

MITP, May 1 2018

Non-standard charged-current interactions

(from beta decays to the LHC)

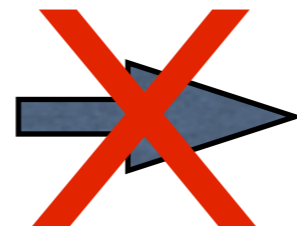
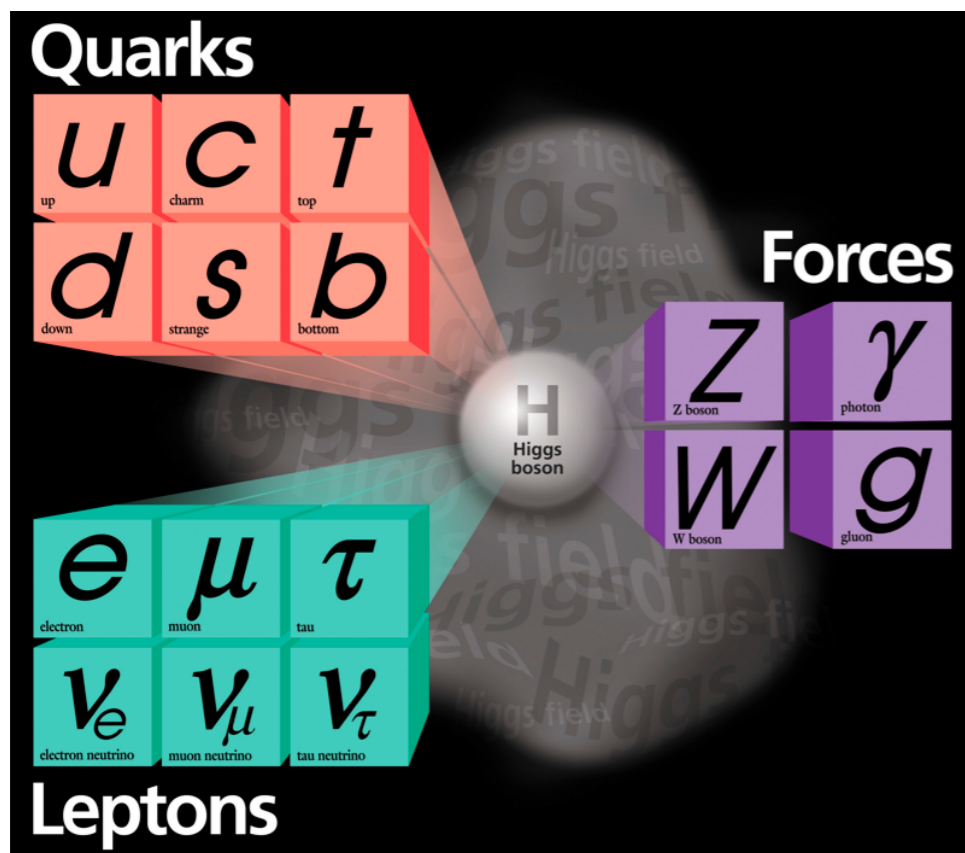
Vincenzo Cirigliano

Los Alamos National Laboratory



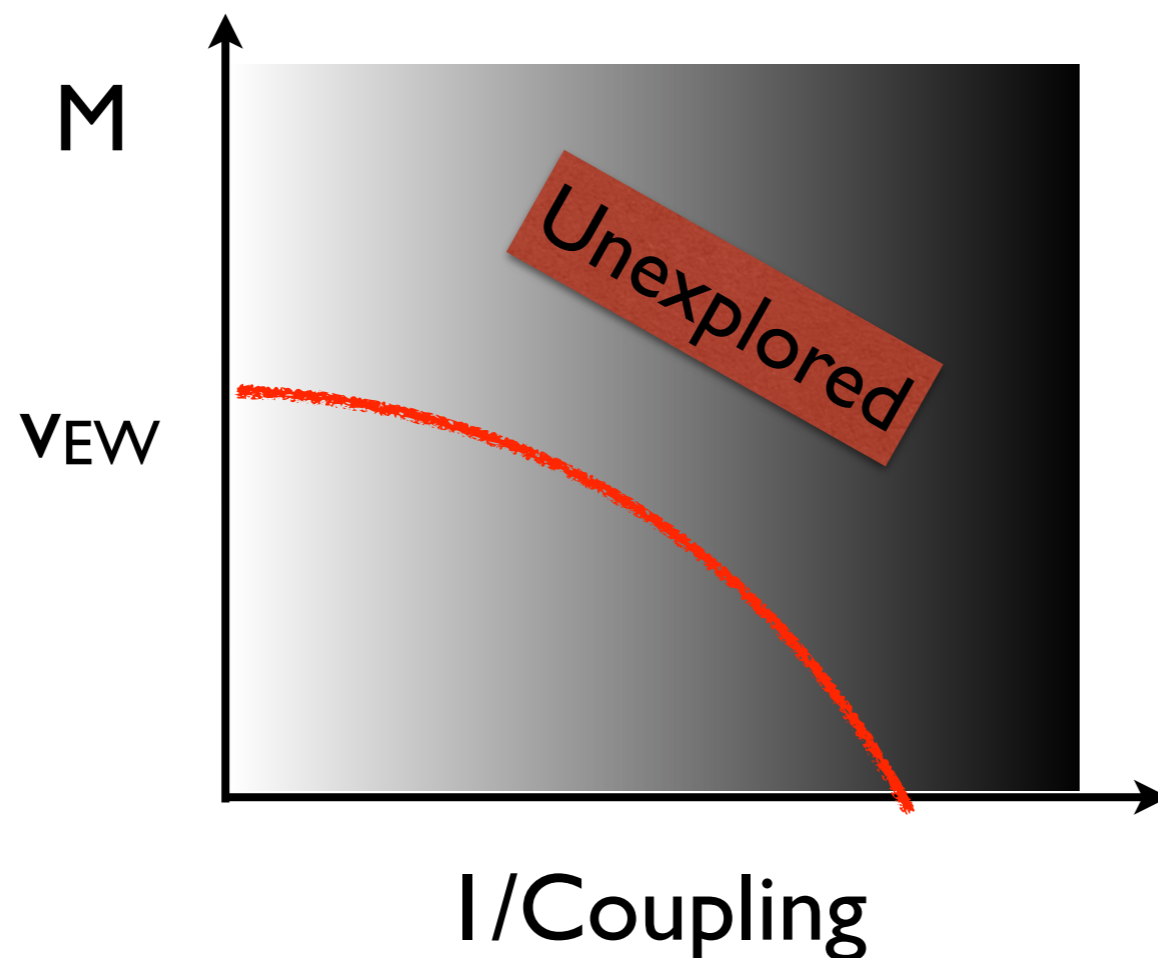
New physics: why?

- The SM is remarkably successful, but it's probably not the whole story



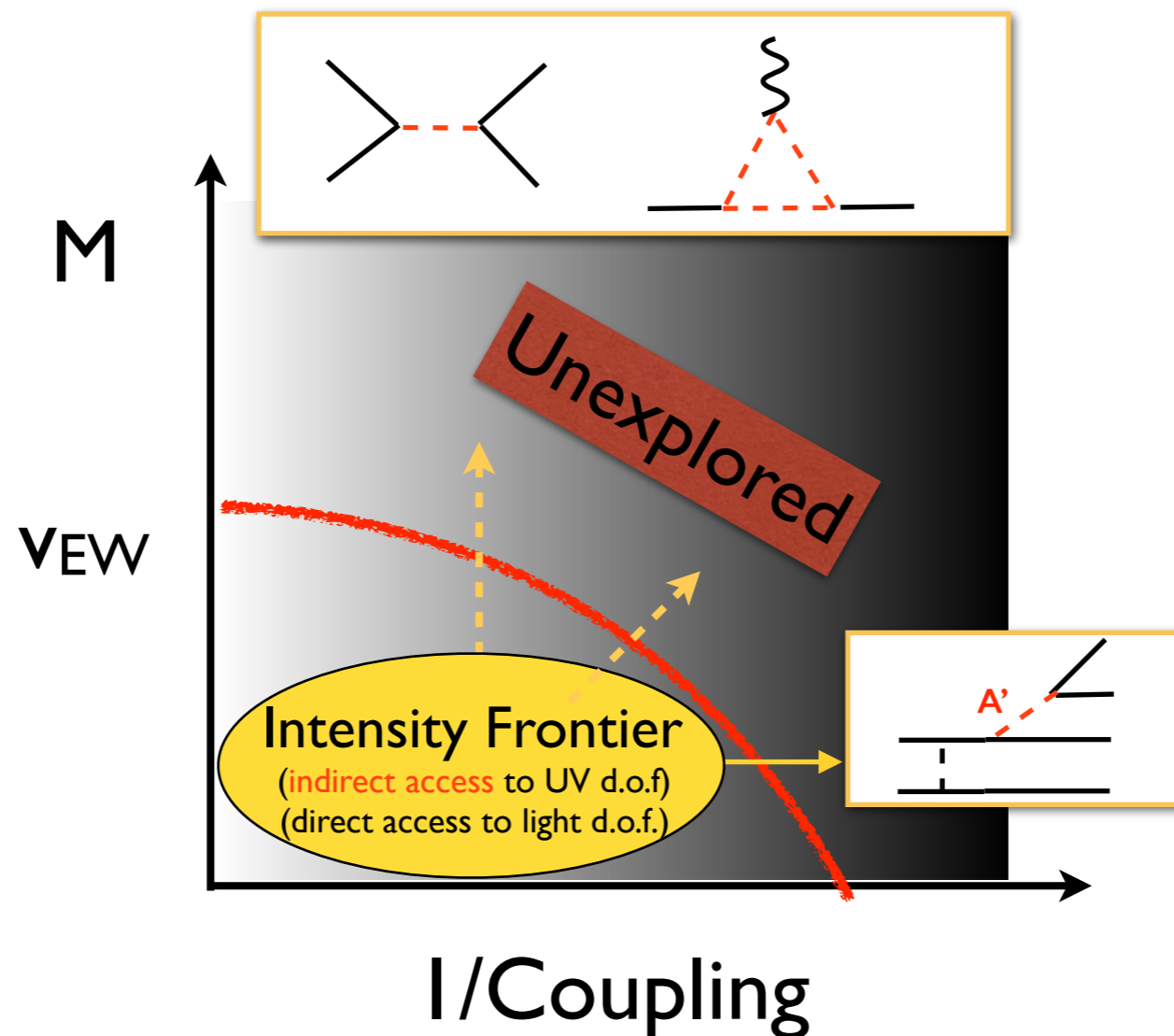
New physics: where?

- New degrees of freedom: Heavy? Light & weakly coupled?
- Two complementary laboratory paths to probe \mathcal{L}_{BSM} :
energy and intensity / precision frontiers



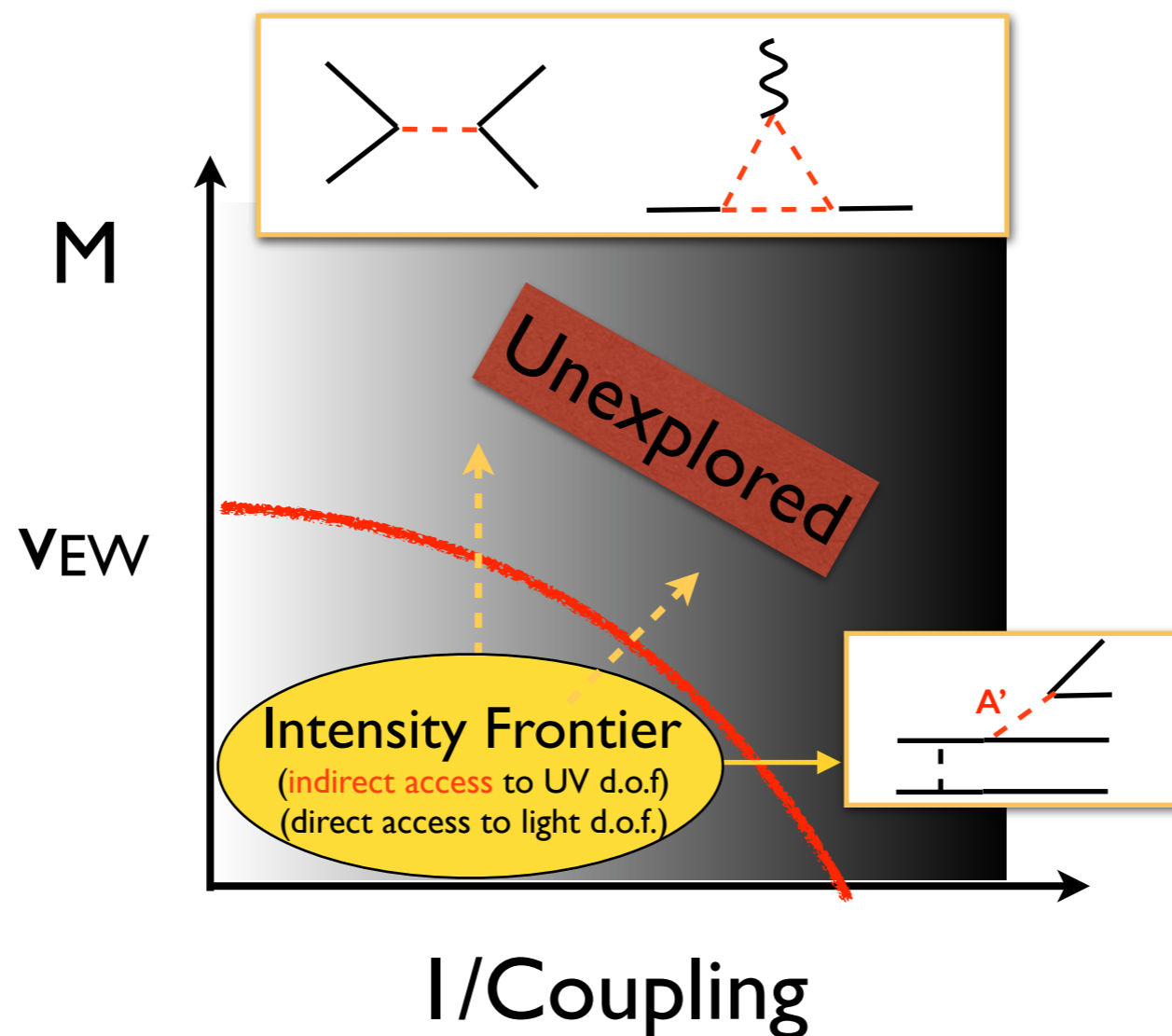
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In this talk
assume new
physics at
 $M > VEW$

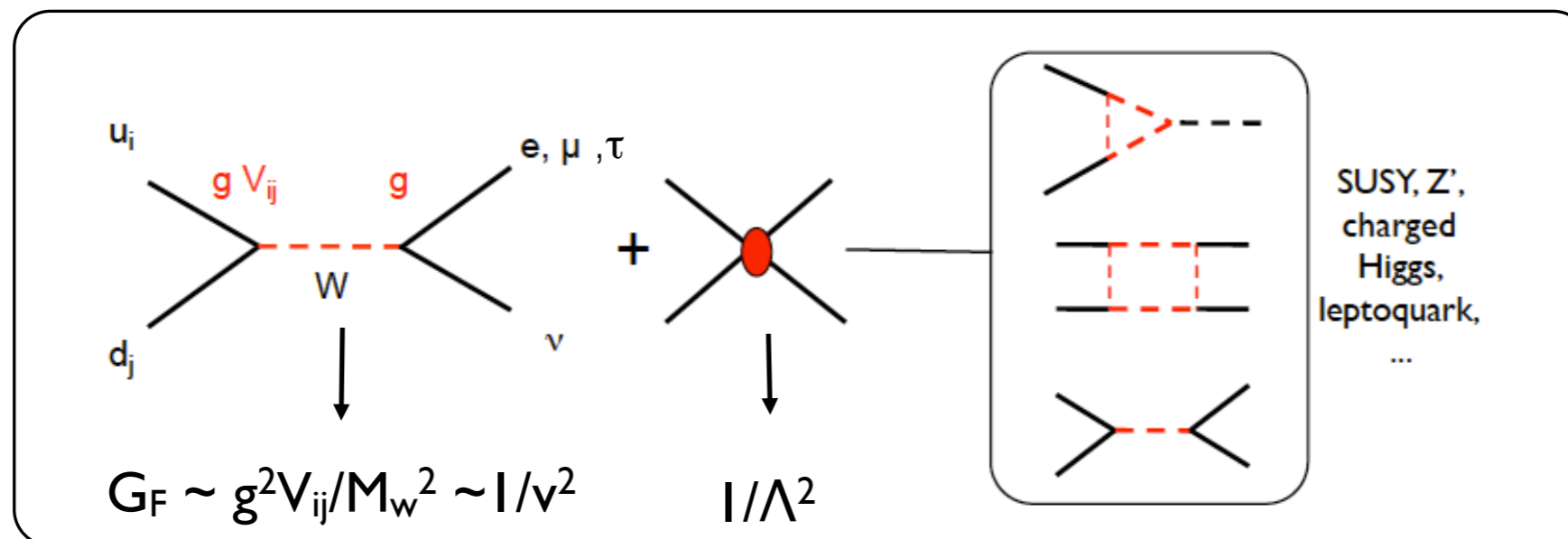
Outline

- Charged current interactions in the “Standard Model EFT”
- Probing **first-generation** quarks and lepton couplings:
 - precision beta decay measurements → LHC
- Probing **tau lepton** couplings to light quarks
 - Inclusive and exclusive tau decays → LHC
- Conclusion

