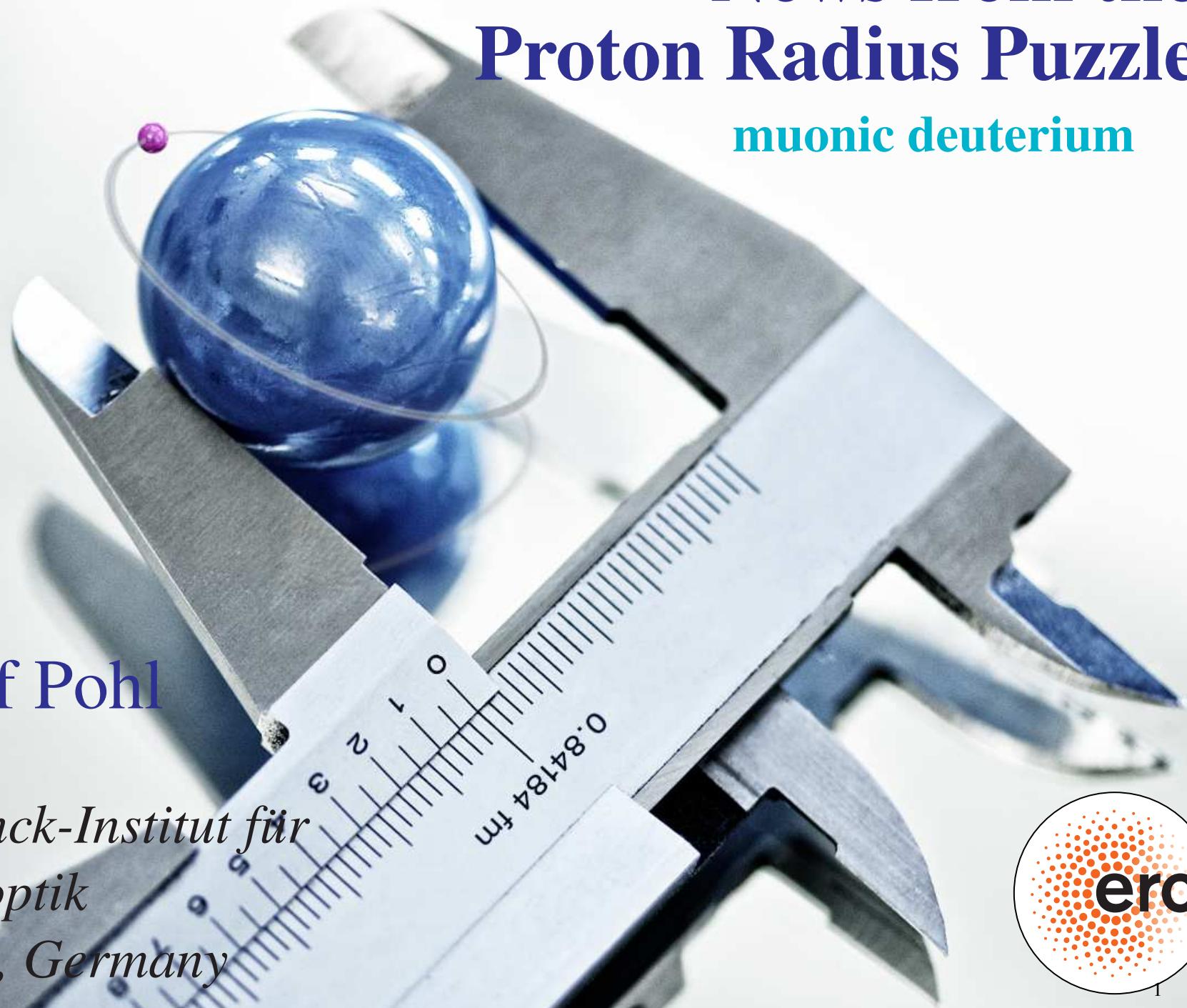


# News from the Proton Radius Puzzle

## muonic deuterium

Randolf Pohl

*Max-Planck-Institut für  
Quantenoptik  
Garching, Germany*

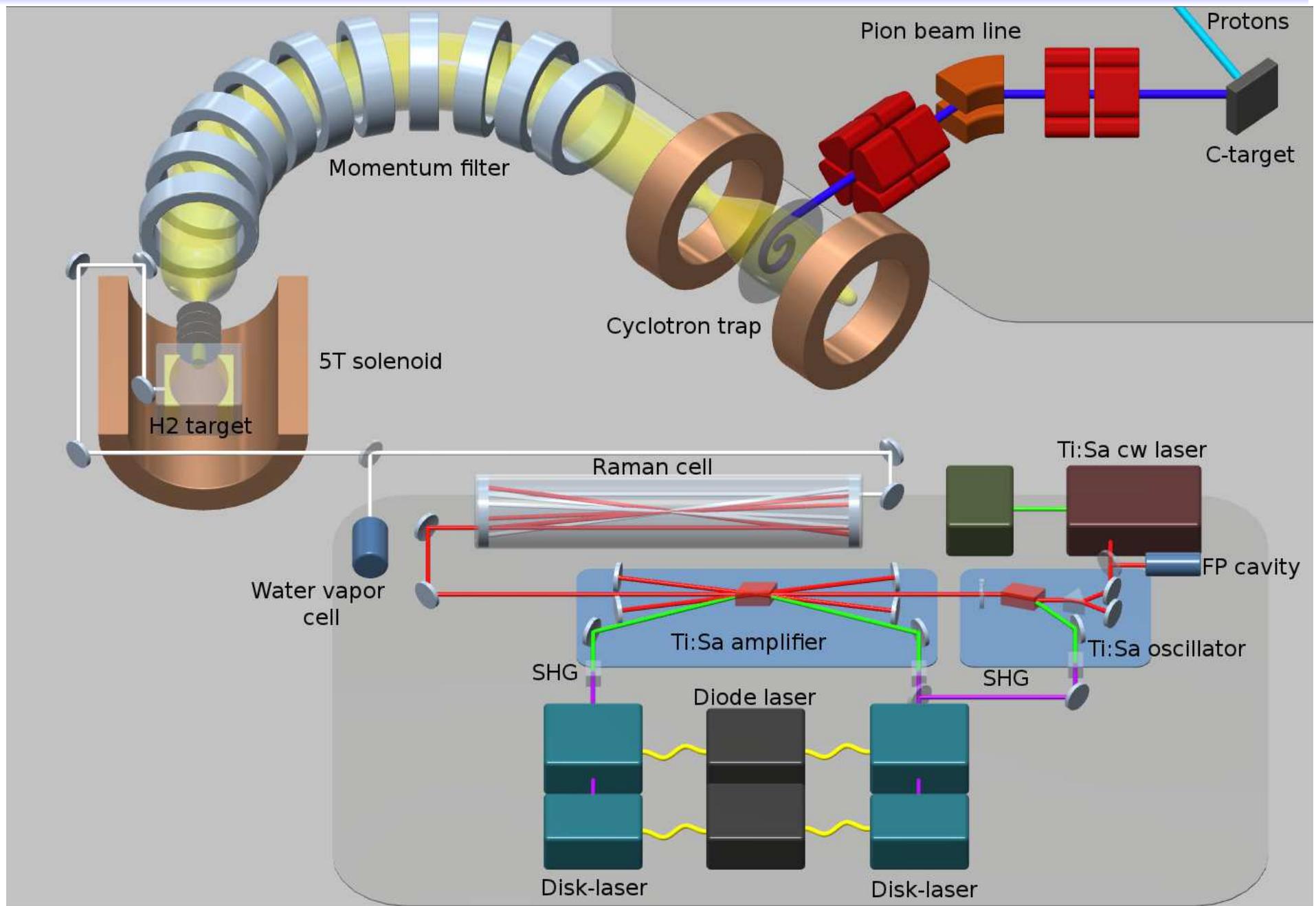


# Outline

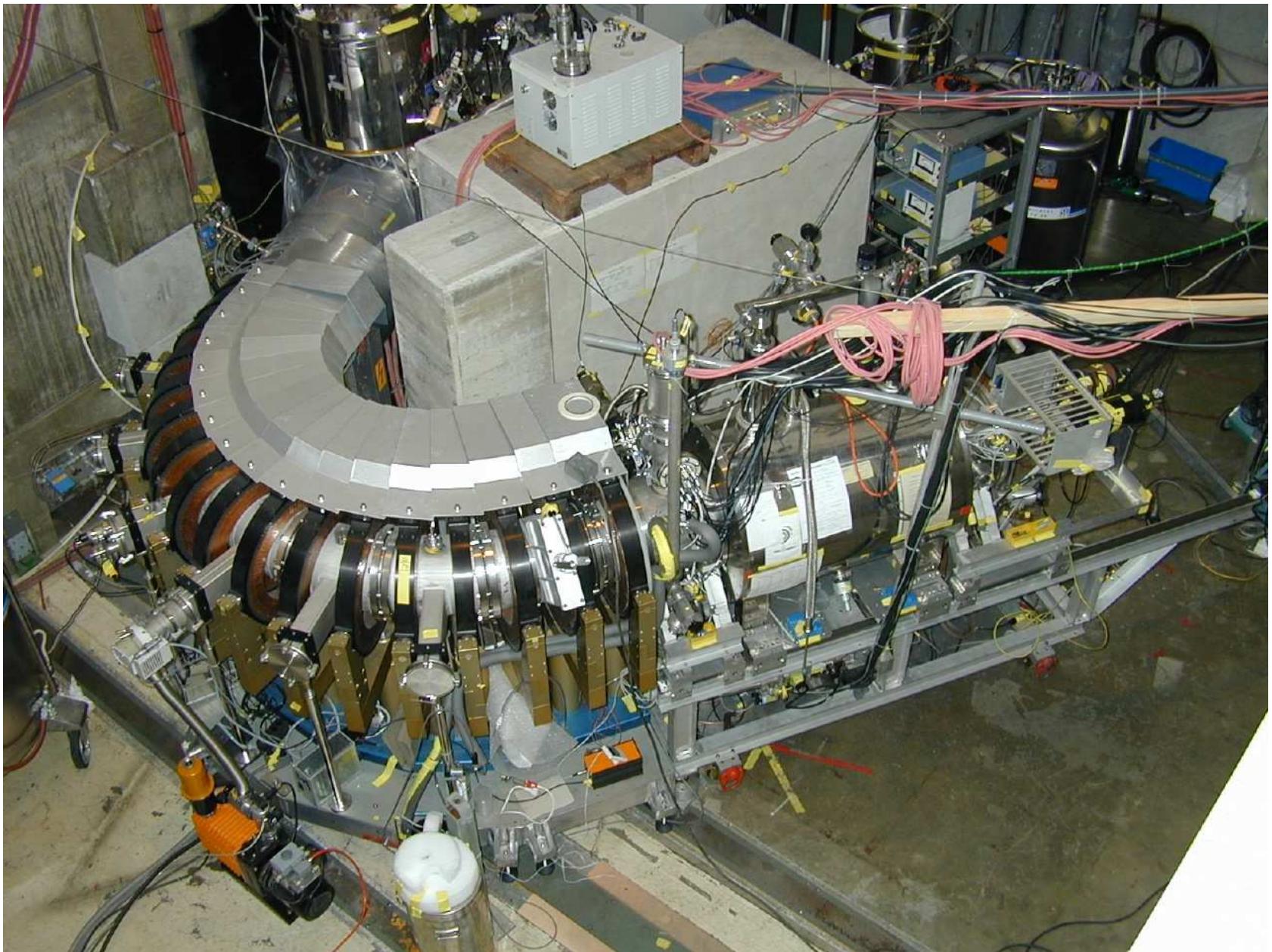
- The problem:
  - Proton rms charge radius  $r_p$  from muonic hydrogen  $\mu p$  is 4 % smaller than the values from elastic electron-proton scattering and hydrogen spectroscopy.  
That's  $5\sigma \dots 8\sigma$ .  
But the  $\mu p$  result is 10 times more accurate than any other measurement.
- Introduction
- Muonic hydrogen
- Muonic deuterium
- Muonic helium
- Muonic future

# Muonic measurements.

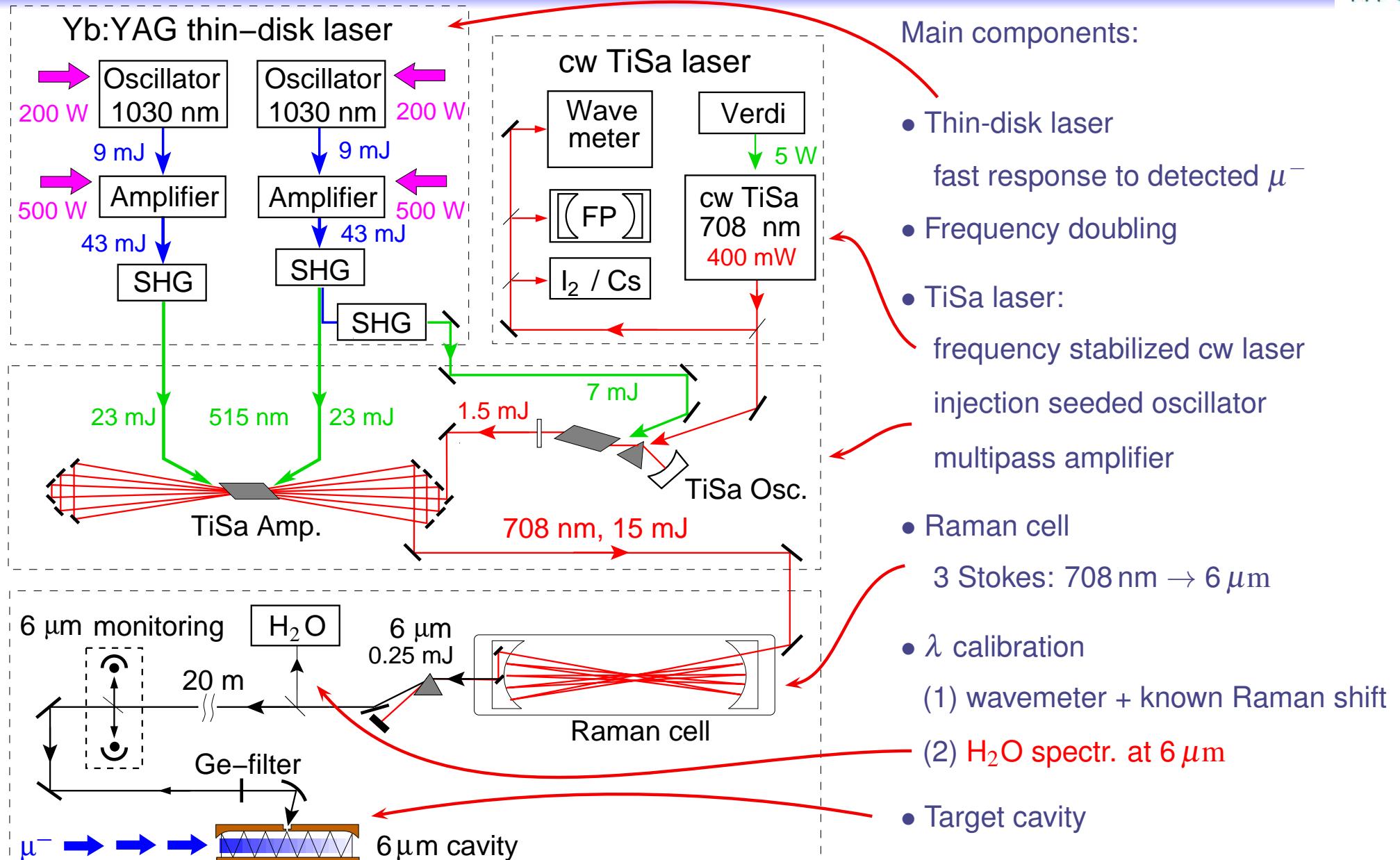
# Setup



# Muon beam line



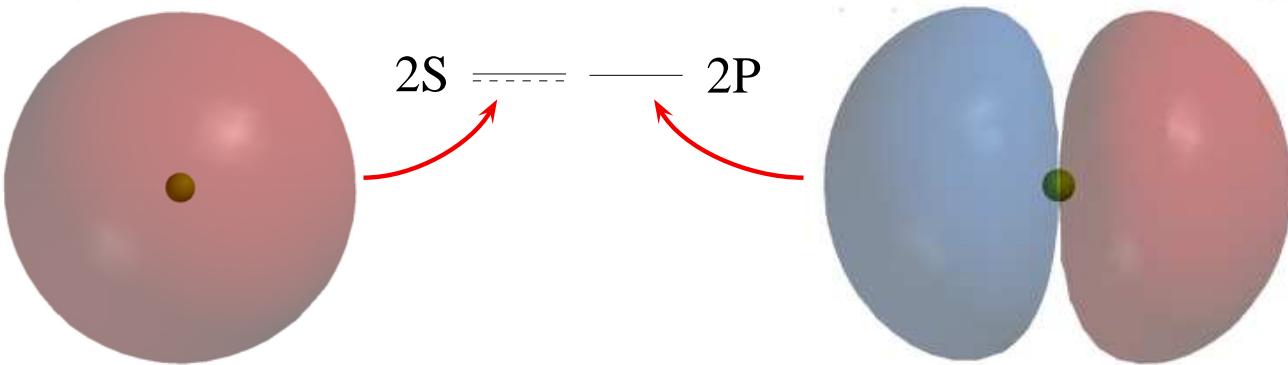
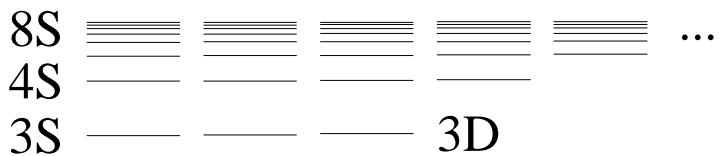
# The laser system



A. Antognini, RP et. al., Opt. Comm. 253, 362 (2005)

# Atomic physics

Wave functions of S and P states:



S states: max. at  $r=0$

Electron sometimes **inside** the proton.

S states are shifted.

Shift ist proportional to the

size of the proton

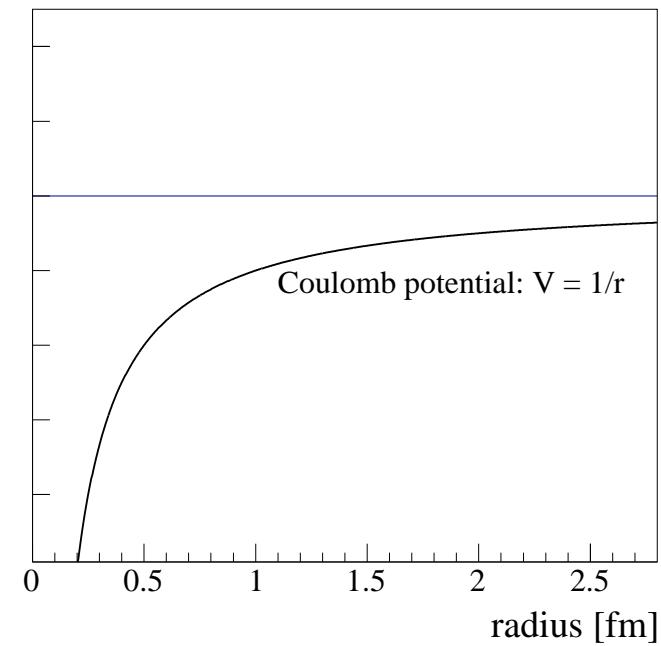
P states: zero at  $r=0$

Electron is **not** inside the proton.



