

Transition form factors of π^0 and η mesons (experiments)

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MITP "g-2" workshop, April 4th, 2014

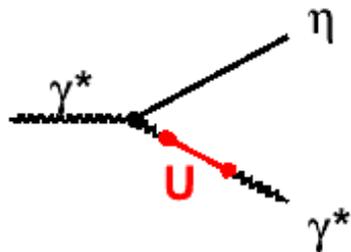
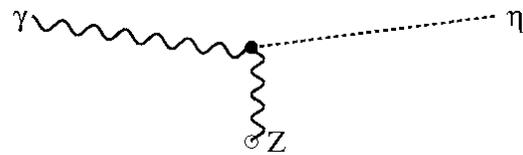
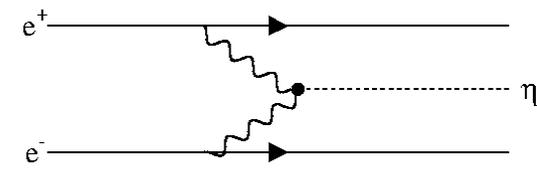
Pseudoscalar Transition Form Factors (TFF)

Structure of light mesons

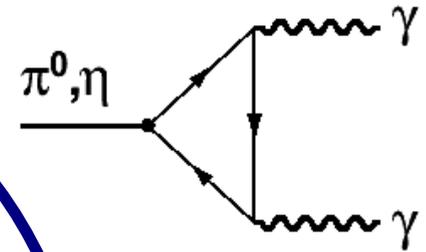
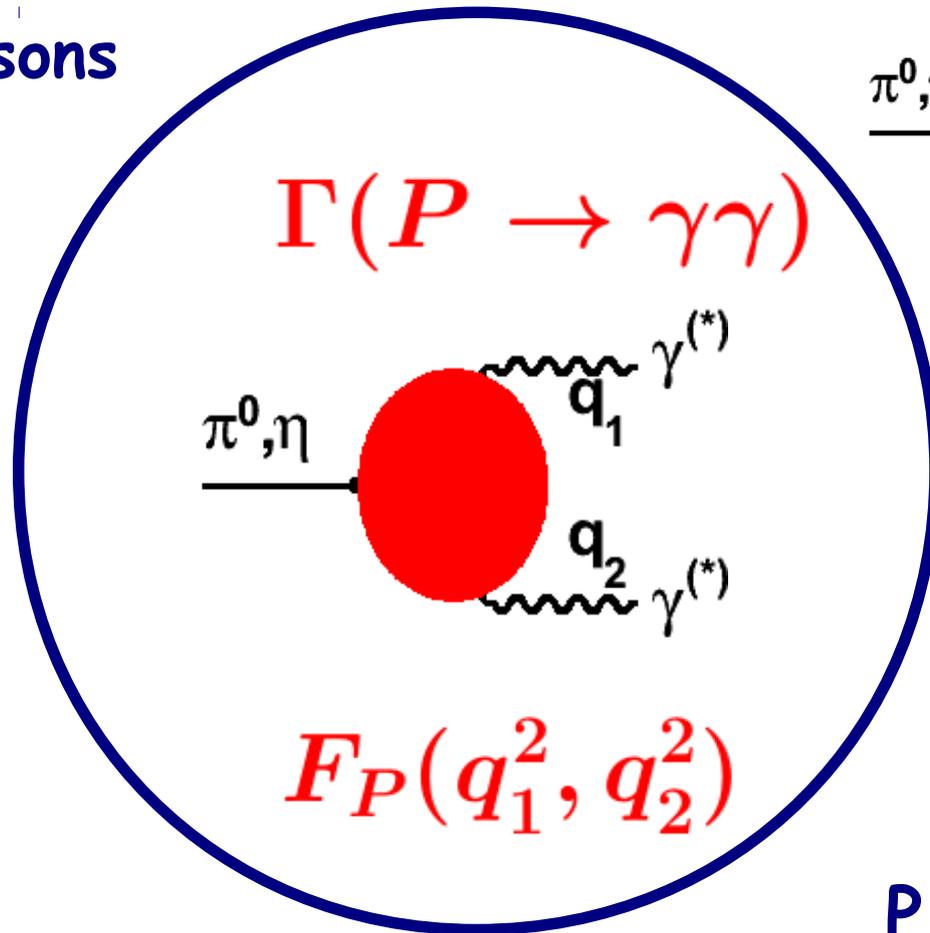
L/H energy QDC LAB

l^+l^- spectra in HIon

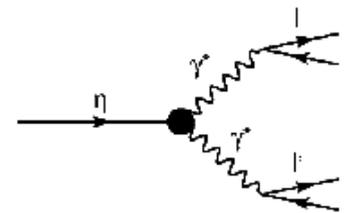
$F_{\pi^0} q^2 \rightarrow \infty$ puzzle



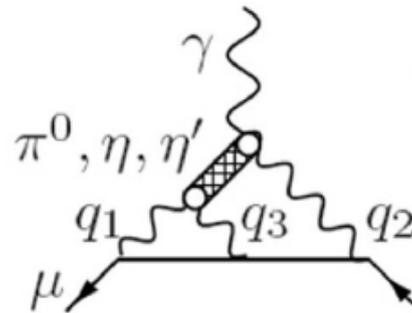
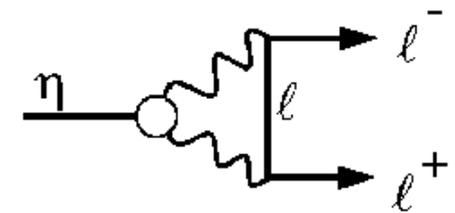
Dark photon



$\eta: \Gamma_{\gamma\gamma}$
 m_u/m_d



$P \rightarrow l^+l^-$



$g-2$ HLbL

Radiative widths of η, π^0

η, π^0 : narrow and short lived

$$\Rightarrow \Gamma_{\text{tot}} = \Gamma_{\gamma\gamma} / \text{BR}_{\gamma\gamma}$$

$$\eta: 5 \times 10^{-19} \text{ s}; \Gamma = 1.3 \text{ keV} \quad \eta \rightarrow \gamma\gamma$$

$$\pi^0: 8 \times 10^{-17} \text{ s}; c\tau = 25 \text{ nm} \quad \pi^0 \rightarrow \gamma\gamma$$

Two exp. techniques:

$\gamma Z \rightarrow \eta, \pi^0$ Primakoff

$$\delta\Gamma(\pi^0 \rightarrow \gamma\gamma) \sim 2.8\%$$

PrimEx PRL 106,162303(2011)

$e^+e^-: \gamma\gamma \rightarrow \eta, \pi^0$

KLOE-2 Taggers

$$5\text{fb}^{-1} \Rightarrow \delta\Gamma(\pi^0 \rightarrow \gamma\gamma) \sim 1\%$$

Details: [EPJC 72, 1917 (2012)]

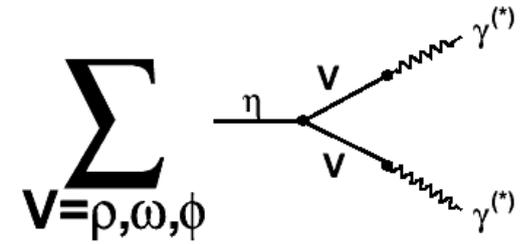
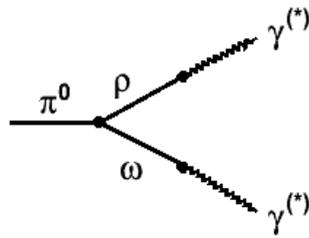
VALUE (keV)	EVTS	DOCUMENT ID	TECN	COMMENT
0.510 ± 0.026	OUR FIT	$\delta\Gamma(\eta \rightarrow \gamma\gamma) \sim 5\%$		
0.510 ± 0.026	OUR AVERAGE			
0.51 ± 0.12 ± 0.05	36	BARU	90 MD1	$e^+e^- \rightarrow e^+e^-\eta$
0.490 ± 0.010 ± 0.048	2287	ROE	90 ASP	$e^+e^- \rightarrow e^+e^-\eta$
0.514 ± 0.017 ± 0.035	1295	WILLIAMS	88 CBAL	$e^+e^- \rightarrow e^+e^-\eta$
0.53 ± 0.04 ± 0.04		BARTEL	85E JADE	$e^+e^- \rightarrow e^+e^-\eta$
*** We do not use the following data for averages, fits, limits, etc. ***				
0.476 ± 0.062		¹ RODRIGUES	08 CNTR	Reanalysis
0.64 ± 0.14 ± 0.13		AIHARA	86 TPC	$e^+e^- \rightarrow e^+e^-\eta$
0.56 ± 0.16	56	WEINSTEIN	83 CBAL	$e^+e^- \rightarrow e^+e^-\eta$
0.324 ± 0.046		BROWMAN	74B CNTR	Primakoff effect
1.00 ± 0.22		² BEMPORAD	67 CNTR	Primakoff effect

$$\sigma(e^+e^- \rightarrow e^+e^-\eta, \sqrt{s}=1\text{GeV})$$

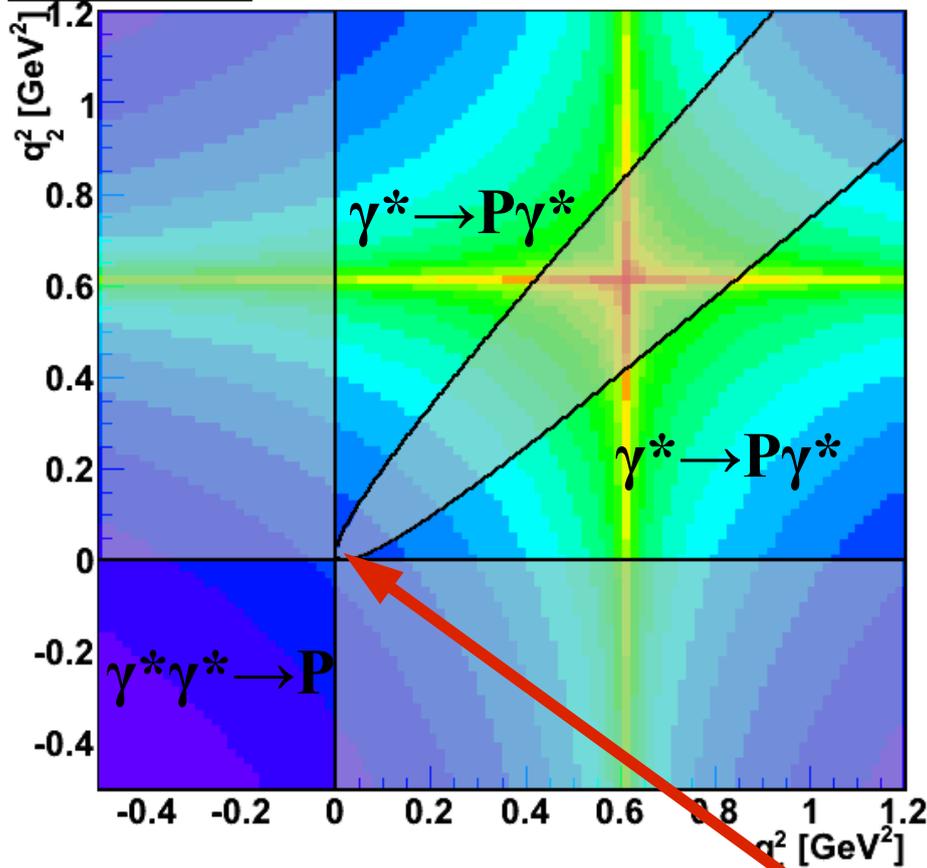
$$\Gamma_{\gamma\gamma} = 520 \pm 20_{\text{stat}} \pm 13_{\text{syst}} \text{ eV}$$

