$\sqrt{s(s+t)}$	$s^0$	$s^0$
- , - , + , -	$\frac{1}{\sqrt{s}}$	-	-	-	-	$\frac{m_Z(s_W^2 t - 3c_W^2(2s+t))}{\sqrt{-t}}$	-	$\frac{1}{\sqrt{s}}$	$\frac{1}{\sqrt{s}}$
- , - , + , +	-	-	-	-	$m_W \sqrt{-t}$	$m_Z \sqrt{-t}$	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$
- , + , - , -	$\frac{1}{s}$	-	-	-	-	-	$\sqrt{s(s+t)}$	$s^0$	$s^0$
- , + , - , +	$s^0$	$s^0$	$s^0$	-	-	-	-	$s^0$	$s^0$
- , + , + , -	$\frac{1}{\sqrt{s}}$	-	-	-	-	-	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$
- , + , + , +	$\frac{1}{\sqrt{s}}$	-	-	-	-	$\frac{m_W(s+t)}{\sqrt{-t}}$	-	$\frac{1}{\sqrt{s}}$	$\frac{1}{\sqrt{s}}$

$\mathcal{O}_{\varphi tb}, \lambda_b, \lambda_t = +, +$

$\lambda_Z \backslash \lambda_W$	0	+	-
0	$\sqrt{s(s+t)}$	$m_W \sqrt{-t}$	-
+	$m_Z \sqrt{-t}$	$s^0$	-
-	-	-	$s^0$

$\mathcal{O}_{\varphi tb}, \lambda_b, \lambda_t = +, -$

$\lambda_Z \backslash \lambda_W$	0	+	-
0	-	-	$s^0$
+	$s^0$	-	-
-	$s^0$	-	-

Consistent with non-interference theorem in  $2 \rightarrow 2$

[Cheung & Shen; PRL 115 (2015) 071601]  
 [Azatov, Contino & Riva; PRD 95 (2017) 065014]

# Results

- Fixed order using Madgraph5\_aMC@NLO

- NNPDF3.0 LO/NLO PDF sets
- 5-flavor scheme

$$m_t = 172.5 \text{ GeV}, \quad m_H = 125 \text{ GeV}, \quad m_Z = 91.1876 \text{ GeV}, \\ \alpha_{EW}^{-1} = 127.9, \quad G_F = 1.16637 \times 10^{-5} \text{ GeV}^{-2}.$$

- Scale choice

- t H j:  $\mu_0 = (m_H + m_t)/4$
- t Z j:  $\mu_0 = (m_Z + m_t)/4$

[Demartin, Maltoni & Mawatari; EPJC 75 (2015) 267]

- Uncertainties:

$$\sigma_{\pm \delta \mu_0 [\delta \mu_{EFT}]} \pm \delta_{PDF}$$

- 9 point variation of factorisation and renormalisation scale ( $\mu_0/2$ ,  $\mu_0$ ,  $2\mu_0$ )
- PDF uncertainties
- EFT scale variation from QCD running of operators (where relevant)

$$\sigma(\mu_0) = \sigma_{SM} + \sum_i \frac{1 \text{ TeV}^2}{\Lambda^2} C_i(\mu_0) \sigma_i(\mu_0) + \sum_{i,j} \frac{1 \text{ TeV}^4}{\Lambda^4} C_i(\mu_0) C_j(\mu_0) \sigma_{ij}(\mu_0)$$

$\sigma$ [fb]	LO	NLO	K-factor
$\sigma_{SM}$	$57.56(4)^{+11.2\%}_{-7.4\%} \pm 10.2\%$	$75.87(4)^{+2.2\%}_{-6.4\%} \pm 1.2\%$	1.32
$\sigma_{\varphi W}$	$8.12(2)^{+13.1\%}_{-9.3\%} \pm 9.3\%$	$7.76(2)^{+7.0\%}_{-6.3\%} \pm 1.0\%$	0.96
$\sigma_{\varphi W, \varphi W}$	$5.212(7)^{+10.6\%}_{-6.8\%} \pm 10.2\%$	$6.263(7)^{+2.6\%}_{-7.8\%} \pm 1.3\%$	1.20
$\sigma_{t\varphi}$	$-1.203(6)^{+12.0\%}_{-15.6\%} \pm 8.9\%$	$-0.246(6)^{+144.5[31.4]\%}_{-157.8[19.0]\%} \pm 2.1\%$	0.20
$\sigma_{t\varphi, t\varphi}$	$0.6682(9)^{+12.7\%}_{-8.9\%} \pm 9.6\%$	$0.7306(8)^{+4.6[0.6]\%}_{-7.3[0.2]\%} \pm 1.0\%$	1.09
$\sigma_{tW}$	$19.38(6)^{+13.0\%}_{-9.3\%} \pm 9.4\%$	$22.18(6)^{+3.8[0.4]\%}_{-6.8[0.9]\%} \pm 1.0\%$	1.14
$\sigma_{tW, tW}$	$46.40(8)^{+9.3\%}_{-5.5\%} \pm 11.1\%$	$71.24(8)^{+7.4[1.5]\%}_{-14.0[6.9]\%} \pm 1.9\%$	1.54
$\sigma_{\varphi Q^{(3)}}$	$-3.03(3)^{+0.0\%}_{-2.2\%} \pm 15.4\%$	$-10.04(4)^{+11.1\%}_{-8.9\%} \pm 1.8\%$	3.31
$\sigma_{\varphi Q^{(3)}, \varphi Q^{(3)}}$	$11.23(2)^{+9.4\%}_{-5.6\%} \pm 11.2\%$	$15.28(2)^{+5.0\%}_{-10.9\%} \pm 1.8\%$	1.36
$\sigma_{\varphi tb}$	0	0	—
$\sigma_{\varphi tb, \varphi tb}$	$2.752(4)^{+9.4\%}_{-5.5\%} \pm 11.3\%$	$3.768(4)^{+5.0\%}_{-10.9\%} \pm 1.8\%$	1.54
$\sigma_{HW}$	$-3.526(4)^{+5.6\%}_{-9.5\%} \pm 10.9\%$	$-5.27(1)^{+6.5\%}_{-2.9\%} \pm 1.5\%$	1.50
$\sigma_{HW, HW}$	$0.9356(4)^{+7.9\%}_{-4.0\%} \pm 12.3\%$	$1.058(1)^{+4.8\%}_{-11.9\%} \pm 2.3\%$	1.13
$\sigma_{tG}$		$-0.418(5)^{+12.3\%}_{-9.8\%} \pm 1.1\%$	—
$\sigma_{tG, tG}$		$1.413(1)^{+21.3\%}_{-30.6\%} \pm 2.5\%$	—
$\sigma_{Qq^{(3,1)}}$	$-22.50(5)^{+8.0\%}_{-11.8\%} \pm 9.7\%$	$-20.10(5)^{+13.8\%}_{-13.3\%} \pm 1.1\%$	0.89
$\sigma_{Qq^{(3,1)}, Qq^{(3,1)}}$	$69.78(3)^{+8.0\%}_{-4.1\%} \pm 12.1\%$	$62.20(3)^{+11.5\%}_{-15.9\%} \pm 2.3\%$	0.89
$\sigma_{Qq^{(3,8)}}$	—	$0.25(3)^{+25.4\%}_{-27.1\%} \pm 4.7\%$	—
$\sigma_{Qq^{(3,8)}, Qq^{(3,8)}}$	$15.53(2)^{+8.0\%}_{-4.1\%} \pm 12.1\%$	$14.07(2)^{+11.0\%}_{-15.7\%} \pm 2.1\%$	0.91