Orbital pictures from Wikipedia

# Atomic physics



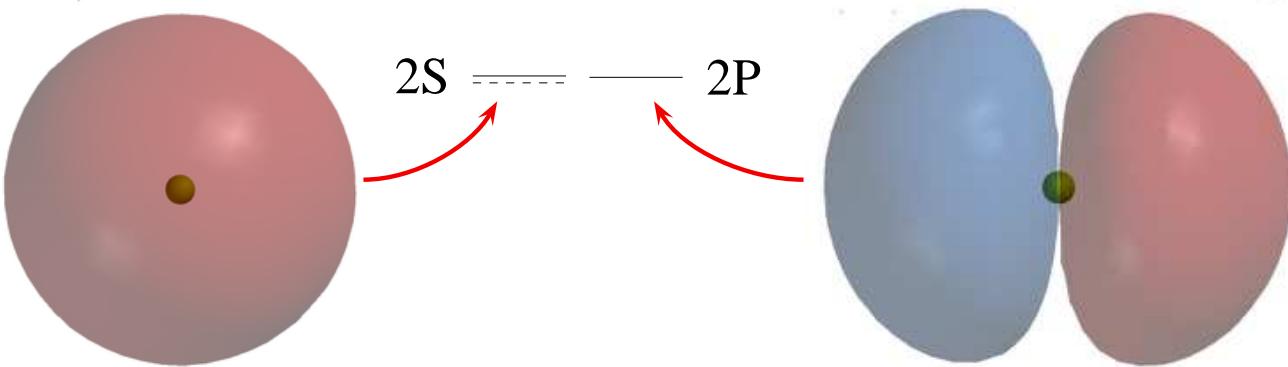
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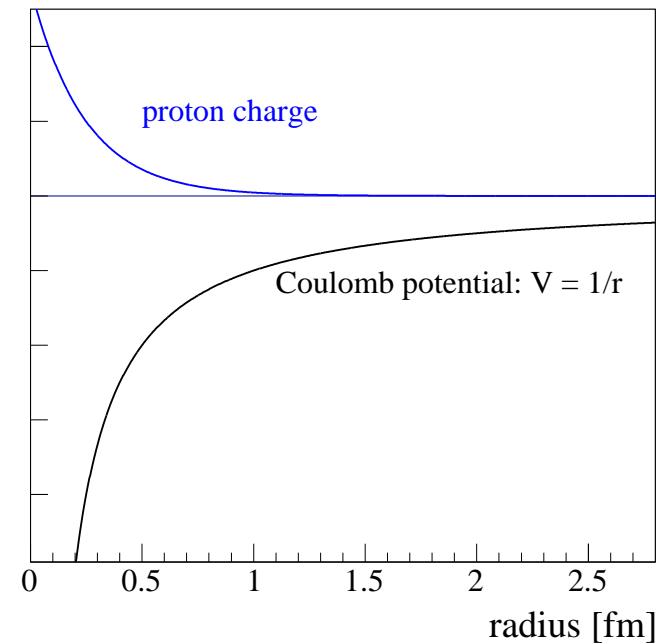
P states: zero at  $r=0$

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Orbital pictures from Wikipedia

# Atomic and nuclear physics



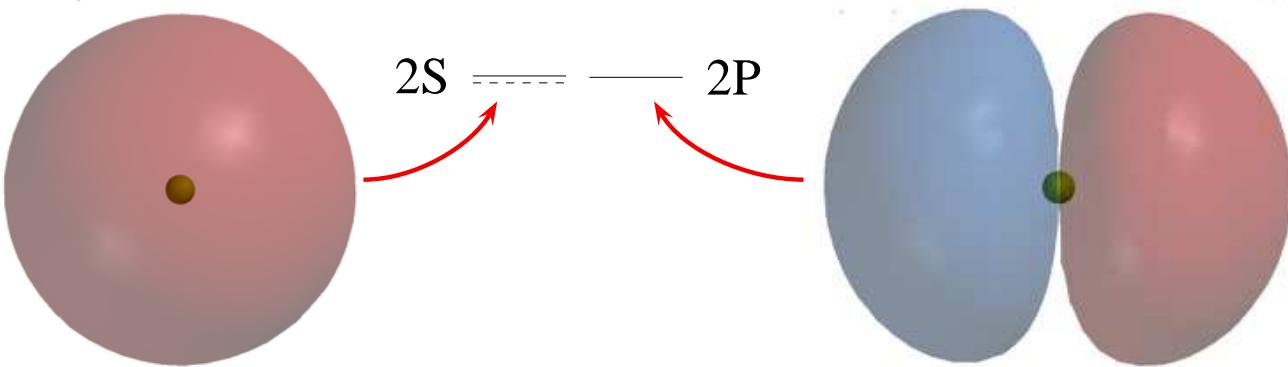
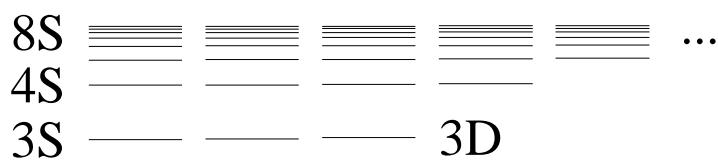
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S states are shifted.

Shift ist proportional to the

size of the proton



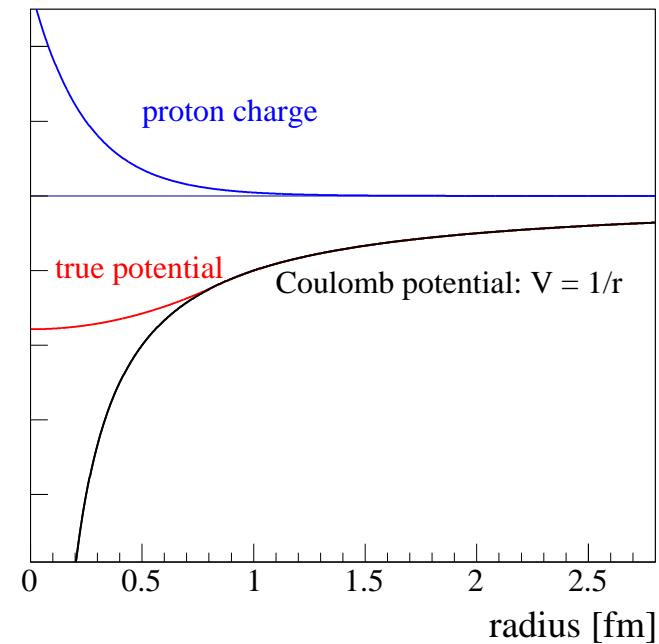
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Orbital pictures from Wikipedia

# Atomic and nuclear physics



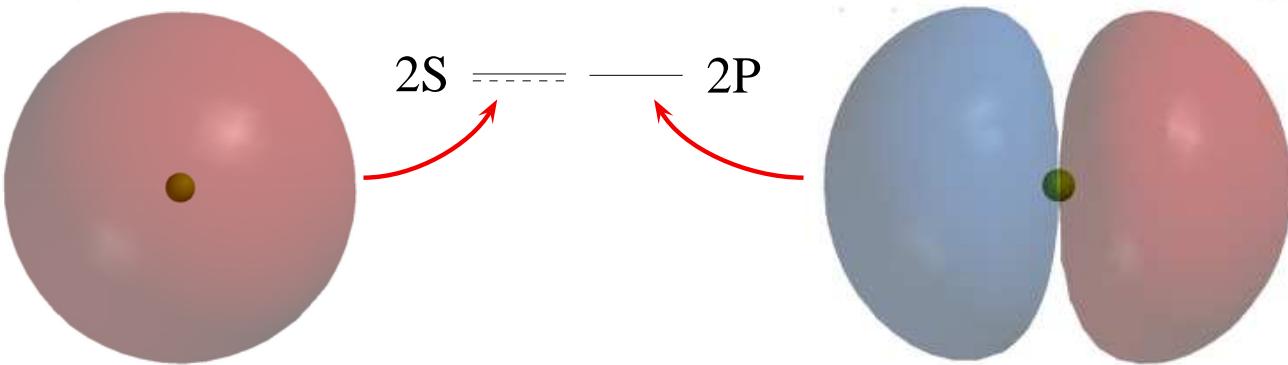
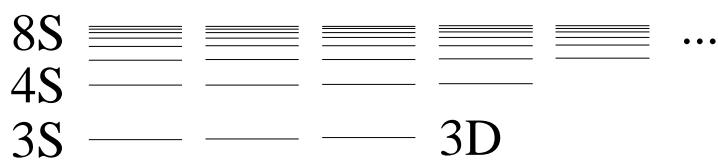
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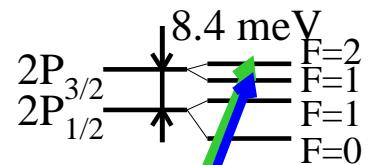
Orbital pictures from Wikipedia

# Proton charge radius and muonic hydrogen

Lamb shift in  $\mu p$  [meV]:

$$\Delta E = 206.0668(25) - 5.2275(10) r_p^2$$

$\mu p(n=2)$  levels:



Proton size effect is **2%** of the  $\mu p$  Lamb shift

Measure to  $10^{-5}$   $\Rightarrow$   $r_p$  to 0.05 %

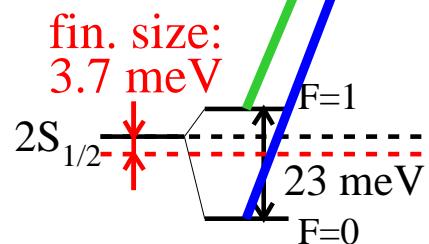
Experiment:

R. Pohl *et al.*, Nature 466, 213 (2010).

A. Antognini, RP *et al.*, Science 339, 417 (2013).

Theory summary:

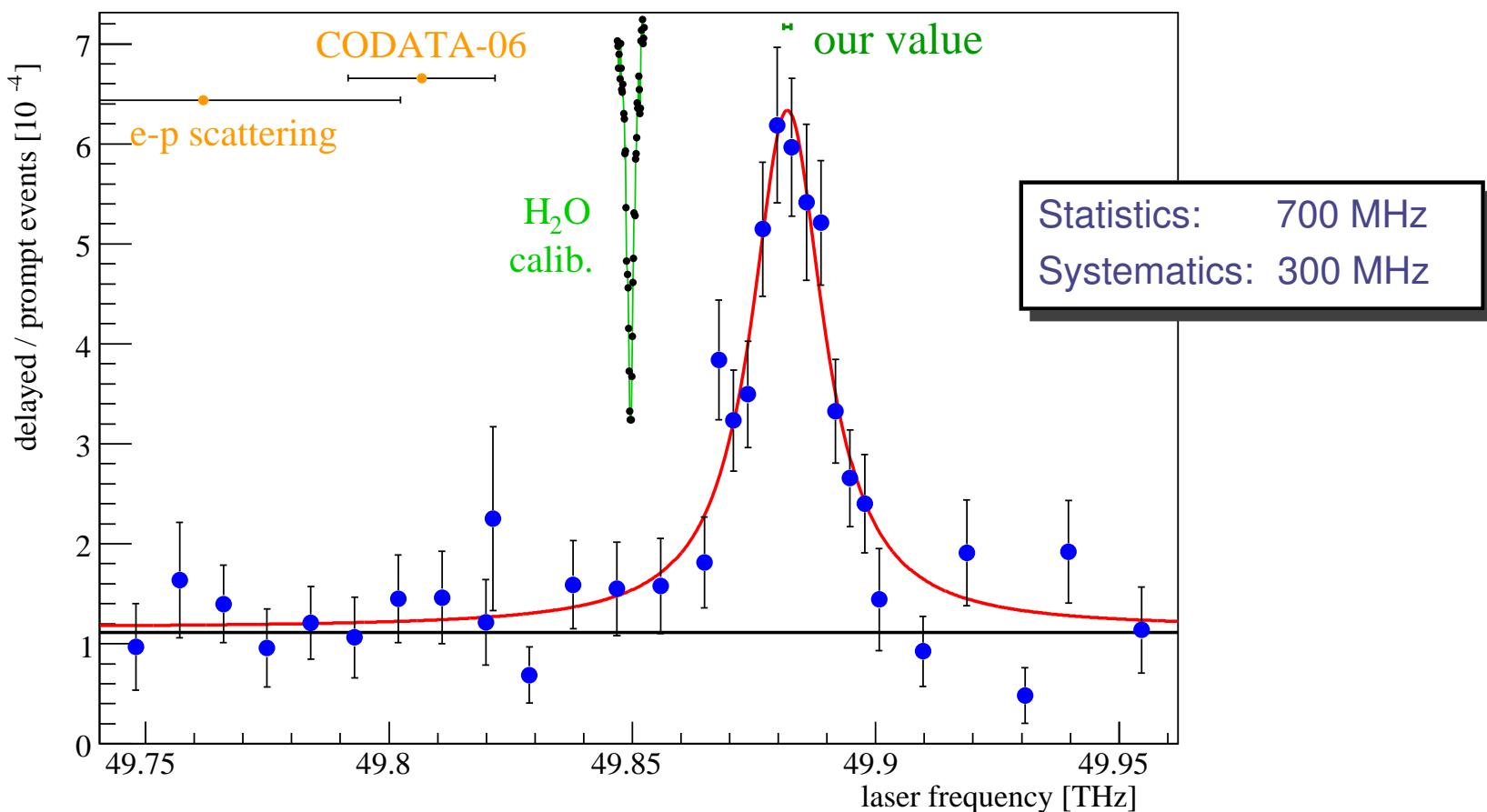
A. Antognini, RP *et al.*, Ann. Phys. 331, 127 (2013).



# The resonance: discrepancy, sys., stat.

Water-line/laser wavelength:  
300 MHz uncertainty

$\Delta\nu$  water-line to resonance:  
200 kHz uncertainty



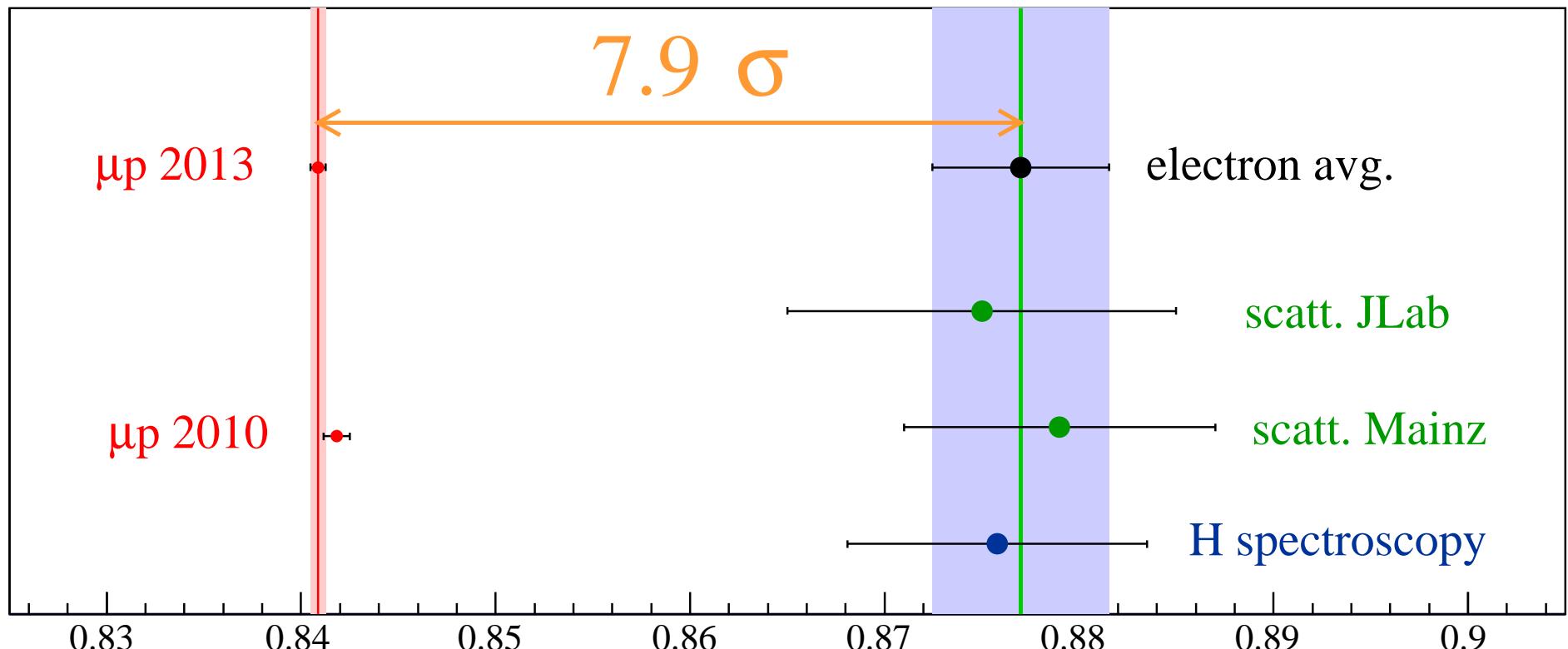
Discrepancy:  
 $5.0\sigma \leftrightarrow 75 \text{ GHz} \leftrightarrow \delta\nu/\nu = 1.5 \times 10^{-3}$

