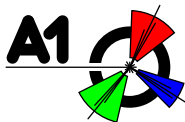


OLYMPUS and fits

Jan C. Bernauer

MITP Proton Radius Workshop, June 2014



Massachusetts Institute of Technology

- TPE: Motivation
- Status of OLYMPUS
- Mainz fits
- TPE results from VEPP-3, (JLab)

Cross section and form factors for elastic e-p scattering

The cross section:

$$\frac{\left(\frac{d\sigma}{d\Omega}\right)}{\left(\frac{d\sigma}{d\Omega}\right)_{Mott}} = \frac{1}{\varepsilon(1+\tau)} \left[\varepsilon G_E^2(Q^2) + \tau G_M^2(Q^2) \right]$$

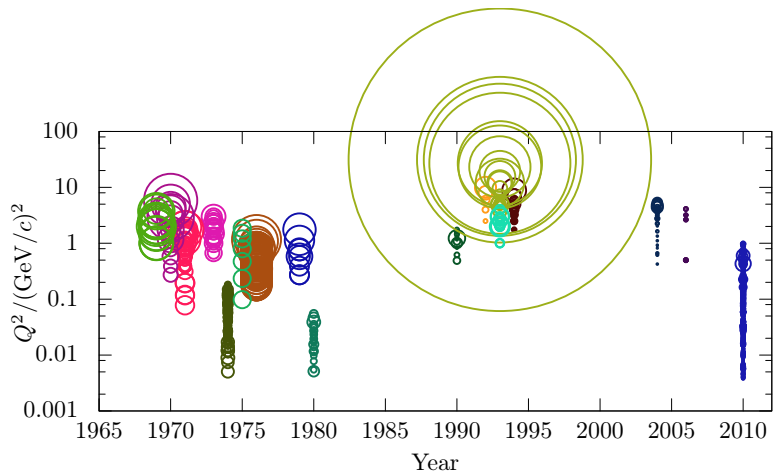
with:

$$\tau = \frac{Q^2}{4m_p^2}, \quad \varepsilon = \left(1 + 2(1+\tau) \tan^2 \frac{\theta_e}{2} \right)^{-1}$$

Fourier-transform of $G_E, G_M \longrightarrow$ spatial distribution (Breit frame)

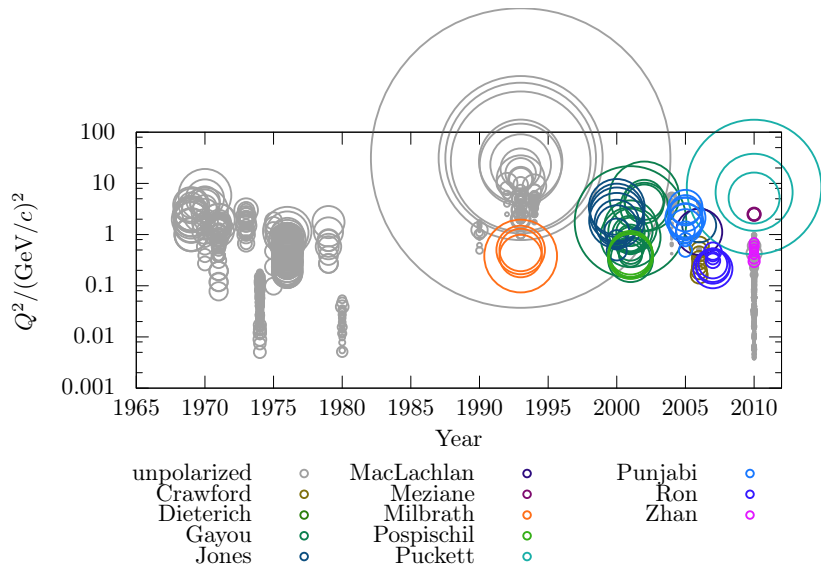
$$\langle r_E^2 \rangle = -6\hbar^2 \left. \frac{dG_E}{dQ^2} \right|_{Q^2=0} \quad \langle r_M^2 \rangle = -6\hbar^2 \left. \frac{d(G_M/\mu_p)}{dQ^2} \right|_{Q^2=0}$$

Unpolarized: Rosenbluth

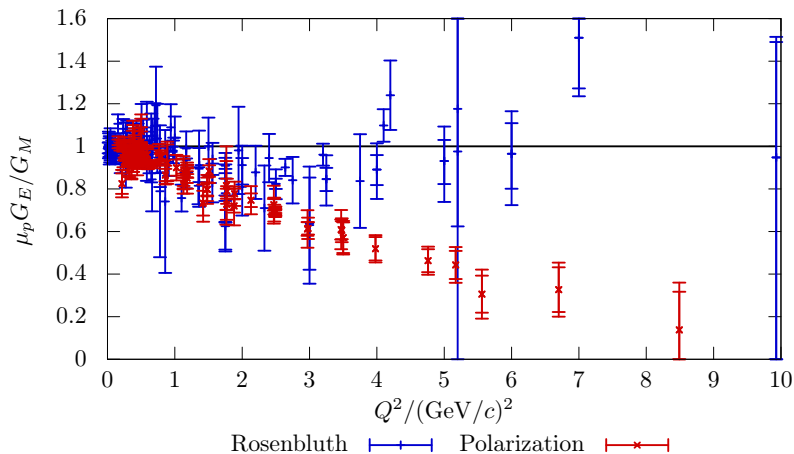


- | | | | | |
|-------------|-------------|------------|---------|----------|
| ○ Andivahis | ○ Borkowski | ○ Janssens | ○ Rock | ○ Walker |
| ○ Bartel | ○ Bosted | ○ Litt | ○ Sill | |
| ○ Berger | ○ Christy | ○ Price | ○ Simon | |
| ○ Bernauer | ○ Goitein | ○ Qattan | ○ Stein | |

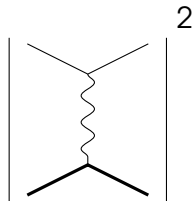
Polarized: Ratio



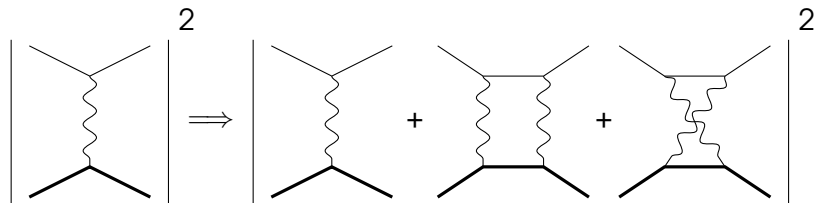
Ratio: Difference!