K-factors **not universal**

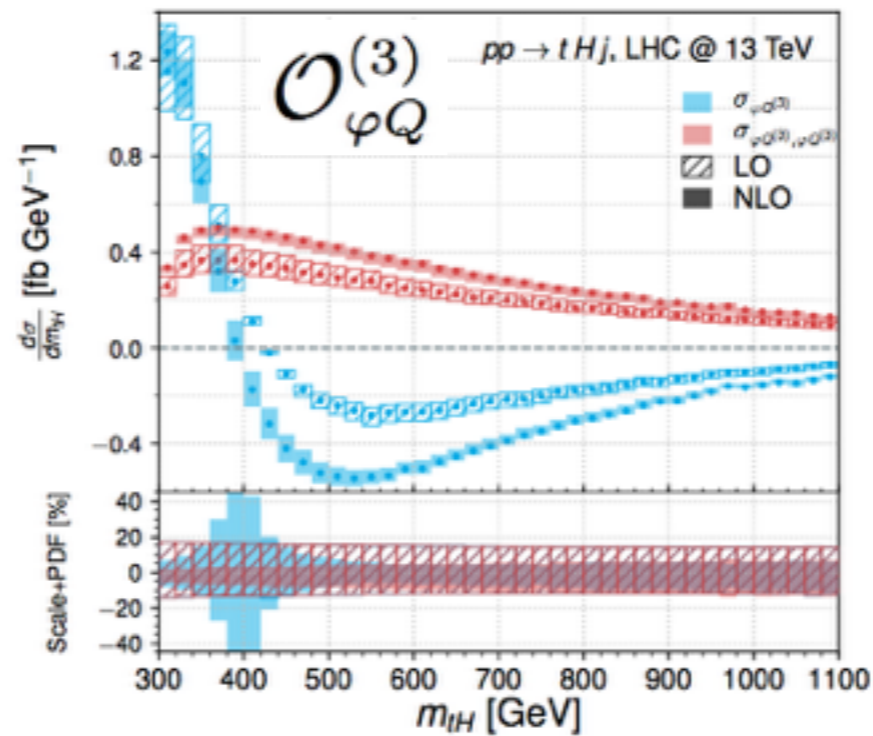
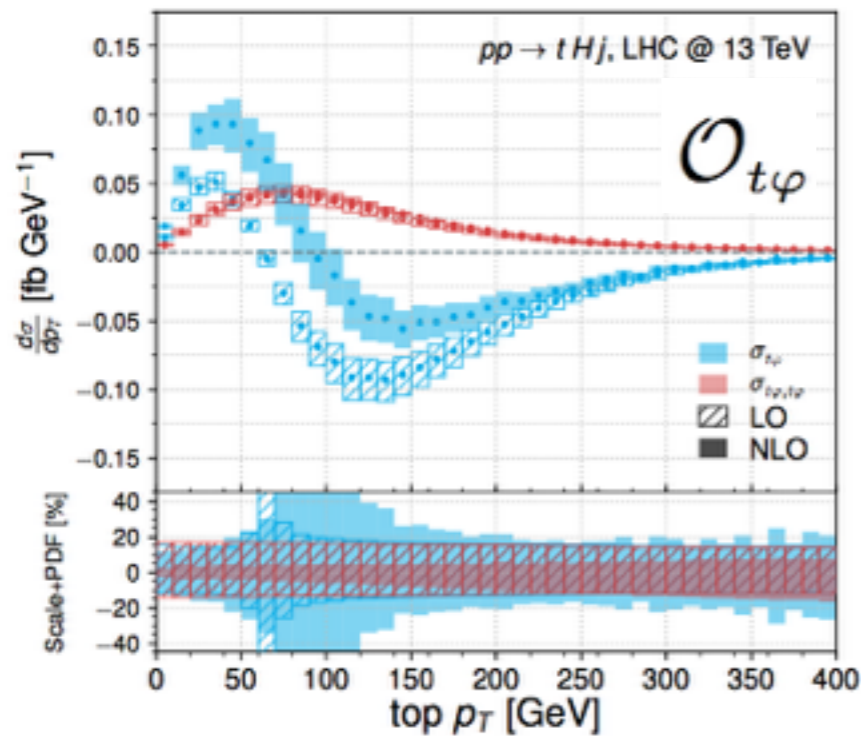
**Reduction** of QCD scale/PDF uncertainties

EFT scale uncertainty **subdominant**

Some very **strong dependence** on EFT operators

O(> 1) deviations within current direct bounds

# Inclusive results: $tHj$



Cancellations over the PS appear/disappear for the interference contributions.

- Between top and antitop
- Strange  $K$ -factors
- Large scale uncert.

$\sigma_{ij}$	$C_{\phi W}$	$C_{t\phi}$	$C_{tW}$	$C_{\phi Q}^{(3)}$	$C_{HW}$	$C_{u31}$	$C_{u38}$
$C_{\phi W}$	—	2.752 (1.29)	12.88 (0.61)	6.384 (0.65)	-0.43 (-0.17)	—	—
$C_{t\phi}$	2.514 (1.35)	—	-1.912 (-0.27)	-4.168 (-1.25)	-0.699 (-0.80)	—	—
$C_{tW}$	10.54 (0.68)	-1.772 (-0.32)	—	-26.24 (-0.79)	3.988 (0.46)	—	—
$C_{\phi Q}^{(3)}$	5.12 (0.67)	-3.584 (-1.31)	-11.2 (-0.49)	—	4.864 (1.21)	—	—
$C_{HW}$	-0.402 (-0.18)	-0.6138 (-0.78)	3.124 (0.47)	3.5784 (1.10)	—	—	—
$C_{u31}$	-13.475 (-0.71)	5.16 (0.76)	-19.1 (-0.34)	-15.44 (-0.55)	-6.96 (-0.86)	—	4.525 (0.15)
$C_{u38}$	—	—	—	—	—	—	—