R. Pohl *et al.*, Nature 466, 213 (2010).  
A. Antognini, RP *et al.*, Science 339, 417 (2013).

# The proton radius puzzle.

# The proton radius puzzle

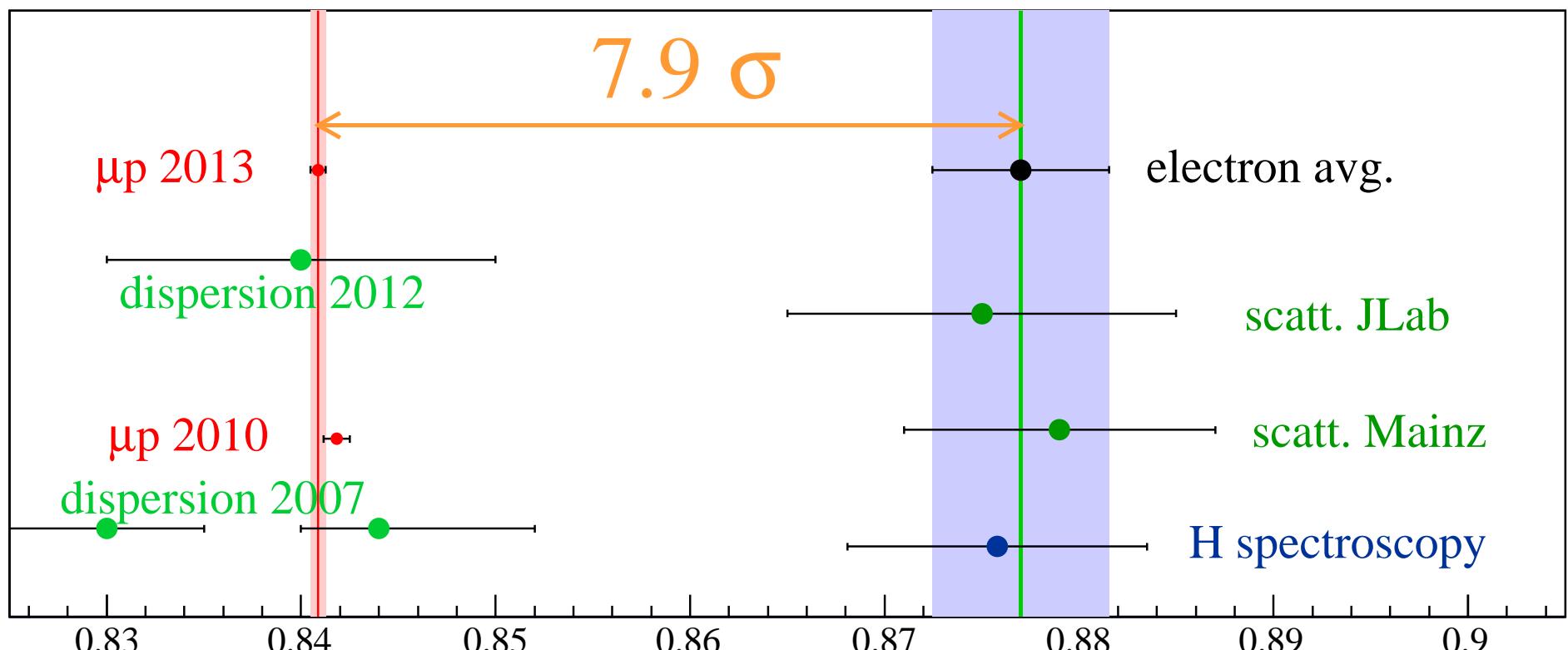
The proton rms charge radius measured with  
electrons:  $0.8770 \pm 0.0045$  fm  
muons:  $0.8409 \pm 0.0004$  fm



R. Pohl *et al.*, Nature 466, 213 (2010).  
A. Antognini *et al.*, Science 339, 417 (2013).

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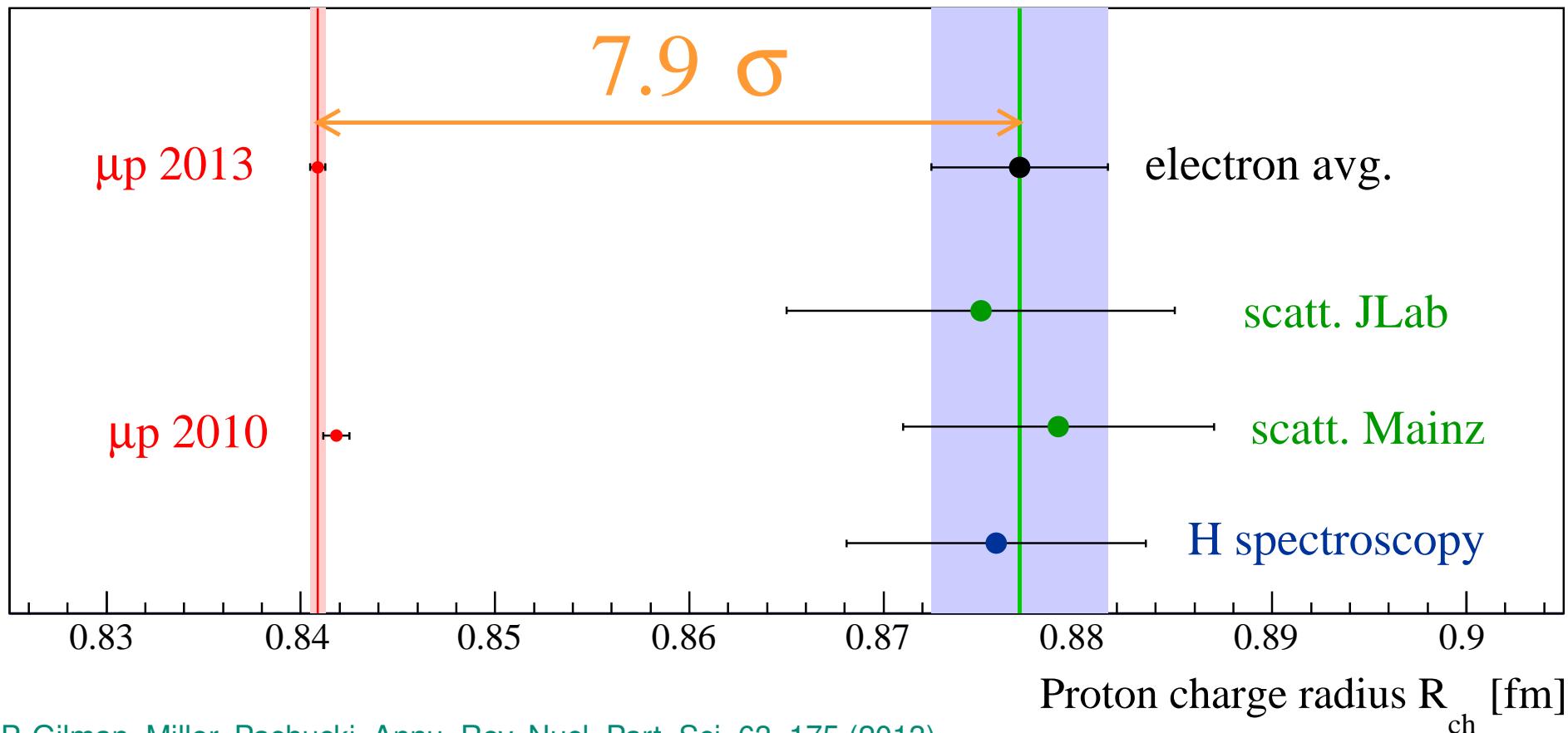


Belushkin, Hammer, Meissner PRC 75, 035202 (2007).

Lorenz, Hammer, Meissner EPJ A 48, 151 (2012).

# The proton radius puzzle

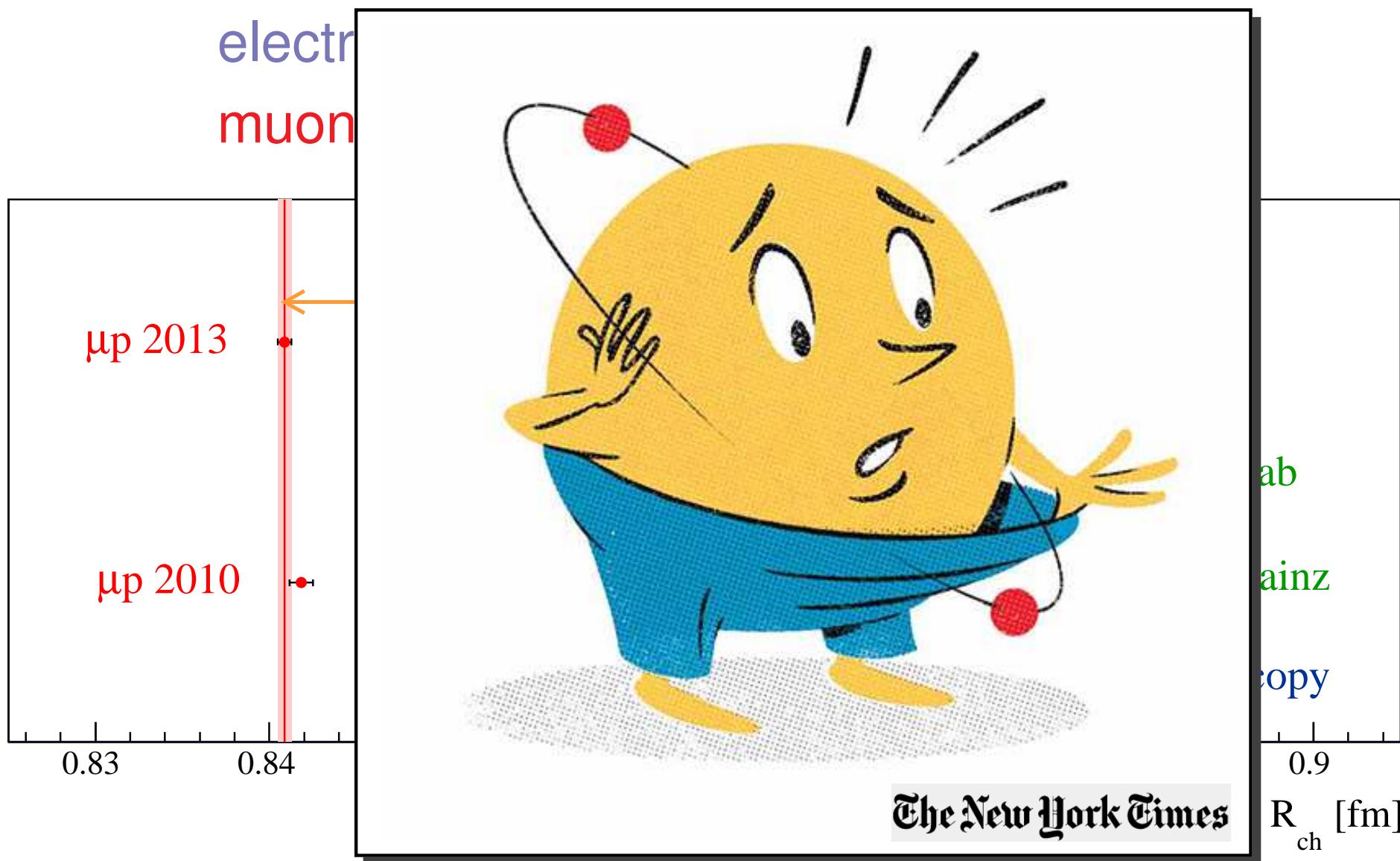
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muons:  $0.8409 \pm 0.0004$  fm



RP, Gilman, Miller, Pachucki, Annu. Rev. Nucl. Part. Sci. 63, 175 (2013).

# The proton radius puzzle

The proton rms charge radius measured with



# Muons in the news



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# nature

OIL SPILLS  
There's more to come

PLAGIARISM  
It's worse than you think

CHIMPANZEES  
The battle for survival

NATUREJOBS  
Researchers for hire

## SHRINKING THE PROTON

New value from exotic atom trims radius by four per cent

\$10.00US \$12.99CAN

275

0 71486 03070 6

# Muons in the news



8 July 2010 | www.nature.com/nature | \$10 THE INTERNATIONAL WEEKLY JOURNAL OF SCIENCE ASSOCIATION OF ASIA PACIFIC PHYSICAL SOCIETIES

# nature APPS

Volume 23 Number 2 APRIL 2013 Bulletin

OIL SPILLS There's more to come  
PLAGIARISM It's worse than you think  
CHIMPANZEES The battle for survival  
NATUREJOBS Researchers for hire

## Proton Size Puzzle Reinforced

The diagram illustrates a complex scientific apparatus. At the top, a 'Proton beam line' with 'Protons' is directed towards a 'C-target'. Below this, a 'Momentum filter' and a 'Cyclotron trap' are shown. A 'BT solenoid' is positioned above a 'Ti target'. A 'Water vapor cell' is connected to a 'Raman cell'. A 'Ti:Sa cw laser' provides light for the Raman cell. A 'PP cavity' is connected to a 'Ti:Sa oscillator'. Two 'Disk-laser' units are at the bottom, each connected to a 'Ti:Sa amplifier' and a 'SHG' (Second Harmonic Generation) unit. A 'Diode laser' is also present.

ISSN 0218-2203

<b>Feature Articles</b> <ul style="list-style-type: none"><li>• Neutrino Oscillation and Mixing</li><li>• Status and Prospect of Telescope Array Experiment</li></ul>	<b>Activities and Research News</b> <ul style="list-style-type: none"><li>• Proton Size Puzzle Reinforced</li><li>• Asia Pacific School/Workshop on Gravitation and Cosmology 2013</li></ul>	<b>Institutes in Asia Pacific</b> <ul style="list-style-type: none"><li>• Department of Physics Yonsei University</li><li>• Department of Physics at Korea University</li></ul>
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# Muons in the news



8 July 2010 | www.nature.com/nature | \$10 THE INTERNATIONAL WEEKLY JOURNAL OF SCIENCE ASSOCIATION OF ASIA PACIFIC PHYSICAL SOCIETIES

# nature

INSIDE THE NEANDERTHAL BRAIN  
First hints of how their minds differed from ours

# NewScientist

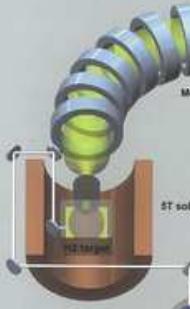
WEEKLY July 20 - 26, 2013

OIL SPILLS  
There's more to come

PLAGIARISM  
It's worse than you think

CHIMPANZEES  
The battle for survival

NATUREJOBS  
Researchers for hire



# TINY PARTICLE BIG PROBLEM

The humble proton is nothing like we expected



Feature Articles:

- Neutrino Oscillation and Mixing
- Status and Prospect of Telescope Array Experiment

No 2926 US\$5.95 CAN\$5.95

EVOLUTION IN MINIATURE

It works differently if you're small

Science and technology news [www.newscientist.com](http://www.newscientist.com) US jobs in science

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CAR HACKING  
Could cyberattackers arrange a crash?

LONG STORY  
How the Diplodocus got its neck

WINDS OF CHANGE  
Gale-force warnings from Antarctica

# Muons in the news



J. Bernauer, RP

# Muons in the news



J. Bernauer, RP

# ECT\* Workshop



“The Proton Radius Puzzle”, Trento, Italy, Oct. 28 - Nov. 2, 2012



G.A. Miller, R. Gilman, RP

47 theorists + experimentalists

- atomic physics
- electron scattering
- nuclear physics
- Beyond SM

38 talks

3 “fighting” sessions

⇒ no solution

voting: more data needed

RP, R. Gilman, G.A. Miller, K. Pachucki,  
“Muonic hydrogen and the proton radius  
puzzle”,  
Annu. Rev. Nucl. Part. Sci. **63**, 175 (2013)  
(arXiv 1301.0905)

# What may be wrong?

$$\tilde{L}_{\mu p}^{\text{theo.}}(r_p^{\text{CODATA}}) - \tilde{L}_{\mu p}^{\text{exp.}} = \begin{cases} 75 \text{ GHz} \\ 0.31 \text{ meV} \\ 0.15 \% \end{cases}$$

$\mu p$  theory wrong?  
 $\mu p$  experiment wrong?  
 H theory wrong?  
 H experiments wrong?  $\rightarrow R_\infty$  wrong?  
 AND e-p scattering exp. wrong?  
 Standard Model wrong?!?

RP, R. Gilman, G.A. Miller, K. Pachucki, "Muonic hydrogen and the proton radius puzzle",  
 Annu. Rev. Nucl. Part. Sci. **63**, 175 (2013) (arXiv 1301.0905)

# What may be wrong?

$$\tilde{L}_{\mu p}^{\text{theo.}}(r_p^{\text{CODATA}}) - \tilde{L}_{\mu p}^{\text{exp.}} = \begin{cases} 75 \text{ GHz} \\ 0.31 \text{ meV} \\ 0.15 \% \end{cases}$$

$\mu p$  theory

New measurements:

- Muonic hydrogen, deuterium, helium ions
- Hydrogen spectroscopy  $\Rightarrow$  Rydberg constant,  $r_p$
- Helium ion  $\Rightarrow$  Rydberg constant, QED test
- Elastic electron scattering at lower  $Q^2$ , p, d, He
- Muon scattering: MUSE @ PSI

Theory:

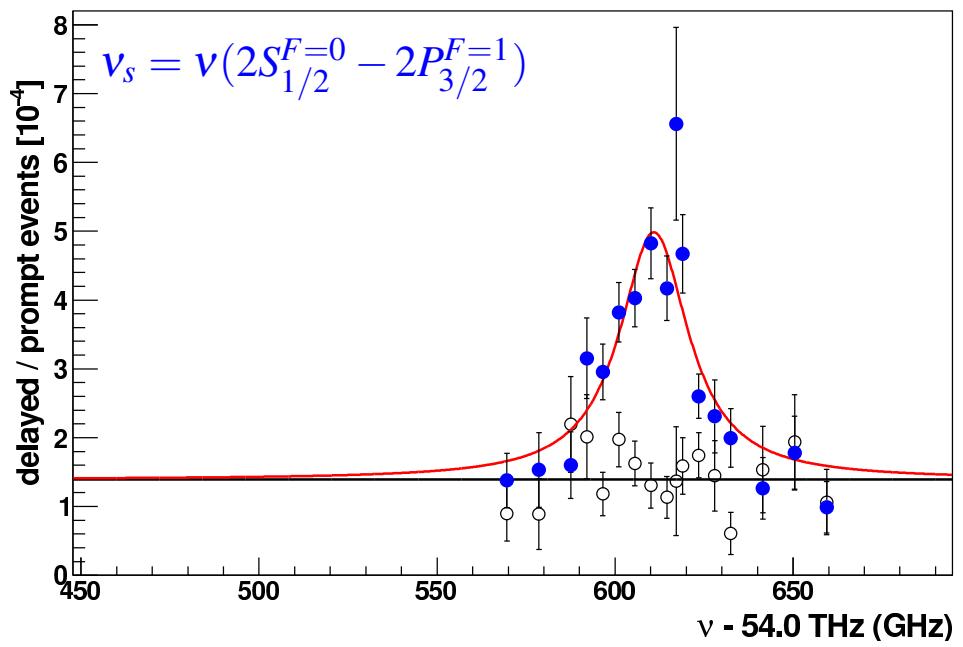
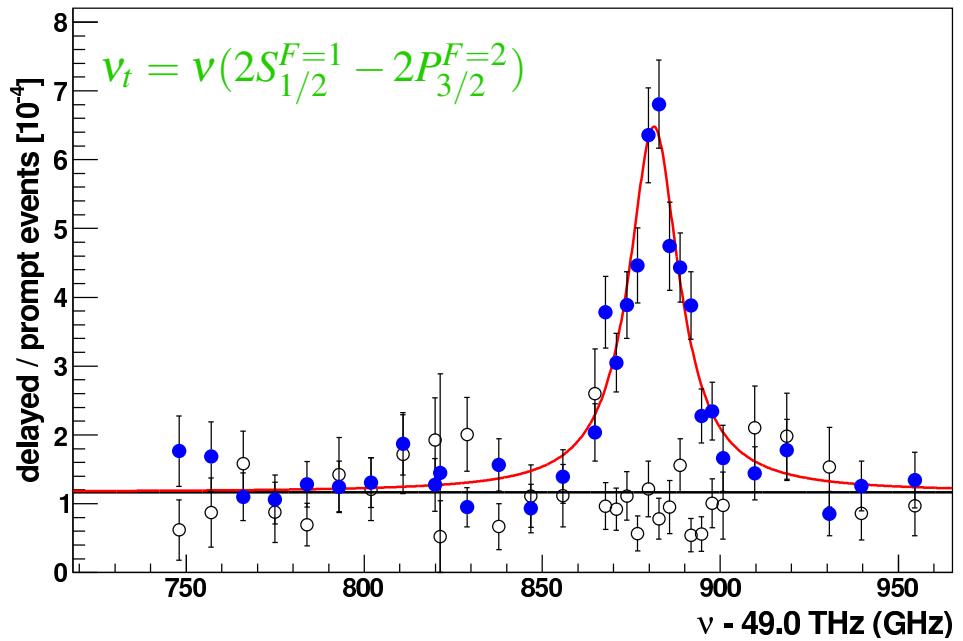
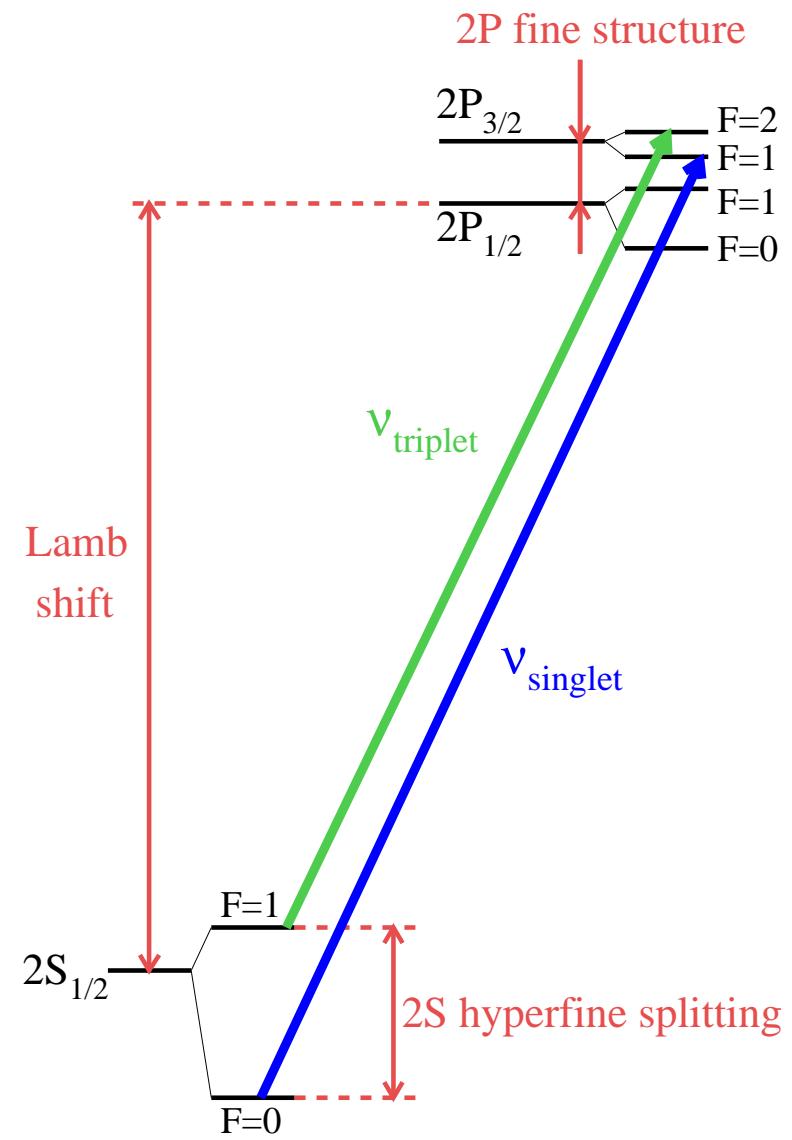
- QED in electronic and muonic atoms
- Nucl. structure effects: p, d,  $^{3,4}\text{He}$ , ...
- Electron scattering
- Lattice
- ...

RP, R. Gilma

Annu. Rev. Nucl. Part. Sci. 63, 173 (2013) (arXiv:1307.0008)

# Muonic hydrogen

# We have measured two transitions in $\mu$ p



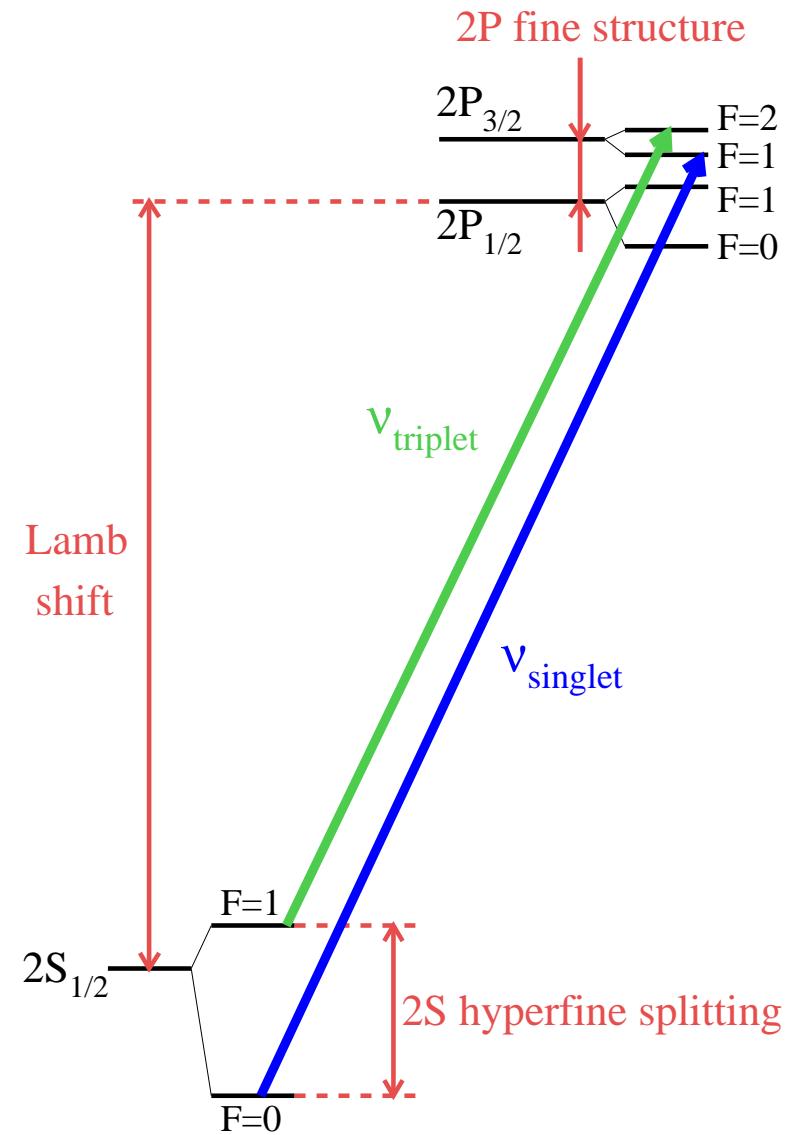
# We have measured two transitions in $\mu$ p

- Consider the two measurements separately

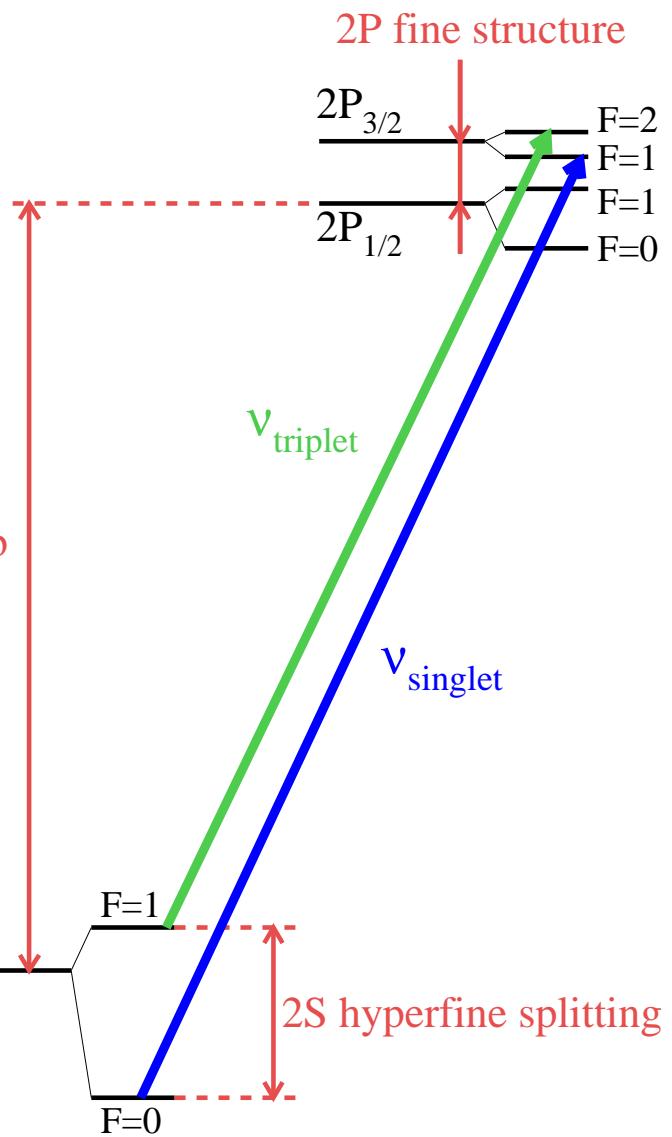
Two independent determinations of  $r_p$

( $v_t \rightarrow r_p$  ,  $v_s \rightarrow r_p$ )

Consistent results!



# We have measured two transitions in $\mu$ p



- Consider the two measurements separately

Two independent determinations of  $r_p$

( $v_t \rightarrow r_p$ ,  $v_s \rightarrow r_p$ )

Consistent results!

- Combine the two measurements

Two measurements  $\rightarrow$  determine two parameters

$v_t, v_s \rightarrow \Delta E_L, \Delta E_{\text{HFS}}$

$r_p, r_z$

$$\begin{aligned}\frac{3}{4}v_t + \frac{1}{4}v_s &= \Delta E_L(r_p) + 8.8123 \text{ meV} \\ v_s - v_t &= \Delta E_{\text{HFS}}(r_z) - 3.2480 \text{ meV}\end{aligned}$$

# Proton charge radius

$$\nu(2S_{1/2}^{F=1} \rightarrow 2P_{3/2}^{F=2}) = 49881.88(76) \text{ GHz} \quad \text{R. Pohl } et al., \text{ Nature 466, 213 (2010)}$$

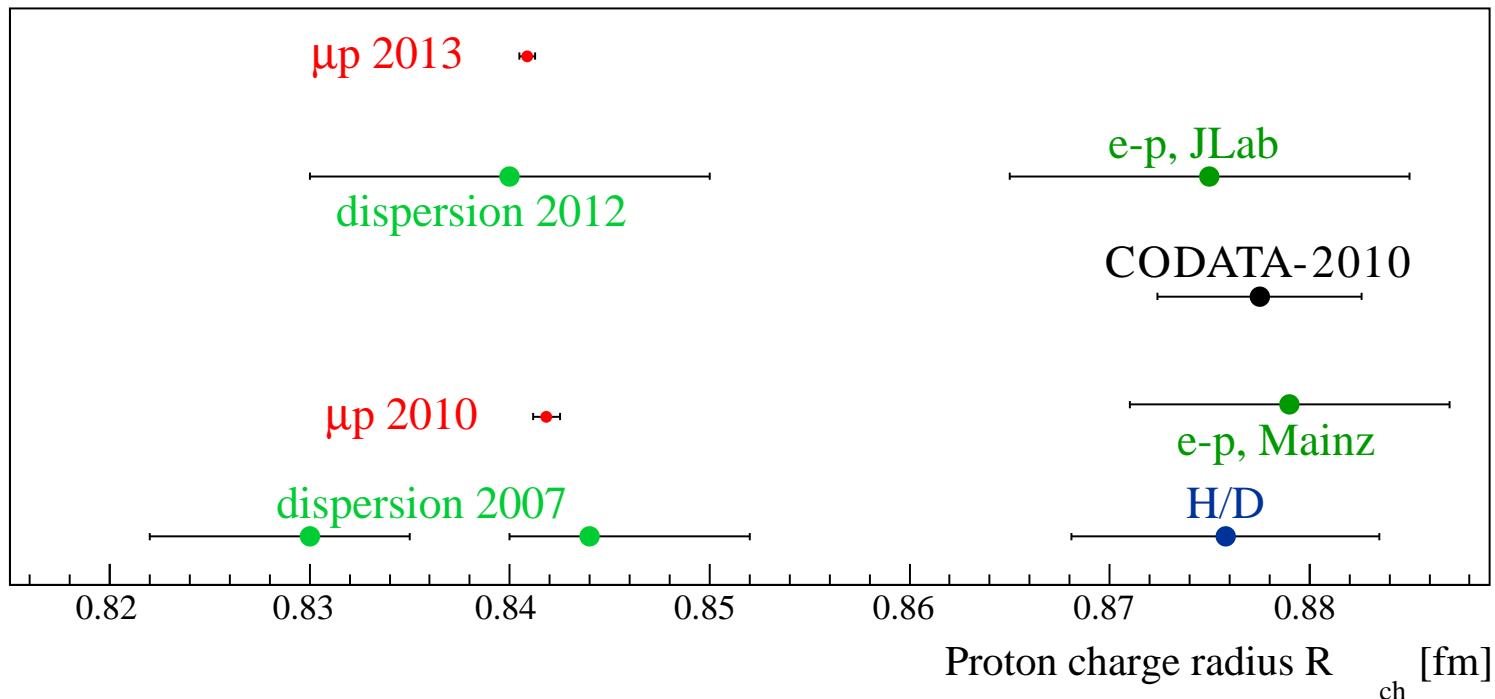
$$\nu(2S_{1/2}^{F=0} \rightarrow 2P_{3/2}^{F=1}) = 49881.35(65) \text{ GHz}$$

$$\nu(2S_{1/2}^{F=0} \rightarrow 2P_{3/2}^{F=1}) = 54611.16(1.05) \text{ GHz} \quad \left. \begin{array}{l} \\ \end{array} \right\} \begin{array}{l} \text{A. Antognini, RP } et al., \\ \text{Science 339, 417 (2013)} \end{array}$$

Proton charge radius:

$$r_p = 0.84087(26)_{\text{exp}}(29)_{\text{th}} = 0.84087(39) \text{ fm}$$

$\mu p$  theory summary: A. Antognini, RP *et al.*, Ann. Phys. 331, 127 (2013) [arXiv :1208.2637 (atom-ph)]



# Proton Zemach radius

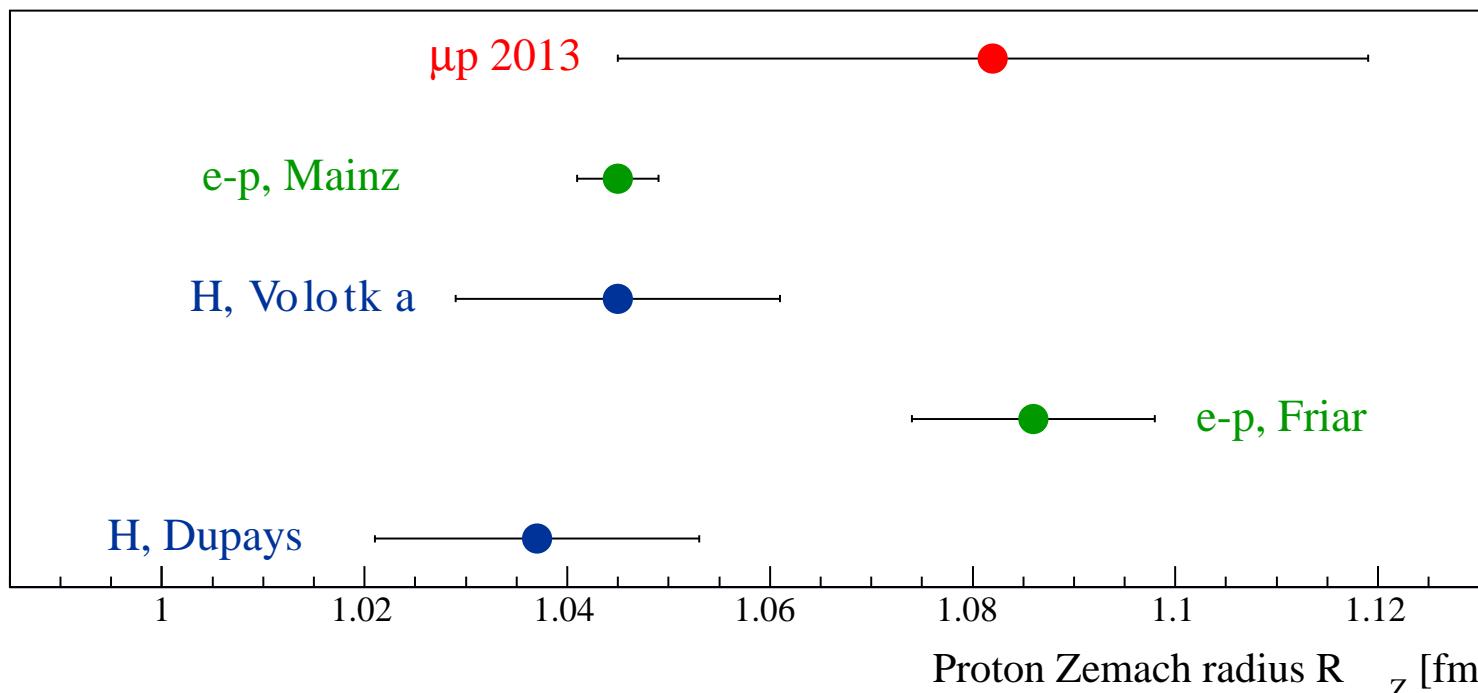
2S hyperfine splitting in  $\mu p$  is:  $\Delta E_{\text{HFS}} = 22.9843(30) - 0.1621(10) r_Z$  [fm] meV

