

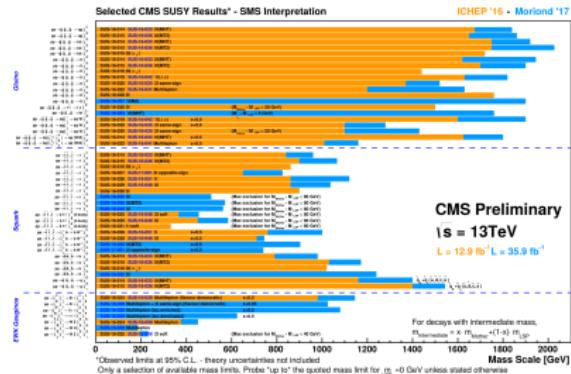
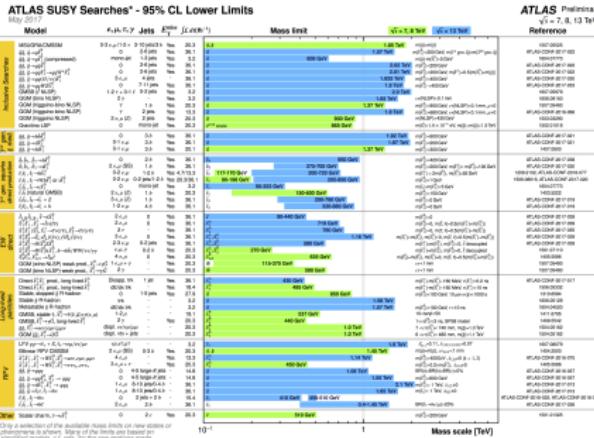
Introduction to EFT

Ian Lewis
University of Kansas

February 27, 2018
Probing Physics Beyond the Standard Model with Precision
MITP

Goal: Find New BSM Physics

- LHC very successful so far: Discovered Higgs boson and obtained huge amount of data.
 - However, have only confirmed the SM.
 - $O(1 \text{ TeV})$ lower bounds on new physics:



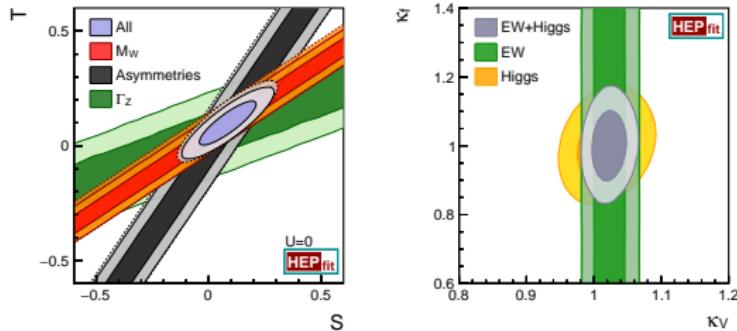
“Model Independent” Parameterization

- In the absence of direct evidence, useful to have a model independent formulation of new physics.
- Philosophy:
 - We know the SM is there at the EW scale with a very SM-like Higgs boson.
 - Treat $SU(2) \times U(1)_Y$ as a good symmetry.
- SM effective field theory (EFT) [Buchmuller, Wyler NPB268 \(1986\) 621; Grzadkowski, Iskrzynski, Misiak, Rosiek, JHEP 1010 \(2010\) 085; Giudice, Grojean, Pomarol, Rattazzi JHEP 0706 \(2007\) 045; Hagiwara, Ishihara, Szalapski, Zeppenfeld PRD48 \(1993\) 2182; Brivio, Trott arXiv:1706.08945](#)

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_{n=1}^{\infty} \sum_k \frac{c_{n,k}}{\Lambda^n} O_{n,k}$$

- $O_{n,k}$: $SU(3) \times SU(2)_L \times U(1)_Y$ gauge invariant $4+n$ dimensional higher order operators.
- Λ : scale of new physics.
- Allows for a systematic parameterization of deviations from SM predictions without doing too much damage to lower energy measurements.

Electroweak Precision



de Blas, et al arXiv:1710.05402

- LEP constraints on anomalous quark couplings [Falkowski, Riva JHEP 1502](#):

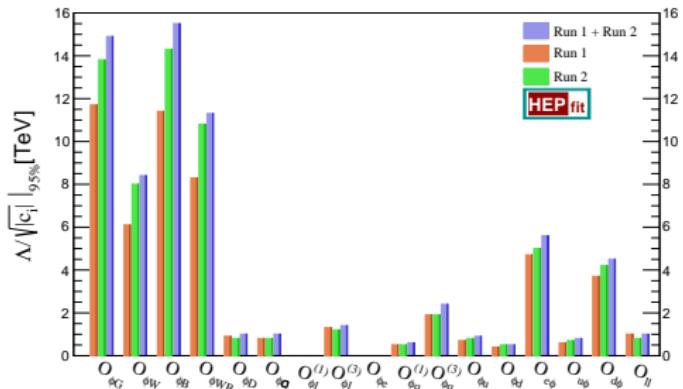
$$\delta g_L^{Zd} = (2.3 \pm 1) \times 10^{-3}$$