$\sigma$ [fb]	LO	NLO	K-factor
$\sigma_{SM}$	660.8(4) $^{+13.7\%}_{-9.6\%} \pm 9.7\%$	839.1(5) $^{+1.1\%}_{-5.1\%} \pm 1.0\%$	1.27
$\sigma_W$	-7.87(7) $^{+8.4\%}_{-12.6\%} \pm 9.7\%$	-8.77(8) $^{+8.5\%}_{-4.3\%} \pm 1.1\%$	1.12
$\sigma_{W,W}$	34.58(3) $^{+8.2\%}_{-3.9\%} \pm 13.0\%$	43.80(4) $^{+6.6\%}_{-15.1\%} \pm 2.8\%$	1.27
$\sigma_{tB}$	2.23(2) $^{+14.7[0.9]\%}_{-10.7[1.0]\%} \pm 9.4\%$	2.94(2) $^{+2.3[0.4]\%}_{-3.0[0.7]\%} \pm 1.1\%$	1.32
$\sigma_{tB,tB}$	2.833(2) $^{+10.5[1.7]\%}_{-6.3[1.9]\%} \pm 11.1\%$	4.155(3) $^{+4.7[0.9]\%}_{-10.1[1.4]\%} \pm 1.7\%$	1.47
$\sigma_{tW}$	2.66(4) $^{+18.8[0.9]\%}_{-15.3[1.0]\%} \pm 11.4\%$	13.0(1) $^{+15.8[2.1]\%}_{-22.8[0.0]\%} \pm 1.2\%$	4.90
$\sigma_{tW,tW}$	48.16(4) $^{+10.0[1.7]\%}_{-5.8[1.9]\%} \pm 11.3\%$	80.00(4) $^{+7.9[1.3]\%}_{-14.7[1.6]\%} \pm 1.9\%$	1.66
$\sigma_{\varphi dtR}$	4.20(1) $^{+14.9\%}_{-10.9\%} \pm 9.3\%$	4.94(2) $^{+3.4\%}_{-6.7\%} \pm 1.0\%$	1.18
$\sigma_{\varphi dtR,\varphi dtR}$	0.3326(3) $^{+13.6\%}_{-9.5\%} \pm 9.6\%$	0.4402(5) $^{+3.7\%}_{-9.3\%} \pm 1.0\%$	1.32
$\sigma_{\varphi Q}$	14.98(2) $^{+14.5\%}_{-10.5\%} \pm 9.4\%$	18.07(3) $^{+2.3\%}_{-1.6\%} \pm 1.0\%$	1.21
$\sigma_{\varphi Q,\varphi Q}$	0.7442(7) $^{+14.1\%}_{-10.0\%} \pm 9.5\%$	1.028(1) $^{+2.8\%}_{-7.3\%} \pm 1.0\%$	1.38
$\sigma_{\varphi Q(3)}$	130.04(8) $^{+13.8\%}_{-9.8\%} \pm 9.5\%$	161.4(1) $^{+0.9\%}_{-4.8\%} \pm 1.0\%$	1.24
$\sigma_{\varphi Q(3),\varphi Q(3)}$	17.82(2) $^{+11.7\%}_{-7.5\%} \pm 10.5\%$	23.98(2) $^{+3.7\%}_{-9.3\%} \pm 1.4\%$	1.35
$\sigma_{\varphi tb}$	0	0	-
$\sigma_{\varphi tb,\varphi tb}$	2.949(2) $^{+10.5\%}_{-6.2\%} \pm 11.1\%$	4.154(4) $^{+5.1\%}_{-11.2\%} \pm 1.8\%$	1.41
$\sigma_{HW}$	-5.16(6) $^{+7.8\%}_{-12.0\%} \pm 10.5\%$	-6.88(8) $^{+6.4\%}_{-2.0\%} \pm 1.4\%$	1.33
$\sigma_{HW,HW}$	0.912(2) $^{+9.4\%}_{-5.2\%} \pm 12.0\%$	1.048(2) $^{+5.2\%}_{-12.8\%} \pm 2.1\%$	1.15
$\sigma_{HB}$	-3.015(9) $^{+9.9\%}_{-13.9\%} \pm 9.5\%$	-3.76(1) $^{+5.2\%}_{-1.0\%} \pm 1.0\%$	1.25
$\sigma_{HB,HB}$	0.02324(6) $^{+12.7\%}_{-8.5\%} \pm 9.9\%$	0.02893(6) $^{+2.3\%}_{-7.5\%} \pm 1.1\%$	1.24
$\sigma_{tG}$		0.45(2) $^{+93.0\%}_{-148.8\%} \pm 4.9\%$	-
$\sigma_{tG,tG}$		2.251(4) $^{+20.9\%}_{-30.0\%} \pm 2.5\%$	-
$\sigma_{Qq(3,1)}$	-393.5(5) $^{+8.1\%}_{-12.3\%} \pm 10.0\%$	-498(1) $^{+8.9\%}_{-3.2\%} \pm 1.2\%$	1.26
$\sigma_{Qq(3,1),Qq(3,1)}$	462.25(3) $^{+8.4\%}_{-4.1\%} \pm 12.7\%$	545.50(5) $^{+7.4\%}_{-17.4\%} \pm 2.9\%$	1.18
$\sigma_{Qq(3,8)}$	0	-0.9(3) $^{+23.3\%}_{-26.3\%} \pm 19.2\%$	-
$\sigma_{Qq(3,8),Qq(3,8)}$	102.73(5) $^{+8.4\%}_{-4.1\%} \pm 12.7\%$	111.18(5) $^{+9.3\%}_{-18.4\%} \pm 2.8\%$	1.08

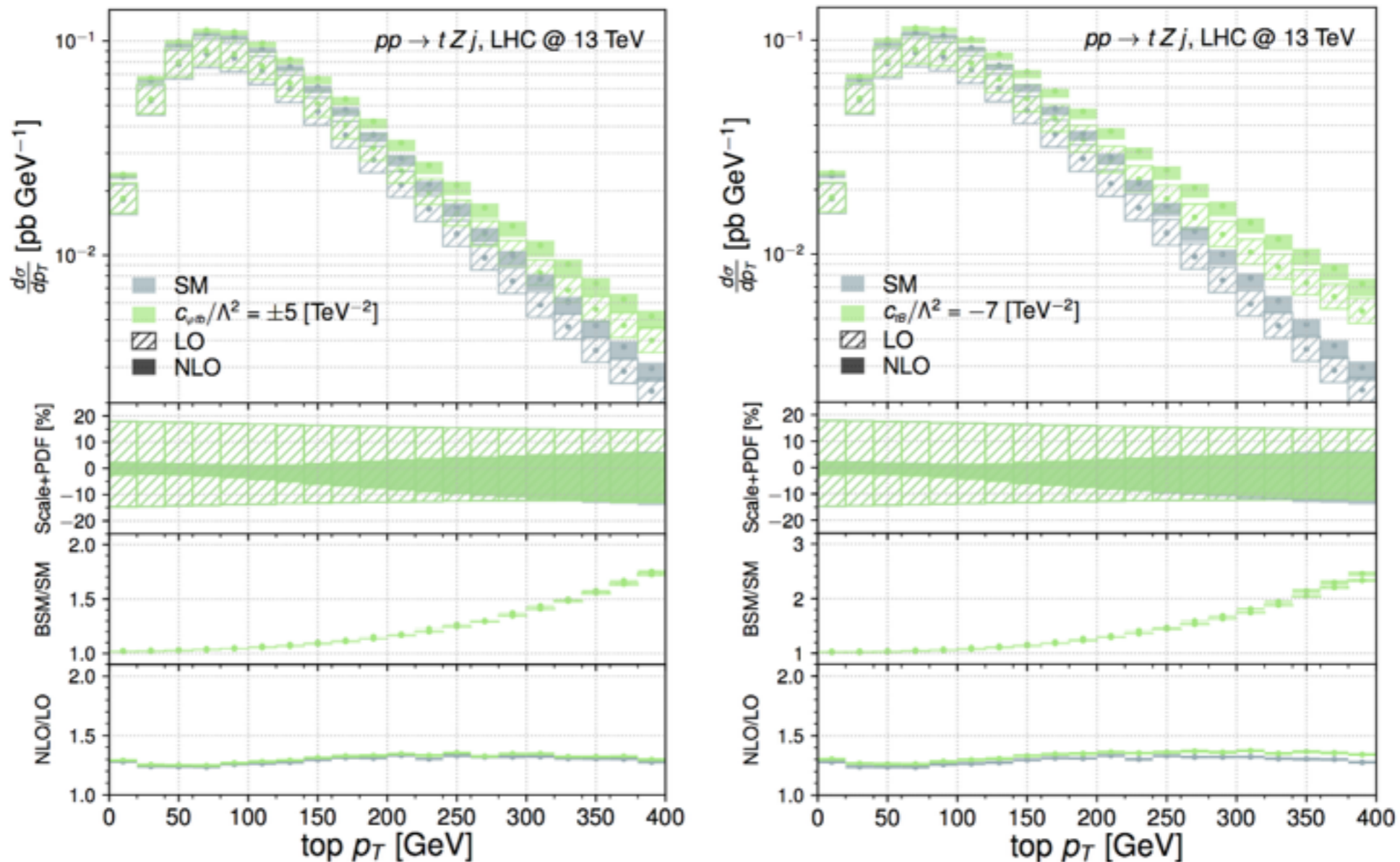
$tZj \sim 10$  times bigger than  $tHj$

NLO corrections: similar features to  $tHj$

EFT contributions smaller relative to SM

Higgs always radiated from top/EW gauge boson  
 Z boson can also come from light quark leg