[KLOE JHEP1301 (2013) 119]

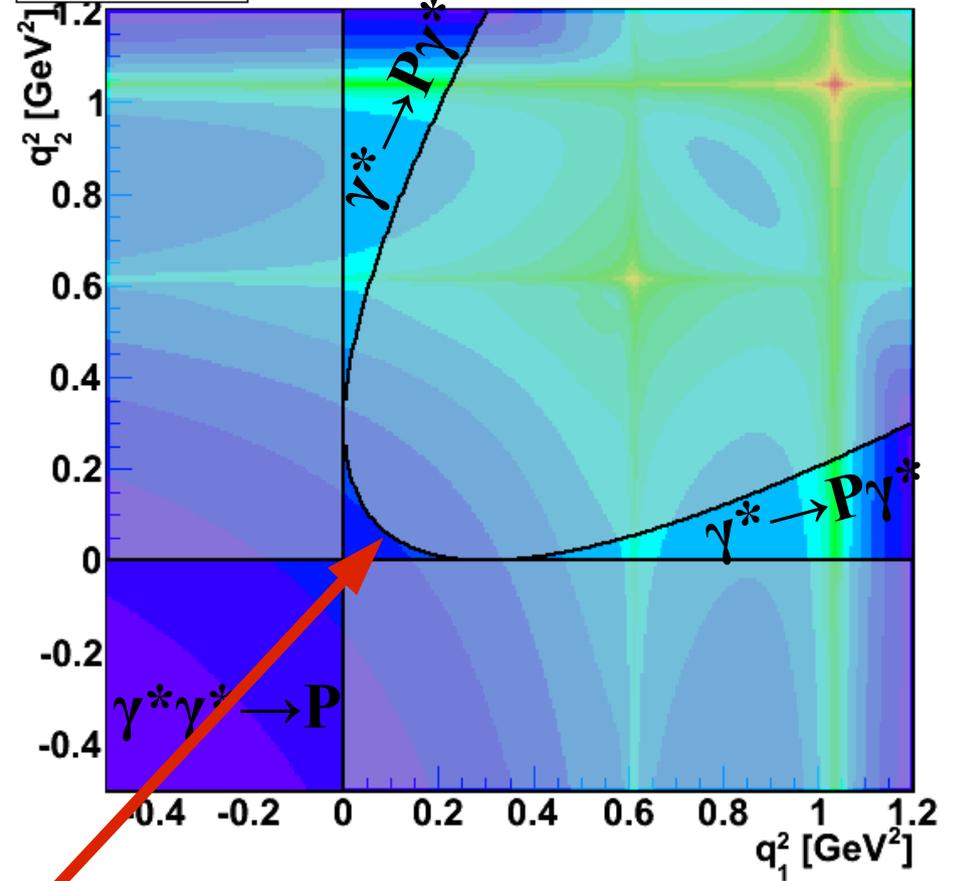
TFF kinematic regions: π^0, η



$|F_{\pi^0}(q_1^2, q_2^2)|^2$ π^0

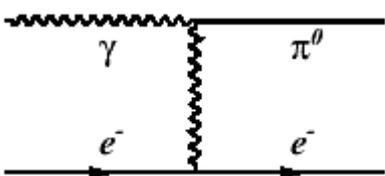
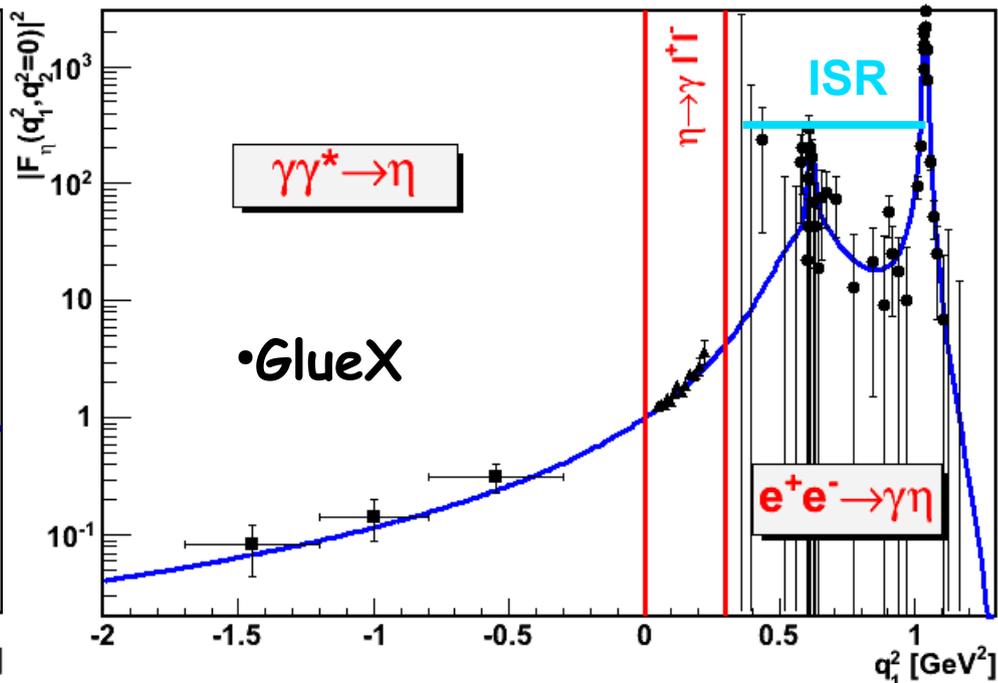
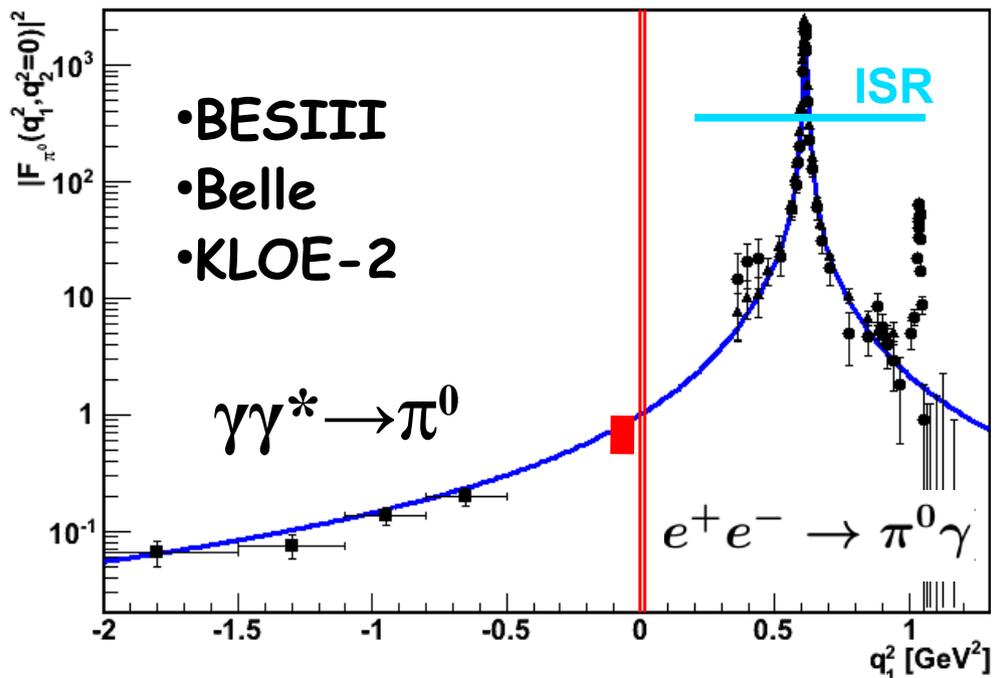


$|F_{\eta}(q_1^2, q_2^2)|^2$ η



$P \rightarrow \gamma^* \gamma^*$

η, π^0 single off shell TFF



$$\frac{d\sigma}{dt}(e^- \gamma \rightarrow e^- P) = \frac{16 \pi \alpha}{3 s m_P^3} \Gamma_{\gamma\gamma} |F_P(t, 0)|^2 \frac{s - m_P^2 + t}{t}$$

$P \rightarrow \gamma^* \gamma$

Dalitz decays:

KLOE, WASA, CBall, BESIII

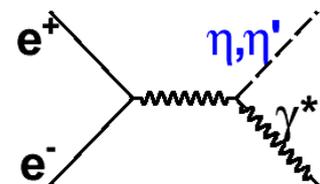
CLAS, NA48

$\gamma^* \rightarrow P \gamma$

VEPP 2000 0.3-2 GeV

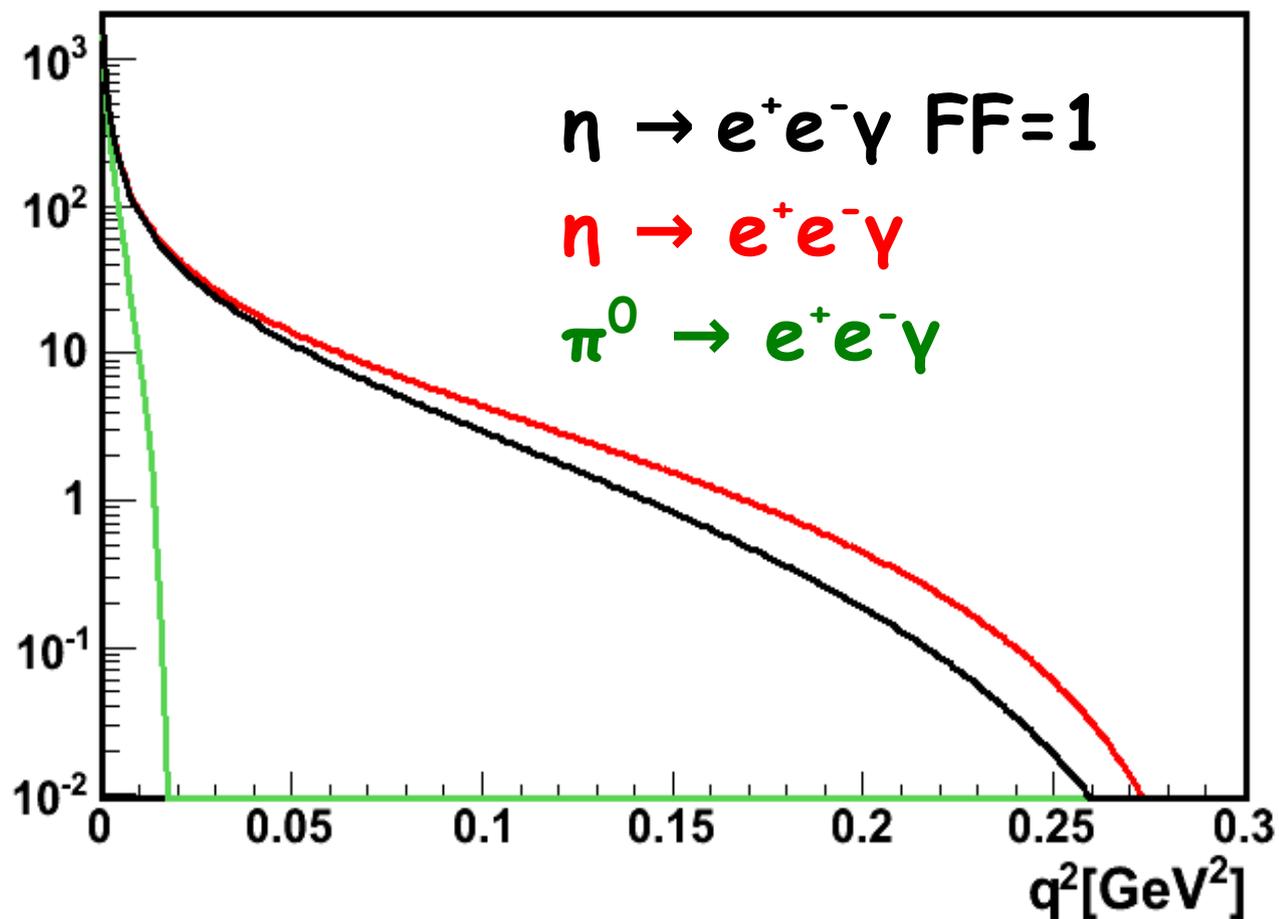
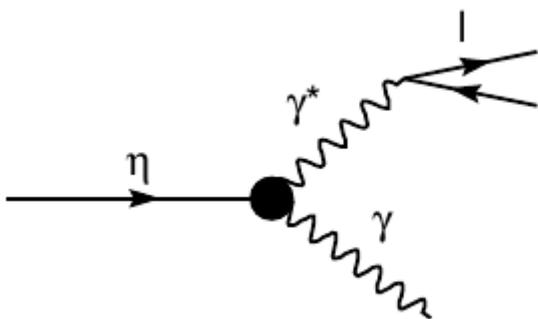
KLOE-2 ISR, BESIII

$$\sigma(e^+ e^- \rightarrow P \gamma) = \frac{8}{3} \pi \alpha \Gamma_{\gamma\gamma} |F_P(s, 0)|^2 \left(\frac{s - m_P^2}{s m_P} \right)^3$$



