

New AdS/CFT duals through non-Abelian T-duality

Yolanda Lozano (U. Oviedo)

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Universidad de Oviedo

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In this talk we will use NATD to generate new AdS_6 and AdS_4 backgrounds

We will analyze the dual CFTs and provide an interpretation for the running of the non-compact direction

AdS_6 : AdS_6 backgrounds are quite unique (“no-go” theorem) (Passias’12; Apruzzi, Fazzi, Passias, Ross, Tomasiello’14)

Dual to 5d CFT’s (fixed point theories with interesting properties)

(Seiberg’96; Intriligator, Morrison, Seiberg’97)

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AdS_4 : Dual to 3d CFT

AdS_4 IIB background with N=2 SUSY not in Lüst, Tsimpis’09

Interesting realization in the CFT of the running of the non-compact direction generated by NATD:

Spectral flow (Y.L., Macpherson, arXiv:1408.0912)

I. Non-Abelian T-duality in AdS/CFT

- In 4 dim:

Sfetsos & Thompson'10:

$$AdS_5 \times S^5 \xrightarrow[\substack{\text{Uplift to} \\ \text{11 dim}}]{\text{NATD}} \text{Gaiotto \& Maldacena geometries} \\ (\text{dual to Gaiotto's N=2 SCFTs})$$

Itsios, Nuñez, Sfetsos & Thompson'13:

$$AdS_5 \times T^{1,1} \xrightarrow[\substack{\text{Uplift to} \\ \text{11 dim}}]{\text{NATD}} \text{Bah, Beem, Bobev, Wecht sols.} \\ (\text{dual to N=1 SCFTs (Sicilian quivers} \\ \text{(Benini, Tachikawa, Wecht) ..)})$$

$$\text{Non-conformal} \quad \xrightarrow{\text{NATD}} \quad \begin{aligned} & \text{(MN, KT, KS)} & \text{New geometries in massive IIA} \\ & & \text{Confining quarks, domain walls,} \\ & & \text{Seiberg duality,...} \end{aligned}$$

(Nuñez, Gaillard, Macpherson, Sfetsos, Thompson, Cáceres, Barranco (13-14)..)

- In 5 dim: Y.L., O Colgain, Rodriguez-Gomez, Sfetsos'12;
Y.L., O Colgain, Rodriguez-Gomez'13

$$AdS_6 \times S^4 \xrightarrow{\text{NATD}} \begin{array}{l} \text{New } AdS_6 \text{ geometry in IIB} \\ \text{Dual CFT quiver with two nodes} \end{array}$$

- In 3 dim: Y.L., Macpherson'14

$$AdS_4 \times CP^3 \xrightarrow{\text{NATD}} \begin{array}{l} \text{New } AdS_4 \text{ geometry in IIB} \\ \text{Dual CFT quiver with four nodes and} \\ \text{a spectral flow} \end{array}$$

2. Non-Abelian T-duality back in the 90's

Rocek and Verlinde's formulation of Abelian T-duality for ST in a curved background (Buscher'88) :

$$S = \frac{1}{4\pi\alpha'} \int \left(g_{\mu\nu} dX^\mu \wedge *dX^\nu + B_{\mu\nu} dX^\mu \wedge dX^\nu \right) + \frac{1}{4\pi} \int R^{(2)} \phi$$

In the presence of an **Abelian isometry**:

- i) Go to adapted coordinates: $X^\mu = \{\theta, X^\alpha\}$ such that
 $\theta \rightarrow \theta + \epsilon$ and $\partial_\theta(\text{backgrounds}) = 0$
- ii) Gauge the isometry: $d\theta \rightarrow D\theta = d\theta + A$
A non-dynamical gauge field / $\delta A = -d\epsilon$

iii) Add a Lagrange multiplier term: $\tilde{\theta} dA$, such that

$$\int \mathcal{D}\tilde{\theta} \rightarrow dA = 0 \Rightarrow A \text{ exact (trivial worldsheets)}$$