Most likely solution: Two Photon Exchange



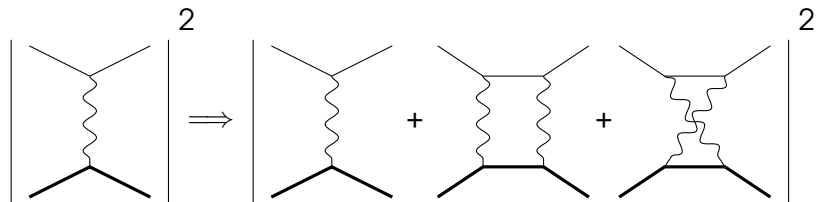
Most likely solution: Two Photon Exchange



Two-Photon-Exchange

- Not in standard radiative corrections
- Off-shell proton!
- How to handle high momenta in loop?

Most likely solution: Two Photon Exchange



Two-Photon-Exchange

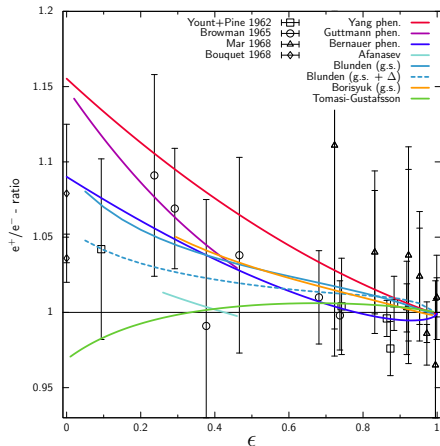
- Not in standard radiative corrections
- Off-shell proton!
- How to handle high momenta in loop?

Measurement

- Rosenbluth/polarized reconciled?
- How to treat the hadron line?

Measure Two Photon Exchange

- Interference term changes sign with lepton sign!
- Measured in the 1960s
- Not much data
- A lot of predictions!



Three modern experiments

CLAS

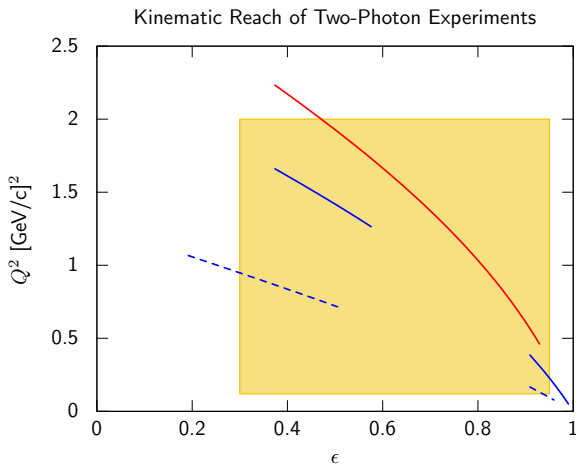
- e^- to γ to $e^{+/-}$
-beam

VEPP-3

- 1.6/1 GeV beam
- no field
- preliminary results

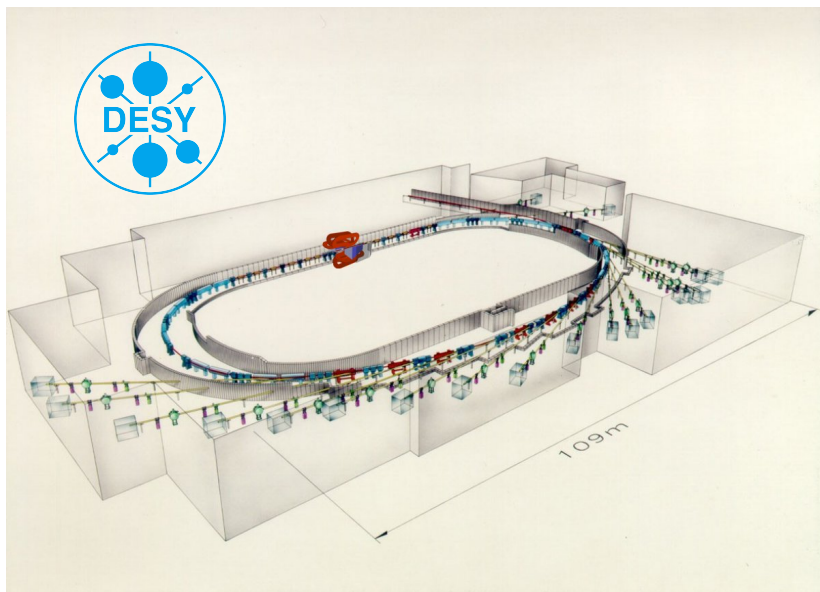
~~OLYMPUS~~

- DORIS @ DESY
- 2 GeV beam
- data taking finished
01/2013
- no results yet :(

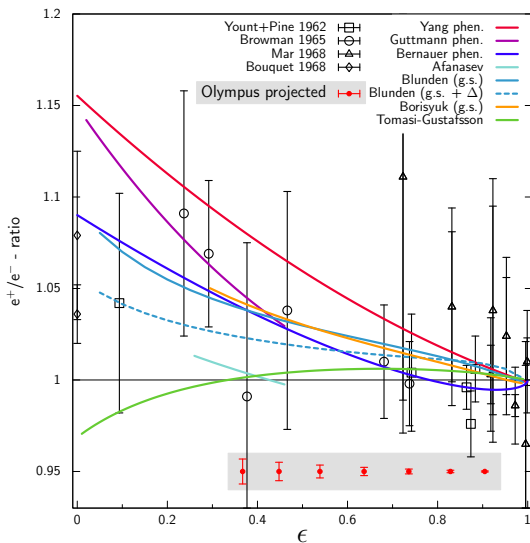


The OLYMPUS collaboration

- Arizona State University, USA
- DESY, Hamburg, Germany
- Hampton University, USA
- INFN, Bari, Italy
- INFN, Ferrara, Italy
- INFN, Rome, Italy
- MIT Laboratory for Nuclear Science, Cambridge, USA
- Petersburg Nuclear Physics Institute, Gatchina, Russia
- University of Bonn, Bonn, Germany
- University of Glasgow, United Kingdom
- University of Mainz, Mainz, Germany
- University of New Hampshire, USA
- Yerevan Physics Institute, Armenia

