B⁺ leptonic decays: review and prospects for Belle II

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Challenges in Semileptonic B decays @ MITP, Mainz

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 B^+ leptonic decays: review and prospects for Belle II

Apr.12, 2018, MITP

Outline

- Motivations and features
 - * To tag, or not to tag
- $\blacktriangleright \ B^+ \to \tau^+ \nu$
- $\blacktriangleright B^+ \to \ell^+ \nu(\gamma)$
- ► Prospects (Belle II)

Features of $B^+ \rightarrow \ell^+ \nu$

SM predictions

$$\Gamma(B^+ o \ell^+
u) = rac{G_F^2 m_B m_\ell^2}{8\pi} \left(1 - rac{m_\ell^2}{m_B^2}
ight)^2 f_B^2 |V_{ub}|^2$$

$$\begin{array}{l} \blacktriangleright \ \mathcal{B}(B^+ \to \tau^+ \nu) \sim 10^{-4} \\ \blacktriangleright \ \mathcal{B}(B^+ \to \mu^+ \nu) \sim \mathcal{B}(B^+ \to \tau^+ \nu)/300 \\ \vdash \ \mathcal{B}(B^+ \to e^+ \nu) \sim \mathcal{B}(B^+ \to \tau^+ \nu)/10^7 \end{array}$$

Experimental features

B⁺ → τ⁺ν large BF, but multiple ν's
 B⁺ → ℓ⁺ν (ℓ ≠ τ) *E*_ℓ ~ *M*_B/2, but small BF

Motivations for $B^+ \rightarrow \ell^+ \nu$



 very clean place to measure f_B|V_{ub}| and/or search for new physics (e.g. H⁺, LQ)

Motivations for $B^+ \rightarrow \ell^+ \nu$



 very clean place to measure *f_B*|*V_{ub}*| and/or search for new physics (e.g. *H*⁺, LQ)

• ultimate test of LUV $\Gamma(B^+ \to \ell^+ \nu) / \Gamma(B^+ \to \tau^+ \nu) = f(m_{\ell}^2, m_{\tau}^2),$ and all other parameters cancel!

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$B^+ \rightarrow \tau^+ \nu$ by new physics, e.g. H^+



B⁺ → τ⁺ν can be affected by new physics effects
 For instance, H⁺ of 2-Higgs doublet model (type II)

$${\cal B}(B^+ o au^+
u)={\cal B}_{
m SM}(B^+ o au^+
u) imes r_H$$
where $r_H=ig[1-(m_B^2/m_H^2) an^2etaig]^2$ w.s. Hou, PRD 48, 2342 (1993

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$B^+ \rightarrow \tau^+ \nu$ for new physics

Two useful (for NP) ratios

$$R_{\rm ps} = \frac{\tau_{B^0}}{\tau_{B^+}} \frac{\mathcal{B}(B^+ \to \tau^+ \nu)}{\mathcal{B}(B^0 \to \pi^- \ell^+ \nu)}$$
$$R_{\rm pl} = \frac{\mathcal{B}(B^+ \to \tau^+ \nu)}{\mathcal{B}(B^+ \to \mu^+ \nu)}$$

$$\begin{split} R_{\rm ps}^{\rm NP} &= (0.539 \pm 0.043) \big| 1 + r_{\rm NP}^{\tau} \big|^2 \,, \\ R_{\rm pl}^{\rm NP} &= \frac{m_{\tau}^2}{m_{\mu}^2} \frac{(1 - m_{\tau}^2/m_B^2)^2}{(1 - m_{\mu}^2/m_B^2)^2} \big| 1 + r_{\rm NP}^{\tau} \big|^2 \simeq 222.37 \, \big| 1 + r_{\rm NP}^{\tau} \big|^2 \end{split}$$

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To tag, or not to tag

- ► Why bother?
 - * $B^+ \rightarrow \tau^+ \nu$ has multiple ν 's in the final state
 - * need extra kinematic constraints to improve sensitivity
 - * exploit $\Upsilon(4S)$ producing $B\overline{B}$ and nothing else

$$e^+e^-
ightarrow \Upsilon(4S)
ightarrow B_{
m sig}\overline{B}_{
m tag}$$

- ► How to tag?
 - * "hadronic tagging" full reconstruction of the decay chain of B_{tag}
 - * "semileptonic tagging" use $B^+ \to \overline{D}^{(*)} \ell^+ \nu$