Charged currents and new physics

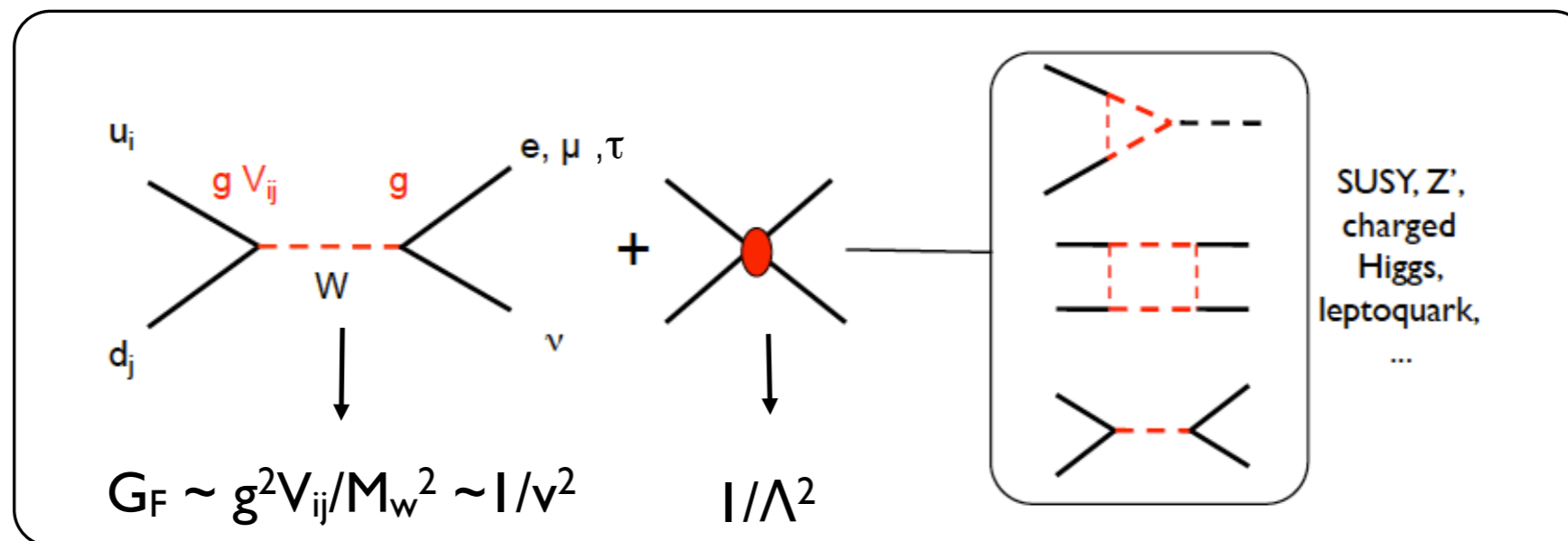
CC processes in the SM and beyond

- In the SM, W exchange \Rightarrow V-A currents, universality



CC processes in the SM and beyond

- In the SM, W exchange \Rightarrow V-A currents, universality



SUSY analyses:

Bauman, Eler,
 Ramsey-Musolf,
 arXiv:1204.0035,

...
 Hagiwara et
 al1995

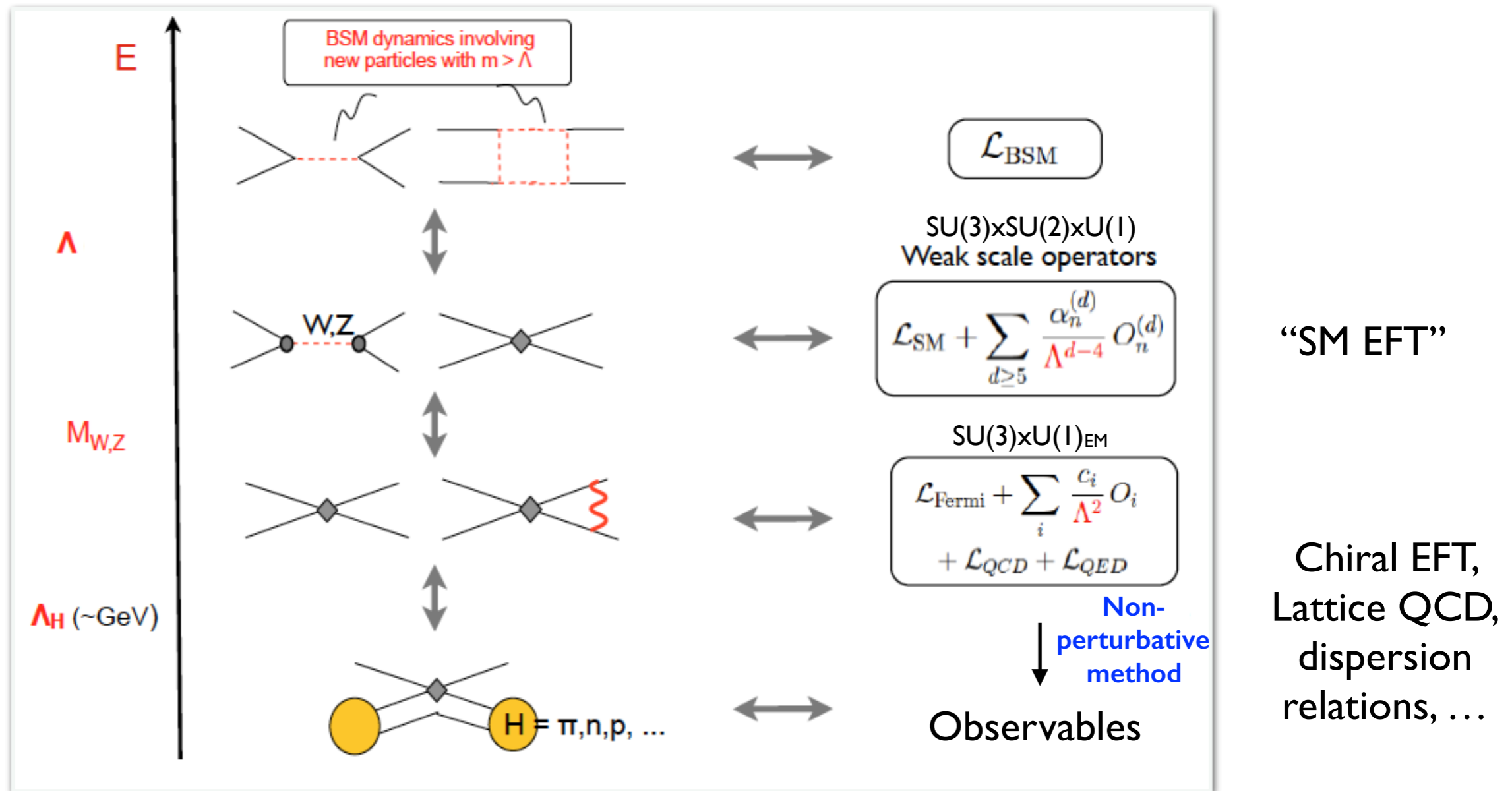
...
 Barbieri et al
 1985

...

- Sensitivity to broad variety of BSM scenarios
- Experimental and theoretical precision at or approaching 0.1% level
 Probe effective scale Λ in the 5-10 TeV range

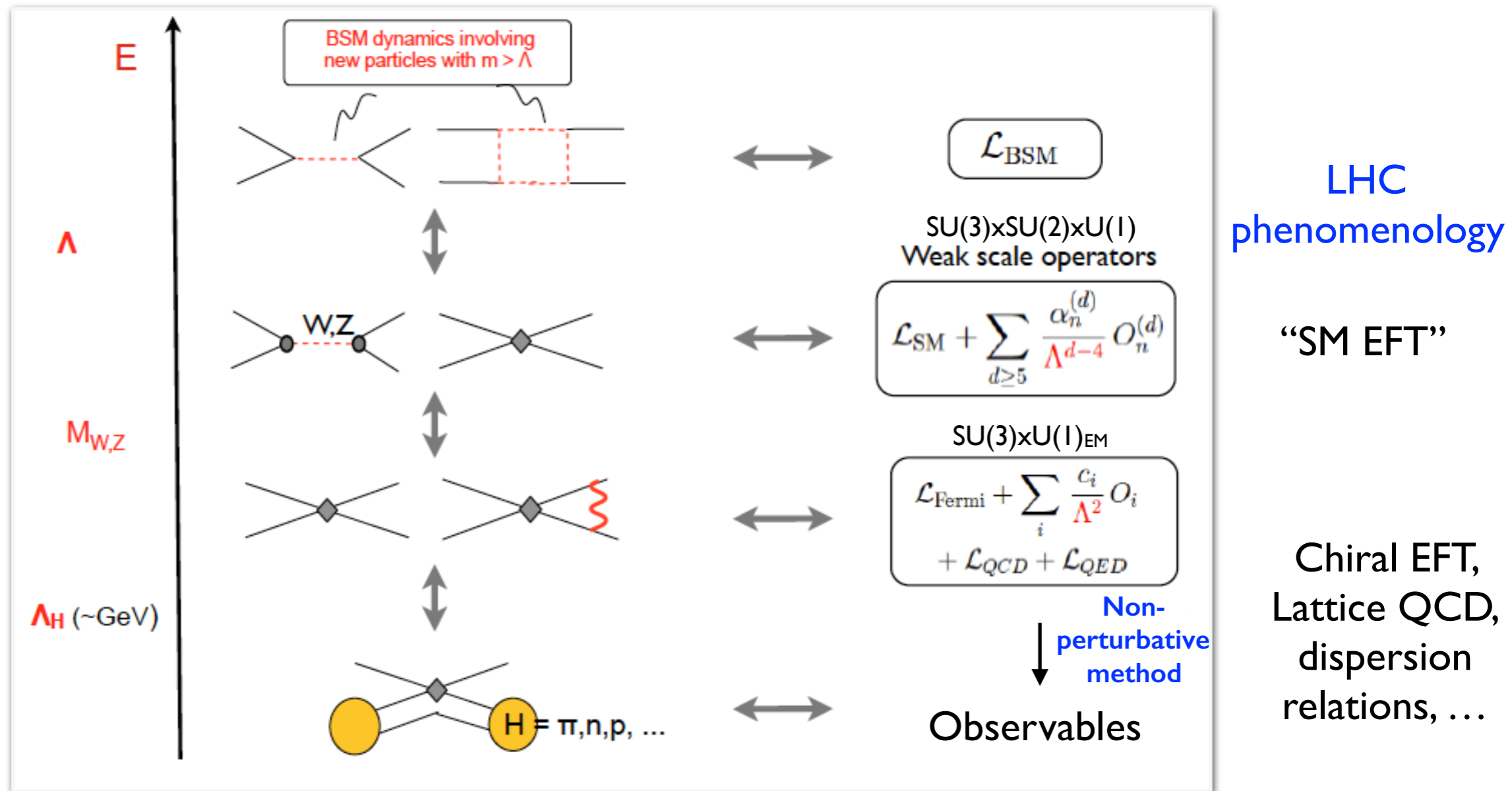
EFT framework: connecting scales

- To interpret (positive or null) searches in terms of new physics at $\Lambda > v_{ew}$ need several steps



EFT framework: connecting scales

- To interpret (positive or null) searches in terms of new physics at $\Lambda > v_{ew}$ need several steps



- If $\Lambda > \text{few TeV}$, can use EW-scale \mathcal{L}_{eff} for LHC: connection of low-E and collider phenomenology

Effective Lagrangian at $E \sim \text{GeV}$

- New physics effects are encoded in **ten quark-level couplings**

$$\begin{aligned}
 \mathcal{L}_{\text{CC}} = & -\frac{G_F^{(0)} V_{u_i d_j}}{\sqrt{2}} \\
 & \times \left[(1 + \delta_{RC} + \epsilon_L) \bar{\ell} \gamma_\mu (1 - \gamma_5) \nu_\ell \cdot \bar{u}_i \gamma^\mu (1 - \gamma_5) d_j \right. \\
 & + \epsilon_R \bar{\ell} \gamma_\mu (1 - \gamma_5) \nu_\ell \cdot \bar{u}_i \gamma^\mu (1 + \gamma_5) d_j \\
 & + \epsilon_S \bar{\ell} (1 - \gamma_5) \nu_\ell \cdot \bar{u}_i d_j \\
 & - \epsilon_P \bar{\ell} (1 - \gamma_5) \nu_\ell \cdot \bar{u}_i \gamma_5 d_j \\
 & \left. + \epsilon_T \bar{\ell} \sigma_{\mu\nu} (1 - \gamma_5) \nu_\ell \cdot \bar{u}_i \sigma^{\mu\nu} (1 - \gamma_5) d_j \right] + \text{h.c.}
 \end{aligned}$$

$$\epsilon_i, \tilde{\epsilon}_i \sim (M_W/\Lambda)^2$$

Linear
sensitivity to ϵ_i
(interference
with SM)

Effective Lagrangian at $E \sim \text{GeV}$

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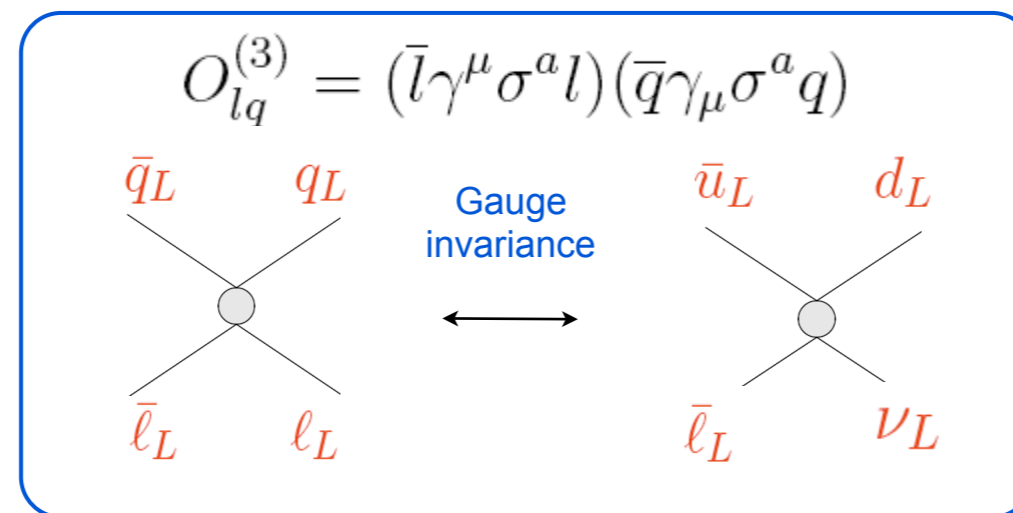
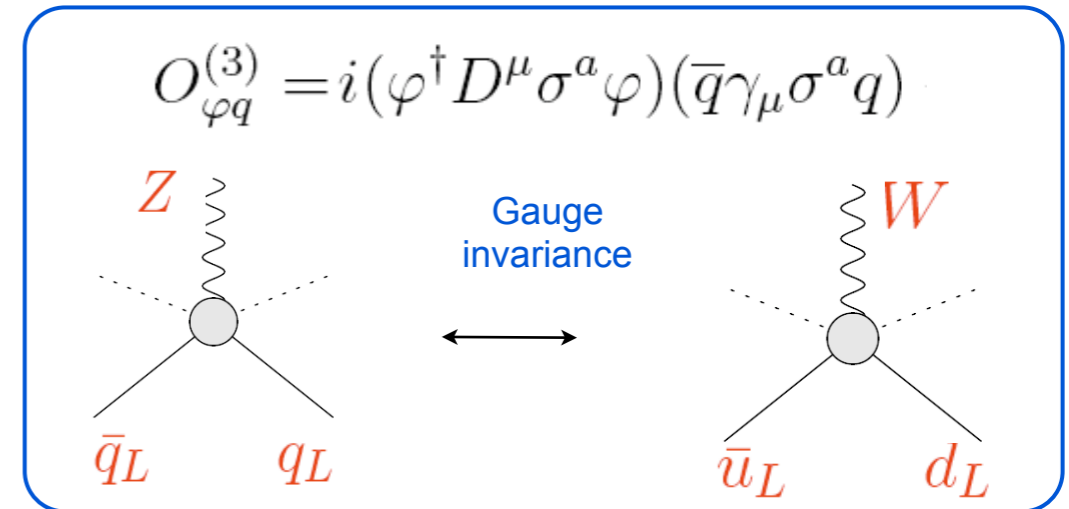
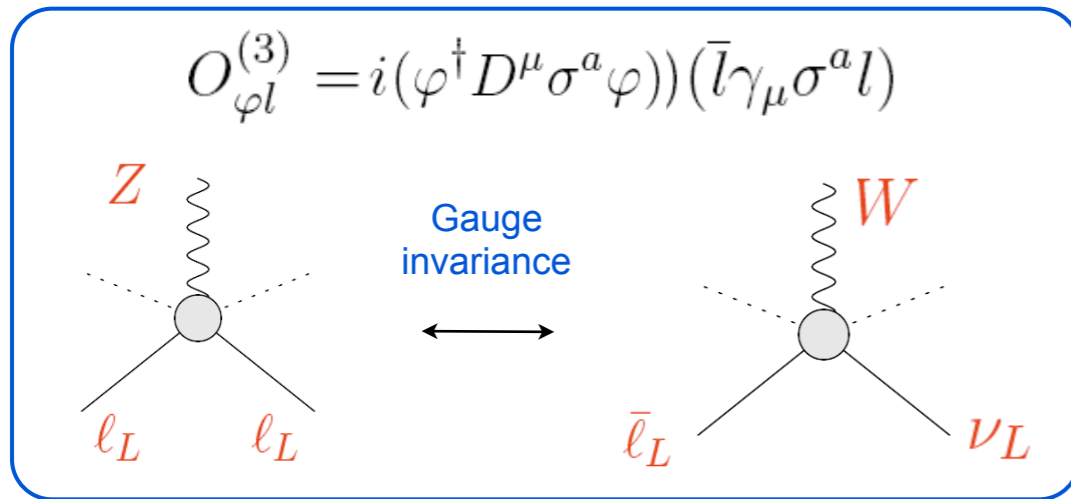
Linear sensitivity to ϵ_i (interference with SM)

Quadratic sensitivity to $\tilde{\epsilon}_i$ (interference suppressed by m_ν/E)

$$+ \quad \epsilon_i \longrightarrow \tilde{\epsilon}_i \quad (1 - \gamma_5) \nu_\ell \longrightarrow (1 + \gamma_5) \nu_\ell$$