$$\text{with } r_Z = \int d^3r \int d^3r' r \rho_E(r) \rho_M(r - r')$$

We measured

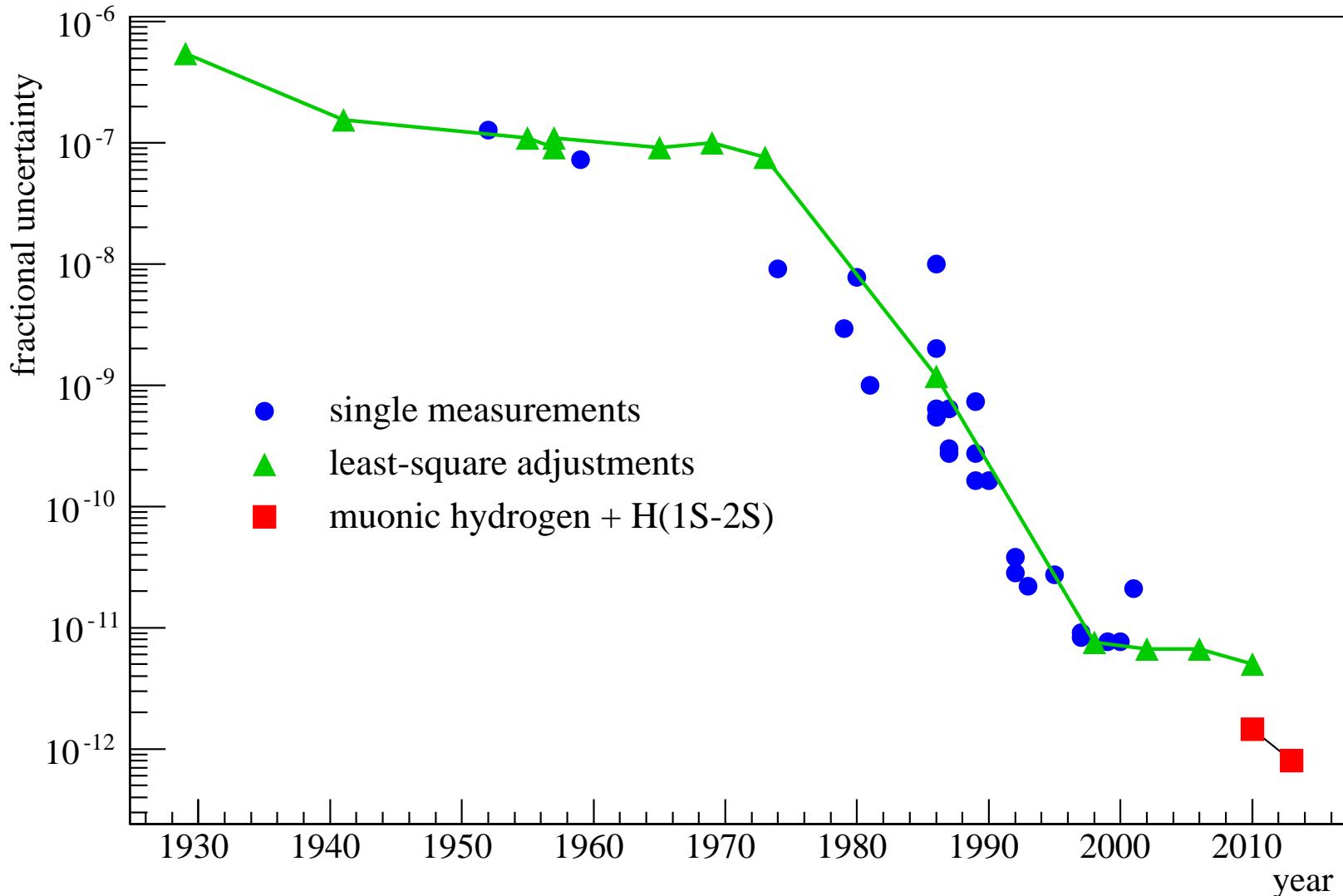
$$\Delta E_{\text{HFS}} = 22.8089(51) \text{ meV}$$

This gives a proton Zemach radius  $r_Z = 1.082(31)_{\text{exp}}(20)_{\text{th}} = 1.082(37) \text{ fm}$



A. Antognini, RP et al., Science 339, 417 (2013)

# Rydberg constant



H(1S-2S): C.G. Parthey, RP *et al.*, PRL 107, 203001 (2011).

$r_p$ : A. Antognini, RP *et al.*, Science 339, 417 (2013).

# Rydberg constant

Hydrogen spectroscopy (Lamb shift):

$$L_{1S}(r_p) = 8171.636(4) + 1.5645 \langle r_p^2 \rangle \text{ MHz}$$



2S ————— 2P

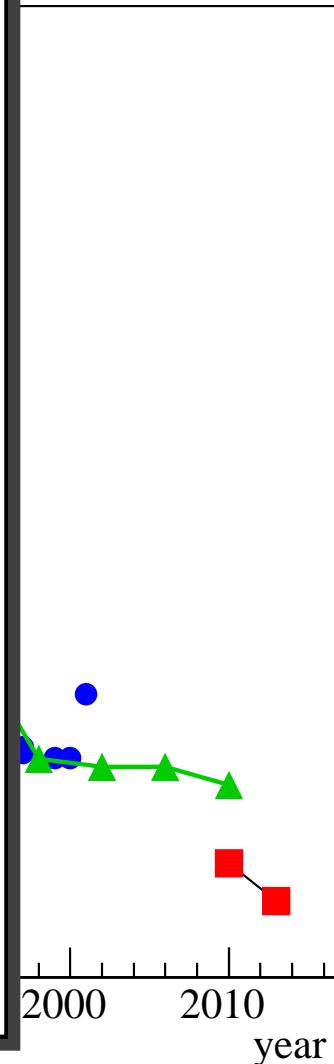
$$E_{nS} \simeq -\frac{R_\infty}{n^2} + \frac{L_{1S}}{n^3}$$

1S-2S

2 unknowns  $\Rightarrow$  2 transitions

- Rydberg constant  $R_\infty$
- Lamb shift  $L_{1S} \leftarrow r_p$

1S

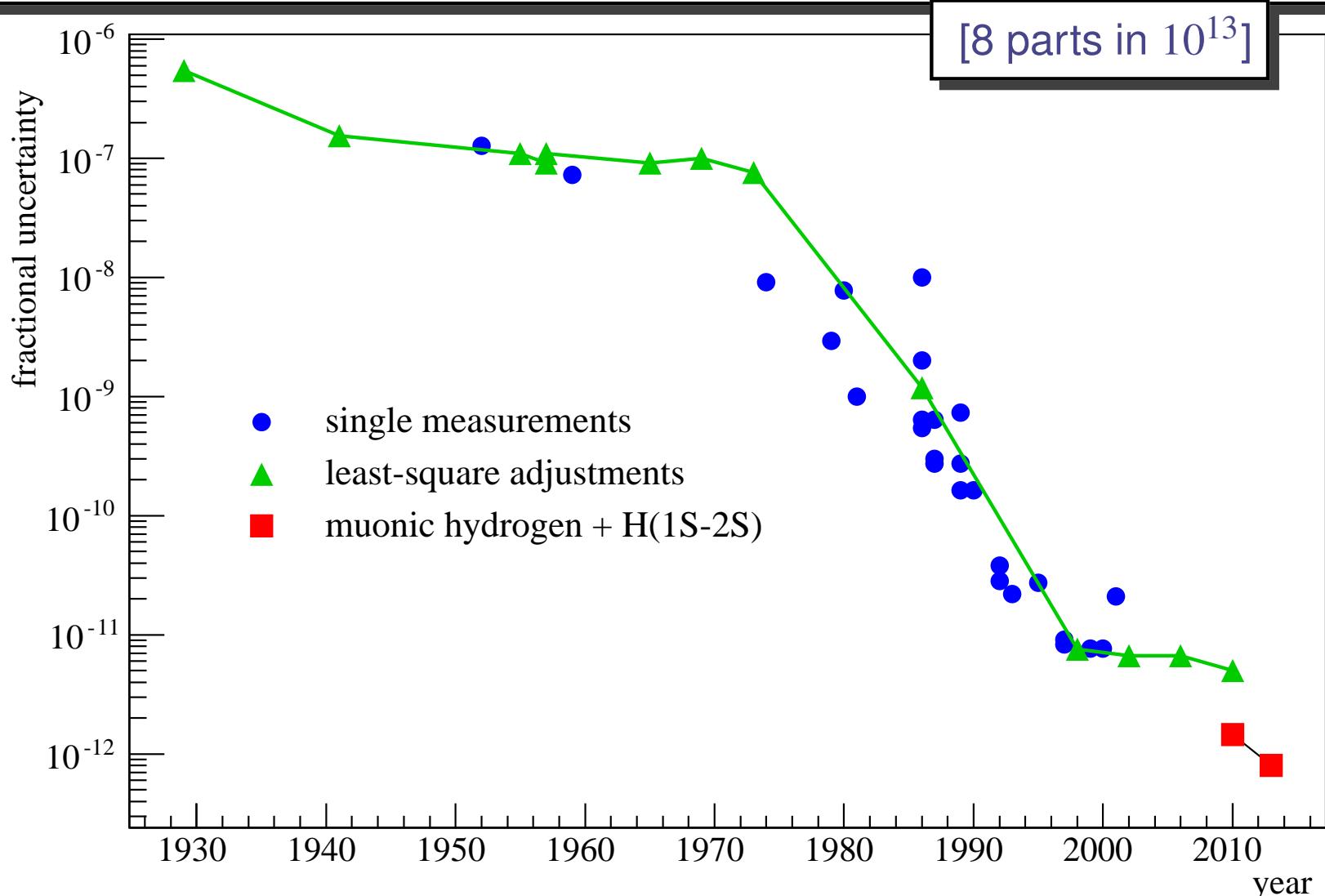


H(1S-2S): C.G. Parthey, RP *et al.*, PRL 107, 203001 (2011).

$r_p$ : A. Antognini, RP *et al.*, Science 339, 417 (2013).

# Rydberg constant

$$R_\infty = 3.289\ 841\ 960\ 249\ 5 (10)^{r_p} (25)^{\text{QED}} \times 10^{15} \text{ Hz/c}$$



H(1S-2S): C.G. Parthey, RP *et al.*, PRL 107, 203001 (2011).

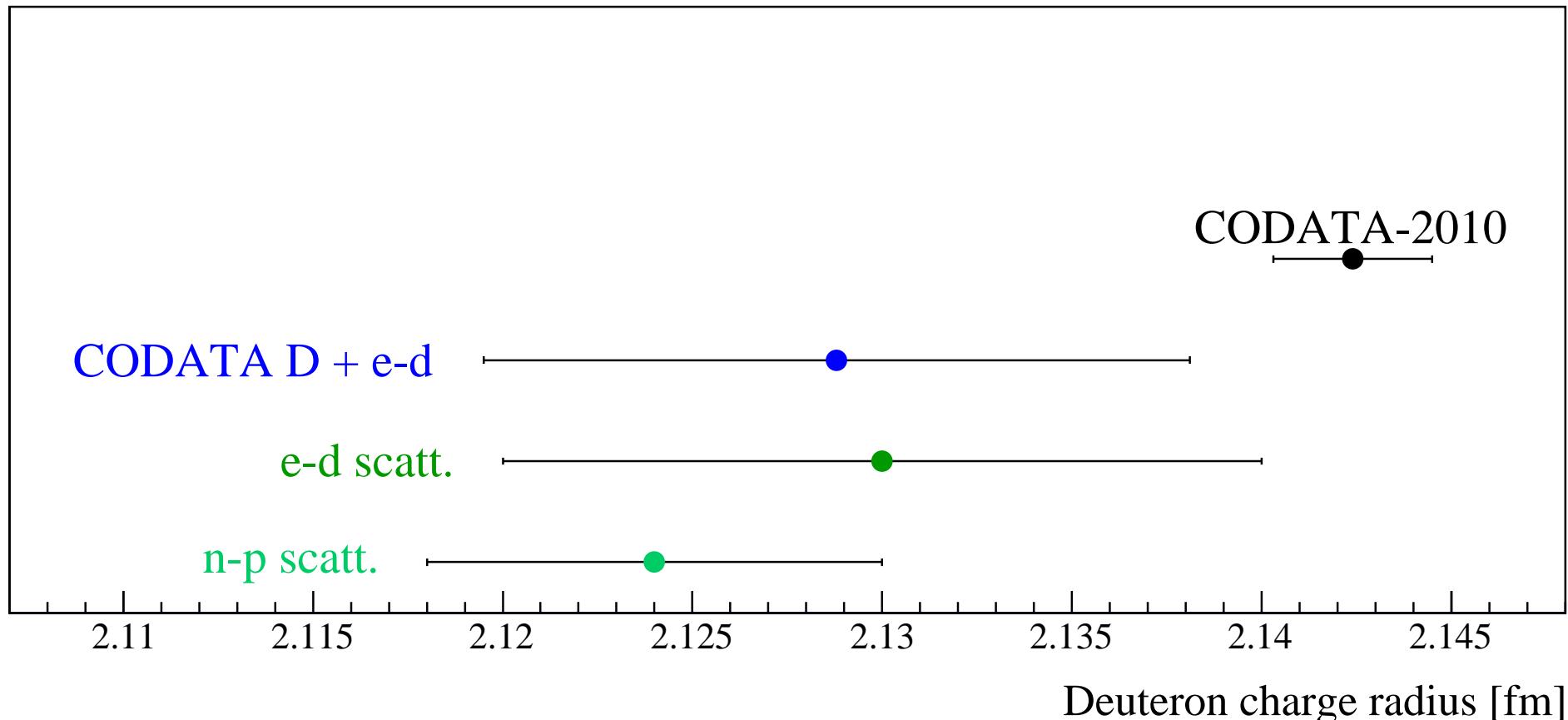
$r_p$ : A. Antognini, RP *et al.*, Science 339, 417 (2013).

# Deuteron charge radius

$$\text{H/D isotope shift: } r_d^2 - r_p^2 = 3.82007(65) \text{ fm}^2$$

C.G. Parthey, RP *et al.*, PRL **104**, 233001 (2010)

CODATA 2010     $r_d = 2.1424(21) \text{ fm}$



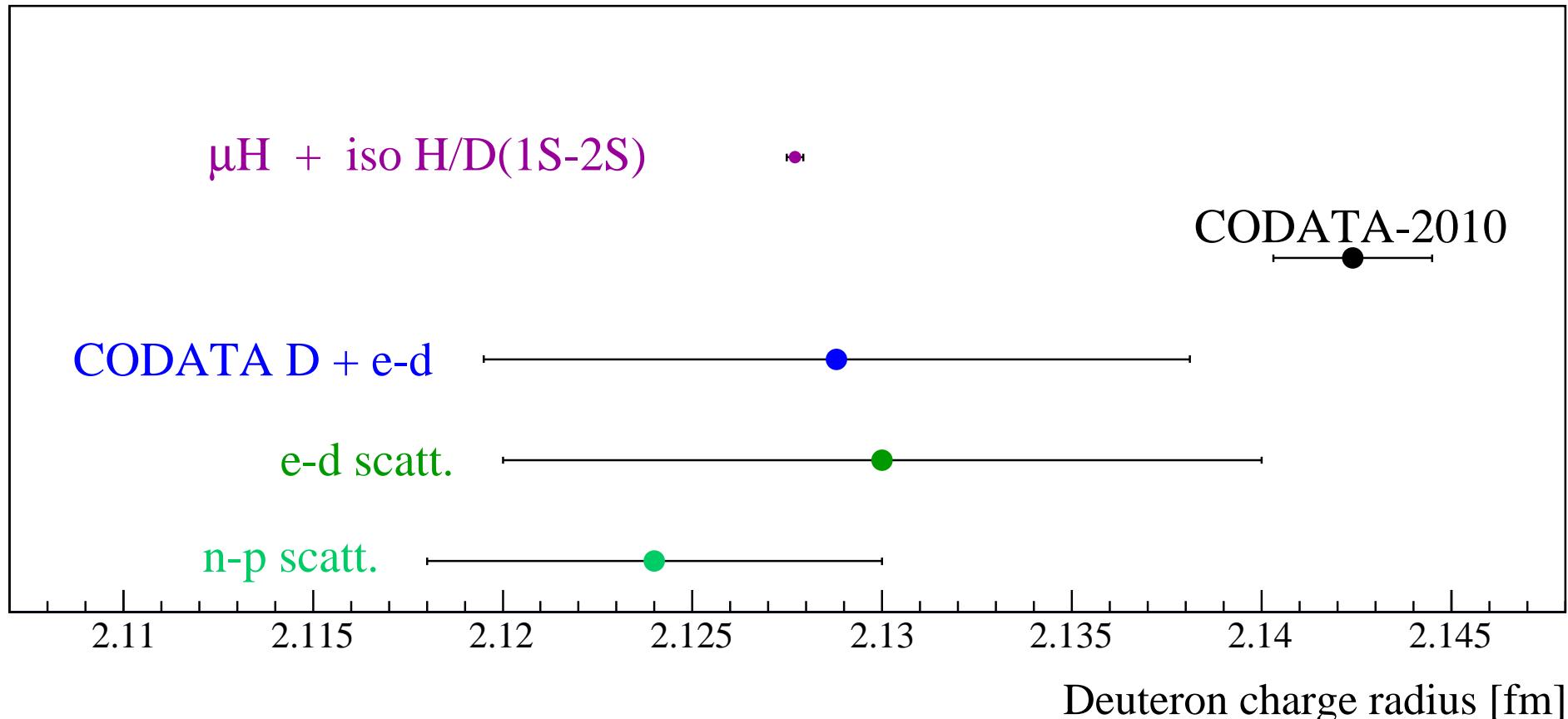
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C.G. Parthey, RP *et al.*, PRL **104**, 233001 (2010)

CODATA 2010     $r_d = 2.1424(21) \text{ fm}$

$r_p = 0.84087(39) \text{ fm}$  from  $\mu\text{H}$  gives     $r_d = 2.12771(22) \text{ fm}$



