Constraining certain Higgs EFT couplings at the HL-LHC and beyond

Shankha Banerjee IPPP, Durham University

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Based on

Phys. Rev. D 89, 053010 (2014)

(with S. Mukhopadhyay and B.Mukhopadhyaya)

JHEP 1502 (2015) 128

(with G. Amar, S. Buddenbrock, A. Cornell, T.Mandal, B.Mellado and B. Mukhopadhyaya)

JHEP 1509 (2015) 057

(with T. Mandal, B. Mellado and B. Mukhopadhyaya)

ongoing work

(with R. S. Gupta, C. Englert and M. Spannowsky)

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The story so far

- The nature of the discovered boson is more or less consistent with the SM Higgs
- Its combined (CMS + ATLAS) mass, from run-I data, is measured to be $M_h = 125.09 \pm 0.21$ (stat.) ± 0.11 (syst.) GeV in the $h \rightarrow \gamma\gamma$ and the $h \rightarrow ZZ^* \rightarrow 4\ell$ channels
- A CP-even spin zero hypothesis is favoured
- If it is "the Higgs", then its mass has fixed the SM
- Still to be measured: $h \rightarrow Z\gamma$, $h \rightarrow \mu^+\mu^-$, y_t , λ_{hhh}
- Till a reliable measurement of self-coupling is available it is best to consider the available final states that reflect the Higgs couplings

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Signal strengths (7 + 8 TeV @ 25 fb⁻¹)

Final states



Production modes



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Introduction

- Many reasons to go beyond the SM, *viz.* gauge hierarchy, neutrino mass, dark matter, baryon asymmetry etc.
- Plethora of BSM theories
- Two phenomenological approaches:
 - Model dependent: study the signatures of each model individually
 - *Model independent:* low energy effective theory formalism analogous to Fermi's theory of beta decay
- $\bullet\,$ The SM here is a low energy effective theory valid below a cut-off scale $\Lambda\,$
- \bullet A bigger theory is assumed to supersede the SM above the scale Λ
- At the perturbative level, all heavy (> Λ) DOF are decoupled from the low energy theory (Appelquist-Carazzone theorem)
- \bullet Appearance of HD operators in the effective Lagrangian valid below Λ

$$\mathcal{L} = \mathcal{L}_{SM}^{d=4} + \sum_{d \ge 5} \sum_{i} \frac{f_i}{\Lambda^{d-4}} \mathcal{O}_i^d$$
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HD operators

- Higher-dimensional Operators: invariant under SM gauge group
- d = 5: Unique operator \rightarrow Majorana mass to the neutrinos: $\frac{1}{\Lambda} (\Phi^{\dagger} L)^{T} C (\Phi^{\dagger} L)$
- d = 6: 59 = 15 + 19 + 25 independent operators. Lowest dimension (after d = 4) which induces HVV interactions [W. Buchmuller and D. Wyler; B. Grzadkowski, M. Iskrzynski, M. Misiak and J. Rosiek; K.Hagiwara, D. Zeppenfeld et. al.]
- d = 7: Such operators appear in Higgs portal dark matter models
- d = 8: Lowest dimension inducing neutral TGC interactions
- To understand the EWSB sector better, we first consider a subset of d = 6 operators involving Φ, ∂_μΦ, X_{μν} (where X = G, B, W)

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Gauge-invariant D6 CP⁺ operators : Higgs-Gauge sector