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$B^+ \rightarrow \tau^+ \nu$ (Belle, had) – signal extraction

- ► Signal τ modes: $\tau^+ \to e^+ \nu_e \overline{\nu}_\tau, \ \mu^+ \nu_\mu \overline{\nu}_\tau, \ \pi^+ \overline{\nu}_\tau, \ \rho^+ \overline{\nu}_\tau$
- ▶ π^0 , K_L^0 veto demand no trace of π^0 , K_L^0 after reconstructing B_{tag} and B_{sig}
 - K_L^0 gives $\sim 5\%$ improvement in the expected sensitivity
- ▶ 2D fitting to $E_{\text{ECL}} \& M_{\text{miss}}^2$
 - improve sensitivity by $\sim 20\%$; more robust against peaking backgs. in E_{ECL}



 E_{ECL} = residual energy in the EM calorimeter (ECL) that has not been attributed to either B_{sig} or B_{tag}

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$B^+ \to \tau^+ \nu$ (Belle, had) – Result

Simultaneous fit to different τ decay modes
 Figures below shown for the sum of different τ decay modes



- ► Signal yield: $62_{-22}^{+23} \pm 6$ significance = 3.0σ incl. systematic error Major sources of systematic error are: background PDF (8.8%), K_L^0 efficiency (7.3%), and B_{tag} efficiency (7.1%).
- $\mathcal{B}(B^+ \to \tau^+ \nu) = \left(0.72^{+0.27}_{-0.25} \pm 0.11\right) \times 10^{-4}$ PRL 110, 131801 (2013)

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 $B^+ \rightarrow \tau^+ \nu$ (BABAR, had) – Result

- Hadronic *B*-tagging analysis with $N_{B\bar{B}} = 468 \times 10^6$
- Signal τ modes: $\tau^+ \rightarrow e^+ \nu_e \overline{\nu}_{\tau}, \ \mu^+ \nu_{\mu} \overline{\nu}_{\tau}, \ \pi^+ \overline{\nu}_{\tau}, \ \rho^+ \overline{\nu}_{\tau}$
- Signal extraction via E_{extra} (= E_{ECL}) N_{sig} = 62.1 ± 17.3 from simultaneous fit to the four τ modes
- $\mathcal{B}(B^+ \to \tau^+ \nu) = (1.83^{+0.53}_{-0.49} \pm 0.24) \times 10^{-4}$
- Major systematic uncertainties are from background PDF's (10%), B-tag efficiency (5%), etc.



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PRD 88, 031102(R) (2013)

$B^+ \rightarrow \tau^+ \nu$ (Belle, SL-tag)





- tagged by $B^- \to D^{(*)0} \ell^- \overline{\nu}$
- Signal extraction by 2D-fitting (*E*_{ECL}, *p*^{*}_{sig})
 *N*_{sig} = 222 ± 50 events
- $\mathcal{B}(B^+ \to \tau^+ \nu) = (1.25 \pm 0.28 \pm 0.27) \times 10^{-4}$

 4.6σ significance by combining had-tag and SL-tag analyses of Belle

PRD 92, 051102(R) (2015)



 $\begin{array}{l} \mbox{Belle combined: } \mathcal{B}(B^+ \to \tau^+ \nu) = (0.91 \pm 0.22) \times 10^{-4} \\ \mbox{BABAR combined: } \mathcal{B}(B^+ \to \tau^+ \nu) = (1.79 \pm 0.48) \times 10^{-4} \\ \mbox{World avg: } \mathcal{B}(B^+ \to \tau^+ \nu) = (1.06 \pm 0.19) \times 10^{-4} \\ \mbox{HFLAV (2017)} \end{array}$

- Belle vs. BABAR consistent within $\sim 1.7\sigma$
- The average is consistent with SM

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$B^+ \rightarrow \tau^+ \nu$ constraints on charged Higgs

• With 2-Higgs doublet model (type II), $\mathcal{B}(B^+ \to \tau^+ \nu) = \mathcal{B}_{\text{SM}}(B^+ \to \tau^+ \nu) \times \left[1 - (m_B^2/m_H^2) \tan^2 \beta\right]^2$



Plots are from PRD 88, 031102(R) (2013), by BABAR, based on BABAR's combined $\mathcal{B}(B^+ \to \tau^+ \nu)$.

