

Center for Experimental Nuclear Physics and Astrophysics (CENPA) University of Washington



Cyclotron radiation spectroscopy to search for tensor currents

A. Garcia Mainz Institute for Theoretical Physics "PVES18" April, 2018



Nuclear beta decay: beyond V-A?

$$H_{V,A} = \sum_{i=V,A} \overline{\Psi}_f O_i^{\mu} \Psi_0 \left[(C_i + C_i') \overline{e}^L O_{i,\mu} v_e^L + (C_i - C_i') \overline{e}^R O_{i,\mu} v_e^R \right]$$

$$O_i^{\mu} = \begin{cases} \gamma^{\mu} & i = V \\ \gamma^{\mu} \gamma_5 & i = A \end{cases}$$

$$H_{S,T} = \sum_{i=S,T} \overline{\Psi}_f O_i \ \Psi_0 [(C_i + C_i') \overline{e}^R O_i v_e^L + (C_i - C_i') \overline{e}^L O_i v_e^R]$$

$$O_i^{\mu} = \begin{cases} 1 & i = S \\ \sigma^{\mu\nu} & i = T \end{cases}$$

Nuclear beta decay: beyond V-A?

- Will not address right-handed currents.
- Existing good limits on scalar currents.
- Will concentrate on tensor.

$$H_{A} = \overline{\Psi}_{f} \gamma^{\mu} \gamma_{5} \Psi_{0} \begin{bmatrix} (2C_{A}) \ \bar{e}^{L} \gamma_{\mu} \gamma_{5} \nu_{e}^{L} \end{bmatrix} + \qquad \text{chirality flipping} \\ \overline{\Psi}_{f} \sigma^{\mu\nu} \Psi_{0} \begin{bmatrix} (C_{T} + C_{T}') \ \bar{e}^{R} \sigma_{\mu\nu} \nu_{e}^{L} + (C_{T} - C_{T}') \ \bar{e}^{L} \sigma_{\mu\nu} \nu_{e}^{R} \end{bmatrix}$$



Standard Model

Charged weak current in SM only sensitive to *L*:

 $\bar{\psi}_e O^\mu \psi_\nu = \overline{\psi}_e^L \gamma^\mu \psi_\nu^L$

Sorting this out took much experimental effort and ingenuity to come out of confusing times





From "The 7% solution" article in Surely you are joking, Mr. Feynman!



When I came back to the United States, I wanted to know what the situation was with beta decay. I went to Professor Wu's laboratory at Columbia, and she wasn't there, spinning to the left in the beta decay, came out on the right in some cases. Nothing fit anything. When I got back to Caltech, I asked some of the experimenters what the situation was with beta decay. I remember three guys, Hans Jensen, Aaldert Wapstra, and Felix Boehm, sitting me down on a little stool, and starting to tell me all these facts: experimental results from other parts of the country, and their own experimental results. Since I knew those guys, and how careful they were, I paid more attention to their results than to the others. Their results, alone, were not so inconsistent; it was all the others plus theirs. Finally they get all this stuff into me, and they say, "The situation is so mixed up that even some of the things they've established for years are being questioned - such as the beta decay of the neutron is S and T. It's so messed up. Murray says it might even be V and A."

I jump up from the stool and say, "Then I understand EVVVVVERYTHING!"

Chirality-flipping as means of detection of new physics.



⁶He β -v angular correlation at CENPA

Y. Bagdasarova¹, K. Bailey², X. Fléchard³, A. Garcia^{1,*}, R. Hong¹, A. Knecht⁴, A. Leredde², E. Liennard³, P. Mueller^{2,*}, O. Naviliat-Cuncic⁵, T. O'Connor², M. Sternberg¹, H.E. Swanson¹, F. Wauters¹

¹UW, ²ANL, ³LPC-CAEN(France), ⁴PSI, ⁵NSCL

*Spokepersons

• Goal: measure "little a" to 0.1% in ⁶He

- pure Gamow-Teller decay
- sensitive to tensor couplings
- simple nuclear and atomic structure
- Laser cooling and trapping to prepare ⁶He source
- Detect electron and ⁶Li in coincidence
- ∆E-E scintillator system for electron detection (energy, start of time-of-flight)
- Micro-channel plate detector for ⁶Li detection (position, time-of-flight)