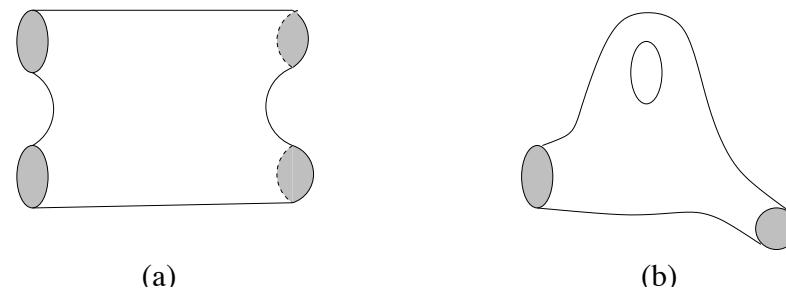
+ fix the gauge: $A = 0 \rightarrow \text{Original theory}$

iv) Integrate the gauge field

+ fix the gauge: $\theta = 0 \rightarrow \text{Dual sigma model:}$

$\{\theta, X^\alpha\} \rightarrow \{\tilde{\theta}, X^\alpha\}$ and $(\tilde{g}, \tilde{B}_2, \tilde{\phi})$ given by Buscher's formulae

- **Arbitrary worldsheets?** (symmetry of string perturbation theory):



\Rightarrow Non-trivial topologies + compact isometry orbits

Large gauge transformations: $\oint_{\gamma} d\epsilon = 2\pi n ; n \in \mathbb{Z}$

To fix them:

Multivalued Lagrange multiplier: $\oint_{\gamma} d\tilde{\theta} = 2\pi m ; m \in \mathbb{Z}$
such that

$$\int [\text{exact}] \rightarrow dA = 0 \quad + \quad \int [\text{harmonic}] \Rightarrow A \text{ exact}$$

\Rightarrow The gauging procedure works for all genera
(Rocek, Verlinde'91)

- Conformally invariant

Non-Abelian T-duality (De la Ossa, Quevedo'93)

Non-Abelian continuous isometry: $X^m \rightarrow g_n^m X^n, g \in G$

i) **Gauge it:** $dX^m \rightarrow DX^m = dX^m + A_n^m X^n$

$A \in \text{Lie algebra of } G \quad A \rightarrow g(A + d)g^{-1}$

ii) **Add a Lagrange multiplier term:** $\text{Tr}(\chi F)$

$$F = dA - A \wedge A$$

$\chi \in \text{Lie Algebra of } G, \chi \rightarrow g\chi g^{-1}$, such that

$\int \mathcal{D}\chi \rightarrow F = 0 \Rightarrow A \text{ pure gauge}$
(in a topologically trivial worldsheet)

+ fix the gauge: $A = 0 \Rightarrow$ **Original theory**

iii) Integrate the gauge field + fix the gauge \rightarrow **Dual theory**

However,

- Non-involutive
- Higher genus generalization? Set to zero $W_\gamma = P e^{\oint_\gamma A}$
- Global properties?
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True symmetry in String Theory?

NATD as a solution generating technique

(Sfetsos, Thompson'10)

Need to know how the RR fields transform

In the Abelian case: Reduce to a unique N=2, d=9 SUGRA
(Bergshoeff, Hull, Ortín'95)

Hassan'99: Implement the relative twist between left and right movers in the bispinor formed by the RR fields:

$$\hat{P} = P\Omega^{-1} \quad P = \frac{e^\phi}{2} \sum_k \frac{1}{k!} F_{\mu_1 \dots \mu_k} \Gamma^{\mu_1 \dots \mu_k}$$

with $\Omega = \sqrt{g_{00}^{-1}} \Gamma_{11} \Gamma^0$

Same thing in the non-Abelian case

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Given that NATD is not guaranteed to be a symmetry of ST:

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- In fact, possibly new CFTs!

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Explore 5d and 3d examples

3. Non-Abelian T-duality and 5d fixed point theories

5d gauge theories are non-renormalizable:

$$[g^2] = M^{-1} \rightarrow g^2 E \rightarrow \text{UV completion}$$

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- They are intrinsically strongly coupled $\rightarrow AdS/CFT$
- The string theory realization is however only known in very specific cases
- In particular, $Sp(N)$ (with specific matter content) can be realized in a D4/D8/O8 system. (Seiberg'96)
An AdS_6 background arises as the near horizon geometry
(Brandhuber, Oz'99)

