JLab Experiment E08-007 Proton Electromagnetic Form Factor Ratio at Low Q²

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Outline

- Stuff we (should ?) know
- E08-007 form factor measurements
 - Motivation
 - Analysis

Mainz, June 2014

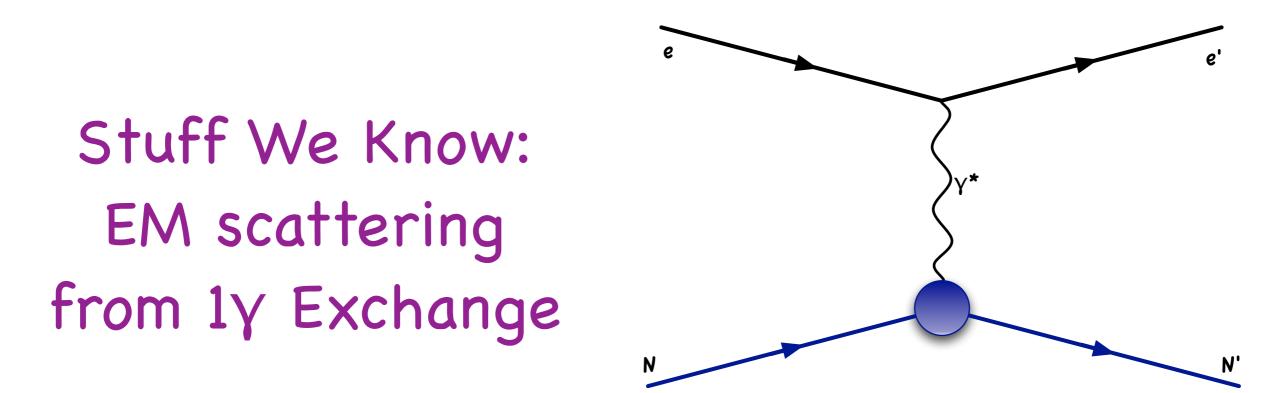
The E08-007 Collaboration:

Guy Ron, spokesperson

Moshe Friedman, Ph.D. student

et al.

*Thanks to: US NSF grant PHY 09-69239, 12-63280, JLab, MITP, ...

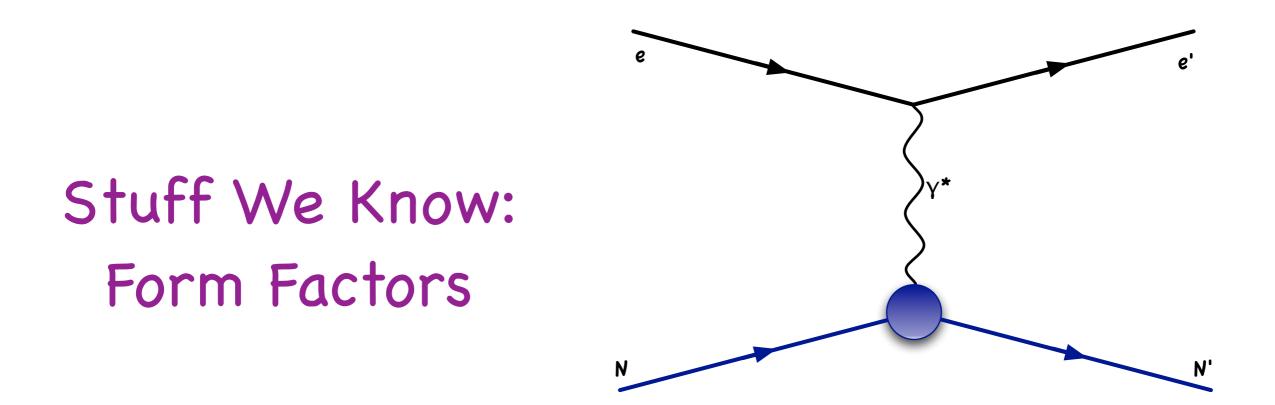


Cross section formulas derived and put in modern form \approx 60 years ago – Rosenbluth separation.

$$\frac{d\sigma_{Str}}{d\Omega} = \frac{d\sigma_M}{d\Omega} \times \left[G_E^2(Q^2) + \frac{\tau}{\varepsilon} G_M^2(Q^2) \right] \quad \begin{array}{l} \text{Rosenbluth} & -\\ \text{Spin-1/2 with} \\ \text{Structure} \end{array}$$
$$\tau = \frac{Q^2}{4M^2}, \ \varepsilon = \left[1 + 2(1+\tau) \tan^2 \frac{\theta_e}{2} \right]^{-1}$$

Assumptions: one-photon exchange, electron mass small





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$$G_E^p(0) = 1$$
 $G_E^n(0) = 0$
 $G_M^p = 2.793$ $G_M^n = -1.91$

Sometimes $G_E = F_1 - \tau F_2$ written using: $G_M = F1 + F_2$ Two relativistic-invariant functions of four-momentum transfer Q²

 G_M 's roughly follow the dipole form, $(1+Q^2/\Lambda^2)^{-2}$, which has no theoretical significance



Stuff We Know: Radius means slope of FF at Q² = 0, it does not mean radius.

In NRQM, scattering theory, F.T. 3d spatial distributions, small-Q² expansion:

$$G_{E,M}(Q^2) = 1 - \frac{1}{6} \left\langle r_{E,M}^2 \right\rangle Q^2 + \frac{1}{120} \left\langle r_{E,M}^4 \right\rangle Q^4 - \frac{1}{5040} \left\langle r_{E,M}^6 \right\rangle Q^6 + \cdots$$

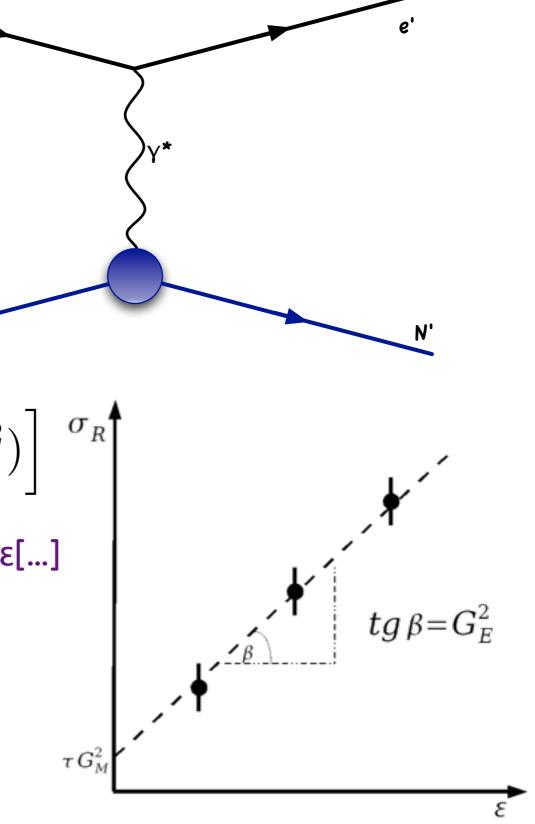
Sometimes you get the "right" answer despite the wrong approach Overall factor

$$-6\frac{dG_{E,M}}{dQ^2}\Big|_{Q^2=0} = \left< r_{E,M}^2 \right> \equiv r_{E,M}^2 \qquad \qquad \text{out of } \mathbf{G}_{\mathbf{M}}$$

Slope of $G_{E,M}$ at $Q^2=0$ defines the radii. This is what FF experiments quote.