⁶He Trap/Detector Chamber



⁶He β -v angular correlation at CENPA

⁶He Source: Reliable source of ~10¹⁰ ⁶He's/s in low-background A. Knecht et al. NIM A. **660**, 43 (2011)

Laser trapping and detection systems: All systems working after much development





Status:

- Now efficiencies good for little-*a* statistics at the 1% level in 3 days.
- Aiming for $\Delta a/a < 1\%$ in near future.
- Presently working on systematic uncertainties.

Charge distribution of ⁶Li ions in ⁶He decay: a simple problem? Phys. Rev. A **96**, 053411 (2017)

Helium electronic structure + sudden approximation. Very simple, but...



TOF between fast beta and ⁶Li ions

Calculated vs Measured ⁶Li ion charge fractions in % for ⁶He decays



Connection to LHC data via EFT calculations

Cirigliano et al. PPNP **71**, 93 (2013)

LHC (I): contact interactions

- If the new physics originates at scales $\Lambda > \text{TeV}$, then can use EFT framework at LHC energies
- The effective couplings ε_{α} contribute to the process $p p \rightarrow e v + X$



differential cumulative CMS Prelimin 2010 20107 **CMS Preliminary** L dt = 1.03 th 010 No excess ×106 Va = 7 Tev = 7 TeV £105 events in 9104 $m_T \equiv \sqrt{2E_T^e E_T^\nu (1 - \cos \Delta \phi_{e\nu})}$ transverse mass 10³ 10 10² distribution: 10 10 bounds on \mathcal{E}_{α} 101 101 10-2 10-2 200 400 600 800 1000 1200 1400 200 400 600 800 1000 1200 1400 m_T(GeV) m_T(GeV)

Precision beta decay versus others: Can "precision" compete with "energy"?

Bhattacharya et al. Phys. Rev. D **94**, 054508 (2016)





Detect little *b*

Is it possible to reach into $b < 10^{-3}$?

Ongoing efforts in neutron beta decay:

- Nab aiming at $b \approx 3 \times 10^{-3}$.
- PERC, $b \approx 1 \times 10^{-3}$.

Nab:



Figure 9. Principle of the Nab spectrometer in the vertical orientation. Magnetic field lines (shown in blue) electrodes (light green boxes), and coils (not shown) possess cylindrical symmetry around the vertical axis. The neutron beam is unpolarized for Nab, but can be polarized for later experiments.

PERC/Vienna: *RxB* spectrometer to measure *b* NIM A **701**, 254 (2013)



Fig. 5. The design of the $R\times B$ drift spectrometer at the end of PERC, and the simulated trajectories of $e^-/p^+.$

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An experiment using ⁶He could confirm a signal and potentially move beyond



PERC/Vienna: *RxB* spectrometer to measure *b*

NIM A **701**, 254 (2013)



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6He at NSCL: Naviliat-Cuncic et al.



6He at NSCL: Naviliat-Cuncic et al.

Beam ON/OFF sequence Csl-run145-segs:0,1,2-Ew:1000-5000 10⁵ Sample of experimental 10⁴ spectra ⁶He decay 10^{3} Beam induced background Ambient background 11 12 3 5 6 8 9 10 Time (s)

No traces of "short lived" beam induced background



We collected typically 10⁷ events in 1 h run

 We define 7 slices between 3 and 5 s, with 10⁶ events in each spectrum.