• The operators containing the Higgs doublet Φ and its derivatives:

$$\mathcal{O}_{\Phi,1} = (D_\mu \Phi)^\dagger \Phi \Phi^\dagger (D^\mu \Phi); \quad \mathcal{O}_{\Phi,2} = rac{1}{2} \partial_\mu (\Phi^\dagger \Phi) \partial^\mu (\Phi^\dagger \Phi); \quad \mathcal{O}_{\Phi,3} = rac{1}{3} (\Phi^\dagger \Phi)^3$$

$$\mathcal{O}_{GG} = \Phi^{\dagger} \Phi G^{a}_{\mu\nu} G^{a\,\mu\nu}; \quad \mathcal{O}_{BW} = \Phi^{\dagger} \hat{B}_{\mu\nu} \hat{W}^{\mu\nu} \Phi; \quad \mathcal{O}_{WW} = \Phi^{\dagger} \hat{W}_{\mu\nu} \hat{W}^{\mu\nu} \Phi$$
$$\mathcal{O}_{W} = (D_{\mu} \Phi)^{\dagger} \hat{W}^{\mu\nu} (D_{\nu} \Phi); \quad \mathcal{O}_{BB} = \Phi^{\dagger} \hat{B}_{\mu\nu} \hat{B}^{\mu\nu} \Phi; \quad \mathcal{O}_{B} = (D_{\mu} \Phi)^{\dagger} \hat{B}^{\mu\nu} (D_{\nu} \Phi),$$
$$\hat{W}^{\mu\nu} = i \frac{g}{2} \sigma_{a} W^{a\,\mu\nu}, \quad \hat{B}^{\mu\nu} = i \frac{g}{2} B^{\mu\nu}; \quad g, g' : SU(2)_{L}, \quad U(1)_{Y} \text{ gauge couplings}$$
$$V^{a}_{\mu\nu} = \partial_{\mu} W^{a}_{\nu} - \partial_{\nu} W^{a}_{\mu} - g \epsilon^{abc} W^{b}_{\mu} W^{c}_{\nu}; \qquad B_{\mu\nu} = \partial_{\mu} B_{\nu} - \partial_{\nu} B_{\mu}$$
$$\mathcal{G}^{a}_{\mu\nu} = \partial_{\mu} G^{a}_{\nu} - \partial_{\nu} G^{a}_{\mu} - g_{s} f^{abc} G^{b}_{\mu} G^{c}_{\nu}$$

 Φ : Higgs doublet, $D_{\mu}\Phi = (\partial_{\mu} + \frac{i}{2}g'B_{\mu} + ig\frac{\sigma_a}{2}W^a_{\mu})\Phi$: Covariant derivative

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Properties of these operators

- $\mathcal{O}_{\Phi,1}$: Custodial symmetry violated \rightarrow severely constrained by *T*-parameter
- O_{Φ,2}: Custodial symmetry preserved; modifies SM HVV couplings by multiplicative factors (same Lorentz structure)
- O_{Φ,3}: Modifies only the Higgs self-interaction; gives additional contribution to the Higgs potential
- \mathcal{O}_{GG} : Introduces *HGG* coupling with same Lorentz structure as in the SM; constrained from single Higgs production
- \mathcal{O}_{BW} : Drives tree-level $Z \leftrightarrow \gamma$ mixing \rightarrow highly constrained by EWPT
- O_{WW}, O_W, O_{BB}, O_B: Modifies the HVV couplings by introducing new Lorentz structures in the Lagrangian; not all are severely constrained by the EWPT

Effective Lagrangian

$$\mathcal{L} = \beta \left(\frac{2m_W^2}{v} H W_{\mu}^+ W^{\mu-} + \frac{m_Z^2}{v} H Z_{\mu} Z^{\mu} \right) + \sum_i \frac{f_i}{\Lambda^2} \mathcal{O}_i$$

$$\begin{split} \mathcal{L}_{eff} \supset g_{HWW}^{(1)} & (W_{\mu\nu}^{+} W^{-\mu} \partial^{\nu} H + h.c.) + g_{HWW}^{(2)} HW_{\mu\nu}^{+} W^{-\mu\nu} \\ & + g_{HZZ}^{(1)} Z_{\mu\nu} Z^{\mu} \partial^{\nu} H + g_{HZZ}^{(2)} HZ_{\mu\nu} Z^{\mu\nu} \\ & + g_{HZ\gamma}^{(1)} A_{\mu\nu} Z^{\mu} \partial^{\nu} H + g_{HZ\gamma}^{(2)} HA_{\mu\nu} Z^{\mu\nu} + g_{H\gamma\gamma} HA_{\mu\nu} A^{\mu\nu}; \end{split}$$