Relation to weak-scale operators

- \mathcal{E}_L : vertex corrections and 4-fermion contacts



$$\varphi = \begin{pmatrix} \varphi^+ \\ \varphi^0 \end{pmatrix}$$

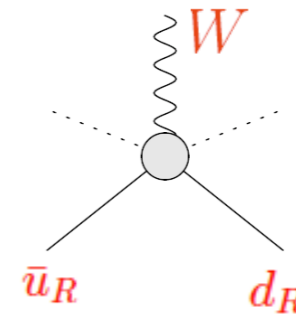
$$q^i = \begin{pmatrix} u_L^i \\ d_L^i \end{pmatrix}$$

$$l^i = \begin{pmatrix} \nu_L^i \\ e_L^i \end{pmatrix}$$

Relation to weak-scale operators

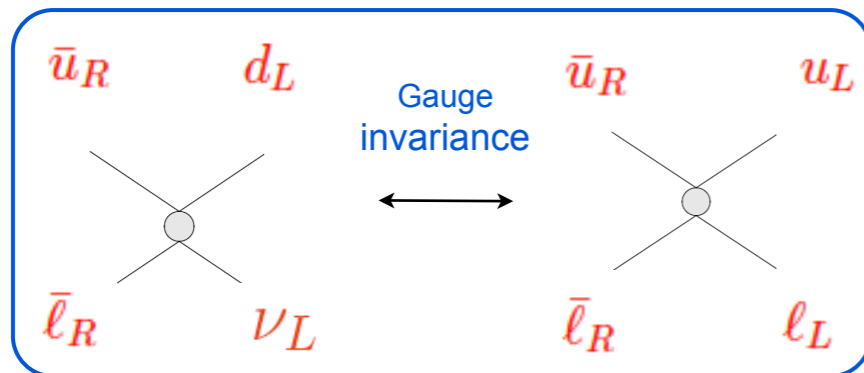
- $\mathcal{E}_R \Leftrightarrow$ weak-scale R-handed quark coupling

$$O_{\varphi\varphi} = i(\varphi^T \epsilon D_\mu \varphi)(\bar{u}\gamma^\mu d)$$



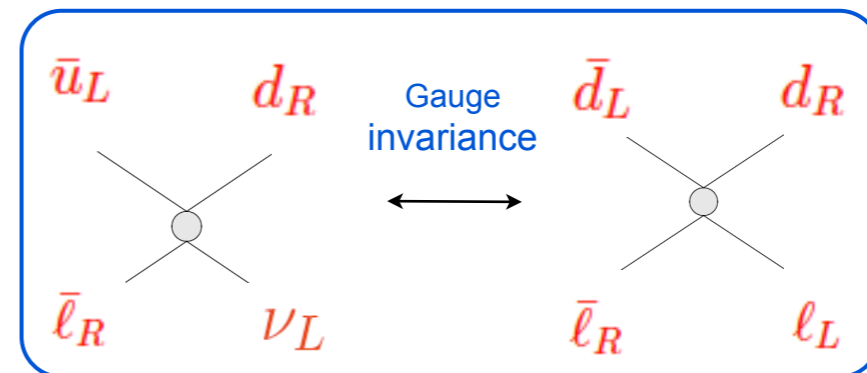
- $\mathcal{E}_{S,P} \Leftrightarrow$ 2 independent scalar structures

$$O_{lq} = (\bar{l}_a e) \epsilon^{ab} (\bar{q}_b u) + \text{h.c.}$$



$\mathcal{E}_S + \mathcal{E}_P$

$$O_{qde} = (\bar{l} e) (\bar{d} q) + \text{h.c.}$$



$\mathcal{E}_S - \mathcal{E}_P$

- $\mathcal{E}_T \Leftrightarrow$ weak-scale tensor structure

$$O_{lq}^t = (\bar{l}_a \sigma^{\mu\nu} e) \epsilon^{ab} (\bar{q}_b \sigma_{\mu\nu} u) + \text{h.c.}$$

How to probe the ϵ_α

- $(\epsilon_\alpha)^{de}$
 - Beta decays: half-lives (weak universality), correlations
 - LHC ($pp \rightarrow e\nu + X$, $pp \rightarrow e\bar{e} + X$), if $\Lambda > \text{few TeV}$

RECENT REVIEW: [Gonzalez-Alonso, Naviliat-Cuncic, Severijns, 1803.08732](#)

- $(\epsilon_\alpha)^{d\tau}$
 - Hadronic tau decays (exclusive and inclusive)
 - LHC ($pp \rightarrow \tau\nu + X$, $pp \rightarrow \tau\bar{\tau} + X$), if $\Lambda > \text{few TeV}$

First generation couplings:

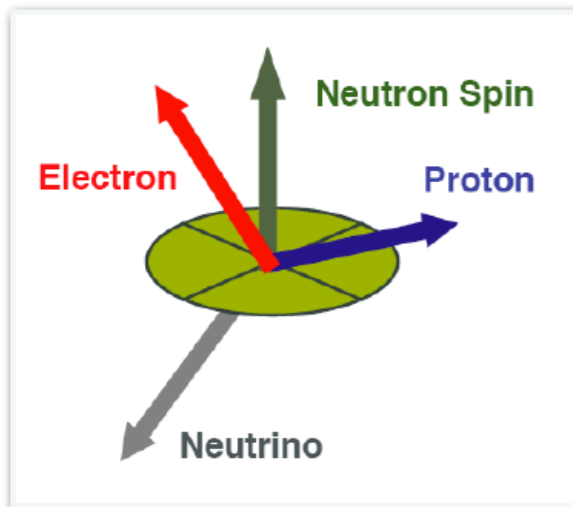
$$(\varepsilon_{\alpha})^{\text{de}}$$

Beta decay sensitivity to the ϵ_α

I. Differential decay distribution

$$d\Gamma \propto F(E_e) \left\{ 1 + b \frac{m_e}{E_e} + a \frac{\vec{p}_e \cdot \vec{p}_\nu}{E_e E_\nu} + \langle \vec{J} \rangle \cdot \left[A \frac{\vec{p}_e}{E_e} + B \frac{\vec{p}_\nu}{E_\nu} + \dots \right] \right\}$$

Lee-Yang, 1956 Jackson-Treiman-Wyld 1957



$a(g_A, g_\alpha \epsilon_\alpha)$, $A(g_A, g_\alpha \epsilon_\alpha)$, $B(g_A, g_\alpha \epsilon_\alpha)$,

...

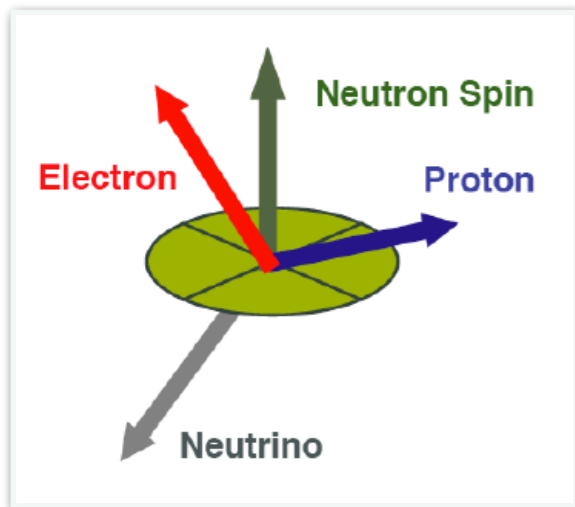
isolated via suitable experimental
asymmetries

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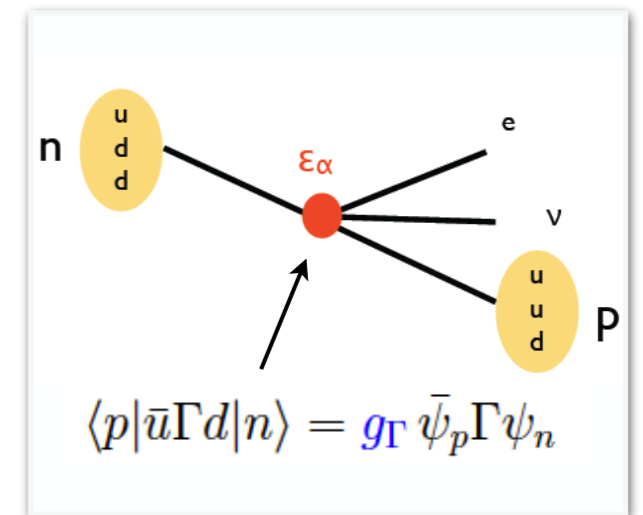
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$$a(g_A, g_\alpha \epsilon_\alpha), \quad A(g_A, g_\alpha \epsilon_\alpha), \quad B(g_A, g_\alpha \epsilon_\alpha),$$

...

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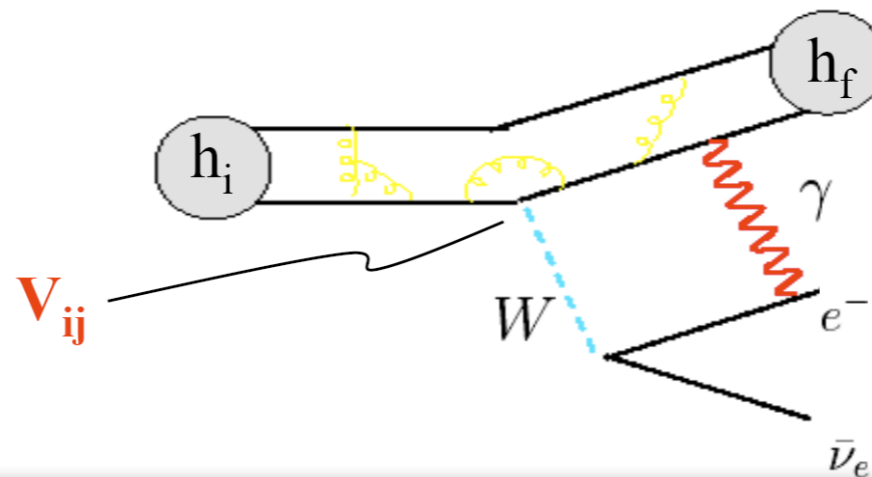


Theory input: $g_{V,A,S,T}$ (great progress in lattice QCD) + rad. corr.

LANL results: Bhattacharya, et al 1606.07049

Beta decay sensitivity to the ϵ_α

2. Decay rate



$$\Gamma_k = (G_F^{(\mu)})^2 \times |\bar{V}_{ij}|^2 \times |M_{\text{had}}|^2 \times (1 + \delta_{RC}) \times F_{\text{kin}}$$

$$\bar{V}_{ud} = V_{ud} \left[1 + \epsilon_L + \epsilon_R + b(\epsilon_S, \epsilon_T) F_{\text{kin}} \right]$$

Channel-dependent effective
CKM element**

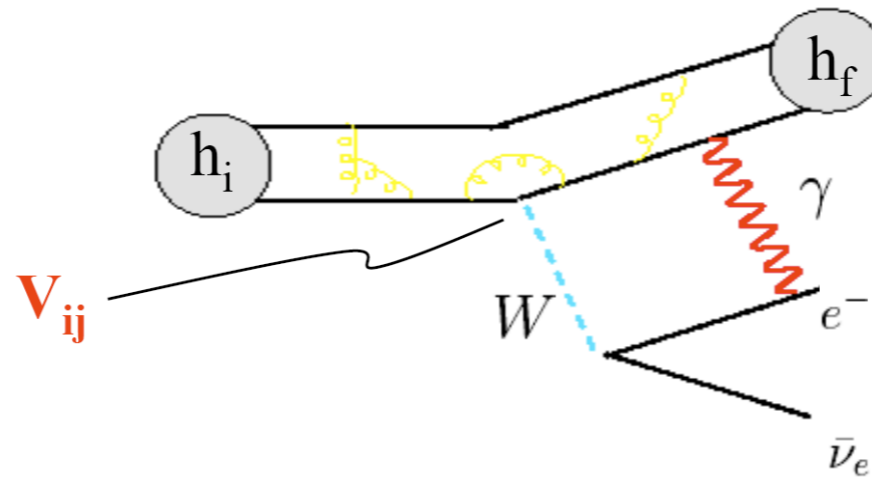
Hadronic / nuclear
matrix elements (ϵ_α)
and radiative corrections

LQCD, χ PT,
dispersion relations,

...

Beta decay sensitivity to the ϵ_α

2. Decay rate



Neutron
case:

$$|\bar{V}_{ud}|^2 \tau_n (1 + 3\bar{g}_A^2) = 4908.6(1.9) s$$

Czarnecki,
Marciano, Sirlin
1802.01804

$$\bar{V}_{ud} = V_{ud} \left[1 + \epsilon_L + \epsilon_R + b(\epsilon_S, \epsilon_T) F_{\text{kin}} \right]$$

Channel-dependent effective
CKM element**

$$\bar{g}_A = g_A (1 - 2\epsilon_R)$$

Axial charge contaminated
by R-handed coupling

Snapshot of the field

- This table summarizes a large number of measurements and th. input
- Already quite impressive. Effective scales in the range $\Lambda = 1-10 \text{ TeV}$ ($\Lambda_{\text{SM}} \approx 0.2 \text{ TeV}$)

Non-standard coupling	Observable	Current sensitivity	Prospective sensitivity
$\text{Re}(\epsilon_L + \epsilon_R)$	Δ_{CKM}	$\sim 0.05\%$	$< 0.05\%$ *
$\text{Im}(\epsilon_R)$	D_n	$\sim 0.05\%$	
$\epsilon_P, \tilde{\epsilon}_P$	$R_\pi = \frac{\Gamma(\pi \rightarrow e\nu)}{\Gamma(\pi \rightarrow \mu\nu)}$	$\sim 0.05\%$	
$\text{Re}(\epsilon_S)$	$b, B, [\tilde{a}, \tilde{A}, \tilde{G}]$	$\sim 0.5\%$	$< 0.3\%$
$\text{Im}(\epsilon_S)$	R_n	$\sim 10\%$	
$\text{Re}(\epsilon_T)$	$b, B, [\tilde{a}, \tilde{A}, \tilde{G}], \pi \rightarrow e\nu\gamma$	$\sim 0.1\%$	$< 0.03\%$
$\text{Im}(\epsilon_T)$	R_{sLi}	$\sim 0.2\%$	$\sim 0.05\%$
$\tilde{\epsilon}_{\alpha \neq P}$	a, b, B, A	$\sim 5 - 10\%$	

$$\tilde{Y}(E_e) = \frac{Y(E_e)}{1 + b m_e / E_e + \dots}$$

Snapshot of the field

- This table summarizes a large number of measurements and th. input
- Already quite impressive. Effective scales in the range $\Lambda = 1-10 \text{ TeV}$ ($\Lambda_{\text{SM}} \approx 0.2 \text{ TeV}$)
- Probes that depend on the ϵ 's *linearly*

$$\tilde{Y}(E_e) = \frac{Y(E_e)}{1 + b m_e / E_e + \dots}$$

Non-standard coupling	Observable	Current sensitivity	Prospective sensitivity
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$\text{Re}(\epsilon_S)$	$b, B, [\tilde{a}, \tilde{A}, \tilde{G}]$	$\sim 0.5\%$	$< 0.3\%$
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$\text{Re}(\epsilon_T)$	$b, B, [\tilde{a}, \tilde{A}, \tilde{G}], \pi \rightarrow e\nu\gamma$	$\sim 0.1\%$	$< 0.03\%$
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CKM unitarity test

$$|\bar{V}_{ud}|^2 + |\bar{V}_{us}|^2 + |\bar{V}_{ub}|^2 = 1 + \Delta_{\text{CKM}}(\epsilon_i)$$

Currently, extraction
dominated by $0^+ \rightarrow 0^+$
nuclear transitions

Hardy-Towner 1411.5987

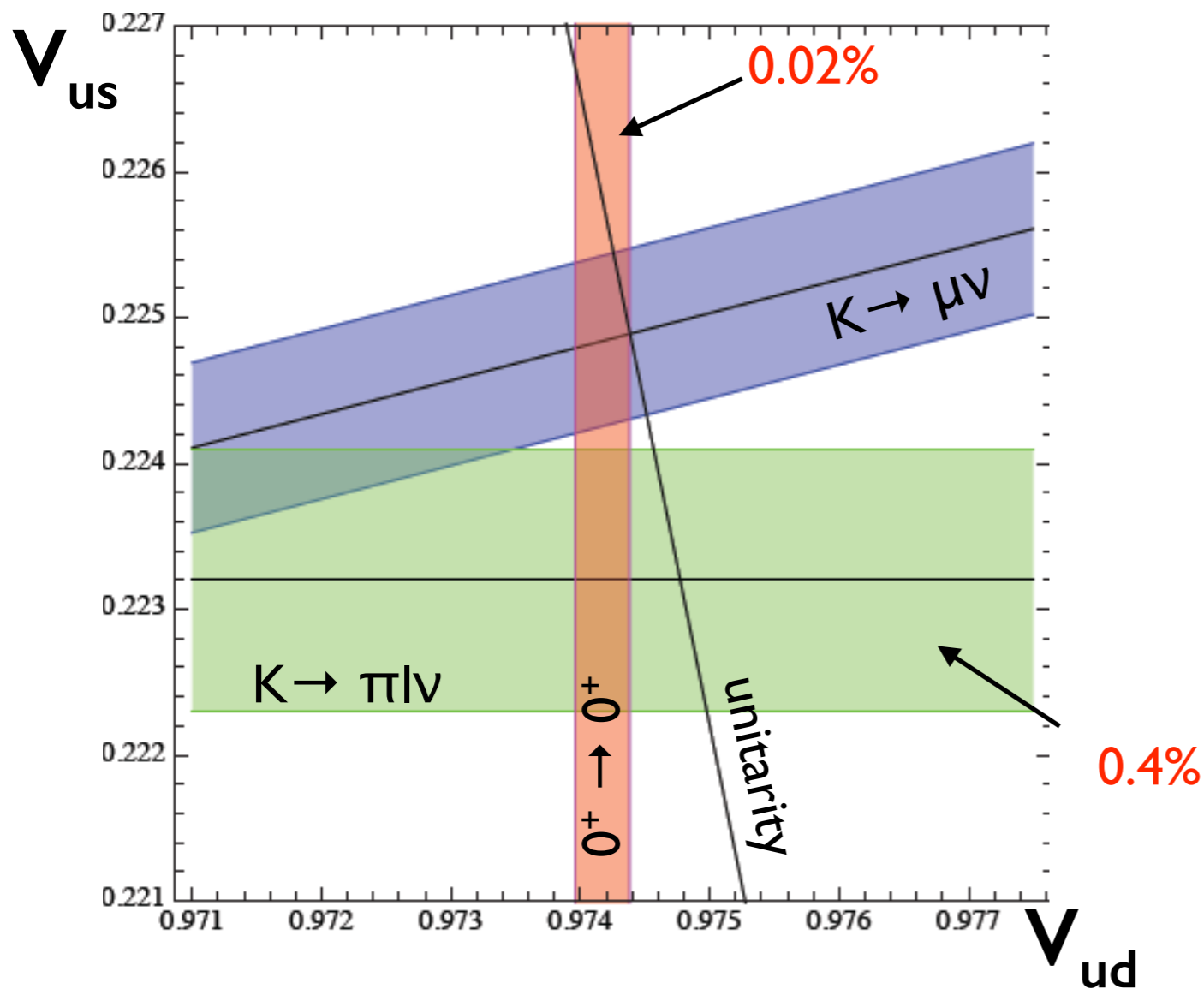
Extraction
dominated by
Kaon decays

FLAVIANET report I005.2323 and refs therein

Lattice QCD input from FLAG I607.00299 and refs therein

CKM unitarity test

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V_{us} from $K \rightarrow \mu \nu$