Stuff We Know: Rosenbluth separations do not determine FF with small contribution to cross section well $\frac{d\sigma_{Str}}{d\Omega} = \frac{d\sigma_M}{d\Omega} \times \left[G_E^2(Q^2) + \frac{\tau}{\varepsilon} G_M^2(Q^2) \right]^{\sigma_R}$ For Rosenbluth, multiply RHS by ϵ/ϵ and use $\sigma_R = \epsilon[...]$ At high Q^2 , τ is large and G_E is hard to determine At low Q^2 , τ is small and G_M is hard to determine (except for $\theta \approx 180^\circ$)

Solution already known by early 1960s 🕫 polarization measurements



RUTGERS

Monday, June 2, 2014

Stuff We Know:
Polarization Transfer

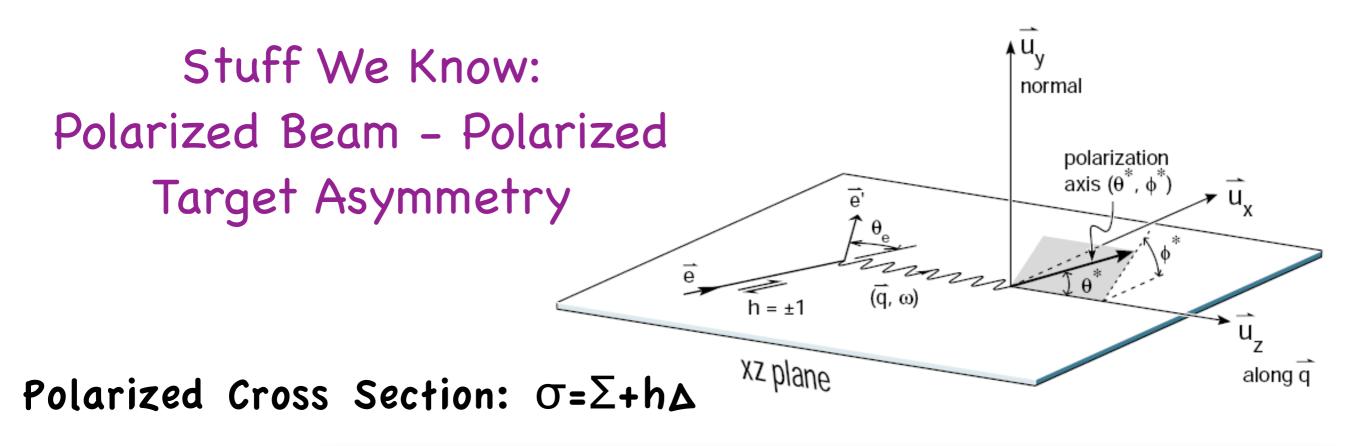
$$I_0P_t = -2\sqrt{\tau(1+\tau)}G_EG_M \tan \frac{\theta_e}{2}$$

$$I_0P_l = \frac{E_e + E_{e'}}{M}\sqrt{\tau(1+\tau)}G_M^2 \tan^2 \frac{\theta_e}{2}$$

$$P_n = 0 (1\gamma)$$

$$\mathcal{R} \equiv \mu_p \frac{G_E}{G_M} = -\mu_p \frac{P_t}{P_l} \frac{E_e + E_{e'}}{2M} \tan \frac{\theta_e}{2}$$

Polarizations worked on by many. Put in modern form first by Akhiezer & Rekalo (1973). "Popularized" in US by Arnold, Carlson & Gross (1981). Polarizations measure the ratio G_E/G_M , not the individual form factors. I_0 is the structure part of the cross section, the [...]. Done at Mainz, MIT Bates, and JLab.



$$\mathcal{A} = \frac{\sigma_{+} - \sigma_{-}}{\sigma_{+} + \sigma_{-}} \left(\mathcal{A} = fP_{b}P_{t} \underbrace{\overbrace{a \cos\theta^{*} G_{M}^{2} + b \sin\theta^{*} \cos\phi^{*} G_{E}G_{M}}^{A_{LT}}}_{cG_{M}^{2} + dG_{E}^{2}} \right)$$

For a single polarization measurement, uncertainties can be limited by polarimetry, to a few percent. For two simultaneous polarization measurements, these uncertainties can cancel in the ratio of the two. Can swap between systematic & statistical uncertainties.

a, b, c, d are kinematic factors



Why E08-007?

Back in 2008, we perceived a need for better low Q² form factors
Measure to better precision the low Q² form factor ratio, and how it starts deviating from unity