# Differential results in $tZj$



Potentially large deviations in the tails (saturating current limits)  
 $tHj$  process is very rare, differential results not likely at LHC

# LHC sensitivity

Usual EFT story: looking at **high energy tails** increases sensitivity  
 Important to put into context **w.r.t single top** which has a much larger rate

$r = \sigma_i / \sigma_{SM}$	$tj$	$tj$	$tZj$	$tZj$	$tHj$
		$(p_T^t > 350 \text{ GeV})$		$(p_T^t > 250 \text{ GeV})$	
$\sigma_{SM}$	224 pb	880 fb	839 fb	69 fb	75.9 fb
$r_{tW}$	0.028	0.024	0.0156	0.0104	0.292
$r_{tW,tW}$	0.016	0.356	0.096	0.672	0.940
$r_{\varphi Q^{(3)}}$	0.120	0.120	0.192	0.686	-0.132
$r_{\varphi Q^{(3)},\varphi Q^{(3)}}$	0.0037	0.0037	0.023	0.28	0.21
$r_{\varphi tb,\varphi tb}$	0.00090	0.0008	0.0050	0.00052	0.050
$r_{tG}$	0.0003	-0.01	0.00053	-0.0048	-0.0055
$r_{tG,tG}$	0.00062	0.045	0.0027	0.022	0.025
$r_{Qq^{(3,1)}}$	-0.353	-4.4	-0.595	-2.22	-0.39
$r_{Qq^{(3,1)},Qq^{(3,1)}}$	0.126	11.5	0.70	5.08	1.21
$r_{Qq^{(3,8)},Qq^{(3,8)}}$	0.0308	2.73	0.16	1.01	1.08

Increased sensitivity for **dipoles, RHCC**

Consistent with  $2 \rightarrow 2$  subamplitude analysis

New energy growth in  $tZj$  for **SU(2) current** w.r.t **single top**

Single top should eventually outperform  $tHj/tZj$  for **four fermion operators**

# Current sensitivity

- Gauge sensitivity of these processes at LHC
- Recent measurements of  $tZj$  at CMS & ATLAS
  - Signal strengths  $0.75 \pm 0.27$  &  $1.31 \pm 0.47$  *[CMS; PLB 779 (2018) 358-384]*
  - Cast into naive ‘confidence intervals’ *[ATLAS; CERN-EP-2017-188]*
  - Ignore acceptance effects & contribution of operators to bkg processes
  - Which include  $tW$ ,  $ttV$ ,  $ttH$ ,  $tWZ$ ,  $tHW$  !
- CMS analysis of  $tHj + tHW + ttH$  *[CMS-PAS-HIG-17-005]*

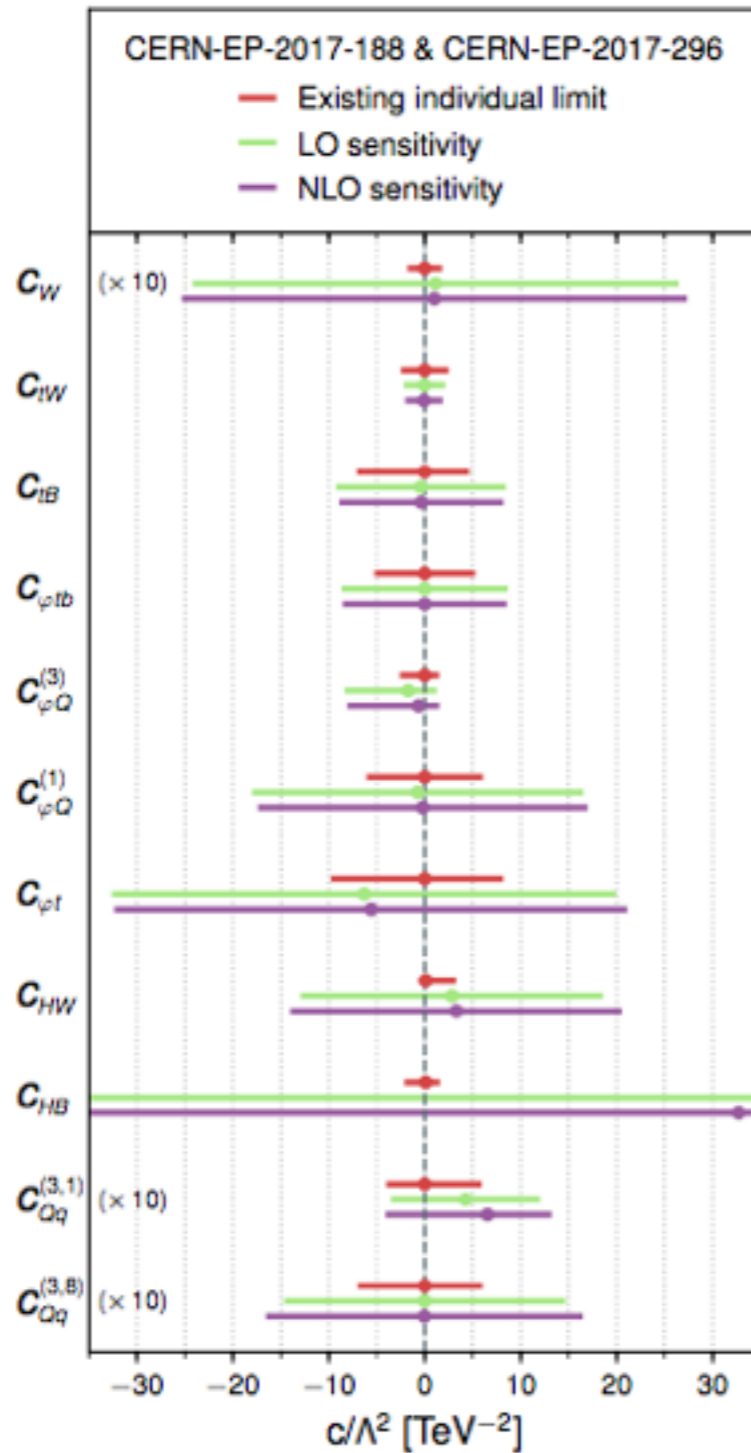
- Combined signal strength  $1.8 \pm 0.67$
- Take into account only modifications to  $tZj$
- Except top Yukawa operator contribution to  $ttH$

