

**AUTOMATED NLO QCD+EW
CORRECTIONS AND THE
COMPLEX-MASS SCHEME**

WITHIN MG5_AMC

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IN COLLABORATION WITH

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MITP

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OUTLINE

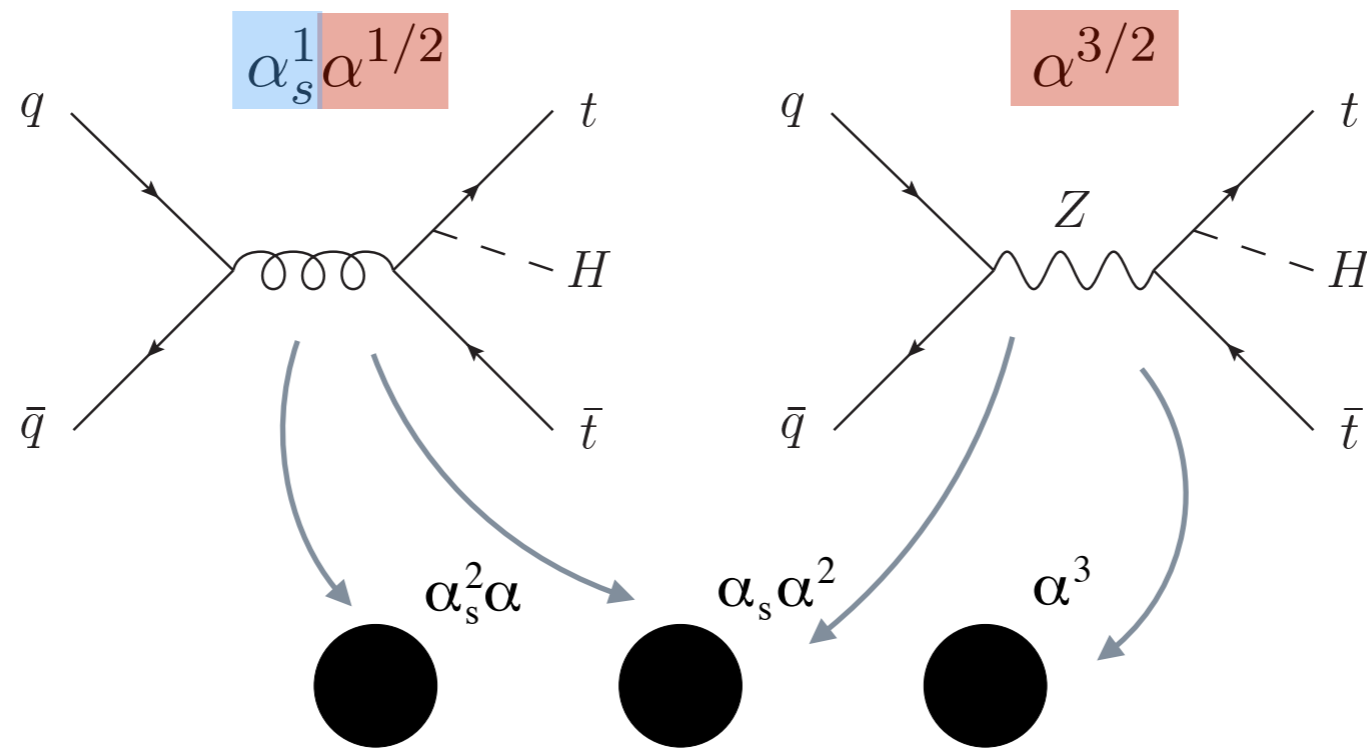
- NLO QCD+EW automating with MG5_aMC
 - ▶ Our **approach** to this problem
 - ▶ Some results and **sub-leading NLO EW** contributions
- Subtleties in the complex-mass (CM) scheme
 - ▶ Underlying **principles** of the CM renormalisation scheme
 - ▶ **Analytic continuation** of the two-point function
 - ▶ Implication of setting $|\alpha|$
 - ▶ Mixed scheme: **CM + On-Shell (OS)** renormalisation

MIXED NLO QCD+EW WITH MG5_AMC v3.0 BETA

[Frederix, Frixione, VH, Pagani, Shao '18]

GENERAL STRUCTURE OF NLO EW-QCD

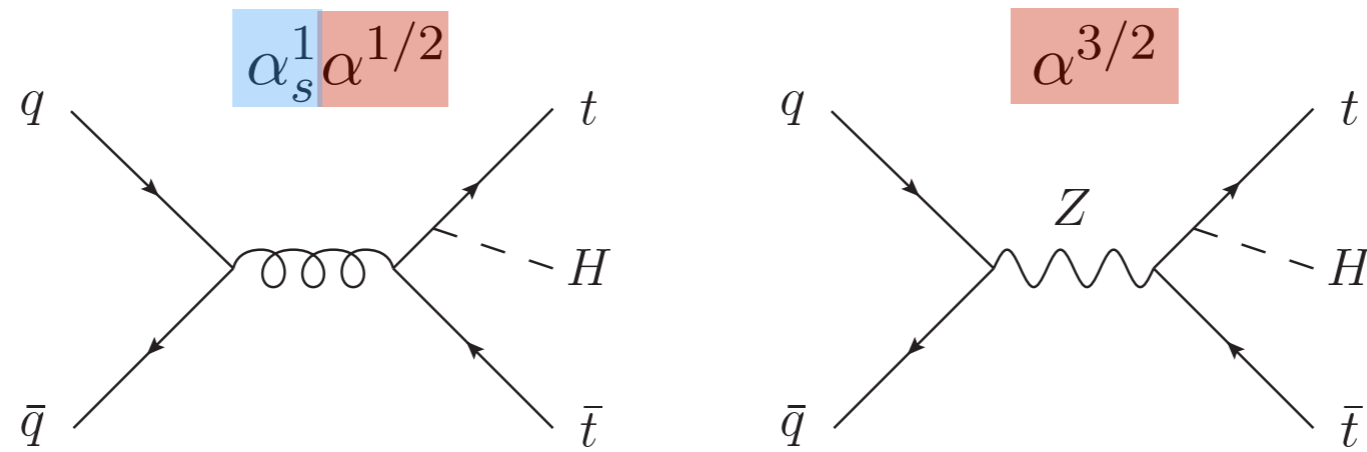
The ttH case: [Frixione, VH, Pagani, Shao, Zaro, '15]