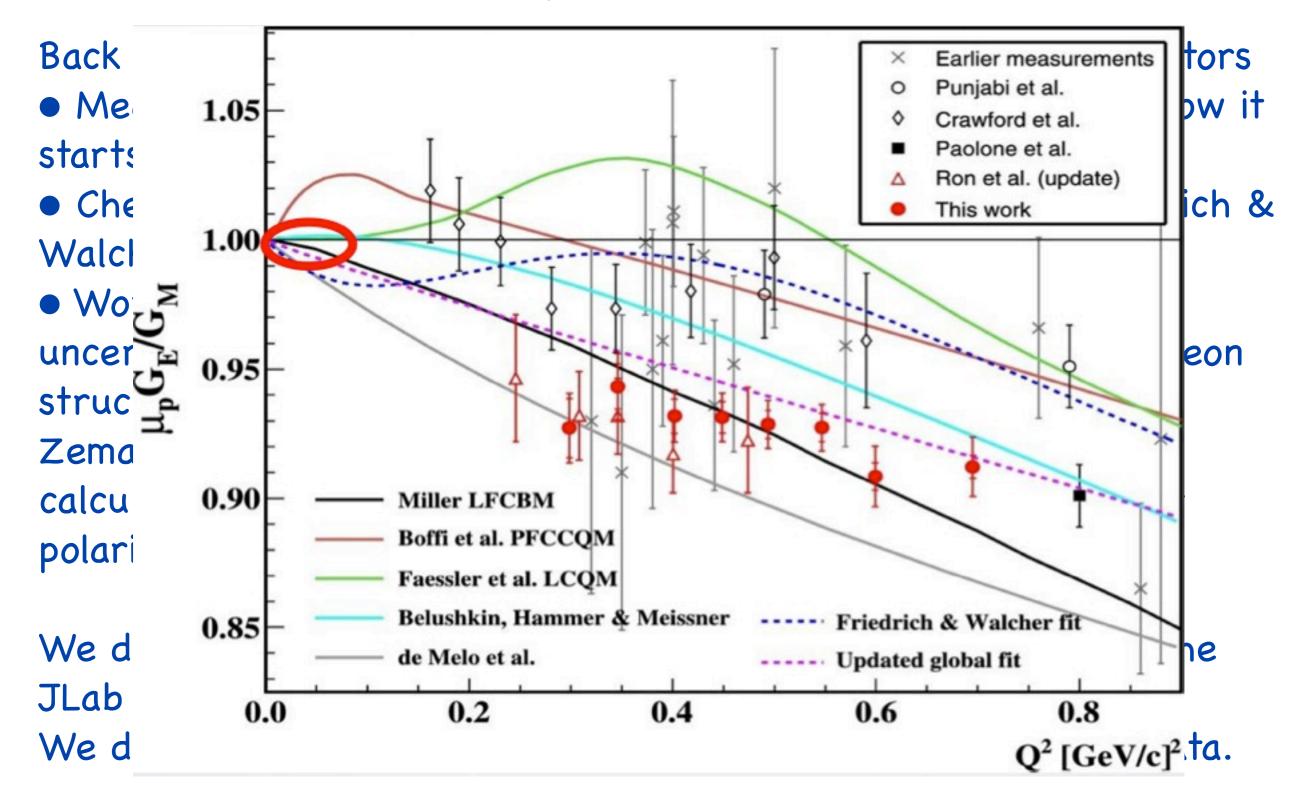
• Check claims of structure in the low Q^2 form factors (Friedrich & Walcher)

• Work by Carlson, Griffeoen, et al., pointed out that leading uncertainties in hyperfine splitting theory were related to nucleon structure – improved elastic form factors to calculate a better Zemach radius, and improved polarized inelastic scattering to calculate a better polarizibility correction – the subject of our polarized target "sister" experiment, E08–027, by Slifer et al.

We did not anticipate a proton radius puzzle. But neither did the JLab PAC. We did not anticipate the quality and quantity of the Mainz data.



Why E08-007?





But polarizations only measure ratios... ?

While the polarization data only measure ratios, they help constrain the normalization of cross section data sets, leading to improved form factors.

The number of polarization data points is comparable to the amount of non-Bernauer et al cross section data points.



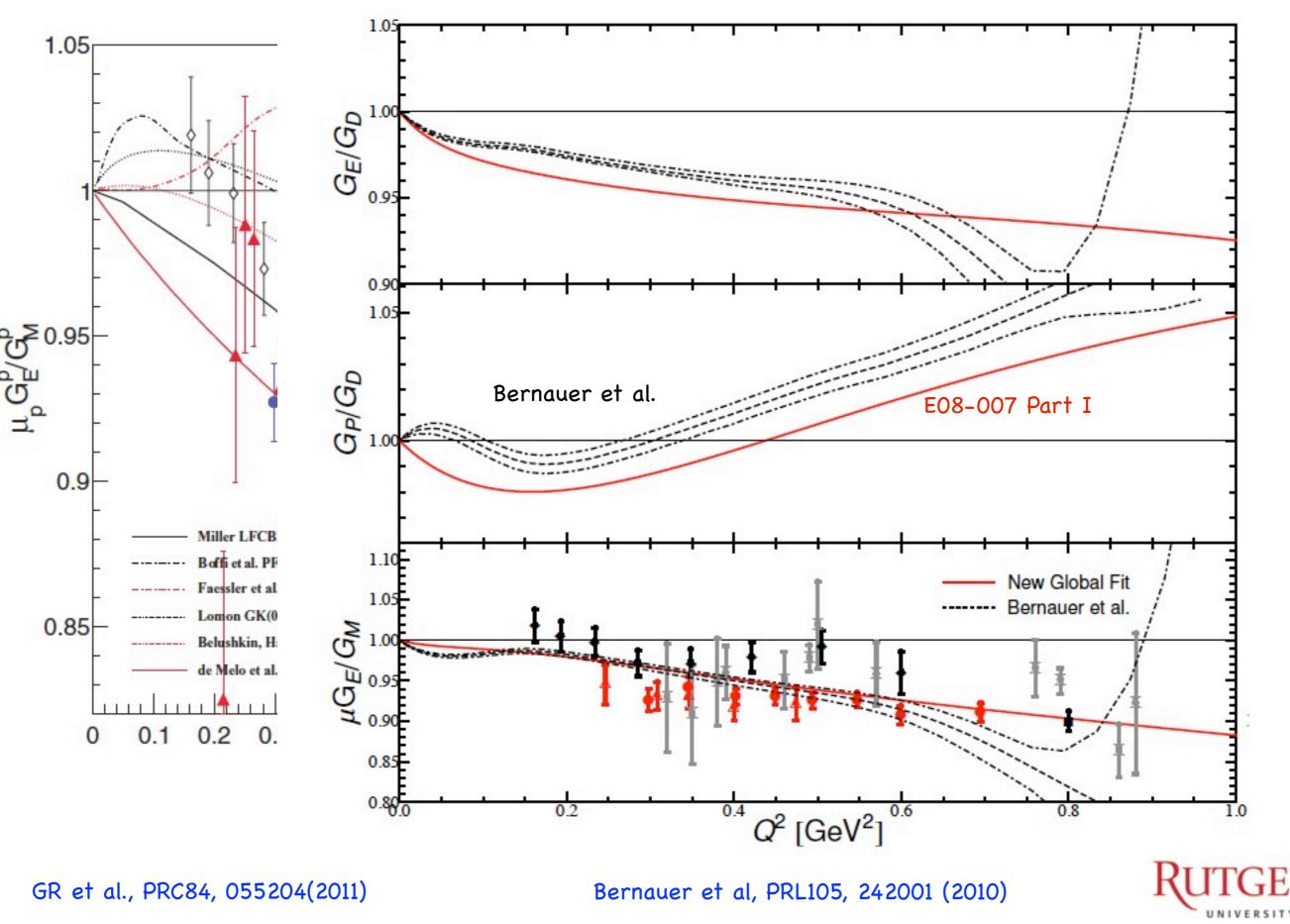
E08-007 Overview

Proposed in 2008 by G Ron et al. as a two-part measurement:

- Part I:
 - Recoil polarization for $Q^2 \approx 0.3 0.7 \text{ GeV}^2$
 - Ran 2008
 - Published as Zhan et al., PLB, 2011
- Part II:
 - Polarized target asymmetries for lower Q²
 - ...

