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$$\theta_W = 29,2^\circ$$

# A new, high precision measurement of the weak mixing angle $\sin^2 \theta_W$

Frank Maas

(Helmholtz Institute Mainz,  
Institute for Nuclear Physics,  
PRISMA cluster of excellence

Johannes Gutenberg University Mainz)

MITP-Workshop, “Bridging the Standard Model to New Physics with the  
Parity Violation Program at MESA”, April 23 – May 4, 2018





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# A new, high precision measurement of the Weinberg angle $\sin^2 \theta_W$


$$\theta_W$$

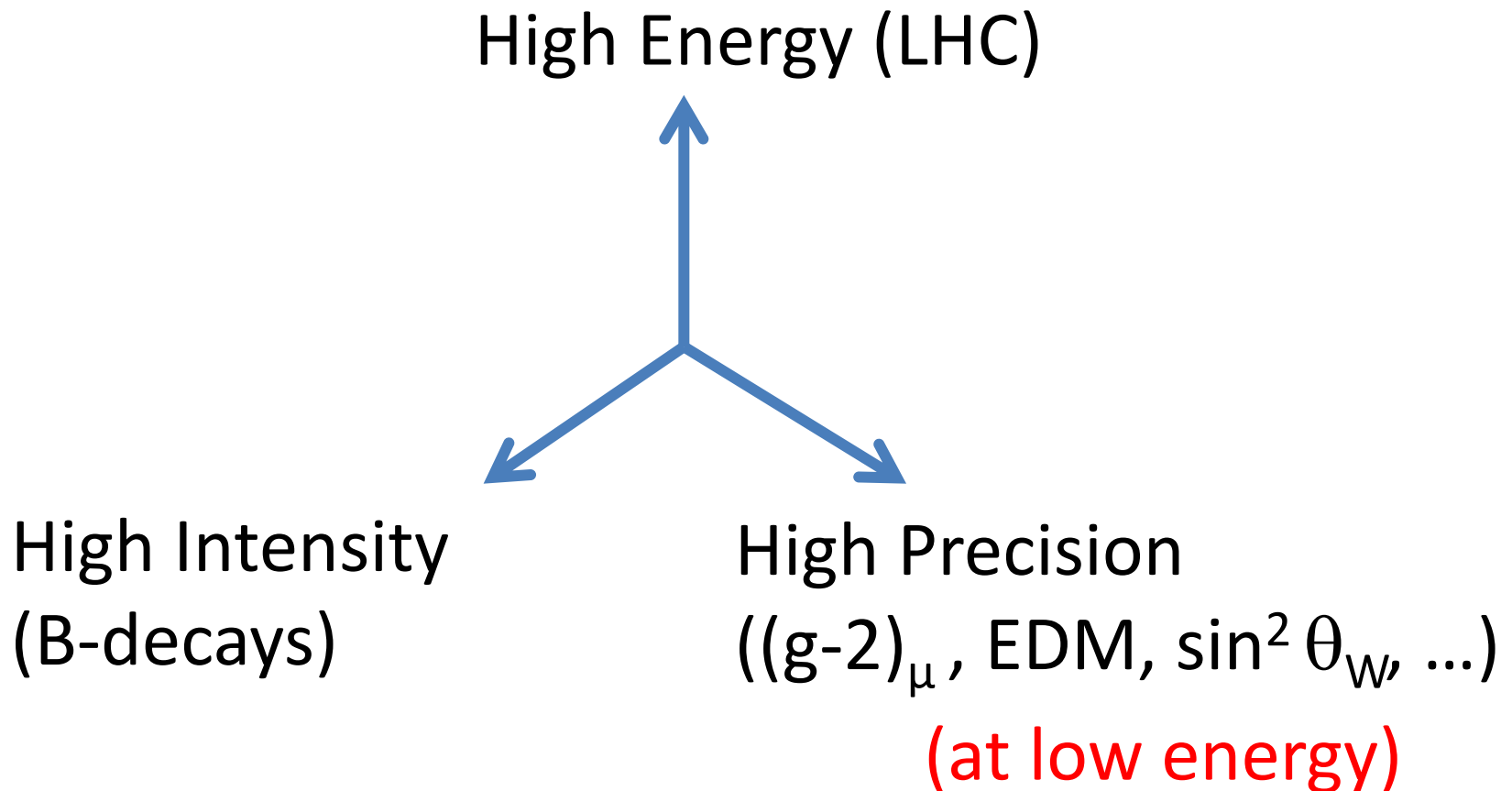
Frank Maas  
(Helmholtz Institute Mainz,  
Institute for Nuclear Physics,  
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Johannes Gutenberg University Mainz)

50 Jahre Beschleunigerphysik in Mainz, 15./16. Februar 2018





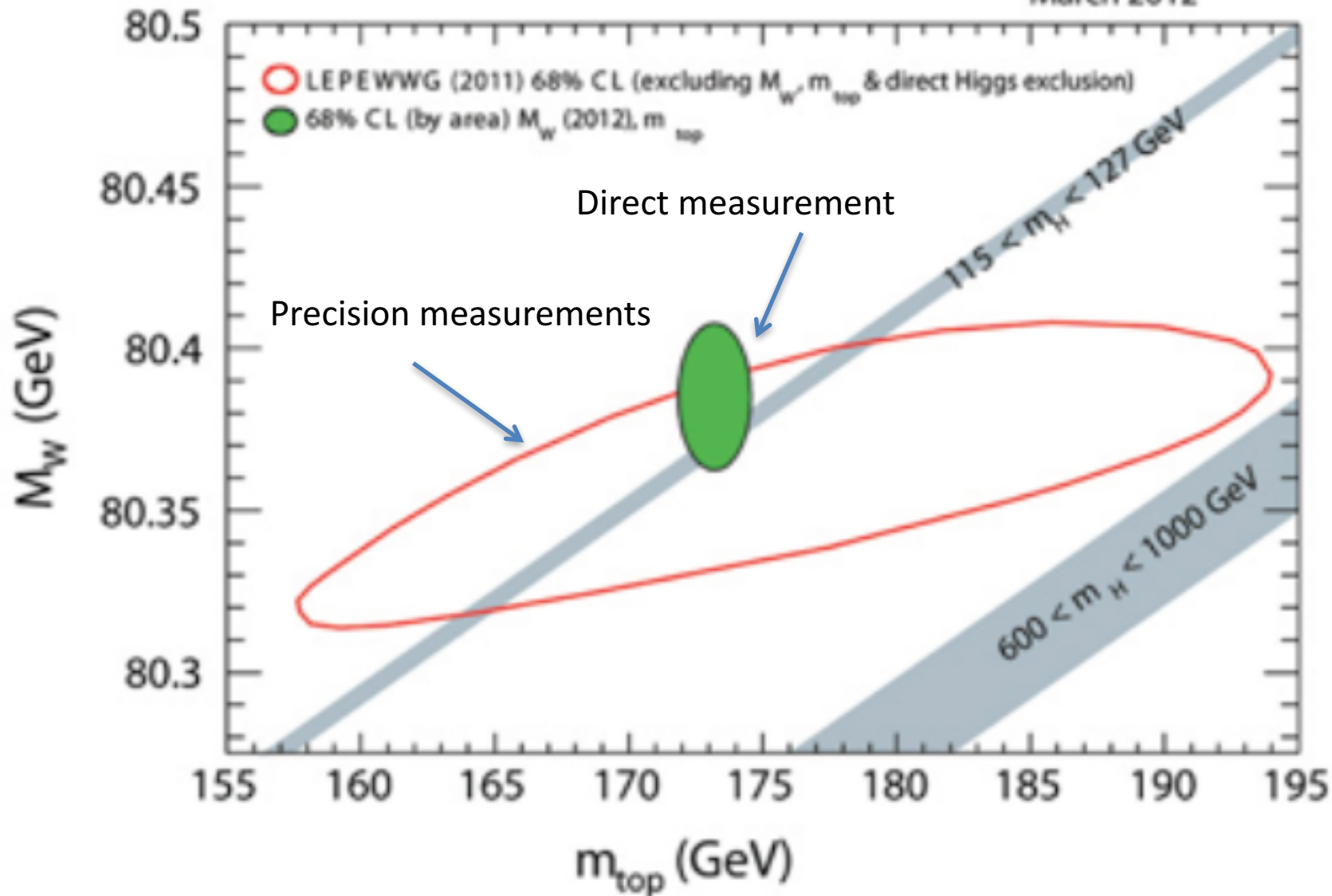
## Search for New Physics: Various Methods