3a. The D4/D8/O8 system

5d SUSY fixed points with E_{N_f+1} global symmetry can be obtained in the infinite bare coupling limit of N=1 SYM with gauge group $Sp(N)$, one antisymmetric hypermultiplet and $N_f < 8$ fundamental hypermultiplets (Seiberg'96)

The theory can be engineered in Type I' ST on a stack of N D4-branes probing a $O8^-$ plane with N_f D8-branes

From the D4-D4 sector:

Vector multiplet with $Sp(N)$ gauge symmetry
Massless hyper in the antisym. of $Sp(N)$

From the D4-D8 sector:

Massless hypers in the fundamental of $SO(2N_f)$

The near horizon geometry of the D4-D8 system is a
fibration of AdS_6 over half- S^4 with an S^3 boundary at the
position of the O8-plane, preserving 16 SUSYs

$$ds^2 = \frac{W^2 L^2}{4} \left[9 ds^2(AdS_6) + 4 ds^2(S^4) \right] \quad \theta \in [0, \frac{\pi}{2}]$$

$$F_4 = 5 L^4 W^{-2} \sin^3 \theta d\theta \wedge \text{Vol}(S^3)$$

$$e^{-\phi} = \frac{3L}{2W^5}, \quad W = (m \cos \theta)^{-\frac{1}{6}} \quad m = \frac{8 - N_f}{2\pi l_s}$$

- $SO(5)$ symmetry broken to $SO(4) \sim SU(2) \times SU(2)$:
 - $SU(2) \leftrightarrow SU(2)_R$ R-symmetry of the field theory
 - $SU(2) \leftrightarrow$ global symmetry massless antisym. hyper
- $SO(2, 5) \leftrightarrow$ Conformal symmetry

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New fixed point theory?

3b. The non-Abelian T-dual of Brandhuber and Oz

- Take the $AdS_6 \times S^4$ background

$$ds^2 = \frac{W^2 L^2}{4} \left[9 ds^2(AdS_6) + 4 \left(d\theta^2 + \sin^2 \theta ds^2(S^3) \right) \right]$$

$$F_4 = 5L^4 W^{-2} \sin^3 \theta \, d\theta \wedge \text{Vol}(S^3)$$

- Dualize it w.r.t. one of the $SU(2)$ symmetries

In spherical coordinates adapted to the remaining $SU(2)$:

$$ds^2 = \frac{W^2 L^2}{4} \left[9 ds^2(AdS_6) + 4 d\theta^2 \right] + e^{-2A} dr^2 + \frac{r^2 e^{2A}}{r^2 + e^{4A}} ds^2(S^2)$$

$$B_2 = \frac{r^3}{r^2 + e^{4A}} \text{Vol}(S^2) \quad e^{-\phi} = \frac{3L}{2W^5} e^A \sqrt{r^2 + e^{4A}}$$

$$F_1 = -G_1 - m r dr \quad F_3 = \frac{r^2}{r^2 + e^{4A}} [-r G_1 + m e^{4A} dr] \wedge \text{Vol}(S^2)$$

- It solves the IIB equations of motion
- SUSY preserved! First example of a non-Abelian T-dual geometry with supersymmetry fully preserved

This is because the internal symmetry is really $SU(2) \times SU(2)_R$ and we dualize on the $SU(2)$ global symmetry *

- Boundary at $\theta = \frac{\pi}{2}$ inherited.
- What about r ?
 - Background perfectly smooth for all $r \in \mathbb{R}^+$
 - No global properties inferred from the non-Abelian transf.
 - Puzzle to the dual CFT (!)