Search for $B^+ \to \ell^+ \nu$

- ► (*experimental*) very clean
 - * just a mono-energetic charged lepton and nothing else
- (*theoretical*) very small branching fraction compared to $B^+ \to \tau^+ \nu$
 - * helicity suppression: $\Gamma \propto m_\ell^2$
- Tagged vs. Untagged for $B^+ \rightarrow \ell^+ \nu$,
 - * tagging is not really necessary \because mono-energetic ℓ^+ in the final state
 - * Nonetheless, analyses with tagging have also been tried

$\Gamma(B^+ \to e^+ \nu_e) / \Gamma_{\text{total}}$

	COMMENT	TECN	NT ID	DOCUME	6	.UE (10 ⁻⁶) CL%	VALL
untagged	$e^+ e^- \rightarrow \Upsilon(4S)$	BELL	A 2007	SATOYAN	1	.98 90	< 0.9
*** We do not use the following data for averages, fits, limits, etc ***							
had tag	$e^+~e^- \to \Upsilon(4S)$	BELL	2015	YOOK	2	90	<3.5
SL tag	$e^+~e^- \to \Upsilon(4S)$	BABR	2010E	AUBERT	1	90	<8
untagged	$e^+~e^-\to\Upsilon(4S)$	BABR	2009V	AUBERT	1	90	<1.9
had tag	$e^+~e^- \to \Upsilon(4S)$	BABR	2008AD	AUBERT	1	90	<5.2

 $\Gamma(B^+ \to \mu^+ \nu_\mu) / \Gamma_{\text{total}}$

	VALUE (10^{-6})	CL%		DOCUMEN	T ID	TECN	COMMENT
untagged	< 1.0	90	1	AUBERT	2009V	BABR	$e^+~e^- \to \Upsilon(4S)$
	*** We do not use the following data for averages, fits, limits, etc ***						mits, etc ***
had tag	<2.7	90	2	YOOK	2015	BELL	$e^+~e^- \to \Upsilon(4S)$
SL tag	<11	90	1	AUBERT	2010E	BABR	$e^+~e^- \to \Upsilon(4S)$
had tag	<5.6	90	1	AUBERT 2	008AD	BABR	$e^+~e^- \to \Upsilon(4S)$
untagged	<1.7	90	1	SATOYAMA	2007	BELL	$e^+~e^- \to \Upsilon(4S)$

Why then bother with 'tagged' for $B^+ \rightarrow \ell^+ \nu$?



- The signal lepton candidate's momentum in B_{sig} rest frame. -

- much better resolution of p_{ℓ}^{B} with the full-recon. tagging
- ▶ But, does it make a case for 'full-recon-tagged' analysis of $B^+ \rightarrow \ell^+ \nu$?

Why then bother with 'tagged' for $B^+ \rightarrow \ell^+ \nu$?

- ► Note: $\mathcal{B}_{SM}(B^+ \to e^+\nu) \sim 10^{-11}$ and $\mathcal{B}_{SM}(B^+ \to \mu^+\nu) \sim 3 \times 10^{-7}$
 - \Rightarrow Any signal for $B^+ \rightarrow e^+ \nu$ at the Belle sensitivity is way beyond the SM
- In that case, are we sure what we see is really B⁺ → e⁺ν? What about B⁰ → e⁺τ⁻? How about B⁺ → e⁺X⁰ where X⁰ is any unknown particle from NP?
- With full-recon., we can use p_{ℓ}^{B} to discern many such cases



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 $B^+ \rightarrow \ell^+ X^0$ (Belle)