## Direct observation versus precision measurements: top-quark

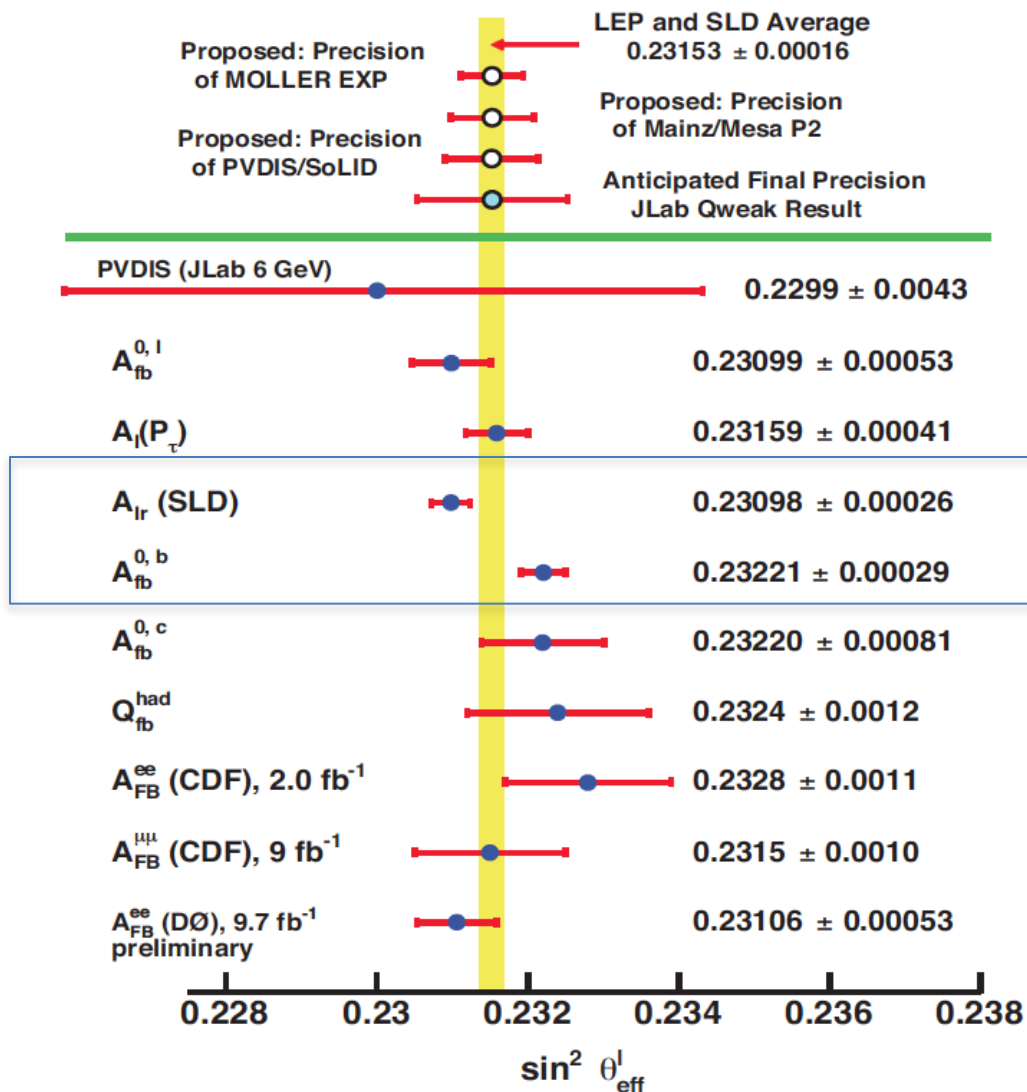
March 2012

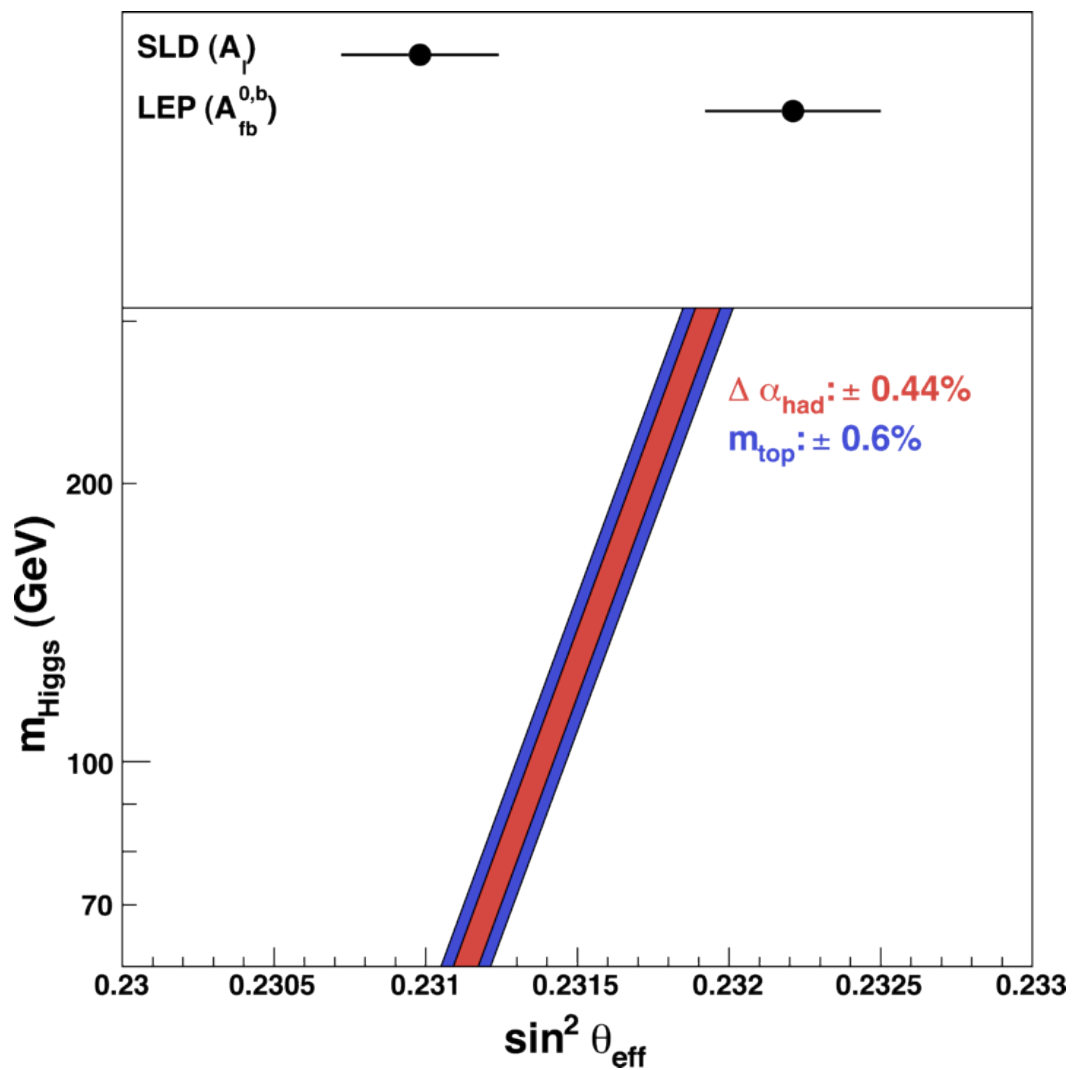




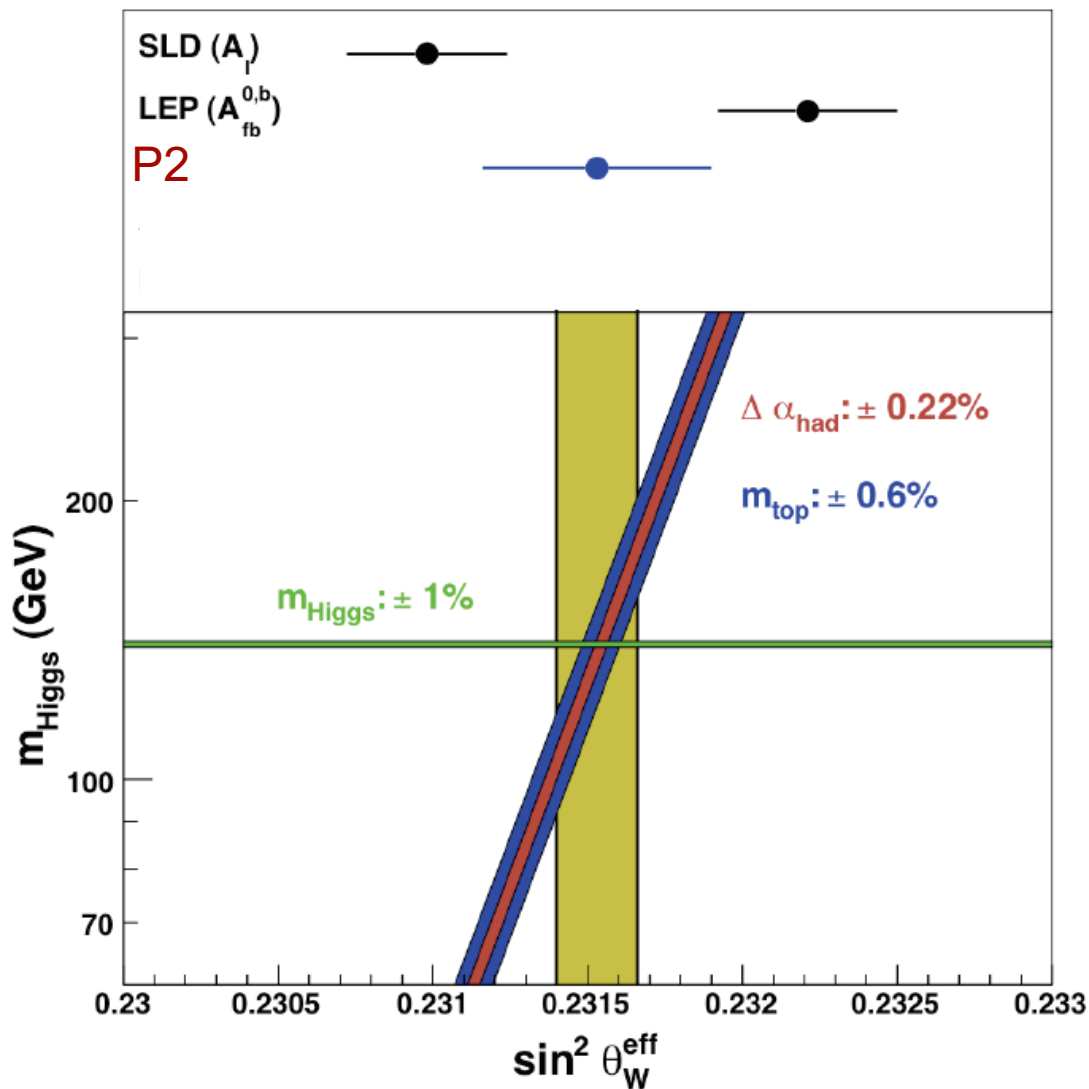


## Summary: Measurements of $\sin^2\theta_{W(\text{effective})}$





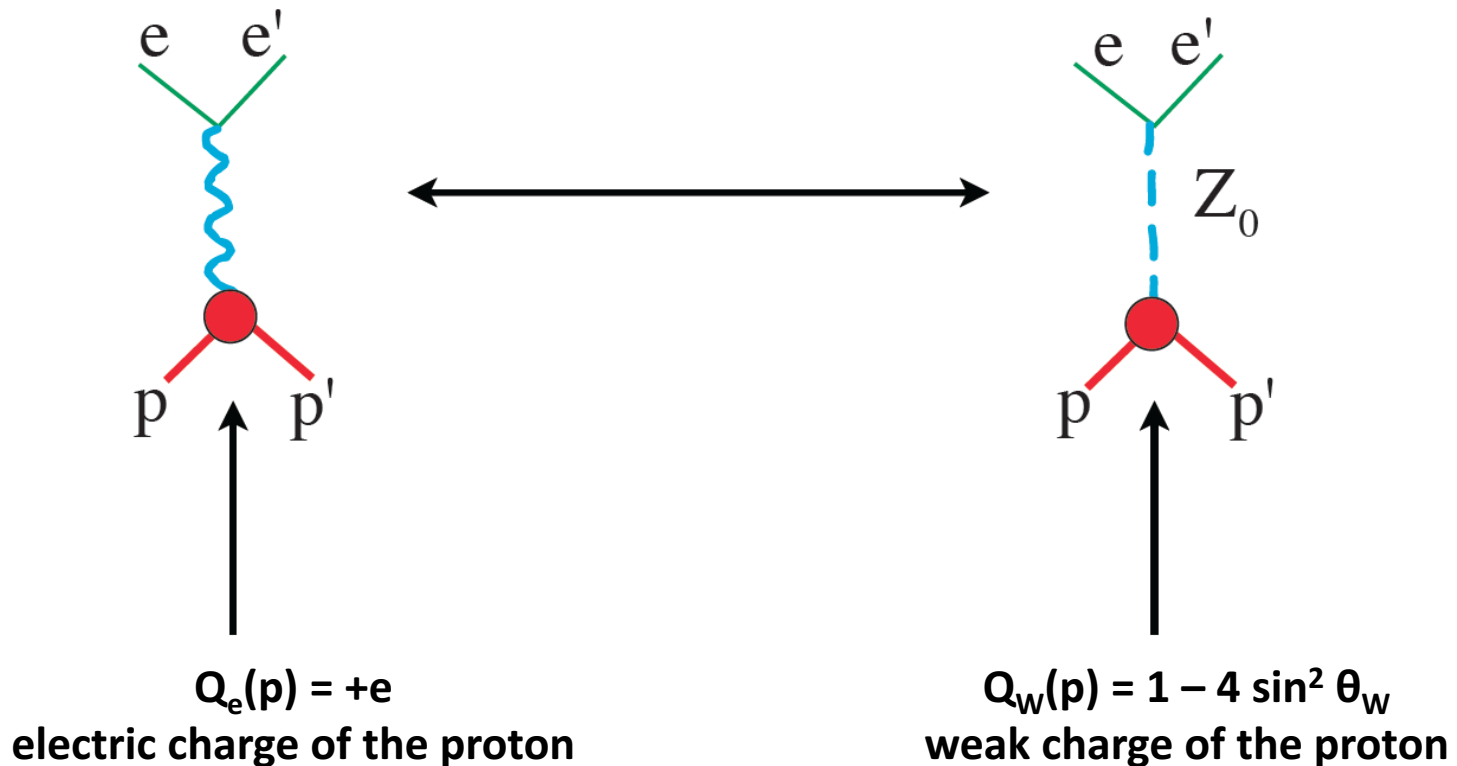






## The role of the weak mixing angle

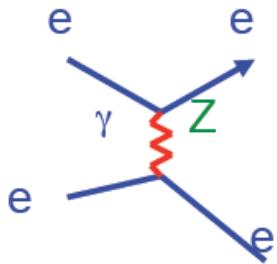
The **relative strength** between the weak and electromagnetic interaction is determined by the **weak mixing angle**:  $\sin^2(\theta_w)$



$\sin^2 \theta_w$ : a **central parameter** of the standard model

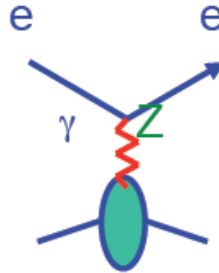


## Møller Scattering



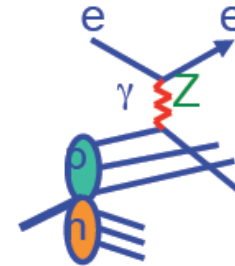
- Purely Leptonic

## Q-Weak (JLab) P2 (Mainz/MESA)



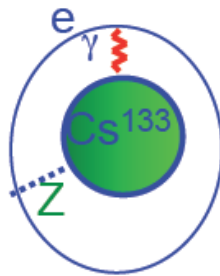
- Coherent quarks in p
- in operation now
- $2(2C_{1u} + C_{1d})$

## e-DIS



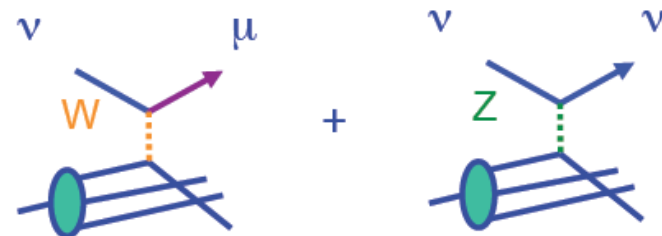
- Isoscalar quark scattering
- $(2C_{1u} - C_{1d}) + Y(2C_{2u} - C_{2d})$

## Atomic Parity Violation



- Coherent quarks in entire nucleus
- Nuclear structure uncertainties
- $-376 C_{1u} - 422 C_{1d}$

## Neutrino Scattering



- Quark scattering (from nucleus)
- Weak charged and neutral current difference



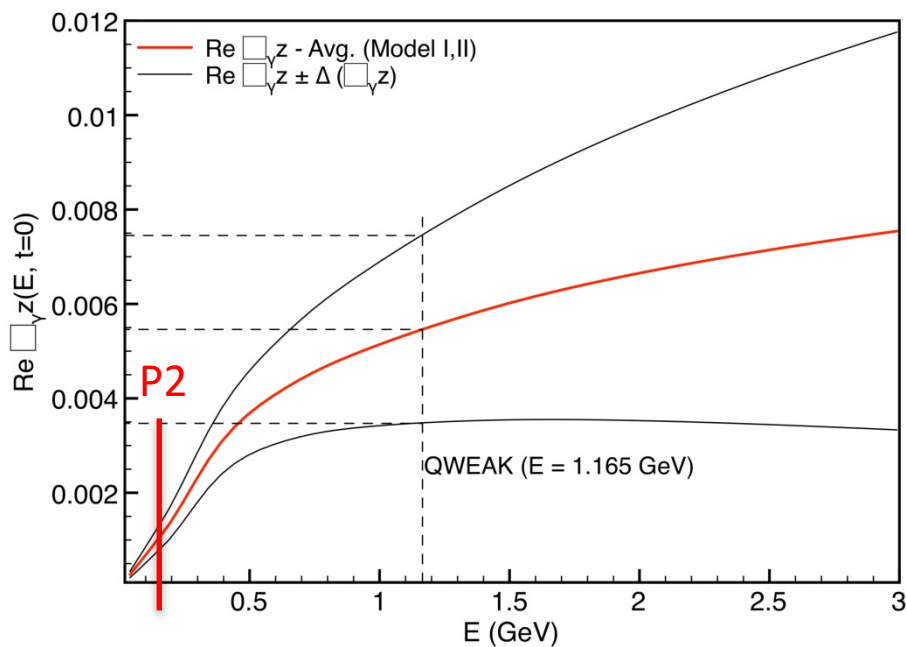
„running“  $\sin^2 \theta_{\text{eff}}$  or  $\sin^2 \theta_w(\mu)$





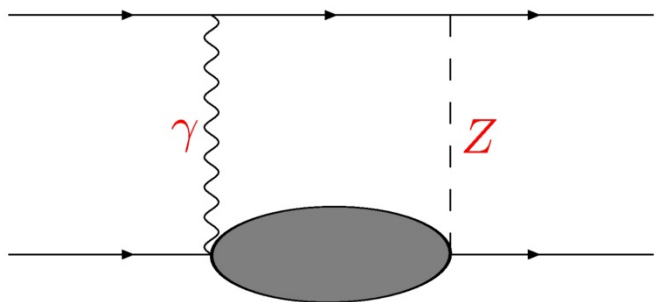


➤  $\gamma Z$  box graph contributions obtained by modelling hadronic effects:



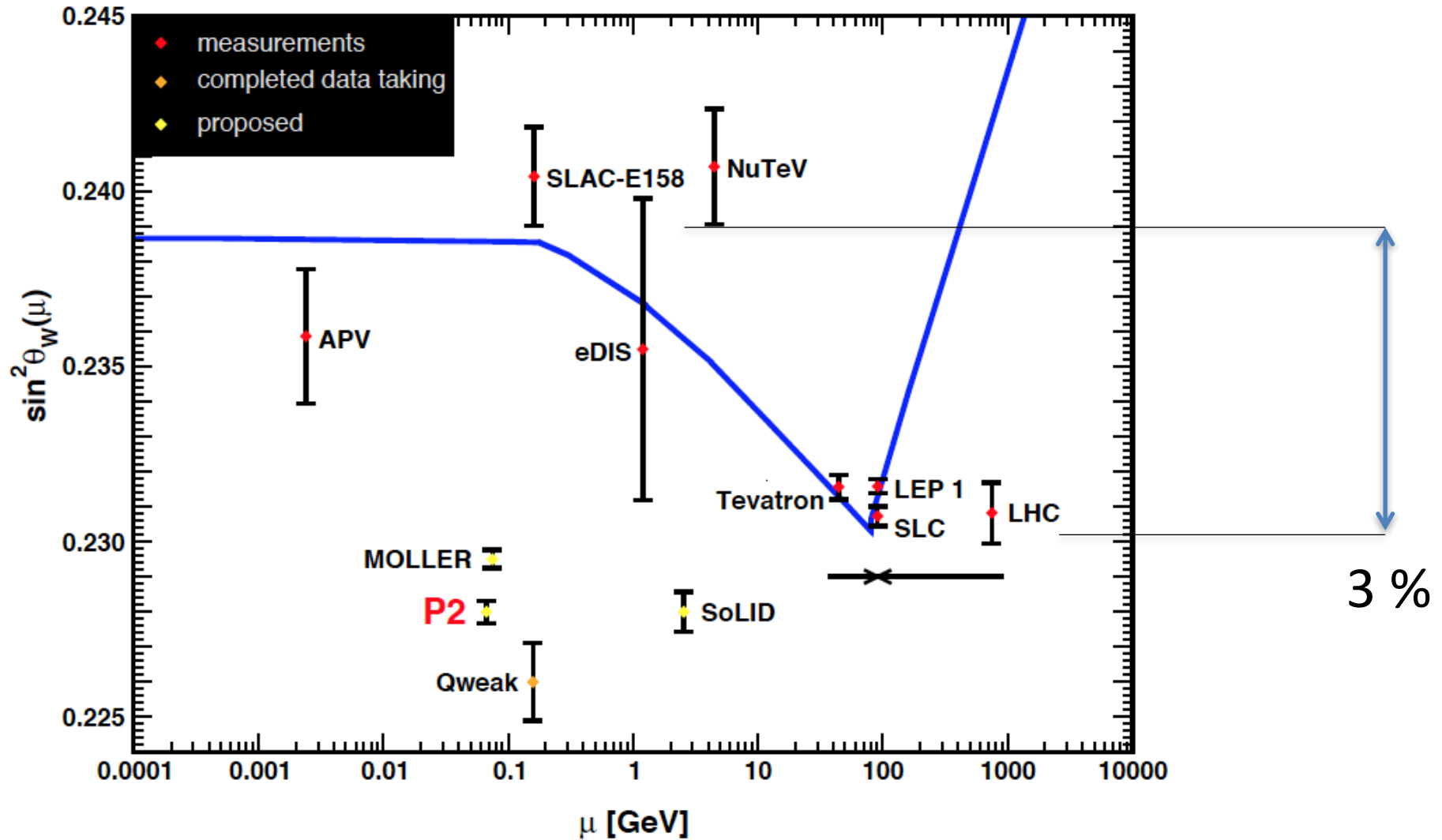
[Gorchstein, Horowitz & Ramsey-Musolf 2011]

- Hadronic uncertainties suppressed at lower energies
- Low beam energy experiment:  
**P2 @ MESA**



Progress in Theory

- Theory uncertainties in box diagrams
- 2 loop corrections
- Hadronic contributions in loops
- Auxiliary measurements
- PV-asymmetry in Carbon