$$\delta g_L^{Zu} = (-2.6 \pm 1.6) \times 10^{-3}$$

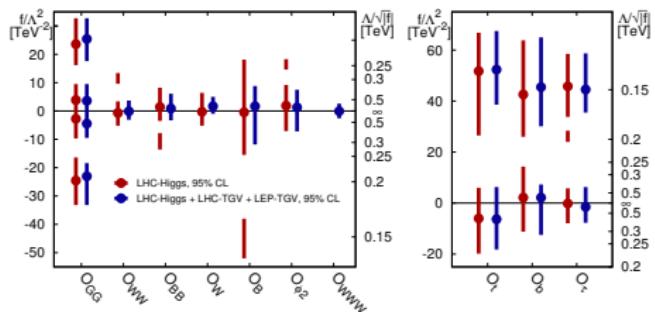
$$\delta g_R^{Zd} = (16.0 \pm 5.2) \times 10^{-3}$$

$$\delta g_R^{Zu} = (-3.6 \pm 3.5) \times 10^{-3}$$

Fits to LHC Data

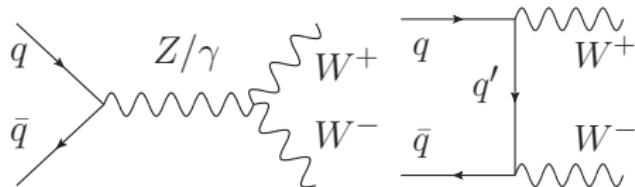


de Blas, et al arXiv:1710.05402



Butter et al JHEP 1607 (2016) 152

W^+W^- production



- Informative to focus on one process.
 - Of particular interest is the electroweak sector.
 - Focus on W^+W^- production at the LHC.
 - Sensitive to anomalous trilinear gauge boson couplings (ATGCs)
- Operators affecting ATGCs:

$$\begin{aligned} O_{3W} &= \epsilon^{abc} W_\mu^{av} W_v^{bp} W_p^{cu} & O_{HD} &= |\Phi^\dagger D_\mu \Phi|^2 & O_{HWB} &= \Phi^\dagger \sigma^a \Phi W_{\mu\nu}^a B^{\mu\nu} \\ O_{H\ell}^{(3)} &= i \left(\Phi^\dagger \overleftrightarrow{D}_\mu \sigma^a \Phi \right) \bar{\ell}_L \gamma^\mu \sigma^a \ell_L & O_{ll} &= (\bar{\ell}_L \gamma^\mu \ell_L)(\bar{\ell}_L \gamma_\mu \ell_L) \end{aligned}$$

W^+W^- production

- Another language, anomalous couplings [Hagiwara, Peccei, Zeppenfeld, Hikasa NPB482 \(1987\)](#):

$$\delta\mathcal{L} = -ig_{WWV} \left(g_1^V (W_{\mu\nu}^+ W^{-\mu} V^\nu - W_{\mu\nu}^- W^{+\mu} V^\nu) + \kappa^V W_\mu^+ W_\nu^- V^{\mu\nu} + \frac{\lambda^V}{M_W^2} W_{\rho\mu}^+ W^{-\mu} V^\nu V^{\rho\nu} \right)$$

- $V = Z, \gamma$
- $g_{WWZ} = g \cos \theta_w, \quad g_{WW\gamma} = e$

- Parameterize deviations from SM:

$$g_1^Z = 1 + \delta g_1^Z \quad g_1^\gamma = 1 + \delta g_1^\gamma \quad \kappa^Z = 1 + \delta \kappa^Z \quad \kappa^\gamma = 1 + \delta \kappa^\gamma$$

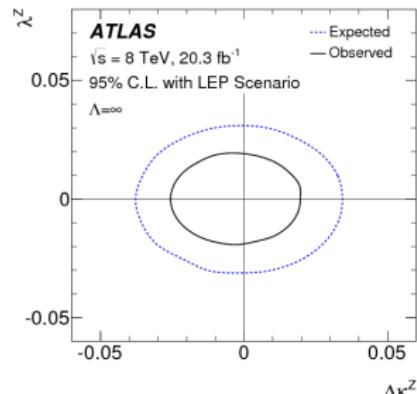
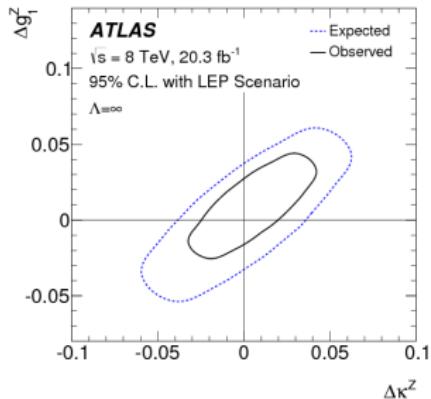
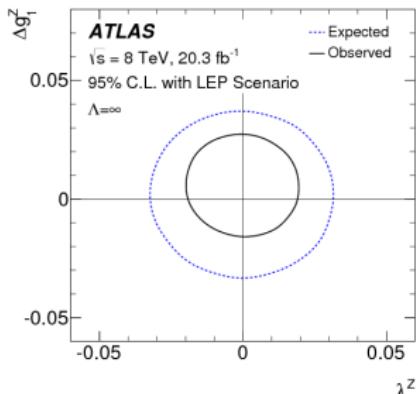
- $\lambda^Z = 0$ and $\lambda^\gamma = 0$ in SM.
- $SU(2)_L$ implies:

$$\delta g_1^\gamma = 0 \quad \lambda^\gamma = \lambda^Z \quad \delta \kappa^\gamma = \frac{\cos^2 \theta_W}{\sin^2 \theta_W} (\delta g_1^Z - \delta \kappa^Z)$$