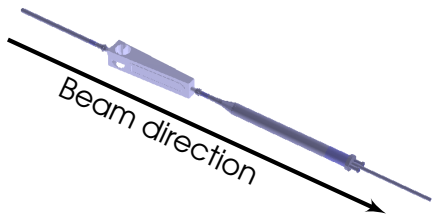


Projected performance

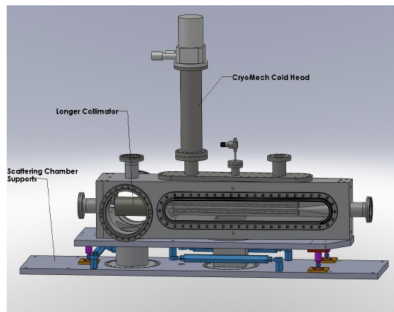


2 GeV beam, Q^2 -range: 0.6 to 2.2 GeV^2

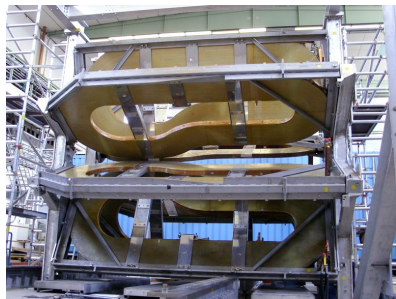
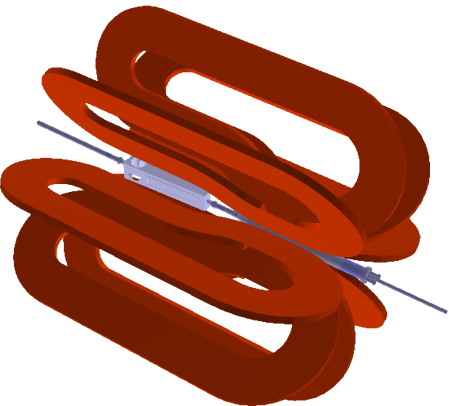
Target / Vacuum



- Open cell design
- Cryogenic
- Target density: $3 \cdot 10^{15} \text{ cm}^{-2}$
- Multi-stage pump system

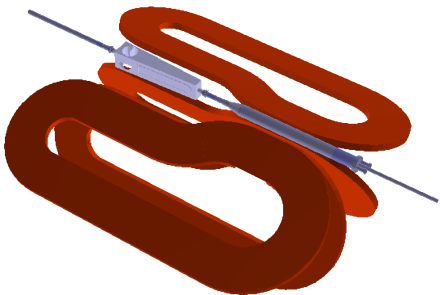


Toroid



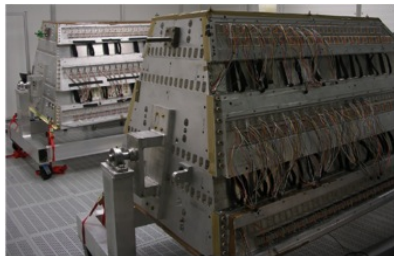
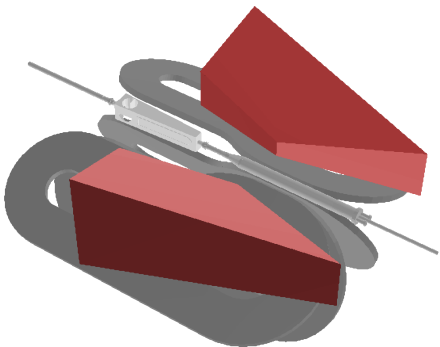
- From BLAST
- ± 5000 A = 75% of BLAST
- \Rightarrow Peak field: 2.8 kG
- 8 coils

Toroid



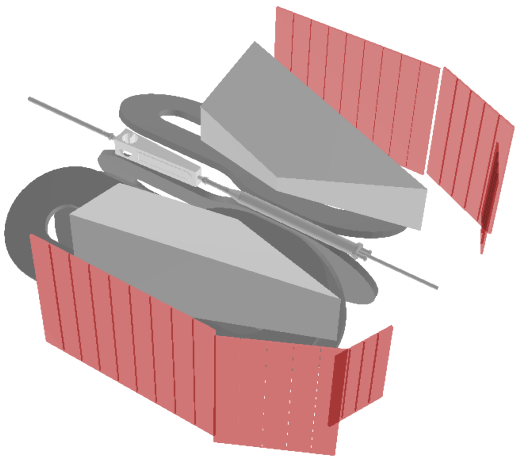
- From BLAST
- ± 5000 A = 75% of BLAST
- \Rightarrow Peak field: 2.8 kG
- 8 coils
- 4 shown

Wire chamber



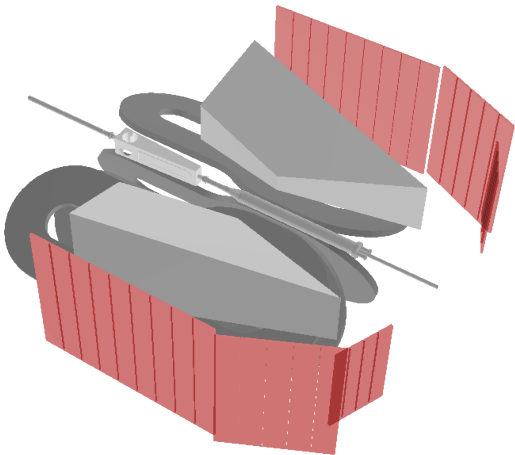
- From BLAST
- HDC design, 3 signal wires
- completely rewired
- 2 · 3 planes / chamber, 3 chambers / side
- 10° stereo angle

Time Of Flight

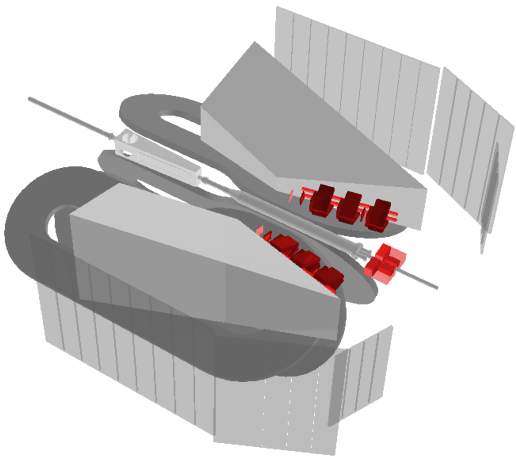


- From BLAST
- Rewrapped, tested
- Trigger
 - Top/bottom coinc.
 - kinematically constrained