$\sigma$ [fb]	LO	NLO
$t H j$	57.5	75.9
$t \bar{t} H$	464	507
$t H W$	14.5	15.9

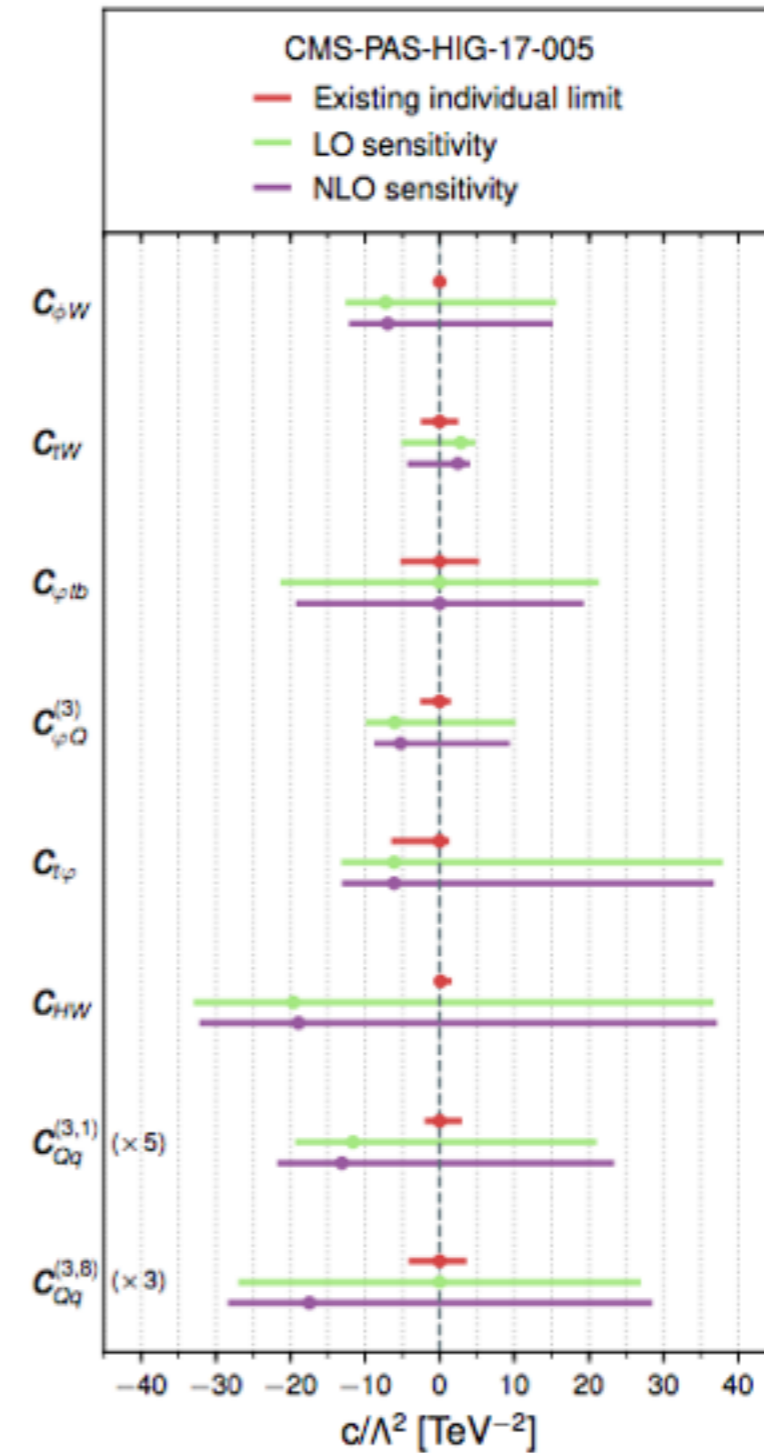


# Current sensitivity

tZj



tHj

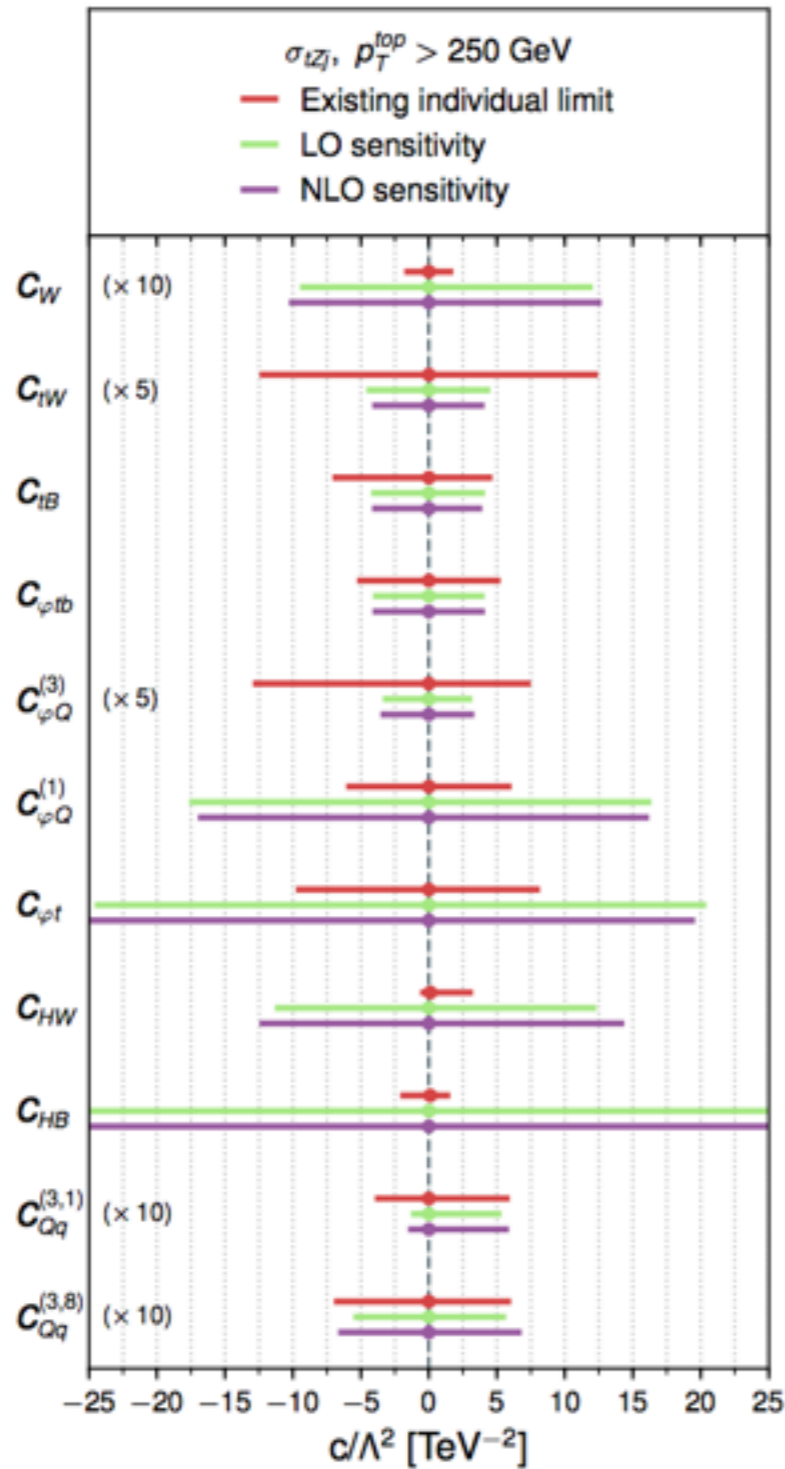


# Future sensitivity

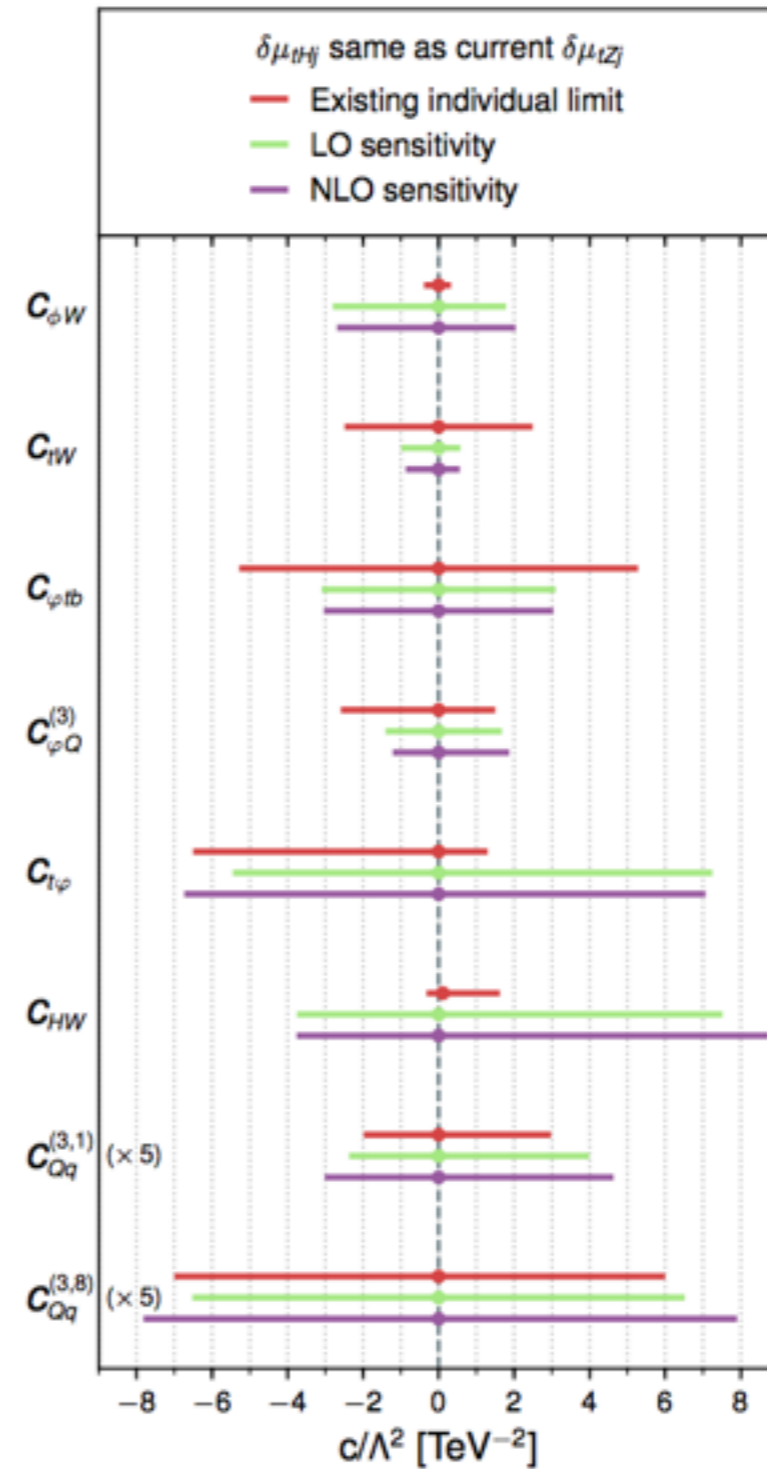
- tZj: take high top  $p_T$  region  $> 250$  GeV
  - 10x smaller cross section  $\rightarrow$  end of Run II or HL-LHC
- tHj: assume it is measured with the current tZj precision
  - tHj inclusive cross section is similar to the high  $p_T$  tZj cross section
  - target for HL-LHC
- Start to improve on existing limits for certain operators
  - Dipoles, RHCC, (top Yukawa)
- NLO predictions increase sensitivity
  - Bring theory uncertainties down below experimental stat. and syst.

# Future sensitivity

tZj



tHj



# Global top/Higgs/EW

- Several interesting  $2 \rightarrow 2$  sub-amplitudes & processes

$bW \rightarrow tH : tHj$

$bW \rightarrow tZ : tZj$

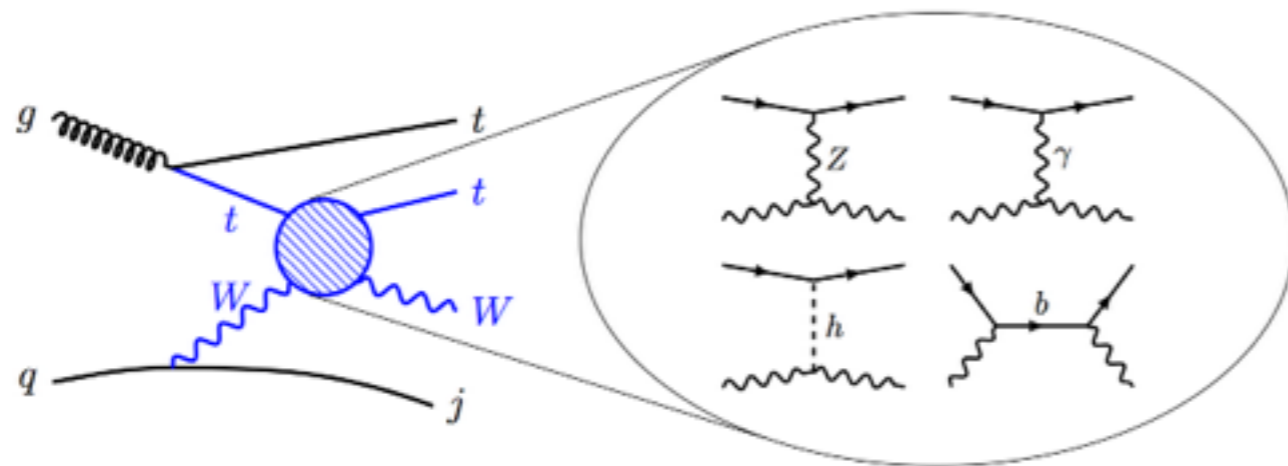
$tW \rightarrow tW : ttW$  (EW)

$tZ \rightarrow tH : ttH$  (EW)

$tZ \rightarrow tZ : ttZ$

$tH \rightarrow tH : ?$

- Possibly access higher energies by *e.g.*  $ttW+j$



Similar operators contribute to all of these

[Dror et al.; JHEP 01 (2016) 071]