$$g_{HWW}^{(1)} = \left(\frac{gM_W}{\Lambda^2}\right) \frac{f_W}{2}; \quad g_{HWW}^{(2)} = -\left(\frac{gM_W}{\Lambda^2}\right) f_{WW}$$

$$g_{HZZ}^{(1)} = \left(\frac{gM_W}{\Lambda^2}\right) \frac{c^2 f_W + s^2 f_B}{2c^2}; \quad g_{HZZ}^{(2)} = -\left(\frac{gM_W}{\Lambda^2}\right) \frac{s^4 f_{BB} + c^4 f_{WW}}{2c^2}$$

$$g_{HZ\gamma}^{(1)} = \left(\frac{gM_W}{\Lambda^2}\right) \frac{s(f_W - f_B)}{2c}; \quad g_{HZ\gamma}^{(2)} = \left(\frac{gM_W}{\Lambda^2}\right) \frac{s(s^2 f_{BB} - c^2 f_{WW})}{c}$$

$$g_{H\gamma\gamma} = -\left(\frac{gM_W}{\Lambda^2}\right) \frac{s^2(f_{BB} + f_{WW})}{2}$$

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Anomalous charged TGC interactions

We also consider the anomalous VVV interactions by

$$\mathcal{L}_{WWV} = -ig_{WWV} \{ g_1^V \left(W_{\mu\nu}^+ W^{-\mu} V^{\nu} - W_{\mu}^+ V_{\nu} W^{-\mu\nu} \right) \\ + \kappa_V W_{\mu}^+ W_{\nu}^- V^{\mu\nu} + \frac{\lambda_V}{M_W^2} W_{\mu\nu}^+ W^{-\nu\rho} V_{\rho}^{\mu} \}$$

where $g_{WWV} = g s$, $g_{WWZ} = g c$, $\kappa_V = 1 + \Delta \kappa_V$ and $g_1^Z = 1 + \Delta g_1^Z$ with

$$\begin{split} \Delta \kappa_{\gamma} &= \frac{M_W^2}{2\Lambda^2} \left(f_W + f_B \right); \quad \lambda_{\gamma} = \lambda_Z = \frac{3g^2 M_W^2}{2\Lambda^2} f_{WWW} \\ \Delta g_1^Z &= \frac{M_W^2}{2c^2\Lambda^2} f_W; \quad \Delta \kappa_Z = \frac{M_W^2}{2c^2\Lambda^2} \left(c^2 f_W - s^2 f_B \right) \end{split}$$

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Modified efficiencies: Case study $(pp \rightarrow Hjj \rightarrow WW^*jj)$

We consider the H → WW* + 2j, WW* → l⁺νl⁻ν̄ (l = {e, μ}) channel which includes contributions from both VBF and VH production modes.

 $\epsilon_{WW^*+\geq 2-\text{jets}} = \frac{50.98\beta^4 + 121.76\beta^3 f_{WW} + 22.85\beta^2 f_{WW}^2 + 0.15\beta f_{WW}^3 + 0.01 f_{WW}^4}{1601.43\beta^4 + 3796.63\beta^3 f_{WW} + 666.79\beta^2 f_{WW}^2 - 1.98\beta f_{WW}^3 + 0.73 f_{WW}^4}$



• Percentage modification of the combined efficiency of all cuts compared to the SM case. Grey region : $\epsilon_{BSM} = \epsilon_{SM}$

Phenomenology at e^+e^- colliders

Two main Higgs production processes are



- $e^+e^-
 ightarrow
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 u} H$ process ightarrow admixture of s and t-channel processes
- Possible to separate s and t-channel from $e^+e^- \rightarrow \nu \bar{\nu} H$ events by applying

$$E_{H}$$
-cut: $\left|E_{H}-\frac{S+M_{H}^{2}-M_{Z}^{2}}{2\sqrt{S}}\right| \leq \Delta(=5 \text{ GeV})$