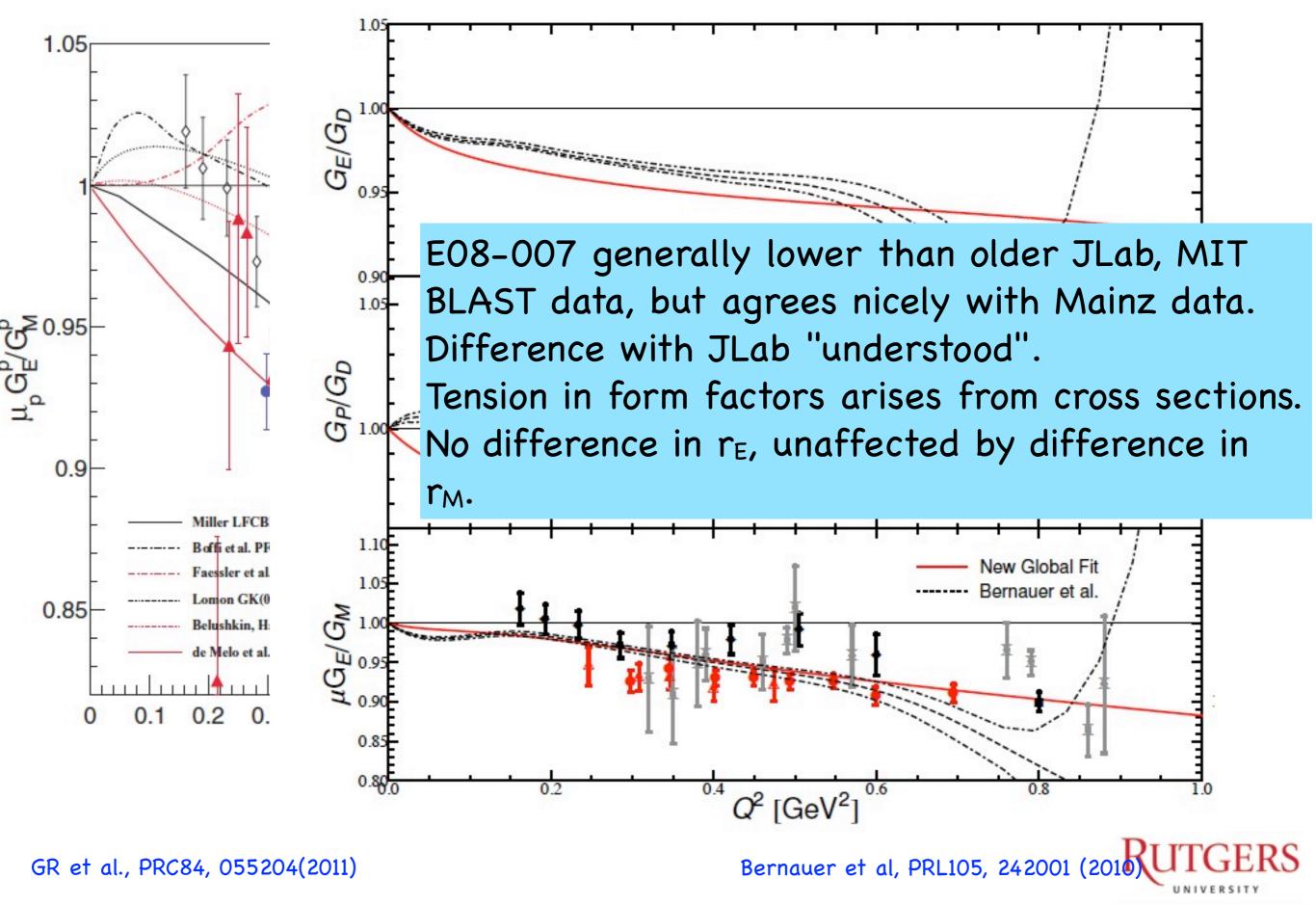


E08-007 Part I



Monday, June 2, 2014

E08-007 Part I



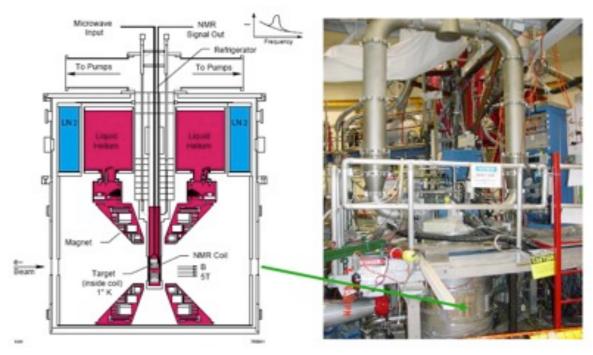
E08-007 Part II Overview

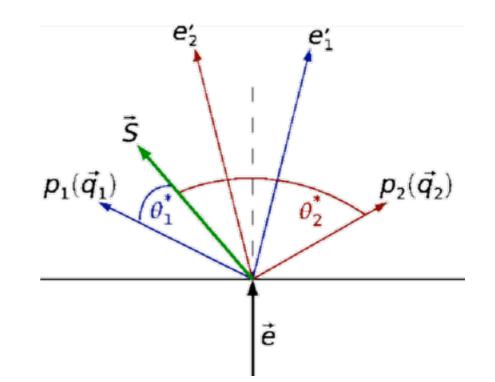
Experiment ran along with E08-027 in "late 2011 / early 2012".

Due to numerous technical problems, particularly with polarized target magnet, this was reduced to Feb – May 2012.

The data range was much reduced. Planned for high precision (\approx 1%) survey of the FF ratio at Q²=0.01 – 0.16 GeV². Lost "high" Q² points.