# Top/Higgs/EW EFT @ LHC

- Clear that a **global effort** must be undertaken
- **Individual** measurements of these processes may not easily lend themselves to EFT interpretation
- *e.g.* CMS measurement of  $ttW/ttZ$  cross section ratio  
[CMS-PAS-TOP-17-005]
  - “Backgrounds”:  $ttH$ ,  $tqZ$ ,  $tHq$ ,...
- Global fits to LHC top quark observables [Buckley et al.; PRD 92 (2016) 9 091501]
  - top pair, single top (s+t channel),  $ttZ$ ,  $tt\gamma$
  - Extension to top/Higg/EW sector will be a valuable exercise
  - SMEFTatNLO model implementation a necessary ingredient
- Model public soon

# Conclusion

- Presented a FeynRules/NLOCT UFO implementation of top/EW/Higgs sector in SMEFT
  - Leading MFV expansion to select **top quark** operators
  - Allows for NLOQCD+PS predictions for **any relevant process** in, *e.g.*, MG5
- Fixed order NLO predictions for **tZj** & **tHj** in SMEFT at LHC
  - Challenging process that showcases implementation
  - Related to mass generation/unitarity cancellations in SM
  - Complete predictions for large operator set → can be used in fits
- Current & future LHC sensitivity study
  - New energy growth in SU(2) current op.
  - Interesting future sensitivity at high energy to dipoles, RHCC, 4F ops.