Dalitz decays

$$\frac{d\Gamma(P \rightarrow \ell^+ \ell^- \gamma)}{dq^2 \Gamma_{\gamma\gamma}} = \frac{2\alpha}{3\pi} \frac{1}{q^2} \sqrt{1 - \frac{4m_\ell^2}{q^2}} \left(1 + \frac{2m_\ell^2}{q^2}\right) \left(1 - \frac{q^2}{M_P^2}\right)^3 |F_P(q^2, 0)|^2$$

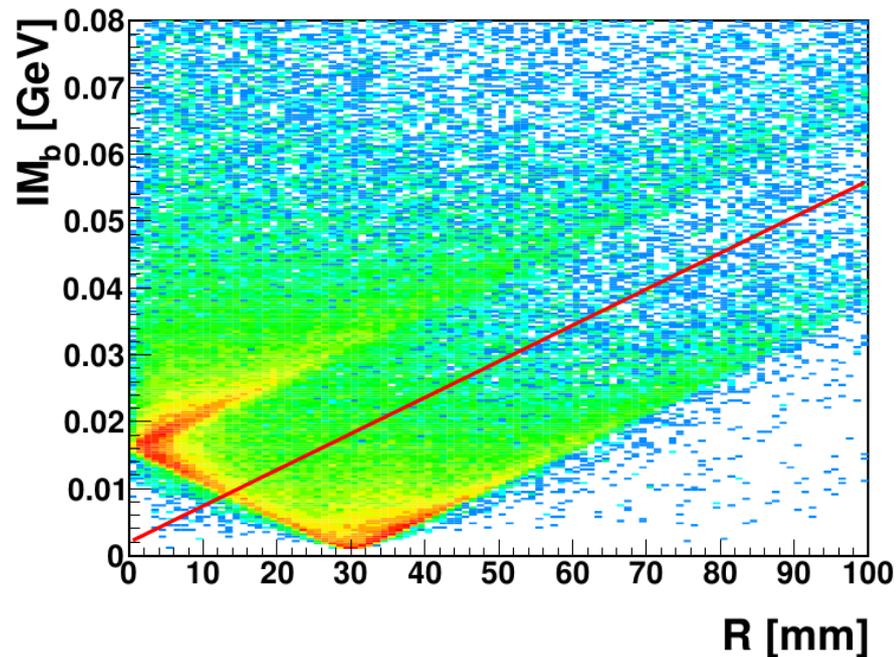
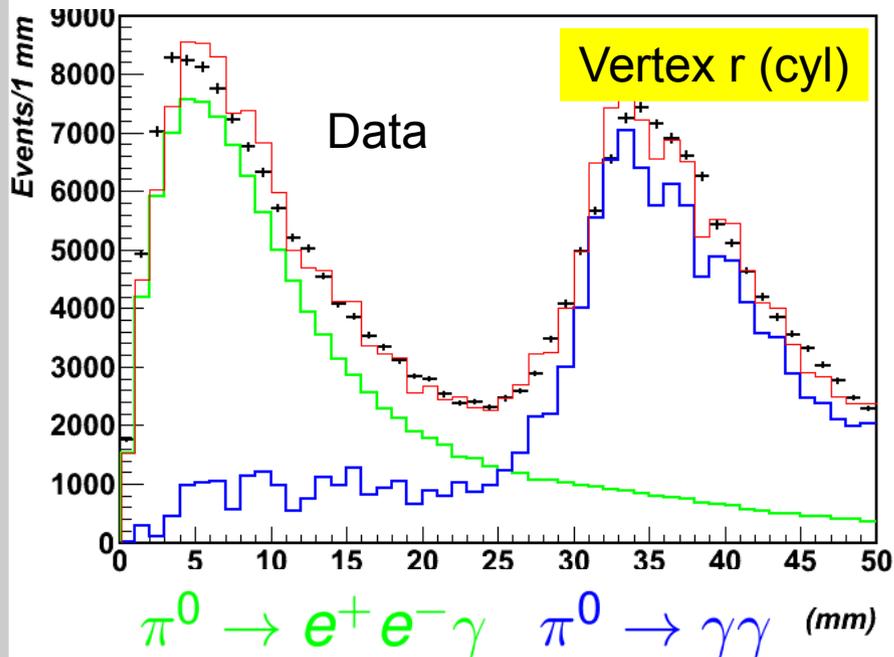
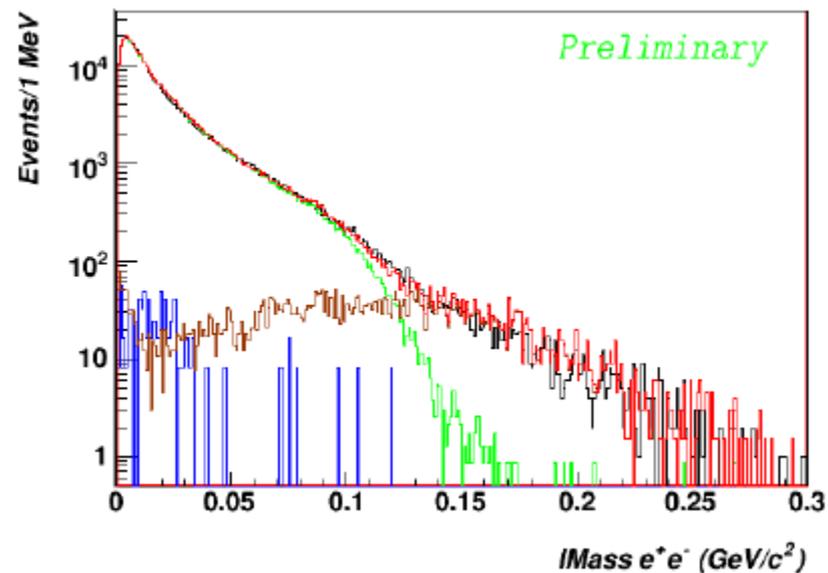
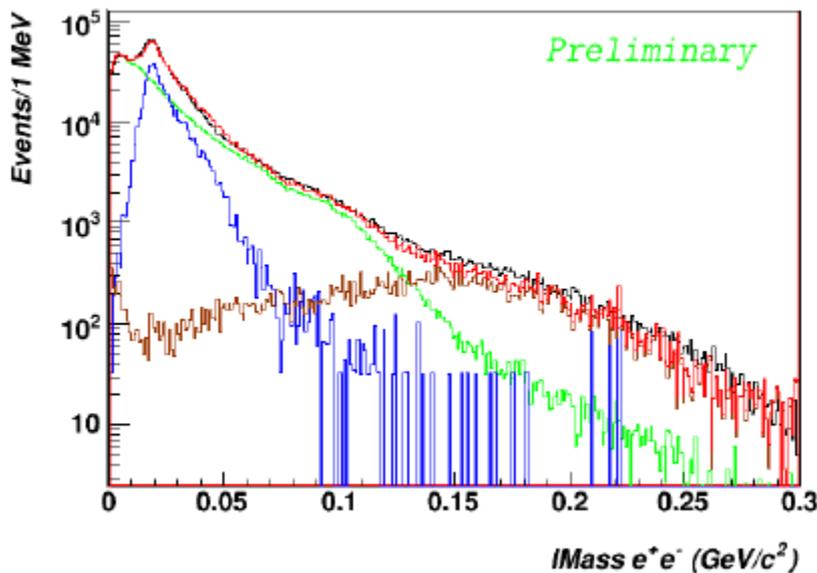




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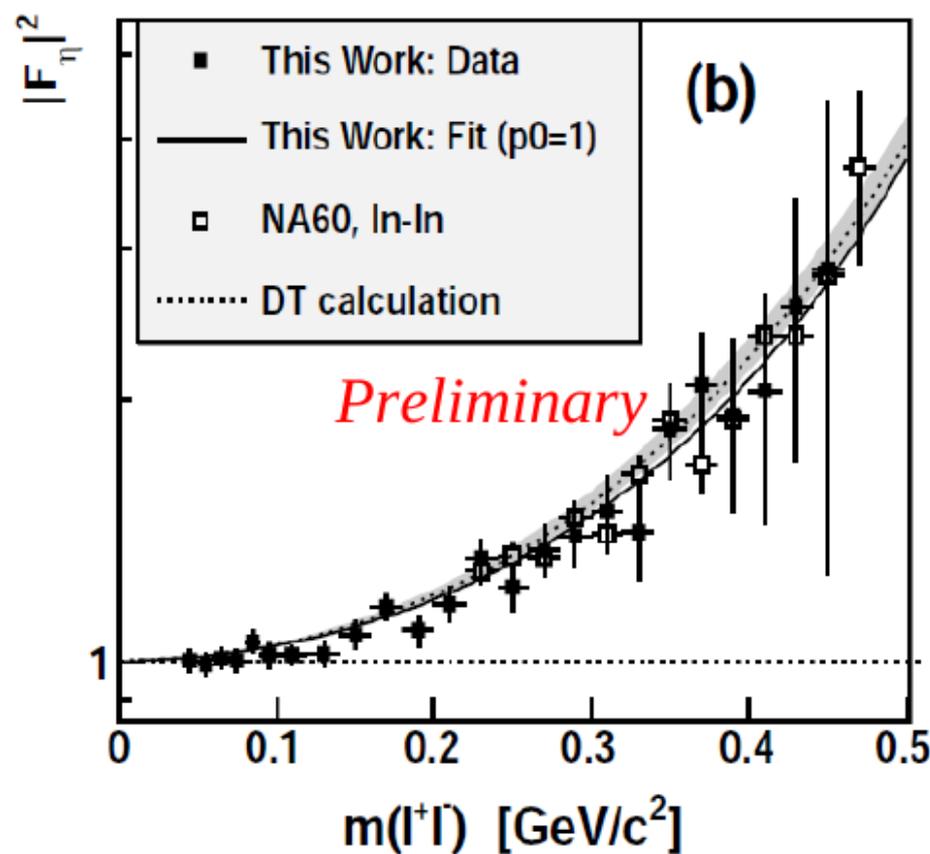
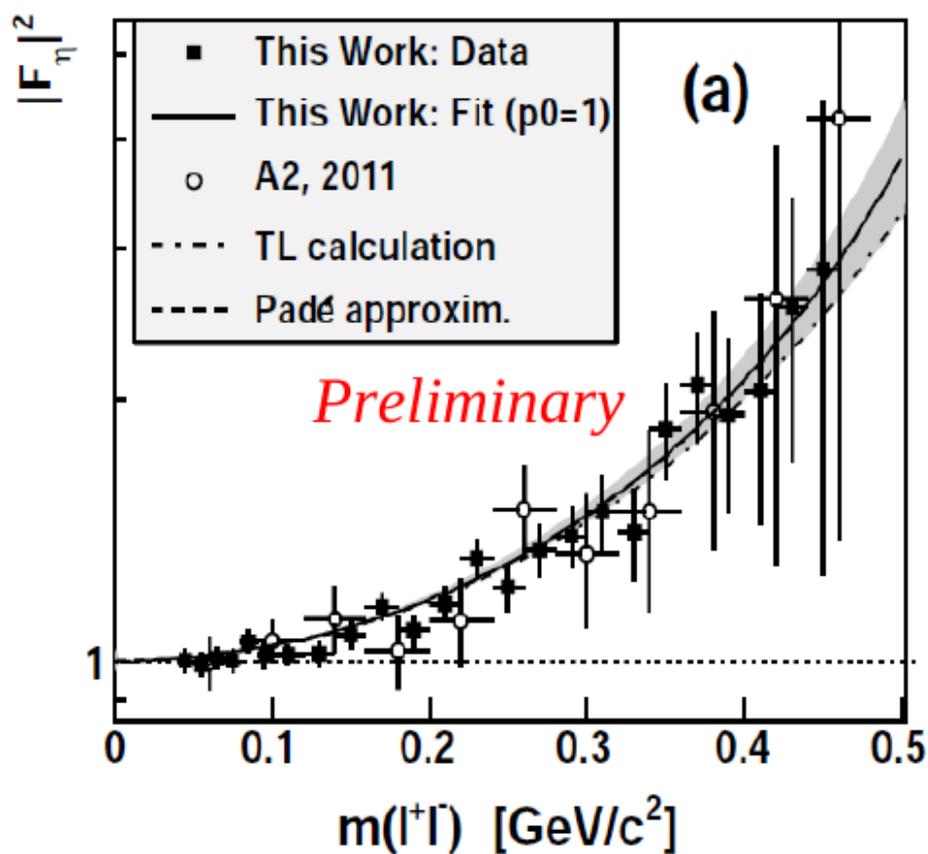
Analysis: $\pi^0 \rightarrow \gamma e^+ e^-$