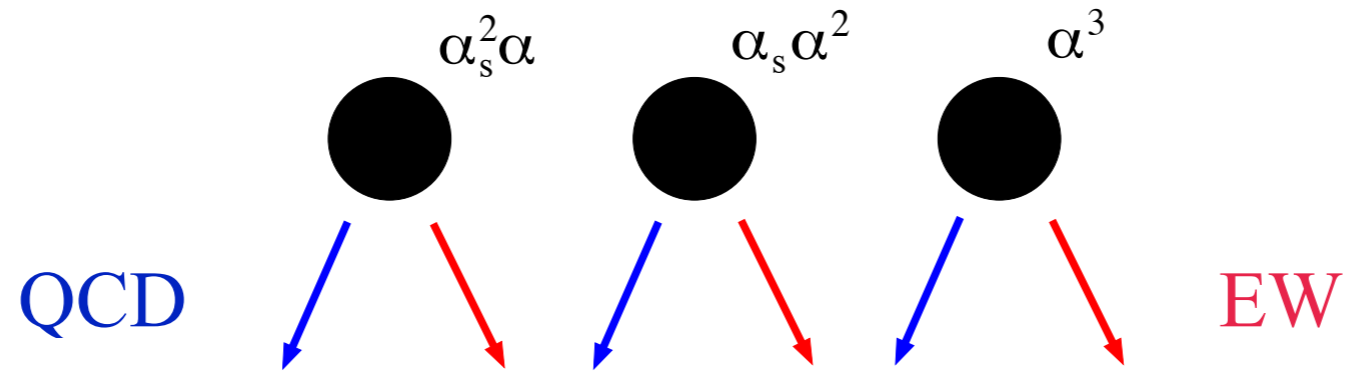
LO

STRUCTURE OF NLO EW-QCD CORRECTIONS

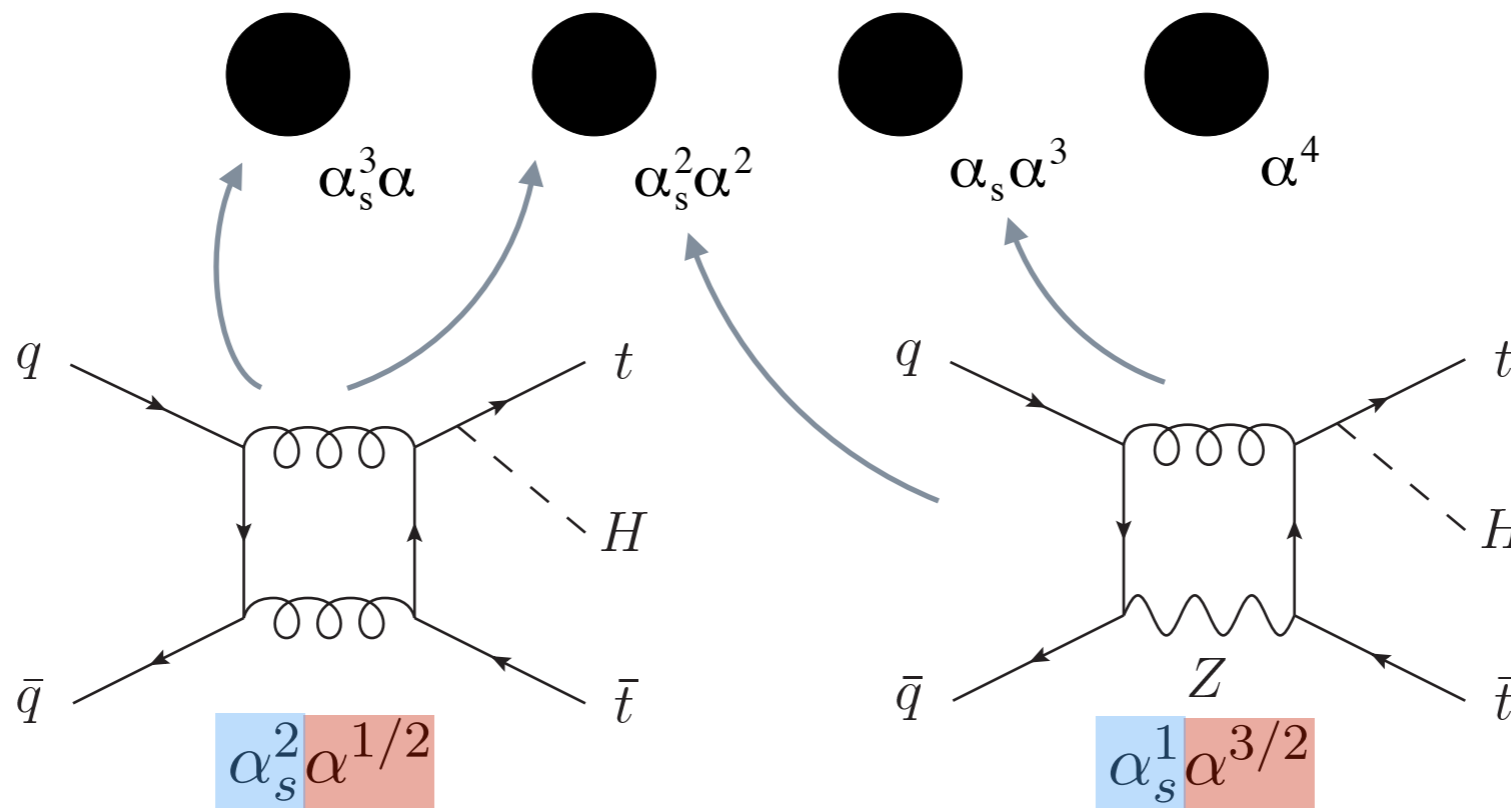
The $t\bar{t}H$ case: S.Frixione, V.Hirschi, D. Pagani, H.-S. Shao, M. Zaro [arXiv:1504.03446]



LO



NLO

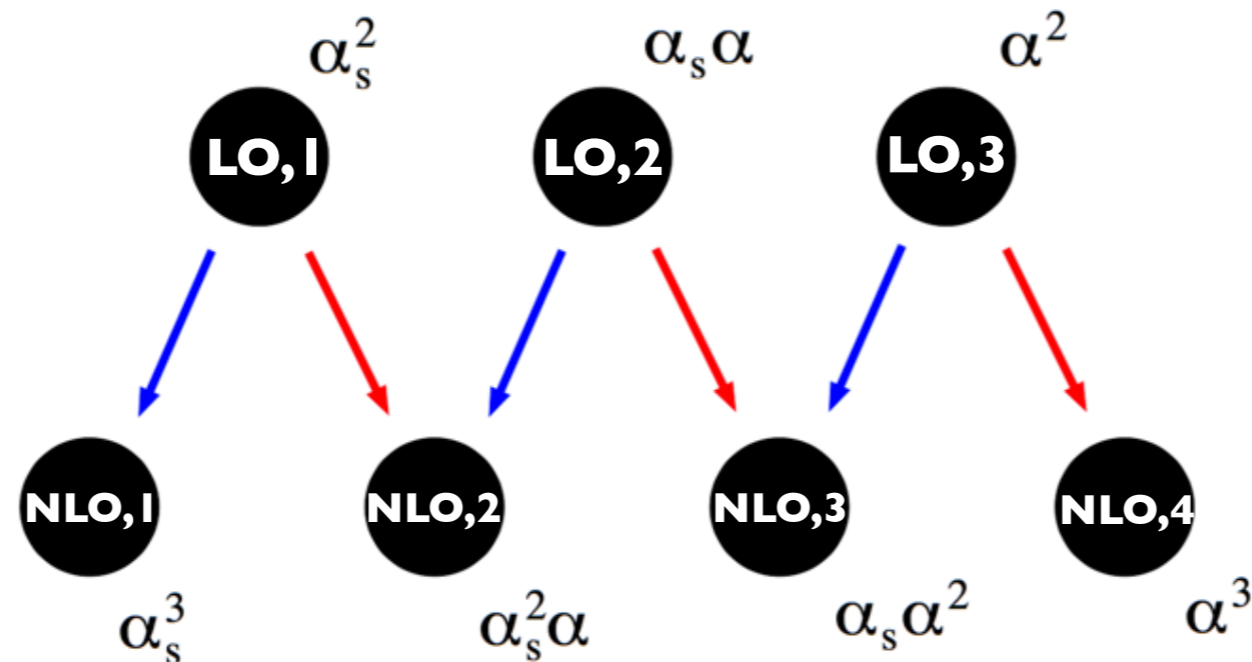


STRUCTURE OF NLO EW-QCD CORRECTIONS

Notation for an observable Σ

$$\begin{aligned}\Sigma^{(\text{LO})}(\alpha_s, \alpha) &= \alpha_s^2 \Sigma_{2,0} + \alpha_s \alpha \Sigma_{2,1} + \alpha^2 \Sigma_{2,2} \\ &\equiv \Sigma_{\text{LO},1} + \Sigma_{\text{LO},2} + \Sigma_{\text{LO},3} \\ \Sigma^{(\text{NLO})}(\alpha_s, \alpha) &= \alpha_s^3 \Sigma_{3,0} + \alpha_s^2 \alpha \Sigma_{3,1} + \alpha_s \alpha^2 \Sigma_{3,2} + \alpha^3 \Sigma_{3,3} \\ &\equiv \Sigma_{\text{NLO},1} + \Sigma_{\text{NLO},2} + \Sigma_{\text{NLO},3} + \Sigma_{\text{NLO},4}\end{aligned}$$

Usually, $\Sigma_{\text{NLO},1} = \text{NLO QCD}$, $\Sigma_{\text{NLO},2} = \text{NLO EW (weak+QED)}$



MADLOOP @ EW LOOPS

$$\sigma^{\text{NLO}} = \int_m d^{(d)} \sigma^V + \underbrace{\int_{m+1} d^{(d)} \sigma^R}_{\text{Real emission part}} + \int_m d^{(4)} \sigma^B$$

Virtual part
MadLoop

MadFKS

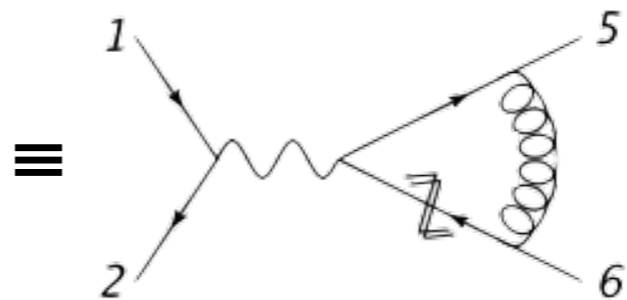
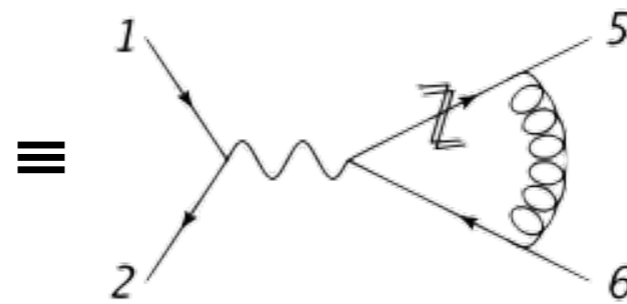
Born
Solved

- ▶ Hand-written dedicated **UFO Model** for **QCD+EW** corrections
- ▶ G_μ and $\alpha(M_Z^2)$ **renormalization scheme**, not $\alpha(0)$
- ▶ **Complex mass scheme** for handling unstable particle
- ▶ Work within the **Feynman gauge**, yielding **polynomial** numerators

MADLOOP @ EW LOOPS

- No external tool for loop diagram generation:
Reuse *MG5_aMC* efficient tree level diagram generation.
- Cut loops have **two extra** external particles

Trees ($e^+e^- \rightarrow u u\bar{u} u u\bar{u}$) \equiv Loops ($e^+e^- \rightarrow u u\bar{u}$)



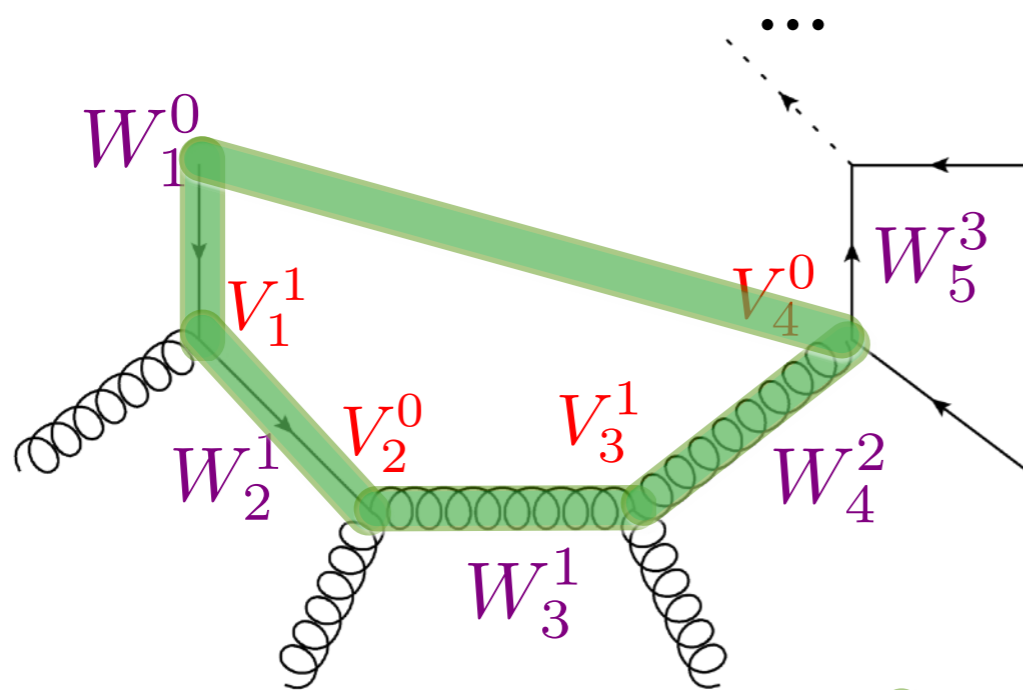
USING OPEN-LOOPS TECHNIQUE

[S. Pozzorini & al. hep-ph/1111.5206]