 Search for massive neutral invisible fermion "X⁰"

a heavy neutrino, or an LSP in RPV models, or whatever

- Very similar experimental signature to $B^+ \rightarrow \ell^+ \nu$
- But, p_{ℓ}^B gives a handle on M_X

$^+ \rightarrow \ell^+ X^0$ (Belle)



PRD 94, 012003 (2016)

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new untagged $B^+ \rightarrow \mu^+ \nu$ (Belle)

- ► all particles except for the µ⁺ are to come from the other *B*, but its decay chain is not explicitly reconstructed (*hence, untagged*)
- require $M_{\rm bc}$ > 5.1 and $-3.0 < \Delta E < +2.0$



new untagged $B^+ \rightarrow \mu^+ \nu$ (Belle)



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new untagged $B^+ \rightarrow \mu^+ \nu$ (Belle)

- ► all particles except for the µ⁺ are to come from the other *B*, but its decay chain is not explicitly reconstructed (*hence, untagged*)
- require $M_{\rm bc}$ > 5.1 and $-3.0 < \Delta E < +2.0$
- In the B⁺ rest frame, p_µ = 2.64 GeV (*sharp*!), but in the CM frame, 2.45 < p^{*}_µ < 2.85 GeV</p>
- Use p_{μ}^* and neural net (NN) for signal extraction (2D fit)

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NN variables

- $R_1^{\mu o}/R_0^{\mu o}$, $R_2^{\mu o}/R_0^{\mu o}$, $R_3^{\mu o}/R_0^{\mu o}$ where $R_i^{\mu o} = \sum_j$ $\frac{\vec{n}_t \cdot \vec{p}_{\mu}}{|\vec{n}_t||\vec{p}_{\mu}|}$ angle between thrust and muon the muon, and $P_i(x)$ is the *i*th Legendre polynor 17b. 17c.
- R_1^{oo}/R_0^{oo} where $R_i^{oo} = \sum_k \sum_j |\vec{p}_k| |\vec{p}_j| P_i(\cos \theta_{kj}),$
- $R_1^{\text{KFW}} = \sum_k \sum_{j>k} |\vec{p}_k| |\vec{p}_j| P_i(\cos \theta_{kj})$, the first Kaku cm frame, see Fig. 17e.
- $\cos(\theta_{\text{miss}})$ angle of missing momentum in the
- $\sqrt{\sqrt{\Delta Z^2}}$ distance between reconstructed ztransformation tries to make the strongly peak the neural net catch the small difference bety shown in Fig. 17g. The square root function se discriminating variable away from zero.

•
$$s = 1 - \vec{n}_t^2$$
 – sphericity, see Fig. 17i

- ΔE difference between the sum of energy signal muon and expected energy of B mes
- $\frac{\vec{n}_{t}^{\text{ECL}} \cdot \vec{p}_{\mu}}{|\vec{n}^{\text{ECL}}||\vec{n}|}$ where the thrust vector \vec{n}_{t}^{ECL} i and calculated in the lab frame, \vec{p}_{μ} is in th
- $(q_{\mu} + q_{\text{tag}}) \times q_{\mu}$ charge balance, see Fig. 1
- $\frac{\vec{p}_{\mu} \cdot \vec{p}_{B_{\text{tag}}}}{|\vec{p}_{\mu}||\vec{p}_{B_{\text{tag}}}|}$ angle between muon and tag 1
- $\cos \theta_{\mu}$ muon angle in the cm frame, see F

NN variables



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2D distributions (MC) for signal fit



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new untagged $B^+ \rightarrow \mu^+ \nu^-$

Result



 ${\mathfrak{F}} \longrightarrow {\mathfrak{F}} {\mathfrak{F}} {\mathfrak{F}} {\mathfrak{F}}$ studied in detail by FF variation