Vertex r 20 mm + PID



New A2 Result for η TFF

S. Prakhov, M. Unverzagt et al., accepted by Phys. Rev. C, arXiv: 1309.5648 [hep-ex]



$$\Lambda^{-2} = (1.95 \pm 0.15_{\text{stat}} \pm 0.10_{\text{syst}}) \text{ GeV}^{-2} \quad \textit{preliminary}$$

A2, 2011: H. Berghäuser et al., Phys. Rev. B **701** (2011) 562-567.

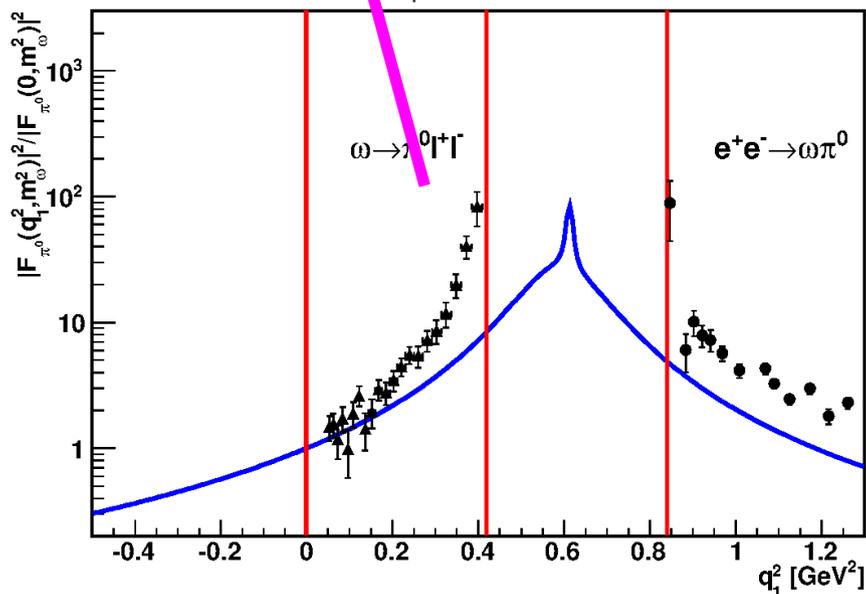
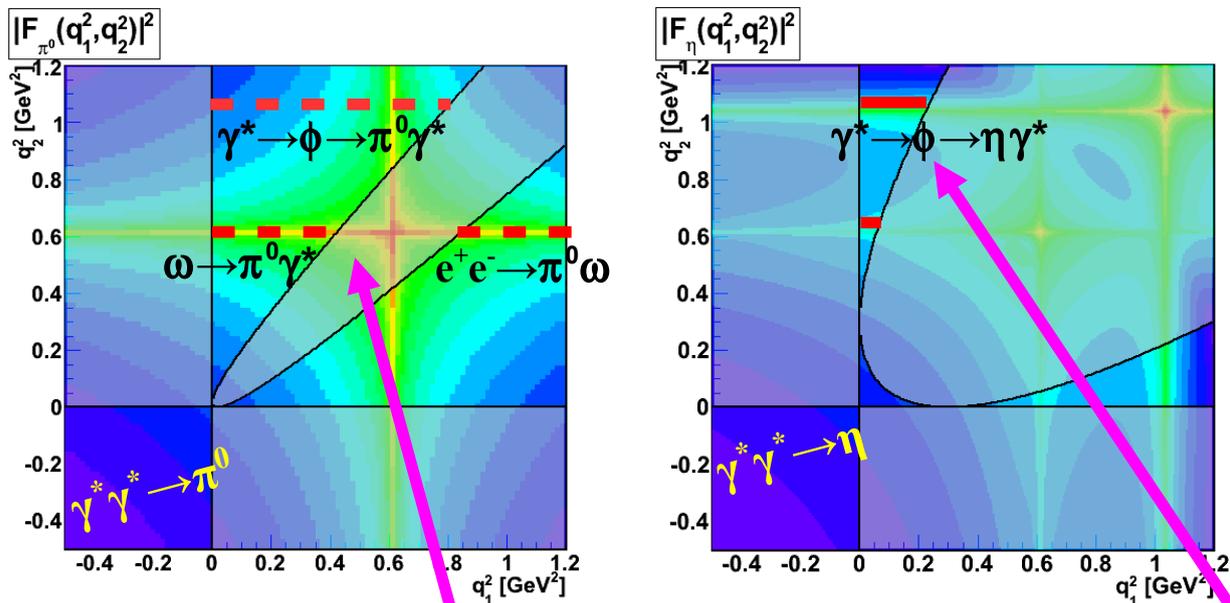
NA60, In-In: R. Arnaldi et al., Phys. Lett. B **677** (2009) 260.

TL calculation: C. Terschlüsen, Diploma thesis, University Gießen, 2010.

Padé-approximants: R. Escribano, P. Masjuan, P. Sanchez-Puertas, arXiv:1307.2061 [hep-ph].

DT calculation: C. Hahnhart, A. Kupś, U.-G. Meißner, F. Stollenwerk, A. Wirzba, Eur. Phys. J. C **73** (2013) 2668.

$V \rightarrow P\gamma^*$ and $e^+e^- \rightarrow PV$ processes

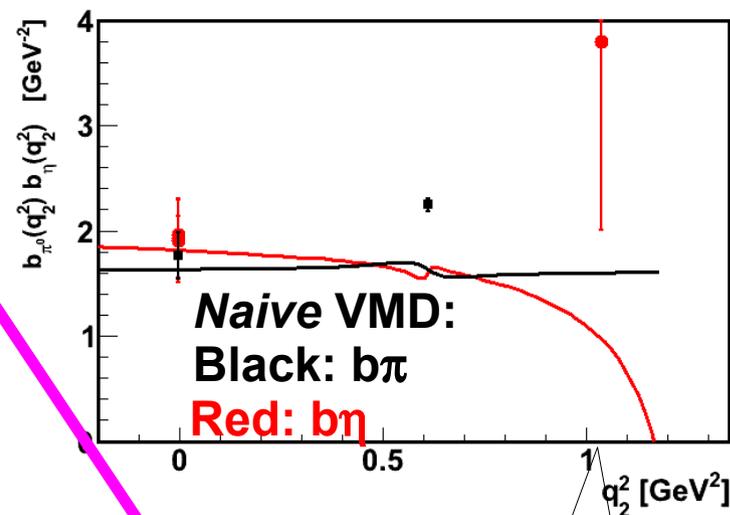


TH: → Bastian talk

Relation to $\omega/\phi \rightarrow \pi^+\pi^-\pi^0$

slopes b_π, b_η

$$b_P(q_2^2) = \left. \frac{\partial \ln |F(q_1^2, q_2^2)|}{\partial q_1^2} \right|_{q_1^2=0}$$



Naive VMD:

Black: b_π

Red: b_η

KLOE prel result

$\phi \rightarrow \eta \gamma^*$ BR 10^{-4}

$b_{\pi^0}(m_\phi^2) \phi \rightarrow \pi^0 \gamma^*$ BR 10^{-5}

$b_\eta(m_\phi^2)$

BESIIIJ/ $\psi \rightarrow P e^+ e^-$ arXiv:1403.7042

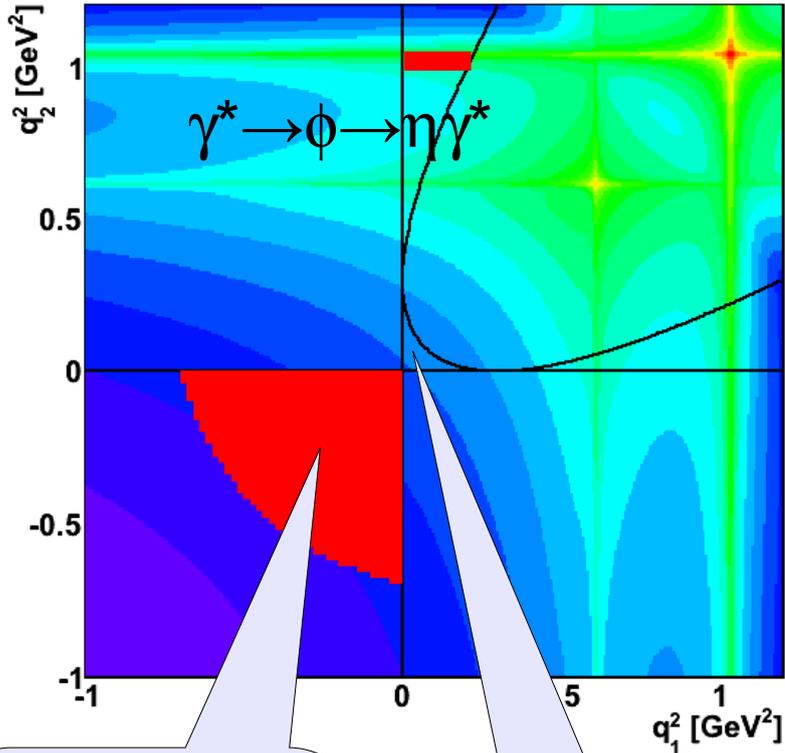


Double off shell TFF

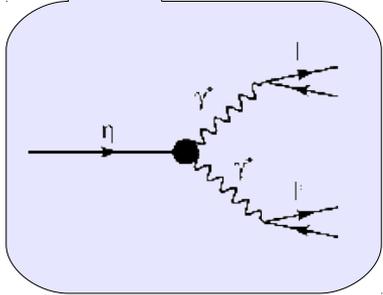
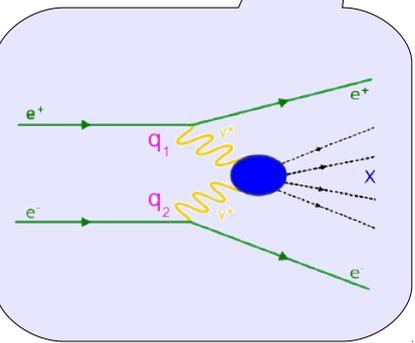