- Lite-Motive: Be **Numerical** where you can and **analytical** where you should.

$$\mathcal{N}(l^\mu) = \sum_{r=0}^{r_{max}} C_{\mu_0 \mu_1 \dots \mu_r}^{(r)} l^{\mu_0} l^{\mu_1} \dots l^{\mu_r}$$

- How to get these coefficients? (Wavefunction and 4-momenta indices now omitted)



$$W_j^{(r)} = \sum_{i=0}^r w_j^i l^i \quad V_j^{(r=0,1)} = \sum_{i=0}^r v_j^i l^i$$

$$W_1^{(0)} = w_1^0 = 1$$

$$W_2^{(1)} = (v_1^1 l + v_1^0) w_1^0$$

$$W_3^{(1)} = v_2^0 W_2^{(1)} = v_2^0 (v_1^1 l + v_1^0) w_1^0$$

$$W_4^{(1)} = V_3^{(1)} W_2^{(1)} = (v_3^1 l + v_3^0) v_2^0 (v_1^1 l + v_1^0) w_1^0$$

... or end of loop and $C^{(2)} = v_3^1 v_2^0 v_1^1 w_1^0, C^{(1)} = v_2^0 w_1^0 (v_3^1 v_1^0 + v_3^0 v_1^1), C^0 = \dots$

REDUCTION

▶ OPP integrand-level:

CUTTOOLS G.Ossola, C.G.Papadopoulos, R.Pittau [[arXiv:0711.3596](#)]

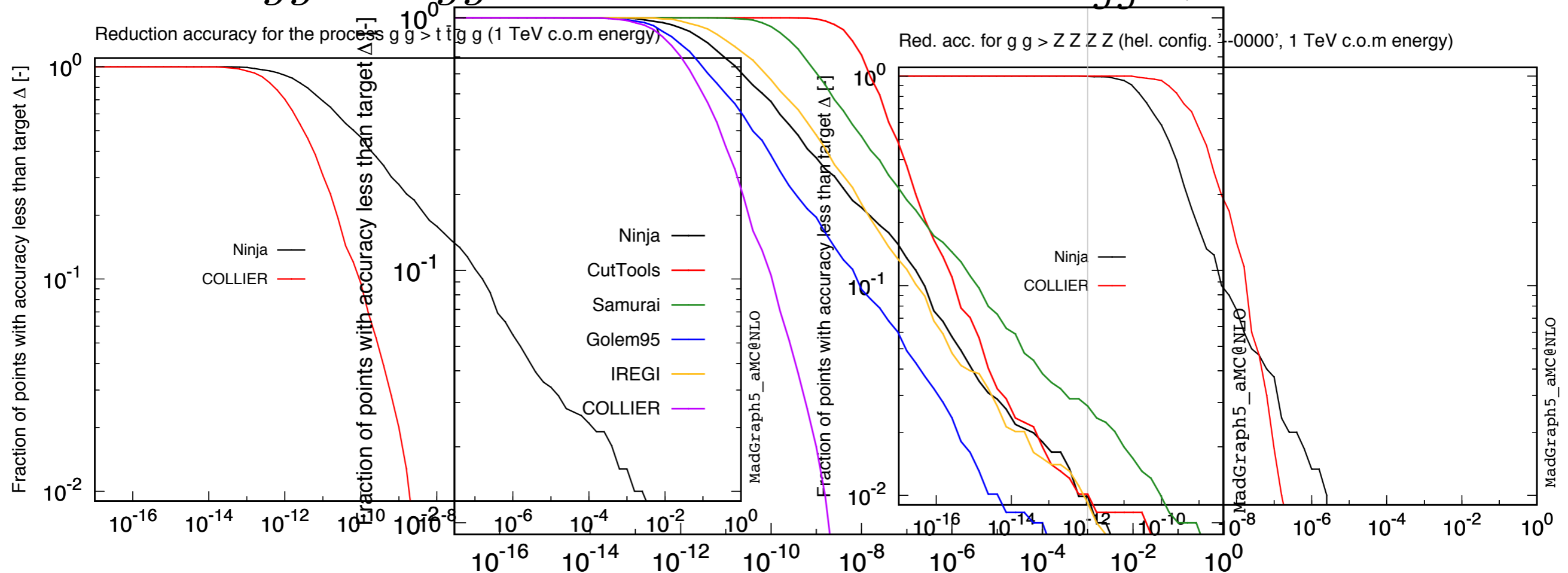
NINJA T.Peraro [[arXiv:1403.1229](#)], V.H., T.Peraro [[arXiv:1604.01363](#)]

▶ Tensor Integral Reduction:

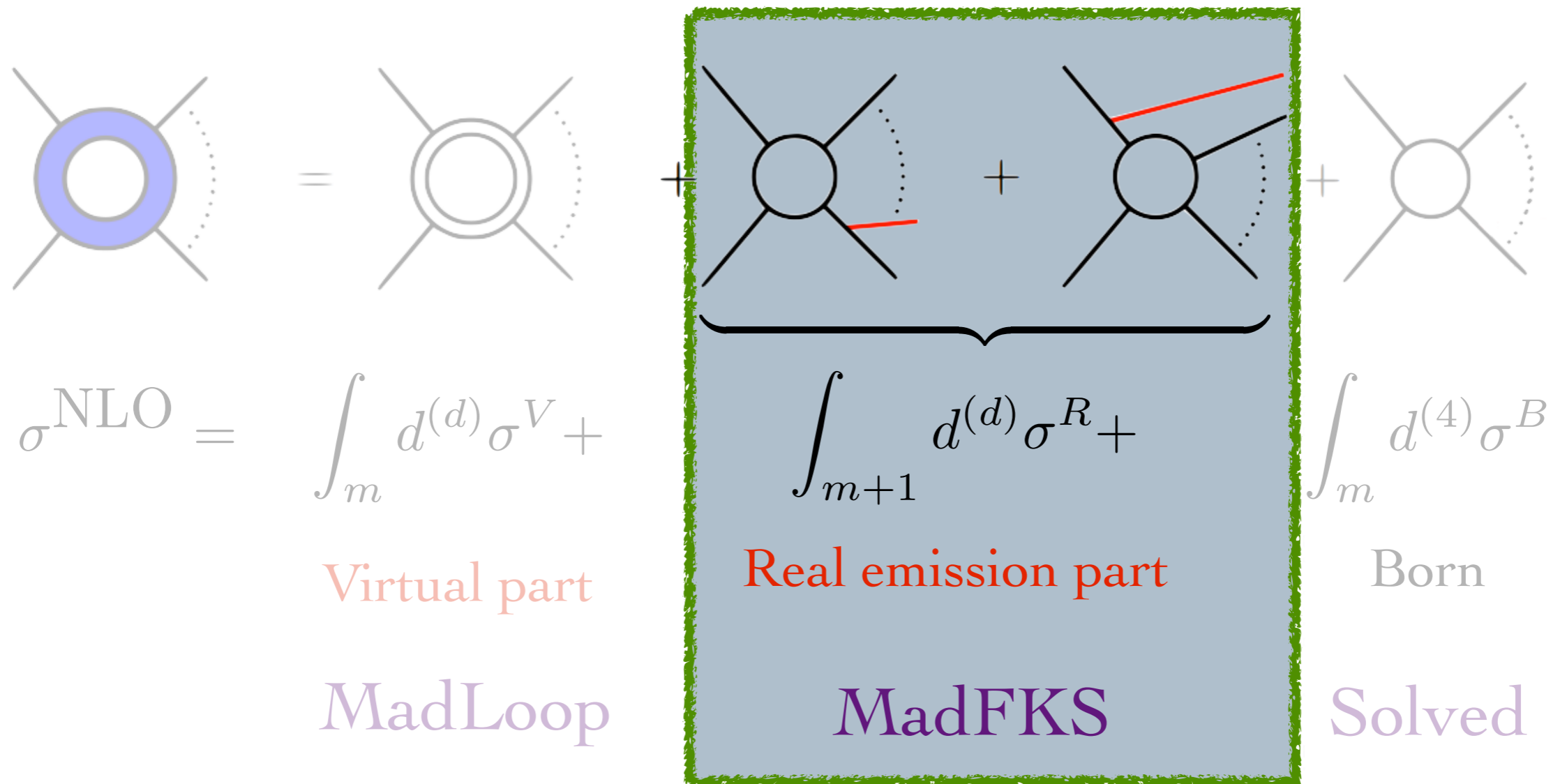
COLLIER A. Denner, D. Dittmaier, L. Hofer [[arXiv:1604.06792](#)]

▶ Alternatives: IREGI, GOLEM95, PJFRY++, SAMURAI

$gg \rightarrow t\bar{t}gg$ Reduction accuracy for the process $gg \rightarrow t\bar{t}gg$ (1 TeV c.o.m energy) $gg \rightarrow ZZZZ$