Time Of Flight



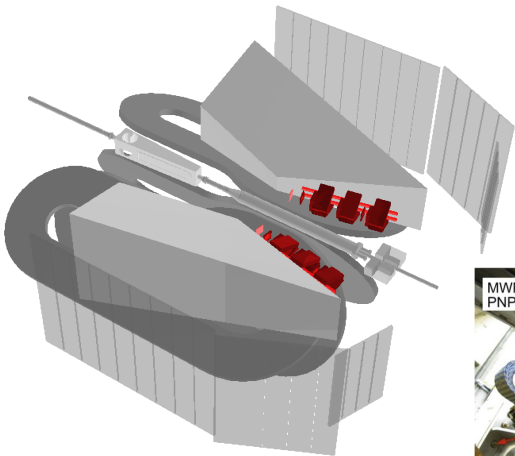
- From BLAST
- Rewrapped, tested
- Trigger
 - Top/bottom coinc.
 - kinematically constrained
 - + 2nd level WC



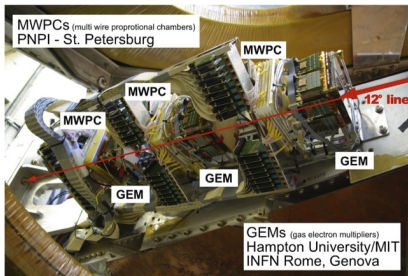
Tight control crucial!
Redundant systems:

- 12°-detector
- Symmetric
Møller/Bhabha

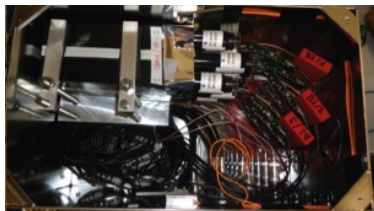
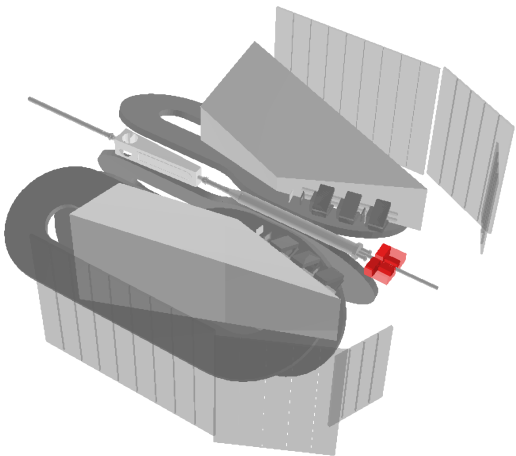
12°-detector



- 3 GEM (Hampton) + 3 MWPC (PNPI) each
- highly redundant
- SiPM trigger scintillators



Symmetric Møller/Bhabha



- 2×9 crystals (Mainz)
- 1.2° symmetric angle
- high rate, no deadtime

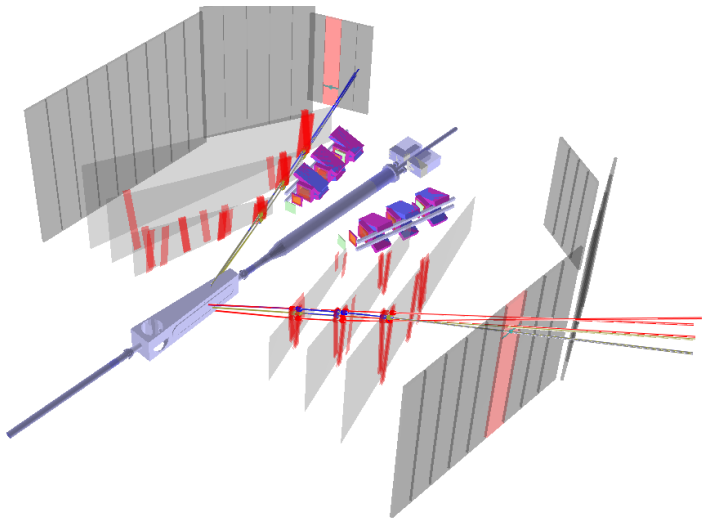


Timeline

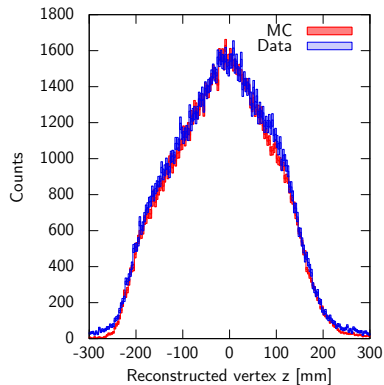
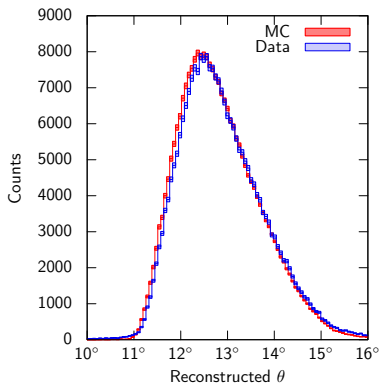
OLYMPUS full proposal	September 2008
Experiment funded by DOE	January 2010
BLAST moved to Germany	Spring 2010
Target test experiment	February 2011
Drift chambers installed	Spring 2011
Luminosity monitors installed	Summer 2011
Olympus roll-in	July 2011
First full Olympus test	August 2011
Sym. Møller/Bhabha installed	Fall 2011
First data run	January 2012
Second data run	October-December 2012
DORIS shut down	January 2013

CAVEAT: The analysis is ongoing. All plots are preliminary.