~100 spectra with Csl(Na)

~100 spectra with Nal(TI)

PRL 114, 162501 (2015)

Selected for a Viewpoint in *Physics* PHYSICAL REVIEW LETTERS

week ending 24 APRIL 2015

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Single-Electron Detection and Spectroscopy via Relativistic Cyclotron Radiation

D. M. Asner,¹ R. F. Bradley,² L. de Viveiros,³ P. J. Doe,⁴ J. L. Fernandes,¹ M. Fertl,⁴ E. C. Finn,¹ J. A. Formaggio,⁵
D. Furse,⁵ A. M. Jones,¹ J. N. Kofron,⁴ B. H. LaRoque,³ M. Leber,³ E. L. McBride,⁴ M. L. Miller,⁴ P. Mohanmurthy,⁵
B. Monreal,³ N. S. Oblath,⁵ R. G. H. Robertson,⁴ L. J Rosenberg,⁴ G. Rybka,⁴ D. Rysewyk,⁵ M. G. Stemberg,⁴
J. R. Tedeschi,¹ T. Thümmler,⁶ B. A. VanDevender,¹ and N. L. Woods⁴

(Project 8 Collaboration)



Project 8 in a nutshell

Looking at Tritium decay to get v mass. Electrons emitted in an RF guide within an axial *B* field. Antenna at end detects cyclotron radiation.





 $\omega = \frac{qB}{F}$

Some details

Motion can be thought off as cyclotron orbits, axial oscillations and magnetron motion.

 $\omega_c : \omega_z : \omega_{mag} =$ ~ 1 : 4 × 10⁻³ : 2 × 10⁻⁵.







Longitudinal comp. of momentum decreases as *B* increases up to return point, z_{max} . Axial oscillations with ω_z .

Project 8 in a nutshell

Looking at Tritium decay to get v mass. Electrons emitted in an RF guide within an axial *B* field. Antenna at end detects cyclotron radiation.



$$\omega = \frac{qB}{E}$$



Why do we like the Project-8 technique for ⁶He?

- Measures beta energy at creation, before complicated energy-loss mechanisms.
- High resolution allows debugging of systematic uncertainties.
- Room photon or e scattering does not yield background.
- 6He in gaseous form works well with the technique.
- 6He ion-trap (shown by others to work) allows sensitivity higher than any other proposed.
- Counts needed not a big demand on running time.
 Time bins ~ 30 μs.



Project-8 technique



Power from a single electron orbiting in a magnetic field versus time and the frequency of the electron's orbit. The straight streaks correspond to the electron losing energy (and orbiting faster) as it radiates. The jumps correspond to the loss of energy when the electron collides with an atom or molecule. [Asner et al. [PRL **114**, 162501]

⁶He source: produced via ⁷Li(d,³He)⁶He







⁶He production: 10¹⁰ ⁶He/s delivered to clean lab in a stable fashion.

Knecht et al. NIM A 660, 43 (2011)

April 2018

Tensor via cyclotron radiation

⁶He's per sec

Research with the accelerator: ⁶He source [°]He [°]He [°]H beam [°]He [°]H beam [°]H beam

10^{10 6}He/s in clean lab in a stable fashion.

"Statistics for searching for new physics", compare decay densities to neutron sources:

UCN: 10^3 UCN/cc $\rightarrow \approx 1$ (decay/s)/cc

CN: 10^{10} CN/s cm2 $\rightarrow 2 \times 10^{5}$ CN/cc ≈ 200 (decay/s)/cc

⁶He: $\approx 2 \times 10^6$ (decay/s)/cc

Important for using CRES technique in an RF guide.

Emerging ⁶He little-*b* collaboration

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²Argonne National Lab,
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⁴Pacific Northwest National Laboratory
⁵Tulane University

• Goals:

- measure "little *b*" to better than 10^{-3} in ⁶He.
- Highest sensitivity to tensor couplings

Technique

- Use Cyclotron Emission Spectroscopy. Similar to Project 8 setup for tritium decay
- Need to extend the technique to higher energy betas and to a precision determination of a continuum spectrum.

We have put together a collaboration, written and submitted a proposal. Now kick-started by DOE and UW funds.