MADFKS: QED SUBTRACTION



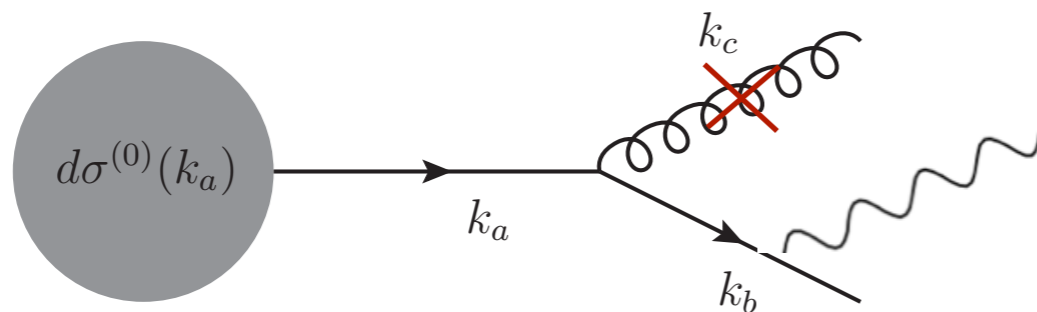
FULL NLO EW-QCD CORRECTIONS

[Frederix, Frixione, VH, Pagani, Shao '18]

- ▶ Improved **MadFKS** to subtract **QED** singularities



Isn't that just a **trivial modification** of the **counterterms**?



$$k_b = zk_a + k_T + \beta_b \hat{n}$$

$$k_c = (1 - z)k_a - k_T + \beta_c \hat{n}$$

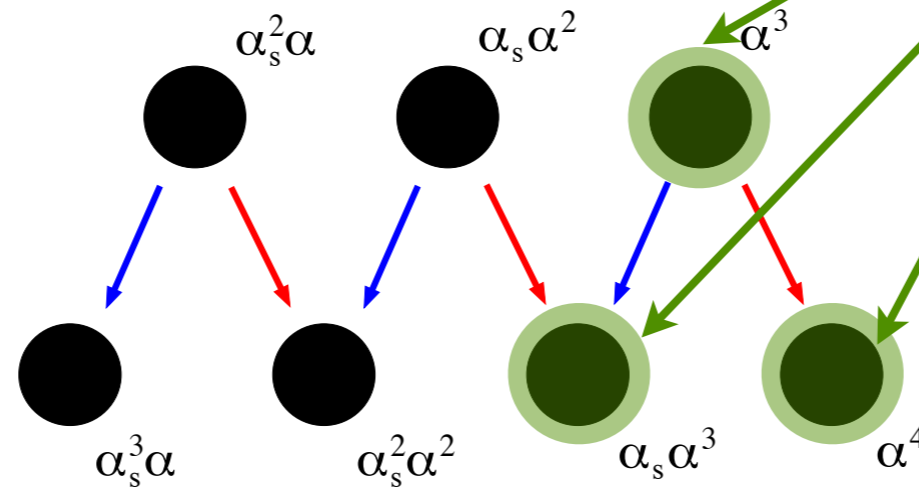
$$d\sigma^{(1,R)} = \frac{\alpha}{2\pi} \int dk_T^2 \int_0^1 dz \frac{Q_f}{C_F} \frac{1+z^2}{1-z} \frac{1}{k_T^2} d\sigma^{(0)}(k_a) + \mathcal{R}$$

For ttH/V **mostly yes...** but jets complicate things

FULL NLO EW-QCD CORRECTIONS

S.Frixione, V.H, D. Pagani, H.-S. Shao, M. Zaro [arXiv:1504.03446]

- ▶ We can compute **all** NLO contribs, incl. **subleading corrections**

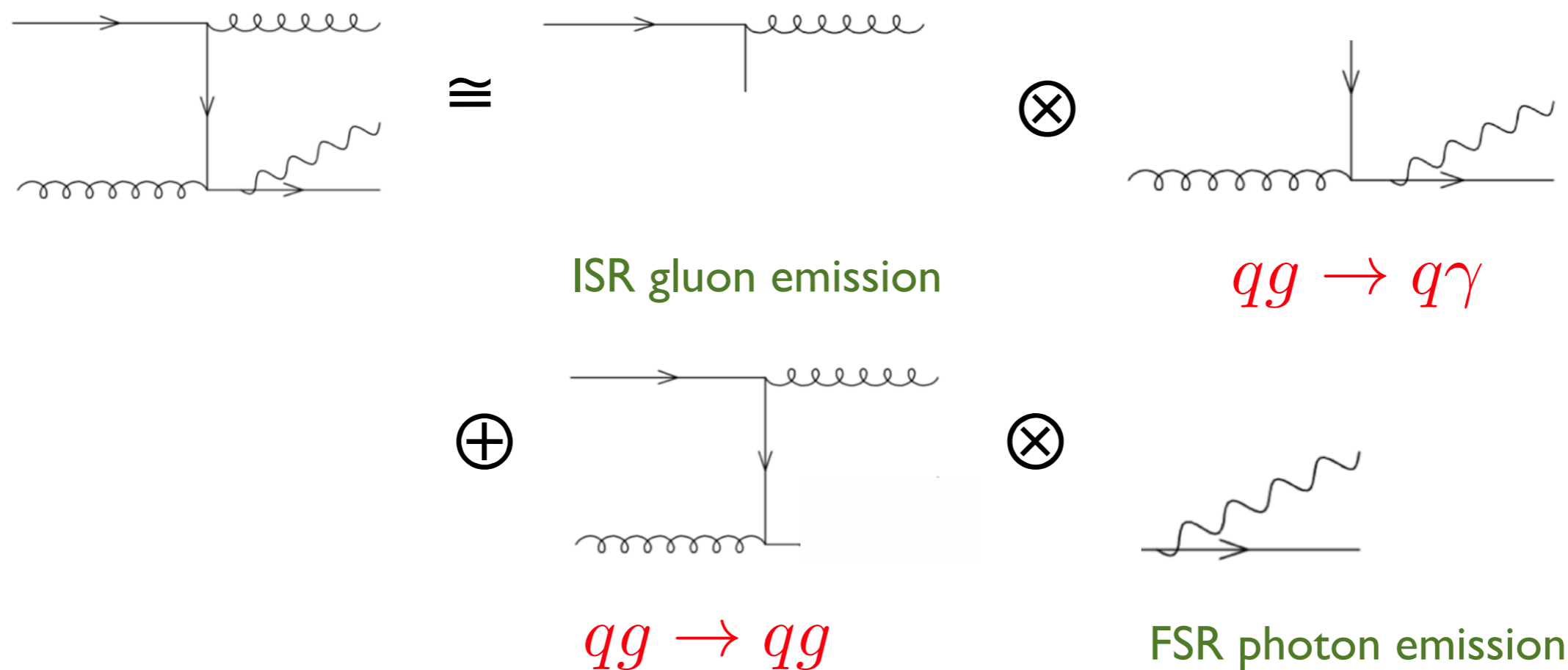


- ▶ Attack **dijet** so as to address most **remaining difficulties at once**

ALL DIJET NLO EW-QCD CORRECTIONS

S.Frixione, V.H, D. Pagani, H.-S. Shao, M. Zaro [arXiv:1504.03446]

- ▶ QCD still requires **soft/collinear gluon** limit to be **regular**



- ▶ More **book-keeping** → **requires full automation**
- ▶ Must include **both gluons** and **photons** in **jets** → **democratic jet clustering**
- ▶ Need to define **hadronic jet** → **requires IR-safe definition of photon jets**

ALL NLO EW-QCD CORRECTIONS

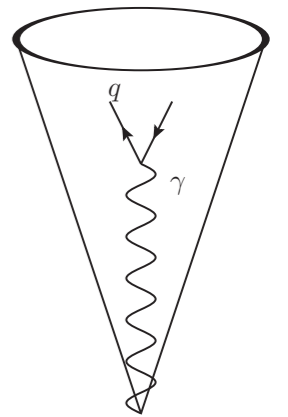
S.Frixione, V.H, D. Pagani, H.-S. Shao, M. Zaro [arXiv:1504.03446]

► Issues with democratic jets:

Experimentalist typically do not consider photon-jets as jets

Solution: cluster democratically, but discard jets where $E_\gamma > z_{cut} E_{jet}$

However: E_γ is not a well-defined quantity in pQED ($\gamma \rightarrow q\bar{q}$)