• $\Delta \sim \Delta E_{jet}$ where $\Delta E_{jet}/E_{jet} \lesssim 0.3/\sqrt{E_{jet}}$. For two *b*-jets each with energy ~100 GeV, $\Delta E_{jet} = \sqrt{2 \times (0.3 \times \sqrt{100})^2} \sim 4 \text{ GeV}$

The amplitudes : An example



$$M = i(\frac{gM_W}{c})[\beta g^{\alpha\beta} + T^{\alpha\beta}]$$

$$T^{\alpha\beta} = \frac{1}{2\Lambda^2 c} \{ 4(s^4 f_{BB} + c^4 f_{WW}) [g^{\alpha\beta}(k_1 \cdot k_2) - k_2^{\alpha} k_1^{\beta}] + (c^2 f_W + s^2 f_B) \\ \times [-g^{\alpha\beta}(k_1^2 + k_2^2 + 2k_1 \cdot k_2) + (k_1^{\alpha} k_1^{\beta} + 2k_2^{\alpha} k_1^{\beta} + k_2^{\alpha} k_2^{\beta})] \}$$

M_{e⁺e⁻→ZH} is a linear combination of x_i ∈ {β, f_{WW}, f_W, f_{BB}, f_B}
 Cross-section can always be expressed as a bilinear combination

$$\sigma_{ZH}(\sqrt{S}, x_i) = \sum_{i, j=1}^{5} x_i C_{ij}(\sqrt{S}) x_j$$

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Fitted cross-sections

$$\sigma(\sqrt{S}) = \mathcal{X} \cdot \mathcal{M}(\sqrt{S}) \cdot \mathcal{X}^{\mathsf{T}}$$

where $\mathcal{X} = (\beta, f_{WW}, f_W, f_{BB}, f_B)$ is a row vector on parameter-space

$$\mathcal{M}^{s}_{ZH}(300 \ GeV) = \begin{pmatrix} 181.67 & -6.43 & -2.99 & -0.51 & -0.71 \\ -6.43 & 0.46 & 0.18 & -0.03 & -0.08 \\ -2.99 & 0.18 & 0.14 & -0.02 & -0.06 \\ -0.51 & -0.03 & -0.02 & 0.02 & 0.03 \\ -0.71 & -0.08 & -0.06 & 0.03 & 0.08 \end{pmatrix}$$

$$\mathcal{M}_{\nu\bar{\nu}H}^{t}(300 \; GeV) = \begin{pmatrix} 15.36 & 0.04 & 0.07 \\ 0.04 & 1.2 \times 10^{-3} & -7.7 \times 10^{-4} \\ 0.07 & -7.7 \times 10^{-4} & 4.6 \times 10^{-4} \end{pmatrix}$$

• σ^s is less sensitive on \mathcal{O}_{BB} and \mathcal{O}_B but σ^t is almost insensitive to HDOs



Benchmark points: $BP1 = \{1, 0, 5, 0, 0\}$, $BP2 = \{1, 0, -5, 0, 0\}$ (allowed by *EWPT* constraints and *LHC* data)



- In the SM: $\sigma_{ZH} \sim 1/S$ and $\sigma^t_{\nu\bar{\nu}H} \sim \ln(S/M_H^2)$
- In presence of HDOs, the √S-dependency is non-trivial especially for the s-channel process

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θ_H distributions

Benchmark points: $BP3 = \{1, -3, 8, -4, 3\}$ (allowed by *EWPT* constraints and *LHC* data)



Varying two parameters at the same time

Two parameters are varied keeping others fixed ($\sqrt{S} = 300$ GeV). Brown patches signify $\sigma_{SM} \pm \sigma_{SM} \times 10\%$