$$|F_\eta(q_1^2, q_2^2)|^2$$

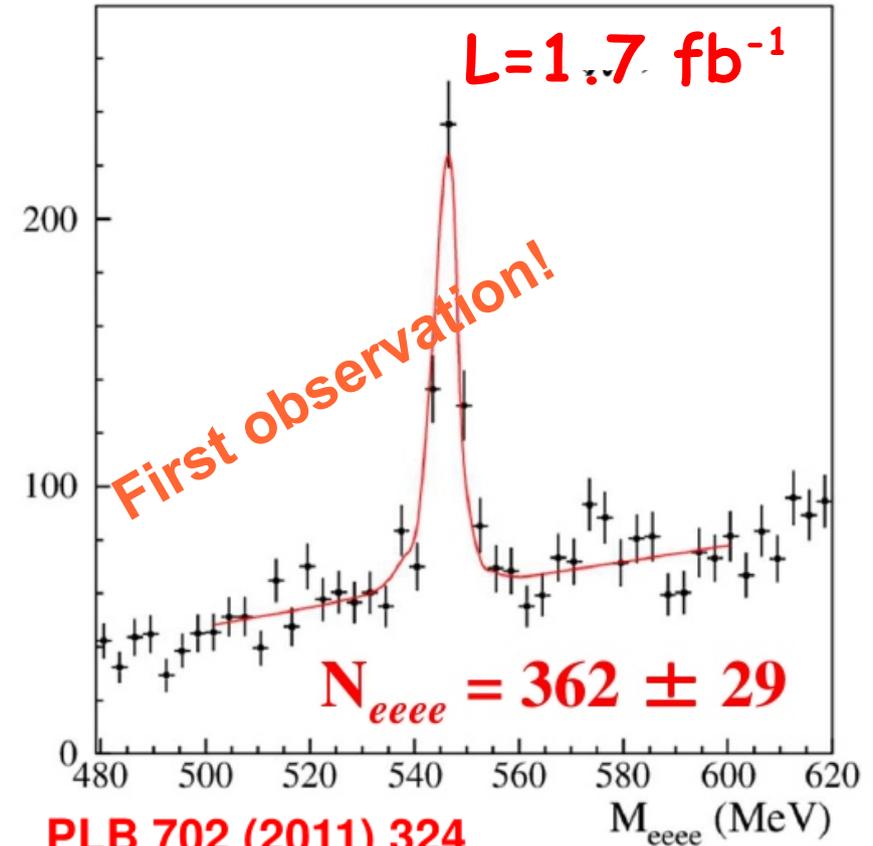
η



$\gamma^* \rightarrow \phi \rightarrow \eta \gamma^*$



$$\eta \rightarrow e^+ e^- e^+ e^-$$

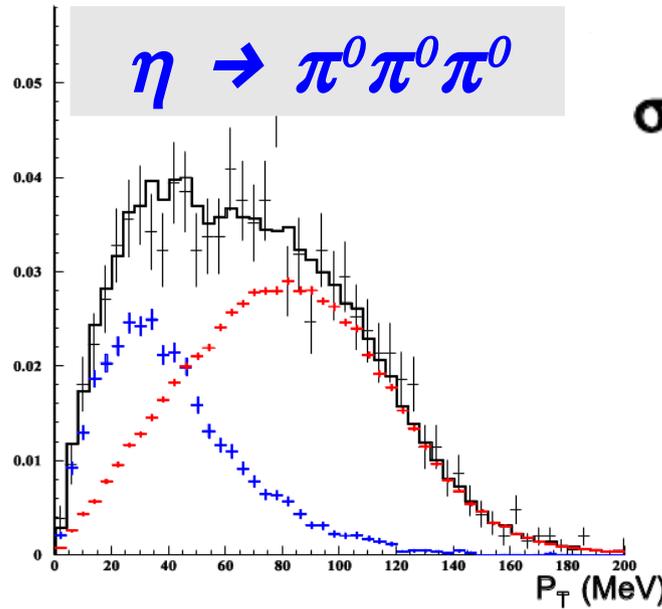
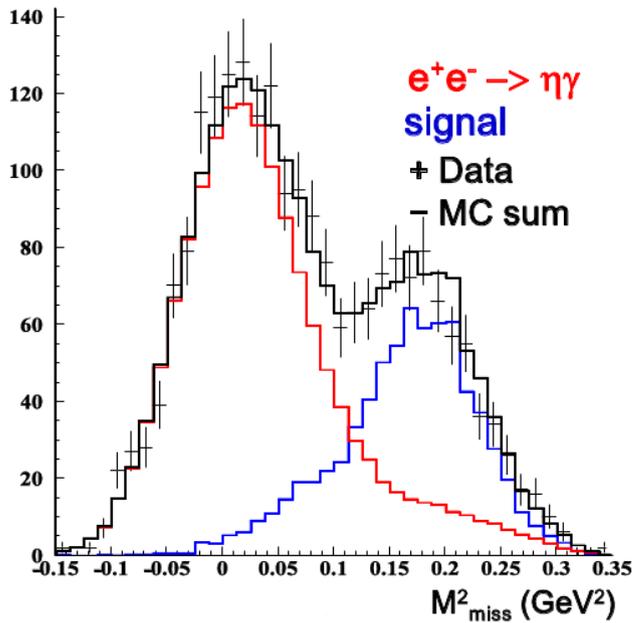


PLB 702 (2011) 324

$$BR(\eta \rightarrow e^+ e^- e^+ e^- (\gamma)) = (2.4 \pm 0.2_{\text{stat}} \pm 0.1_{\text{syst}}) \times 10^{-5}$$



η meson radiative decay width

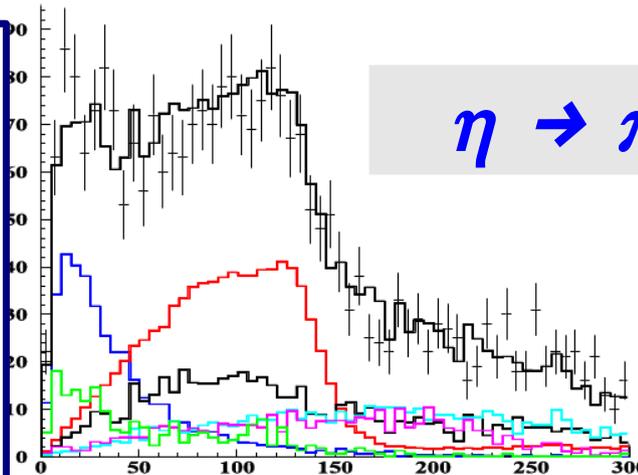
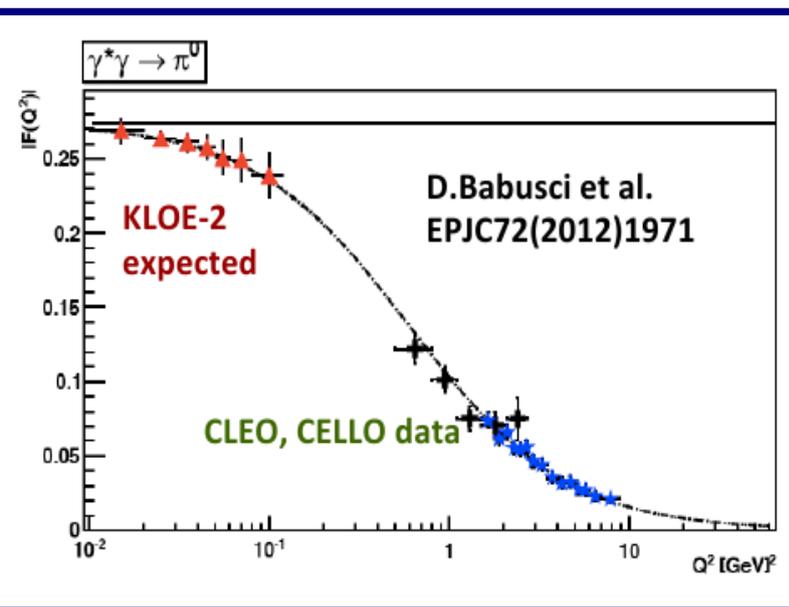