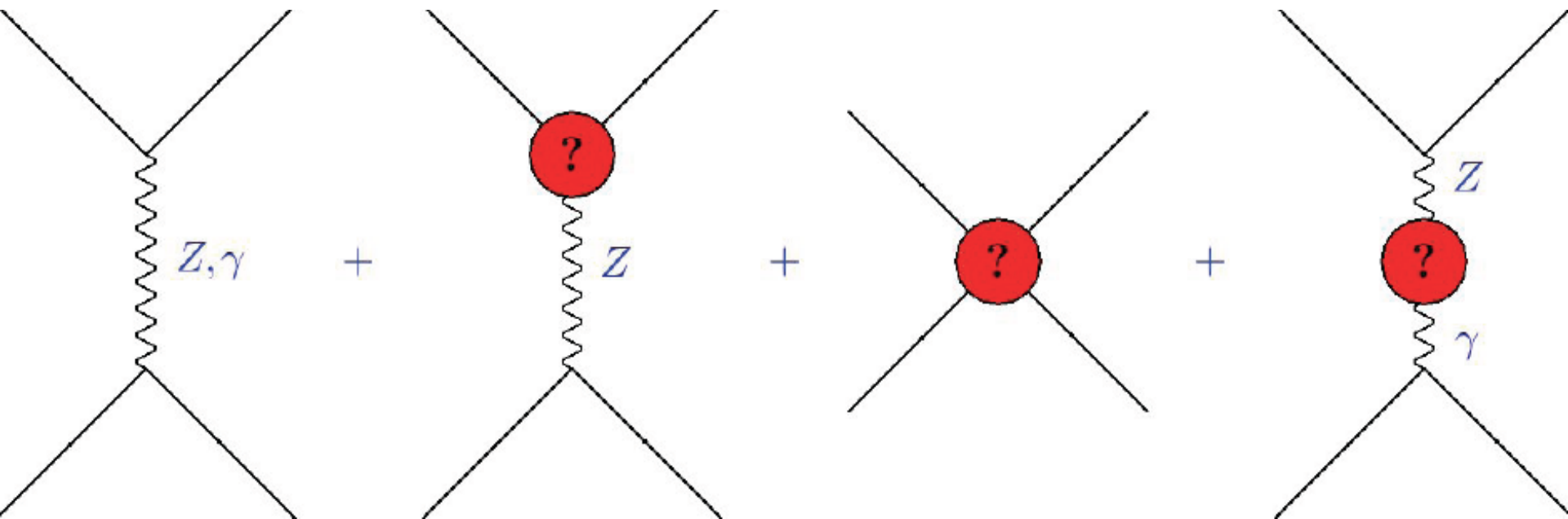


Sensitivity to new physics beyond the Standard Model





## Sensitivity to new physics beyond the Standard Model



Extra Z

Mixing with  
Dark photon or  
Dark Z

Contact interaction

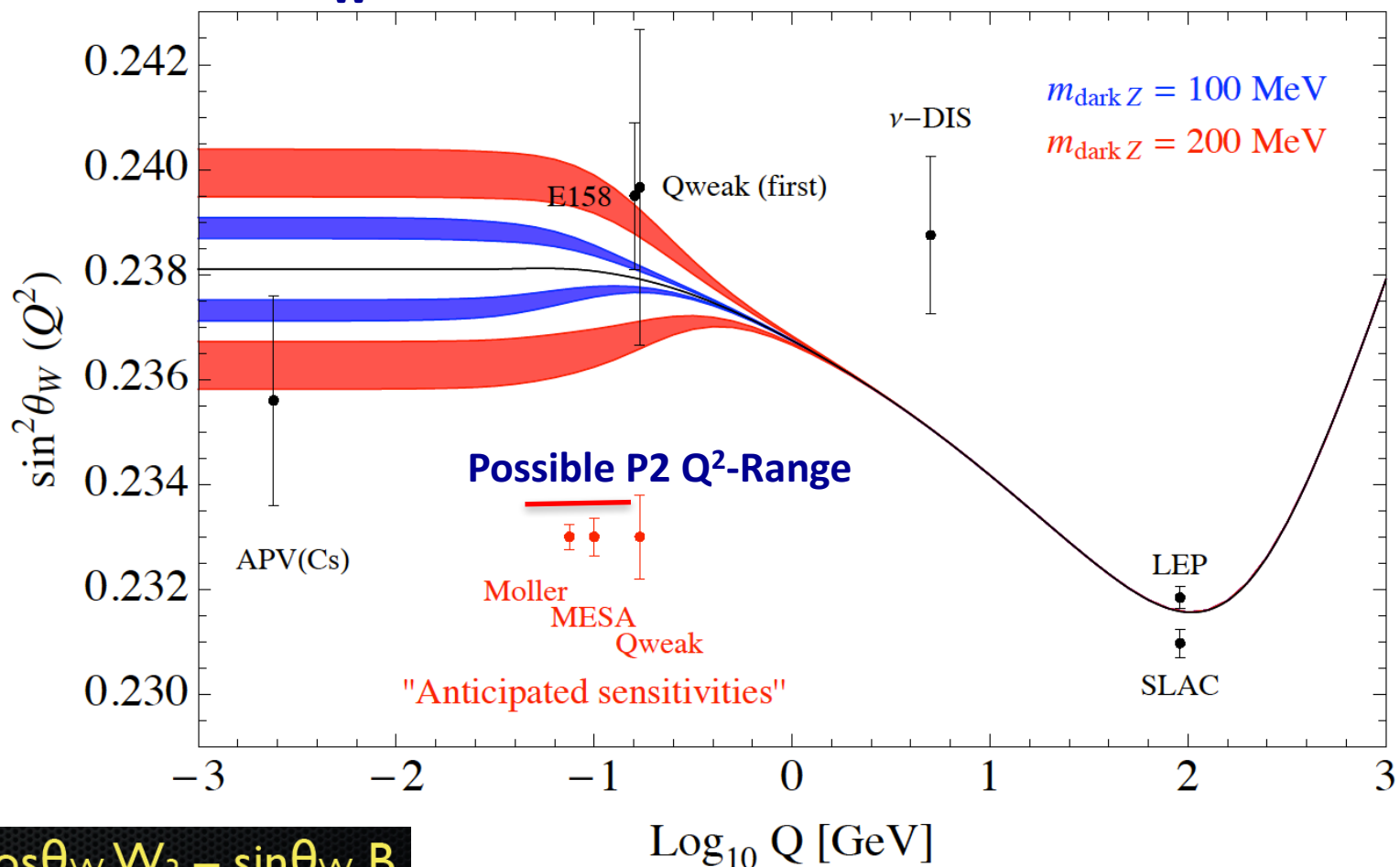
New  
Fermions



## Dark Photon, Z-Boson



# Running $\sin^2 \theta_W$ and Dark Parity Violation

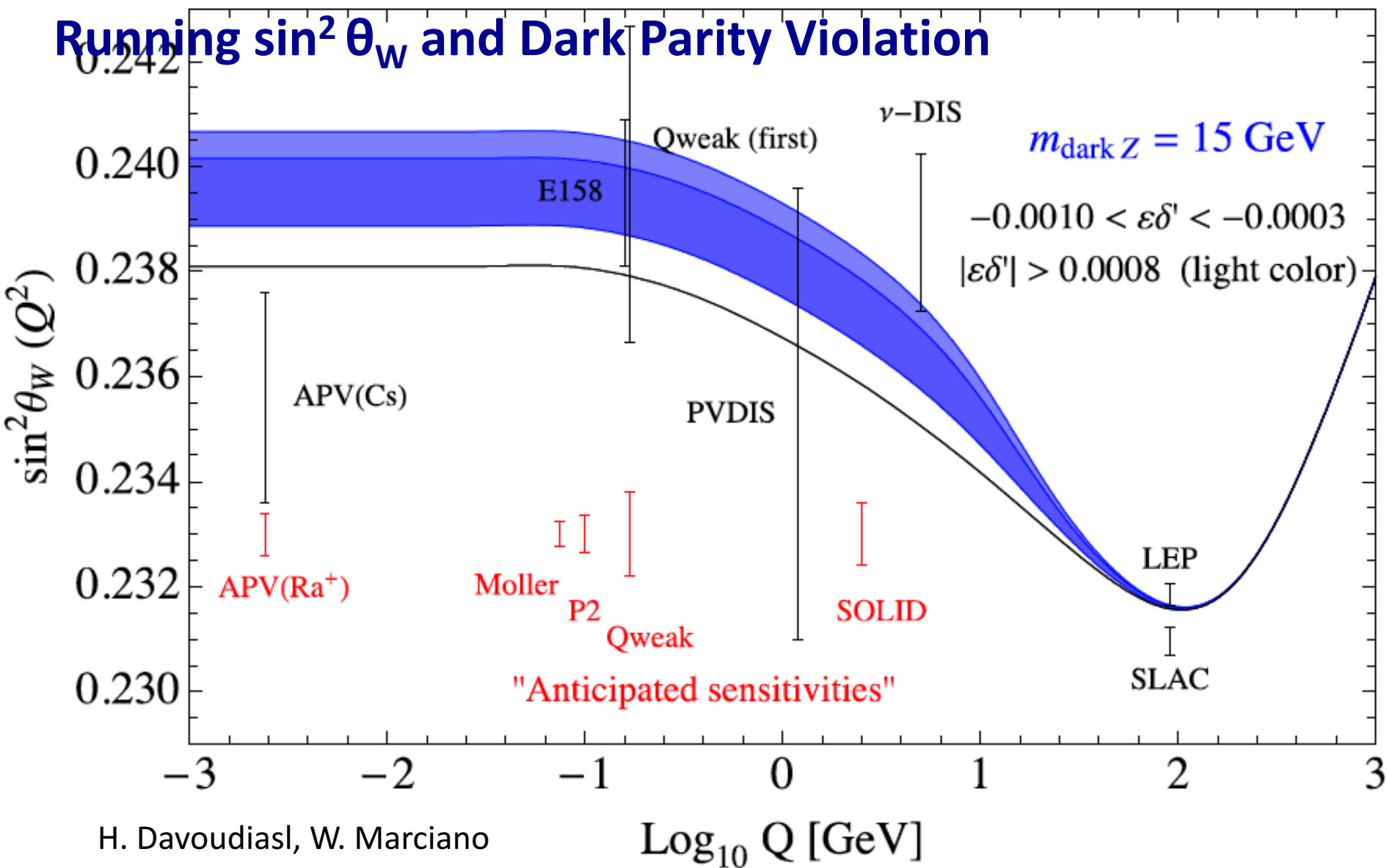


$$Z = \cos \theta_W W_3 - \sin \theta_W B$$

$$A = \sin \theta_W W_3 + \cos \theta_W B$$



## Running $\sin^2 \theta_W$ and Dark Parity Violation





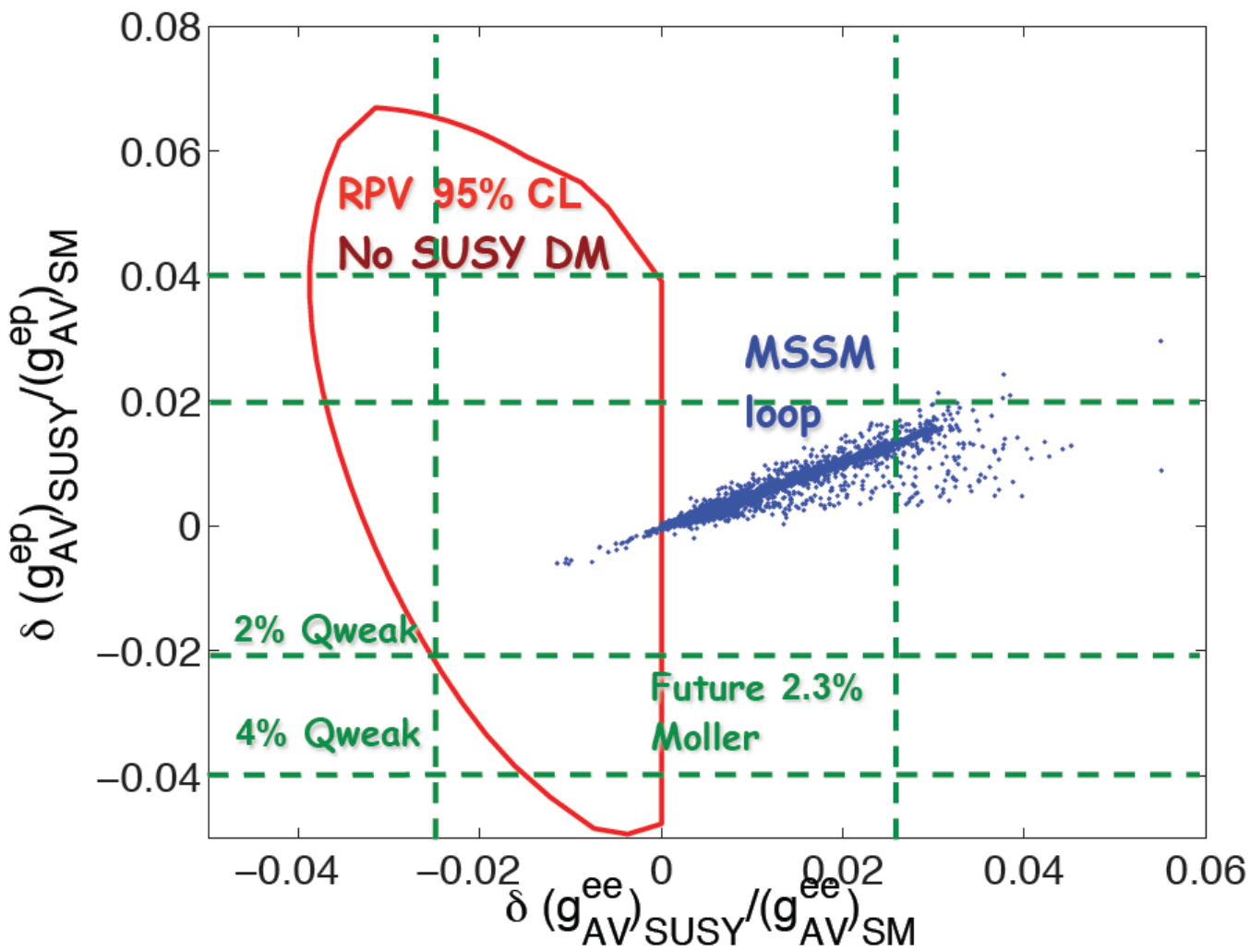


## Supersymmetry



Example: Supersymmetric standard model extensions

Kurylov, Ramsey-Musolf, Su (2003), updated



After LHC  
Run 1



- Complementary access by weak charges of proton and electron

Weak charge of the proton:

$$Q_W^p = 0.0716$$

$$\pm 0.0029$$

Experiment

SUSY-Loops

$E_6 Z'$

RPV SUSY

Leptoquarks

SM

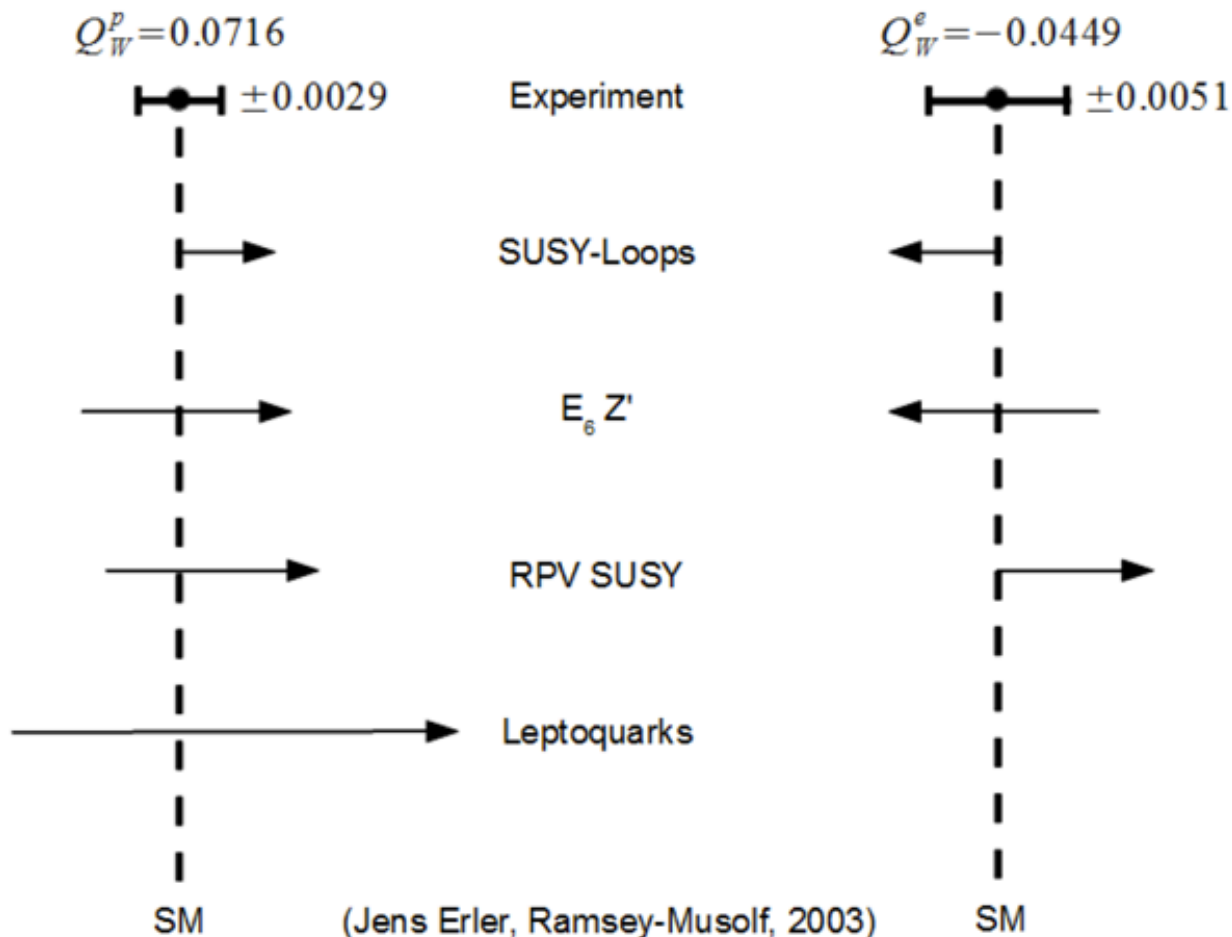
(Jens Erler, Ramsey-Musolf, 2003)

Weak charge of the electron:

$$Q_W^e = -0.0449$$

$$\pm 0.0051$$

SM





Weak  
Charge  
Of  
Proton:  
Qweak (Jlab),  
P2 (MESA)

Weak  
Charge  
Of  
Electron:  
MOELLER  
(JLAB)

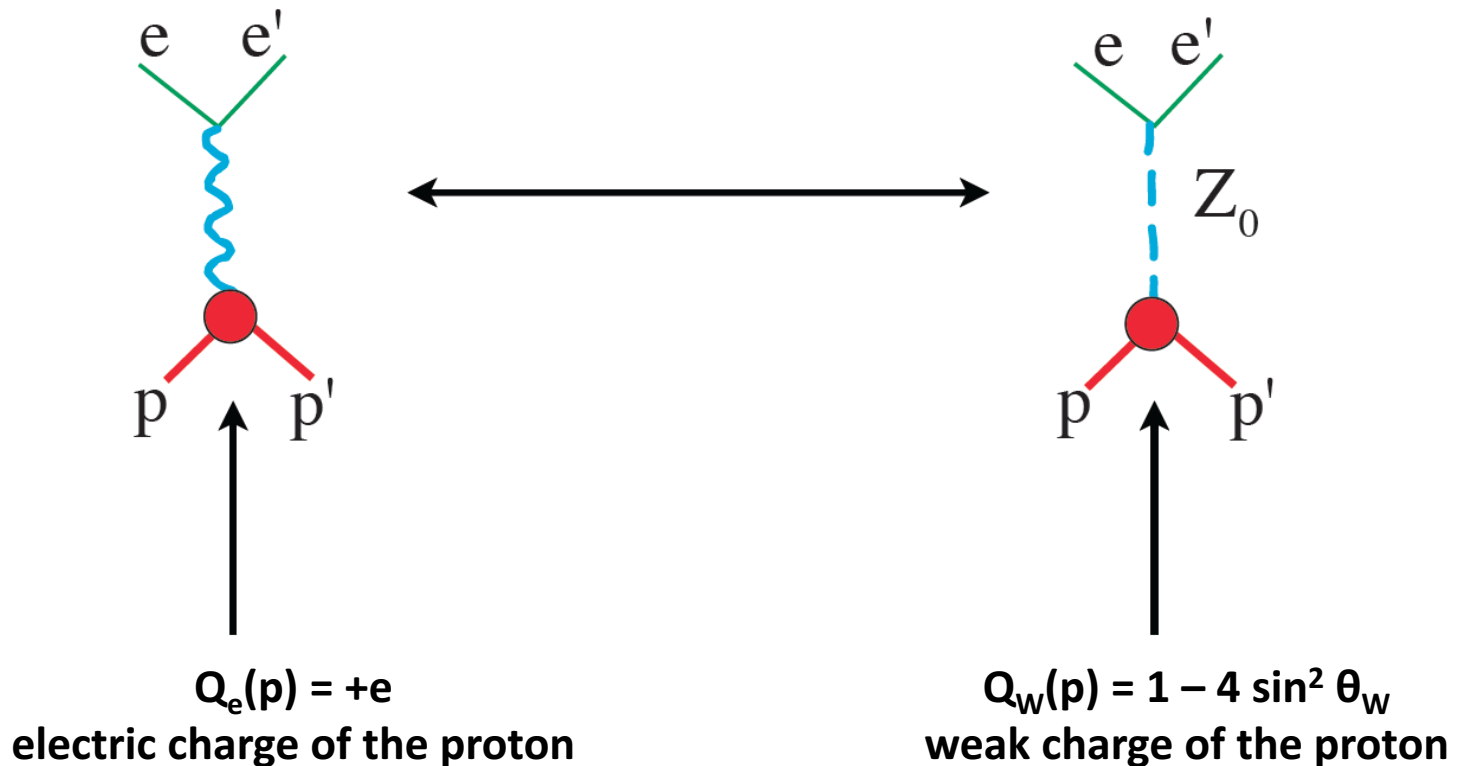
Weak  
Charge  
Of  
Quarks:  
SOLID  
(PVDIS)  
(JLAB)





## The role of the weak mixing angle

The **relative strength** between the weak and electromagnetic interaction is determined by the **weak mixing angle**:  $\sin^2(\theta_w)$



$\sin^2 \theta_w$ : a **central parameter** of the standard model



## Proton: special case

$$\text{Proton Weak charge: } Q_W(p) = 1 - 4 \sin^2 \theta_W$$

$$\text{Error: } \Delta Q_W(p) = 4 \Delta \sin^2 \theta_W$$

$$\text{Rel. error: } \Delta Q_W(p)/Q_W(p) = 4 / ( (1/\sin^2 \theta_W) - 4 ) (\Delta \sin^2 \theta_W / \sin^2 \theta_W)$$

$$\text{Rel. error } \Delta \sin^2 \theta_W / \sin^2 \theta_W = ( (1/\sin^2 \theta_W) - 4 ) / 4 \Delta Q_W(p) / Q_W(p)$$

$$\text{Example: } \sin^2 \theta_W (50 \text{ MeV}) = 0.238$$

$$4 / ( (1/\sin^2 \theta_W) - 4 ) \sim 20$$

$$\Delta Q_W(p) / Q_W(p) = 2\% \quad \text{from Experiment}$$

$$\Delta \sin^2 \theta_W / \sin^2 \theta_W = 0.1\% \quad \text{same precision as LEP, SLAC}$$

### Neutron Weak charge:

$$\Delta Q_W(p) / Q_W(n) = \Delta \sin^2 \theta_W / \sin^2 \theta_W$$



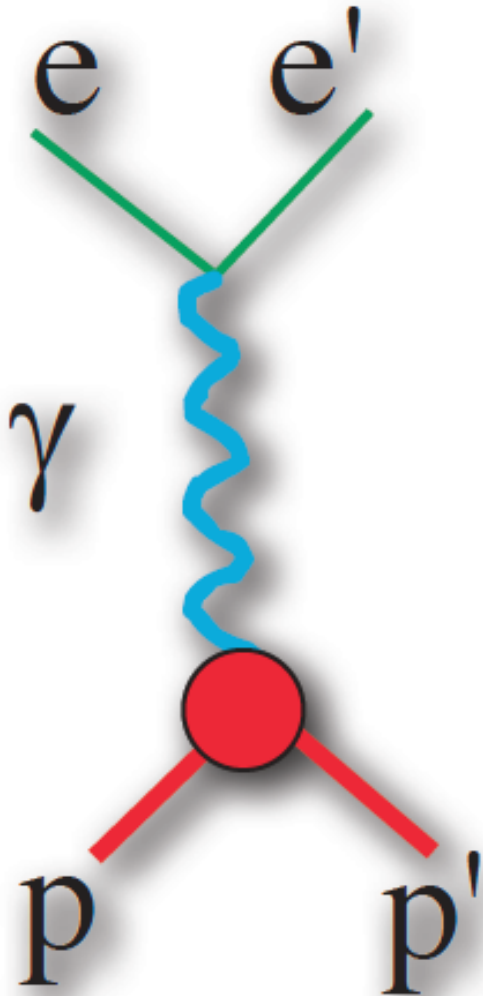
## Physics sensitivity from contact interaction (LEP2 convention, $g^2 = 4\pi$ )

	precision	$\Delta \sin^2 \bar{\theta}_W(0)$	$\Lambda_{\text{new}}$ (expected)
APV Cs	0.58 %	0.0019	32.3 TeV
E158	14 %	0.0013	17.0 TeV
Qweak I	19 %	0.0030	17.0 TeV
Qweak final	4.5 %	0.0008	33 TeV
PVDIS	4.5 %	0.0050	7.6 TeV
SoLID	0.6 %	0.00057	22 TeV
MOLLER	2.3 %	0.00026	39 TeV
P2	2.0 %	0.00036	49 TeV
PVES $^{12}\text{C}$	0.3 %	0.0007	49 TeV