Wire chamber / Event-Display

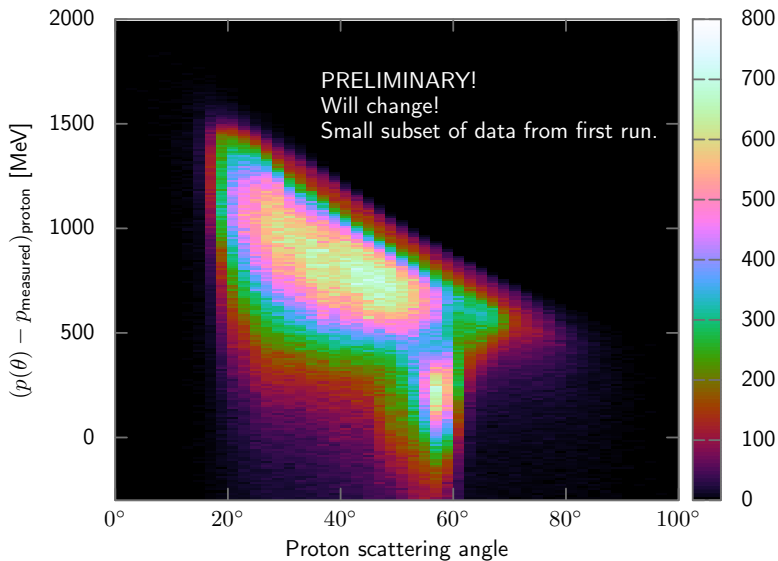


Luminosity: Comparison Data/MC

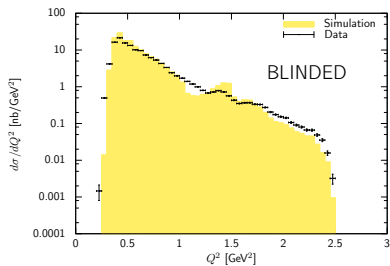


Analysis: Brian Henderson

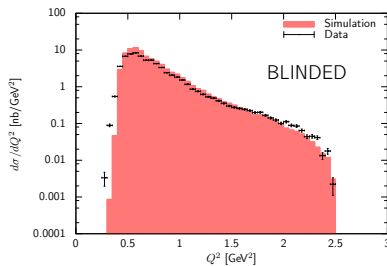
Reconstructed proton momentum



Positrons



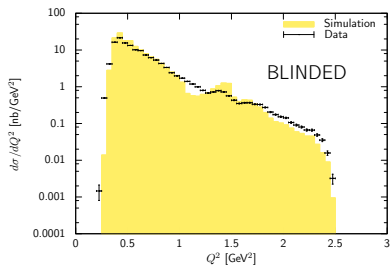
Electrons



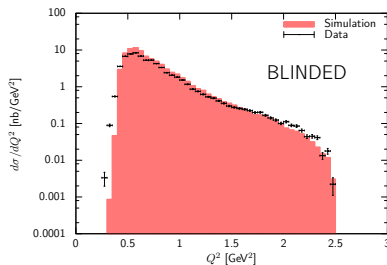
Analysis: Axel Schmidt

Preliminary Analysis

Positrons



Electrons



Analysis: Axel Schmidt

Expect results end of 2014

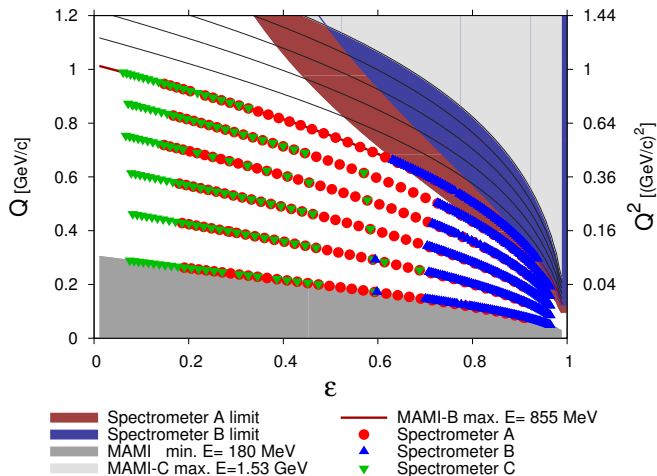
Form factor fits

High-precision $p(e,e')p$ measurement at MAMI

Three spectrometer facility of the A1 collaboration:

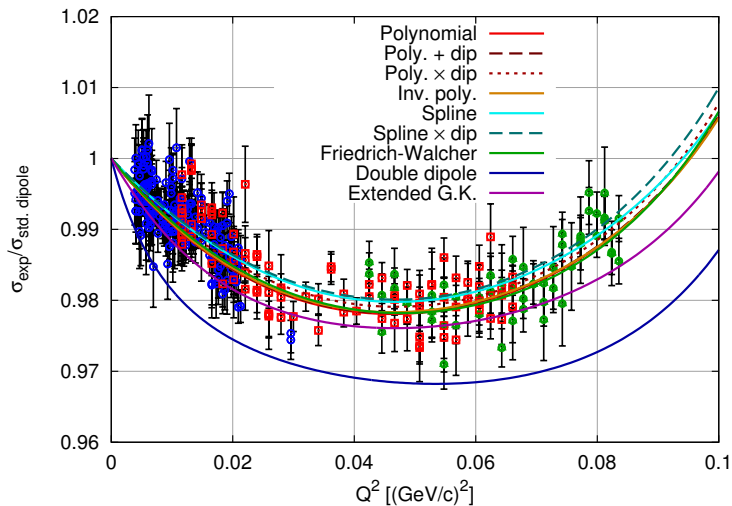


Measured settings



1400 settings

Cross sections: 180 MeV



Inclusion of world data

- Extend data base with world data
⇒ Cross check, extend Q^2 reach

Inclusion of world data

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- Take **cross sections** from Rosenbluth exp's
- Sidestep unknown error correlation
 - Update / standardize radiative corrections
 - One normalization parameter per source (Andivahis: 2)

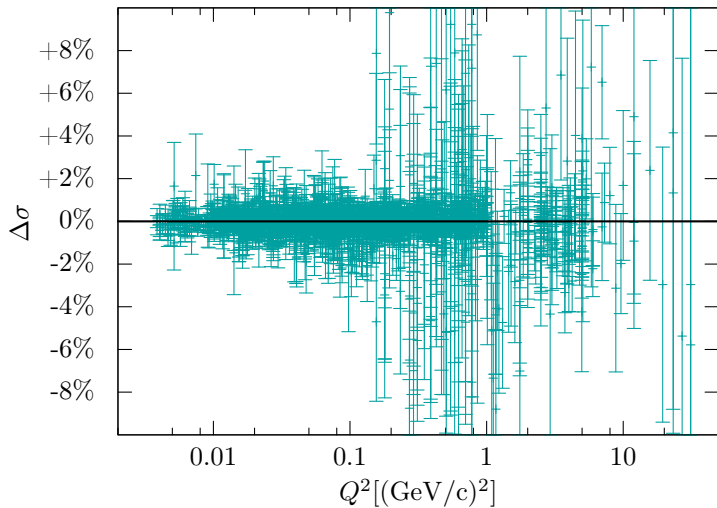
L. Andivahis *et al.*,
Phys. Rev. D50, 5491 (1994).
F. Borkowski *et al.*,
Nucl. Phys. B93, 461 (1975).
F. Borkowski *et al.*,
Nucl. Phys. A222, 269 (1974).
P. E. Bosted *et al.*,
Phys. Rev. C 42, 38 (1990).
M. E. Christy *et al.*,
Phys. Rev. C70, 015206 (2004).
M. Goitein *et al.*,
Phys. Rev. D 1, 2449 (1970).
T. Janssens *et al.*,
Phys. Rev. 142, 922 (1966).
J. Litt *et al.*,
Phys. Lett. B31, 40 (1970).
L. E. Price *et al.*,
Phys. Rev. D4, 45 (1971).
I. A. Qattan *et al.*,
Phys. Rev. Lett. 94, 142301 (2005).
S. Rock *et al.*,
Phys. Rev. D 46, 24 (1992).
A. F. Sill *et al.*,
Phys. Rev. D 48, 29 (1993).
G. G. Simon *et al.*,
Nucl. Phys. A 333, 381 (1980).
S. Stein *et al.*,
Phys. Rev. D 12, 1884 (1975).
R. C. Walker *et al.*,
Phys. Rev. D 49, 5671 (1994).