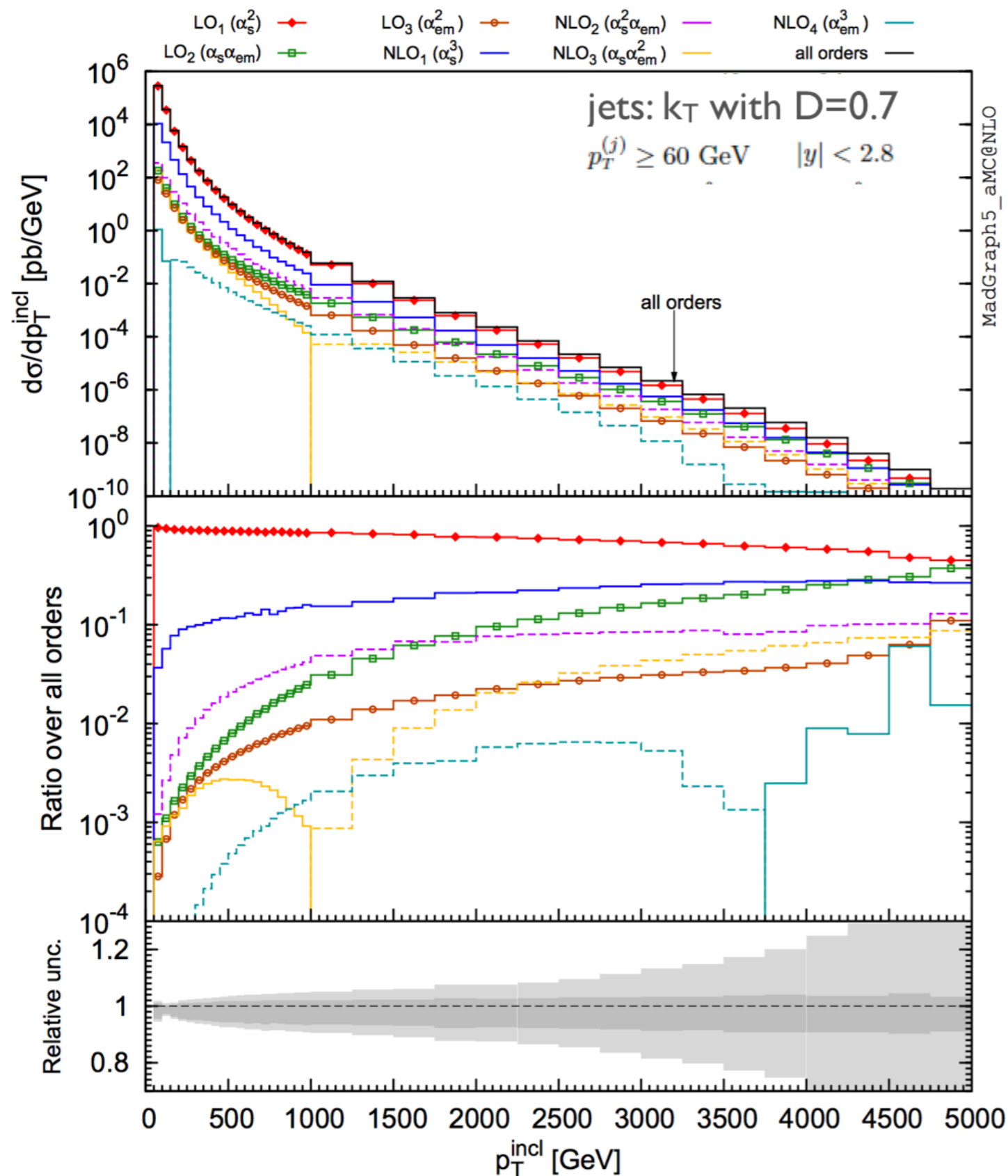


This is a problem only at $\Sigma_{\text{NLO},3}$ and beyond (at least two EW couplings are needed): in principle it can be ignored at NLO EW.

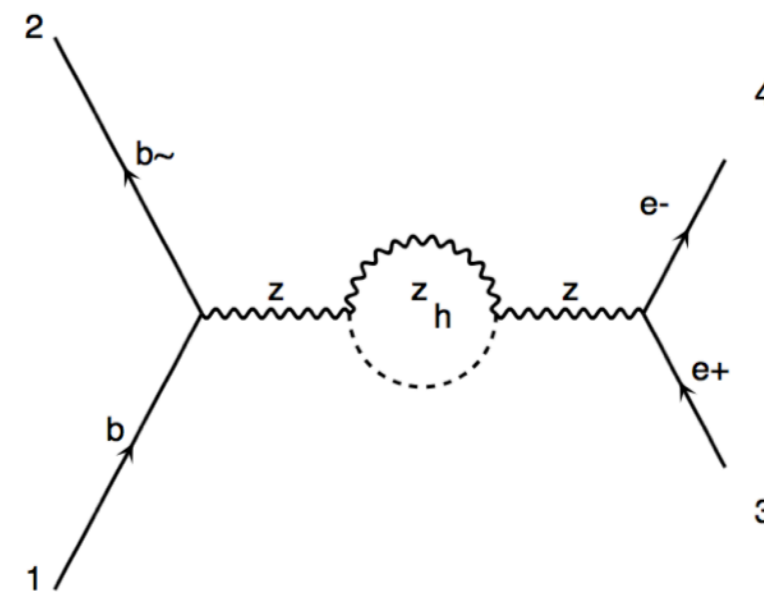
When not using the $\alpha(0)$ scheme, the use of **fragmentation functions** to **define taggable short-distance** photon offers a general solution.

COMPLETE DIJET QCD+EW NLO CORRECTIONS

R. Frederix, S. Frixione, V. H., D. Pagani, H-S. Shao, M. Zaro [arXiv:1612.06548]



- All $\mathcal{O}(\alpha_s^m, \alpha^n)$, $m + n = 2, 3$ contributions to dijet. Use G_μ scheme
- Necessitated large computing resources, 219 subprocesses
- This process involves the whole particle spectrum of the SM. Yes, even the Higgs.



COMPLETE NLO QCD+EW AUTOMATION

[Frederix, Frixione, VH, Pagani, Shao '18]

Current syntax (leading terms, i.e. NLO QCD)

```
MG5_aMC> generate a b > c d e f [QCD]
```

Will become (or something similar):

```
MG5_aMC> generate a b > c d e f QCD=n QED=m [QCD QED]
```

in order to include in the computation all the terms that factorise:

$$\text{LO} \quad \alpha_s^k \alpha^p, \quad k \leq n, \quad p \leq m, \quad k + p = b$$

$$\text{NLO} \quad \alpha_s^k \alpha^p, \quad k \leq n+1, \quad p \leq m+1, \quad k + p = b + 1$$

then

```
MG5_aMC> output
```

```
MG5_aMC> launch NLO
```

COMPLETE NLO QCD+EW **AUTOMATION**

[Frederix, Frixione, VH, Pagani, Shao '18]

► **Subleading EW corrections can matter.**

| | $pp \rightarrow t\bar{t}$ | $pp \rightarrow t\bar{t}Z$ | $pp \rightarrow t\bar{t}W^+$ | $pp \rightarrow t\bar{t}H$ | $pp \rightarrow t\bar{t}j$ |
|------------------|-----------------------------------|--------------------------------------|--------------------------------------|--------------------------------------|-----------------------------------|
| LO ₁ | $4.3803 \pm 0.0005 \cdot 10^2$ pb | $5.0463 \pm 0.0003 \cdot 10^{-1}$ pb | $2.4116 \pm 0.0001 \cdot 10^{-1}$ pb | $3.4483 \pm 0.0003 \cdot 10^{-1}$ pb | $3.0278 \pm 0.0003 \cdot 10^2$ pb |
| LO ₂ | $+0.405 \pm 0.001$ % | -0.691 ± 0.001 % | $+0.000 \pm 0.000$ % | $+0.406 \pm 0.001$ % | $+0.525 \pm 0.001$ % |
| LO ₃ | $+0.630 \pm 0.001$ % | $+2.259 \pm 0.001$ % | $+0.962 \pm 0.000$ % | $+0.702 \pm 0.001$ % | $+1.208 \pm 0.001$ % |
| LO ₄ | | | | | $+0.006 \pm 0.000$ % |
| NLO ₁ | $+46.164 \pm 0.022$ % | $+44.809 \pm 0.028$ % | $+49.504 \pm 0.015$ % | $+28.847 \pm 0.020$ % | $+26.571 \pm 0.063$ % |
| NLO ₂ | -1.075 ± 0.003 % | -0.846 ± 0.004 % | -4.541 ± 0.003 % | $+1.794 \pm 0.005$ % | -1.971 ± 0.022 % |
| NLO ₃ | $+0.552 \pm 0.002$ % | $+0.845 \pm 0.003$ % | $+12.242 \pm 0.014$ % | $+0.483 \pm 0.008$ % | $+0.292 \pm 0.007$ % |
| NLO ₄ | $+0.005 \pm 0.000$ % | -0.082 ± 0.000 % | $+0.017 \pm 0.003$ % | $+0.044 \pm 0.000$ % | $+0.009 \pm 0.000$ % |
| NLO ₅ | | | | | $+0.005 \pm 0.000$ % |

(Monte-Carlo statistical error reported in the above chart)

COMPLEX MASS SCHEME

A. Denner, S.Dittmaier, M.Roth, L.Wieder [[hep-ph/9904472](#) , [hep-ph/0505042](#)]

COMPLEX MASS SCHEME

A. Denner, S.Dittmaier, M.Roth, L.Wieder [hep-ph/9904472 , hep-ph/0505042]

- ▶ **Complex mass scheme** to handle **unstable particle resonances**

$$i \frac{\not{p} + \bar{M}}{p^2 - \bar{M}^2 + i\Gamma\bar{M}} \xrightarrow{m_{cms} \equiv \sqrt{\bar{M}^2 - i\Gamma\bar{M}}} i \frac{\not{p} + m_{cms}}{p^2 - m_{cms}^2}$$

- ▶ The **CM** scheme is a modification of the **OS** scheme.

$$\Sigma_R(p^2) = \Sigma_U(p^2) - \delta M^2 + (p^2 - M^2)\delta Z$$

$$\Re [\Sigma_R(p^2)] \Big|_{p^2=M^2} = 0,$$

$$\lim_{p^2 \rightarrow M^2} \frac{1}{p^2 - M^2} \Re [\Sigma_R(p^2)] = 1,$$

$$\Re [\Sigma_R(p^2 = M^2)] = 0 \quad \Longrightarrow \quad \delta M^2 = \Re [\Sigma_U(p^2 = M^2)]$$

$$\Re [\Sigma'_R(p^2 = M^2)] = 0 \quad \Longrightarrow \quad \delta Z = -\Re [\Sigma'_U(p^2 = M^2)]$$