Detection of cyclotron radiation to search for chirality-flipping interactions and other applications

M. Fertl,¹ A. García,¹ M. Guigue,² D. Hertzog,¹ A. Hime,² P. Kammel,¹ A. Leredde,³ P. Müller,³ N. S. Oblath,² R. G. H. Robertson,¹ G. Rybka,¹ G. Savard,³ D. Stancil,⁴ H. E. Swanson,¹ B. A. VanDevender,² and A. R. Young⁵

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 ⁴Electrical Engineering Department, North Carolina State University, Raleigh, NC 27695
 ⁵Physics Department, North Carolina State University, Raleigh, NC 27695 (Dated: September 27, 2016)

We propose a sensitive search for non-Standard-Model chirality-flipping interactions by measuring the shape of the beta spectrum of ⁶He. We will apply the technique of cyclotron radiation emission spectroscopy (CRES) recently demonstrated by the Project 8 collaboration, extending its use to the broader range of electron energies of the ⁶He β decay. This proposal presents a phased approach to realize the goal of measuring the $b_{\rm Fierz}$ parameter to a precision of better than 10^{-3} . The first phase is aimed at demonstrating the validity of the technique for electrons in the few MeV range. The proposed test of the Standard Model in Phase II will have a sensitivity to new physics in a regime which exceeds the capabilities of the LHC both now and after the luminosity upgrade. Phase III is the most ambitious experiment proposed to date to detect chirality-flipping interactions.

We also intend to develop collaborations with groups that have traditionally used radioactive ion traps and could apply the technique for nuclear-structure related spectroscopy. In particular, the measurement of small Electron Capture branches from radioactive nuclei to set benchmarks for theoretical calculations of double-beta decay matrix elements.

An existing magnet will be re-purposed for the measurement. We ask for funds for RF electronics and data acquisition and for some vacuum equipment. We have put together a collaboration, written and submitted a proposal. Now kick-started by DOE and UW funds.

Phase I: proof of principle 2 GHz bandwidth. Show detection of cycl. radiation from 6He. Study power distribution.

Phase II: first measurement (b < 10⁻³) 6 GHz bandwidth. 6He and 19Ne measurements.

Phase III: ultimate measurement (*b* < 10⁻⁴) ion-trap for no limitation from geometric effect.

Mission for next three years

⁶He little-*b* measurement at Seattle

Goal: measure "little *b*" to 10⁻³ or better in ⁶He

RF guides

⁶He in

Stats not a problem.

RF amps

Starting construction during summer 2018.

Decay volume

vo cooler

2

⁶He little-b measurement at CENPA



⁶He little-b measurement at CENPA

Monte Carlo simulation of observation in Few days of running

Extracting little *b* vs. *B* field Few days of running each point (assumed $b_{MC} = 0.01$)



Obvious worry: efficiency depends on energy.



Cross sectional view of guide with electron orbit. For this radius there is a dead region shown by the white frame on the blue area.

Since blue area depends on energy there is a systematic distortion of the spectrum

Can be studied by varying the *B* field.

Obvious worry: efficiency depends on energy.

Monte Carlo simulation of observation in Few days of running

Radii vs. *B* field Can use this to check geometric effect



Additional tool for calibrations: $^{131m}Xe (t_{1/2} \approx 12 \text{ days})$

Conversion electrons $E_{\rm e}$ = 25, 129, 160 keV

- Studying versus B field allows determining the effect.
- Showing that all is understood with higher *E* electrons is a milestone to move forward.





We have extracted $\approx 10^5$ Becq. of 131m Xe.

Ready to test as soon as we have apparatus.



Need about 50 mCi of ¹³¹I (\rightarrow ^{131m}Xe with t_{1/2} \approx 8 days) (30 µCi of ¹³¹I is a safety concern)



Tensor via cyclotron radiation

Check on signature by measuring ¹⁴O and ¹⁹Ne:

Both ¹⁴O and ¹⁹Ne can be produced in similar quantities as ⁶He at CENPA.

¹⁴O as CO (T_{freeze} = 68 K) Previous work at Louvain and TRIUMF.

¹⁹Ne source developed at Princeton appropriate.