$$\sigma(e^+e^- \rightarrow e^+e^-\eta, \sqrt{s}=1\text{GeV})$$

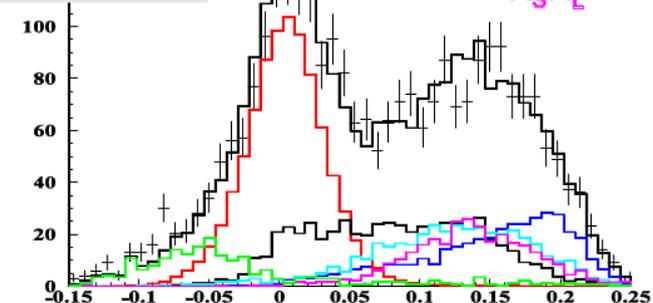
$$L=240 \text{ pb}^{-1}$$

$$\Gamma_{\gamma\gamma}=520 \pm 20 \pm 13 \text{ eV}$$

$$32.0 \pm 1.5 \pm 0.9 \text{ pb}$$



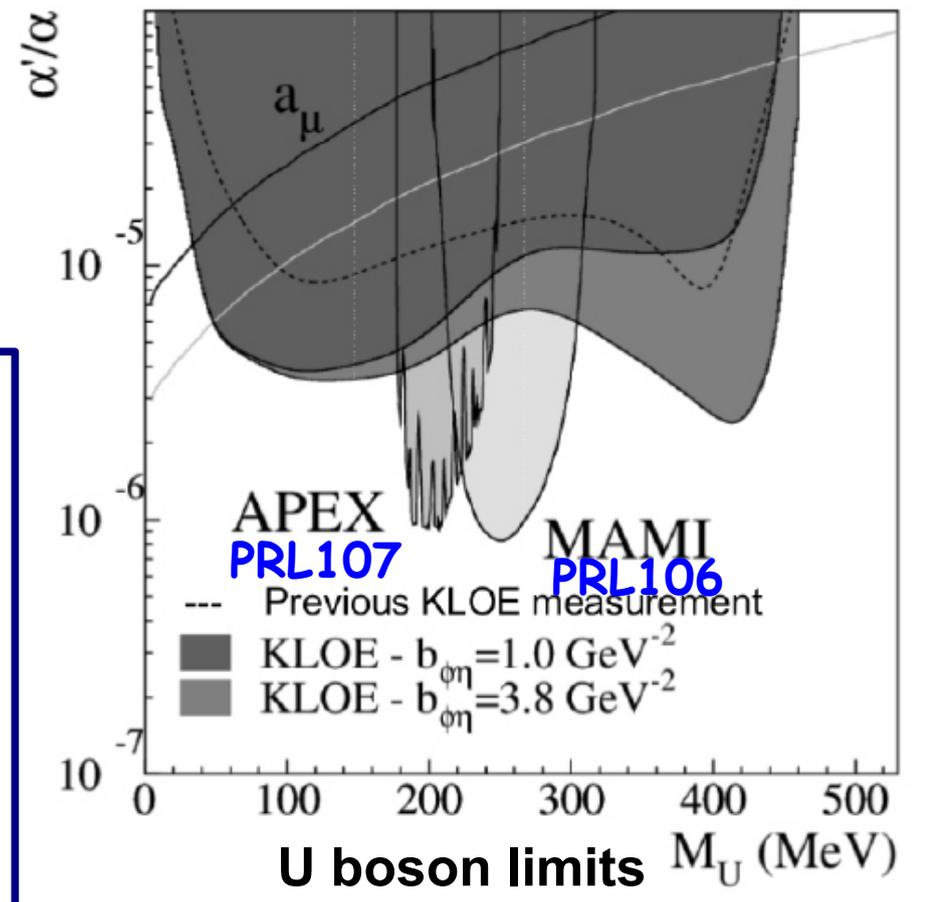
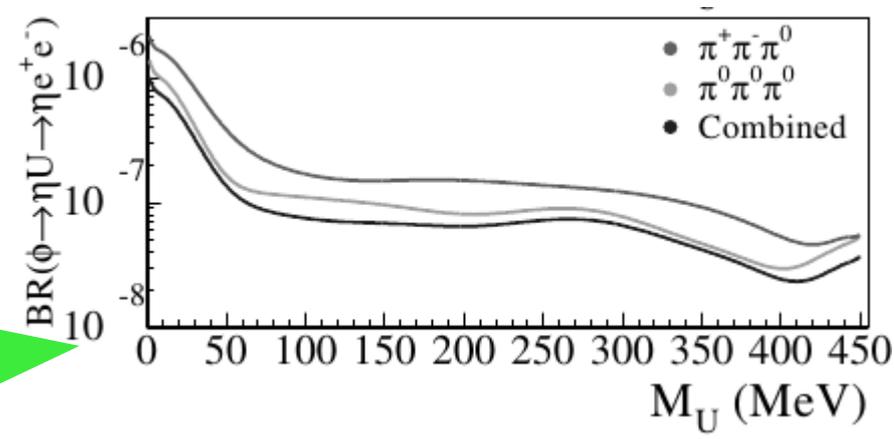
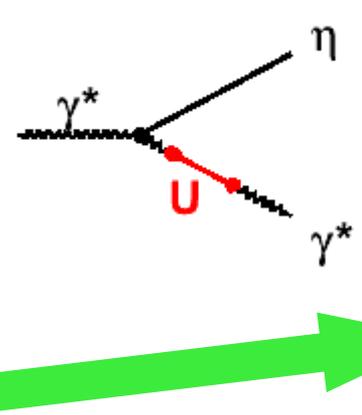
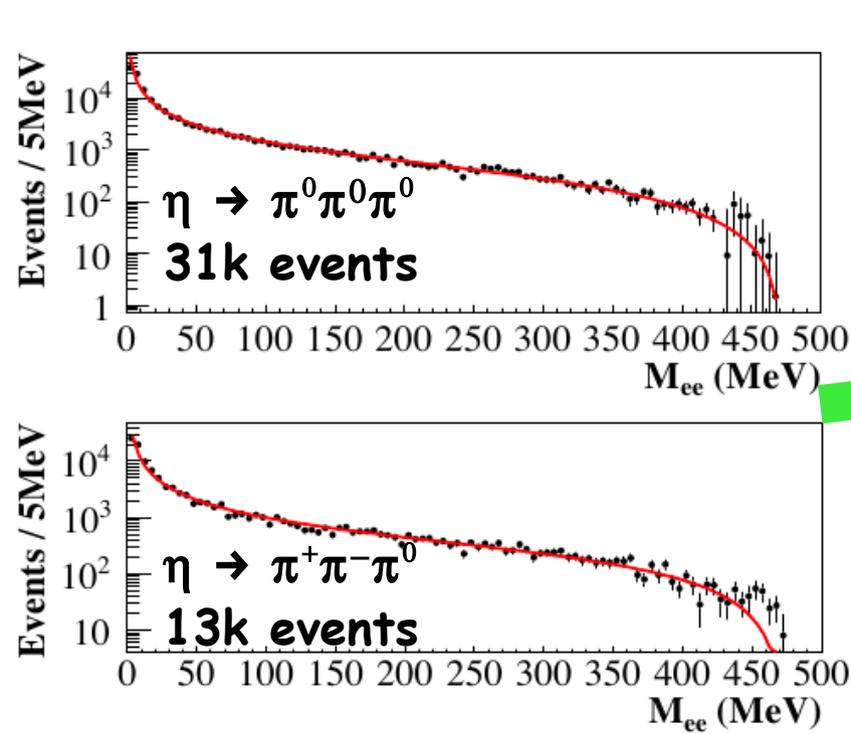
- $\phi \rightarrow \eta \gamma$
- $e^+e^- \rightarrow e^+e^-\gamma$
- $e^+e^- \rightarrow \omega \pi^0$
- Signal
- $e^+e^- \rightarrow K^+K^-$
- $e^+e^- \rightarrow K_S K_L$



$$34.5 \pm 2.5 \pm 1.0 \text{ pb}$$



$\phi \rightarrow e^+e^-\eta$



Form factor/BR:

	SND/CMD-2 (2001)	KLOE – Preliminary Mode	Neutral
$b_{\phi\eta} [\text{GeV}^{-2}]$	$3.8 \pm 1.8 / --$	$1.17 \pm 0.11^{+0.09}_{-0.08}$	
BR ($\times 10^4$)	$1.19 \pm 0.31 / 1.14 \pm 0.16$	$1.131 \pm 0.031 \pm 0.007^{+0.011}_{-0.006}$	

$$F_\eta(q^2, m_\phi^2) \propto \frac{1}{1 - b_\eta(m_\phi^2)q^2}$$



$$\psi \rightarrow e^+e^-\pi^0$$



Value (10^{-5})	CL%	EVTS	Document ID	TECN
1.12 ± 0.28	OUR AVERAGE			
$1.01 \pm 0.28 \pm 0.29$		52	ACHASOV ¹	2002D SND
$1.22 \pm 0.34 \pm 0.21$		46	AKHMETSHIN ₂	2001C CMD2

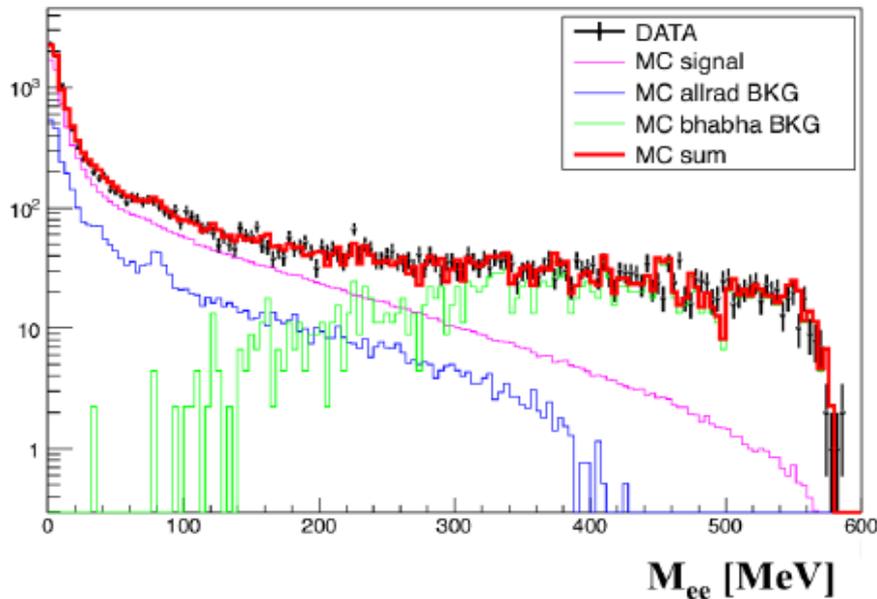
9k events

Background
radiative Bhabha
and $\psi \rightarrow \pi^0\gamma$

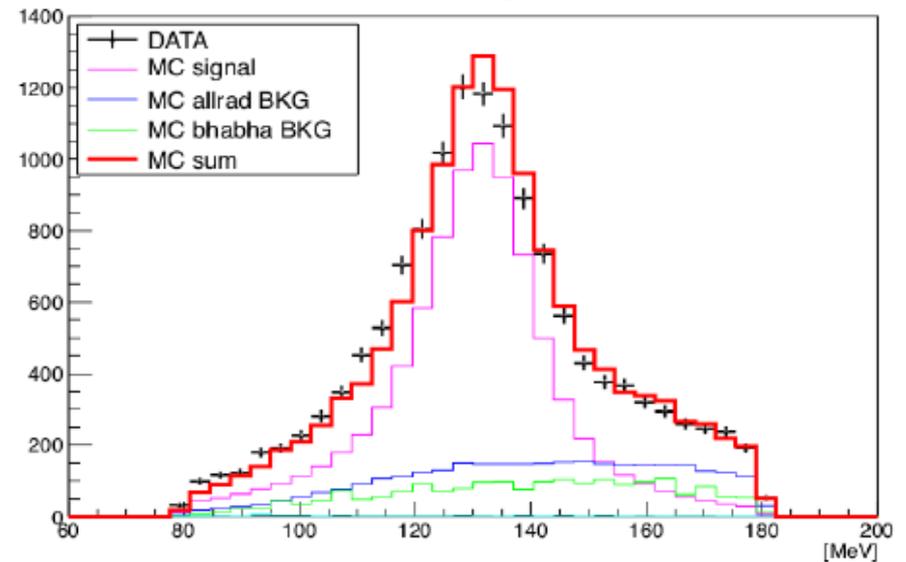
efficiency:
 $15\% \rightarrow 2\%$
low \rightarrow high q