OS scheme

COMPLEX MASS SCHEME

A. Denner, S.Dittmaier, M.Roth, L.Wieder [hep-ph/9904472 , hep-ph/0505042]

CM scheme

$$\bar{M}^2 - i\bar{\Gamma}\bar{M} \equiv m^2 = M_0^2 - \delta m^2$$

$$\Sigma_R(p^2) = \Sigma_U(p^2) - \delta m^2 + (p^2 - m^2)\delta z$$

$$\Sigma_R(p^2 = \bar{M}^2 - i\bar{\Gamma}\bar{M}) = 0 \quad \Longrightarrow \quad \delta m^2 = \Sigma_U(p^2 = \bar{M}^2 - i\bar{\Gamma}\bar{M})$$

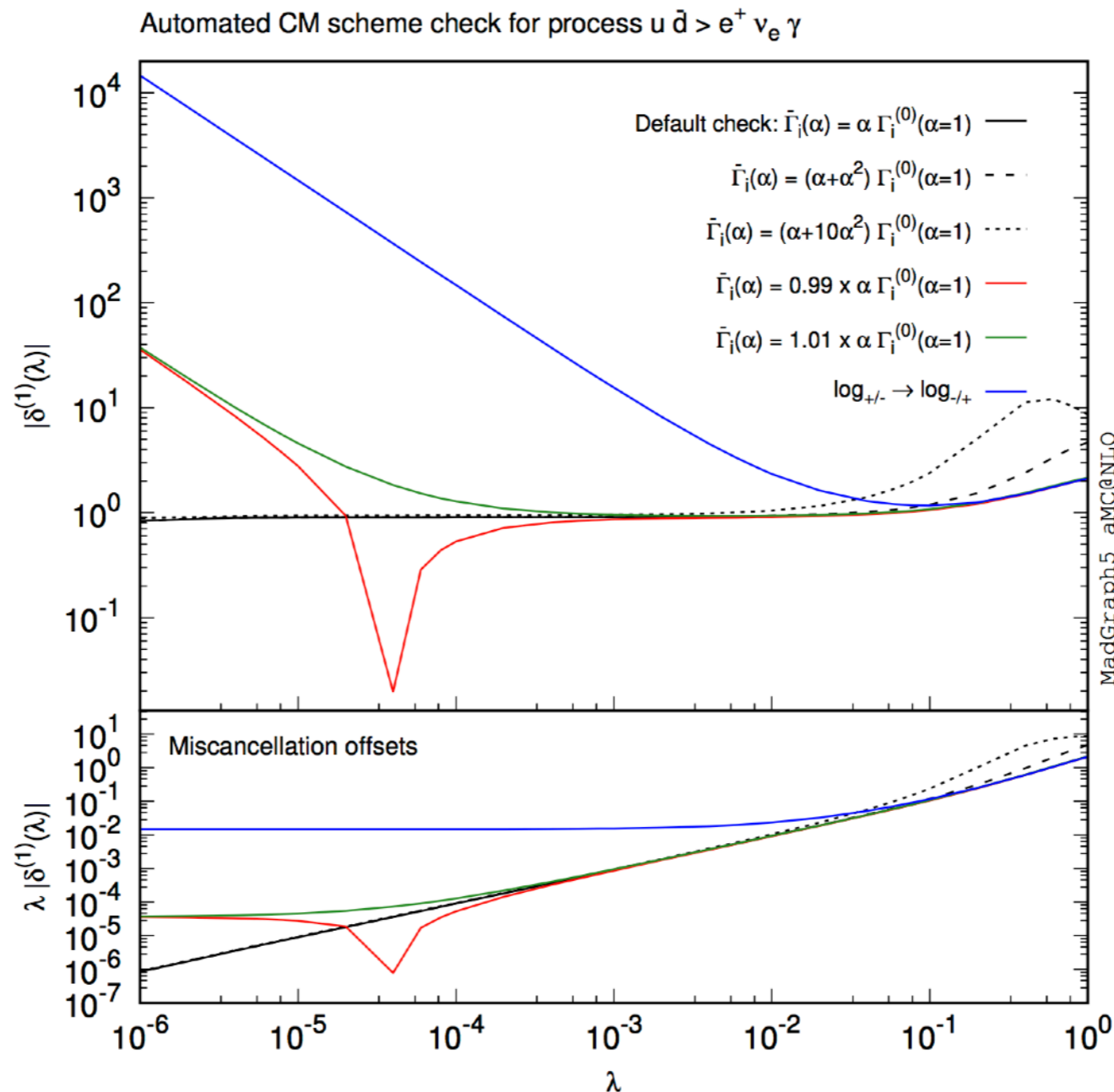
$$\Sigma'_R(p^2 = \bar{M}^2 - i\bar{\Gamma}\bar{M}) = 0 \quad \Longrightarrow \quad \delta z = -\Sigma'_U(p^2 = \bar{M}^2 - i\bar{\Gamma}\bar{M})$$

$$\Im[m^2] = -\bar{\Gamma}\bar{M} = -\Im[\delta m^2] = -\Im[\Sigma_U(p^2 = \bar{M}^2 - i\bar{\Gamma}\bar{M})]$$

► The **CM** scheme re-organises the perturbative expansion:

$$\begin{aligned} (m^2 + \delta m^2) - (M^2 + \delta M^2) &= \\ &= \left(\bar{M}^2 - i\bar{\Gamma}\bar{M} + \Sigma_U(p^2 = \bar{M}^2 - i\bar{\Gamma}\bar{M}) \right) - \left(M^2 + \Re [\Sigma_U(p^2 = M^2)] \right) = \\ &= \left(\bar{M}^2 - M^2 \right) + \left(\Sigma_U(p^2 = \bar{M}^2 - i\bar{\Gamma}\bar{M}) - i\bar{\Gamma}\bar{M} - \Re [\Sigma_U(p^2 = M^2)] \right) \\ &\stackrel{\text{NLO}}{=} \mathcal{O}(\alpha^2). \end{aligned}$$

TESTING THE COMPLEX MASS SCHEME



$$\Delta^{(0)} = \lim_{\lambda \rightarrow 0} \left(\frac{\mathcal{M}_{\text{CM}}^{(0)} - \mathcal{M}_{\text{ZW}}^{(0)}}{\lambda \mathcal{M}_{\text{ZW}}^{(0)}} \Big|_{\alpha = \lambda \alpha^{\text{ref}}} \right) \equiv \lim_{\lambda \rightarrow 0} \delta^{(0)}(\lambda)$$

$$\Delta^{(1)} = \lim_{\lambda \rightarrow 0} \left(\frac{\mathcal{M}_{\text{CM}}^{(1)} + \mathcal{M}_{\text{CM}}^{(0)} - \mathcal{M}_{\text{ZW}}^{(1)} - \mathcal{M}_{\text{ZW}}^{(0)}}{\lambda^2 \mathcal{M}_{\text{ZW}}^{(0)}} \Big|_{\alpha = \lambda \alpha^{\text{ref}}} \right) \equiv \lim_{\lambda \rightarrow 0} \delta^{(1)}(\lambda)$$

$$\mathcal{M}_{\text{ZW}}^{(L)}(\{p_k\}) = \mathcal{M}_{\text{OS}}^{(L)}(\{p_k\}) \Big|_{\{\Gamma_r=0\}}$$

ANALYTIC CONTINUATION OF THE BUBBLE

▶ Example: $\Sigma_{U,T}^{\gamma W}(\bar{M}_W^2 - i\bar{\Gamma}_W \bar{M}_W) \supset B_0(p^2, 0, \bar{M}_W^2 - i\bar{\Gamma}_W \bar{M}_W) \Big|_{p^2 \rightarrow \bar{M}_W^2 - i\bar{\Gamma}_W \bar{M}_W}$

▶ **Exact result:**

$$\frac{1}{i\pi^2} B_0(p^2, 0, \bar{M}_W^2 - i\bar{\Gamma}_W \bar{M}_W) \Big|_{p^2 \rightarrow \bar{M}_W^2 - i\bar{\Gamma}_W \bar{M}_W} = \frac{1}{\epsilon} + 2 + \log \frac{\mu^2}{\bar{M}_W^2 - i\bar{\Gamma}_W \bar{M}_W}$$

▶ The **Taylor expansion** is not correct in this case:

$$\begin{aligned} \rightarrow B_0(p^2, 0, \bar{M}_W^2 - i\bar{\Gamma}_W \bar{M}_W) &= B_0(\bar{M}_W^2, 0, \bar{M}_W^2 - i\bar{\Gamma}_W \bar{M}_W) \\ &+ \left(\frac{p^2 - \bar{M}_W^2}{\bar{M}_W^2} \right) B_0'(\bar{M}_W^2, 0, \bar{M}_W^2 - i\bar{\Gamma}_W \bar{M}_W) + \mathcal{O}\left(\left(\frac{p^2 - \bar{M}_W^2}{\bar{M}_W^2} \right)^2 \right) \end{aligned}$$

Taylor lead to ($p^2 \rightarrow \bar{M}_W^2 - i\bar{\Gamma}_W \bar{M}_W$):