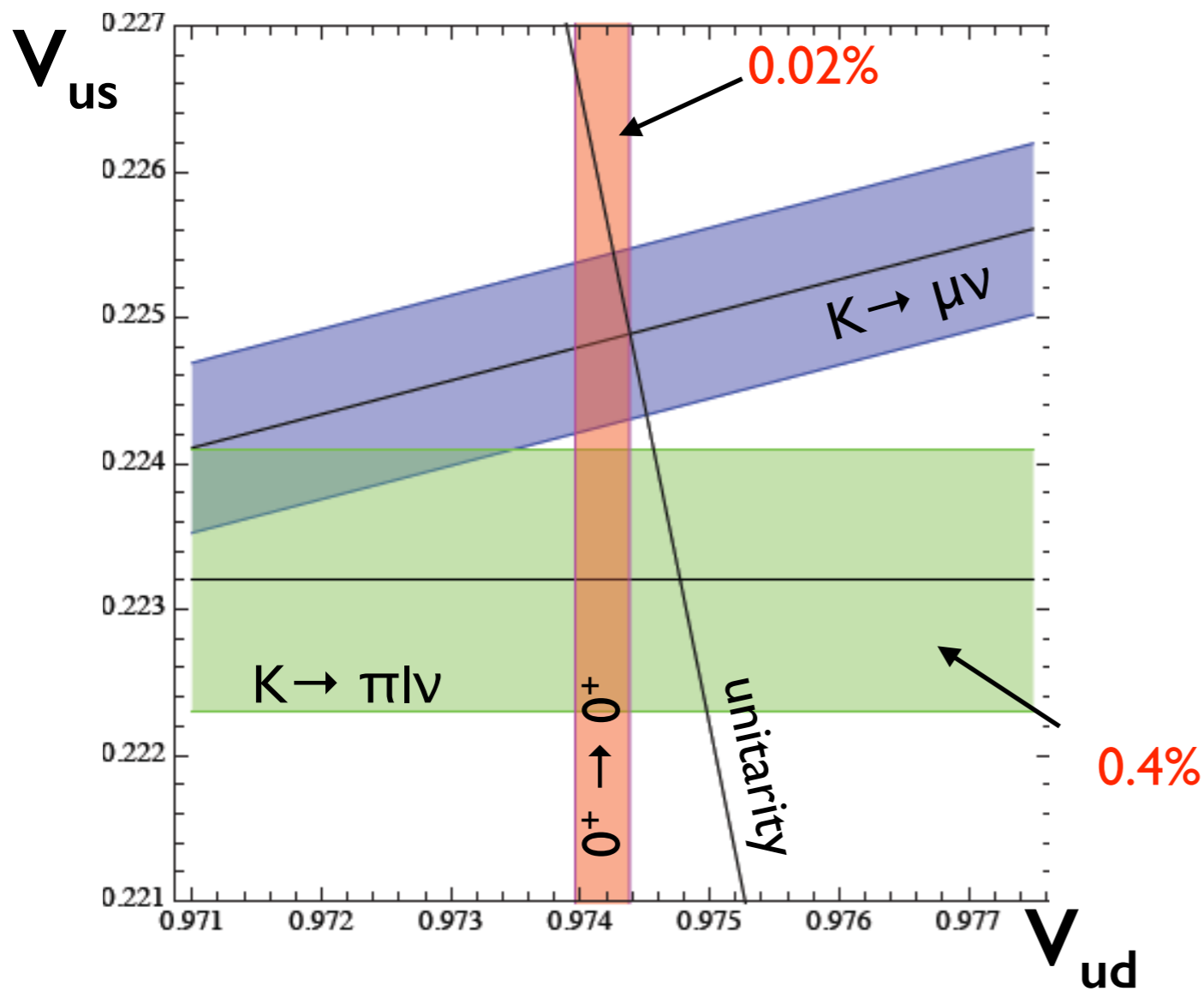
$$\Delta_{\text{CKM}} = -(4 \pm 5) * 10^{-4} \sim 1\sigma$$

$$\Delta_{\text{CKM}} = -(12 \pm 6) * 10^{-4} \sim 2\sigma$$

V_{us} from $K \rightarrow \pi l \nu$

CKM unitarity test

$$|\bar{V}_{ud}|^2 + |\bar{V}_{us}|^2 + |\bar{V}_{ub}|^2 = 1 + \Delta_{\text{CKM}}(\epsilon_i)$$



V_{us} from $K \rightarrow \mu\nu$

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V_{us} from $K \rightarrow \pi lv$

Hint of something?

$[\epsilon_{R,P}^{(s)}, \epsilon_L + \epsilon_R, \text{SM th input}]$

Worth a closer look:
at the level of the best LEP
EW precision tests,
probing scale $\Lambda \sim 10 \text{ TeV}$

Impact of neutrons

- Independent extraction of V_{ud} @ 0.02% requires:

$$\bar{V}_{ud} = \left[\frac{4908.6(1.9) s}{\tau_n (1 + 3\bar{g}_A^2)} \right]^{1/2}$$

Marciano, Sirlin 2006

$$\begin{aligned} \delta\tau_n &\sim 0.35 s \\ \delta\tau_n/\tau_n &\sim 0.04 \% \end{aligned}$$

$$\begin{aligned} \delta g_A/g_A &\sim 0.15\% \rightarrow 0.03\% \\ (\delta a/a, \delta A/A &\sim 0.14\%) \end{aligned}$$

UCNT @ LANL [$\tau_n \sim 877.7(7)(3)s$]
is almost there, will reach $\delta\tau_n \sim 0.2 s$
1707.01817

$\delta A/A < 0.2\%$ can be reached
by PERC, UCNA+

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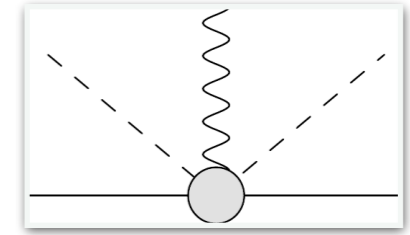
- $V_{ud}(n)$ and $V_{ud}(0^+ \rightarrow 0^+)$ sensitive to different new physics: not a duplicate measurement (similar to $Kl2$ vs $Kl3$ in V_{us})

$$\frac{\bar{V}_{ud}|_n}{\bar{V}_{ud}|_{0^+}} = 1 + c_S \epsilon_S + c_T \epsilon_T$$

$c_S, c_T \sim O(1)$

Probing $\varepsilon_{L,R}$ couplings

- Assume $\varepsilon_{L,R}$ are induced by gauge vertex corrections at high scale (SM-EFT)

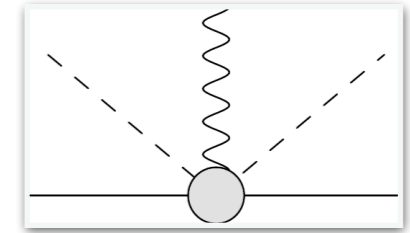


$$\varphi^\dagger \tau^a D_\mu \varphi \quad \bar{q}_L \tau^a \gamma^\mu q_L$$

$$\varphi^T \epsilon D_\mu \varphi \quad \bar{u}_R \gamma^\mu d_R$$

Probing $\varepsilon_{L,R}$ couplings

- Assume $\varepsilon_{L,R}$ are induced by gauge vertex corrections at high scale (SM-EFT)
- Low energy probes:
 - $\Delta_{\text{CKM}} \propto \varepsilon_L + \varepsilon_R$
 - $\delta\Gamma_{(\pi \rightarrow \mu\nu)} \propto \varepsilon_L - \varepsilon_R$ [f_π from LQCD]
 - Neutron decay correlations (A, a, B) $\rightarrow \lambda = g_A (1 - 2\varepsilon_R)$
 - QWeak, Z-pole $\rightarrow \varepsilon_L$

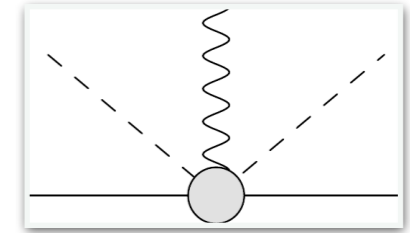


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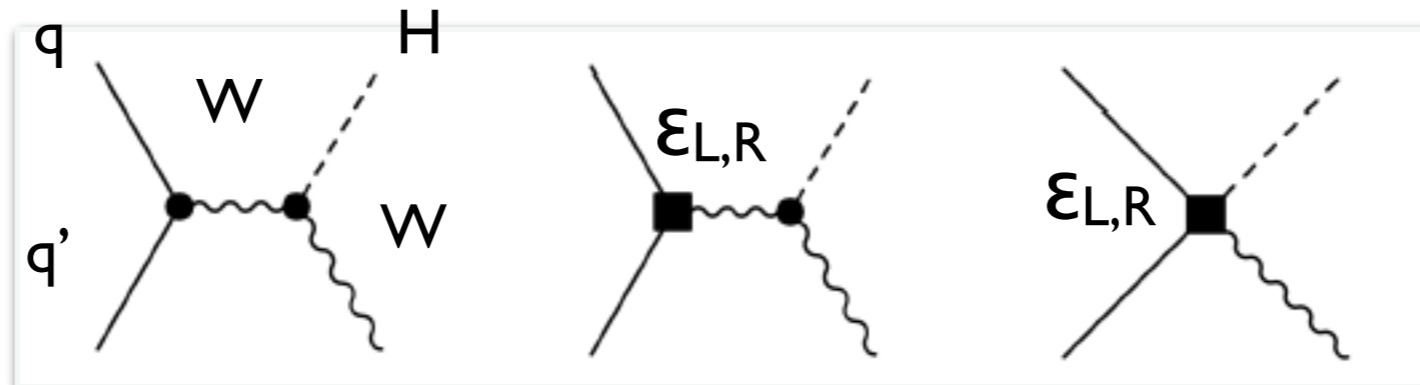
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 - QWeak, Z-pole $\rightarrow \epsilon_L$
- LHC (if $\Lambda > \text{few TeV}$): associated Higgs + W production



$$\varphi^\dagger \tau^a D_\mu \varphi \quad \bar{q}_L \tau^a \gamma^\mu q_L$$

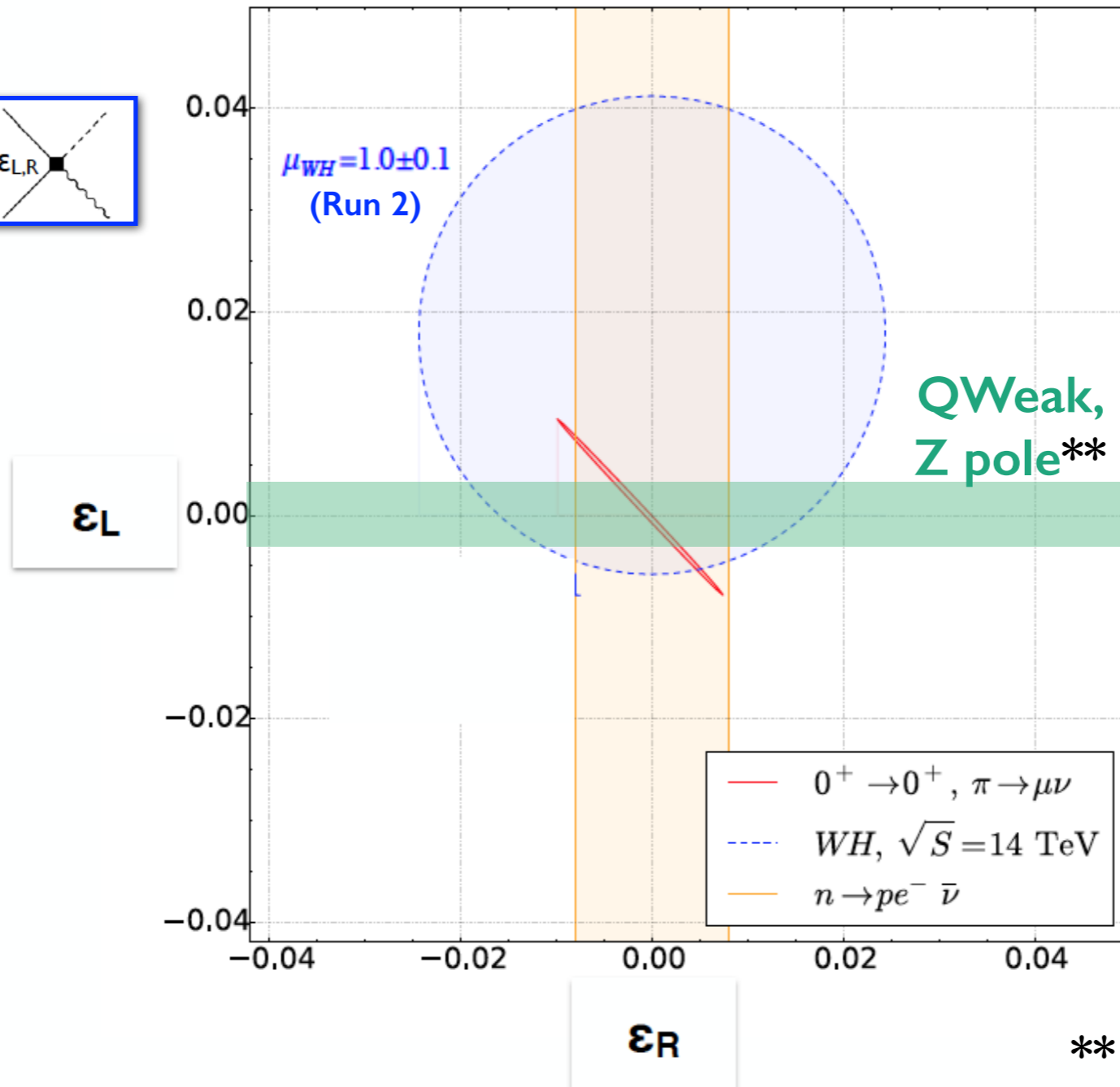
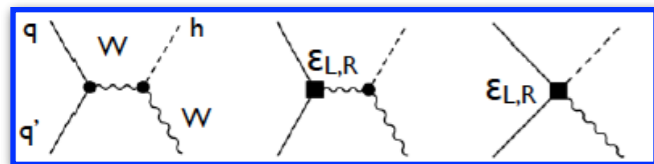
$$\varphi^T \epsilon D_\mu \varphi \quad \bar{u}_R \gamma^\mu d_R$$



Probing $\epsilon_{L,R}$ couplings

1703.04751: S. Alioli, VC, W. Dekens, J. de Vries, E. Mereghetti

Updated plot courtesy of E. Mereghetti



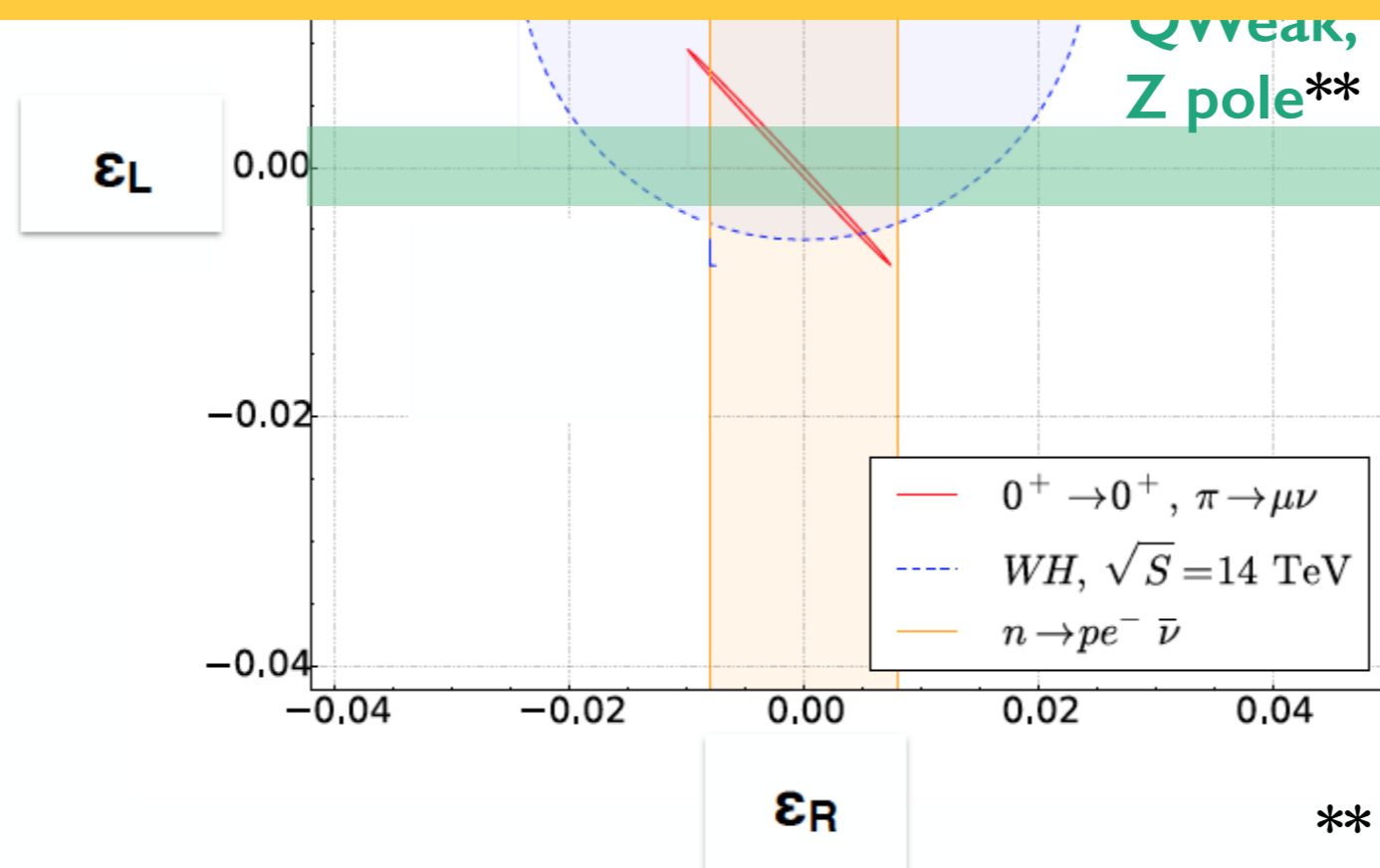
- Δ_{CKM} provides strongest constraint, followed by QWeak
- Neutron decay + LQCD: approaching competitive sensitivity to ϵ_R