Moshe Friedman (HUJI) Thesis project, work in progress

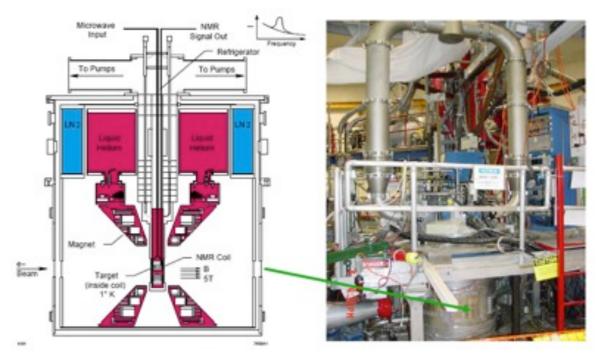


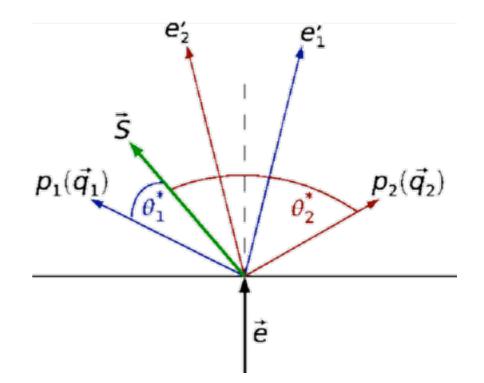




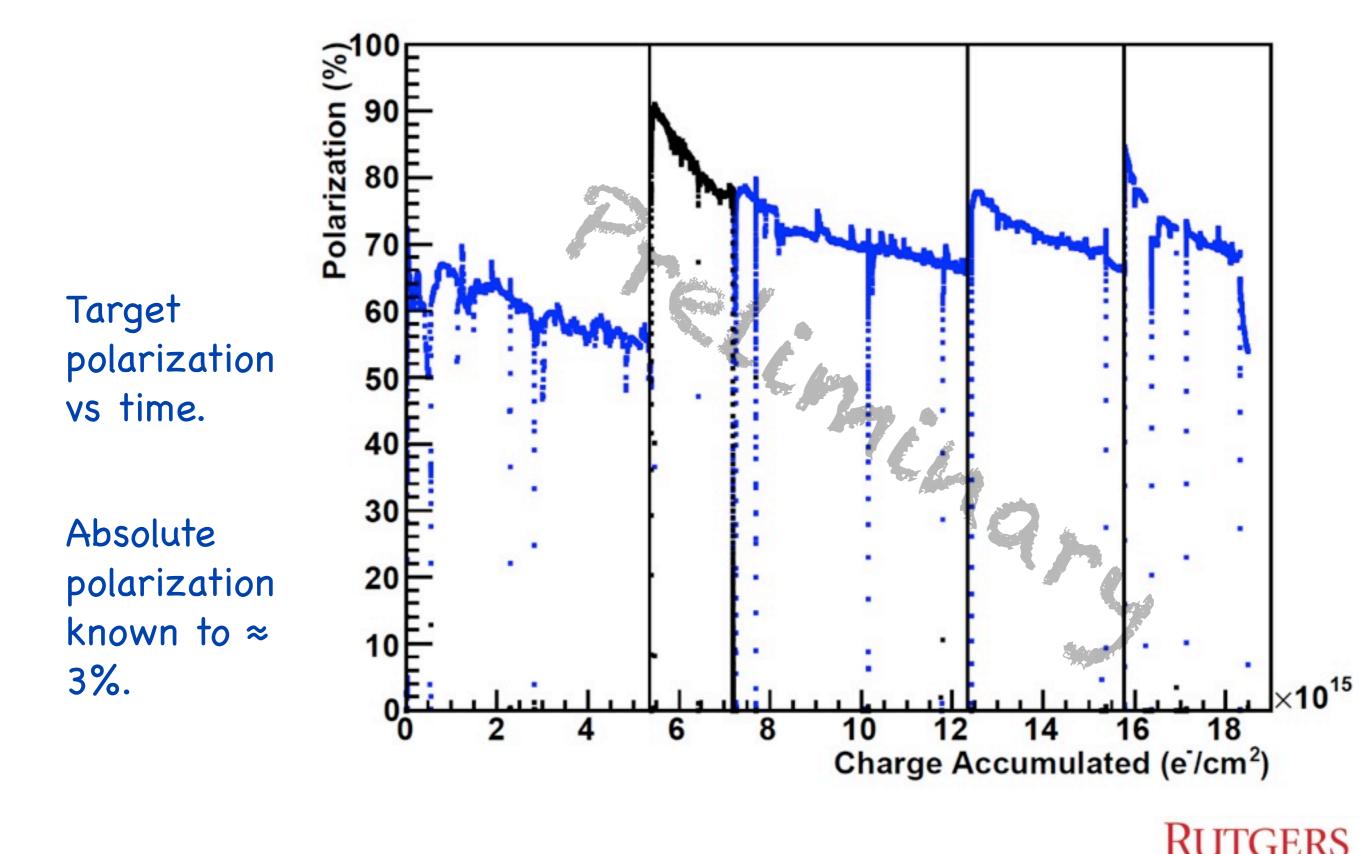
E08-007 Part II Overview

- Measured Beam-target asymmetry in electron scattering from polarized NH₃ target.
- Electrons detected in JLab Hall A's two matched HRS spectrometers.
- Ratio of asymmetries cancels systematic errors → only one target setting to get FF ratio.