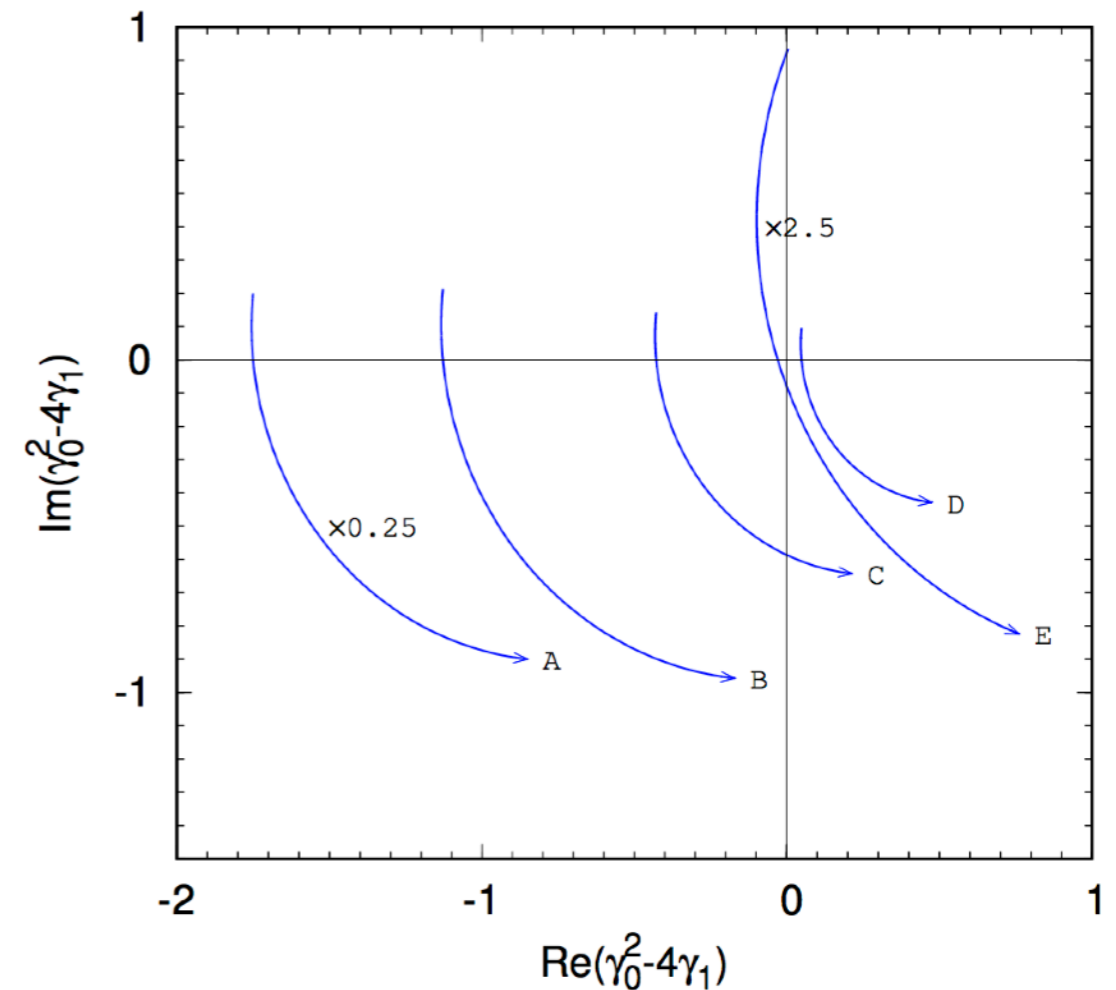
$$\rightarrow \Sigma_{U,T}^{\gamma W}(\bar{M}_W^2 - i\bar{\Gamma}_W \bar{M}_W) - \Sigma_{U,T}^{\gamma W,(1)}(\bar{M}_W^2 - i\bar{\Gamma}_W \bar{M}_W) = \boxed{\frac{\pi^2 \bar{\Gamma}_W}{\bar{M}_W}} + \mathcal{O}\left(\left(\frac{\bar{\Gamma}_W}{\bar{M}_W} \right)^2 \right)$$

ANALYTIC CONTINUATION: GENERAL CASE

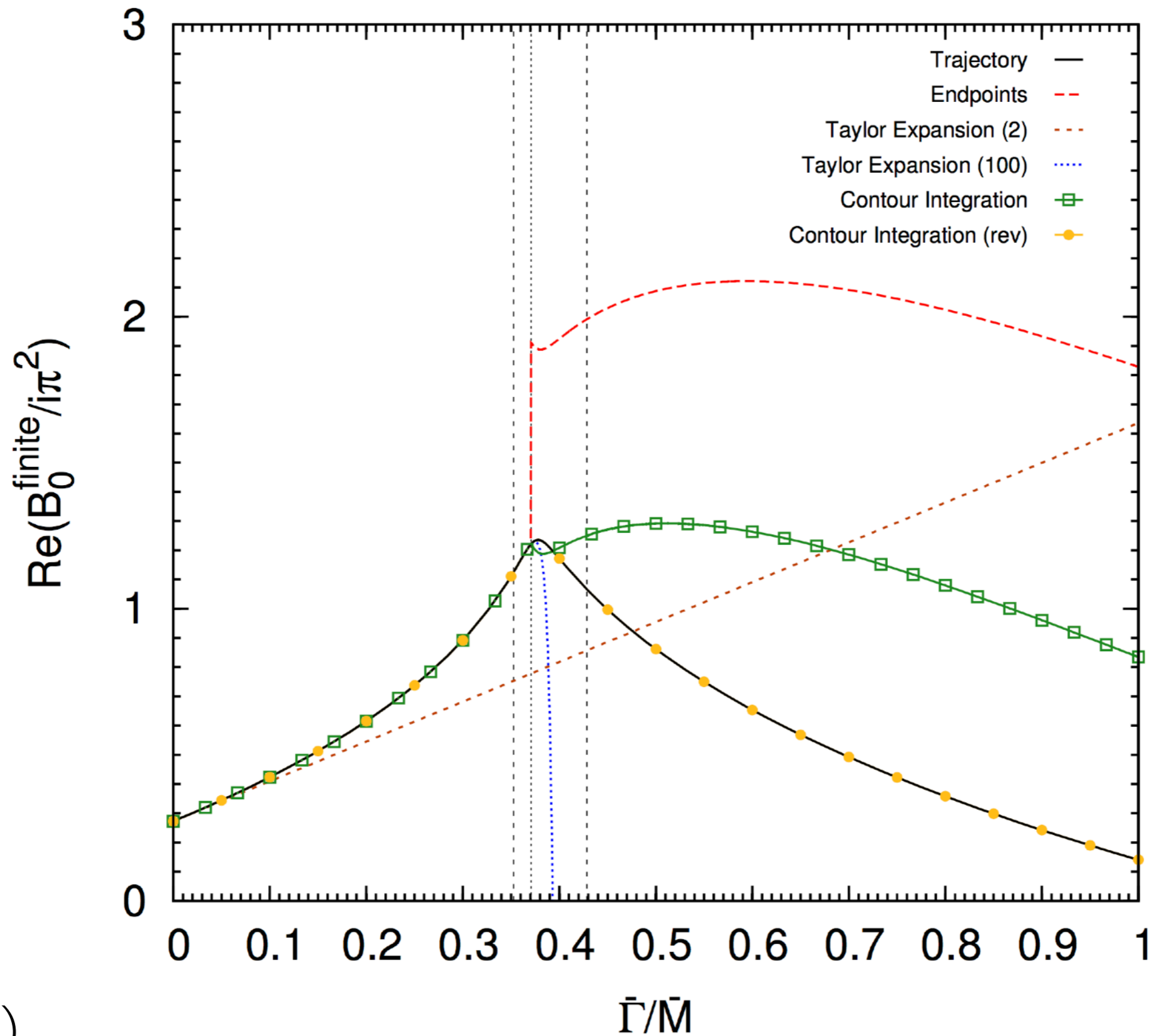
$$\frac{1}{i\pi^2} B_0(p^2, \mu_1^2, \mu_2^2) = \frac{1}{\epsilon} + 2 - \log \frac{p^2 - i0}{\mu^2} + \sum_{i=\pm} \left[\gamma_i \log \frac{\gamma_i - 1}{\gamma_i} - \log(\gamma_i - 1) \right]$$

$$\gamma_{\pm} = \frac{1}{2} \left(\gamma_0 \pm \sqrt{\gamma_0^2 - 4\gamma_1} \right), \quad \gamma_0 = 1 + \frac{\mu_1^2}{p^2} - \frac{\mu_2^2}{p^2}, \quad \gamma_1 = \frac{\mu_1^2}{p^2} - \frac{i0}{p^2}$$

| | \bar{M}^2/\bar{M}_1^2 | \bar{M}_2^2/\bar{M}_1^2 | $\bar{\Gamma}_1/\bar{M}_1$ | $\bar{\Gamma}_2/\bar{M}_2$ |
|---|-------------------------|---------------------------|----------------------------|----------------------------|
| A | 0.5 | 1 | 0.1 | 0.1 |
| B | 1.88 | 1 | 0.1 | 0.1 |
| C | 2.8 | 1 | 0.1 | 0.1 |
| D | 4.2 | 1 | 0.1 | 0.1 |
| E | 5.9 | 2 | 0.8 | 0.1 |



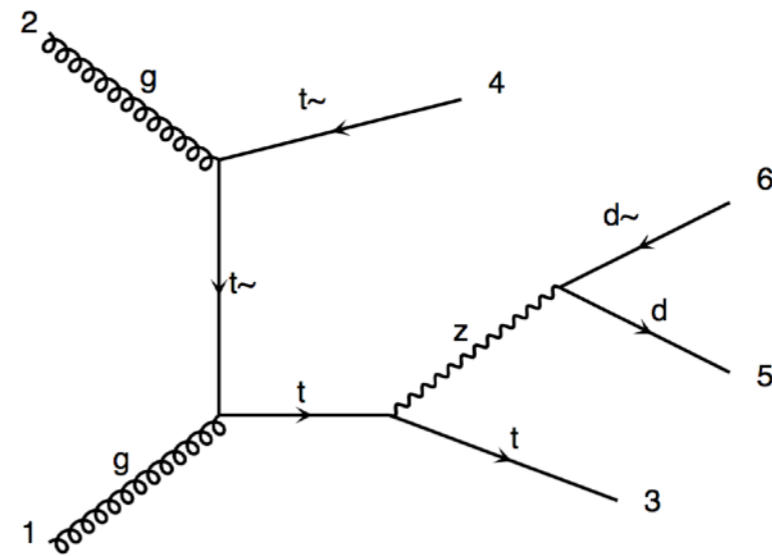
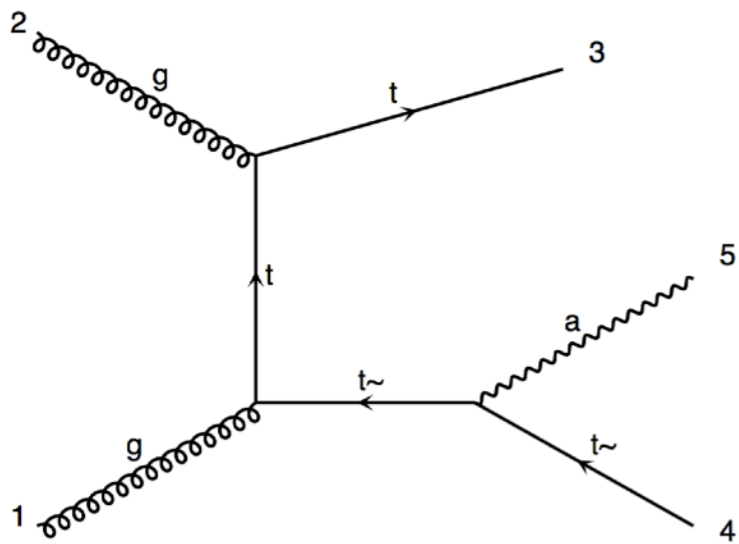
ANALYTIC CONTINUATION: GENERAL CASE