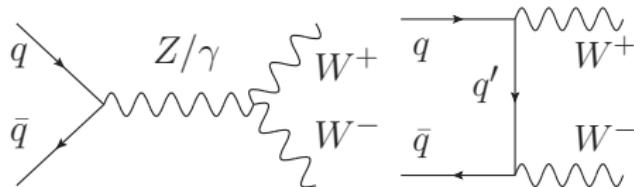
- Three independent parameters: $\lambda^Z, \delta g_1^Z, \delta \kappa^Z$

Experimental results

- ATGCs actively being searched for in W^+W^- production by both ATLAS [JHEP 1609 \(2016\) 029](#) and CMS [Phys.Lett. B772 \(2017\) 21](#)



Missing Terms



- Have not included anomalous quark gauge boson couplings.
 - Highly constrained by LEP.
 - But SM contains cancellations to unitarize amplitudes: growth with energy cancels.
 - Anomalous quark couplings can spoil cancellation and have growth with energy.
 - This was recently pointed out [Zhang PRL118 \(2017\) 011803](#)

Missing Terms

- Anomalous quark-gauge boson couplings occur from the operators

$$O_{HQ,ij}^{(3)} = i \left(\Phi^\dagger \sigma^a D_\mu \Phi - (D_\mu \Phi)^\dagger \sigma^a \Phi \right) \bar{Q}_{Li} \gamma^\mu \sigma^a Q_{Lj}$$

$$O_{HQ,ij}^{(1)} = i \left(\Phi^\dagger D_\mu \Phi - (D_\mu \Phi)^\dagger \Phi \right) \bar{Q}_{Li} \gamma^\mu Q_{Lj}$$

$$O_{Hq,ij} = i \left(\Phi^\dagger D_\mu \Phi - (D_\mu \Phi)^\dagger \Phi \right) \bar{q}_{Ri} \gamma^\mu q_{Rj}$$

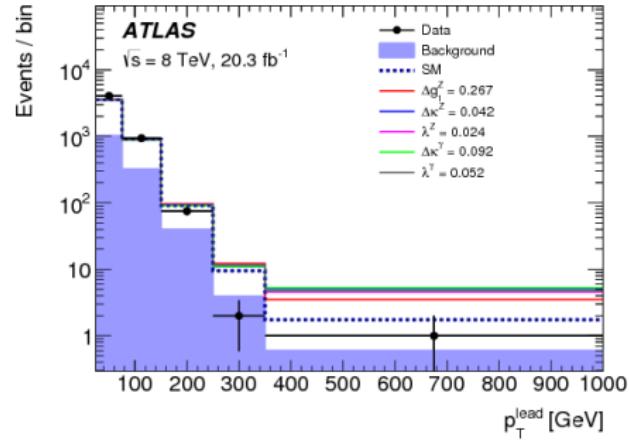
- Parameterize via anomalous couplings:

$$\begin{aligned} \mathcal{L} = & g_Z Z_\mu \bar{q} \gamma^\mu \left\{ \left[T_3 - \sin_W^2 Q_q + \delta g_L^{Zq} \right] P_L + \left[-\sin_W^2 Q_q + \delta g_R^{Zq} \right] P_R \right\} q \\ & + \frac{g}{\sqrt{2}} \left\{ W_\mu^+ (1 + \delta g_L^W) \bar{u} \gamma^\mu P_L d + \text{hc.} \right\} \end{aligned}$$

- $SU(2)$ invariance implies $\delta g_L^W = \delta g_L^{Zu} - \delta g_L^{Zd}$.

Refit Experimental results

- ATGCs limits from ATLAS JHEP 1609.
- In practice want to take differential distributions from experimental collaborations, extract constraints on anomalous couplings.
- We do not decay the W^+ .