Experimental Method:  
Parity Violating Electron Scattering





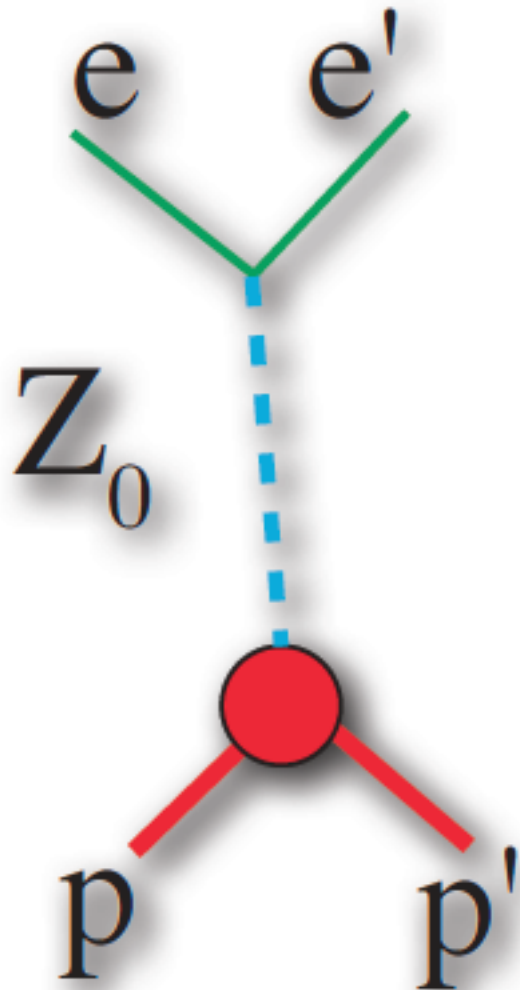
$$\sigma \sim \mathcal{M} \mathcal{M}^* \text{ Phasespace}$$

$$\sim \left( j_\mu \frac{1}{Q^2} J^\mu \right) \left( j_\mu \frac{1}{Q^2} J^\mu \right)^*$$

$$j_\mu \sim \bar{e} \gamma_\mu e \text{ Vector Current}$$

$$J_\gamma^\mu \sim \langle N | q^u \bar{u} \gamma_\mu u + q^d \bar{d} \gamma_\mu d + q^s \bar{s} \gamma_\mu s | N' \rangle$$

$$= \bar{\mathcal{P}} \left[ \gamma^\mu F_1 - i \sigma^{\mu\nu} q_\nu \frac{\kappa_p}{2M_N} F_2 \right] \mathcal{P}$$

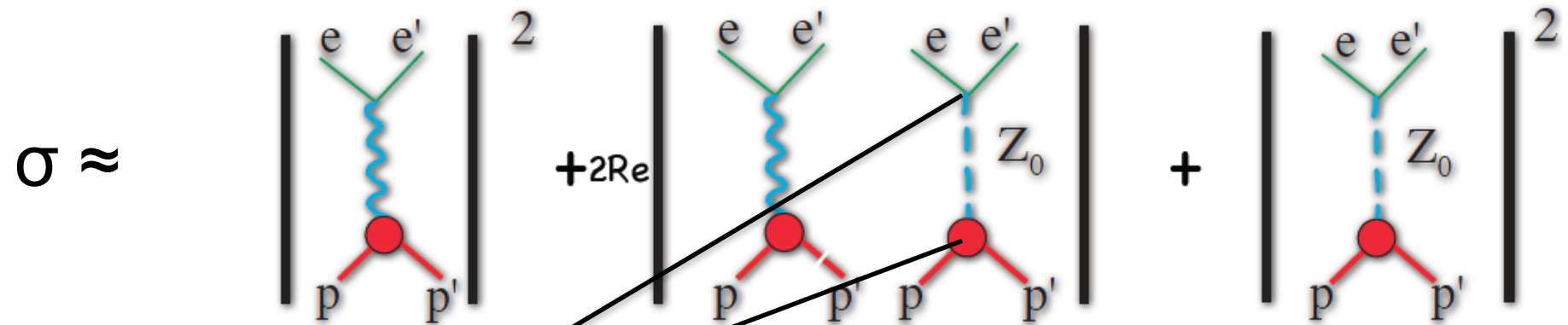


$$\tilde{q}_V^d = \tau_3 - 2q^d \sin^2(\theta_W)$$

$$\begin{aligned} \tilde{J}_Z^\mu &\sim \langle N | \tilde{q}^u \bar{u} \gamma_\mu u + \tilde{q}^d \bar{d} \gamma_\mu d + \tilde{q}^s \bar{s} \gamma_\mu s | N' \rangle \\ &= \bar{\mathcal{P}} \left[ \gamma^\mu \tilde{F}_1 - i \sigma^{\mu\nu} q_\nu \frac{\kappa_p}{2M_N} \tilde{F}_2 \right] \mathcal{P} \end{aligned}$$



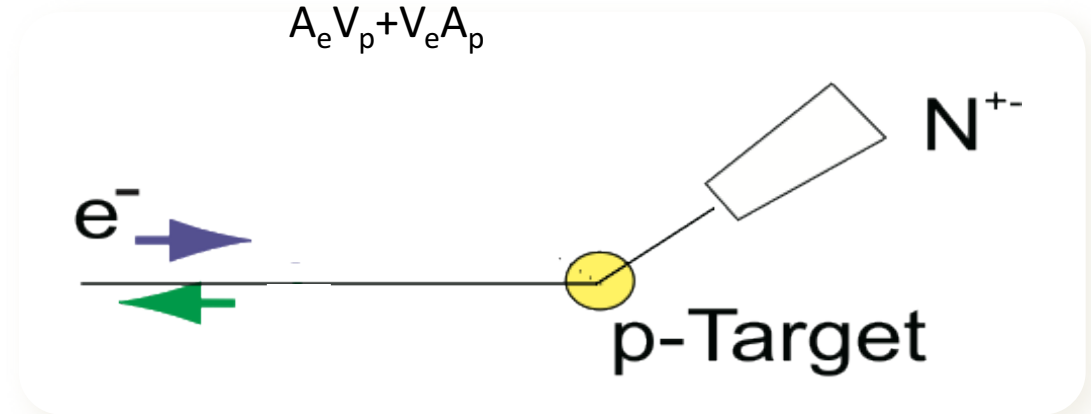
Parity Violating Asymmetry in elastic electron proton scattering



$$(V-A)_e(V-A)_p$$

$$A_e V_p + V_e A_p$$

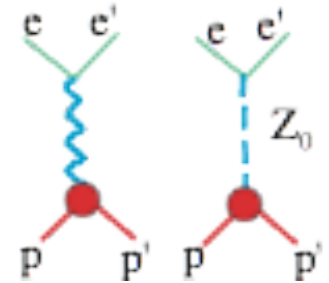
V-A coupling:  
 parity-violating  
 cross section asymmetry  $A_{LR}$   
 longitudinally pol. electrons  
 unpolarised protons





## Parity violating cross section asymmetry

$$A_{ep} = \left[ \frac{G_F Q^2}{4\pi\alpha\sqrt{2}} \right] \frac{\epsilon G_E^Y G_E^Z + \tau G_M^Y G_M^Z - (1 - 4 \sin^2 \theta_W) \epsilon' G_M^Y G_A^Z}{\epsilon (G_E^Y)^2 + \tau (G_M^Y)^2}$$



$$A_{RL} = \underbrace{A_V + A_A}_{= A_0} + A_S \left\{ \begin{array}{l} A_V = -a \rho'_{eq} \left[ (1 - 4 \sin^2 \theta_W) - \frac{\epsilon G_E^p G_E^n + \tau G_M^p G_M^n}{\epsilon (G_E^p)^2 + \tau (G_M^p)^2} \right] \\ A_A = a \frac{(1 - 4 \sin^2 \theta_W) \sqrt{1 - \epsilon^2} \sqrt{\tau(1 + \tau)} G_M^p \tilde{G}_A^p}{\epsilon (G_E^p)^2 + \tau (G_M^p)^2} \\ A_S = a \rho'_{eq} \frac{\epsilon G_E^p G_E^s + \tau G_M^p G_M^s}{\epsilon (G_E^p)^2 + \tau (G_M^p)^2} \end{array} \right. \quad e$$

$$a = -G_F q^2 / 4\pi\alpha\sqrt{2}, \quad \tau = -q^2 / 4M_p^2, \quad \epsilon = [1 + 2(1 + \tau) \tan^2 \theta / 2]^{-1}$$



## Parity violating cross section asymmetry

$$A_{LR} = \frac{\sigma(e \uparrow) - \sigma(e \downarrow)}{\sigma(e \uparrow) + \sigma(e \downarrow)} = - \frac{G_F Q^2}{4\sqrt{2}\pi\alpha} (Q_W - F(Q^2))$$

tracking system                      weak charge

$$Q_W = 1 - 4 \sin^2 \theta_W (\mu)$$

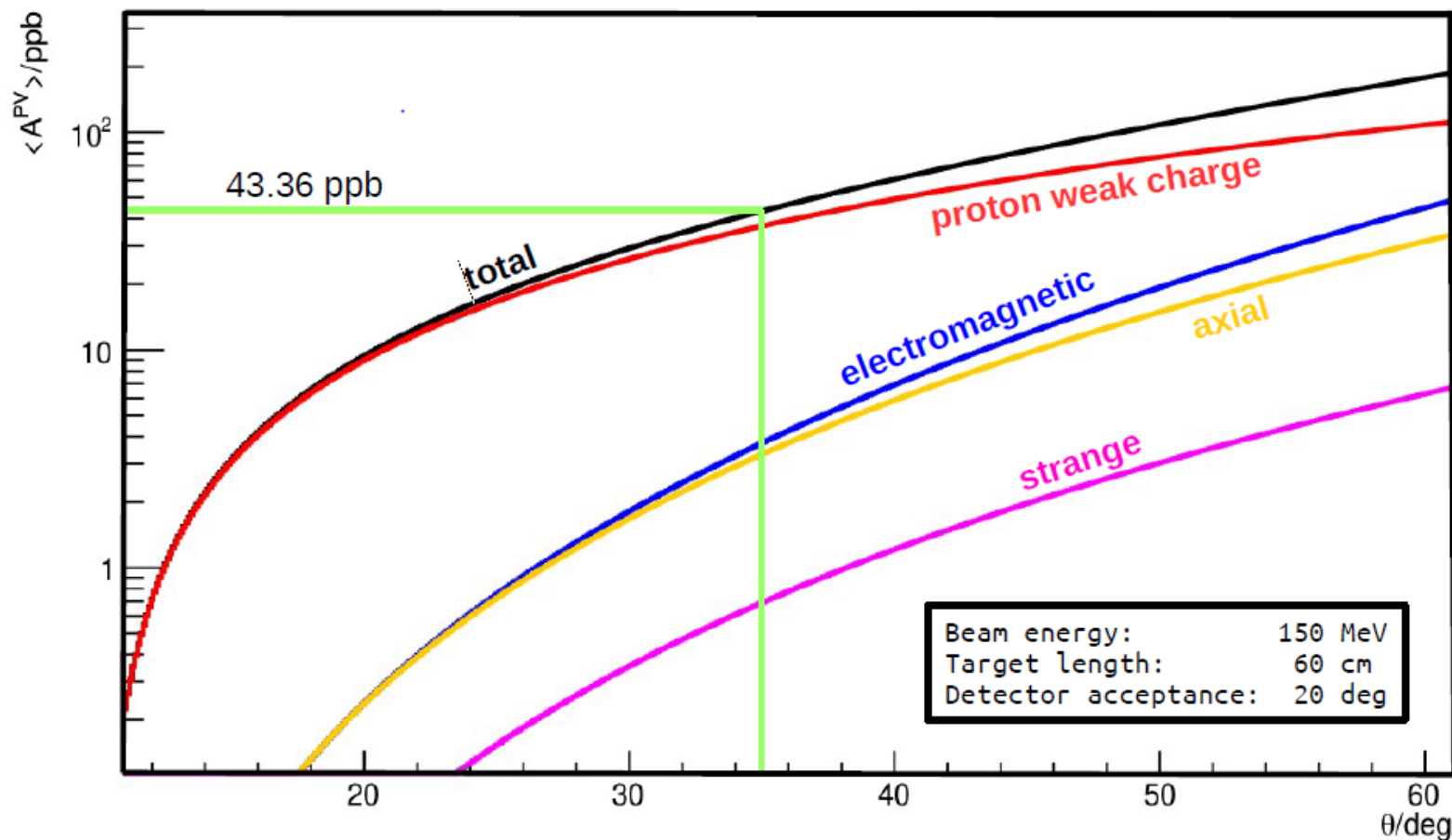
polarisation measurement                      hadron structure

$$F(Q^2) = F_{EM}(Q^2) + F_{Axial}(Q^2) + F_{Strange}(Q^2)$$



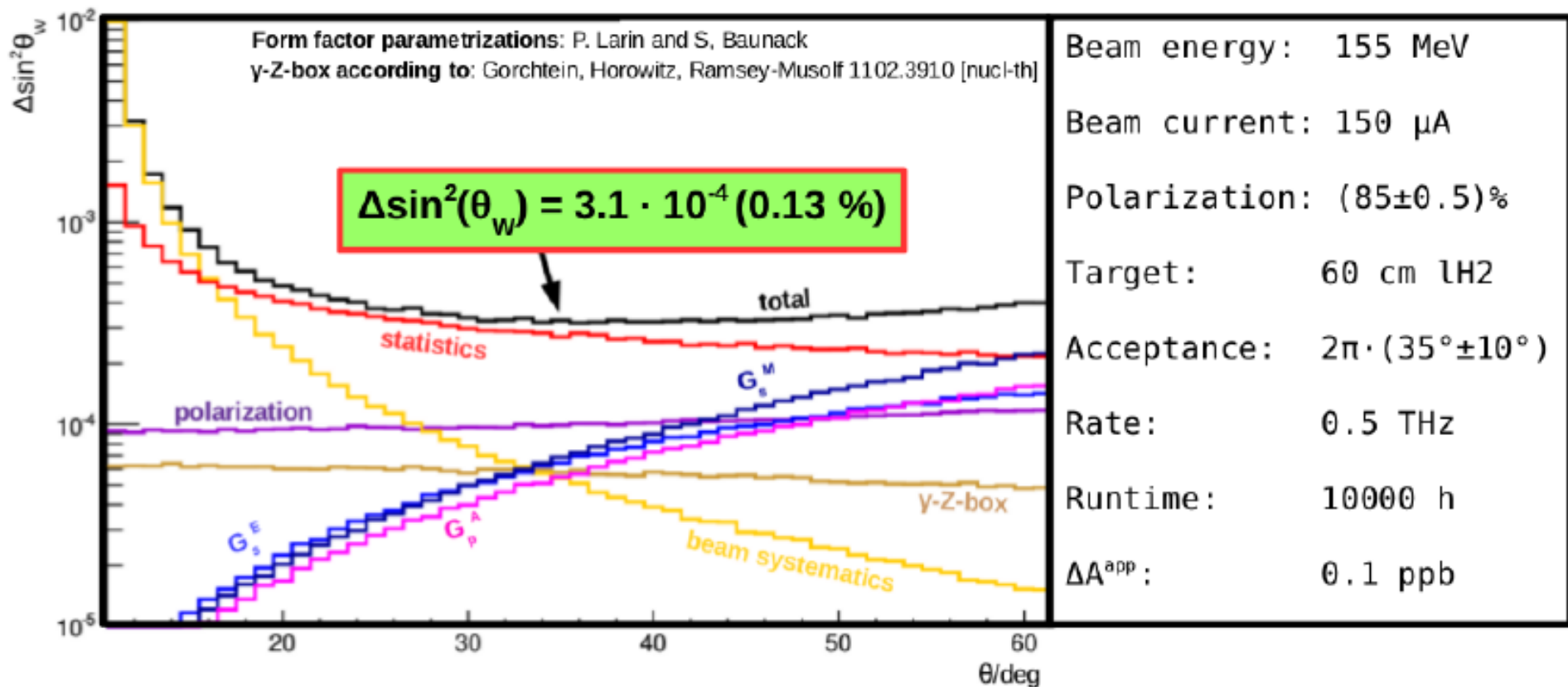


- Contributions to  $\Delta \sin^2 \Theta_W$  for  $35^\circ$  central scattering angle,  $E=150$  MeV, 10000 h of data taking