Estimating D6 coefficients at the HL-LHC

- The HD operator coefficients are constrained to values of $\mathcal{O}(1)/\text{TeV}^2$
- Kinematic variables can show very little variations *w.r.t.* the *SM* for such small coefficients
- One may construct observables sensitive to even small values of the operator coefficients
- Cross-sections and decay widths are sensitive observables
- If we construct ratios, many correlated uncertainties get cancelled

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The ratio \mathcal{R}_1

$$\begin{split} \mathcal{R}_{1}(f_{i}) &= \frac{\sigma_{\text{ggF}} \times \text{BR}_{H \to \gamma \gamma}(f_{i})}{\sigma_{\text{ggF}} \times \text{BR}_{H \to WW^{*} \to 2\ell 2\nu}(f_{i})} \\ \mathcal{R}_{1}(f_{i}) &= \frac{\mu_{\gamma \gamma}^{\text{ggF}}(f_{i})}{\mu_{WW^{*}}^{\text{ggF}}(f_{i})} \times \frac{(\sigma_{\text{ggF}} \times \text{BR}_{H \to \gamma \gamma})^{\text{SM}}}{(\sigma_{\text{ggF}} \times \text{BR}_{H \to WW^{*} \to 2\ell 2\nu})^{\text{SM}}} \end{split}$$

- Strong bounds on O_{WW} and O_{BB}; insensitive to the other two operators O_W and O_B
- $f_{WW} \approx f_{BB}$ allowed region $\approx [-2.76, -2.65] \cup [-0.06, 0.04]$ TeV⁻²



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The ratio \mathcal{R}_2

$$\mathcal{R}_{2}(f_{i}) = rac{\sigma_{\mathrm{VBF}}(f_{i}) imes \mathrm{BR}_{H
ightarrow \gamma \gamma}(f_{i})}{\sigma_{\mathrm{WH}}(f_{i}) imes \mathrm{BR}_{H
ightarrow \gamma \gamma}(f_{i}) imes \mathrm{BR}_{W}}$$

- We consider the bounds from \mathcal{R}_1 for \mathcal{O}_{WW} and see that even such small values can be probed at 14 TeV HL - LHC
- f_{WW}/Λ^2 excluded region : [-1.96, +1.62] TeV⁻², f_W/Λ^2 excluded region : [-2.10, +2.50] TeV⁻²



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The ratio \mathcal{R}_3

$$\mathcal{R}_{3}(f_{i}) = \frac{\sigma_{\mathrm{ggF}} \times \mathrm{BR}_{H \to Z\gamma \to 2\ell\gamma}(f_{i})}{\sigma_{\mathrm{ggF}} \times \mathrm{BR}_{H \to WW^{*} \to 2\ell 2\nu}(f_{i})}$$

- \mathcal{O}_B sensitive only to the ZZ^* and $Z\gamma$ channels.
- Sensitivity to ZZ^* is negligible. Sensitivity to $Z\gamma$ is strong, but $H \rightarrow Z\gamma$ is not yet measured.
- Projected bounds f_B/Λ^2 is [-8.44, -7.17] \cup [-0.72, +0.56] TeV⁻².



Constraining TGC couplings with $pp \rightarrow ZH$ at the HL-LHC

- We have seen from LEP that measuring the oblique S, T parameters can constrain several BSM scenarios at much higher scales than the LEP running energy
- Many vertices ensuing from EFT operators are correlated and hence LEP has already constrained certain operators affecting the Higgs vertices
- We target the higher energy regions in the parameter space in order to compete with the LEP constraints [See Rick's slides for more details]