Constraint on ϵ_R uses
 $g_A = 1.285(17)$
 (CalLat 1710.06523)

** Adam Falkowski, private communication, PRELIMINARY

Probing $\epsilon_{L,R}$ couplings

- Several lessons:
 - Low-energy can be quite competitive with collider bounds
 - Connection between CC and NC (gauge invariance!)
 - Caveat: additional BSM operators can relax these constraints. Combination of low- and high-energy constraints helps reducing “flat directions”



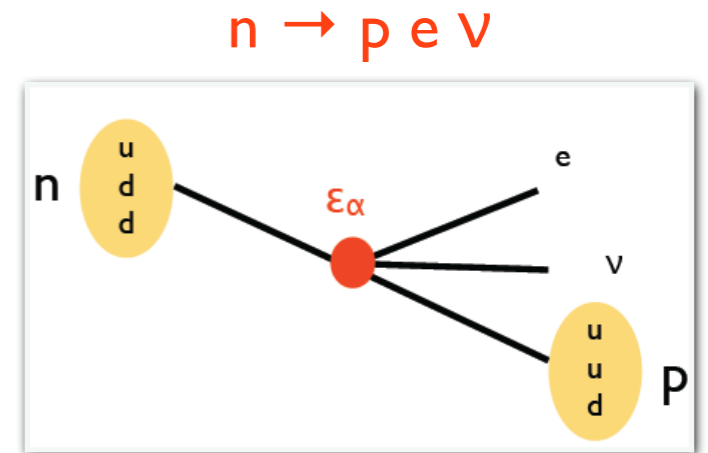
EQCD. approaching competitive sensitivity to ϵ_R

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** Adam Falkowski, private communication, PRELIMINARY

Probing $\epsilon_{S,T}$ couplings

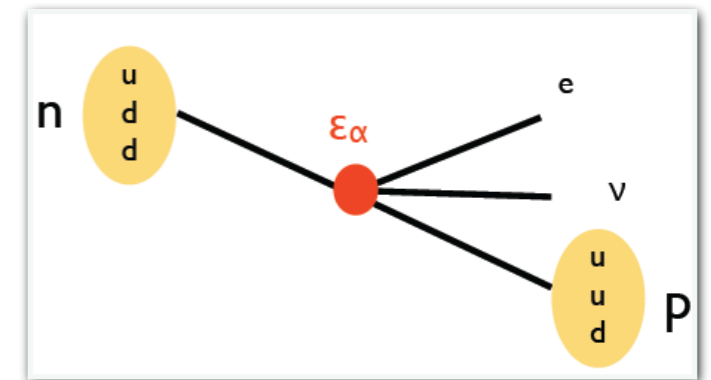
- π , neutron & nuclear decays:
 - Current: $b(0^+ \rightarrow 0^+)$ [ϵ_S]; $\pi \rightarrow e \nu \gamma$ [ϵ_T]
 - Future: b_n, B_n [$\epsilon_{S,T}$] @ 10^{-3} ;
 b_{GT} [ϵ_T] (${}^6\text{He}, \dots$) @ 10^{-3}



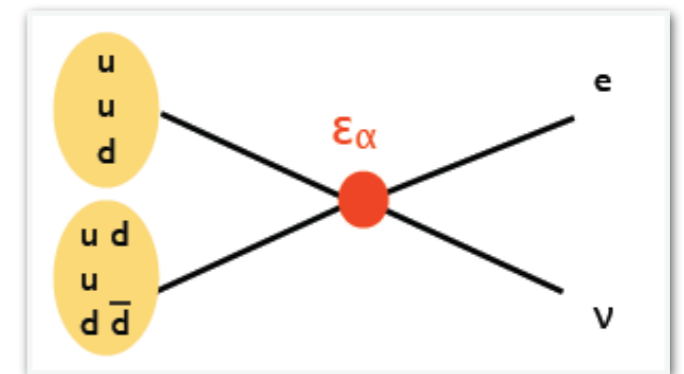
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- Collider: for heavy new mediators probe *same* $\epsilon_{S,T}$

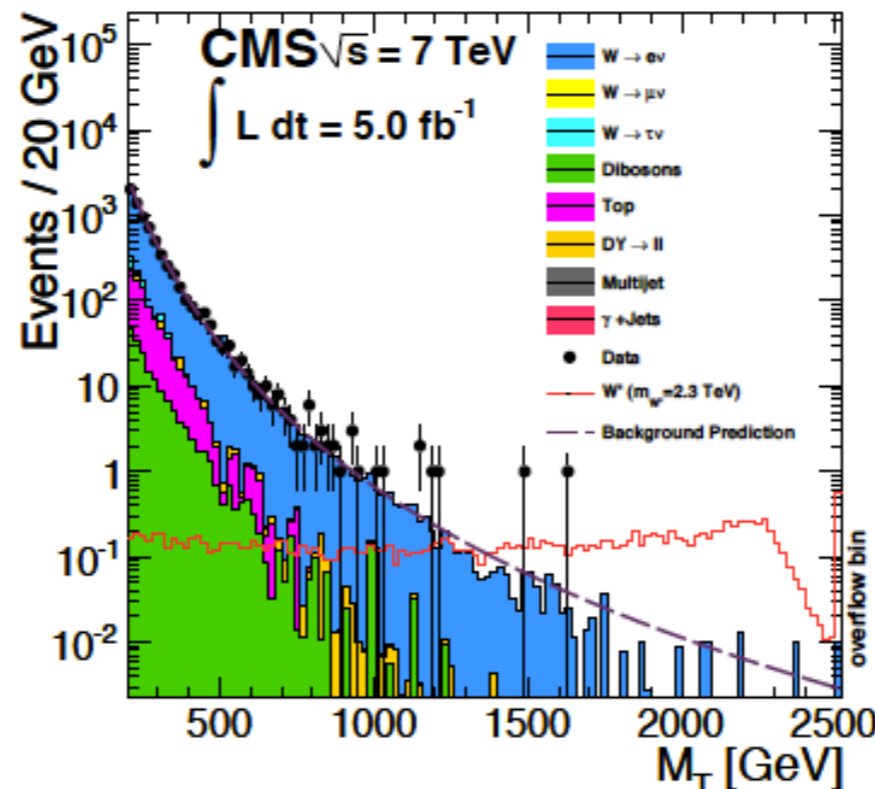
$n \rightarrow p e \nu$



$pp \rightarrow e \nu + X$



$$m_T \equiv \sqrt{2E_T^e E_T^\nu (1 - \cos \Delta\phi_{e\nu})}$$



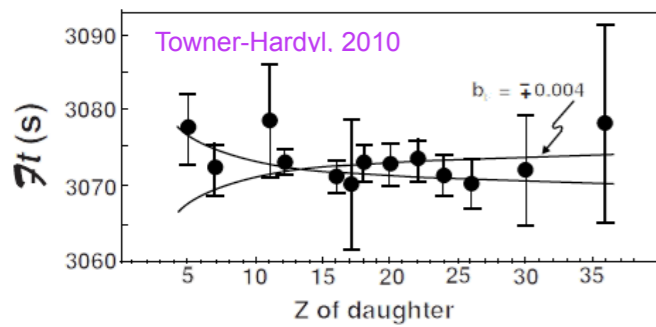
$$n_{\text{obs}} (m_T > m_{T,\text{cut}}) = \epsilon_{\text{eff}} \times L \times (\sigma_W + \sigma_S \times |\epsilon_S|^2 + \sigma_T \times |\epsilon_T|^2)$$

T. Bhattacharya et al, 1110.6448
 VC, Gonzalez-Alonso, Graesser, 1210.4553

...

Probing $\epsilon_{S,T}$ couplings

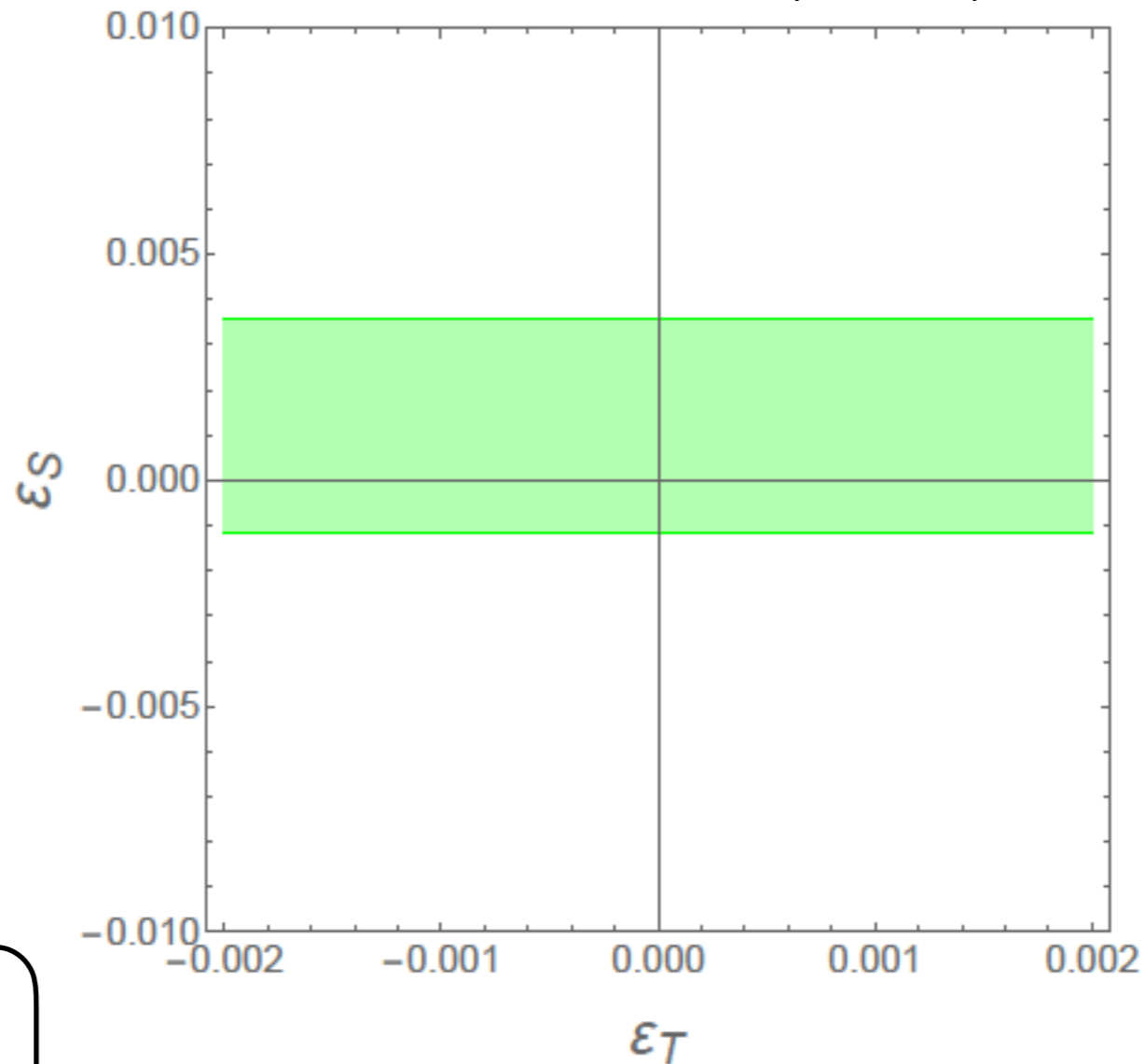
$0^+ \rightarrow 0^+$ (b_F)



$$-1.0 \times 10^{-3} < g_S \epsilon_S < 3.2 \times 10^{-3}$$

CURRENT

$\epsilon_{S,T}$ @ $\mu = 2 \text{ GeV (MS-bar)}$



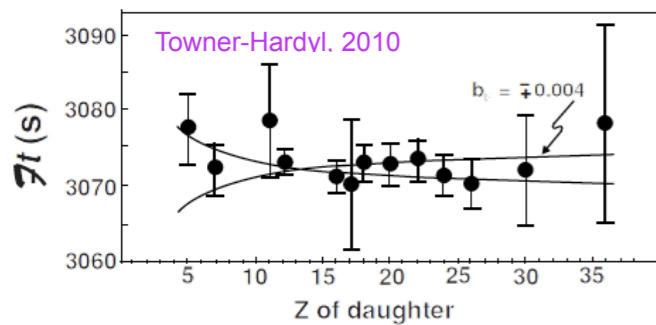
$$g_S = 1.01(10)$$

$$g_T = 0.99(4)$$

Bhattacharya et al (PNDME)
2018, to appear

Probing $\epsilon_{S,T}$ couplings

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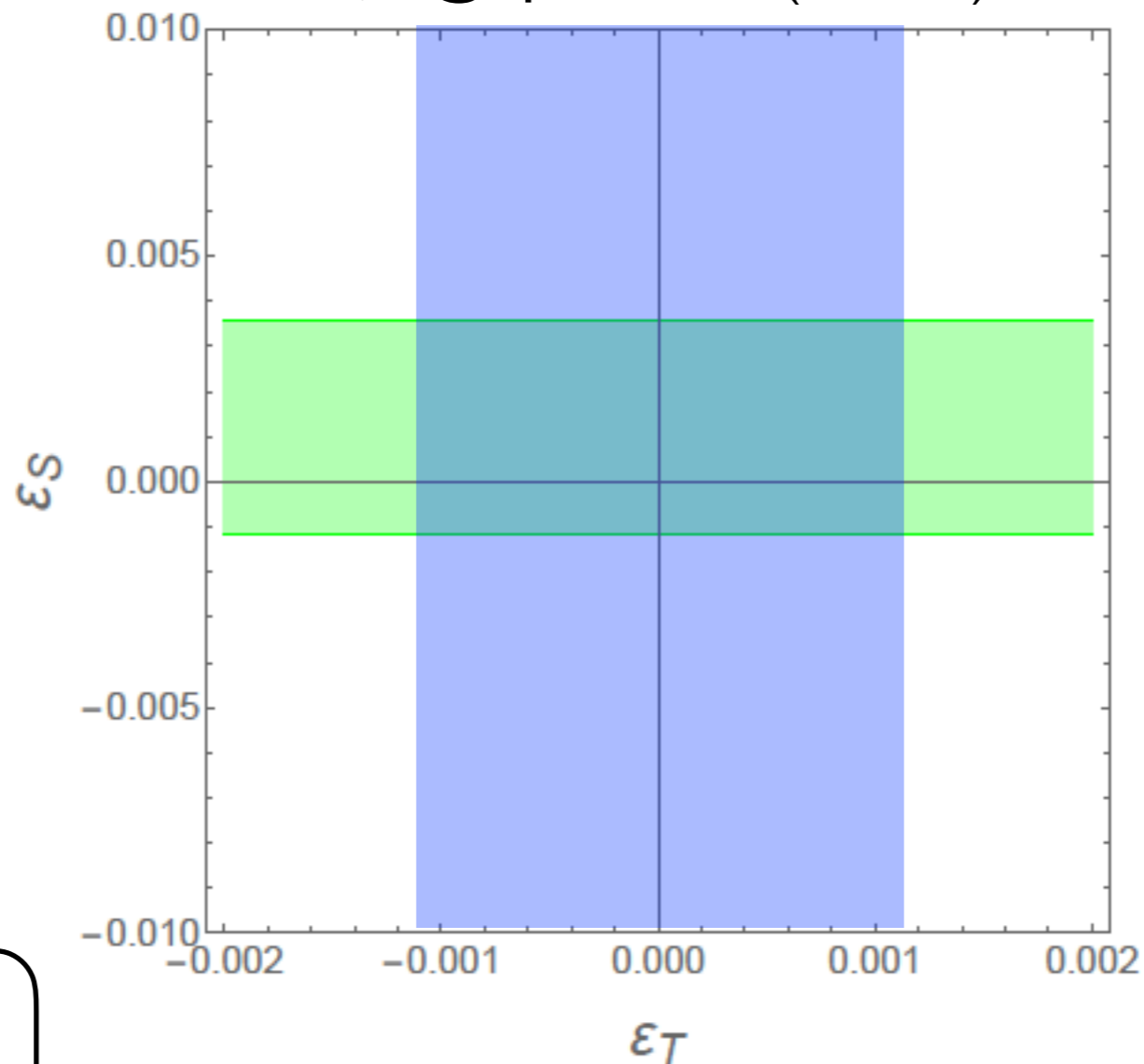
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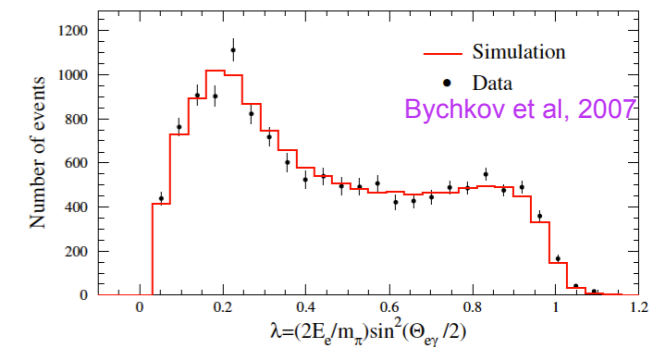
Bhattacharya et al (PNDME)
2018, to appear