Inclusion of world data

- Extend data base with world data
⇒ Cross check, extend Q^2 reach
- Take **cross sections** from Rosenbluth exp's
- Sidestep unknown error correlation
 - Update / standardize radiative corrections
 - One normalization parameter per source (Andivahis: 2)
- Two models:
 - Splines with **variable** knot spacing
⇒ Adapt knot density to data density
 - Padé-Expansion
⇒ Low(er) flexibility, for comparison

L. Andivahis *et al.*,
Phys. Rev. D50, 5491 (1994).
F. Borkowski *et al.*,
Nucl. Phys. B93, 461 (1975).
F. Borkowski *et al.*,
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Nucl. Phys. A 333, 381 (1980).
S. Stein *et al.*,
Phys. Rev. D 12, 1884 (1975).
R. C. Walker *et al.*,
Phys. Rev. D 49, 5671 (1994).

It works!

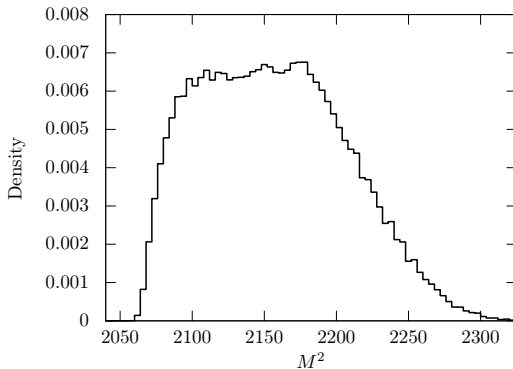


Model dependence

- Spline model has variable knot spacing

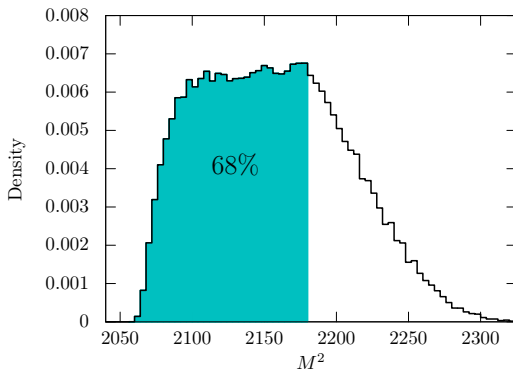
Model dependence

- Spline model has variable knot spacing
- Vary knots, refit, record χ^2 .



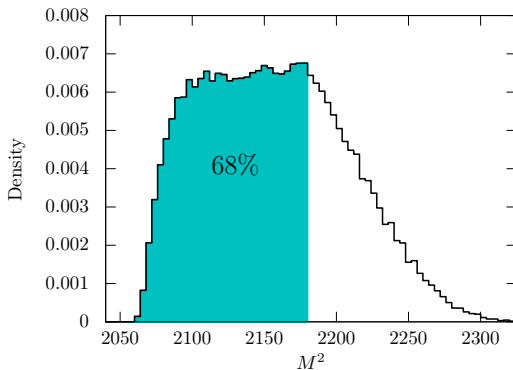
Model dependence

- Spline model has variable knot spacing
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- Select the 68% best tries.



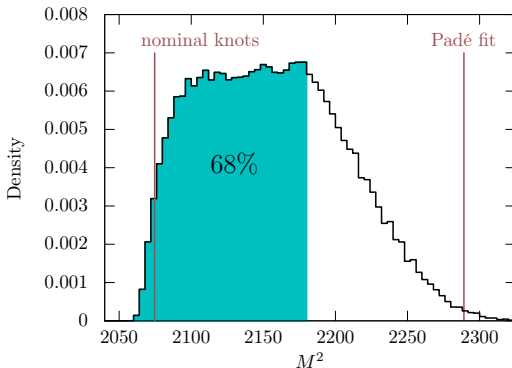
Model dependence

- Spline model has variable knot spacing
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- Select the 68% best tries.
- Construct envelope of models.



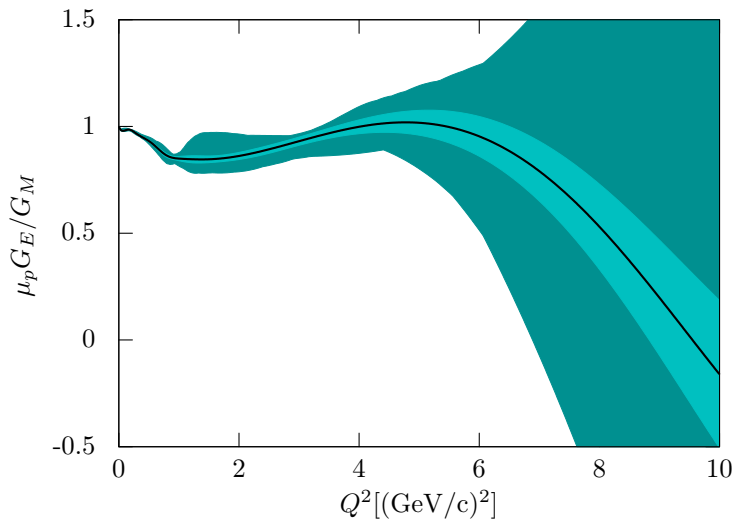
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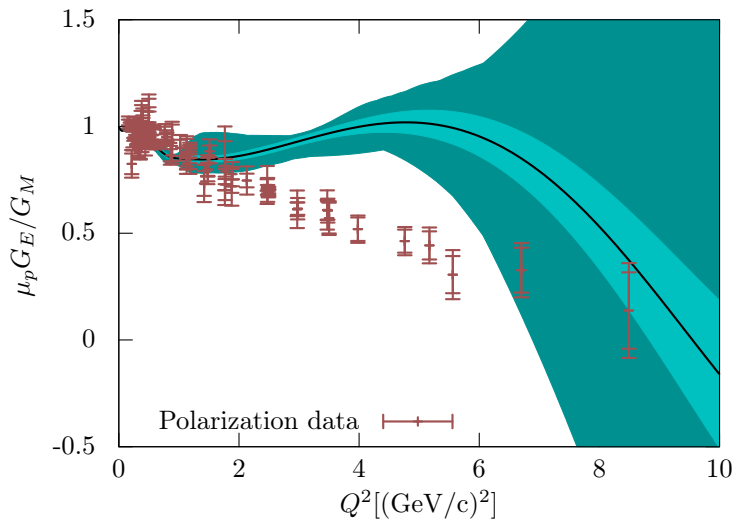


Band will cover at least 68% of all model variations!