Analysis in progress:
background
subtraction +
global efficiency

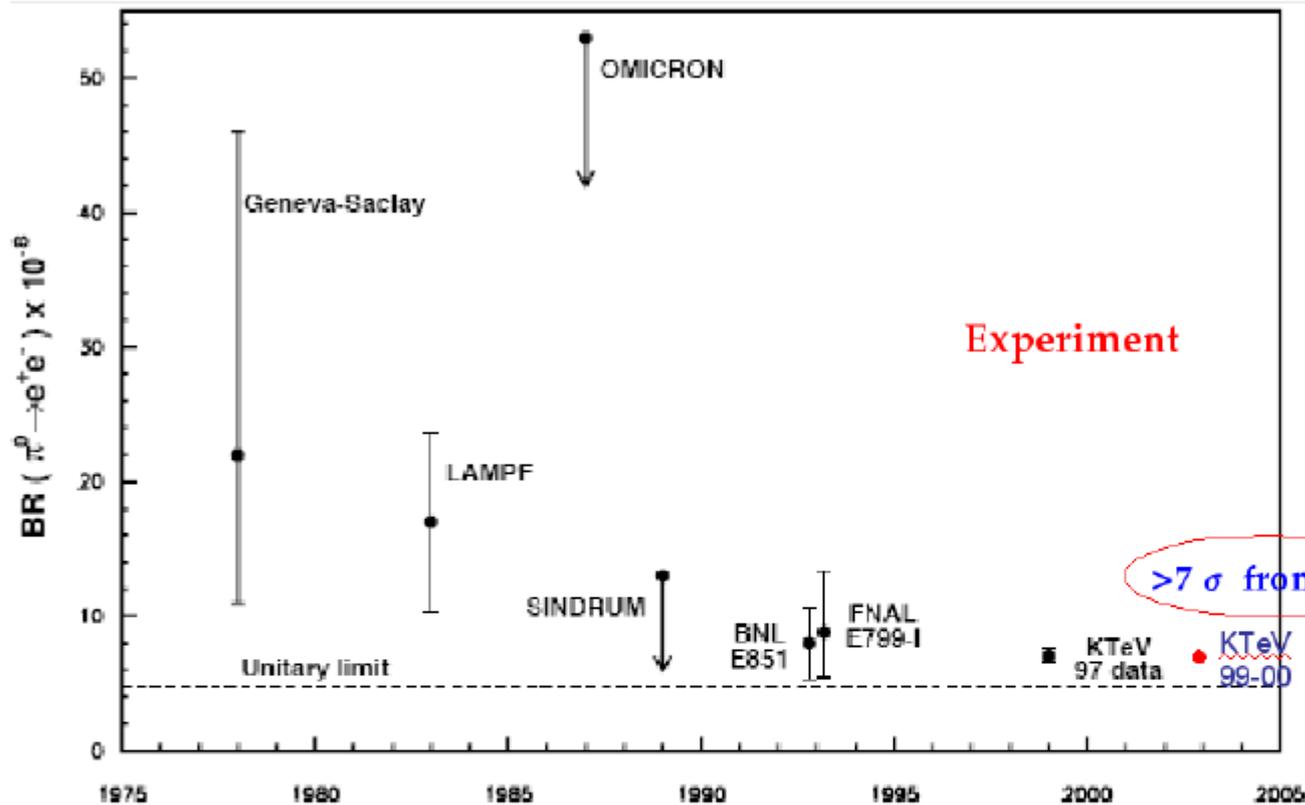
e^+e^- mass spectrum



e^-e^+ missing mass



History of $\pi^0 \rightarrow e^+ e^-$ measurements



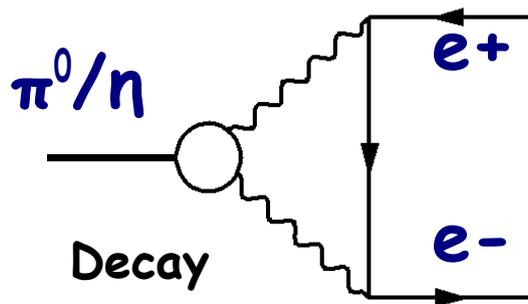
$$BR \approx \alpha^2 \left(\frac{m_e}{m_\pi} \right)^2 \approx O(10^{-8})$$

- Unitary bound (model independent) $BR \geq 4.75 \cdot 10^{-8}$
- Experiment: KTeV (794 events from $K_L \rightarrow 3\pi^0$):

$$BR(\pi^0 \rightarrow e^+ e^-) = (6.44 \pm 0.25_{stat} \pm 0.22_{syst}) \times 10^{-8}$$

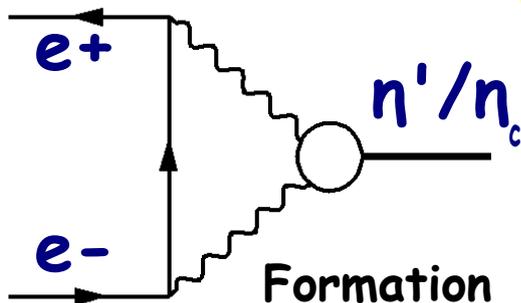
$$BR_{\text{no-rad}}(\pi^0 \rightarrow e^+ e^-) = (7.48 \pm 0.29_{stat} \pm 0.25_{syst}) \times 10^{-8}$$

PRD75:012004(07)



HADES
WASA
CBall
NA48/NA62

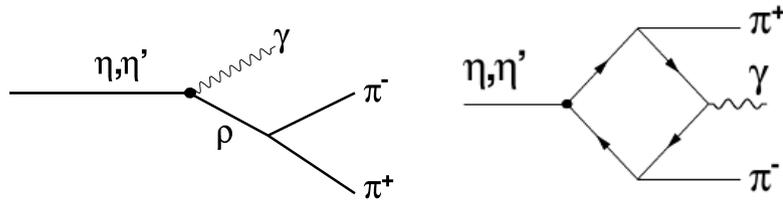
	UB	SM 3σ diff	EXP
$\mathcal{B}(\pi^0 \rightarrow e^+e^-) \times 10^8$	≥ 4.69	6.23 ± 0.12	7.49 ± 0.38 KTeV2007
$\mathcal{B}(\eta \rightarrow e^+e^-) \times 10^9$	≥ 1.78	5.2 ± 0.3	$\leq 5.6 \cdot 10^3$ HADES2012
$\mathcal{B}(\eta' \rightarrow e^+e^-) \times 10^{10}$	≥ 0.36	1.9 ± 0.3	$\leq 2.1 \cdot 10^3$ ND1988
$\mathcal{B}(\eta_c \rightarrow e^+e^-) \times 10^{14}$	≥ 4.2	Dorokhov, PLB667,145	



Searches using formation:
 $e^+e^- \rightarrow \eta'$, $L=0.5\text{pb}^{-1}$
 $\Rightarrow B < 2.1 \cdot 10^{-7}$ 90% CL

Vorobev SJNP 48(1988)273

$\eta \rightarrow \pi^+ \pi^- \gamma$

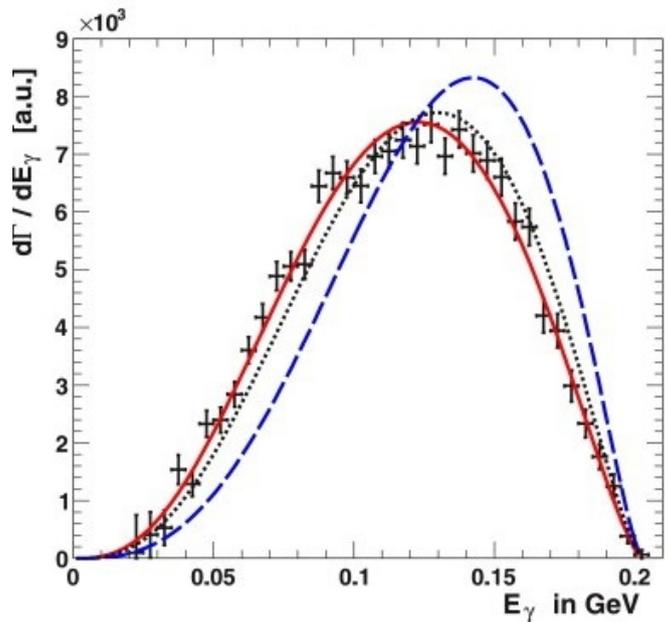


$$\frac{d\Gamma_{\eta(\eta')}}{ds_{\pi\pi}} \propto \left| C + \frac{1}{s_{\pi\pi} - m_\rho^2 - im_\rho \Gamma_\rho} \right|^2$$