CURRENT

$\epsilon_{S,T}$ @ $\mu = 2$ GeV (MS-bar)



$\pi \rightarrow e \nu \gamma$

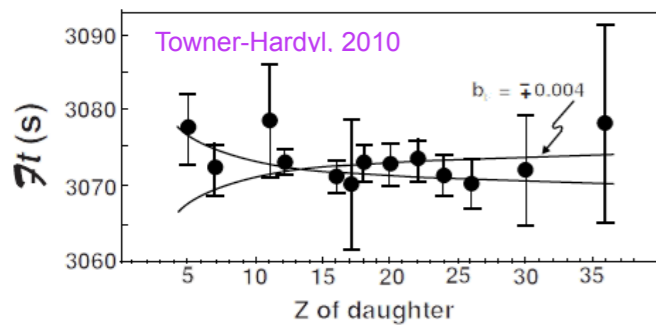


$$-2.0 \times 10^{-4} < f_T \epsilon_T < 2.6 \times 10^{-4}$$

$$f_T = 0.24(4)$$

Probing $\epsilon_{S,T}$ couplings

$0^+ \rightarrow 0^+$ (b_F)



$$-1.0 \times 10^{-3} < g_S \epsilon_S < 3.2 \times 10^{-3}$$

LHC 20 fb^{-1}
 @ 8 TeV

Gonzalez-Alonso 2013
 Gonzalez-Alonso,
 Naviliat-Cuncic,
 Severijns, 1803.08732

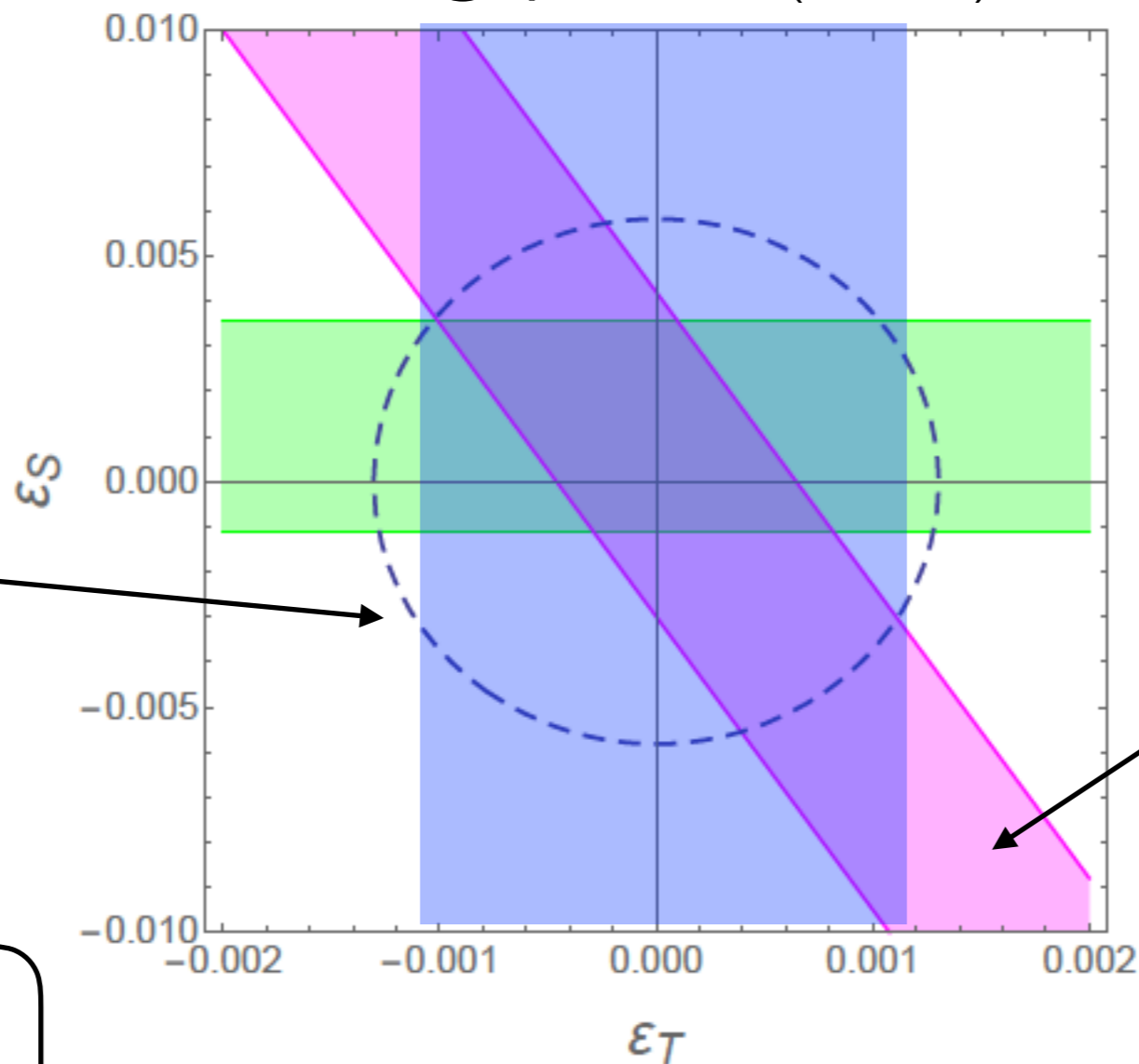
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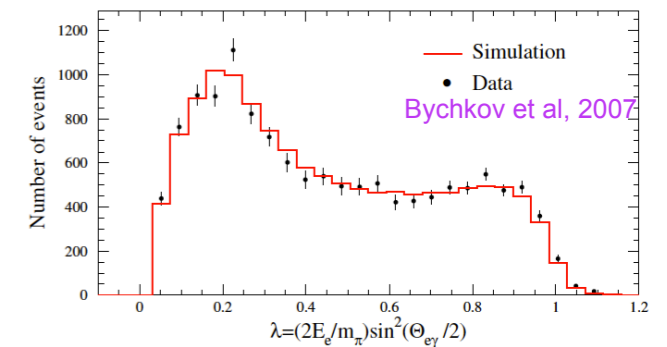
Bhattacharya et al (PNDME)
 2018, to appear

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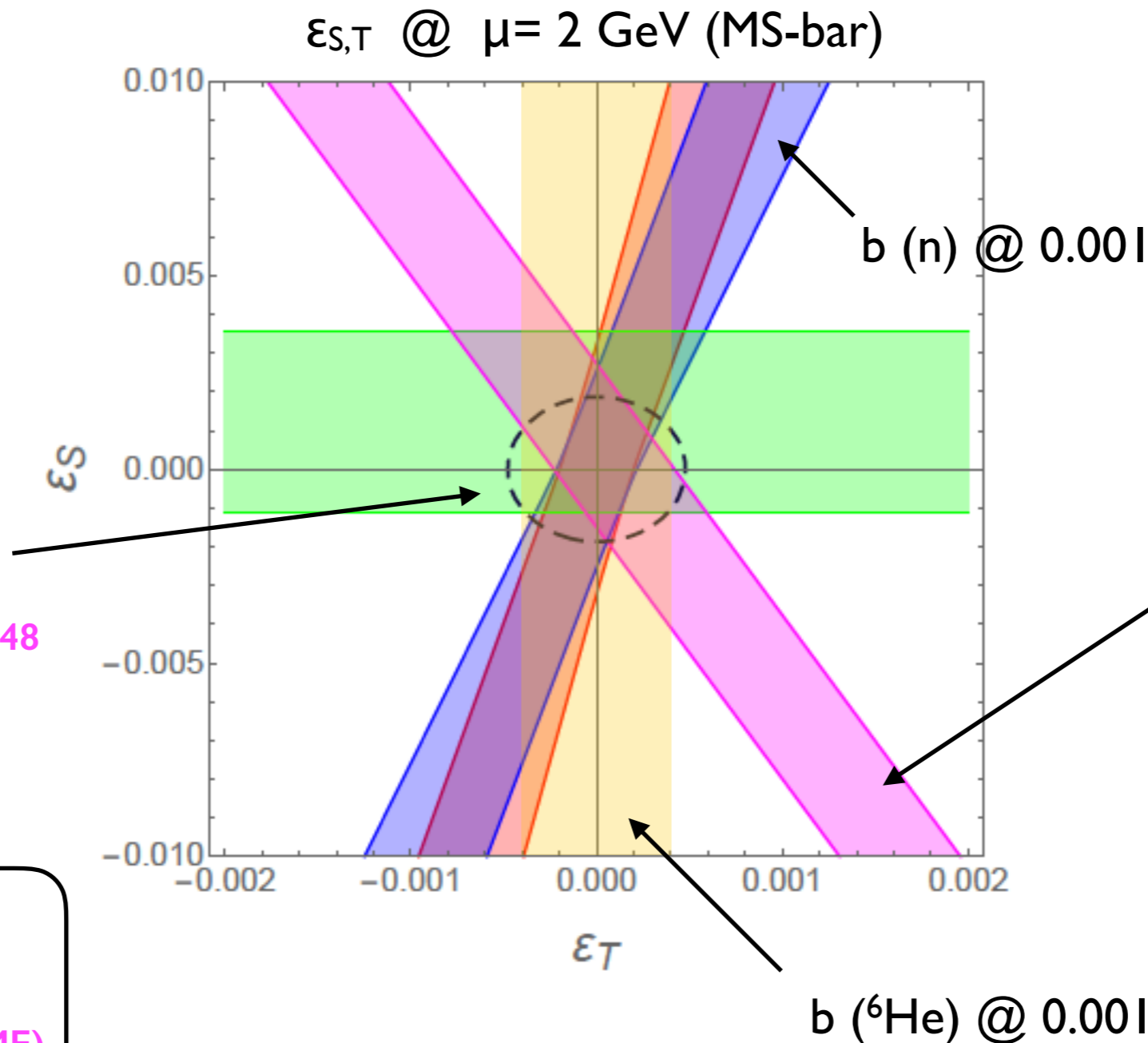
$$V_{ud}(0^+)/V_{ud}(n)$$

$$\delta\tau_n = 0.8 \text{ s}$$

Pattie-Hickerson-Young
 1309.2499

Probing $\epsilon_{S,T}$ couplings

FUTURE



LHC 300 fb⁻¹
@ 14 TeV

Bhattacharya et al | 10.6448

Alioli-Dekens-Girard-
Mereghetti- 1804.07407

$$g_S = 1.01(10)$$

$$g_T = 0.99(4)$$

Bhattacharya et al (PNDME)
2018, to appear

Prospective beta
decay
measurements
competitive with
LHC ~5 years
from now, probing
mass scales
 $\Lambda_{S,T} \sim 5-10$ TeV

$$V_{ud}(0^+)/V_{ud}(n):$$

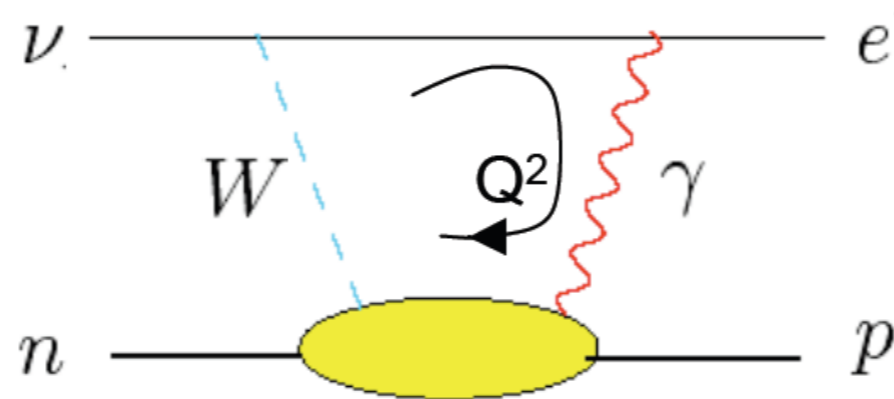
$$\delta A/A \sim 0.1\%$$

$$\delta\tau_n = 0.3 \text{ s}$$

Pattie-Hickerson-Young
1309.2499

Looking ahead

- The next frontier in beta decays will likely include:
 - $\delta\tau_n \sim 0.1s$ (UCNT2, ...)
 - $<0.1\%$ precision in neutron and nuclear correlation coefficients (PERC,...)
 - Improved calculations of radiative corrections^{**}: dispersive methods and lattice QCD (first results for meson decays)



**** This is currently the dominant contribution to V_{ud} error from $0^+ \rightarrow 0^+$:
 $\Delta_R = (2.38 \pm 0.4)\%$
[Marciano-Sirlin 2005]**

τ couplings to light quarks:

$$(\epsilon_\alpha)^{d\tau}$$

Based on ongoing work with Adam Falkowski, Martin Gonzalez-Alonso, Antonio Rodriguez-Sanchez

Special thanks to Antonio Rodriguez-Sanchez for input on the slides

PRELIMINARY RESULTS

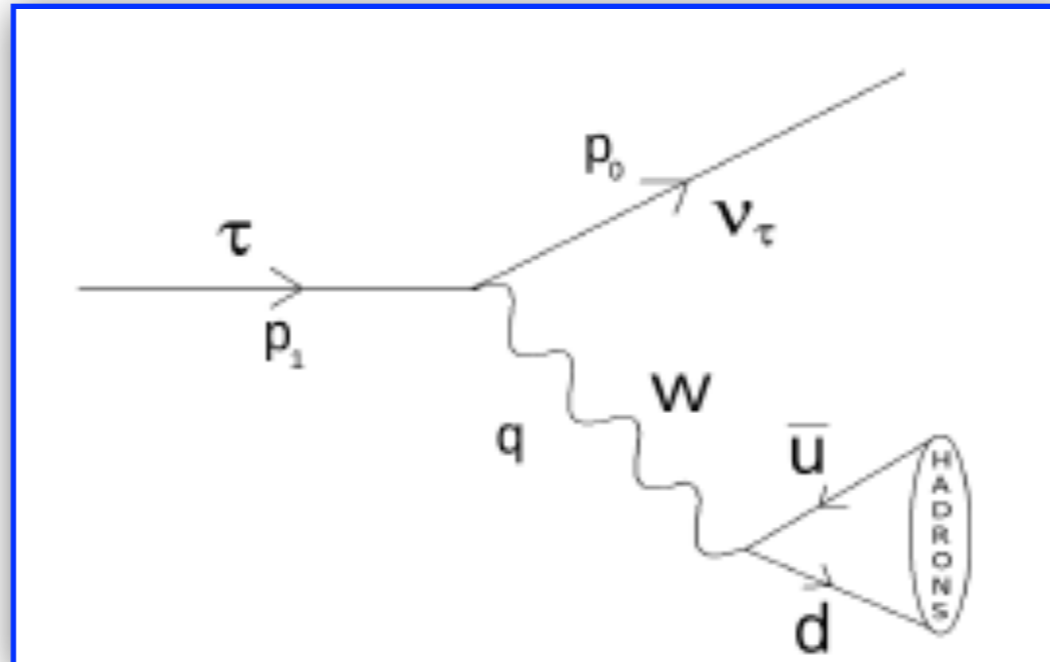
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Hadronic tau decays



$$\frac{d\Gamma_{BSM}(s) - d\Gamma_{SM}(s)}{d\Gamma_{SM}} = \sum a_i(s) \epsilon_i^{d\tau}$$

- Experimental precision at sub-% level
- Theory:
 - **Exclusive decays**: requires decay constants, form-factors
 - **Inclusive**: requires spectral functions. Use “quark-hadron duality”

Exclusive processes (I)

- One-meson decay: $\tau \rightarrow \pi \nu_\tau$

$$\Gamma(\tau^- \rightarrow \pi^- \nu_\tau) = \frac{m_\tau^2 f_\pi^2 G_F^{(e)2} |V_{ud}^{(e)}|^2}{16\pi} (1 + \delta_{RC}^\pi) (1 + 2(\epsilon_L^{d\tau} - \epsilon_L^{de} - \epsilon_R^{d\tau} - \epsilon_R^{de} - \frac{B_0}{m_\tau} \epsilon_P^{d\tau}))$$

f_π : FLAG 2017 (and refs therein)

δ_{RC} : Dekker-Finkemeier 1994 and VC-Rosell 2007

$$\epsilon_L^{d\tau} - \epsilon_L^{de} - \epsilon_R^{d\tau} - \epsilon_R^{de} - \frac{B_0}{m_\tau} \epsilon_P^{d\tau} = -(1.5 \pm 6.7) \cdot 10^{-3}$$

Error dominated by f_π (2x exp. and 5x rad. corr)

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Error dominated by f_π (2x exp. and 5x rad. corr)

- Two-meson decay: $\tau \rightarrow \eta \pi \nu_\tau$ suppressed in the SM

$$a_s(s) = \mathcal{O}\left(\frac{m_\tau}{m_u - m_d}\right) \rightarrow \epsilon_s \approx -(2 \pm 7) \cdot 10^{-3}$$

Graces et al 1708.07802

Exclusive processes (2)

- Two-meson decay: $\tau \rightarrow \pi\pi V_\tau$

$$\frac{d\Gamma_{exp}(s)}{ds} = \frac{d\Gamma_{SM}(s)}{ds} [1 + 2(\epsilon_L^{d\tau} + \epsilon_R^{d\tau} - \epsilon_L^{de} - \epsilon_R^{de}) + a_T(s)\epsilon_T]$$

Known at
(sub)% level

Exclusive processes (2)

- Two-meson decay: $\tau \rightarrow \pi\pi V_\tau$

Tensor FF: use resonance saturation
(shape) + LQCD (normalization)