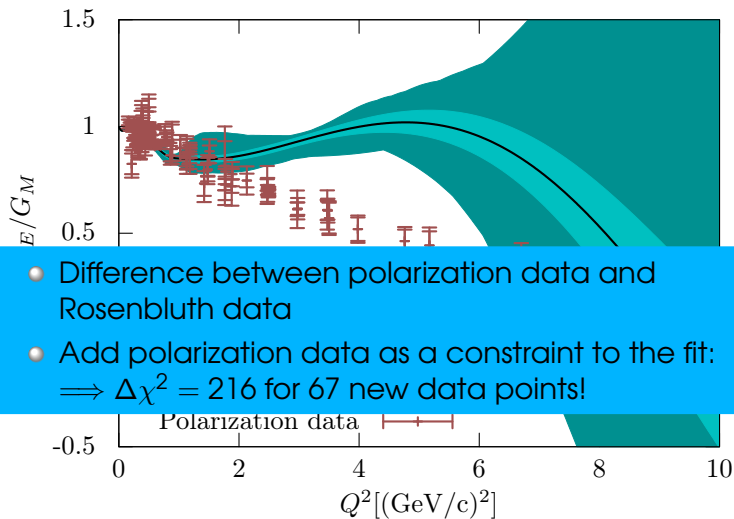
Form factor ratio G_E/G_M



Form factor ratio G_E/G_M



Form factor ratio G_E/G_M



- Difference between polarization data and Rosenbluth data
- Add polarization data as a constraint to the fit:
 $\Rightarrow \Delta\chi^2 = 216$ for 67 new data points!

Two Photon Exchange - A parametrization

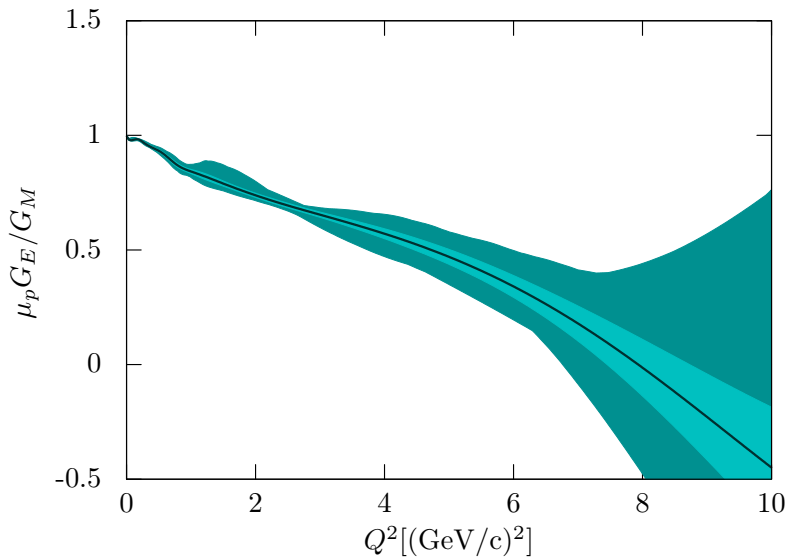
- Available data are sparse
- Mostly Q^2 dependence
- Few data on ε dependence

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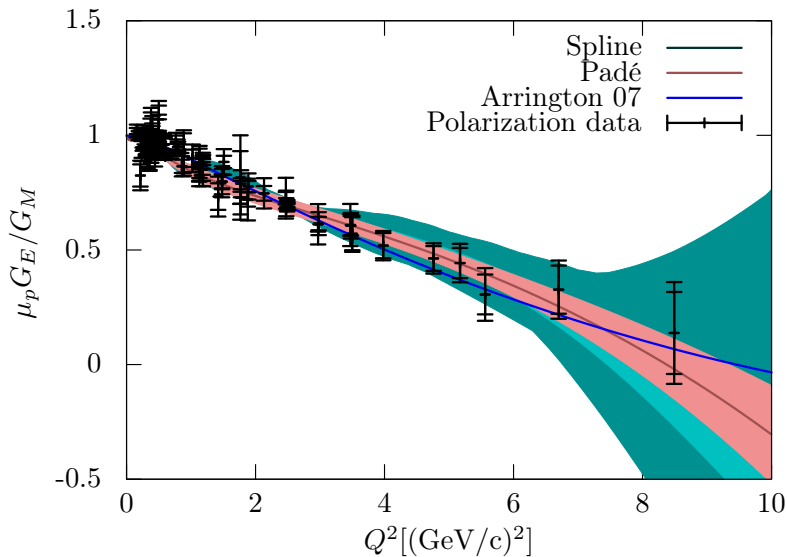
- Available data are sparse
- Mostly Q^2 dependence
- Few data on ε dependence
- Only possible to fit simple model
- In addition to Feshbach Coulomb-correction!

$$\delta = a \cdot (1 - \varepsilon) \cdot \log(1 + b \cdot Q^2)$$

G_E/G_M fit incl. polarized data



G_E/G_M fit incl. polarized data



How does this all affect the radius?

Final result from flexible models

$$r_E = 0.879 \pm 0.005_{\text{stat.}} \pm 0.004_{\text{syst.}} \pm 0.002_{\text{model}} \pm 0.004_{\text{group}} \text{ fm,}$$

$$r_M = 0.777 \pm 0.013_{\text{stat.}} \pm 0.009_{\text{syst.}} \pm 0.005_{\text{model}} \pm 0.002_{\text{group}} \text{ fm.}$$

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More fits

	r_E (fm)	r_M (fm)
spline-type fits	0.875(5)(4)(2)	0.775(12)(9)(4)
polynomial-type fits	0.883(5)(5)(3)	0.778(15)(10)(6)

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With other TPE calculations:

D. Borisyuk et al.	0.876(5)(4)(2)(5)	0.803(13)(9)(5)(3)
Blunden et al.	0.875(5)(4)(2)(5)	0.799(13)(9)(5)(3)

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var. spline + world cs.	0.878	0.772
" " + polarization	0.878	0.769