Refit Experimental Results

- Assume strongest constraint comes from last bin.
- Scan over allowed ATGCs and determine allowed

$$\sigma(p_T^{W^+} > 500 \text{ GeV}) = \int_{500 \text{ GeV}}^{\infty} dp_T^{W^+} \frac{d\sigma}{dp_T^{W^+}}$$

- Now scan over all parameters and determine allowed regions taking into consideration LEP constraints on anomalous quark couplings [Falkowski, Riva JHEP 1502](#):

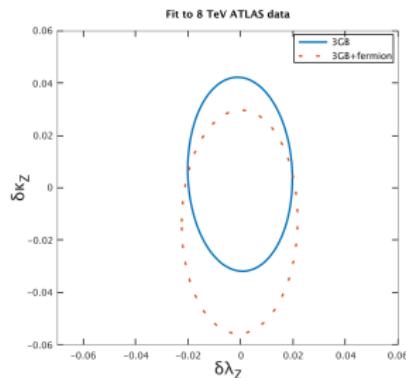
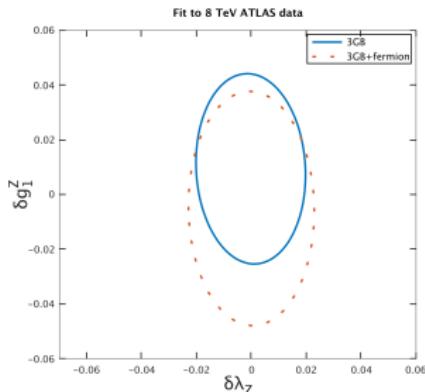
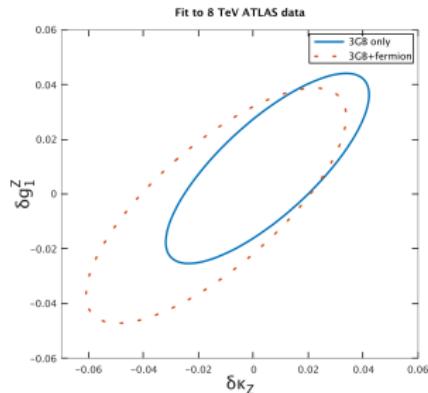
$$\begin{aligned}\delta g_L^{Zd} &= (2.3 \pm 1) \times 10^{-3} \\ \delta g_L^{Zu} &= (-2.6 \pm 1.6) \times 10^{-3} \\ \delta g_R^{Zd} &= (16.0 \pm 5.2) \times 10^{-3} \\ \delta g_R^{Zu} &= (-3.6 \pm 3.5) \times 10^{-3}\end{aligned}$$

- Accept points that fall within allowed region of $\sigma(p_T^{W^+} > 500 \text{ GeV})$.

Refit

- Blue: Including only ATGCs.
- Red dots: adding in anomalous quark couplings
- Inner regions allowed

Baglio, Dawson, IL PRD96 (2017) 073003



Comment on Calculating Cross Sections

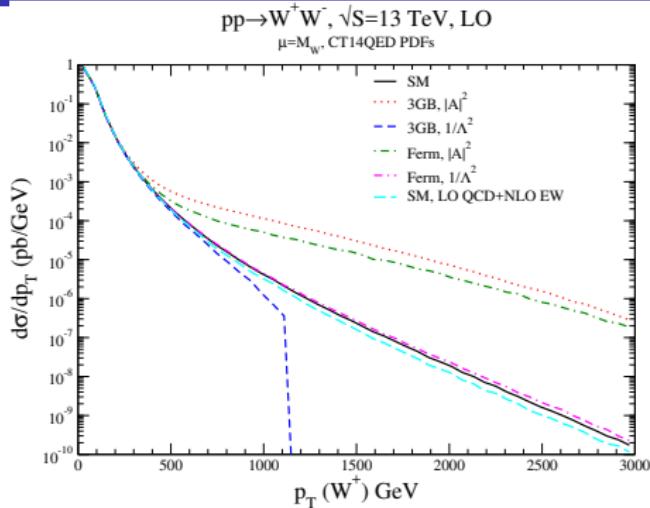
- Previous bounds found using full amplitude squared.
- Includes terms that go as Λ^{-4} :

$$|\mathcal{A}|^2 \sim |g_{SM} + \frac{c_{dim-6}}{\Lambda^2}|^2 \sim g_{SM}^2 + g_{SM} \times \frac{c_{dim-6}}{\Lambda^2} + \frac{c_{dim-6}^2}{\Lambda^4}$$

- Same order as dimension-8 contributions:

$$\begin{aligned} |\mathcal{A}|^2 &\sim |g_{SM} + \frac{c_{dim-6}}{\Lambda^2} + \frac{c_{dim-8}}{\Lambda^4}|^2 \\ &\sim g_{SM}^2 + g_{SM} \times \frac{c_{dim-6}}{\Lambda^2} + \frac{c_{dim-6}^2}{\Lambda^4} + g_{SM} \times \frac{c_{dim-8}}{\Lambda^4} + O(\Lambda^{-6}) \end{aligned}$$