* NATD and SUSY: Kelekci, Y.L., Macpherson, O Colgain, to appear

4. Non-Abelian T-duality in ABJM

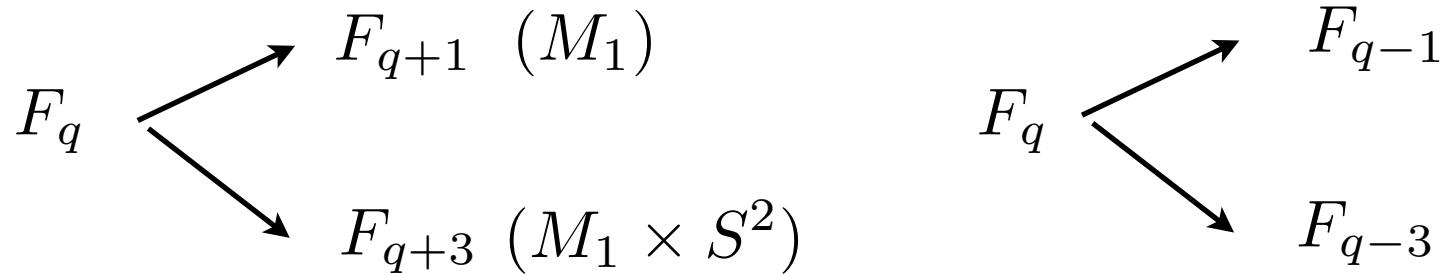
Take the $AdS_4 \times CP^3$ IIA dual +
parameterize the CP^3 as a foliation in $T^{1,1} = S^2 \times S^3$ +
T-dualize w.r.t. the $SU(2)$ symmetry of the S^3

→ IIB AdS_4 solution:

- Metric + B_2 + dilaton + F_1, F_3, F_5
- $U(1) \times U(1)$ symmetric
- N=2 supersymmetric
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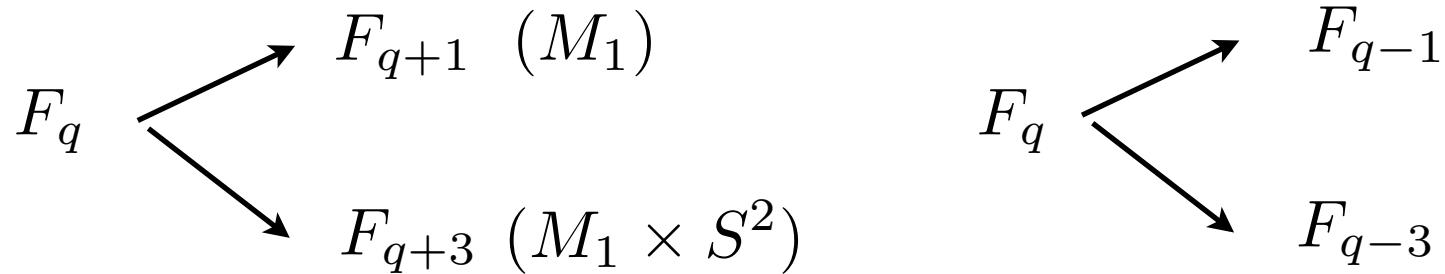
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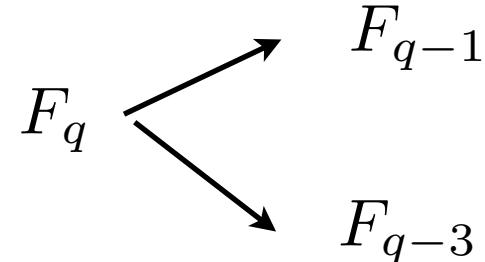
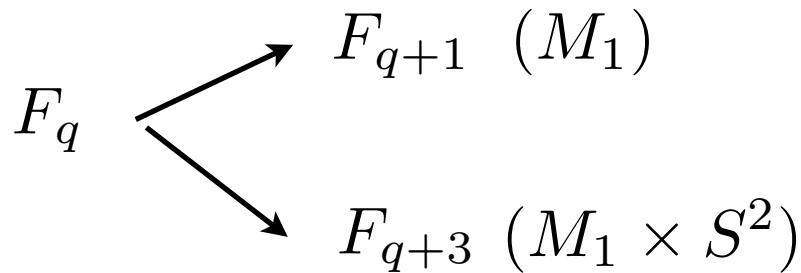
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This generates a doubling of the quantized charges in the dual CFT