6He nuclear structure issues to reach $b < 10^{-3}$

Recoil order corrections and the SM contribution to little b



Dominant factor in recoil-order correction is interference between WM and GT:

$$R(E) \approx \frac{2m}{3M} \frac{\langle WM \rangle}{\langle \sigma \rangle} \left(2\frac{E}{m} - \frac{E_0}{m} - \frac{m}{E} \right)$$

Factor determined to $\sim 2\%$ by connection to γ decay of analogue in 6Li.

Radiative corrections



Model-independent Sirlin factor.

Other nuclear-structure issues? Need to be explored to reach beyond $b < 10^{-3}$

¹⁹Ne?

¹⁴O?

High precision analytical description of the allowed β spectrum shape

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Kazimierz Bodek and Dagmara Rozpedzik Marian Smoluchowski Institute of Physics, Jagiellonian University, 30-348 Cracow, Poland

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improved atomic corrections, an analytical description was presented of the allowed β spectrum shape accurate to a few parts in 10⁻⁴ down to 1 keV for low to medium Z nuclei, thereby extending the work by previous authors by nearly an order of magnitude.

Other worries: DAQ.

To register it all, need to take about 1 byte at 5 GHz.

About 1 Peta-byte/day !!

By triggering and recording only within a Δf of interest one can decrease it to 1 Tera-byte/day.

It is a concern of the Project 8 collaboration, who are working on addressing this (gpu's for FFT's, analysis with PNNL computers, etc...)



Other worries:

- Identify initial frequency? Make sure event starts within observation window.
- Dependence on magnetic-field inhomogeneities? $\omega_c = \frac{qB}{E}$ Good expertise in team on shimming

Good expertise in team on shimming *B* fields

• RF power variations with *E*: efficiency dependency?





Other worries: "Doppler effect" and power into sidebands.

The wave generated by the electron is:

$$e^{i(\beta z -)}$$

The amplifier observes a frequency:

$$\omega + \beta \dot{z0}/\omega$$

"Doppler effect" depends on axial speed of the electron.

Since the electron is oscillating, this leads to frequency modulation. Part of the power goes to sidebands.









Applications: coupling CRES with radioactive ion









A different application: coupling CRES with radioactive ion trap. Benchmarks for nuclear structure?

- $2\nu-2\beta$ decays
- single beta decays
- single electron capture decays

In 3 cases one can check all of the above for the same nucleus: good for understanding overarching issues (role of p-p, p-h correlations, deformation, etc...)

Previous experiments limited by energy resolution. CRES technique would improve it by 100.







⁶He timeline

Finish systematics studies

Little a Commissioning

Run little a

Analysis little a

Develop 19Ne source Design vacuum system magnet assembly Build cryo-coolers & RF assembly Assemble cryocoolers & RF components Build magnet installation Install magnet & cool do Assemble & test data ac Data with 131mXe

Data with 6He

	FY 2017	FY 2018	FY 2019	FY 2020	
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cq.					

Little b Phase I

Conclusion ⁶He

- Exploring the CRES (Project 8) technique
- Presently working on design
- Start assembling during summer 2018
- Monte-Carlo calculations show technique could eventually reach $b < 10^{-4}$, surpassing any other probe.
- THEORISTS: Please help! Is theory reliable to extract $b < 10^{-4}$?
- Our developments (coupling of CRES to ion traps) could lead to spectroscopy technique useful for FRIB.

Backup slides

Previous measurements limited by energy resolution: With Project 8 technique energy resolution could improve by 100!



Both of our results are consistent with complete ground state dominance: just using the ground state accounts for the measured $2\nu-2\beta$ decay rate.





Waveguides: each mode propagates above a certain *cut-off freq*.