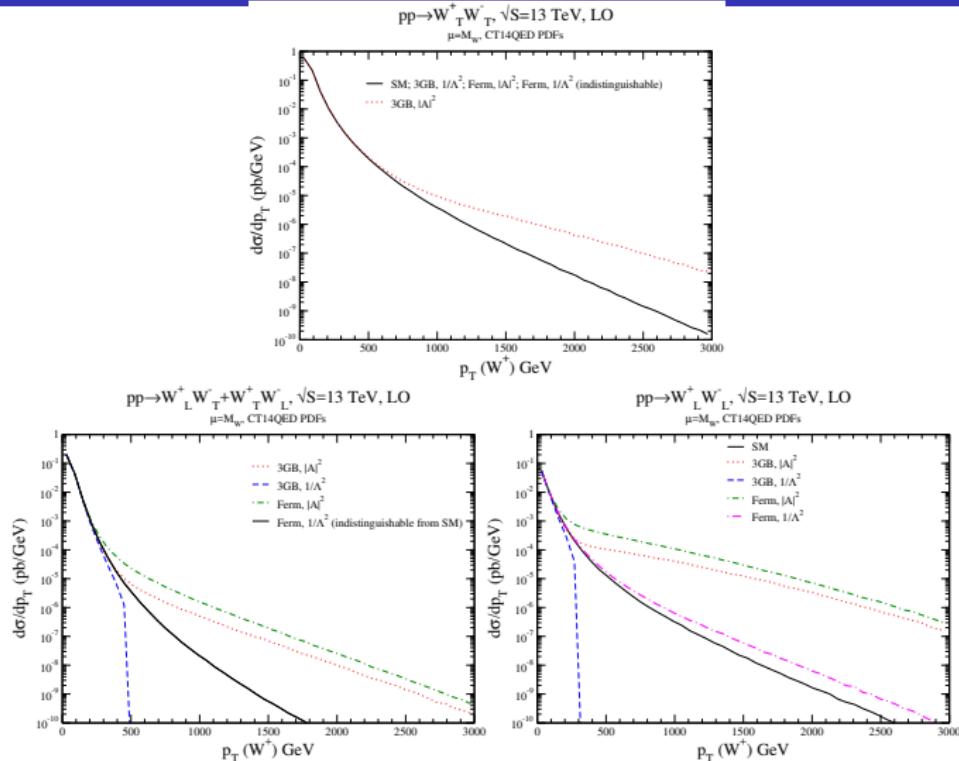
Differential Distributions



Baglio, Dawson, [IL PRD96 \(2017\) 073003](#)

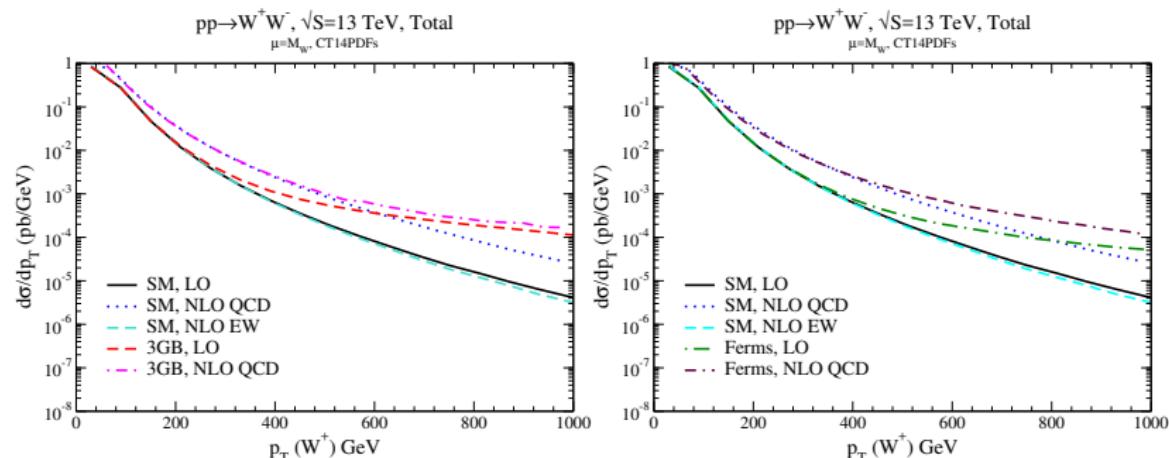
- $1/\Lambda^4$ terms dominate in tails and the bounds on anomalous couplings. [Falkowski, Gonzalez-Alonso, Greijo, Marzocca, Son JHEP 1702 \(2017\) 115](#)
- Ferm: ATGCs set to zero.
- 3GB: Anomalous fermion couplings set to zero.
- Assuming $C_i \lesssim 1$, anomalous couplings correspond to $\Lambda \gtrsim 2.8$ TeV.