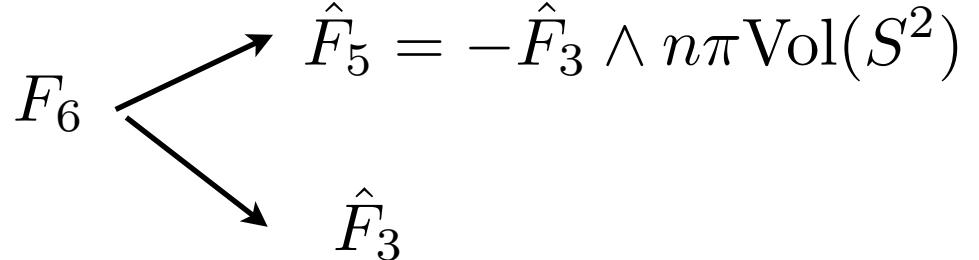
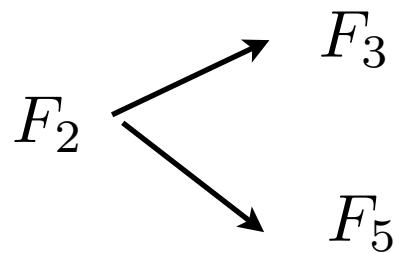
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After an $SU(2)$ NATD:



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In AdS_4 :



→ Two ranks and two levels in the dual CFT

Large gauge transformations:

Singularity at $\zeta = 0$. Close to it the geometry is conformal to a singular cone with S^2 boundary

There $B_2 = -r \text{Vol}(S^2)$

Large gauge transformations must be defined such that

$$\frac{1}{4\pi^2} \left| \int B_2 \right| \in [0, 1)$$

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The division of \mathbb{R}^+ in $[n\pi, (n+1)\pi)$ intervals restricts non-trivially the global properties of the dual background

Color branes:

$$\begin{array}{l} \text{D3 on } \mathbb{R}_{1,2} \times M_1 \quad \longleftrightarrow \quad N_3 = n N_5 \quad , \quad g_{D3}^2 \sim \frac{1}{k_5} \\ \text{D5 on } \mathbb{R}_{1,2} \times M_1 \times S^2 \quad \longleftrightarrow \quad N_5 \quad , \quad g_{D5}^2 \sim \frac{1}{k_3} \end{array}$$

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Moving from an r interval to the previous one:

$N_3 \rightarrow N_3 - N_5$: Seiberg duality in $N=1 \leftrightarrow$ Large gauge transformations as geometric version of Seiberg duality in KT, KS..
(Benini, Canoura, Cremonesi, Nuñez, Ramallo'07)

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D5 on $\mathbb{R}_{1,2} \times M_1 \times S^2$ \longleftrightarrow N_5 , $g_{D5}^2 \sim \frac{1}{k_3}$

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This, together with the analysis of particle-like configurations, giant gravitons, free energy, etc suggests a dual CFT:

$$U(N_3 + N_5)_{k_3} \times U(N_3)_{k_5} \times U(N_3 + N_5)_{-k_3} \times U(N_3)_{-k_5}$$

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In particular, all CFT should be equivalent to the one dual to the solution for $r \in [0, \pi) : U(N_5)_{k_3} \times U(N_5)_{-k_3}$ **(N=2)**

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Speculate with a possible brane realization:

$5_2^2 :$	\times	$ $	\times	\times	\times	\times	\times	$-$	z_1	z_2	$-$
$N_5 D5 :$	\times	$ $	\times	\times	$-$	$-$	$-$	\times	\times	\times	$-$
$(5_2^2, k_3 D3) :$	\times	$ $	\times	\times	$-$	$-$	$\cos \theta$	$-$	$-$	$-$	$\sin \theta$

6. Conclusions and open issues

- NATD useful as a solution generating technique:
Only known AdS_6 solution in IIB (+ Abelian T-dual)
(Only two explicit solutions to the PDEs in IIB recently derived in Apruzzi, Fazzi, Passias, Ross, Tomasiello'04)

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Realization in the CFT of the running of the non-compact direction: Spectral flow very similar to the cascade, but on the internal, not on the holographic, direction

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Also working in other NATD backgrounds?

The same idea works in 5d: $Sp(N_7^\theta)$ gauge theory with N_5^r flavors



New fixed points associated with product gauge groups
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- CFT dual to the new IIB AdS_4 background:

N=2: Low energy effective theory on the w.v. of 5-branes wrapping $\mathbb{R}_{1,2} \times M_3$ (3d-3d correspondence)?

Some of these theories: $U(1)^2$ isometry (Bah, Gabella, Halmagyi'14)

But free energy goes as $N^{3/2}$.. (Gabella, Martelli, Passias, Sparks'12)

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