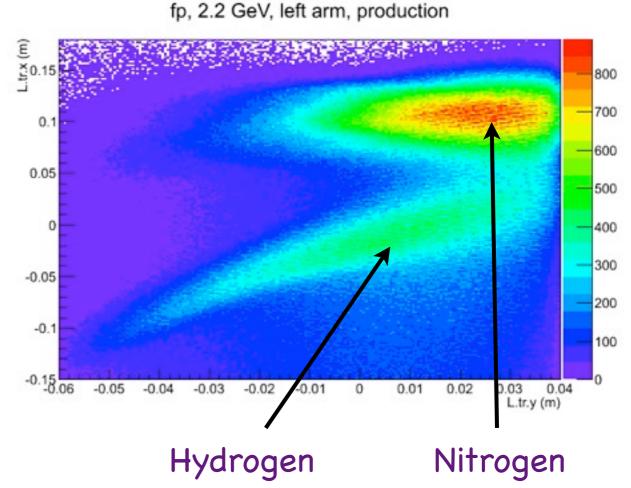




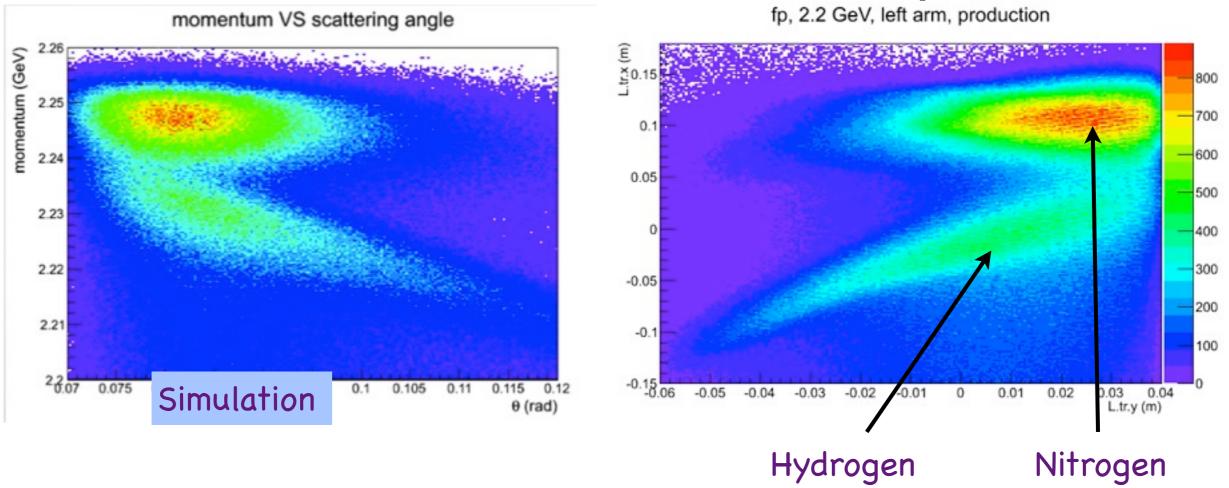




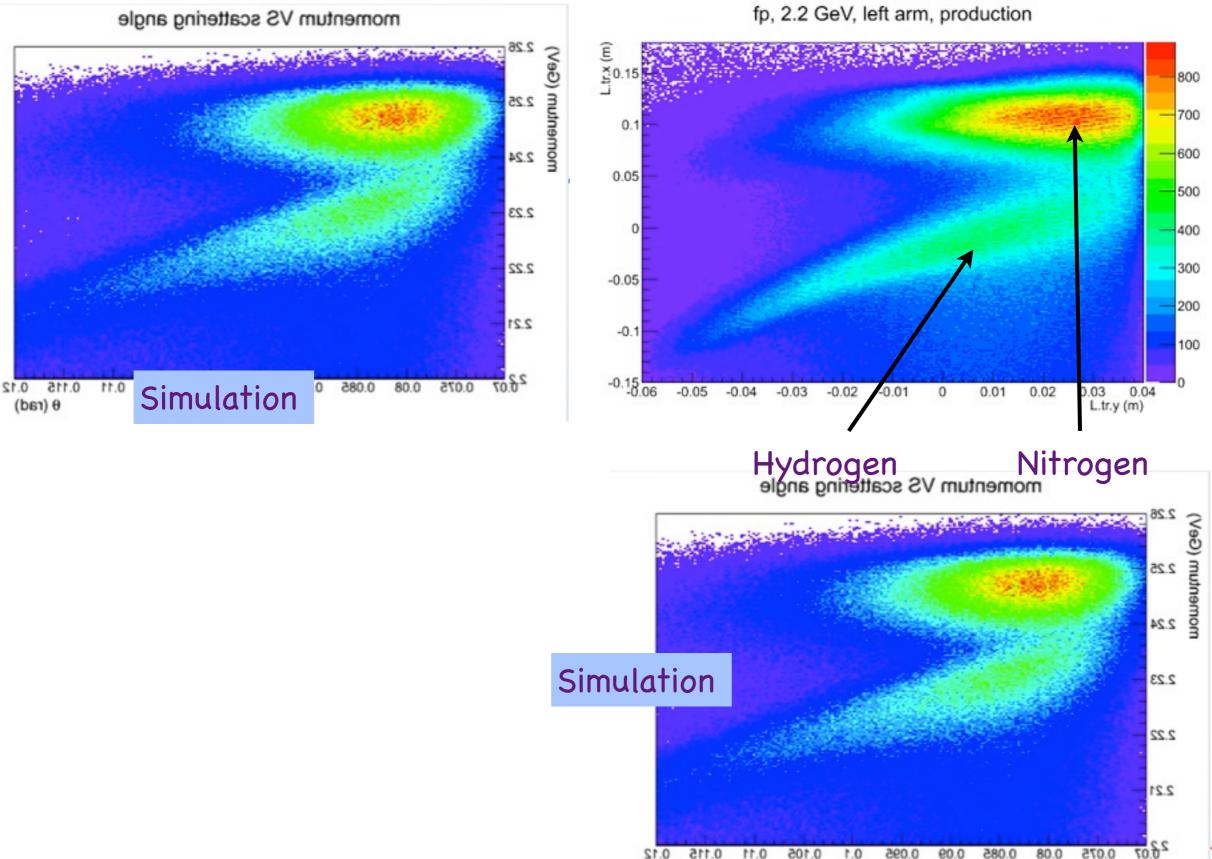
Event distribution on focal plane. Roughly momentum vs scattering angle.





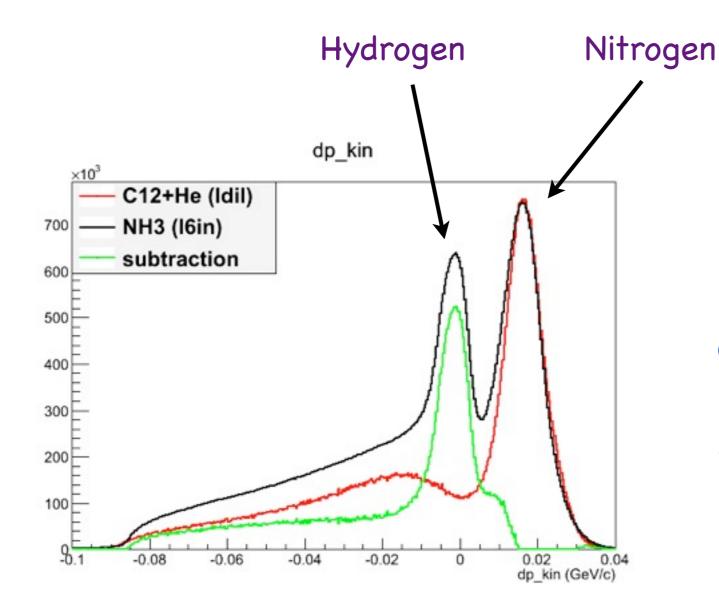






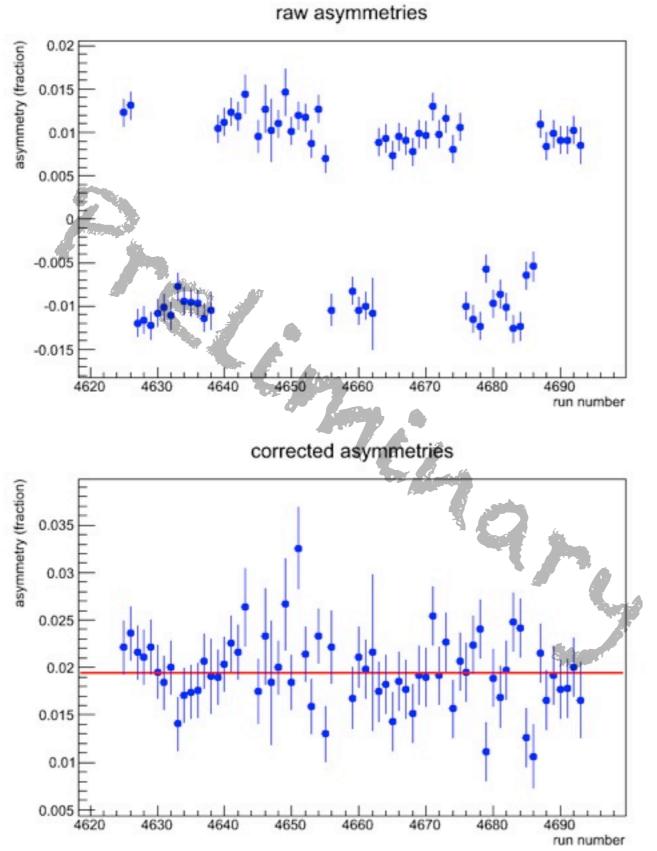
(rad)

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Momentum spectrum of data. C+He is similar to N, but not enough. N data in ≈ same kinematics being analyzed.