0

 $E = E_z + E_t$

$$\left(\nabla^{2} + \frac{\omega^{2}}{c^{2}}\right) \left\{ \begin{matrix} E \\ B \end{matrix} \right\} = 0$$

$$\left\{ \begin{matrix} E(x, y)e^{\pm ikz - i\omega t} \\ B(x, y)e^{\pm ikz - i\omega t} \end{matrix} \right\}$$

$$\left[\nabla^{2}_{t} + \left(\frac{\omega^{2}}{c^{2}} - k^{2}\right)\right] \left\{ \begin{matrix} E(x, y) \\ B(x, y) \end{matrix} \right\} = \frac{\omega^{2}}{c^{2}} - k^{2} \equiv \gamma^{2}$$

TM waves:
$$E_t = \pm \frac{ik}{\gamma^2} \nabla_t \psi$$

TE waves: $H_t = \pm \frac{ik}{\gamma^2} \nabla_t \psi$
 $(\nabla_t^2 + \gamma^2)\psi = 0$

 $\psi_{m,n}(x,y) = H_0 \cos\left(\frac{m\pi x}{a}\right) \cos\left(\frac{n\pi y}{b}\right)$

$$k = \frac{\sqrt{\omega^2 - \omega_c^2}}{c}$$

There are *cutoff frequencies* for each mode







Fundamental symmetries with 6He

Cutoff frequencies for d=1cm guide. For 0.455" divide by 1.1557.

Active in 18-24 GHz: $TE_{1,1}$, $TM_{0,1}$ (but $TM_{0,1}$ doesn't couple to WR42)

\overline{n}	$f_{n,1}^{TE}$	$f_{n,2}^{TE}$	$f_{n,3}^{TE}$	$f_{n,1}^{TM}$	$f_{n,2}^{TM}$	$f_{n,3}^{TM}$
0	36.57	67.00	97.15	22.97	52.71	82.64
1	17.58	50.90	81.51	36.59	67.00	97.15
2	29.16	64.03	95.21	49.03	80.38	110.96



Only the TE11 mode transmits





Little *a* next:

Penning lons allow unique visualization

Issues under control

- Stability of MOT dimensions and position
- MCP position accuracy, MCP efficiency
- MWPC position resolution •
- Scintillator response, ΔE .
- Timing resolution
- Background effects •



Issues to be solved

CENPA

Nov

High-voltage noise and stability

Center for Experimental Nuclear Physics and Astrophysics

- **Electric field scaling**
- Photo-ion TOF data (³He, ⁴He, ⁶He)

MCP Image Zoom: Condition0 CombExpMCP Image Zoom Cond 3.621951e+07 Entries -0.3743 Mean x 35000 Mean v 0.01861 49 Std Dev x 1.339 He6-He6 1.324 Std Dev y 25000 20000 15000-Residue gas 10000 5000 5 may 2 1 0-1-2-3 -1-2-3-4-5 -5 ²⁰⁷Bi source 10 Fit Eunction 10 Bin Count per 10 10 15 0.5 Q [Arbitrary Unit] (da/dx)/aVariable (Sensitivity) da/a (%) dx units MOT - MCP Distance 0.45 15.00 0.030 mm MCP Position Calibration -5.50 0.010 0.06 mm MOT Radial Position 0.50 0.030 0.02 mm MOT Width (Sigma) 0.030 0.05 -1.70 mm **Electric Field Scaling** 8.00 0.010 0.08 fraction

Electrode Spacing 8.70 0.030 0.26 mm Beta Energy Threshold 0.08 0.03 2.400 keV Timing Resolution -0.21 0.040 0.01 ns Scattering* 0.23 2.30 0.100 fraction Background** 20.00 0.003 fraction 0.06 MCP Efficiency Non-Uniformity* 0.18 Total 0.61 Magnetron motion. For harmonic traps no bias (E-dependence)



For each cyclotron turn the orbits displaces: $\Delta \approx R_1 - R_2 \approx R(1 - B_1/B_2) \approx R\left(\frac{\partial B/\partial r}{B}R\right)$

Then the radius *X* of magnetron motion:

$$X \approx \frac{N\Delta}{2\pi} \approx N \frac{R^2}{2\pi} \frac{\partial B}{\partial r}$$

Use
$$\frac{\partial B/\partial r}{B} \sim r \frac{10^{-2}}{cm^2}$$
 Harmonic trap

$$X \approx N \frac{R^2}{2\pi} X \frac{10^{-2}}{cm^2} \rightarrow N = \frac{2\pi}{10^{-2}R^2} \approx 10^5$$

X cancels: magnetron radius independent on R in harmonic trap.