Config. E)

MIXED OS AND CM SCHEME

- ▶ One cannot handle a process like $pp \rightarrow Ze^+e^-$
- ▶ But what about $pp \rightarrow t\bar{t}j$?



- ▶ Can one set $\Gamma_{Z/W} \neq 0$ and $\Gamma_t = 0$? Yes, but care is needed:

MIXED OS AND CM SCHEME

- ▶ One must carefully remove the absorptive part only:

$$\delta Z_t^{L/R} \supset \delta_{(W^+,b)} Z_t^{L/R} = -\tilde{\mathfrak{R}} \left[\Sigma_{(W^+,b)}^{t,L/R}(M_t^2) \right] - M_t \frac{\partial}{\partial p^2} \tilde{\mathfrak{R}} \left[\Sigma_{(W^+,b)}^{t,R}(p^2) + \Sigma_{(W^+,b)}^{t,R}(p^2) + 2\Sigma_{(W^+,b)}^{t,S}(p^2) \right] \Big|_{p^2=M_t^2}$$

$$\Sigma_{(W^+,b)}^{t,S}(p^2) = 0,$$

$$\Sigma_{(W^+,b)}^{t,L}(p^2) = \frac{\alpha}{2\pi} \frac{1}{s_W^2} \left[\frac{1}{4} \frac{1}{\epsilon_{UV}} + \kappa_{\mathfrak{R},\text{fin}}^L(p^2) + i\kappa_{\mathfrak{S},\text{fin}}^L(p^2) \right],$$

$$\Sigma_{(W^+,b)}^{t,R}(p^2) = \frac{\alpha}{2\pi} \frac{M_t^2}{m_W^2 s_W^2} \left[\frac{1}{8} \frac{1}{\epsilon_{UV}} + \kappa_{\mathfrak{R},\text{fin}}^R(p^2) + i\kappa_{\mathfrak{S},\text{fin}}^R(p^2) \right],$$

- ▶ Anti-top wf renormalisation not obtained by complex conjugation!

$$\delta Z_{\bar{t}}^{L/R} \neq \delta Z_t^{L/R*}$$

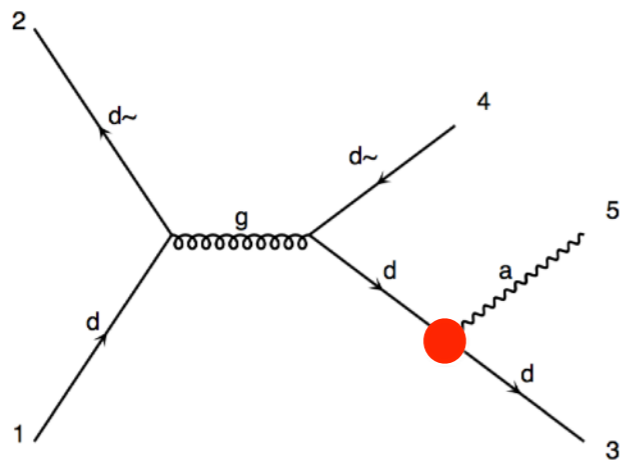
HOW TO HANDLE THE COMPLEX PHASE OF α ?

- ▶ In the G_μ -scheme for example, α is defined as:

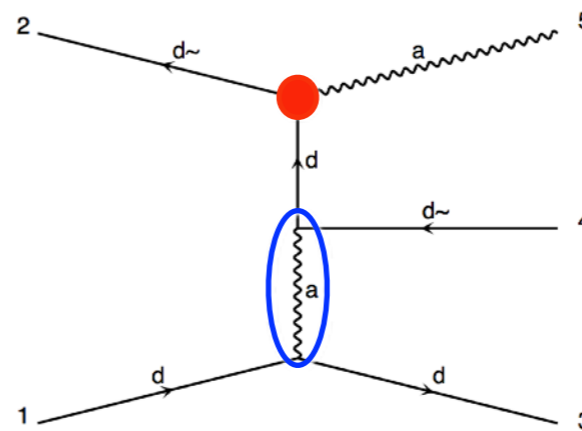
$$\alpha^{(CMS, G_\mu)} = \frac{\sqrt{2}G_f M_W^{(CMS)2} (M_Z^{(CMS)2} - M_W^{(CMS)2})}{\pi M_Z^{(CMS)2}} \longrightarrow \text{Should be complex!}$$

- ▶ In practice the complex phase is often irrelevant because the matrix elements factorize $|\alpha|$. But, in subleading blobs, one can have:

Reals:



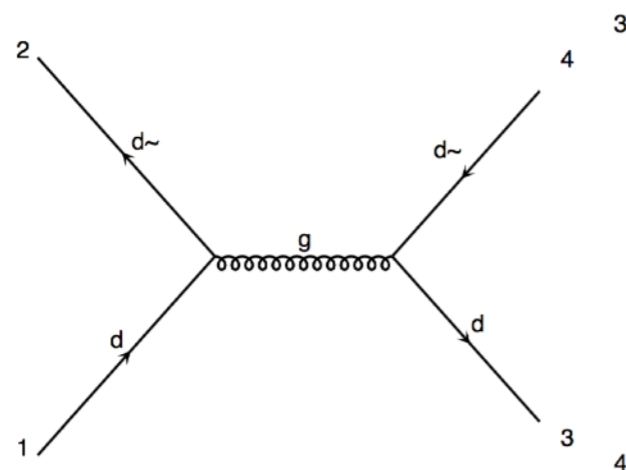
X



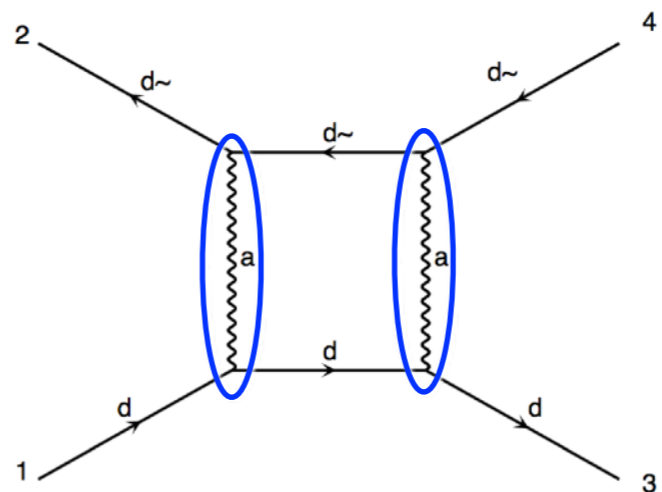
$$\sim |\alpha| \text{Re}(\alpha)$$

\neq

Virtuals:



X



$$\sim |\alpha| \text{Re}^2(\alpha)$$

HOW TO HANDLE THE COMPLEX PHASE OF α ?

- ▶ We **must set $\alpha \rightarrow |\alpha|$** to setup IR factorization.
 - This can induce **gauge violations** whenever sensitive to complex phase of α
 - And correspondingly, a potential **dependance** on **how one writes EW couplings**.

→ It is always possible to assign a phase to G_μ so as to make α real (this is what is effectively done in the $\alpha(M_Z)$ scheme)

step 1 : $\alpha^{(CMS, G_F)} = \left| \left((\sqrt{2}/\pi) |G_F| / M_Z^{(CMS)2} \right) M_W^{(CMS)2} \left(M_Z^{(CMS)2} - M_W^{(CMS)2} \right) \right|$

step 2 : $G_F^{-1} = \left((\sqrt{2}/\pi) \frac{1}{\alpha^{(CMS, G_F)}} / M_Z^{(CMS)2} \right) M_W^{(CMS)2} \left(M_Z^{(CMS)2} - M_W^{(CMS)2} \right)$

$$\rightarrow \overline{G}_\mu^{(G_\mu)} = G_\mu^{(G_\mu)} e^{i \text{Arg} \left[\frac{m_Z^2}{m_W^2 (m_Z^2 - m_W^2)} \right]}$$

TL;DL

- ▶ Computation of **all NLO QCD+EW** now available in **MG5_aMC**.
- ▶ **Complex mass-scheme** is an essential component in the computation of EW corrections. **Subtleties:** complex phase of expansion parameters, analytic continuation, mixed-case with OS scheme,
- ▶ **Outlook**
 - ▶ Use of **fragmentation functions** for (anti-)tagging short-distance photons; though **not necessary for leading NLO EW**
 - ▶ study solutions for **matching** mixed QCD+EW fixed order predictions to parton showers.
 - ▶ study the possibility of automatically generating **UFO@NLO BSM** models suited for QCD+EW NLO predictions.