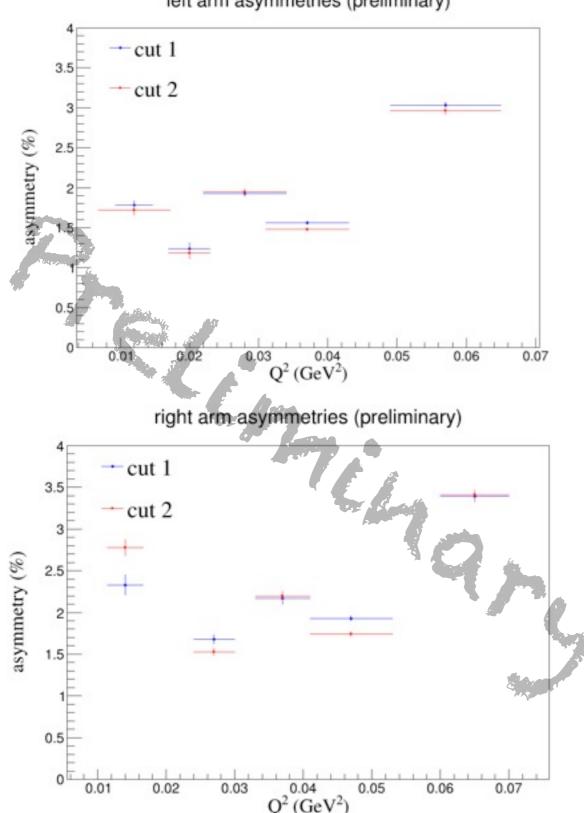




Hydrogen asymmetries reverse sign when target polarization reversed.

Nitrogen asymmetries (not shown) consistent with 0.





left arm asymmetries (preliminary)

Left arm less insensitive to N vs H cut than right arm.

Statistical uncertainties becoming small. Need to better evaluate systematic uncertainties.

Cut 1 is a tighter cut.



E08-007 Part II Issues & Improvements

Optics not finalized. Should get better signal/background separation and thus statistical uncertainty.

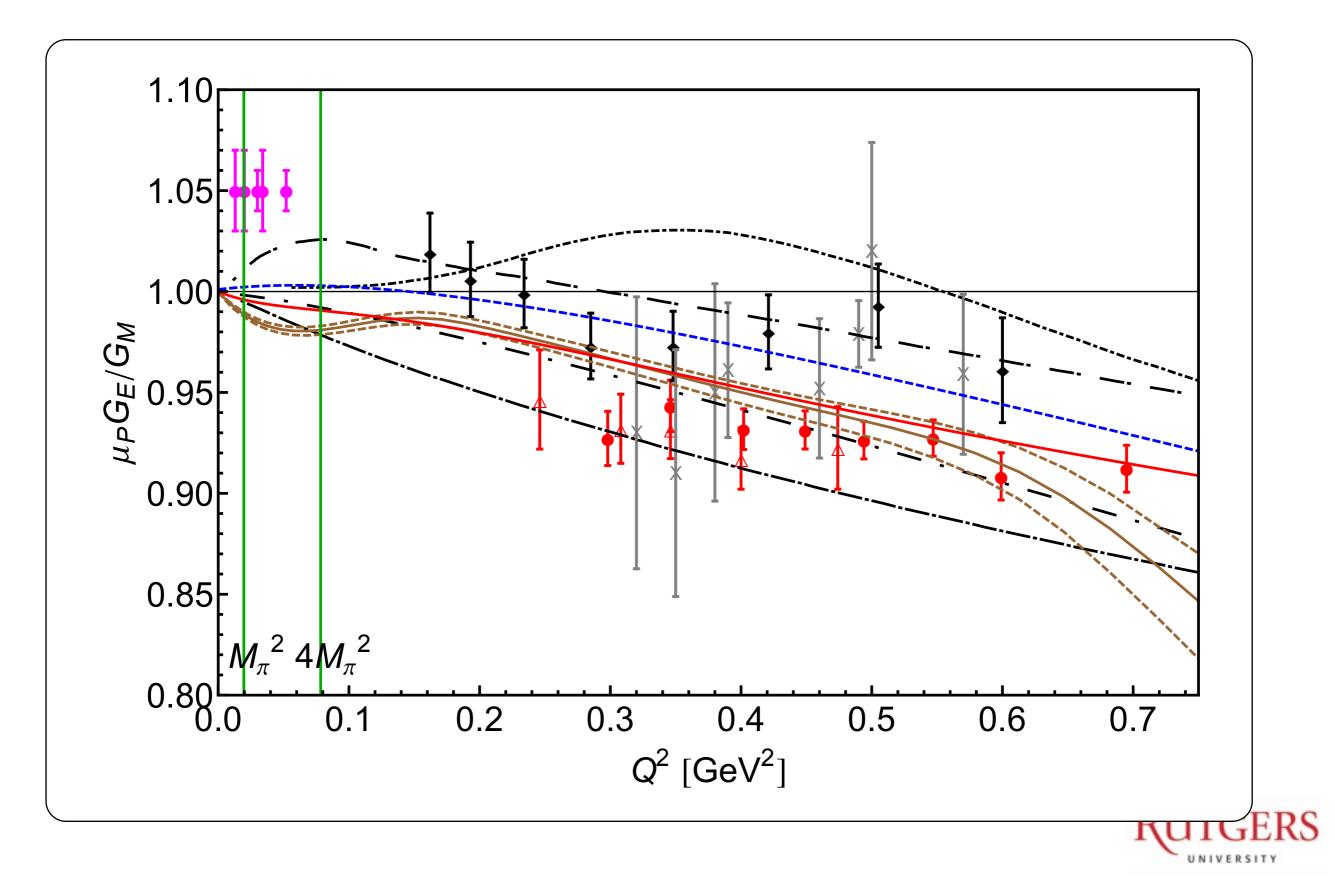
Helicity decoder messes up, diluting asymmetry. Fixing will increase asymmetry and improve $\Delta A/A$.

Nitrogen data should allow better background subtraction.