Differential Distributions by Helicity



Baglio, Dawson, IL PRD96 (2017) 073003

NLO SM Corrections



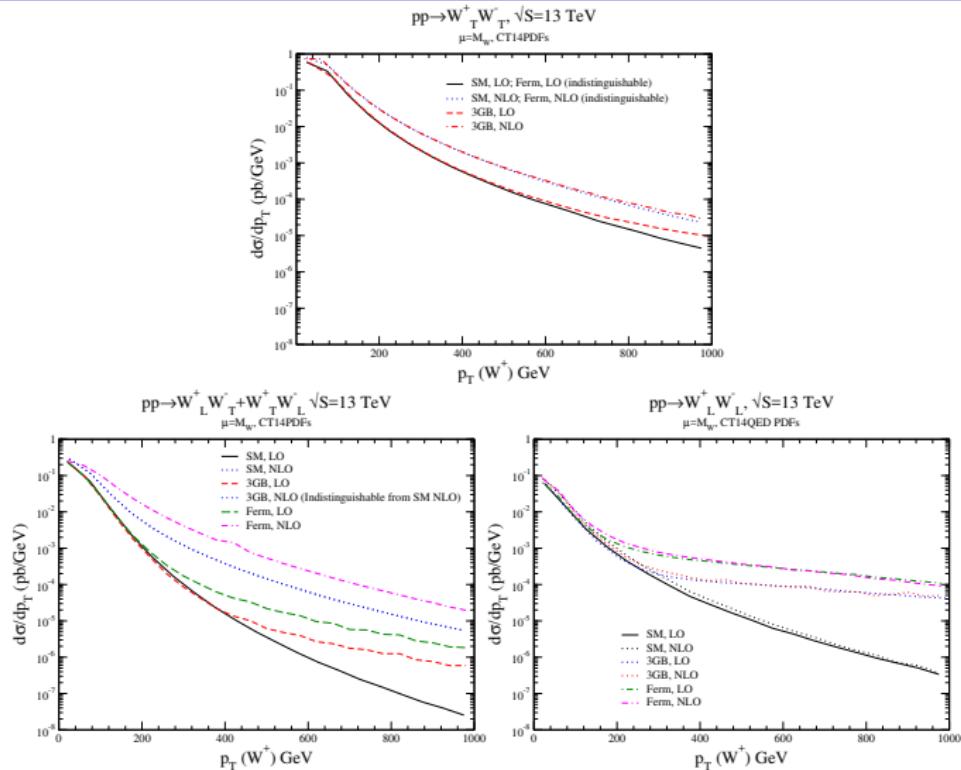
Known up to NNLO in QCD and NLO in EW Frixione NPB410; Ohnemus PRD44; Dixon, Kunszt, Signer NPB531;

Dicus, Kao, Repko PRD36; Glover, van der Bij PLB219; Binotto, Ciccolini, Kauer, Kramer JHEP 0612, JHEP 0503; Baglio, Ninh, Weber PRD94; Bierweiler, Kasprzik, Kuhn, Uccirati JHEP 1211; Bierweiler, Kasprzik, Kuhn JHEP 1312; Billoni, Dittmaier, Jager, Speckner JHEP 1312; Biedermann, Billoni, Denner, Dittmaier, Hofer, Jager, Salfelder JHEP 1606; Gehrmann *et al.* PRL113; Grazzini *et al.* JHEP 1608;

Biedermann *et al.* JHEP 1606

Known up to NLO in QCD for anomalous gauge couplings Dixon, Kunszt, Signer PRD60 (1999) 114037

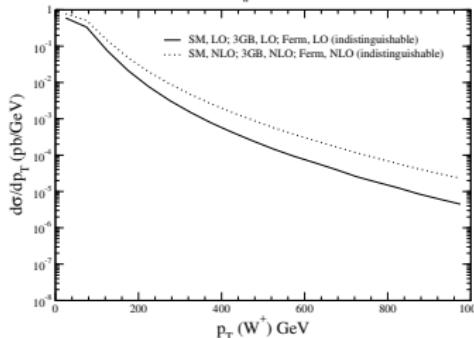
NLO QCD Differential Distributions by Helicity for $|A|^2$



Baglio, Dawson, IL PRD96 (2017) 073003

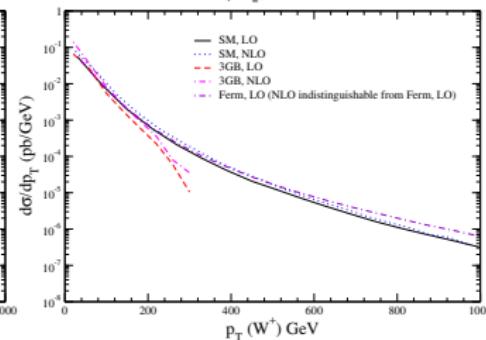
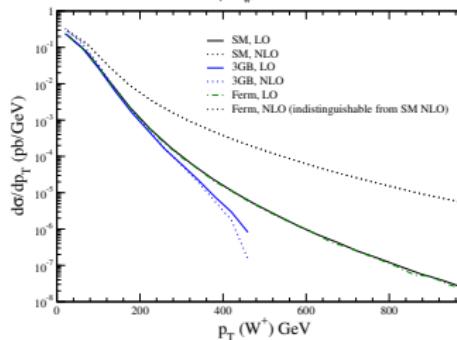
NLO QCD by Helicity for Interference

$pp \rightarrow W_T^+ W_T^-, \sqrt{S}=13 \text{ TeV}, 1/\Lambda^2$
 $\mu=M_W, \text{CT14PDFs}$