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Known at
(sub)% level

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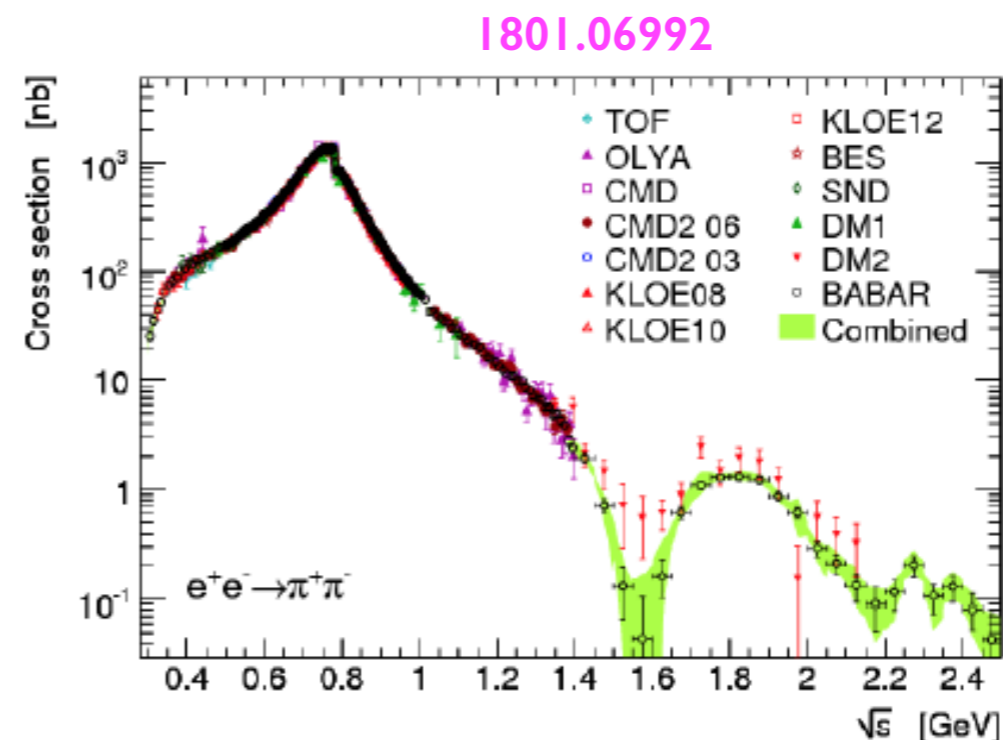
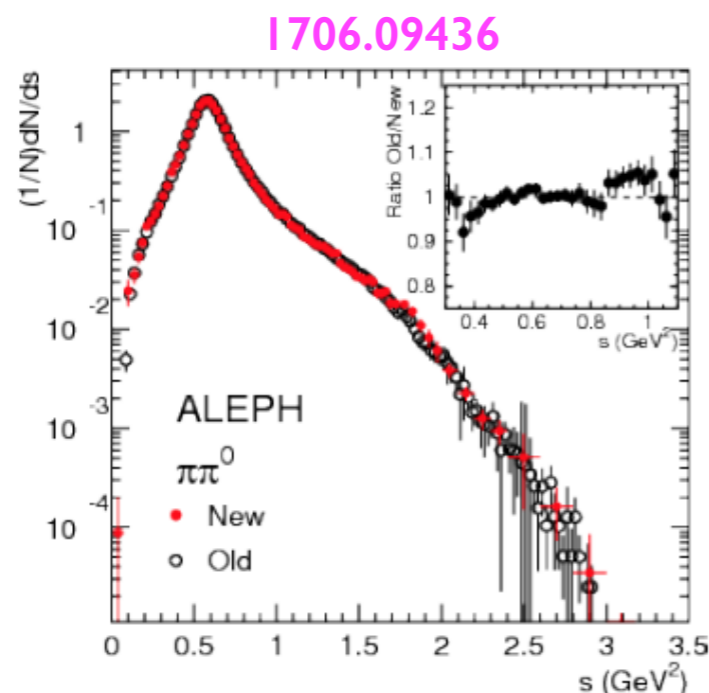
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Known at (sub)% level

Requires $F_V^\tau(s)$. Use $F_V^{e^+e^-}(s) = F_V^\tau(s) \times (1 + \delta_{IB})$

$e^+e^- \rightarrow \pi^+\pi^-$ insensitive to new physics (s/Λ^2 effect)



Exclusive processes (2)

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$e^+e^- \rightarrow \pi^+\pi^-$ insensitive to new physics (s/Λ^2 effect)

- Use integral constraint: $\pi\pi$ contribution to the HVP for $(g-2)_\mu$

Davier et al
1312.1501,
1706.09436

$$\frac{a_\mu^\tau - a_\mu^{ee}}{2 a_\mu^{ee}} = \epsilon_L^{d\tau} - \epsilon_L^{de} + \epsilon_R^{d\tau} - \epsilon_R^{de} + 0.64 \epsilon_T^{d\tau} = 0.0089(44)$$

Inclusive processes: generalities

- Total widths into “V” and “A” final states related to **spectral functions**

$$d\Gamma_V(s) = f_{VV}(s)(1 + 2\epsilon_{L+R}^T - 2\epsilon_{L+R}^e) \text{Im} \Pi_{VV}(s) + \epsilon_T f_{VT}(s) \frac{\text{Im} \Pi_{VT}(s)}{m_\tau}$$

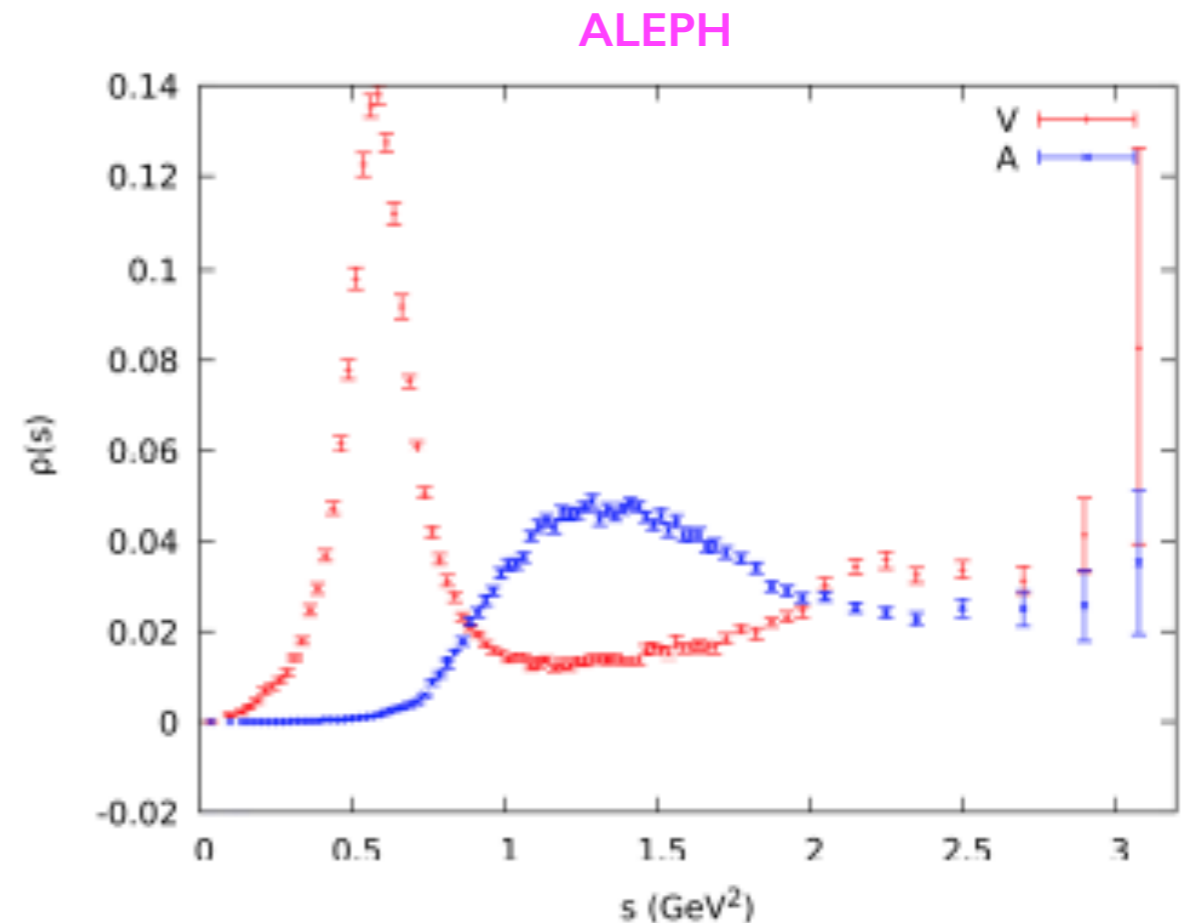
$$d\Gamma_A(s) = f_{AA}(s)(1 + 2\epsilon_{L-R}^T - 2\epsilon_{L+R}^e) \text{Im} \Pi_{AA}(s)$$

$s > 4m_\pi^2$

$$\Pi_{ij}(q) \sim \int dq e^{iqx} \langle 0 | T(J_i(x) J_j(0)) | 0 \rangle$$

$$\text{Im} \Pi_{ij}(s) \equiv \pi \rho_{ij}(s)$$

↑
Spectral functions



Inclusive processes: generalities

- Total widths into “V” and “A” final states related to **spectral functions**

$$d\Gamma_V(s) = f_{VV}(s)(1 + 2\epsilon_{L+R}^T - 2\epsilon_{L+R}^e) \text{Im } \Pi_{VV}(s) + \epsilon_T f_{VT}(s) \frac{\text{Im } \Pi_{VT}(s)}{m_\tau}$$

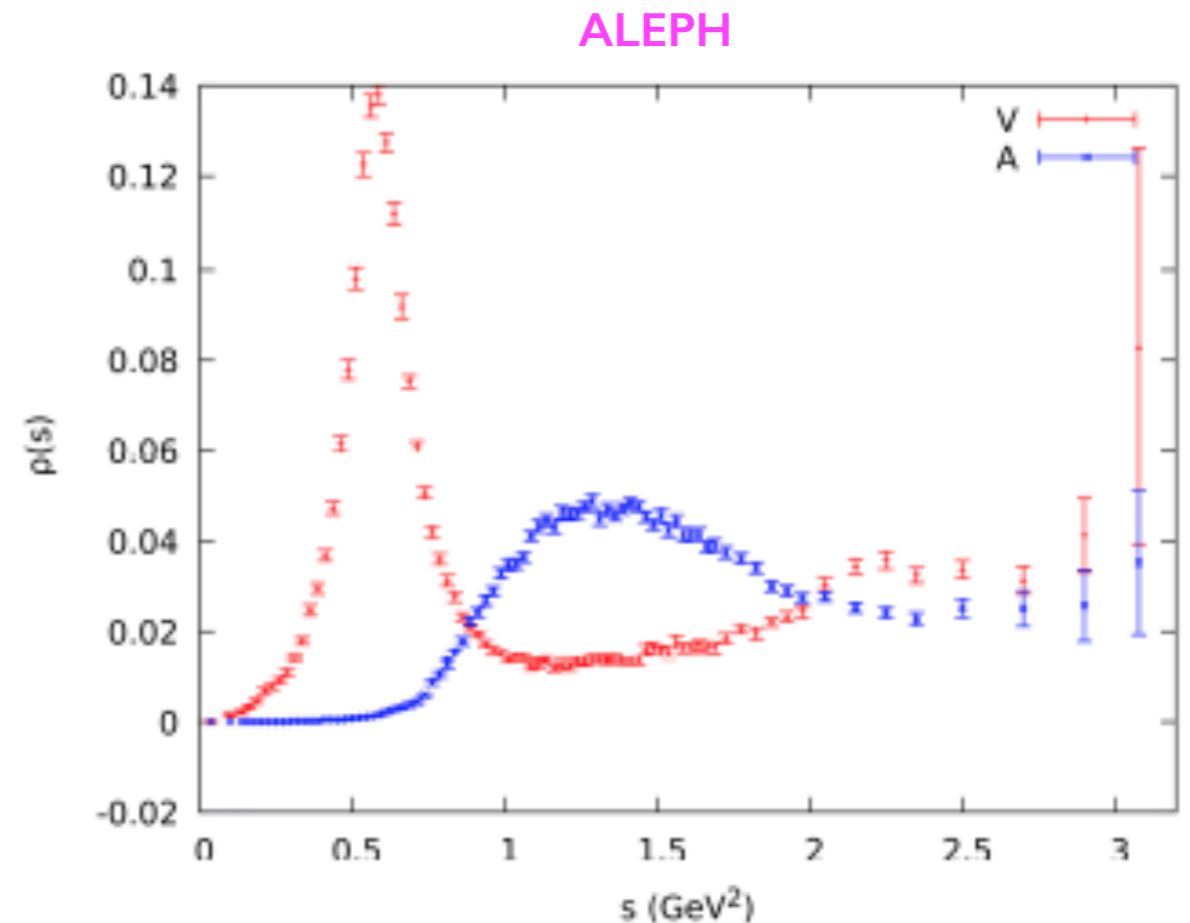
$$d\Gamma_A(s) = f_{AA}(s)(1 + 2\epsilon_{L-R}^T - 2\epsilon_{L+R}^e) \text{Im } \Pi_{AA}(s)$$

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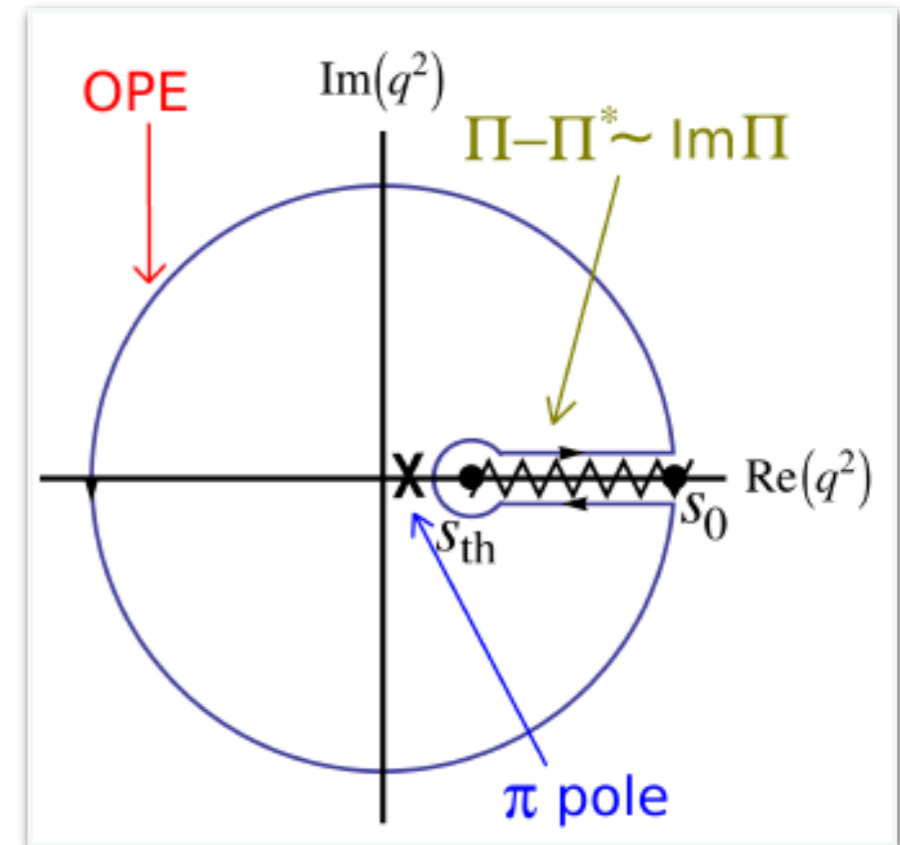
Spectral functions




Inclusive processes: method

- Use Cauchy's theorem for $\omega(s)\Pi(s)$ on the pac-man contour 🍷
- $\Pi(s) \rightarrow \Pi_{\text{OPE}}(s)$ on the circle
- Method used to successfully extract SM parameters ($\alpha_s, m_s, \text{chiral LECs}$). Here put constraints on new physics

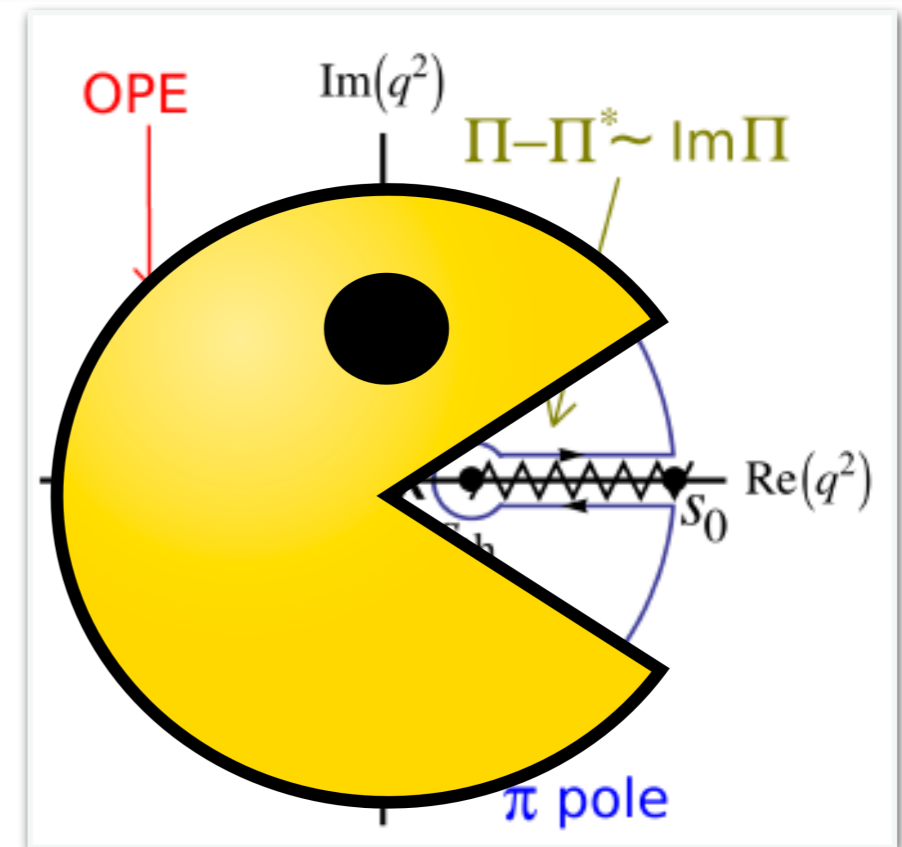
$$\Pi^{\text{OPE}}(Q^2 = -q^2) = \sum_i c_i(\mu, Q^2) \frac{\mathcal{O}_{i,D}(\mu)}{Q^D}$$