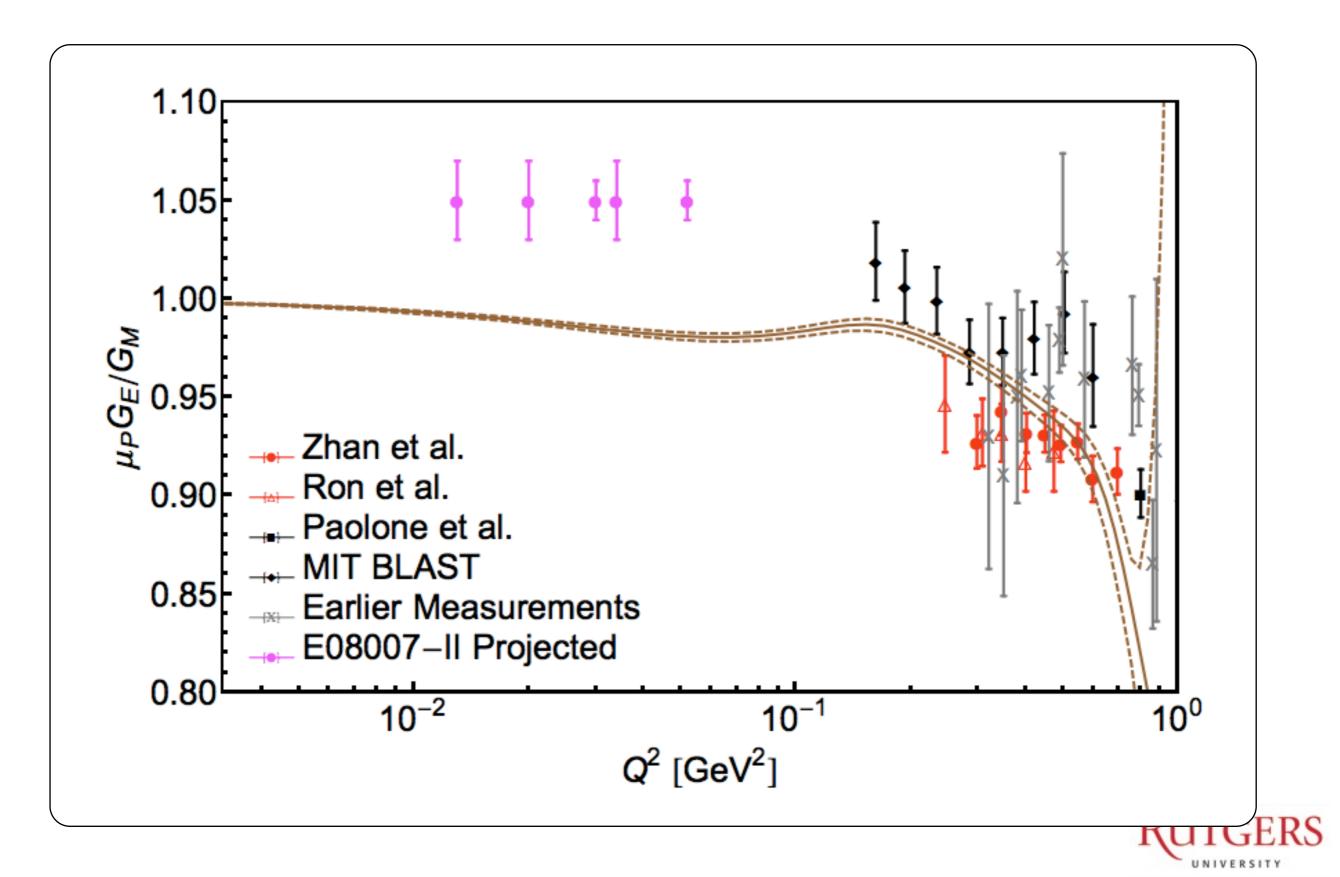
All these are approaching final, and the analysis should be completed later this year.



E08-007 Part II Projected Uncertainties



E08-007 Part II Projected Uncertainties

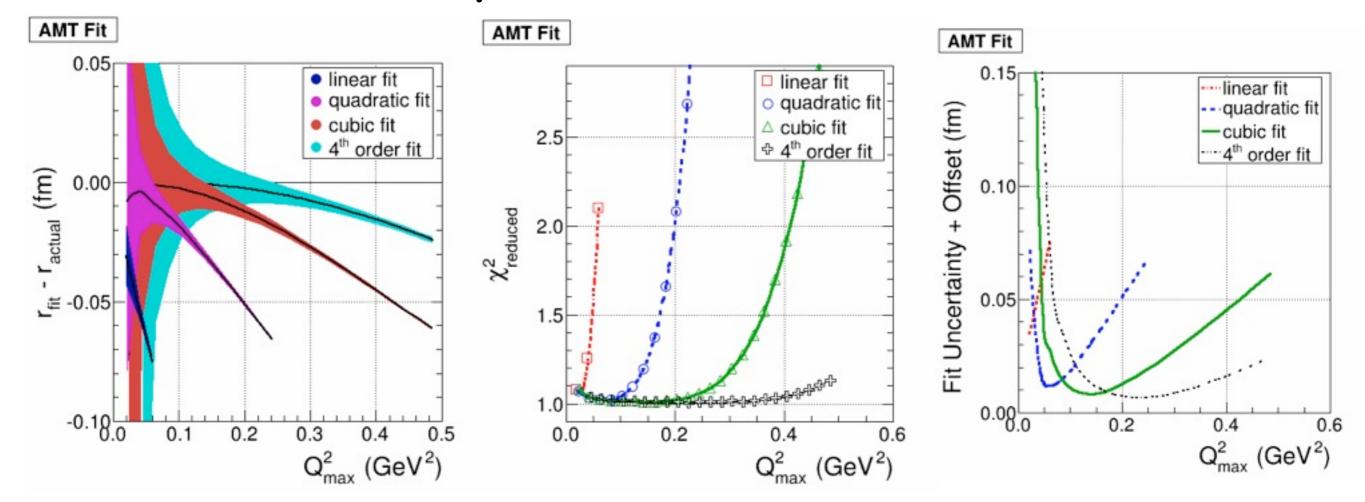


Summary

- Part I: Published in PLB, X. Zhan et al.
 - Improved ratio measurement confirms G_E smaller than previously believed
 - Generally in agreement with Bernauer et al. MAMI data for the ratio
 - Disagreements in detail arise from analysis including old cross section data vs Bernauer data; (in)consistent (r_M) r_E.
- Part II: Data taken in spring 2012
 - Analysis in progress, should be final this year
 - Should obtain statistical uncertainties, systematics to be seen



A quick slide on fits arXiv:1405.4735



Bottom line: Ingo & Michael... have warned us not to do Taylor series fits. We agree.