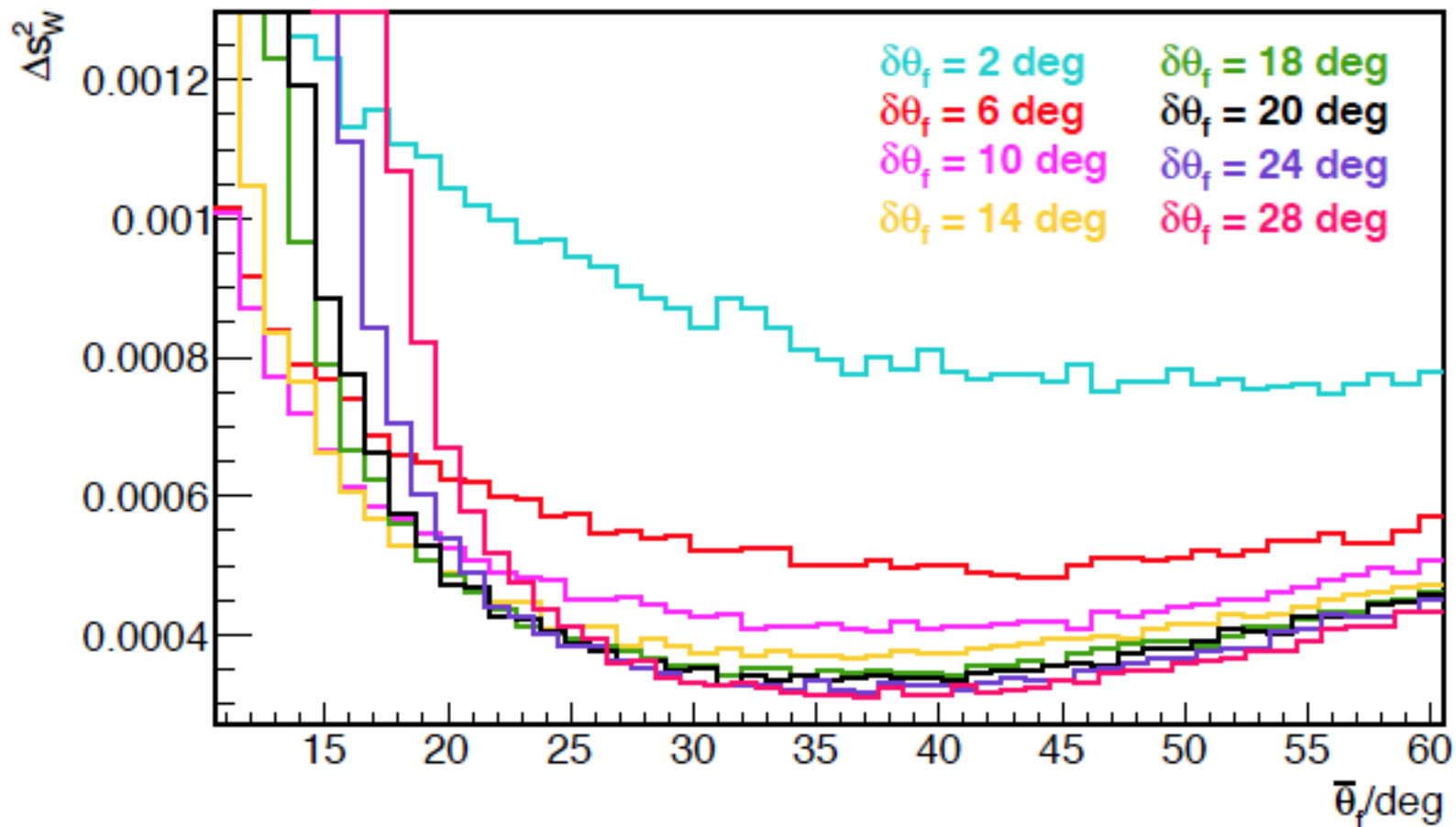




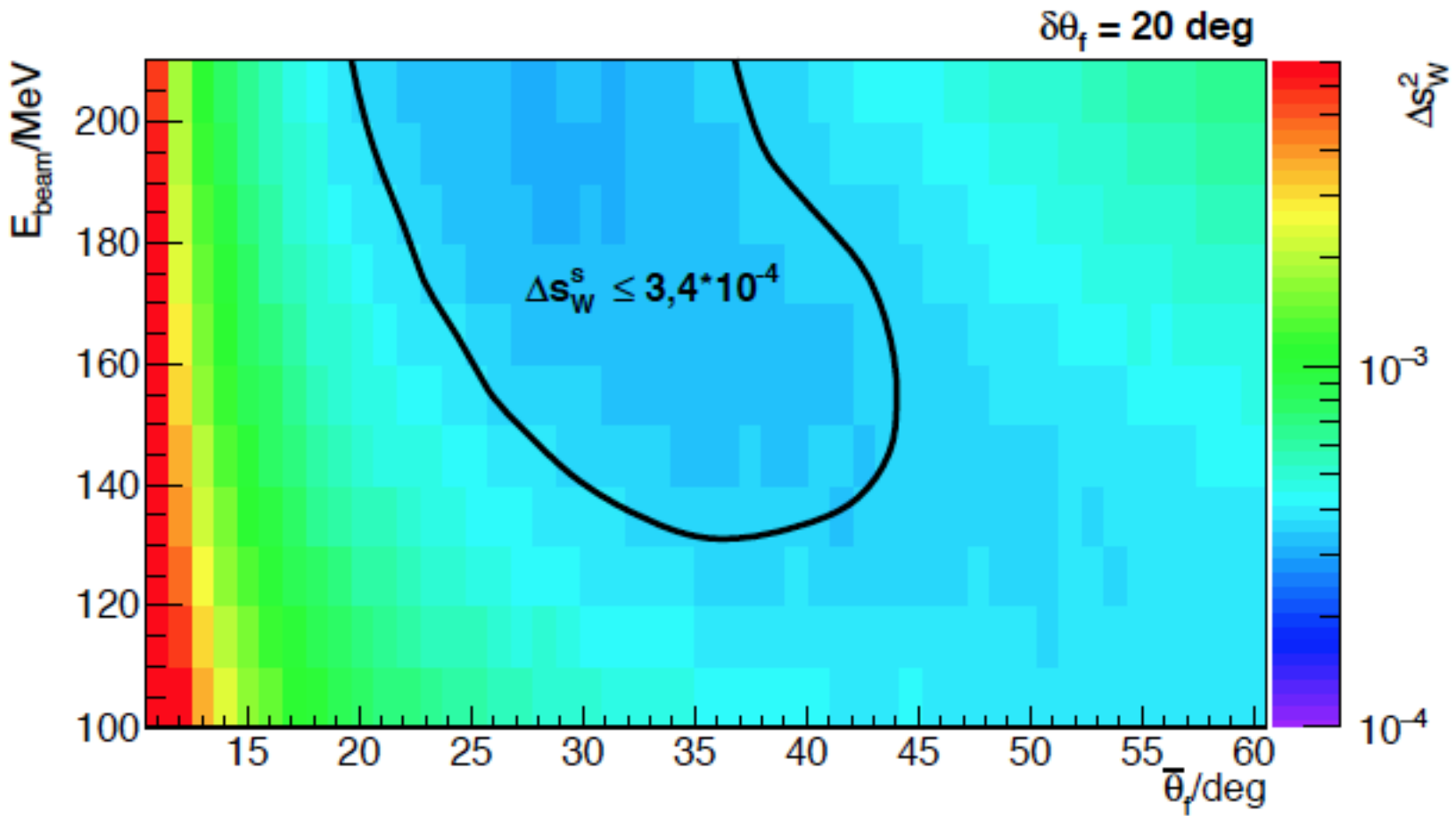
# JGU P2-Precision in $\sin^2 \theta_w$

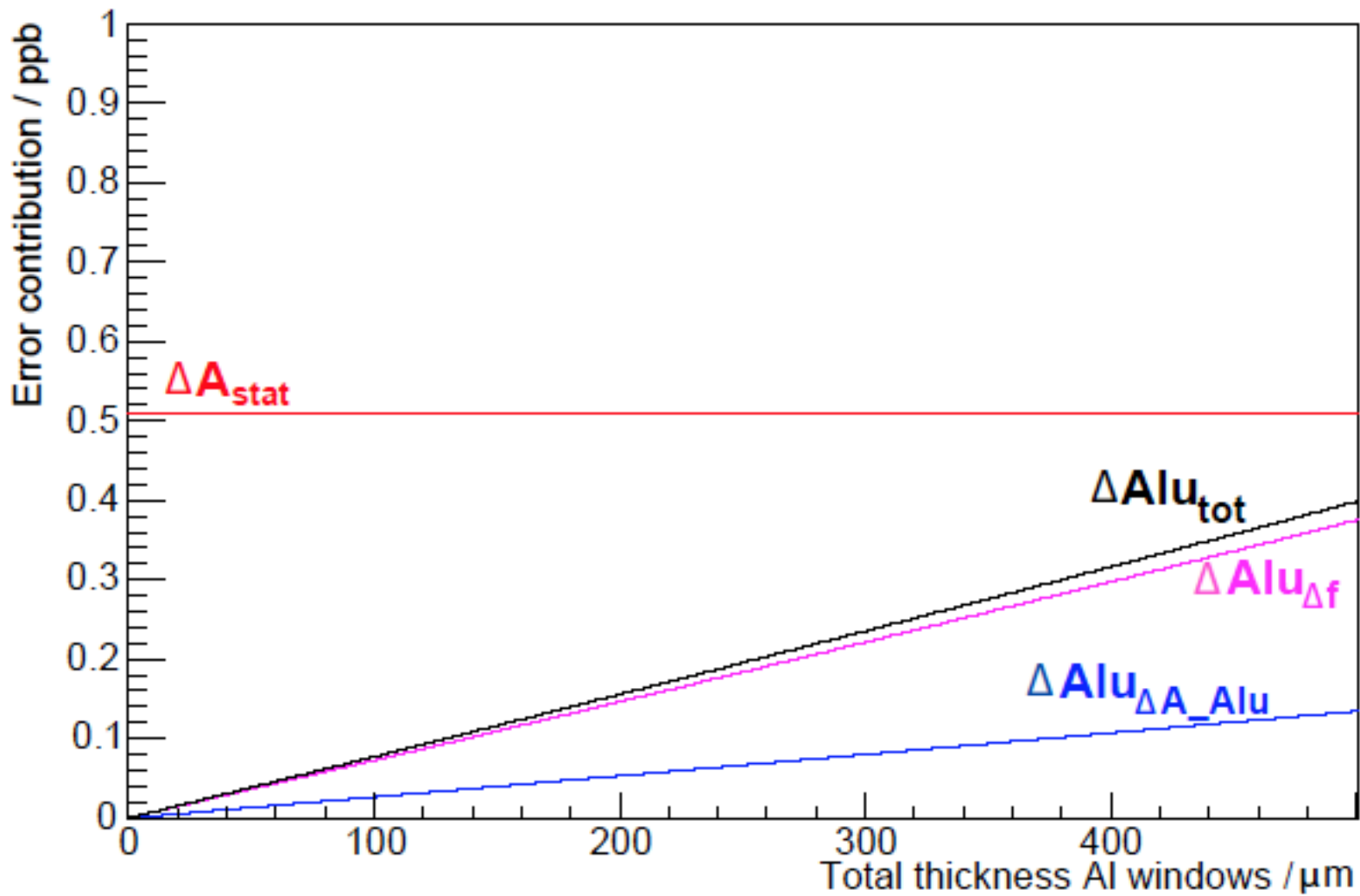


	Total	Statistics	Polarization	Apparative	FF	Re( $\square_{\gamma Z A}$ )
$\Delta \sin^2(\theta_w)$	3.1e-4 (0.13 %)	2.6e-4 (0.11 %)	9.7e-5 (0.04 %)	7.0e-5 (0.03 %)	1.4e-4 (0.04 %)	6e-5 (0.03 %)
$\Delta A^{exp}/ppb$	0.44 (1.5 %)	0.38 (1.34 %)	0.14 (0.49 %)	0.10 (0.35 %)	0.11 (0.38 %)	0.09 (0.32 %)



# Optimization of beam energy and mean scattering angle $\theta$

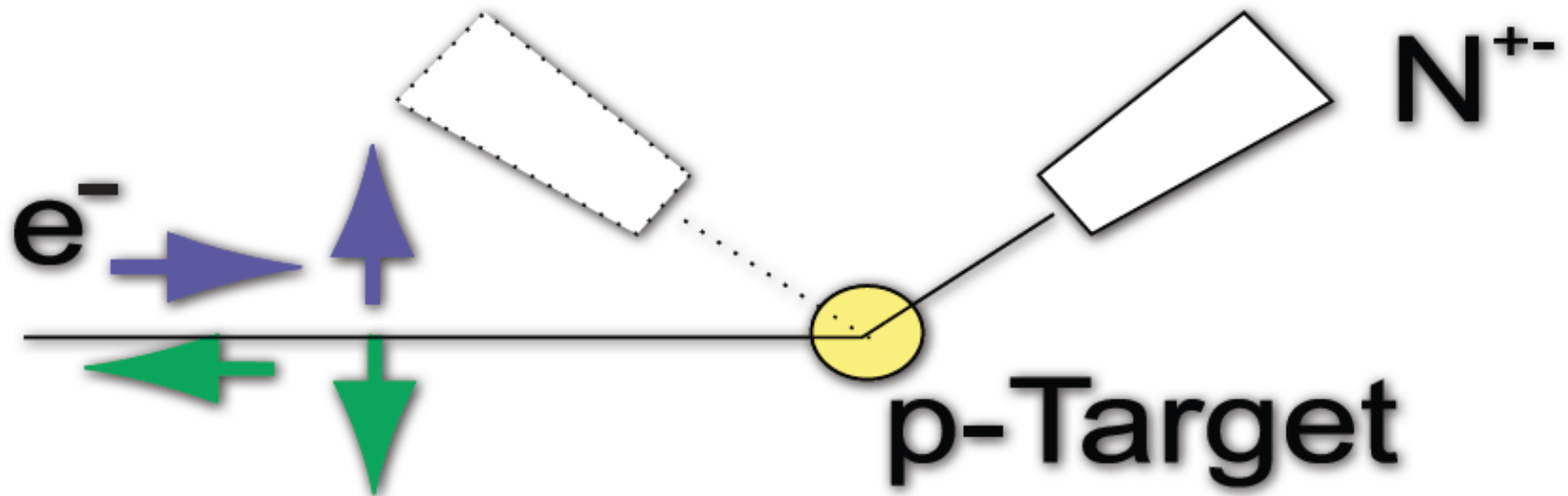




$E_{\text{beam}}$	155 MeV
$\bar{\theta}_f$	35°
$\delta\theta_f$	20°
$\langle Q^2 \rangle_{L=600 \text{ mm}, \delta\theta_f=20^\circ}$	$6 \times 10^{-3} (\text{GeV}/c)^2$
$\langle A^{\text{exp}} \rangle$	-39.94 ppb
$(\Delta A^{\text{exp}})_{\text{Total}}$	0.56 ppb (1.40 %)
$(\Delta A^{\text{exp}})_{\text{Statistics}}$	0.51 ppb (1.28 %)
$(\Delta A^{\text{exp}})_{\text{Polarization}}$	0.21 ppb (0.53 %)
$(\Delta A^{\text{exp}})_{\text{Apparative}}$	0.10 ppb (0.25 %)
$\langle s_W^2 \rangle$	0.231 16
$(\Delta s_W^2)_{\text{Total}}$	$3.3 \times 10^{-4}$ (0.14 %)
$(\Delta s_W^2)_{\text{Statistics}}$	$2.7 \times 10^{-4}$ (0.12 %)
$(\Delta s_W^2)_{\text{Polarization}}$	$1.0 \times 10^{-4}$ (0.04 %)
$(\Delta s_W^2)_{\text{Apparative}}$	$0.5 \times 10^{-4}$ (0.02 %)
$(\Delta s_W^2)_{\square_{\gamma Z}}$	$0.4 \times 10^{-4}$ (0.02 %)
$(\Delta s_W^2)_{\text{nucl. FF}}$	$1.2 \times 10^{-4}$ (0.05 %)
$\langle Q^2 \rangle_{\text{Cherenkov}}$	$4.57 \times 10^{-3} (\text{GeV}/c)^2$
$\langle A^{\text{exp}} \rangle_{\text{Cherenkov}}$	-28.77 ppb



Conceptually very simple experiments



$$A = (N^+ - N^-) / (N^+ + N^-) \quad \Delta A = (N^+ + N^-)^{-1/2} = N^{-1/2}$$

$$A = 20 \times 10^{-9} \quad 2\% \text{ Measurement} \quad N = 6.25 \times 10^{18} \text{ events}$$

Highest rate, measure  $Q^2$ : **Large Solid Angle Spectrometers**



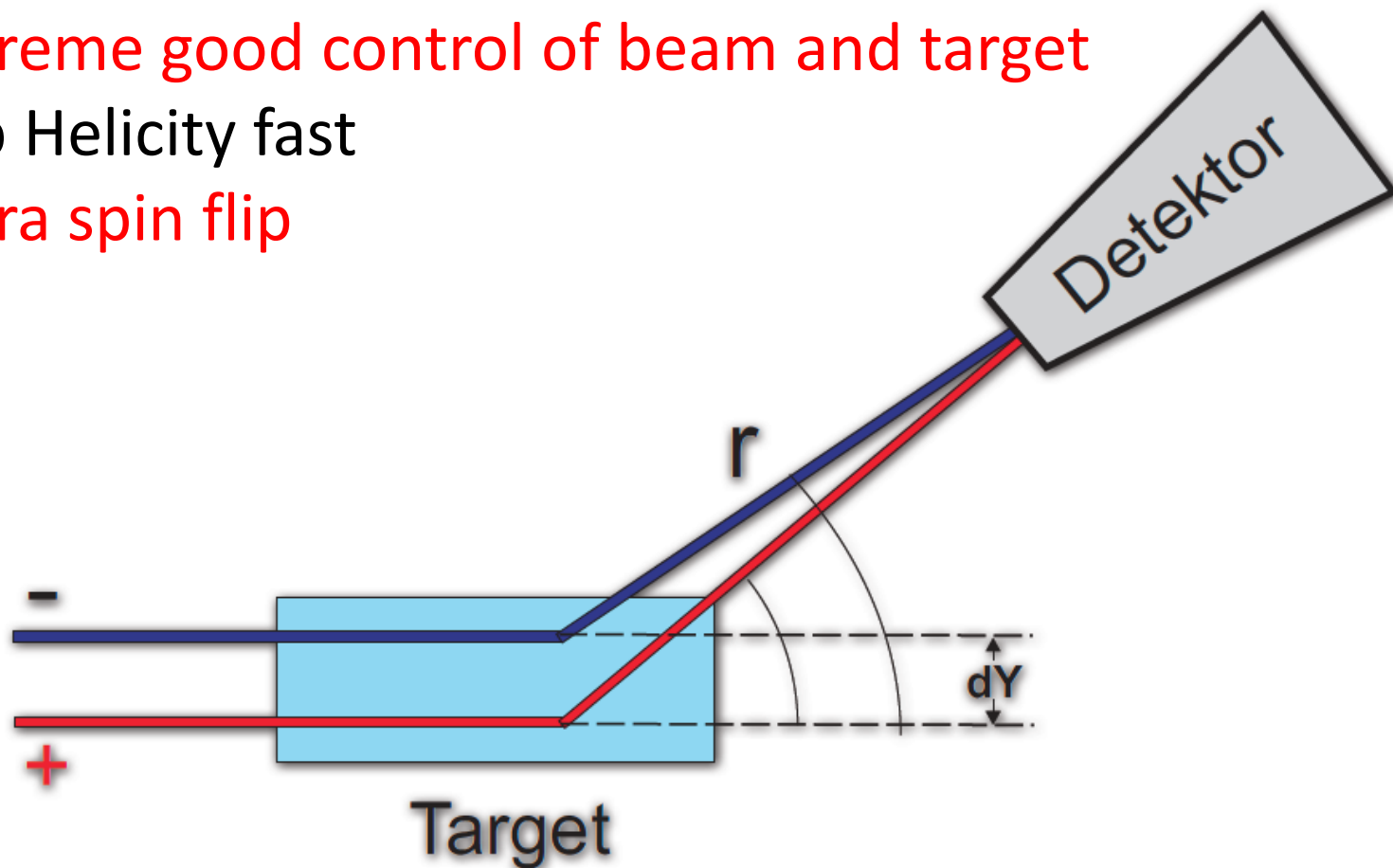


Apparative (false) asymmetries:

Extreme good control of beam and target

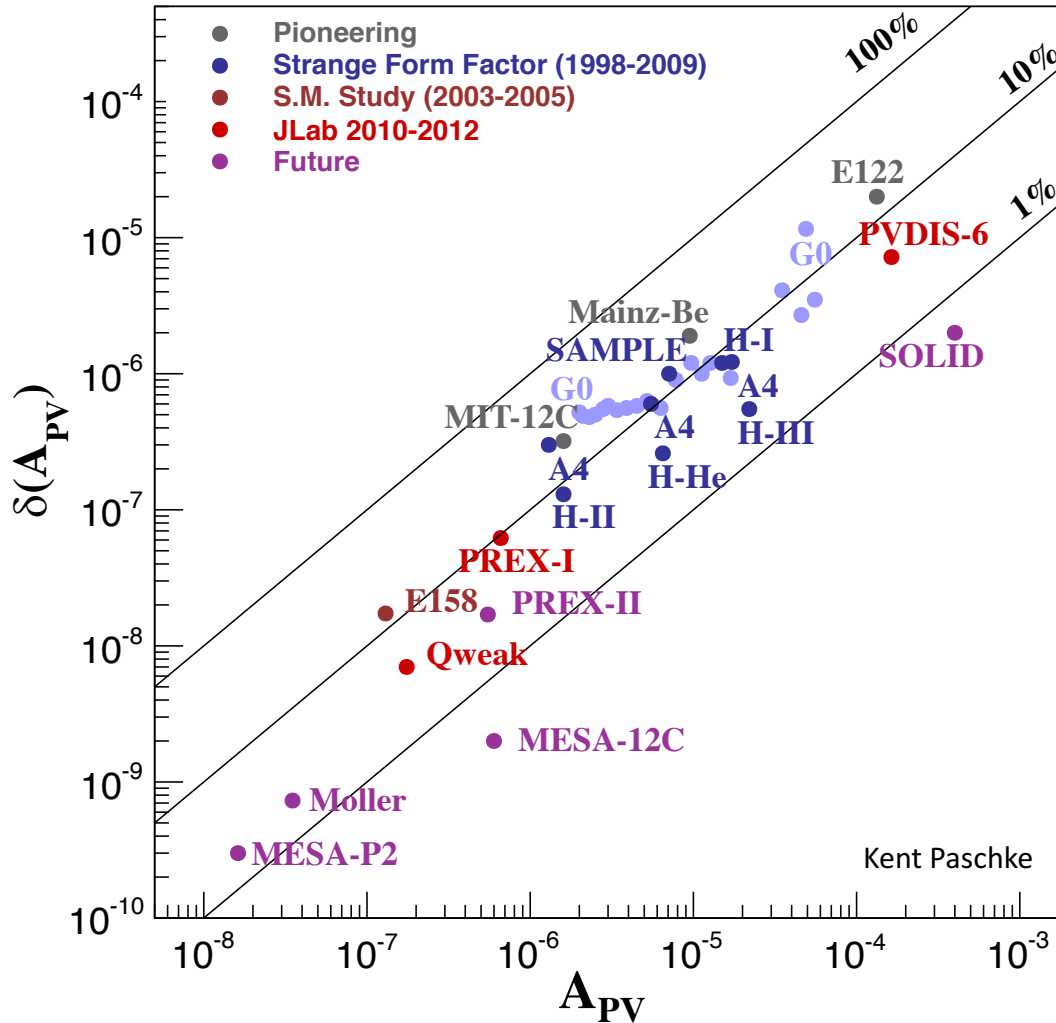
Flip Helicity fast

Extra spin flip



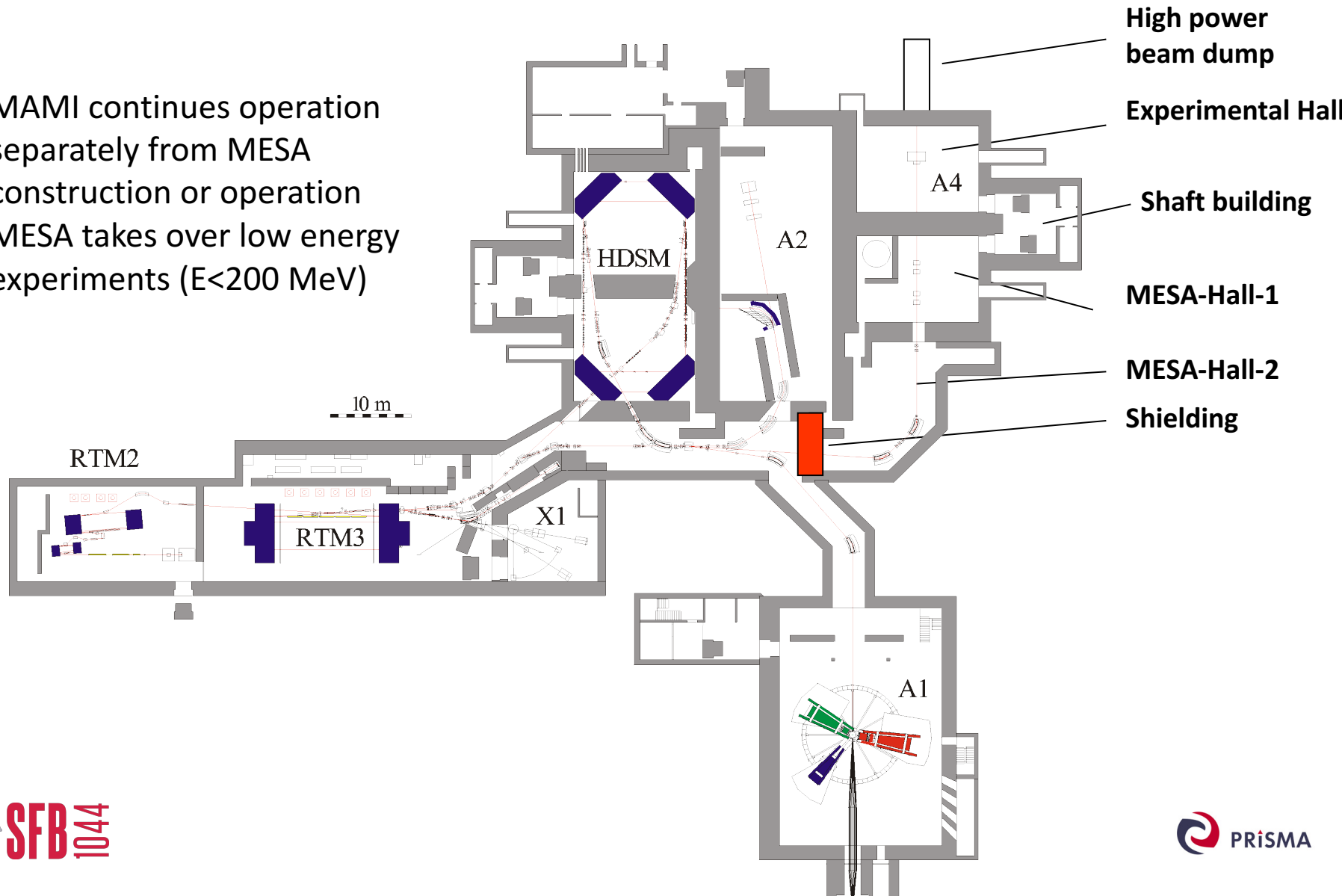


# PVeS Experiment Summary



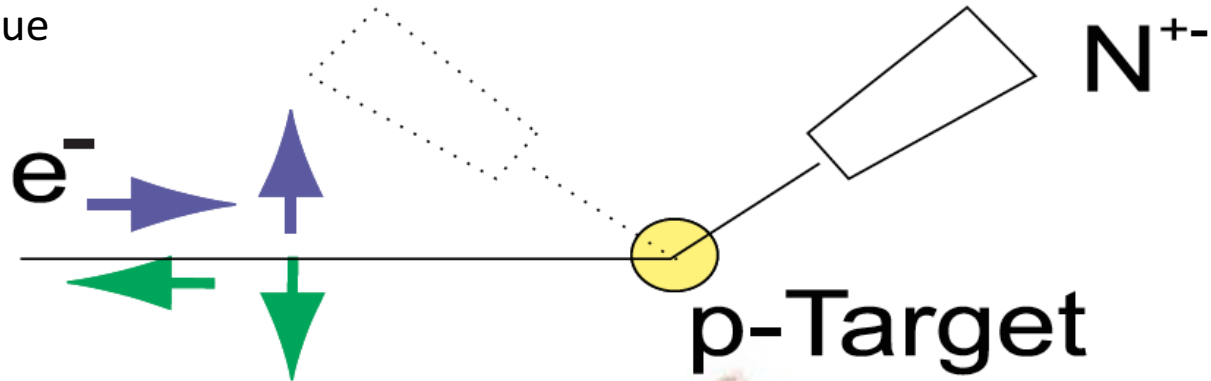


- MAMI continues operation separately from MESA construction or operation
- MESA takes over low energy experiments ( $E < 200$  MeV)





## Counting Technique

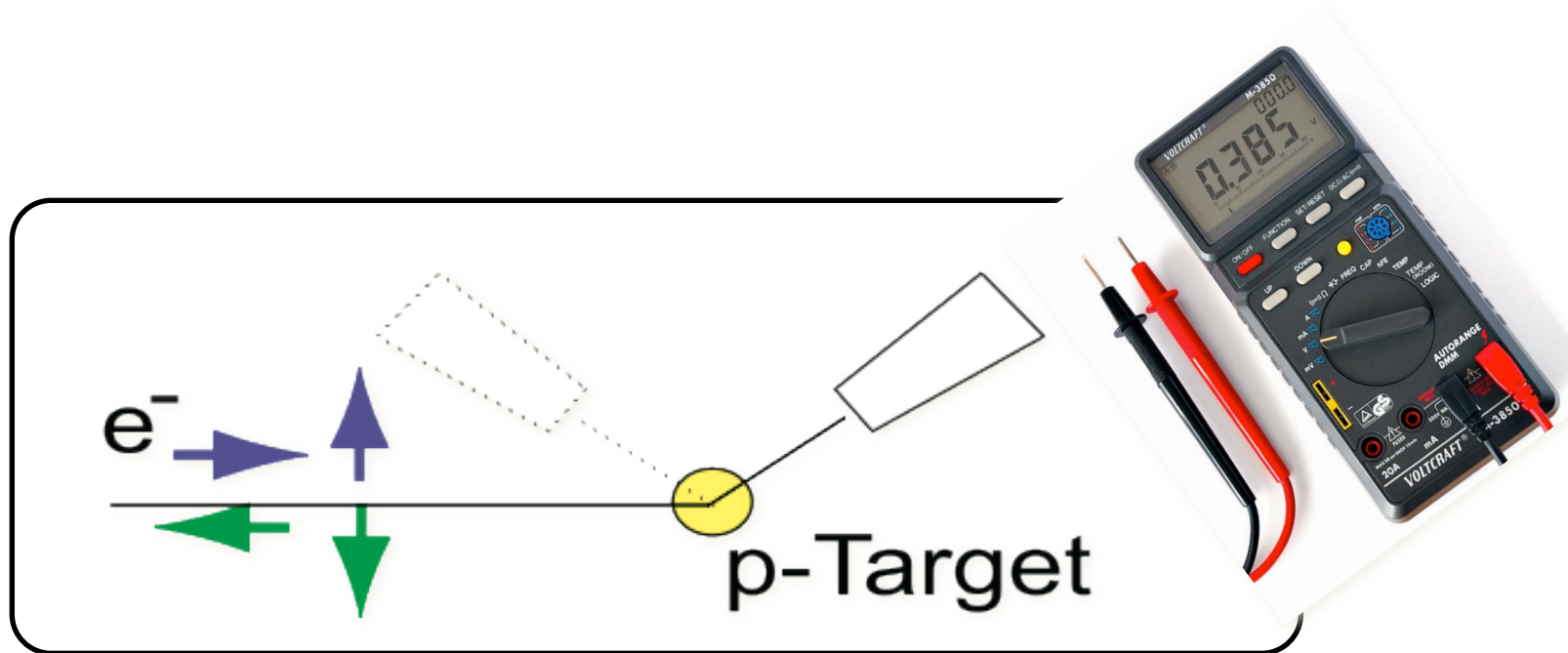


Count scattered electrons:

- pile-up (double count losses)
- Background Asymmetry
- Very Fast Counting (MHz)
- Measure TOF or Energy



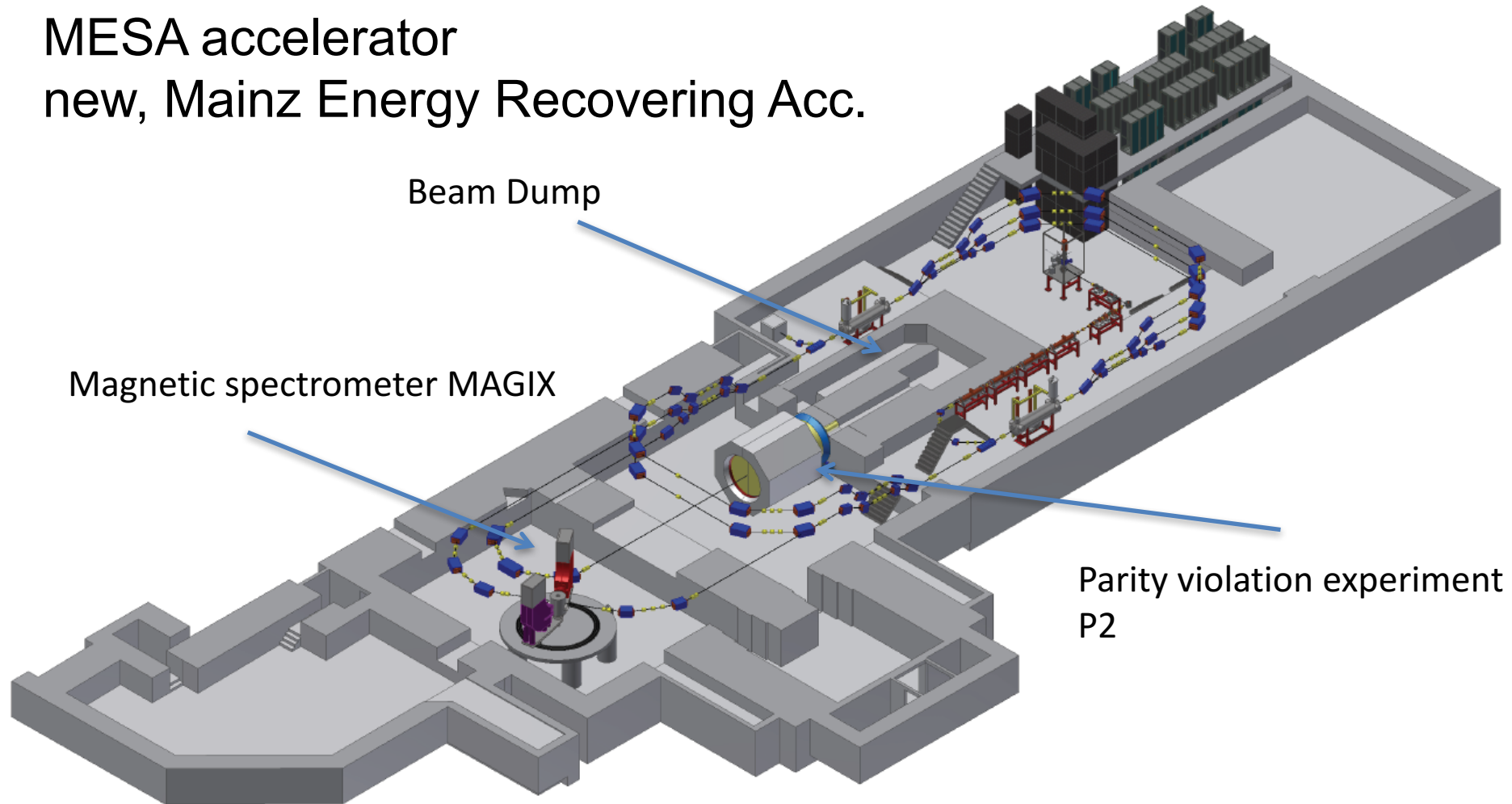
## Analogue Technique



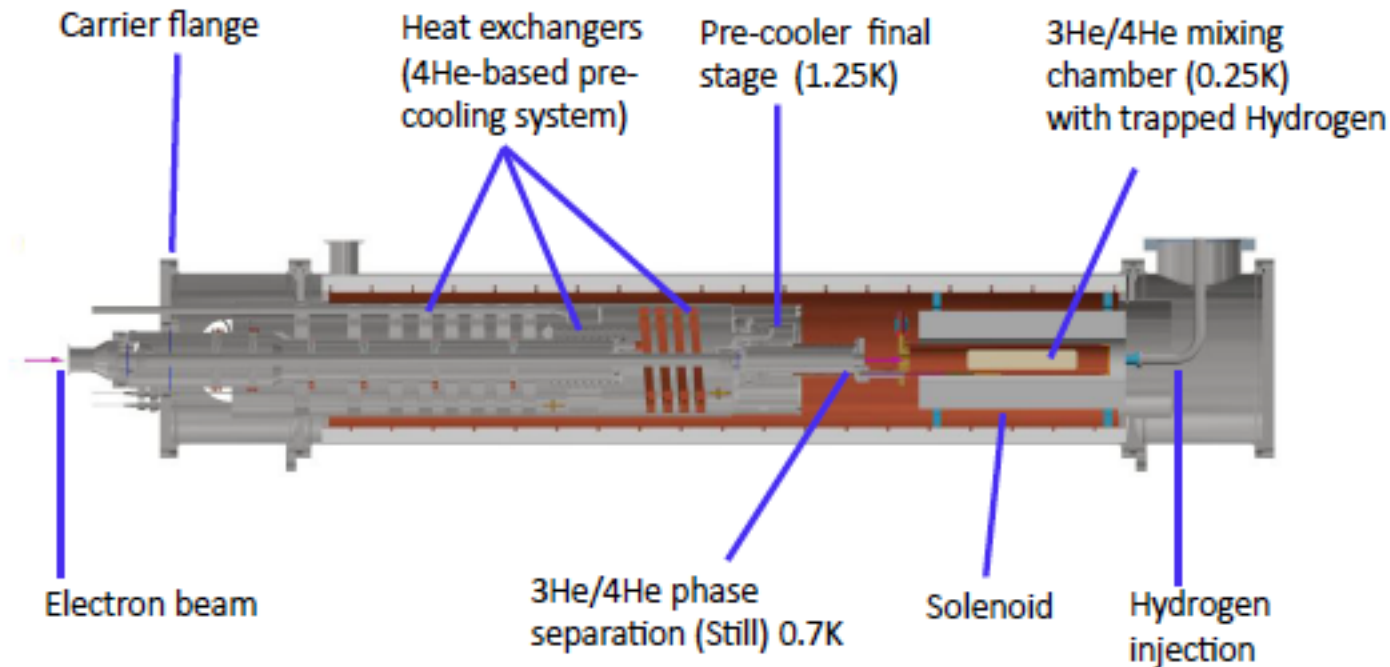
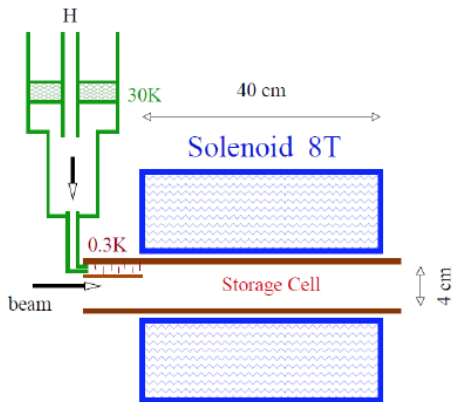
- Measure Flux of Scattered electrons:
- no pile-up (double count losses)
  - sensitive to small electr. fields.
  - no separation of phys. process



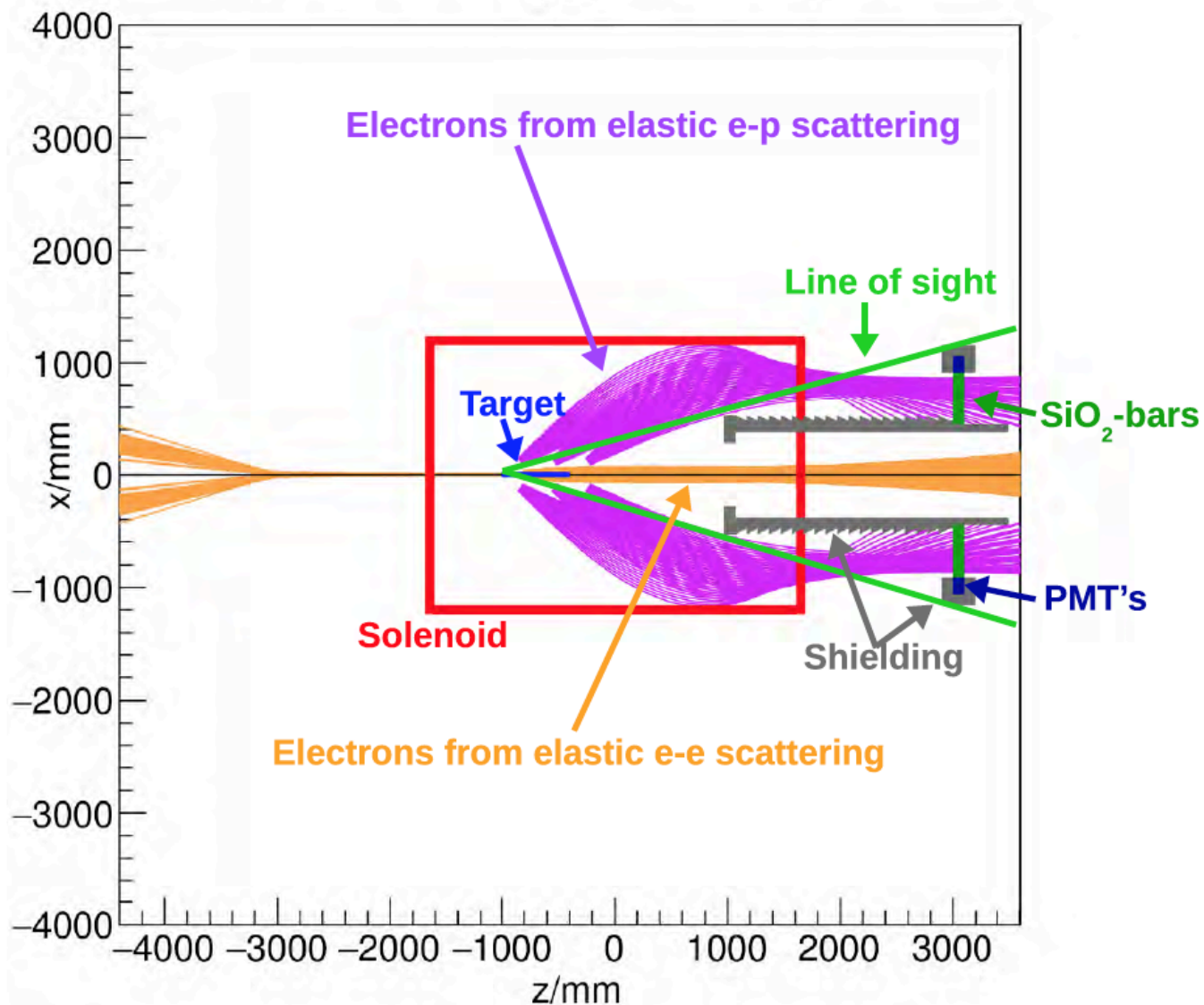
# MESA accelerator new, Mainz Energy Recovering Acc.