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$$\Pi^{\text{OPE}}(Q^2 = -q^2) = \sum_i c_i(\mu, Q^2) \frac{\mathcal{O}_{i,D}(\mu)}{Q^D}$$



$$\underbrace{\int_{s_{th}}^{s_0} \frac{ds}{s_0} \omega(s) \text{Im} \Pi_{V\pm A}^{(1+0)}}_{\text{Experiment-BSM}(\epsilon) = \text{QCD}} \pm 2\pi \frac{f_\pi^2}{s_0} \omega(m_\pi^2) = \frac{i}{2} \oint_{|s|=s_0} \frac{ds}{s_0} \omega(s) \Pi_{V\pm A}^{(1+0), \text{OPE}} + \delta_{DV, V\pm A}^{(\omega)}(s_0)$$

Duality Violation: $\Pi \neq \Pi_{\text{OPE}}$

Inclusive processes: results

- Four weakly correlated constraints
- **V+A**: $\omega(s)=1$, $\omega(s)=\omega_{\text{kin},\tau}(s)$

$$\begin{aligned}\epsilon_{L+R}^{d\tau} - \epsilon_{L+R}^{de} - 0.89\epsilon_R^{d\tau} + 0.73\epsilon_T^{d\tau} &= (8.5 \pm 8.5) \cdot 10^{-3} \\ 0.72(\epsilon_{L+R}^{d\tau} - \epsilon_{L+R}^{de}) - 0.56\epsilon_R^{d\tau} + \epsilon_T^{d\tau} &= (3.2 \pm 11.8) \cdot 10^{-3}\end{aligned}$$

OPE side dominated by perturbative term. Use α_s from lattice QCD

- **V-A**: $\omega(s)=1-s/s_0$, $\omega(s)=(1-s/s_0)^2$ [to reduce duality violations].

$$\begin{aligned}0.15(\epsilon_{L+R}^{d\tau} - \epsilon_{L+R}^{de}) + 0.46\epsilon_R^{d\tau} + \epsilon_T^{d\tau} &= (0.8 \pm 7.6) \cdot 10^{-3} \\ 0.15(\epsilon_{L+R}^{d\tau} - \epsilon_{L+R}^{de}) + 0.29\epsilon_R^{d\tau} + \epsilon_T^{d\tau} &= (0.8 \pm 1.5) \cdot 10^{-3}\end{aligned}$$

OPE side has no perturbative term. Condensates from NDA and kaon physics + chiral symmetry

Constraints from τ decays: summary

$$\begin{pmatrix} \epsilon_L^{d\tau} - \epsilon_L^{de} + \epsilon_R^{d\tau} - \epsilon_R^{de} \\ \epsilon_R^{d\tau} \\ \epsilon_S^{d\tau} \\ \epsilon_P^{d\tau} \\ \epsilon_T^{d\tau} \end{pmatrix} = \begin{pmatrix} 9.6 \pm 6.1 \\ 1.3 \pm 9.0 \\ -2.0 \pm 7.0 \\ -6.1 \pm 11.5 \\ -1.1 \pm 3.8 \end{pmatrix} \times 10^{-3}$$

Connection to “SM-EFT”

$$\epsilon_L^{d\tau} - \epsilon_L^{de} = \underbrace{\delta g_L^{W\tau} - \delta g_L^{We}}_{\text{Independently constrained by EWPO}} - [c_{\ell q}^{(3)}]_{\tau\tau 11} + \underbrace{[c_{\ell q}^{(3)}]_{ee 11}}_{\text{Independently constrained by EWPO}}$$

Independently constrained by EWPO

Independently constrained by EWPO

$$\epsilon_R^{d\tau} = \epsilon_R^{de} = \underbrace{\delta g_R^{Wq_1}}_{\text{Independently constrained by EWPO}}$$

EWPO = A. Falkowski et al,
1706.03783

Independently constrained by EWPO

$$\epsilon_{S,P}^{d\tau} = -\frac{1}{2} [c_{\ell e q u} \pm c_{\ell e d q}]_{\tau\tau 11}^*$$

$$\epsilon_T^{d\tau} = -\frac{1}{2} [c_{\ell e q u}^{(3)}]_{\tau\tau 11}^*$$

Connection to “SM-EFT”

$$\epsilon_L^{d\tau} - \epsilon_L^{de} = \underbrace{\delta g_L^{W\tau} - \delta g_L^{We}}_{\text{Independently constrained by EWPO}} - [c_{lq}^{(3)}]_{\tau\tau 11} + \underbrace{[c_{lq}^{(3)}]_{ee 11}}_{\text{Independently constrained by EWPO}}$$

$$\epsilon_R^{d\tau} = \epsilon_R^{de} = \underbrace{\delta g_R^{Wq1}}_{\text{Independently constrained by EWPO}}$$

EWPO = A. Falkowski et al, 1706.03783

$$\epsilon_{S,P}^{d\tau} = -\frac{1}{2} [c_{lequ} \pm c_{ledq}]_{\tau\tau 11}^*$$

$$\epsilon_T^{d\tau} = -\frac{1}{2} [c_{lequ}^{(3)}]_{\tau\tau 11}^*$$

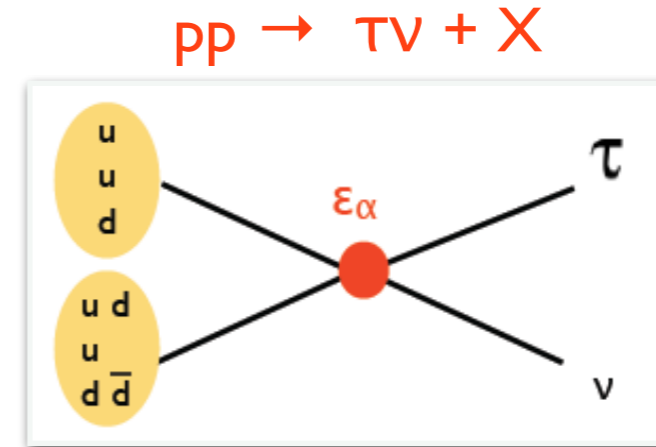
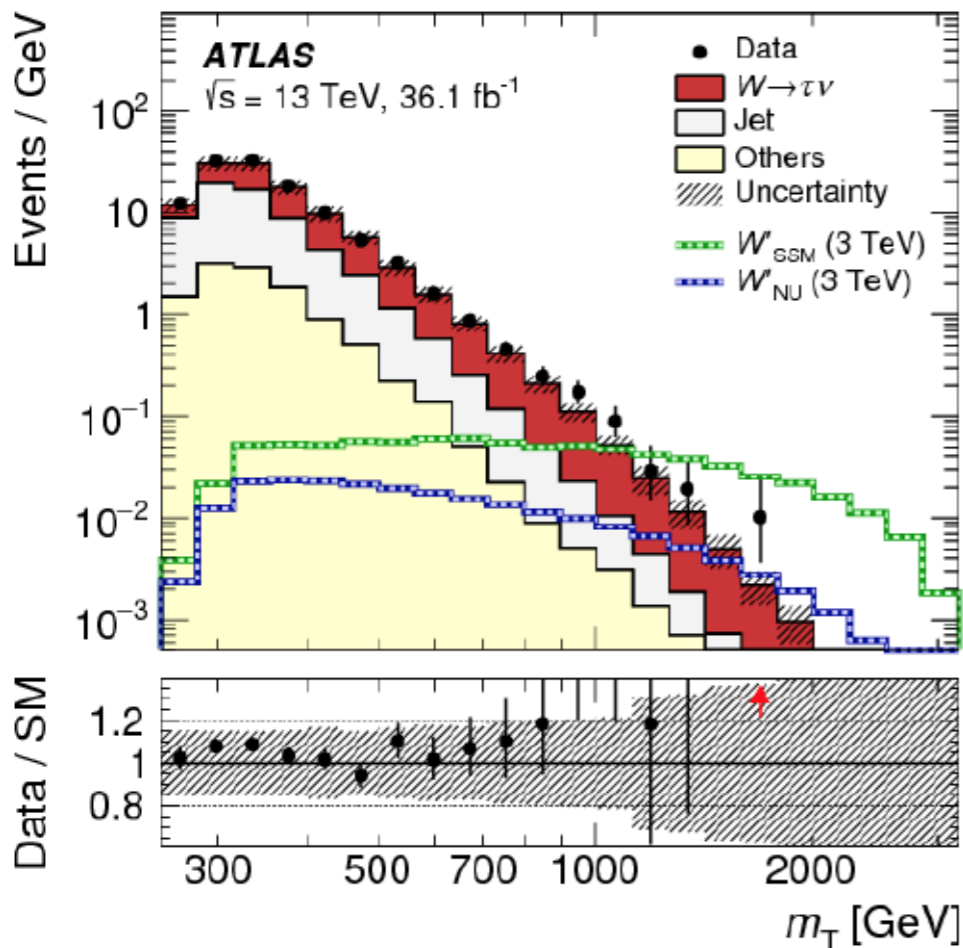
New low-energy constraints on SM-EFT couplings:

$$[c_{lq}^{(3)}, c_{lequ}, c_{ledq}, c_{lequ}^{(3)}]_{\tau\tau 11} = (1.0 \pm 2.9, 0.66 \pm 0.71, -0.43 \pm 0.66, -0.02 \pm 0.82) \times 10^{-2}$$

Constraints from the LHC

- Similar to electron case:

1801.06992



Coefficient	ATLAS $\tau \nu$	Hadronic τ decays
$[c_{\ell q}^{(3)}]_{\tau\tau 11}$	[0.0, 1.1]	[-12.8, 0.0]
$[c_{\ell equ}]_{\tau\tau 11}$	[-4.6, 4.6]	[-3.9, 8.6]
$[c_{\ell edq}]_{\tau\tau 11}$	[-4.6, 4.6]	[-7.7, 4.8]
$[c_{\ell equ}^{(3)}]_{\tau\tau 11}$	[-2.7, 2.7]	[-8.8, 1.8]

95% CL intervals (in 10^{-3} units) for the Wilson coefficients at $\mu = 1 \text{ TeV}$

Impact on gauge vertex corrections

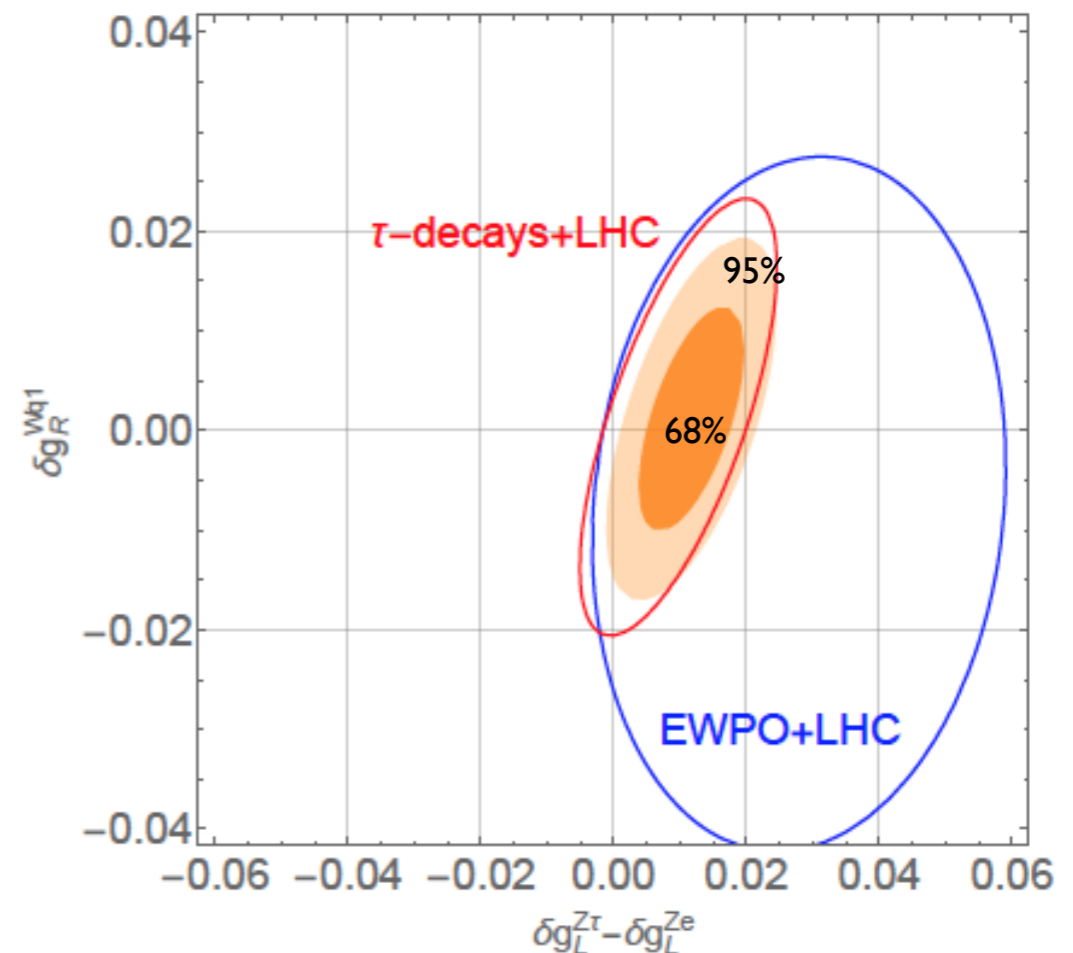
- LHC input constrains 4-fermion “L” couplings at 10^{-3} level

$$\epsilon_L^{d\tau} - \epsilon_L^{de} = \delta g_L^{W\tau} - \delta g_L^{We} - \underbrace{[c_{\ell q}^{(3)}]_{\tau\tau 11} + [c_{\ell q}^{(3)}]_{ee 11}}_{\text{constrained by LHC at 0.1\% level}}$$

$$\epsilon_R^{d\tau} = \epsilon_R^{de} = \delta g_R^{Wq_1}$$

Our analysis +
Greljo-Marzocca
1704.09015

- Hadronic tau decays become a **new %-level probe of lepton flavor universality of vertex corrections**



Impact on gauge vertex corrections

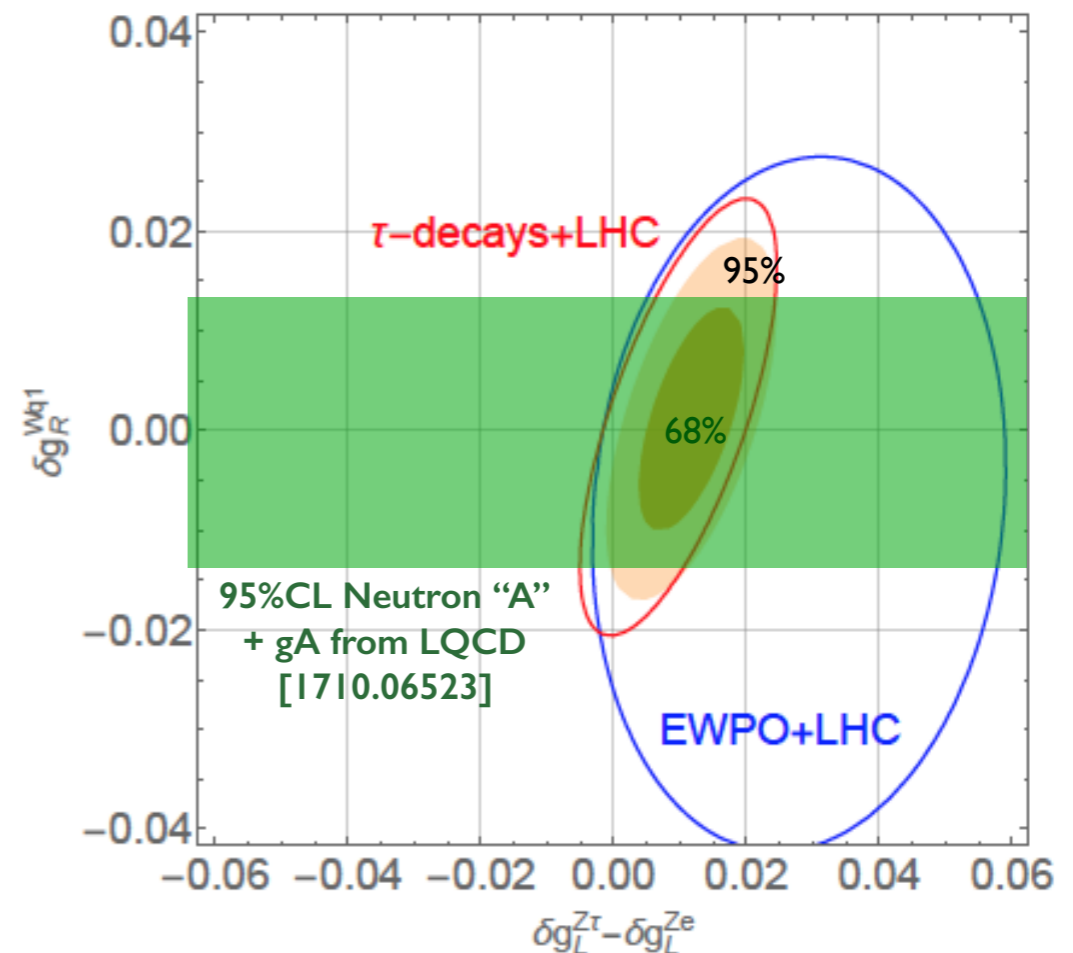
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$$\epsilon_R^{d\tau} = \epsilon_R^{de} = \delta g_R^{Wq1}$$

Our analysis +
Greljo-Marzocca
1704.09015

- Hadronic tau decays become a **new %-level probe of lepton flavor universality of vertex corrections**



Summary

- CC transitions with sufficient th. and expt. precision (β decays at $< 0.1\%$, τ decays at $< 1\%$) provide “broad band” probe of new physics
- Discovery potential depends on the underlying model. However, for heavy mediators, EFT shows that a discovery window exists well into the LHC era (simple examples: ϵ_L - ϵ_R and ϵ_S - ϵ_T plots)
- In general, combination of low- and high-E measurements can
 - provide stronger constraints on certain couplings
 - break coupling degeneracies
 - reduce “flat directions” in space of effective couplings
- Example of global analysis in next talk