# Deuteron charge radius

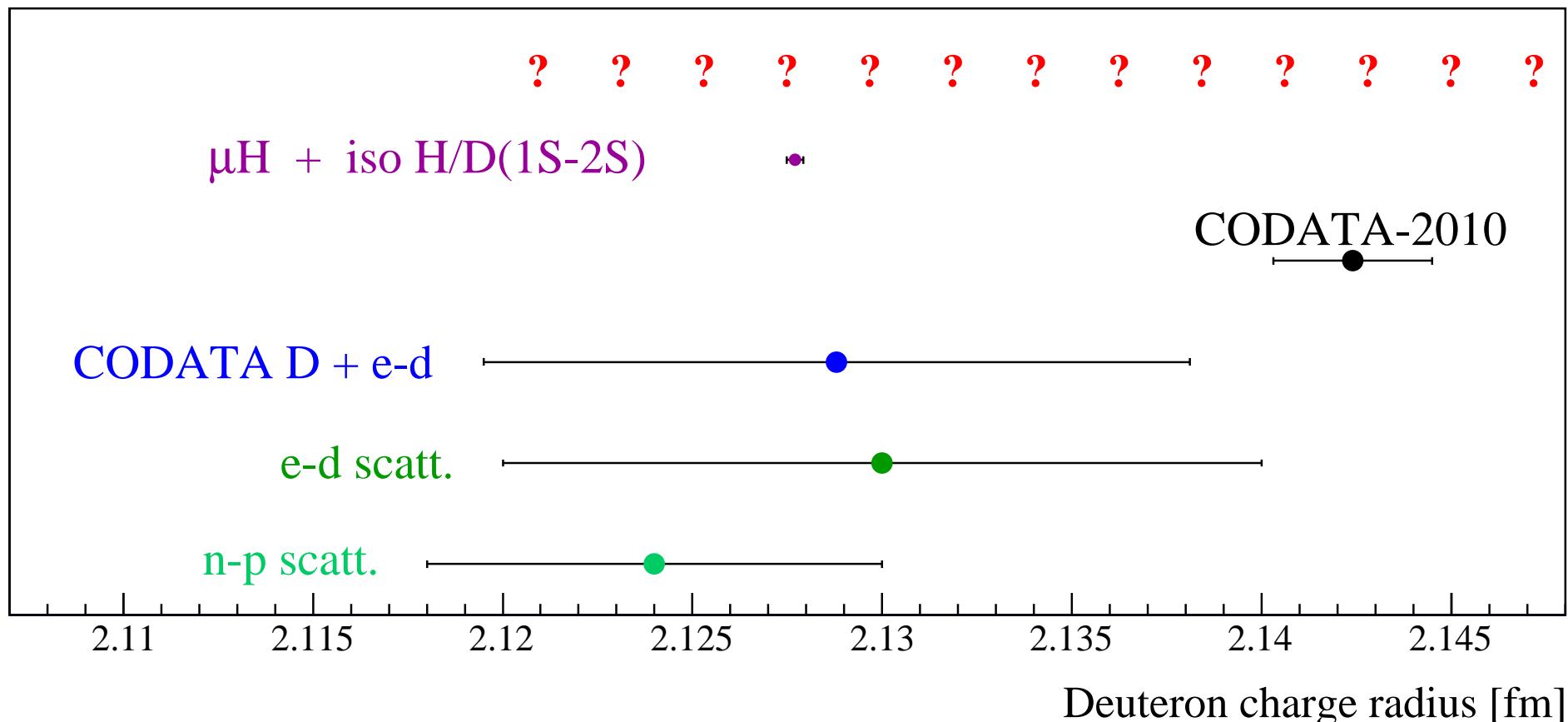
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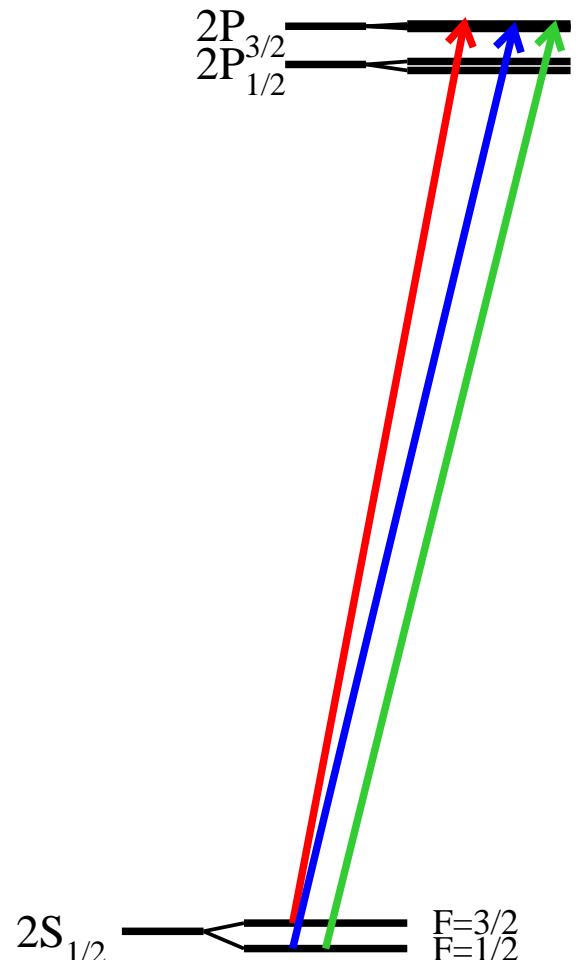
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Lamb shift in muonic DEUTERIUM

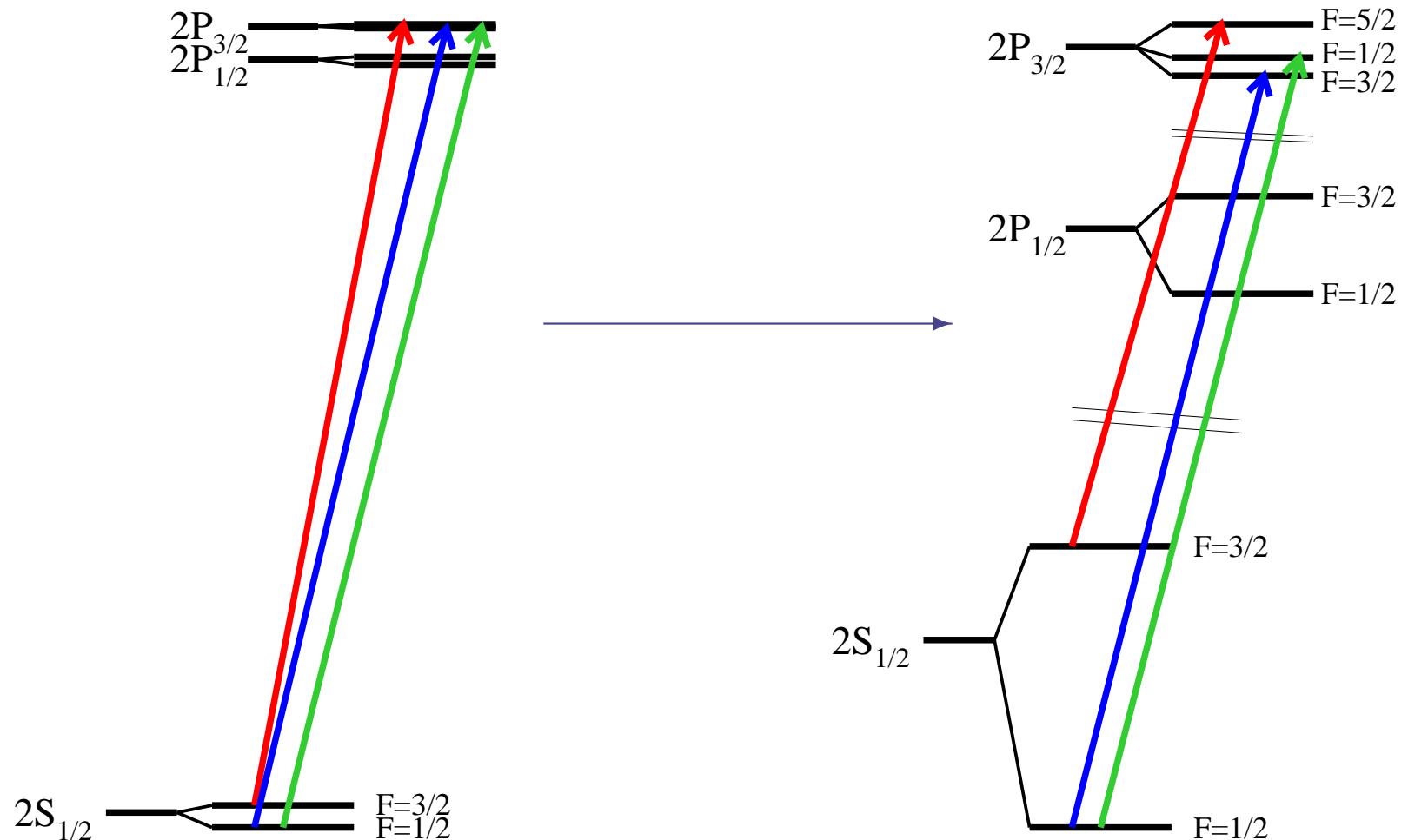


# Muonic deuterium

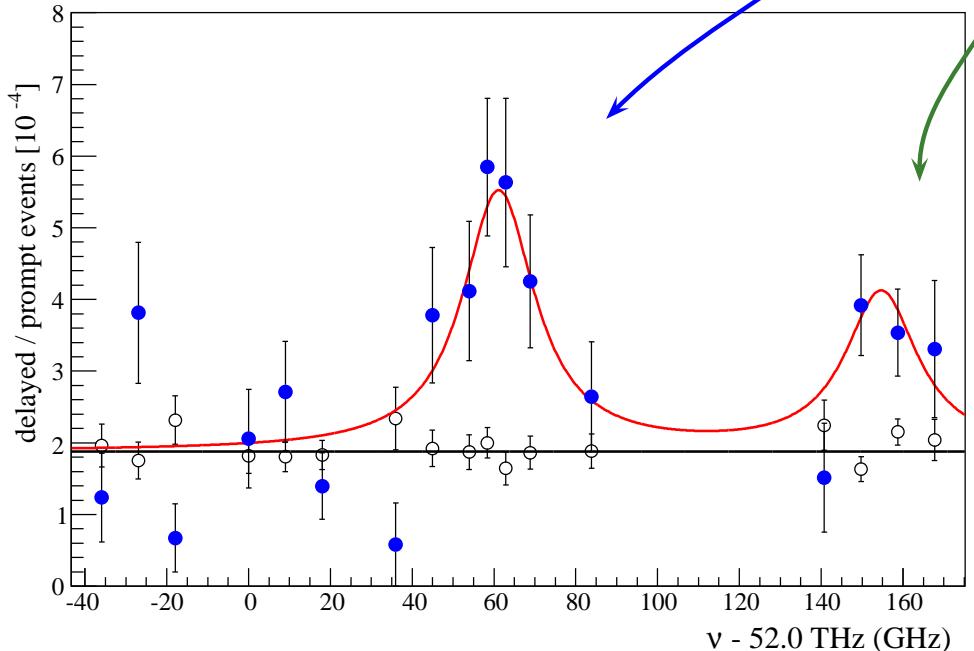
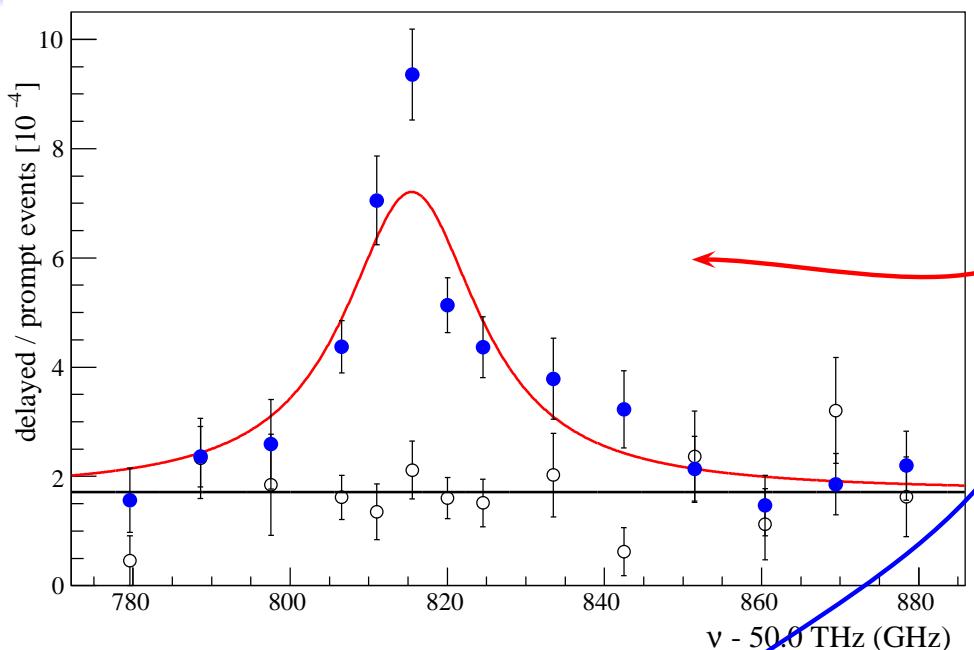
# muonic deuterium



# muonic deuterium



# Muonic DEUTERIUM

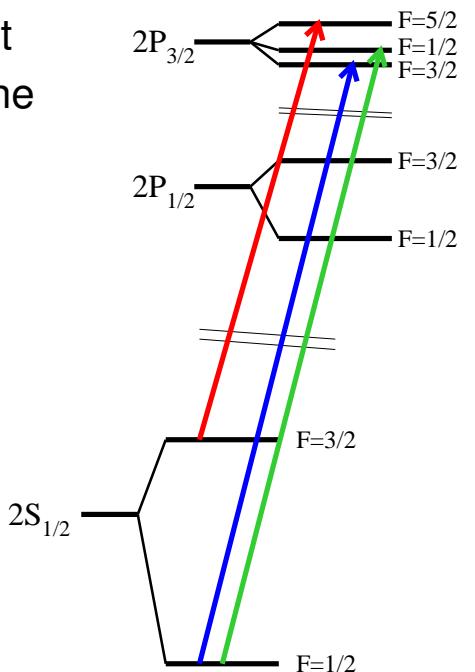


2.5 resonances in muonic **deuterium**

- $\mu d$  [  $2S_{1/2}(F=3/2) \rightarrow 2P_{3/2}(F=5/2)$  ]  
20 ppm (stat., online)

- $\mu d$  [  $2S_{1/2}(F=1/2) \rightarrow 2P_{3/2}(F=3/2)$  ]  
45 ppm (stat., online)

- $\mu d$  [  $2S_{1/2}(F=1/2) \rightarrow 2P_{3/2}(F=1/2)$  ]  
70 ppm (stat., online)  
only  $5\sigma$  significant  
identifies  $F=3/2$  line



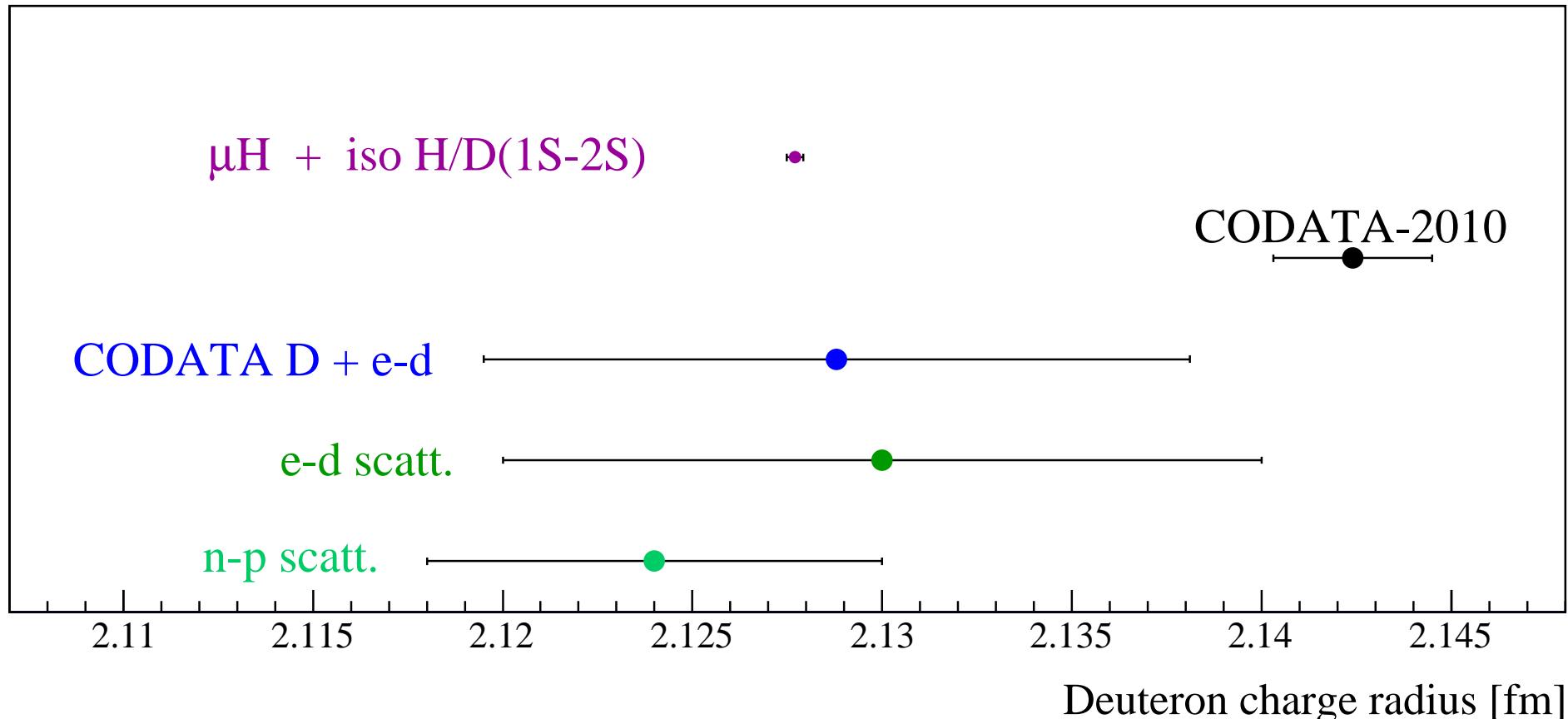
# Deuteron charge radius

$$\text{H/D isotope shift: } r_d^2 - r_p^2 = 3.82007(65) \text{ fm}^2$$

C.G. Parthey, RP *et al.*, PRL **104**, 233001 (2010)

CODATA 2010     $r_d = 2.1424(21) \text{ fm}$

$r_p = 0.84087(39) \text{ fm}$  from  $\mu\text{H}$  gives     $r_d = 2.1277(2) \text{ fm}$