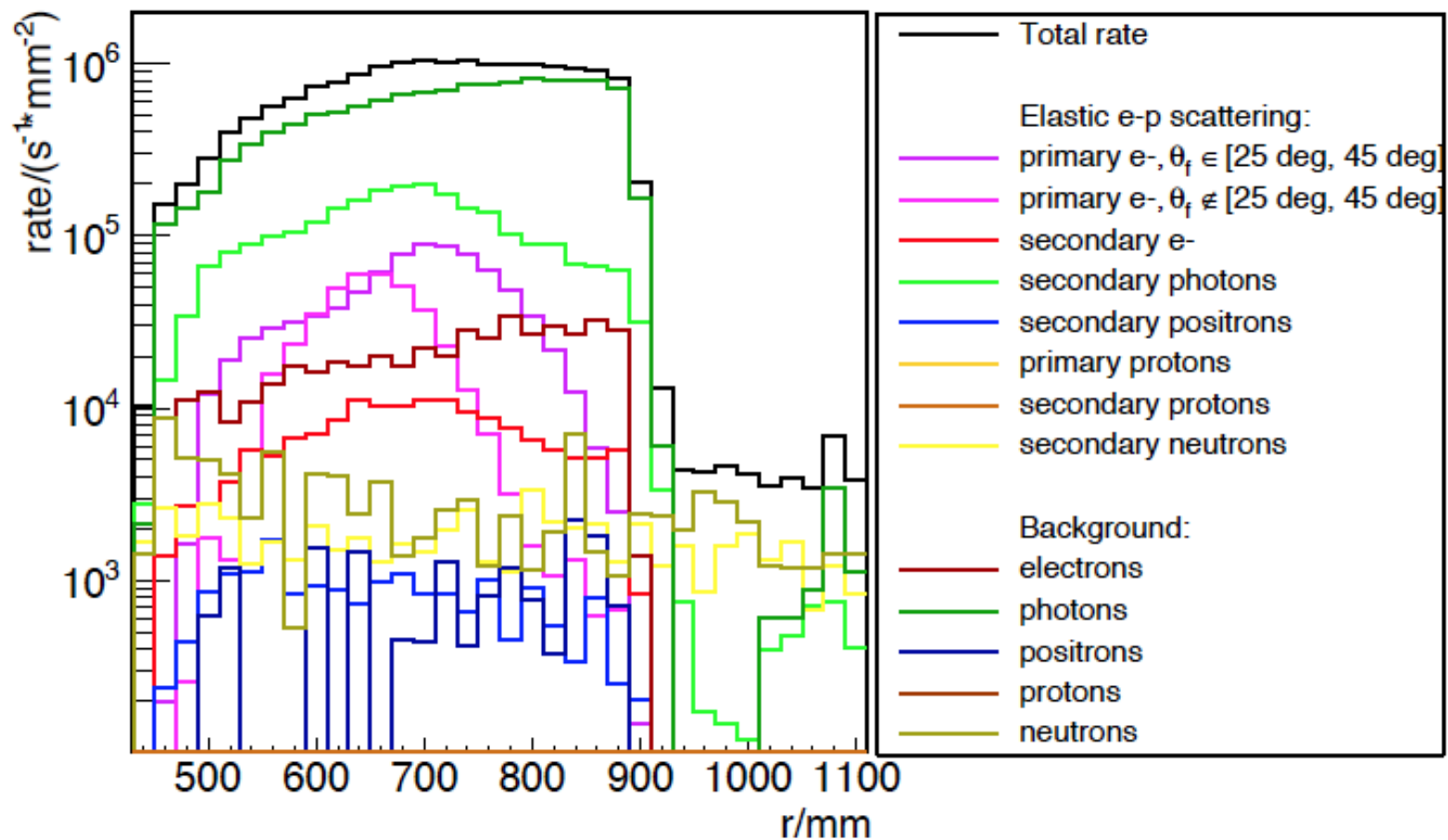


Simple ray-tracing

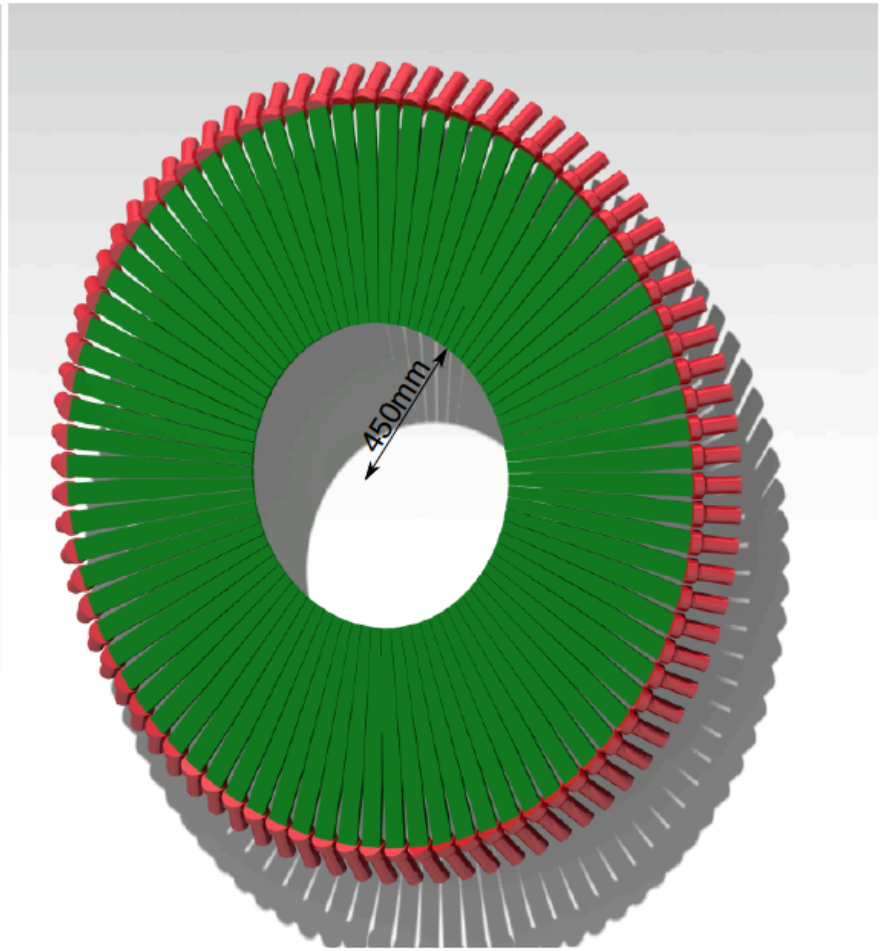
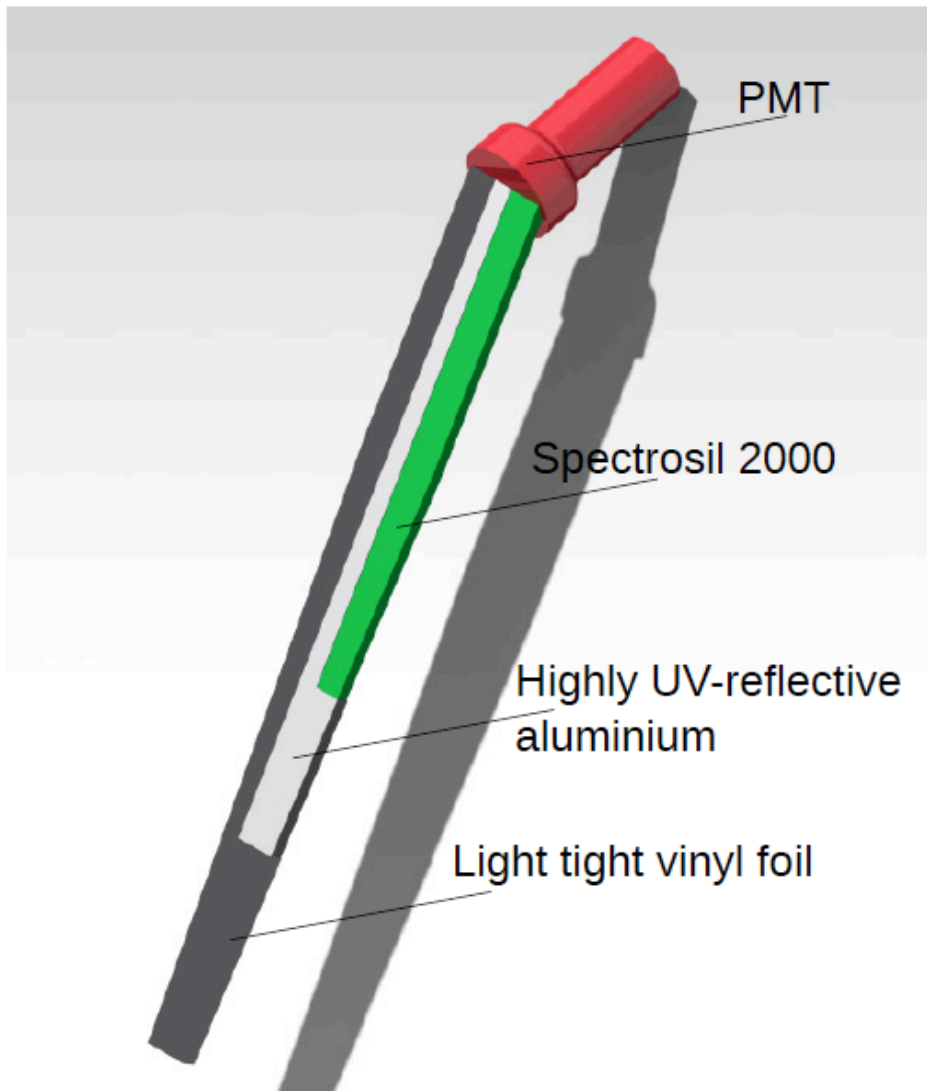




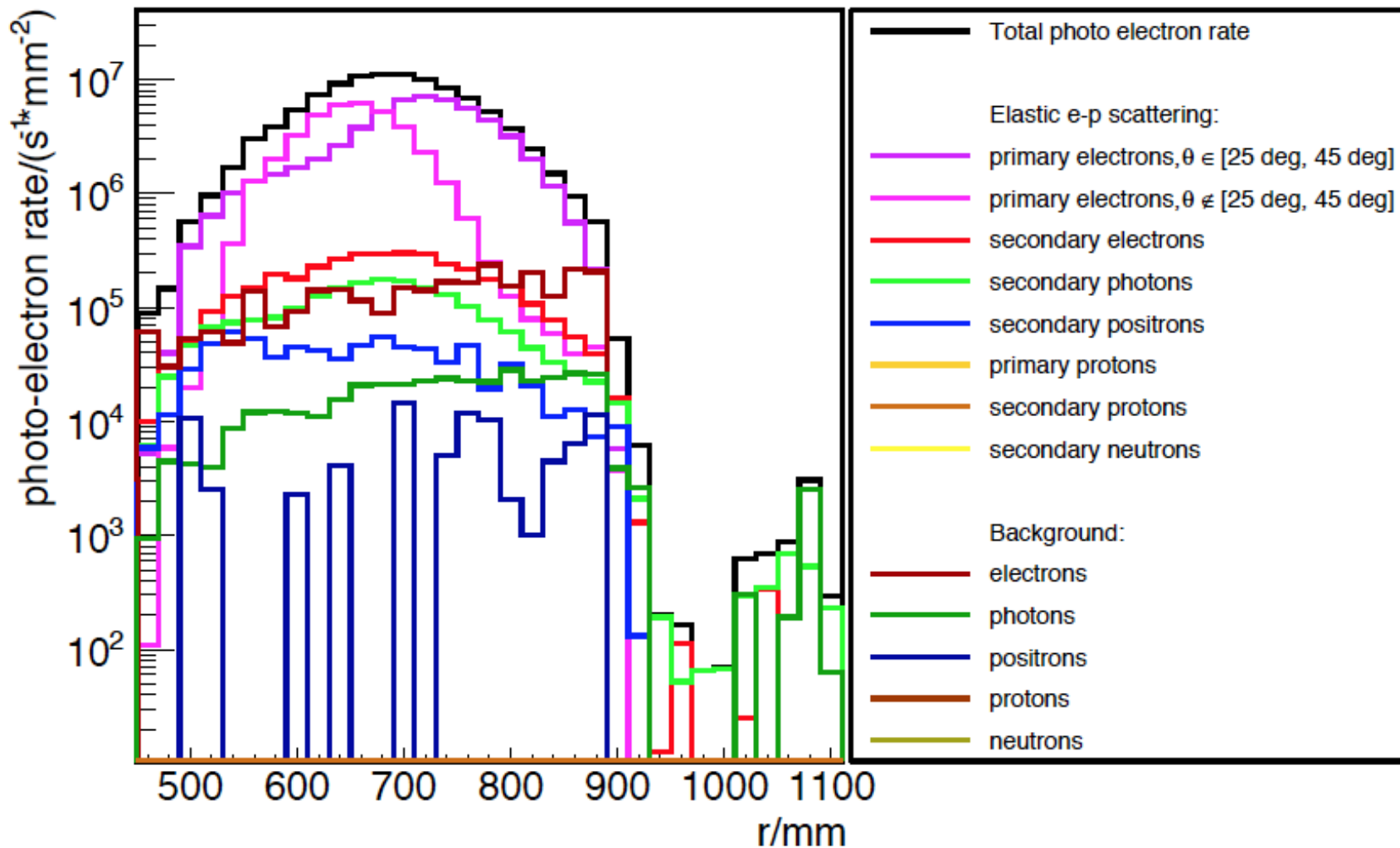
Full GEANT4 simulation



Full GEANT4 simulation



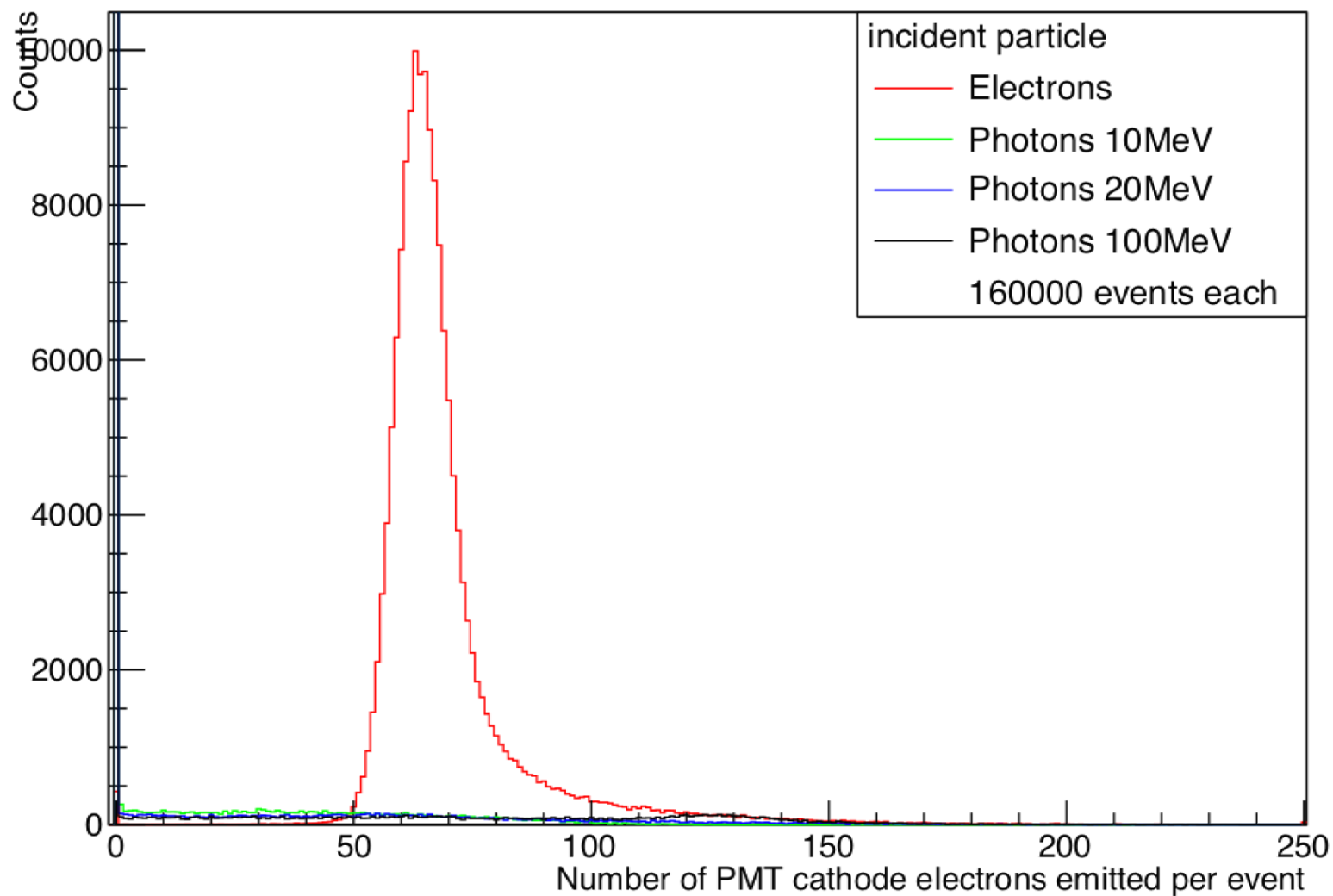
Full GEANT4 simulation



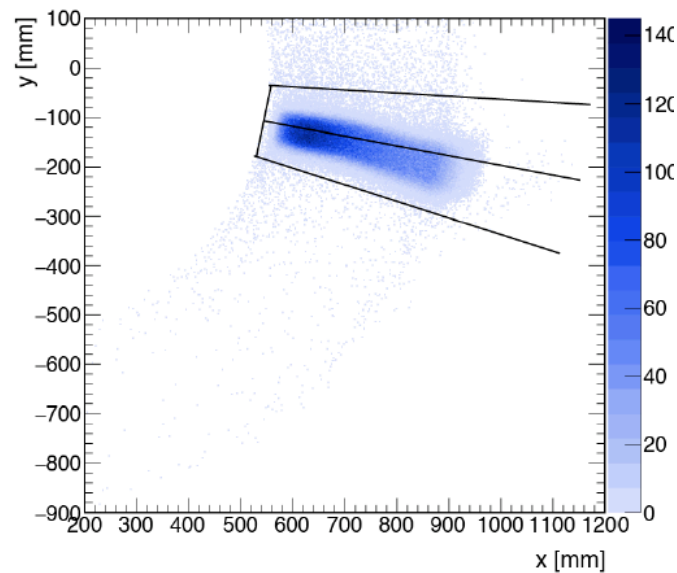
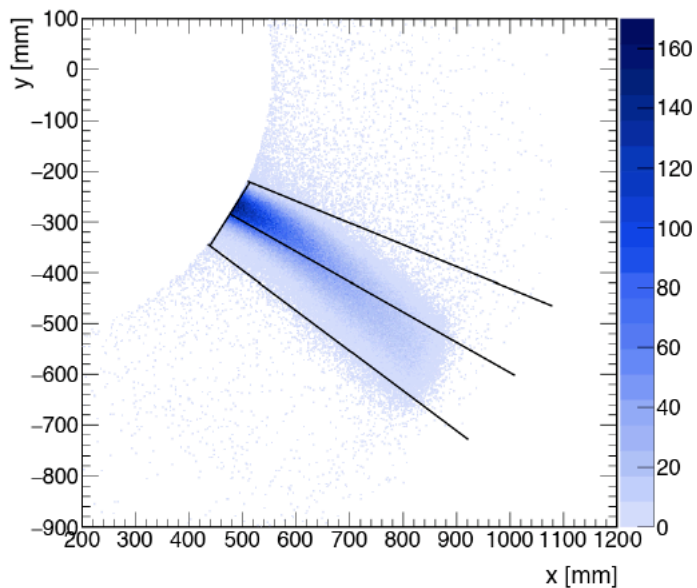
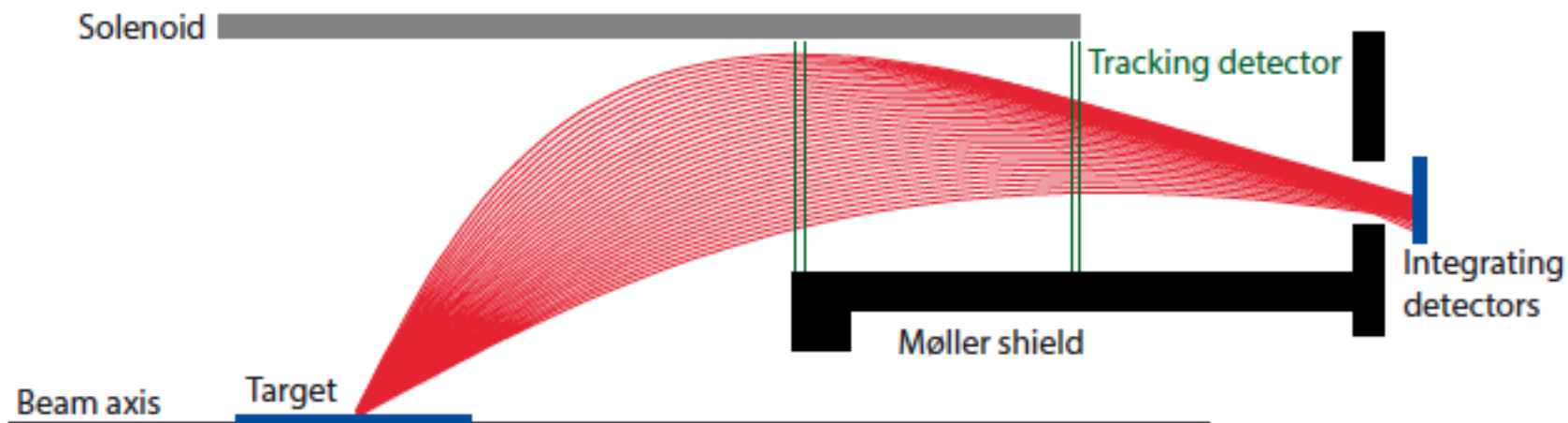