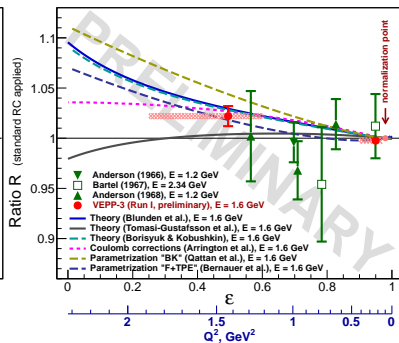
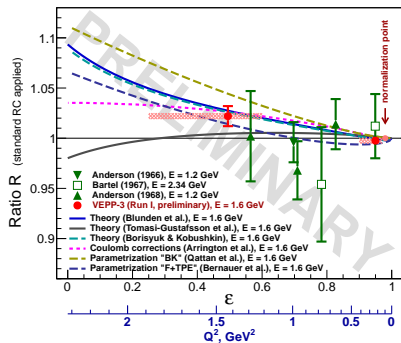
With other TPE calculations:

D. Borisyuk et al.	0.876(5)(4)(2)(5)	0.803(13)(9)(5)(3)
Blunden et al.	0.875(5)(4)(2)(5)	0.799(13)(9)(5)(3)
" " + world (Bad χ^2)	0.875	0.787

Comparison with TPE experiments

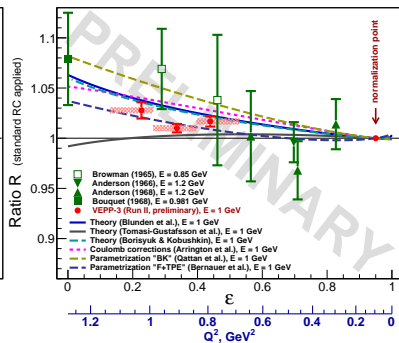
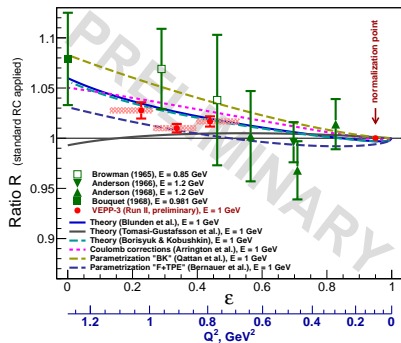
Both VEPP-3 and JLab have preliminary results - let's see.

VEPP-3 result: Run I



Plots by Alexander Gramolin

VEPP-3 result: Run II



Plots by Alexander Gramolin

The take-away

- TPE prime candidate to resolve form factor discrepancy at high Q^2
- Preliminary results from VEPP-3 and JLab + Mainz fit indicate effect is of right magnitude.
- OLYMPUS progresses nicely.
- TPE has so far small effect on extracted charge radius.
- Bigger on magnetic radius!

Model dependence: Charge Radius

Input		Analysis							
		Dipole	Dbl-D.	Poly.	P.+D.	P. \times D.	Spline	S. \times D.	F./W.
Std. dipole	811	0 \pm 1	0 \pm 1	0 \pm 3	0 \pm 3	0 \pm 4	0 \pm 5	0 \pm 7	0 \pm 1
Arrington 07	878	-18 \pm 1	3 \pm 3	-3 \pm 3	-2 \pm 3	-1 \pm 4	-4 \pm 5	-1 \pm 6	-2 \pm 3
Arr. 03 (P)	829	29 \pm 1	10 \pm 1	1 \pm 3	1 \pm 3	0 \pm 4	-1 \pm 5	0 \pm 6	2 \pm 6
Arr. 03 (R)	868	-9 \pm 1	0 \pm 2	0 \pm 3	0 \pm 3	0 \pm 4	-3 \pm 5	0 \pm 6	-1 \pm 3
FW	860	-4 \pm 1	31 \pm 14	-1 \pm 3	-1 \pm 3	1 \pm 4	0 \pm 5	0 \pm 6	0 \pm 3

Arrington 07: Phys. Rev. C 76 035205 (2007)

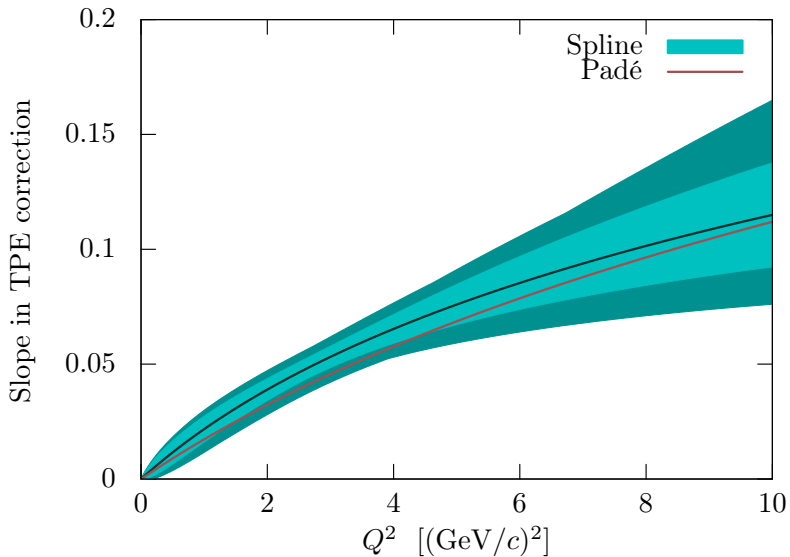
Arr. 03: Phys. Rev. C 68 034325 (2003)

FW: Eur. Phys. J. A 17 607 (2003)

Model dependence: Magnetic Radius

Input		Analysis							
		Dipole	Dbl-D.	Poly.	P.+D.	P. \times D.	Spline	S. \times D.	F./W.
Std. dipole	811	0 \pm 1	0 \pm 1	-1 \pm 7	0 \pm 7	0 \pm 10	2 \pm 14	1 \pm 18	0 \pm 1
Arrington 07	858	-55 \pm 1	4 \pm 4	-5 \pm 6	-4 \pm 6	-1 \pm 9	2 \pm 13	0 \pm 17	-10 \pm 4
Arr. 03 (P)	837	-33 \pm 1	12 \pm 3	-1 \pm 7	0 \pm 7	0 \pm 9	2 \pm 13	0 \pm 19	-5 \pm 5
Arr. 03 (R)	863	-52 \pm 1	2 \pm 4	-4 \pm 6	-3 \pm 6	0 \pm 9	3 \pm 13	0 \pm 17	-8 \pm 4
FW	805	4 \pm 1	49 \pm 2	0 \pm 7	1 \pm 7	-1 \pm 10	1 \pm 13	-1 \pm 18	-1 \pm 4

TPE dependence on Q^2



TPE dependence on ε