$$\frac{d\Gamma}{ds} = |A(1 + \alpha s + \dots) F_V(s)|^2 K_P(s)$$

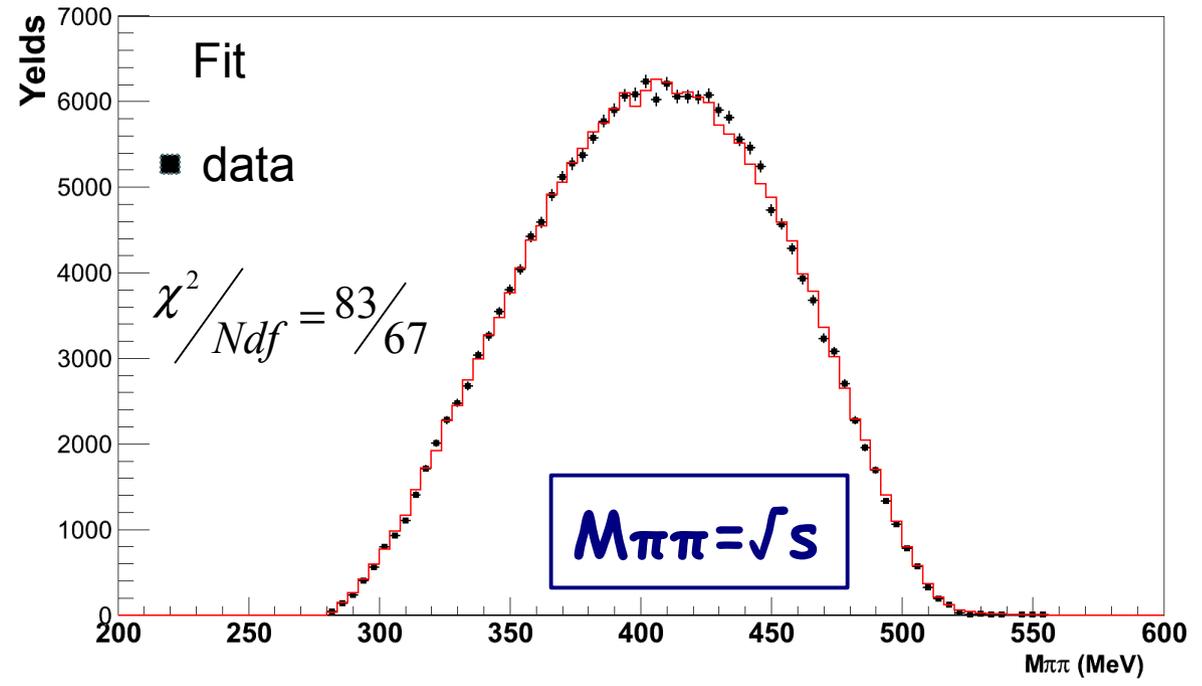
PLB707 (2012) 184

$e^+ e^- \rightarrow \pi^+ \pi^-$



$$\alpha = 1.89 \pm 0.25_{\text{stat}} \pm 0.59_{\text{syst}} \text{ GeV}^{-2}$$

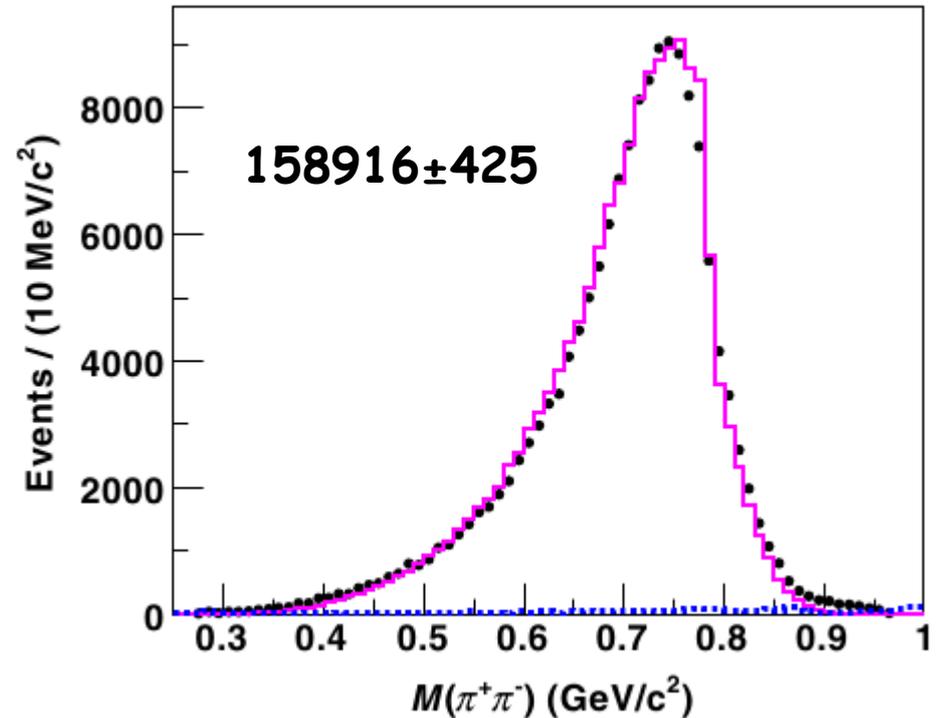
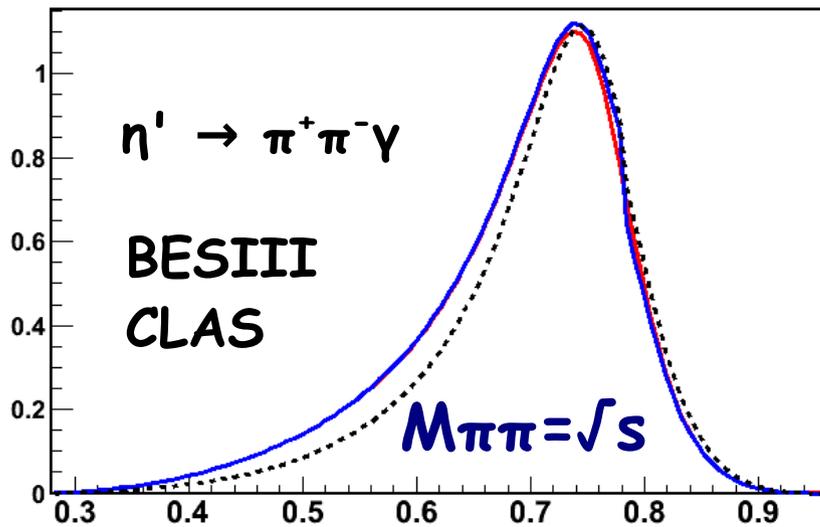
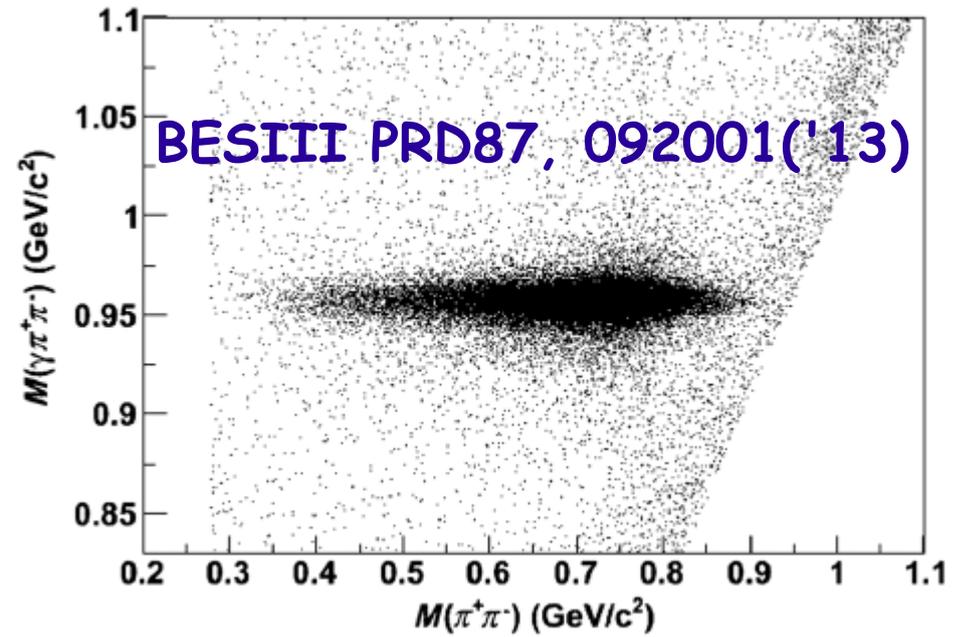
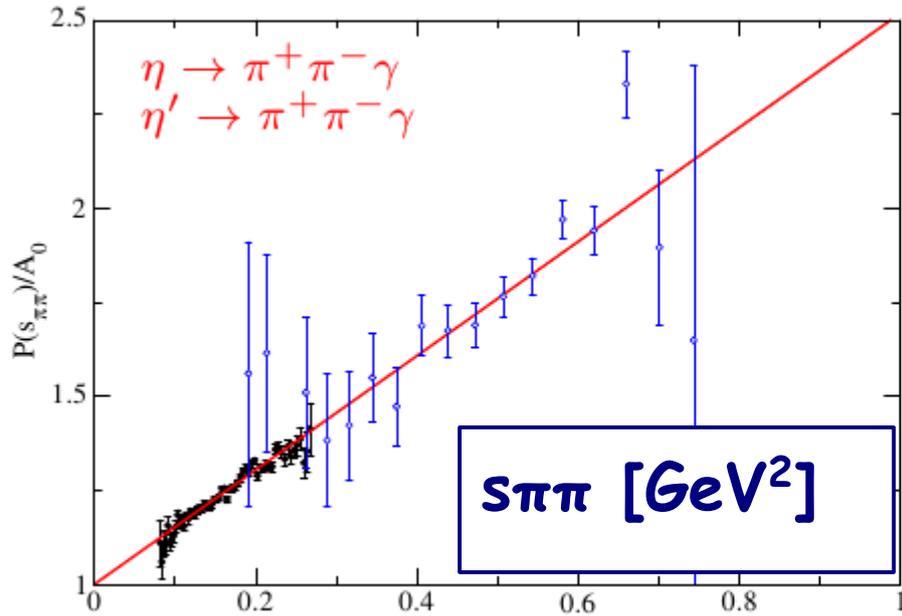
[WASA PLB707 (2012) 243]



$$\alpha = 1.31 \pm 0.08_{\text{stat}} \pm 0.40_{\text{syst}} \text{ GeV}^{-2}$$

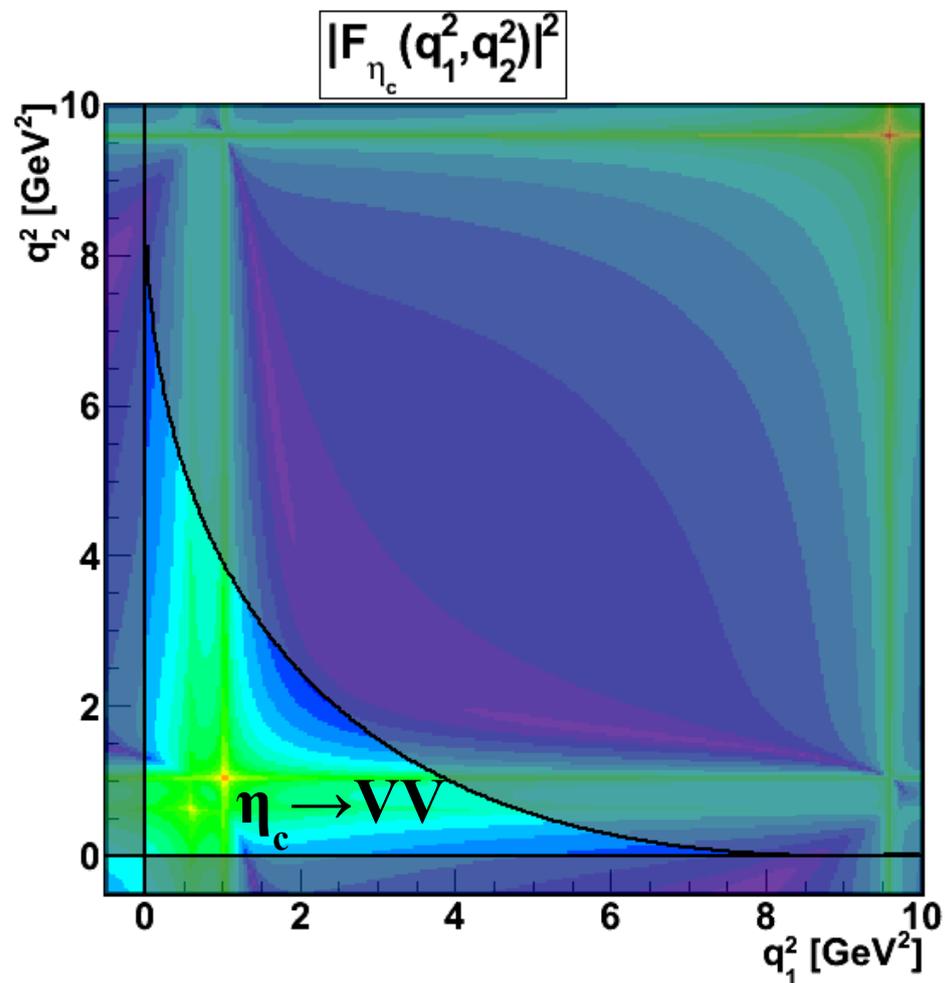
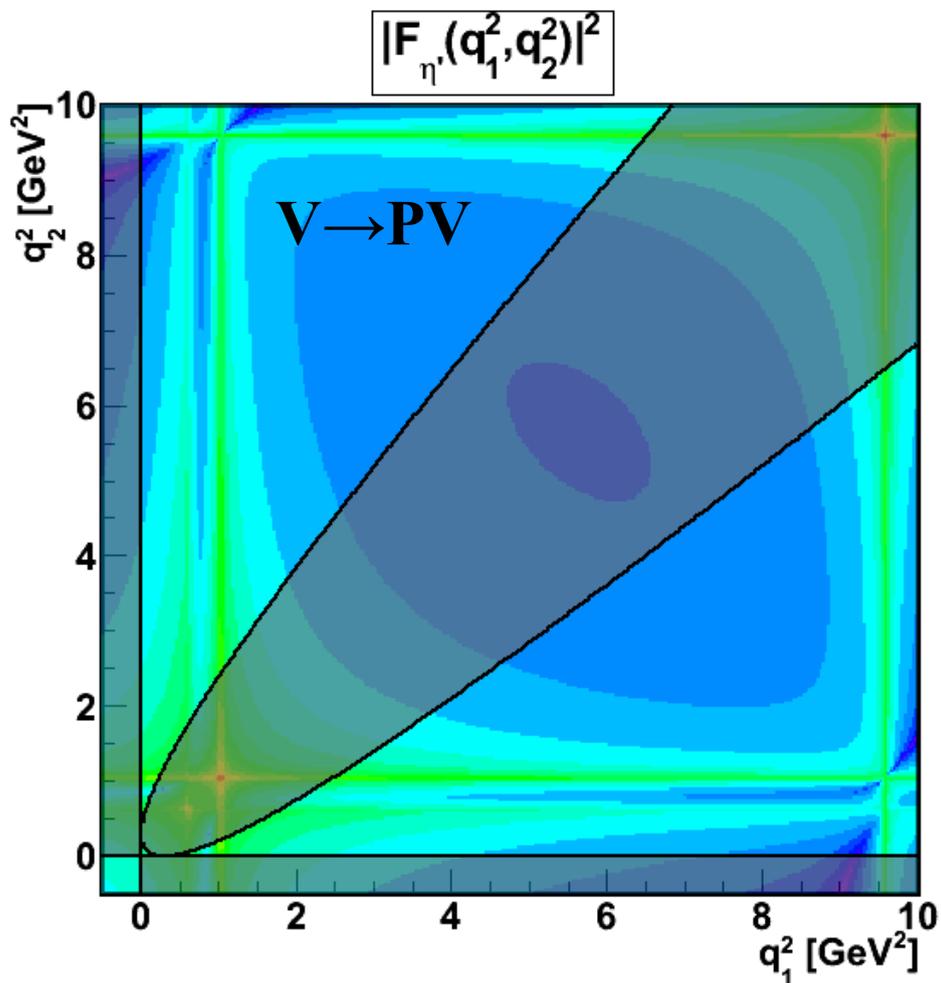
[KLOE PLB718 (2013) 910]

$\eta' \rightarrow \pi^+\pi^-\gamma$



DATA: C Barrel PLB 402,195 ('97); KLOE PL B718, 910 ('13)

Outlook η' , η_c



$\eta' \rightarrow \pi^+\pi^-\pi^+\pi^-$
 $\eta' \rightarrow \pi^+\pi^-\pi^0\pi^0$

arXiv:1404.0096

BESIII:

$> 5 \times 10^6 \eta'$
 $17 \times 10^6 \eta_c$

$\eta_c \rightarrow \rho\rho$ 1.8%
 $\eta_c \rightarrow K^*\bar{K}^*$ 0.7%
 $\eta_c \rightarrow \varphi\varphi$ 0.2%