Constraining TGC couplings with $pp \rightarrow ZH$ at the HL-LHC

$$\begin{split} \Delta \mathcal{L}_{6} &\supset \sum_{f} \delta g_{f}^{Z} Z_{\mu} \bar{f} \gamma^{\mu} f + \delta g_{ud}^{W} (W_{\mu}^{+} \bar{u}_{L} \gamma^{\mu} d_{L} + h.c.) \\ &+ g_{VV}^{h} h \left[W^{+\mu} W_{\mu}^{-} + \frac{1}{2c_{\theta_{W}}^{2}} Z^{\mu} Z_{\mu} \right] + \delta g_{ZI}^{h} h \frac{Z^{\mu} Z_{\mu}}{2c_{\theta_{W}}^{2}} \\ &+ \sum_{f} g_{ZII}^{h} \frac{h}{v} Z_{\mu} \bar{f} \gamma^{\mu} f + g_{Wud}^{h} \frac{h}{v} (W_{\mu}^{+} \bar{u}_{L} \gamma^{\mu} d_{L} + h.c.) \\ &+ \kappa_{Z\gamma} \frac{h}{v} A^{\mu\nu} Z_{\mu\nu} + \kappa_{WW} \frac{h}{v} W^{+\mu\nu} W_{\mu\nu}^{-} + \kappa_{ZZ} \frac{h}{2v} Z^{\mu\nu} Z^{\mu\nu} Z_{\mu\nu} \end{split}$$

Constraining TGC couplings with $pp \rightarrow ZH$ at the HL-LHC

At high energies, the following four directions in the EFT parameter space are isolated by ZH production

$$\begin{array}{lll} g^{h}_{Zu_{L}u_{L}} &=& -\frac{g}{c_{\theta_{W}}} \left((c^{2}_{\theta_{W}} + \frac{s^{2}_{\theta_{W}}}{3}) \delta g^{Z}_{1} + W - \frac{t^{2}_{\theta_{W}}}{3} (\hat{S} - \delta \kappa_{\gamma} - Y) \right) \\ g^{h}_{Zd_{L}d_{L}} &=& -\frac{g}{c_{\theta_{W}}} \left((c^{2}_{\theta_{W}} - \frac{s^{2}_{\theta_{W}}}{3}) \delta g^{Z}_{1} + W + \frac{t^{2}_{\theta_{W}}}{3} (\hat{S} - \delta \kappa_{\gamma} - Y) \right) \\ g^{h}_{Zu_{R}u_{R}} &=& \frac{4gs^{2}_{\theta_{W}}}{3c^{3}_{\theta_{W}}} (\hat{S} - \delta \kappa_{\gamma} + c^{2}_{\theta_{W}} \delta g^{Z}_{1} - Y) \\ g^{h}_{Zd_{R}d_{R}} &=& -\frac{2gs^{2}_{\theta_{W}}}{3c^{3}_{\theta_{W}}} (\hat{S} - \delta \kappa_{\gamma} + c^{2}_{\theta_{W}} \delta g^{Z}_{1} - Y) \end{array}$$

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$pp \rightarrow ZH$ at high energies

- We study the impact of constraining TGC couplings at higher energies
- We study the channel $pp \rightarrow ZH \rightarrow \ell^+ \ell^- b\bar{b}$
- The backgrounds are SM $pp \rightarrow ZH, Zb\bar{b}, t\bar{t}$ and the fake $pp \rightarrow Zjj$ $(j \rightarrow b)$ fake rate taken as 2%)
- Major background *Zbb*
- Boosted substructure analysis with fat-jets of R = 1.5 used



$pp \rightarrow Zh$ at high energies

• Next we perform a two-parameter χ^2 -fit (at 300 fb⁻¹) to find the allowed region in the $\delta g_1^Z - (\delta \kappa_\gamma - \hat{S})$



Grey region: LEP exclusion; pink band: exclusion from *WZ* [Franceschini, Panico, Pomarol, Riva and Wulzer, 2017];

Green (blue) region: exclusion from ZH with only interference (interference plus squared) term

Summary and conclusions

- EFT framework is a powerful tool to understand Higgs coupling deviations and nature of the Higgs (part of a doublet or not?)
- Efficiencies for various acceptance cuts are altered by varying Lorentz structure
- Future e^+e^- colliders can potentially constrain EFT parameters to excellent precision
- Various ratios can be used to see the effect of small values of operator coefficients → cancellation of several uncertainties
- Possible to constrain certain EFT parameters to stronger degrees at HL-LHC than was done at LEP
- Boosted ZH channel helps in constraining TGC couplings