# Deuteron charge radius

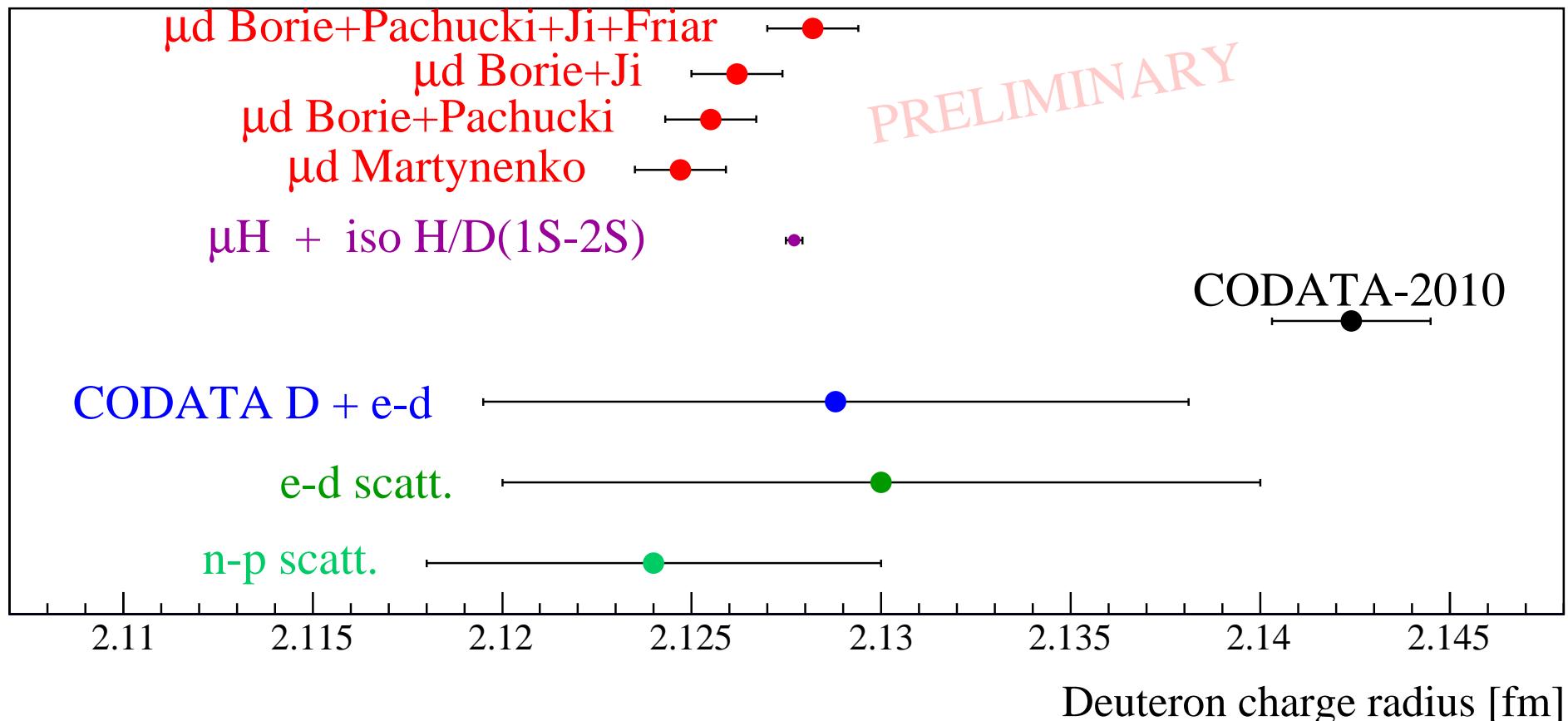
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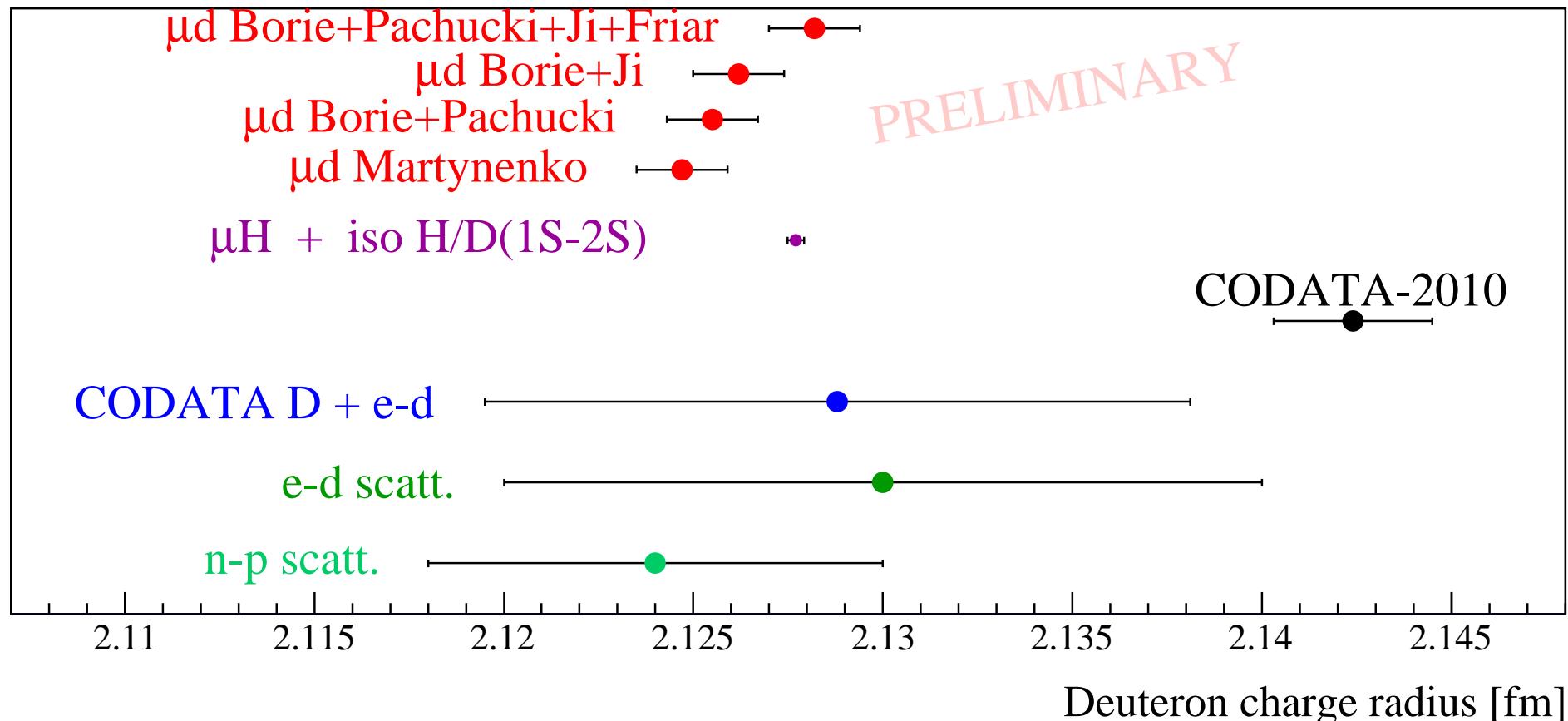
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Lamb shift in muonic DEUTERIUM     $r_d = 2.1282(12) \text{ fm}$     PRELIMINARY!



# Deuteron charge radius

- $\mu H$  and  $\mu D$  are **consistent!**  
(if BSM: no coupling to neutrons)
- WIP: deuteron polarizability (theory) complete? double-counting?
- WIP: shift from QM-interference



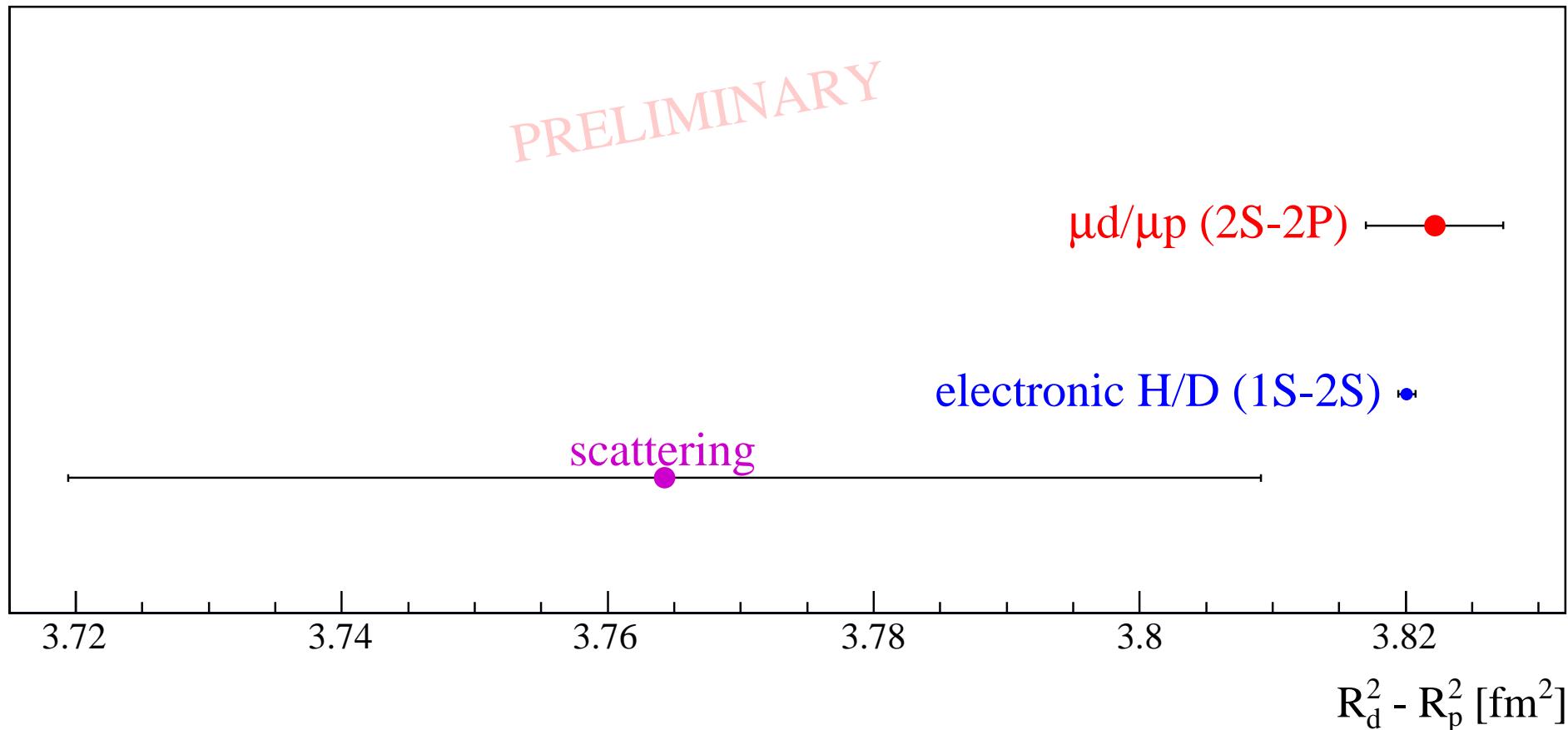
# Proton-deuteron isotope shift

In other words: The muonic isotope shift agrees with the electronic one!

$r_d^2 - r_p^2$ :	H/D isotope shift	$3.82007 \pm 0.00065 \text{ fm}^2$
	muonic Lamb shift	$3.8221 \pm 0.0052 \text{ fm}^2$
	scattering	$3.764 \pm 0.045 \text{ fm}^2$

PRELIMINARY!

The muonic error is conservative (nucl. structure terms).



# Muonic helium.

# Lamb shift in muonic helium

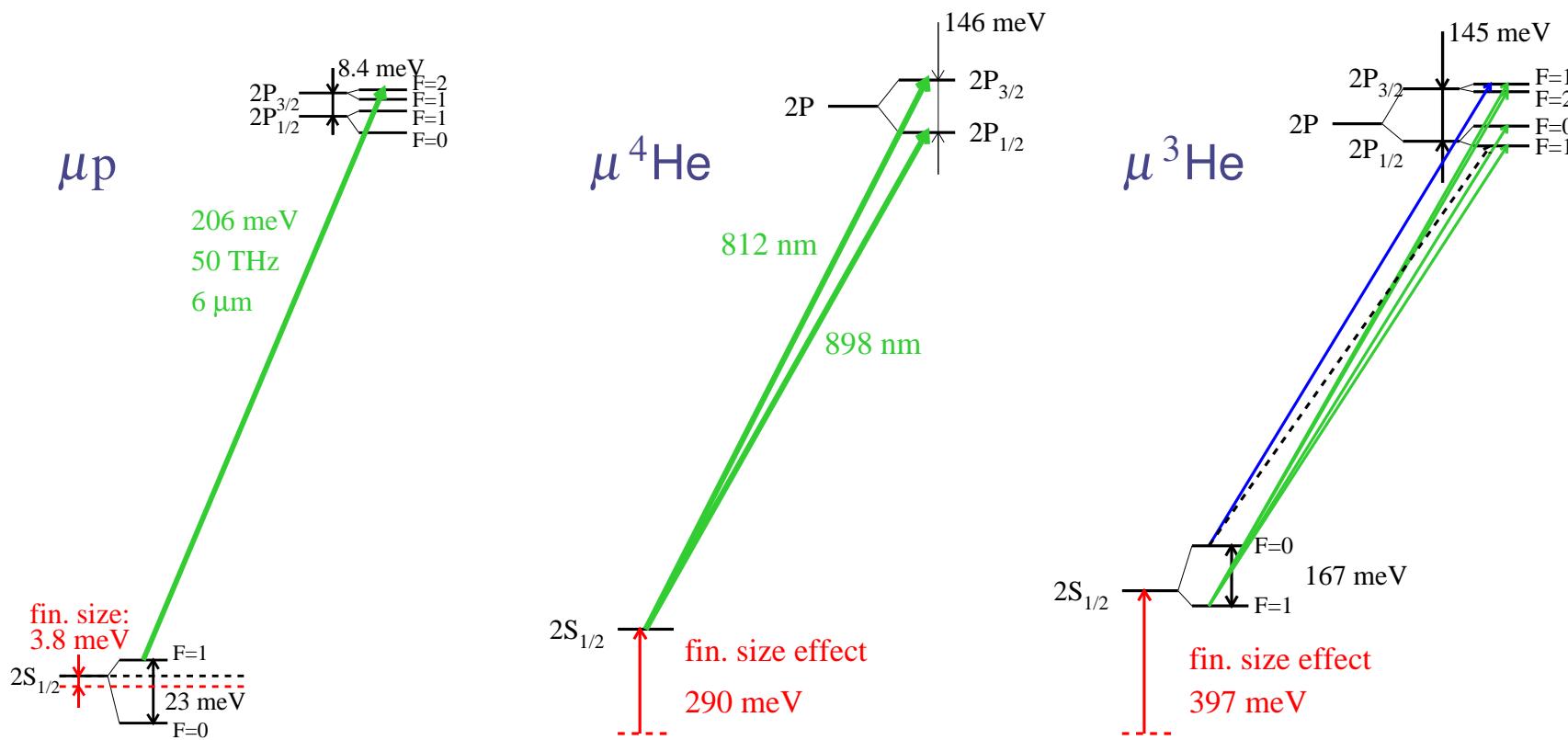


- CREMA collaboration: Charge Radius Experiment with Muonic Atoms
- Goal: Measure  $\Delta E(2S-2P)$  in  $\mu^4\text{He}$ ,  $\mu^3\text{He}$
- ⇒ alpha particle and helion charge radius to  $3 \times 10^{-4}$   
 $(\pm 0.0005 \text{ fm})$



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- aims:
  - help to solve the proton size puzzle
  - absolute charge radii of helion, alpha
  - low-energy effective nuclear models:  $^1\text{H}$ ,  $^2\text{D}$ ,  $^3\text{He}$ ,  $^4\text{He}$
  - QED test with  $\text{He}^+(1S-2S)$  [Udem @ MPQ, Eikema @ Amsterdam]



# Lamb shift in muonic helium



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  - QED test with  $\text{He}^+(1S-2S)$  [Udem @ MPQ, Eikema @ Amsterdam]
- $^4\text{He}$  beam time: Oct.-Dec. 2013
- $^3\text{He}$  beam time: May-Aug. 2014
- Talk by Aldo Antognini, tomorrow morning!

# Future muonic experiments



- Z=1:
  - Muonic hydrogen: HFS
  - Muonic deuterium: Lamb shift, HFS
  - Muonic tritium
- Z=2:
  - Muonic  $^4\text{He}$ : Fine structure
  - Muonic  $^3\text{He}$ : Lamb shift, fine and hyperfine structure
- Z=3, 4, 5:

Lamb shift: absolute charge radius

nuclear polarizability

2S-HFS: Zemach / magnetic radius

nuclear polarizability

PHYSICAL REVIEW A

VOLUME 32, NUMBER 2

AUGUST 1985

## Lamb shifts and fine-structure splittings for the muonic ions $\mu^-$ -Li, $\mu^-$ -Be, and $\mu^-$ -B: A proposed experiment

G. W. F. Drake and Louis L. Byer\*

Department of Physics, University of Windsor, Windsor, Ontario, Canada N9B 3P4

(Received 28 February 1985)

Detailed calculations are presented for the energy splittings of the states  $2s_{1/2}-2p_{1/2}$  and  $2s_{1/2}-2p_{3/2}$  for the muonic ions  $\mu^-$ -Li,  $\mu^-$ -Be, and  $\mu^-$ -B obtained by numerical integration of the Dirac equation. It is shown that there is severe cancellation between the vacuum polarization and finite nuclear size contributions to the energy differences, leading to transition frequencies which lie in the visible region of the spectrum. As a consequence of the cancellation, a measurement of the transition frequency would provide a sensitive probe of nuclear size and structure. The system  $\mu^-$ - $^7\text{Li}$  appears to offer particularly good possibilities for performing such an experiment.

# Future muonic experiments

- Z=1:
  - Muonic hydrogen: HFS
  - Muonic deuterium: Lamb shift, HFS
  - Muonic tritium
- Z=2:
  - Muonic  ${}^4\text{He}$ : Fine structure
  - Muonic  ${}^3\text{He}$ : Lamb shift, fine and hyperfine structure
- Z=3, 4, 5:

Lamb shift: absolute charge radius

nuclear polarizability

2S-HFS: Zemach / magnetic radius

nuclear polarizability

TABLE VII. Calculated absorption wavelengths (in Å) for transitions in muonic ions. The first uncertainty listed for the wavelengths is that due to nuclear polarization and the second is that due to the rms nuclear radius  $R$ .

Ion	$R$ (fm)	$\lambda(2s_{1/2}-2p_{1/2})$	$\lambda(2s_{1/2}-2p_{3/2})$
${}^4\text{He}$	$1.674 \pm 0.012$	$8978.0 \pm 4 \pm 27$	$8118.0 \pm 3 \pm 22$
${}^6\text{Li}$	$2.56 \pm 0.05$	$10097.0 \pm 33 \pm 1072$	$6275.0 \pm 13 \pm 414$
${}^7\text{Li}$	$2.39 \pm 0.03$	$7473.0 \pm 18 \pm 334$	$5147.0 \pm 9 \pm 159$
${}^9\text{Be}$	$2.520 \pm 0.012$	$-9520.0 \pm 116 \pm 703$	$11\,512.0 \pm 173 \pm 1048$
${}^{10}\text{B}$	$2.45 \pm 0.12$	$-1393.0 \pm 3 \pm 354$	$-4033.0 \pm 27 \pm 2947$
${}^{11}\text{B}$	$2.42 \pm 0.12$	$-1481.0 \pm 4 \pm 397$	$-4887.0 \pm 46 \pm 4286$

Drake, Byer, PRA 32, 713 (1985)

# Future muonic experiments

- Z=1:
  - Muonic hydrogen: HFS
  - Muonic deuterium: Lamb shift, HFS
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- Z=2:
  - Muonic  $^4\text{He}$ : Fine structure
  - Muonic  $^3\text{He}$ : Lamb shift, fine and hyperfine structure
- Z=3, 4, 5:
  - (Electronic) isotope shifts have been measured very accurately.  
⇒ (squared) charge radius **differences** are very well known.
  - Muonic Lamb shifts provide **absolute** charge radii.
  - Test of few-electron (QED) calculations.
  - *Ab initio* nuclear structure calculations.
- Also: 1S-2S in (electronic) tritium. “Missing link” at A=3

Lamb shift: absolute charge radius

nuclear polarizability

2S-HFS: Zemach / magnetic radius

nuclear polarizability

# Summary

- Muonic hydrogen gives:
  - Proton charge radius:  $r_p = 0.84087(39)$  fm
  - Proton Zemach radius:  $R_Z = 1.082(37)$  fm
  - Rydberg constant:  

$$R_\infty = 3.289\,841\,960\,249\,5 (10)^{\text{radius}} (25)^{\text{QED}} \times 10^{15} \text{ Hz/c}$$
  - Deuteron charge radius:  $r_d = 2.12771(22)$  fm from  $\mu\text{H} + \text{H/D}(1\text{S}-2\text{S})$
  - The “Proton radius puzzle”
- muonic deuterium:  $r_d = 2.1289(12)$  fm from  $\mu\text{D}$  (PRELIMINARY!)
 