- measure $R \equiv N_{B o \mu
 u} / N_{B o \pi \ell
 u}$ for (partial) cancellation of syst. error
- most significant (2.4 σ), and consistent with SM

$${}^{0}_{0 \ 0.1 \ 0.2 \ 0.3 \ 0.4 \ 0.5 \ 0.6 \ 0.7} \mathcal{B}(B^+_{0.9} \xrightarrow{}_{o_{nn}} \mu^+ \nu) = (6.46 \pm 2.22 \pm 1.60) \times 10^{-7} \\ \in [2.9, 10.7] \times 10^{-7} @ 90\% \text{ C.L.}$$

arXiv:1712.04123, submitted to PRL

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 $B^0 \rightarrow \ell^{\pm} \tau^{\mp}$ (BABAR)







- ► In a hadronic *B*-tagging analysis very similar to $B^+ \rightarrow \ell^+ \nu$, BABAR also searched for $B^0 \rightarrow \ell^{\pm} \tau^{\mp}$.
- Background suppression using $m_{\rm ES}$ and $E_{\rm extra}$
- ▶ Signal extraction by unbinned max. likelihood fit to p_{ℓ}^{B}

 $\begin{array}{l} \mathcal{B}(B^0 \rightarrow e^{\pm} \tau^{\mp}) < 2.8 \times 10^{-5} \\ \mathcal{B}(B^0 \rightarrow \mu^{\pm} \tau^{\mp}) < 2.2 \times 10^{-5} \end{array}$

$B^+ \to \ell^+ \nu \gamma$

• Helicity suppression (of $B^+ \rightarrow \ell^+ \nu$) is avoided by γ .

$$\Gamma(B^+ o \ell^+
u \gamma) \propto rac{lpha_{
m EM} (G_{
m F} m_B^2 | V_{ub} | f_B)^2}{\lambda_B^2}$$

- ► λ_B is needed for QCDF to calculate, e.g., charmless hadronic *B* decays
- SM expectation: $\mathcal{B}(B^+ \to \ell^+ \nu \gamma) \sim \mathcal{O}(10^{-6})$
 - * Calculation is reliable only for $E_{\gamma} > 1$ GeV
- ▶ Most stringent limits from Belle (2015) with hadronic *B*-tagging
 - * using neural net to suppress the most significant background $B^+ \to \pi^0 \ell^+ \nu$

 $B^+ \rightarrow \ell^+ \nu \gamma$ (Belle)



Enhanced signal MC portions in the figures correspond to $\mathcal{B} = 30 \times 10^{-6}$.

PRD 91, 112009 (2015)

 $B^+ \rightarrow \ell^+ \nu \gamma$ (Belle)

PRD 91, 112009 (2015)

• Signal yields and partial \mathcal{B} for $E_{\gamma} > 1$ GeV

Mode	Signal yield	${\cal B}$ (10 $^{-6}$)	Significance (σ)	${\cal B}$ limit (10 $^{-6}$)
${\it B}^+ ightarrow {\it e}^+ u_{\it e} \gamma$	$6.1^{+4.9+1.0}_{-3.9-1.3}$	$3.8^{+3.0+0.7}_{-2.4-0.9}$	1.7	< 6.1
${\cal B}^+ o \mu^+ u_\mu \gamma$	$0.9^{+3.6}_{-2.6}{}^{+1.0}_{-1.5}$	$0.6^{+2.1}_{-1.5}{}^{+0.7}_{-1.1}$	0.4	< 3.4
${\it B}^+ o \ell^+ u_\ell \gamma$	$6.6^{+5.7+1.6}_{-4.7-2.2}$	$2.0^{+1.7}_{-1.4}{}^{+0.6}_{-0.7}$	1.4	< 3.5

- From the partial B, we set λ_B(E_γ > 1 GeV) > 238 MeV By varying input parameters, we obtain λ_B > (172, 410) MeV
- ▶ 2nd analysis with looser cut ($E_{\gamma} > 0.4$ GeV) also gives no signal and consistent results

BABAR result: $\mathcal{B}(B^+ \to \ell^+ \nu \gamma) < 15.6 \times 10^{-6}$, prd 80, 111105(r) (2009)

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$B^+ \to \tau^+ \nu$ Prospects for Belle II