Backup: Ranges of $\mathcal{R}_1, \mathcal{R}_2$ and \mathcal{R}_3

Observable	\mathcal{O}_{WW}	\mathcal{O}_{BB}	\mathcal{O}_W	\mathcal{O}_B
	[-3.32, -2.91]	[-3.32, -2.91]	Not	Not
\mathcal{R}_1 @ 7+8 TeV	U	U	bounded	bounded
	[+0.12, +0.57]	[+0.12, +0.57]		
	[-2.76, -2.65]	[-2.76, -2.65]	Not	Not
\mathcal{R}_1 @ 14 TeV	U	U	bounded	bounded
	[-0.06, +0.04]	[-0.06, +0.04]		
R ₂ @ 14 TeV	[-1.96, +1.62]	Not	[-2.10, +2.50]	Not
		bounded		bounded
	Not	Not	Not	[-8.44, -7.17]
\mathcal{R}_3 @ 14 TeV	used	used	used	U
				[-0.72, +0.56]

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Backup

$$\begin{array}{lll} g^{h}_{Zu_{L}u_{L}} & = & -\frac{g}{c_{\theta_{W}}} \left((c^{2}_{\theta_{W}} + \frac{s^{2}_{\theta_{W}}}{3}) \delta g^{Z}_{1} + W - \frac{t^{2}_{\theta_{W}}}{3} (\hat{S} - \delta \kappa_{\gamma} - Y) \right) \\ g^{h}_{Zd_{L}d_{L}} & = & -\frac{g}{c_{\theta_{W}}} \left((c^{2}_{\theta_{W}} - \frac{s^{2}_{\theta_{W}}}{3}) \delta g^{Z}_{1} + W + \frac{t^{2}_{\theta_{W}}}{3} (\hat{S} - \delta \kappa_{\gamma} - Y) \right) \\ g^{h}_{Zu_{R}u_{R}} & = & \frac{4gs^{2}_{\theta_{W}}}{3c^{2}_{\theta_{W}}} (\hat{S} - \delta \kappa_{\gamma} + c^{2}_{\theta_{W}} \delta g^{Z}_{1} - Y) \\ g^{h}_{Zd_{R}d_{R}} & = & -\frac{2gs^{2}_{\theta_{W}}}{3c^{2}_{\theta_{W}}} (\hat{S} - \delta \kappa_{\gamma} + c^{2}_{\theta_{W}} \delta g^{Z}_{1} - Y) \\ \end{array}$$

$$\begin{split} g^{h}_{Zu_{L}u_{L}} &= -\frac{g}{c_{\theta_{W}}} \frac{m_{W}^{2}}{\Lambda^{2}} (c_{W} + c_{HW} - c_{2W} - \frac{t_{\theta_{W}}}{3} (c_{B} + c_{HB} - c_{2B})) \\ g^{L}_{Zd_{L}d_{L}} &= -\frac{g}{c_{\theta_{W}}} \frac{m_{W}^{2}}{\Lambda^{2}} (c_{W} + c_{HW} - c_{2W} + \frac{t_{\theta_{W}}^{2}}{3} (c_{B} + c_{HB} - c_{2B})) \\ g^{h}_{Zu_{R}u_{R}} &= -\frac{4g}{3} \frac{s_{\theta_{W}}^{2}}{3c_{\theta_{W}}^{2}} \frac{m_{W}^{2}}{\Lambda^{2}} (c_{B} + c_{HB} - c_{2B}) \\ g^{h}_{Zd_{R}d_{R}} &= -\frac{2g}{3} \frac{s_{\theta_{W}}^{2}}{3c_{\theta_{W}}^{2}} \frac{m_{W}^{2}}{\Lambda^{2}} (c_{B} + c_{HB} - c_{2B}) \end{split}$$

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