Thank you

# ttH in SMEFT

$$\mathcal{O}_{t\phi} = (\varphi^\dagger \varphi) (\bar{Q}_L \tilde{\varphi} t_R)$$

$(\mathcal{O}_{t\phi}, \mathcal{O}_{\phi G}, \mathcal{O}_{tG})$

$$\mathcal{O}_{\phi G} = (\varphi^\dagger \varphi) G_{\mu\nu}^A G_A^{\mu\nu}$$

$$\frac{dC_i(\mu)}{d \log \mu} = \frac{\alpha_s}{\pi} \gamma_{ij} C_j(\mu) \quad \gamma = \begin{pmatrix} -2 & 16 & 8 \\ 0 & -7/2 & 1/2 \\ 0 & 0 & 1/3 \end{pmatrix}$$

$$\mathcal{O}_{tG} = (\bar{Q}_L \sigma_{\mu\nu} T^A t_R) \tilde{\varphi} G_A^{\mu\nu}$$

- Operators involving the **top/Higgs/gluon**
  - $gg \rightarrow H$  &  $tt$  production partly constrain the Wilson coefficient space
  - $ttH$  is the only direct probe of the Top-Higgs interaction
  - In principle 3-gluon  $\mathcal{O}_G$  and 4 fermion operators also contribute but turn out to be better constrained by  $tt$  and multi-jet measurements
- **Different K-factors** among SM/dim-6 operators
- **Large  $\Lambda^{-4}$  effects** in both shape & normalisation
  - Scenarios where “EFT-squared” terms are large but energy is below cutoff

$$\frac{E^2}{\Lambda^2} < 1 < c_i^{(6)} \frac{E^2}{\Lambda^2} < c_i^{(6)} c_j^{(6)} \frac{E^4}{\Lambda^4}$$



# EFT scale dependence

- Set of running/mixing EFT couplings
  - Additional source of theoretical uncertainty
  - Like with  $\alpha_s$ , can be estimated by scale variation

$$C_i(\mu) = \Gamma_{ij}(\mu, \mu_0) C_j(\mu_0) \quad \Gamma_{ij}(\mu, \mu_0) = \exp \left( \frac{-2}{\beta_0} \log \frac{\alpha_s(\mu)}{\alpha_s(\mu_0)} \gamma_{ij} \right)$$

$$\beta_0 = 11 - 2/3 n_f ,$$

$$\sigma(\mu_0) = \sigma_{SM} + \sum_i \frac{1\text{TeV}^2}{\Lambda^2} C_i(\mu_0) \sigma_i(\mu_0) + \sum_{i,j} \frac{1\text{TeV}^4}{\Lambda^4} C_i(\mu_0) C_j(\mu_0) \sigma_{ij}(\mu_0)$$

$\mu_0 \rightarrow \mu$

$$\sigma(\mu) = \sigma_{SM} + \sum_i \frac{1\text{TeV}^2}{\Lambda^2} C_i(\mu) \sigma_i(\mu) + \sum_{i,j} \frac{1\text{TeV}^4}{\Lambda^4} C_i(\mu) C_j(\mu) \sigma_{ij}(\mu)$$

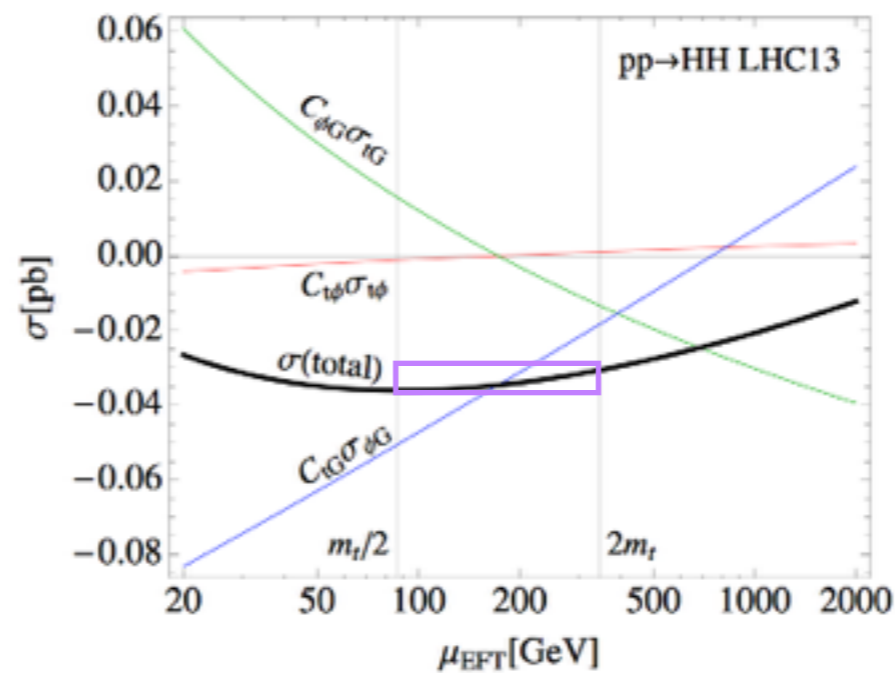
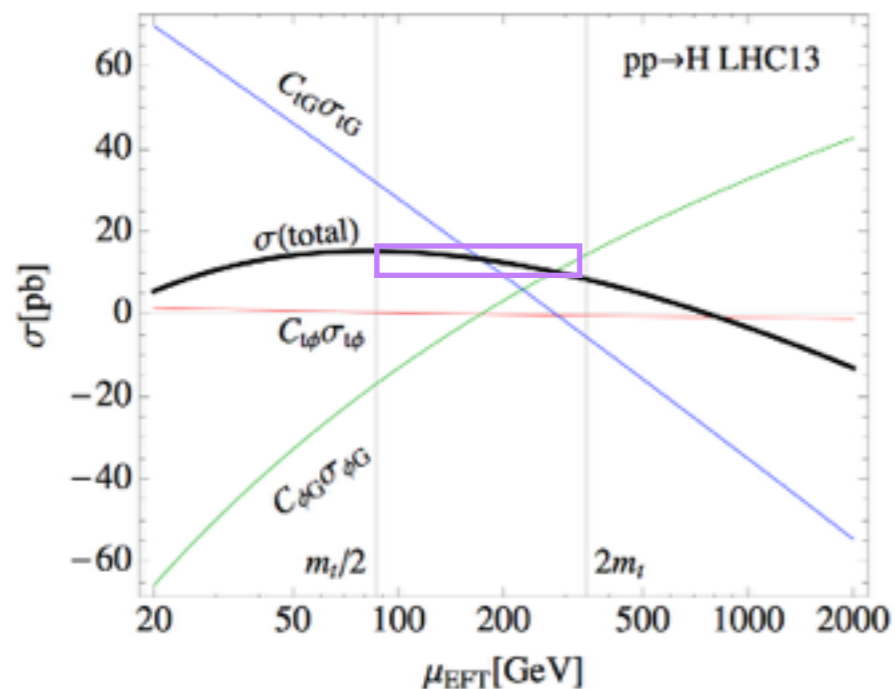
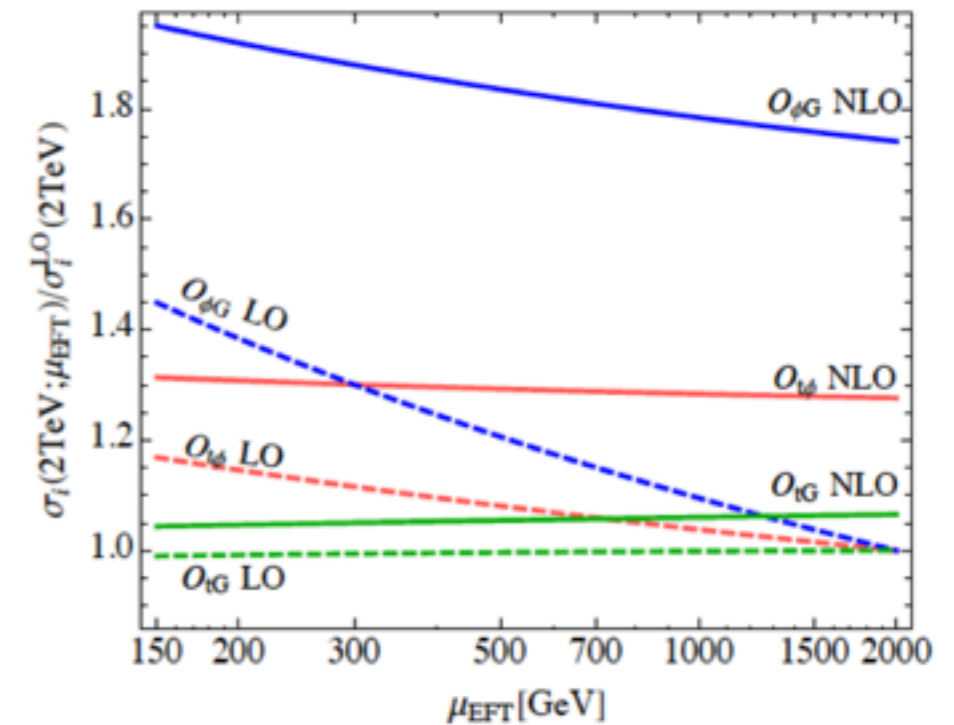
$$= \sigma_{SM} + \sum_i \frac{1\text{TeV}^2}{\Lambda^2} C_i(\mu_0) \sigma_i(\mu_0; \mu) + \sum_{i,j} \frac{1\text{TeV}^4}{\Lambda^4} C_i(\mu_0) C_j(\mu_0) \sigma_{ij}(\mu_0; \mu)$$