- E_{ECL} is crucial for $B^+ \rightarrow \tau^+ \nu$ study
 - * In Belle II, beam background is much higher
 - * But such backgrounds can be rejected by tighter selection based on ECL cluster's energy, timing, shape, etc.
- Expected precision at 1 $ab^{-1} \sim 29\%$ (stat.)
- Major systematic sources (bkg. PDF, K⁰_L veto eff., B_{tag} eff., etc.) can be improved with more data

	Integrated Luminosity (ab^{-1})	1	5	50
hadronic tag	statistical uncertainty (%)	29	13	4
	systematic uncertainty $(\%)$	13	$\overline{7}$	5
	total uncertainty (%)	32	15	6
semileptonic tag	statistical uncertainty (%)	19	8	3
	systematic uncertainty (%)	18	9	5
	total uncertainty (%)	26	12	5

$B^+ \rightarrow \tau^+ \nu$ Prospects for Belle II

Two useful (for NP) ratios

$$\begin{split} R_{\rm ps} &= \frac{\tau_{B^0}}{\tau_{B^+}} \frac{\mathcal{B}(B^+ \to \tau^+ \nu)}{\mathcal{B}(B^0 \to \pi^- \ell^+ \nu)} \\ R_{\rm pl} &= \frac{\mathcal{B}(B^+ \to \tau^+ \nu)}{\mathcal{B}(B^+ \to \mu^+ \nu)} \end{split}$$

$$\begin{split} R_{\rm ps}^{\rm NP} &= (0.539 \pm 0.043) \big| 1 + r_{\rm NP}^{\tau} \big|^2 \,, \\ R_{\rm pl}^{\rm NP} &= \frac{m_\tau^2 \, (1 - m_\tau^2 / m_B^2)^2}{m_\mu^2 \, (1 - m_\mu^2 / m_B^2)^2} \big| 1 + r_{\rm NP}^{\tau} \big|^2 \simeq 222.37 \, \big| 1 + r_{\rm NP}^{\tau} \big|^2 \end{split}$$

Luminosity	$R_{ m ps}$	$R_{ m pl}$
$5{ m ab}^{-1}$	[-0.22, 0.20]	[-0.42, 0.29]
$50{ m ab^{-1}}$	[-0.11, 0.12]	[-0.12, 0.11]

Expected sensitivity @ 95% CL. Assumed: NP contribution is real and $|r_{\rm NP}^{\tau}|<1$

NP contributions to $B^+ \to \tau^+ \nu$ with $|r_{\rm NP}| > \mathcal{O}(0.1)$ can be tested at 95% CL.

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 $B^+ \rightarrow \mu^+ \nu$ Prospects for Belle II

▶ By scaling the FoM of Belle new untagged analysis (arXiv:1712.04123),

$$\mathcal{F}_{B2} = \mathcal{F}_{B1} imes \sqrt{50 \ ab^{-1}/0.711 \ ab^{-1}} \sim 14.5\%$$

corresponding to $\sim 7\%$ statistical precision

- naive expectation (Ref. B2TiP draft)
 - * $B^+ \rightarrow \mu^+ \nu$ can reach 5σ with $\sim 6 \text{ ab}^{-1}$
 - * 5% statistical precision, with full 50 ab^{-1}

$B^+ \rightarrow \ell^+ \nu$ Prospects beyond 50 ab⁻¹



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Concluding Remarks

- ► Leptonic *B* decays, in particular $B^+ \rightarrow \ell^+ \nu$ ($\ell = e, \mu, \tau$), provide powerful probe for new physics beyond the SM.
- ► $B^+ \rightarrow \tau^+ \nu$ decays have been measured at nearly 5σ significance, and new physics models such as 2HDM (II) have been tested.
- ▶ With hadronic *B*-tagging, Belle has searched for *invisible, massive, lepton-like neutral* particle X^0 in $B^+ \rightarrow \ell^+ X^0$ for the first time.
- ▶ Belle II with $\int \mathcal{L} dt = 50 \text{ ab}^{-1}$ branching fractions for both $B^+ \to \tau^+ \nu$ and $B^+ \to \mu^+ \nu$ are expected to be measured with precision of ~ 5%.



Thank you!