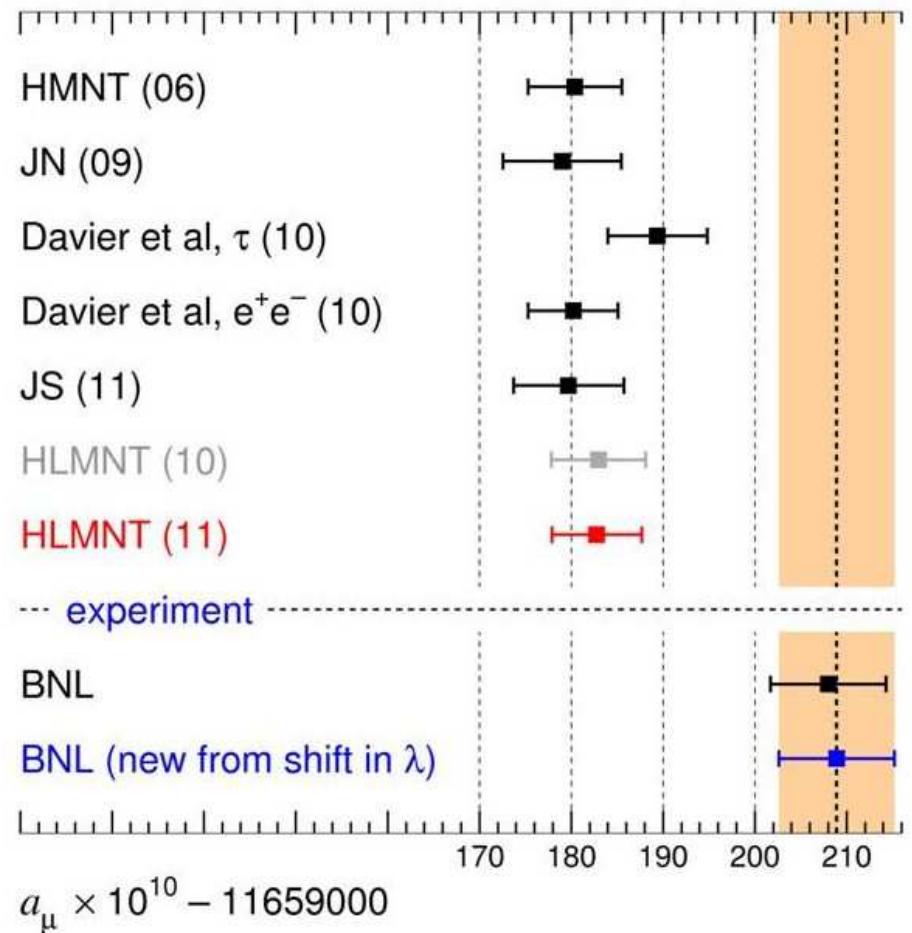
Lamb shift in  $\mu\text{D}$  is ok.  
2S-HFS is missing a large (polarizability) term!
- Proton radius puzzle persists. New data needed!
  - muonic helium
  - hydrogen
  - ...

# Two muon puzzles

- **Anomalous magnetic moment** of the muon

The measured value of  $a_\mu = (g - 2)/2$  of the muon has been in disagreement with the SM predictions for >10 years now!

The discrepancy stands at  $\sim 3.6\sigma$



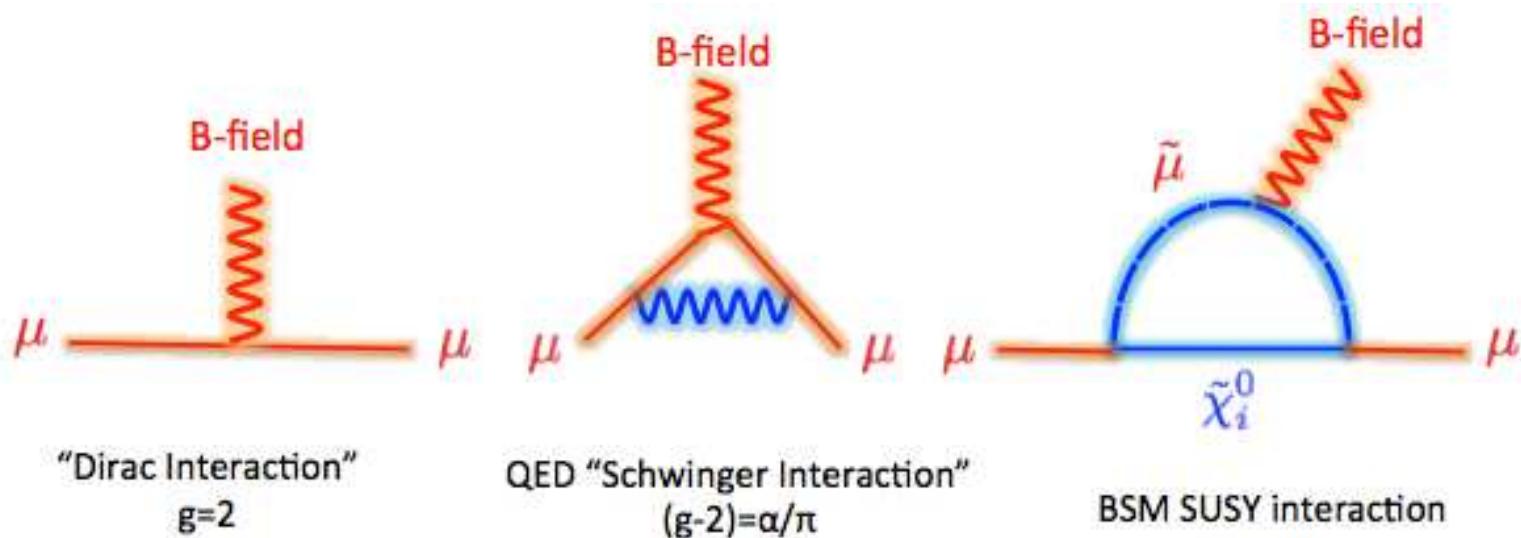
J. Phys. G 38, 085003 (2011)

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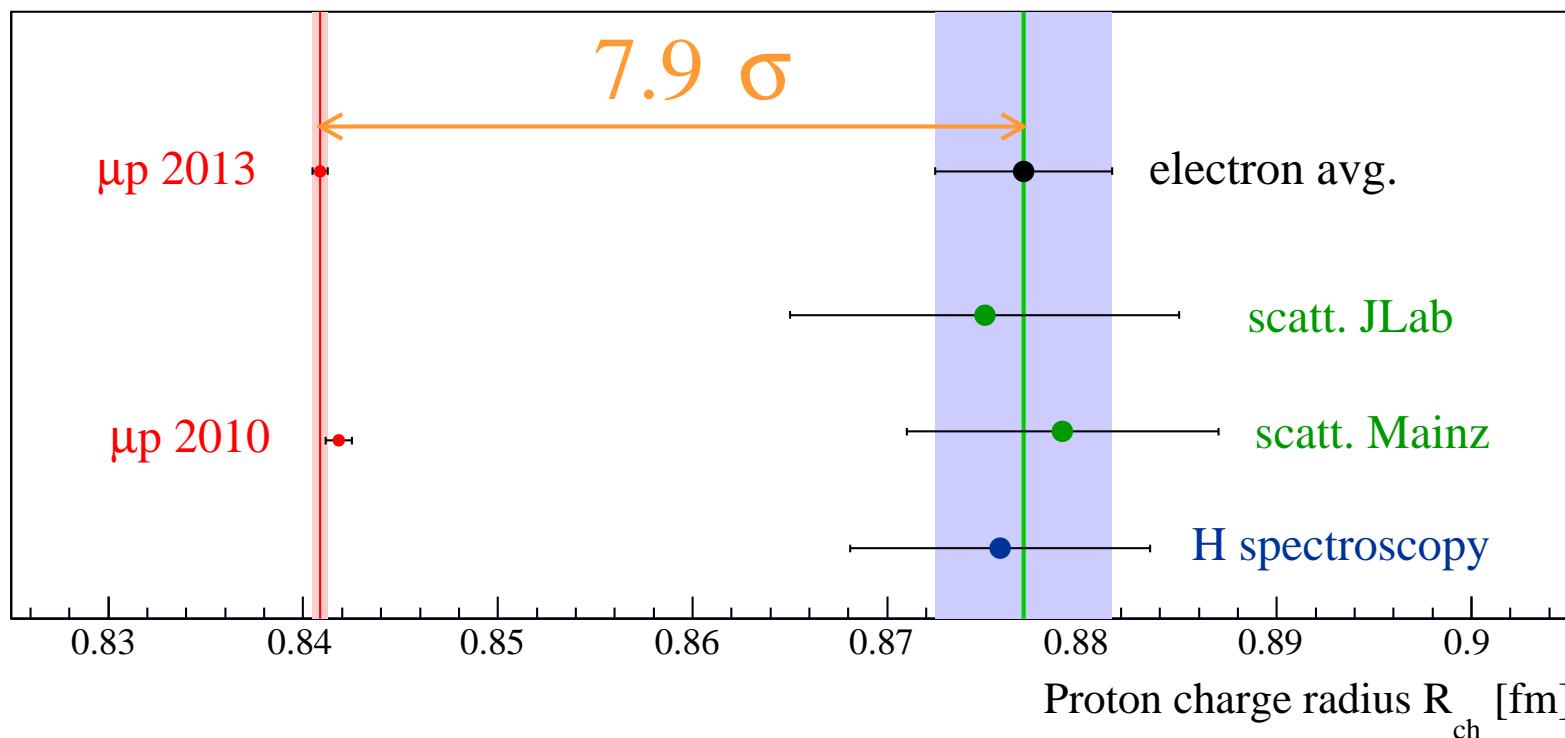


<http://www.hep.ucl.ac.uk/muons/g-2/>

# Two muon puzzles

- Anomalous magnetic moment of the muon  $\sim 3.6\sigma$
- Proton radius from muonic hydrogen

The measured value of the proton rms charge radius from muonic hydrogen  $\mu p$  is 10 times more accurate, but 4% smaller than the value from both **hydrogen spectroscopy** and **elastic electron proton scattering**.



RP et al., Nature 466, 213 (2010); Science 339, 417 (2013); ARNPS 63, 175 (2013).

# Two muon puzzles

- Anomalous magnetic moment of the muon  $\sim 3.6\sigma$
- Proton radius from muonic hydrogen  $\sim 7.9\sigma$
- These 2 discrepancies may be **connected**.

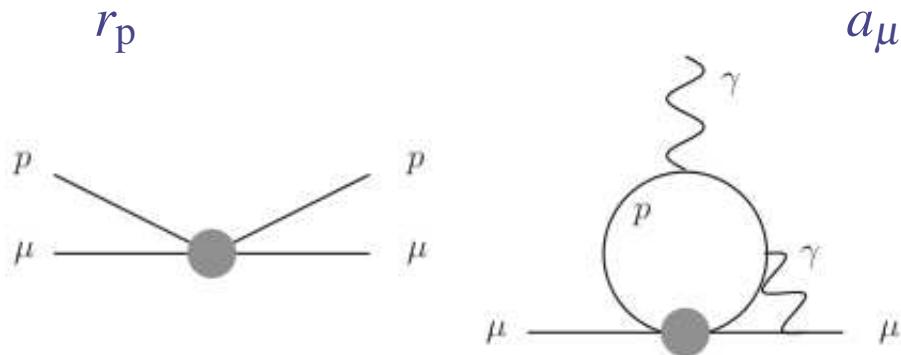
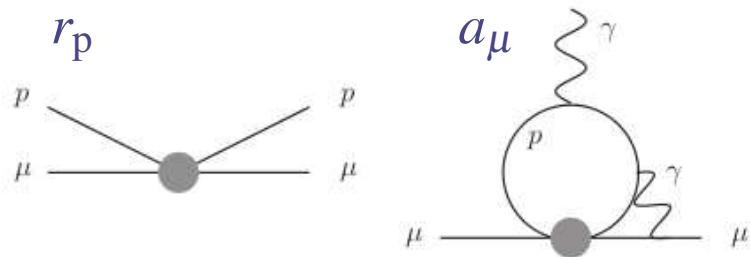


FIG. 1. Left:the effective proton-muon interaction resulting from unexpectedly large QCD effects or new physics that is responsible for the  $r_p$  discrepancy. Right: the two-loop contribution to the muon  $g - 2$  that results from the interaction on the left after integrating out the proton.

Karshenboim, McKeen, Pospelov, arXiv 1401.6156

# $r_p$ and $a_\mu$

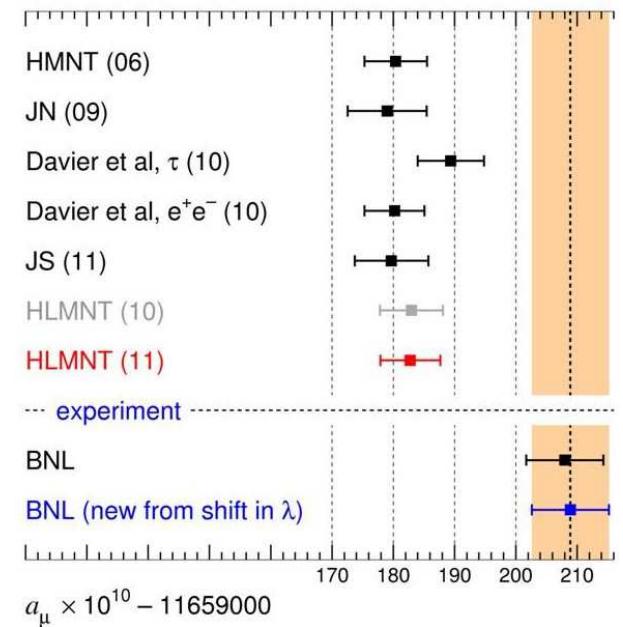
Both the  $r_p$  and the  $a_\mu$  discrepancy could originate from the same new proton structure effect (two-photon-exchange) or “New light Physics” ( $m \approx \text{MeV}$ )



Fixing  $r_p$  could give rise to

$$5 \times 10^{-9} < |\Delta(a_\mu)| < 10^{-7} \quad (\text{for } \Lambda_{\text{had}} = m_\pi \dots p_p).$$

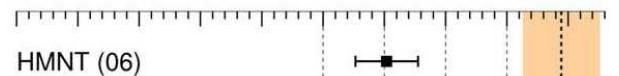
This is much larger than the  $(g-2)_\mu$  discrepancy of  $\sim 1 \times 10^{-9}$ .



J. Phys. G 38, 085003 (2011).

# $r_p$ and $a_\mu$

Both the  $r_p$  and the  $a_\mu$  discrepancy could originate from the same (fermion loop exchange) effect.



Fixing  $r_p$  could

$$5 \times 10^{-9} <$$

This is much

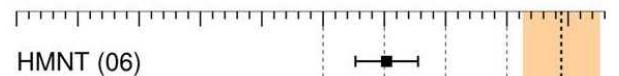


June 22 – July 25, 2013

after Pospelov  
Karshenboim, McKeen, Pospelov, arXiv 1401.6156

# $r_p$ and $a_\mu$

Both the  $r_p$  and the  $a_\mu$  discrepancy could originate

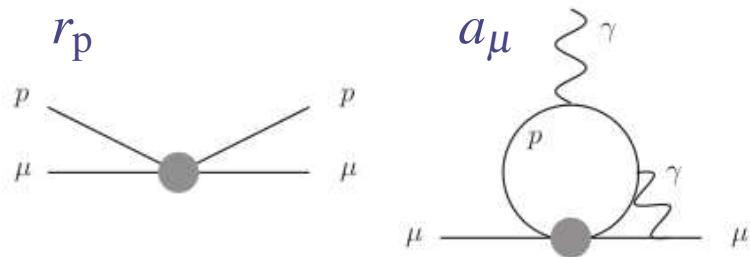


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Karshenboim, McKeen, Pospelov, arXiv 1401.6156

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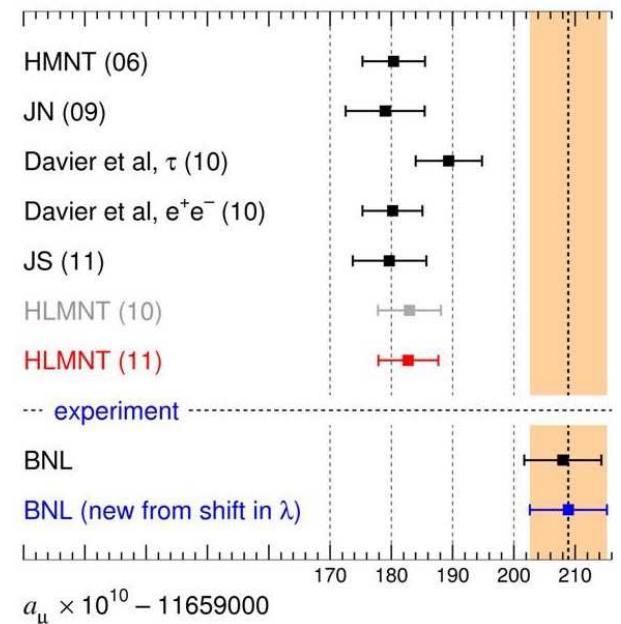
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This is **much larger** than the  $(g-2)_\mu$  discrepancy of  $\sim 1 \times 10^{-9}$ .



J. Phys. G 38, 085003 (2011).

Maybe one can invert the argument:

$a_\mu$  “not so wrong”  $\implies r_p$  is not due to proton TPE or this kind of BSM

after Pospelov  
Karshenboim, McKeen, Pospelov, arXiv 1401.6156



Proton Size Investigators thank you for your attention



# CREMA collaboration in 2009



## Charge Radius Experiment with Muonic Atoms

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