$$\sigma_i(\mu_0; \mu) = \Gamma_{ji}(\mu, \mu_0) \sigma_j(\mu) ,$$

$$\sigma_{ij}(\mu_0; \mu) = \Gamma_{ki}(\mu, \mu_0) \Gamma_{lj}(\mu, \mu_0) \sigma_{kl}(\mu)$$

# EFT scale dependence

- Full NLO stable under scale variation
- Large finite effects: RG improved underestimates NLO
- Scale uncertainty estimate
  - Take  $c_i$  defined at scales  $2\mu_0$  &  $\mu_0/2$  and run back to the central scale



$\delta\mu_{\text{EFT}}$ :  
Does not cancel in  
e.g. cross section  
ratios

## SMEFT - 'EW' sector

$X^3$		$\varphi^6$ and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
$Q_G$	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_\varphi$	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi\Box}$	$(\varphi^\dagger \varphi)\Box(\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$
$Q_W$	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$
$Q_{\tilde{W}}$	$\varepsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$				
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eW}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eB}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$
$Q_{\varphi \tilde{W}}$	$\varphi^\dagger \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uW}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu q_r)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	$Q_{uB}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	$Q_{dG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_p \gamma^\mu u_r)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	$Q_{dW}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$
$Q_{\varphi \tilde{W}B}$	$\varphi^\dagger \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	$Q_{dB}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$

'Warsaw' basis [Grzadkowski et al.; JHEP 1010 (2010) 085]

## SMEFT - 4 fermions

$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
$Q_{ll}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	$Q_{ee}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	$Q_{le}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{uu}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{lu}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{dd}$	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{ld}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{eu}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{qe}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{ed}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		$B$ -violating			
$Q_{ledq}$	$(\bar{l}_p^j e_r)(\bar{d}_s^k q_t^j)$	$Q_{duq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{j k l} [(d_p^\alpha)^T C u_r^\beta] [(q_s^\gamma)^T C l_t^k]$		
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{j k l} (\bar{q}_s^k d_t^l)$	$Q_{qqqu}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{j k l} [(q_p^\alpha)^T C q_r^\beta] [(u_s^\gamma)^T C e_t^l]$		
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{j k l} (\bar{q}_s^k T^A d_t^l)$	$Q_{qqqq}^{(1)}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{j k l m n} [(q_p^\alpha)^T C q_r^\beta] [(q_s^\gamma)^T C l_t^m]$		
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{j k l} (\bar{q}_s^k u_t^l)$	$Q_{qqqq}^{(3)}$	$\varepsilon^{\alpha\beta\gamma} (\tau^I \varepsilon)_{j k l} (\tau^I \varepsilon)_{m n} [(q_p^\alpha)^T C q_r^\beta] [(q_s^\gamma)^T C l_t^m]$		
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{j k l} (\bar{q}_s^k \sigma^{\mu\nu} u_t^l)$	$Q_{duu}$	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t^l]$		

Flavour indices  
= most of the 2499!

[Grzadkowski et al.; JHEP 1010 (2010) 085]

# Non-interference

- Alternatively, one may have  $\sigma^{(6)}_i < \sigma^{(6)}_{ij}$ 
  - **Non-interference** by e.g. helicity selection rules in the high energy limit
- High energy theorem
  - Many  $2 \rightarrow 2$  amplitudes involving **at least one transverse gauge boson** mediated by D=6 operators do not interfere with the SM

[Cheung & Shen; PRL 115 (2015) 071601]

[Azatov, Contino & Riva; PRD 95 (2017) 065014]

Total Helicity

Interference?

$A_4$	$ h(A_4^{\text{SM}}) $	$ h(A_4^{\text{BSM}}) $
VVVV	0	4,2
VV $\phi\phi$	0	2
VV $\psi\psi$	0	2
V $\psi\psi\phi$	0	2
$\psi\psi\psi\psi$	2,0	2,0
$\psi\psi\phi\phi$	0	0
$\phi\phi\phi\phi$	0	0

X

✓

V = Transverse vector

$\phi$  = Longitudinal vector or Higgs

$\psi$  = Fermion

$p p \rightarrow ZH, WH, WW, WZ$

Interference can be recovered:

finite mass effects

higher order corrections

higher multiplicity ( $2 \rightarrow 3, 4, \dots$ )

[Panico, Riva & Wulzer; CERN-TH-2017-85]

45 [Azatov, et al. LHEP 1710 (2017) 027]