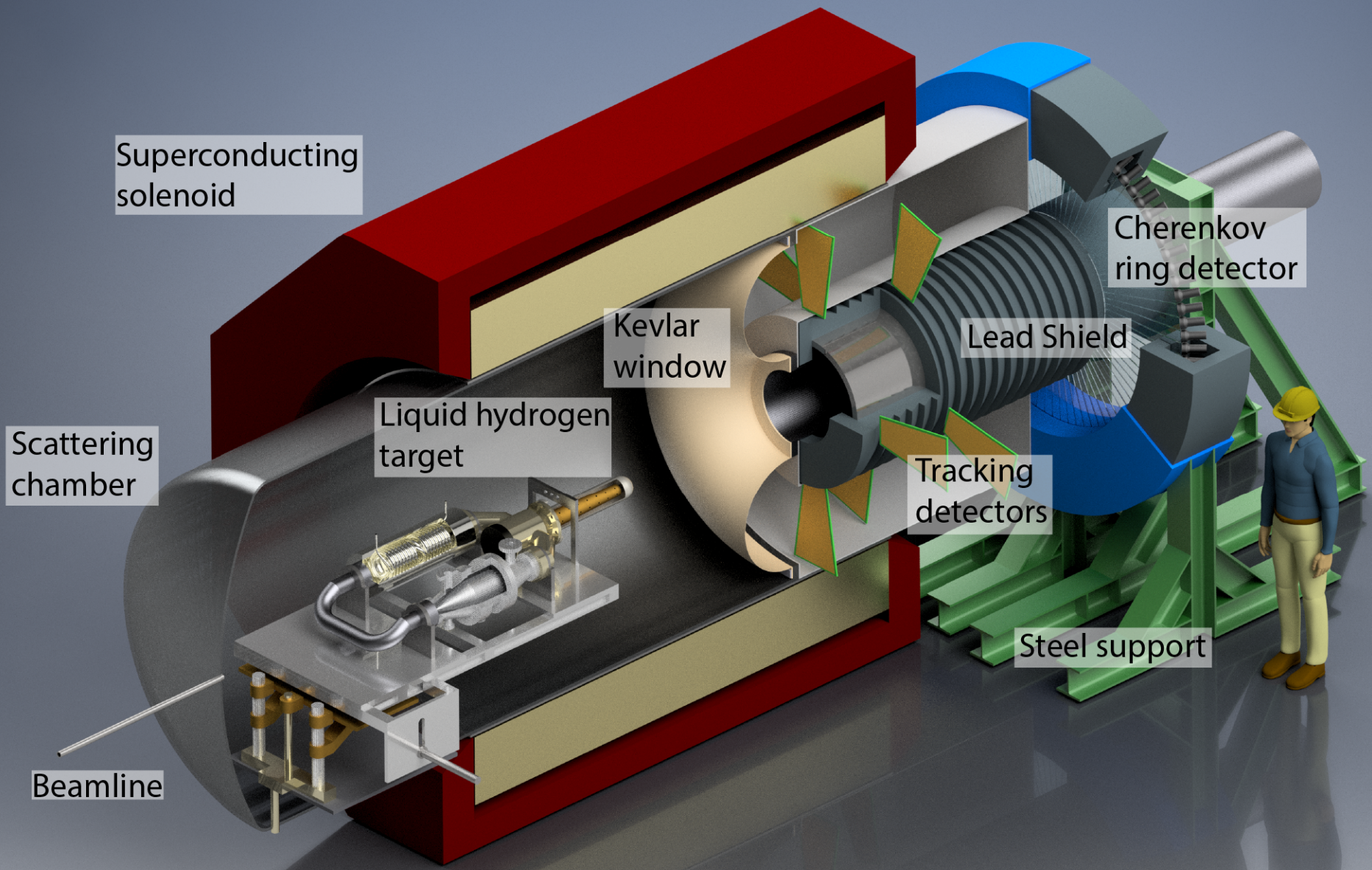
## Number of PMT cathode electrons emitted per event











P2-Experimental Setup



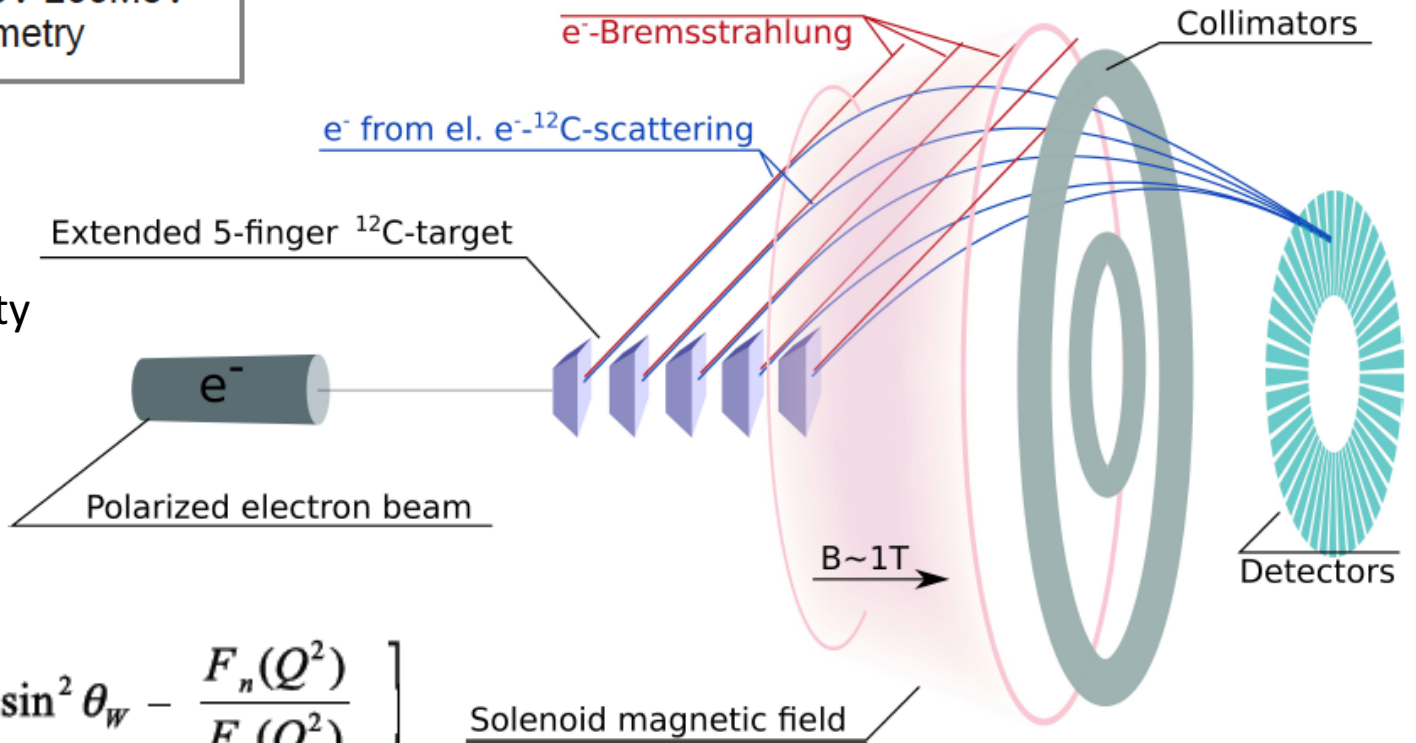
Other Measurements:  
Carbon, Lead



## EXPERIMENTAL REALIZATION

- MESA:
- 150μA
  - 150MeV-200MeV
  - Polarimetry

Enhanced sensitivity  
 To new physics

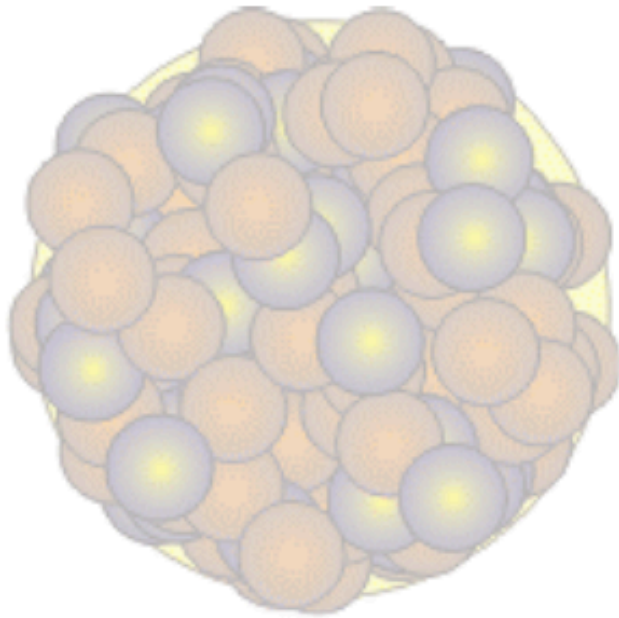


$$-N = \frac{G_F Q^2}{2\pi\alpha\sqrt{2}} \left[ \underbrace{\sin^2 \theta_W}_{\approx 0} - \frac{F_n(Q^2)}{F_p(Q^2)} \right]$$



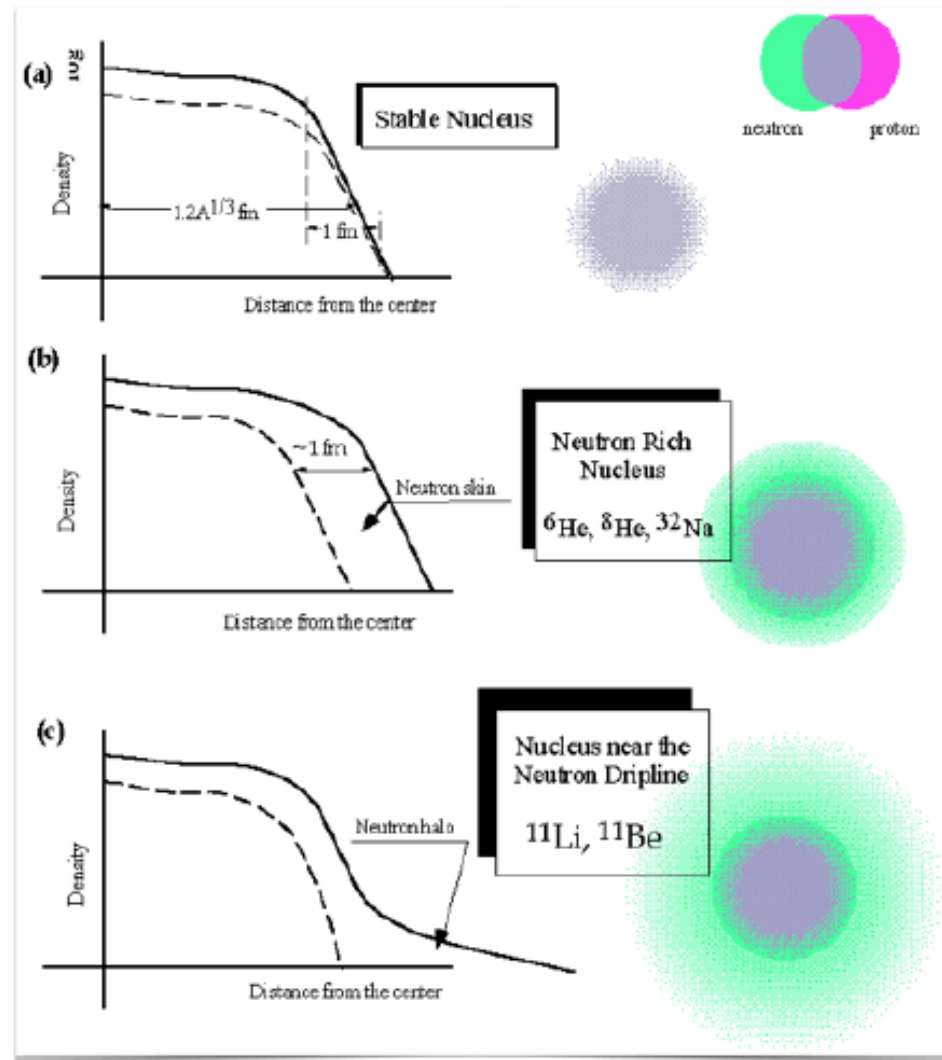
# Neutron Skin for beginner

Where do the neutrons go?



Pressure forces neutrons out against surface tension

→ EOS





## The P2 Experiment [arXiv:1802.04759](https://arxiv.org/abs/1802.04759)

**A future high-precision measurement of the electroweak mixing angle at low momentum transfer**

Dominik Becker<sup>1,2</sup>, Razvan Bucoveanu<sup>1,3</sup>, Carsten Grzesik<sup>1,2</sup>, Ruth Kempf<sup>1,2</sup>, Kathrin Imai<sup>1,2</sup>, Matthias Molitor<sup>1,2</sup>, Alexey Tyukin<sup>1,2</sup>, Marco Zimmermann<sup>1,2</sup>, David Armstrong<sup>4</sup>, Kurt Aulenbacher<sup>1,2,5</sup>, Sebastian Baunack<sup>1,2</sup>, Rakitha Beminiwattha<sup>6</sup>, Niklaus Berger<sup>1,2</sup>, Peter Bernhard<sup>1,7</sup>, Andrea Brogna<sup>1,7</sup>, Luigi Capozza<sup>1,2,5</sup>, Silviu Covrig Dusa<sup>8</sup>, Wouter Deconinck<sup>4</sup>, Jürgen Diefenbach<sup>1,2</sup>, James Dunne<sup>17</sup>, Jens Erler<sup>9</sup>, Ciprian Gal<sup>10</sup>, Boris Gläser<sup>1,2</sup>, Boxing Gou<sup>1,2,5</sup>, Wolfgang Gradl<sup>1,2</sup>, Michael Gericke<sup>11</sup>, Mikhail Gorchtein<sup>1,2</sup>, Yoshio Imai<sup>1,2</sup>, Krishna S. Kumar<sup>12</sup>, Frank Maas<sup>1,2,5,a</sup>, Juliette Mammei<sup>11</sup>, Jie Pan<sup>11</sup>, Preeti Pandey<sup>11</sup>, Kent Paschke<sup>10</sup>, Ivan Perić<sup>13</sup>, Mark Pitt<sup>14</sup>, Sakib Rahman<sup>11</sup>, Seamus Riordan<sup>15</sup>, David Rodríguez Piñeiro<sup>1,2,5</sup>, Concettina Sfienti<sup>1,2,3,7</sup>, Iurii Sorokin<sup>1,2</sup>, Paul Souder<sup>16</sup>, Hubert Spiesberger<sup>1,3</sup>, Michaela Thiel<sup>1,2</sup>, Valery Tyukin<sup>1,2</sup>, and Quirin Weitzel<sup>1,7</sup>

<sup>1</sup> PRISMA Cluster of Excellence, Johannes Gutenberg-Universität Mainz, Germany

<sup>2</sup> Institute of Nuclear Physics, Johannes Gutenberg-Universität Mainz, Germany

<sup>3</sup> Institute of Physics, Johannes Gutenberg-Universität, Mainz, Germany

<sup>4</sup> College of William and Mary, Williamsburg, Virginia, USA

<sup>5</sup> Helmholtz Institute Mainz, Johannes Gutenberg-Universität Mainz, Germany

<sup>6</sup> Louisiana Tech University, Ruston, Louisiana, USA

<sup>7</sup> Detector Laboratory, PRISMA Cluster of Excellence, Johannes Gutenberg-Universität Mainz, Germany

<sup>8</sup> Thomas Jefferson National Accelerator Facility, Newport News, Virginia, USA

<sup>9</sup> Departamento de Física Teórica, Instituto de Física, Universidad Nacional Autónoma de México, CDMX, México

<sup>10</sup> University of Virginia, Charlottesville, Virginia, USA

<sup>11</sup> Department of Physics and Astronomy, University of Manitoba, Winnipeg, Canada

<sup>12</sup> Department of Physics and Astronomy, Stony Brook University, Stony Brook, USA

<sup>13</sup> Institute for Data Processing and Electronics, Karlsruhe Institute of Technology, Karlsruhe, Germany

<sup>14</sup> Virginia Tech University, Blacksburg, Virginia, USA

<sup>15</sup> Physics Division, Argonne National Laboratory, Argonne, USA

<sup>16</sup> Physics Department, Syracuse University, Syracuse, USA

<sup>17</sup> Mississippi State University, Mississippi State, MS, USA





- Parity violating electron scattering: “Low energy frontier” comprises a sensitive test of the standard model **complementary to LHC**
- Determination of  $\sin^2(\theta_w)$  with high precision (similar to Z-pole)
- P2-Experiment (proton weak charge) in Mainz under preparation  
New MESA energy recovering accelerator at 155 MeV, target precision is 2 % in weak proton charge i.e. 0.15% in  $\sin^2(\theta_w)$ ,  
Sensitivity to new physics up to a scale of **50 MeV up to 50 TeV**
- Much more physics from PV electron scattering
- Together with Moeller@Jlab (electron weak charge) and SOLID@Jlab (quark weak charge) very sensitive test of standard model and possibility to narrow in on Standard Model Extension