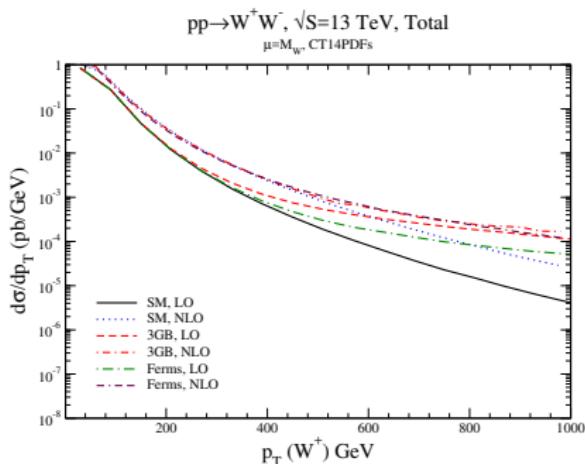
$pp \rightarrow W_L^+ W_T^+ + W_T^+ W_L^-, \sqrt{S}=13 \text{ TeV}, 1/\Lambda^2$
 $\mu=M_W, \text{CT14PDFs}$

$pp \rightarrow W_L^+ W_L^-, \sqrt{S}=13 \text{ TeV}, 1/\Lambda^2$
 $\mu=M_W, \text{CT14PDFs}$

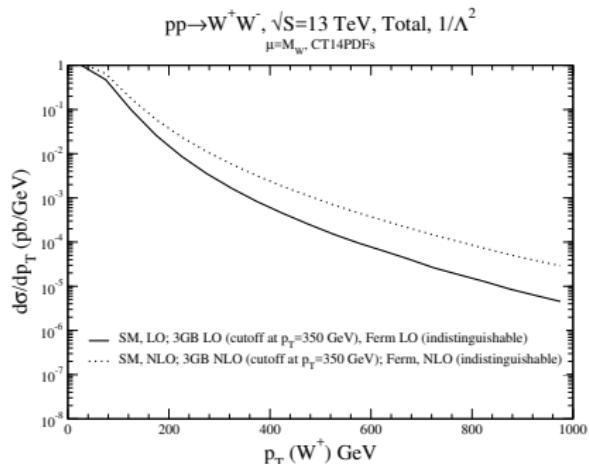


Baglio, Dawson, IL PRD96 (2017) 073003

NLO QCD Corrections



Full Amplitude Squared



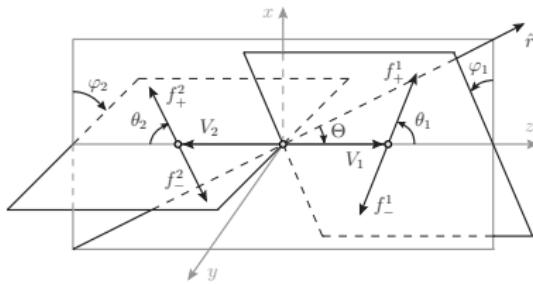
SM+ $1/\Lambda^2$

- “Ferm”: Anomalous trilinear gauge boson couplings set to zero.
- “3GB”: Anomalous quark couplings set to zero.
- $1/\Lambda^4$ contributions from EFT still dominate in tails.

Baglio, Dawson, **IL** PRD96 (2017) 073003

Interference Resurrection

- We have considered on-shell production of W^+W^- , and have not considered their decays.
- In such cases, the interference between the SM and EFT for transversely polarized Ws is negligible at high energy [Azatov, Contino, Machado PRD 95 \(2017\) 065014](#)
- However, when gauge boson decays, sum over polarizations occurs at amplitude level and not amplitudes squared.



- Observables sensitive to interference of different gauge boson polarizations, such as angles between the gauge boson decay planes, can resurrect the interference. [Azatov, Elias-Miro, Reymuaji, Venturini JHEP 1710 \(2017\) 027; Panico, Riva, Wulzer Phys. Lett. B776 \(2018\) 473](#)
- If the gauge bosons are off-shell, interference is also non-negligible. [Helset, Trott arXiv:1711.07954](#)

Higgs Physics

Higgs effective Field Theory

- Higgs precision measurements can constrain effective operators.
- Several operators only rescale SM couplings. For example [Corbett, Eboli, Goncalves, Gonzalez-Fraile, Plehn, Rauch, JHEP 1508 \(2015\) 156](#)

$$(\Phi^\dagger \Phi) \bar{Q}_3 \tilde{\Phi} t_R, \quad \frac{1}{2} \partial^\mu (\Phi^\dagger \Phi) \partial_\mu (\Phi^\dagger \Phi)$$

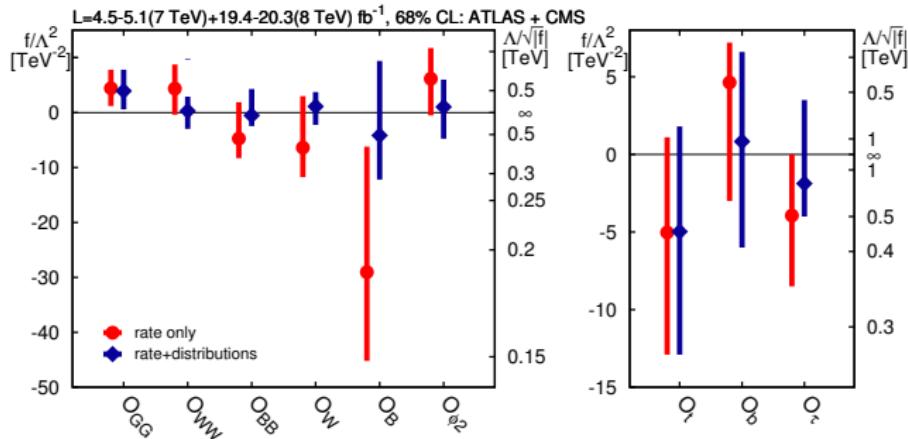
- Operators such as these only rescale SM rates.
- Other operators introduce new Lorentz structures:

$$\Phi^\dagger W_{\mu\nu} W^{\mu\nu} \Phi, \quad \Phi^\dagger B_{\mu\nu} B^{\mu\nu} \Phi, \quad (D_\mu \Phi)^\dagger W^{\mu\nu} (D_\nu \Phi), \quad (D_\mu \Phi)^\dagger B^{\mu\nu} (D_\nu \Phi)$$

- Rate measurements essentially at one scale, measurements of distributions or off-shell Higgs can disentangle new structures from EFT.
- Or, operators can scale differently with energy than the SM contribution:

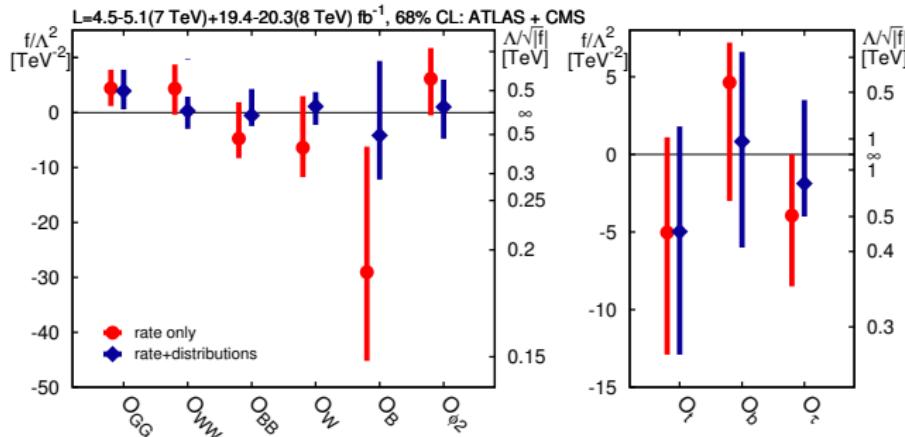
$$\Phi^\dagger \Phi G_{\mu\nu}^a G^{a,\mu\nu}$$

Rate vs. Distribution and Off-Shell

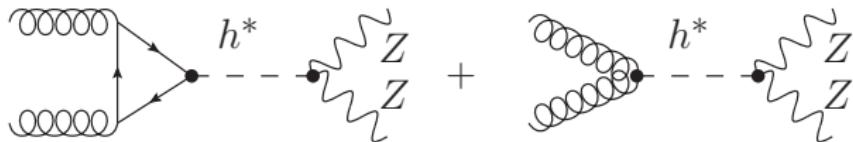


Corbett, Eboli, Goncalves, Gonzalez-Fraile, Plehn, Rauch, JHEP 1508 (2015) 156

Rate vs. Distribution and Off-Shell



Corbett, Eboli, Goncalves, Gonzalez-Fraile, Plehn, Rauch, JHEP 1508 (2015) 156



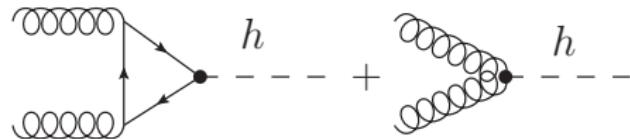
Gainer, Lykken, Matchev, Mrenna, Park PRD91 (2015) 035011; Englert, Soreq, Spannowsky, JHEP 05 (2015) 145; Azatov, Grojean, Paul,

Salvioni J.Exp.Theor.Phys 120 (2015)

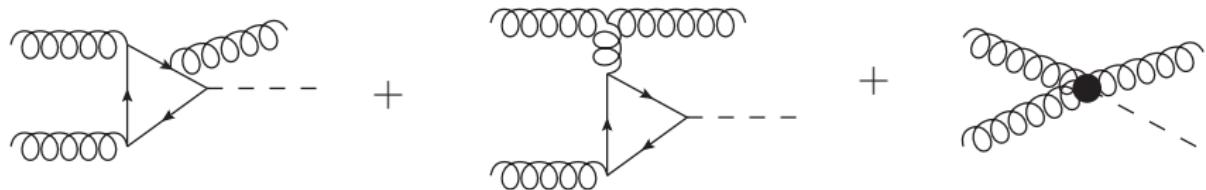
Higgs Plus Jet EFT

$$\mathcal{L} = -\kappa_t \left(\frac{m_t}{v} \right) \bar{t} t h + \kappa_g \left(\frac{\alpha_s}{12\pi v} \right) G^{A,\mu\nu} G_{\mu\nu}^A h$$

- Assume simple deviations from SM predictions.

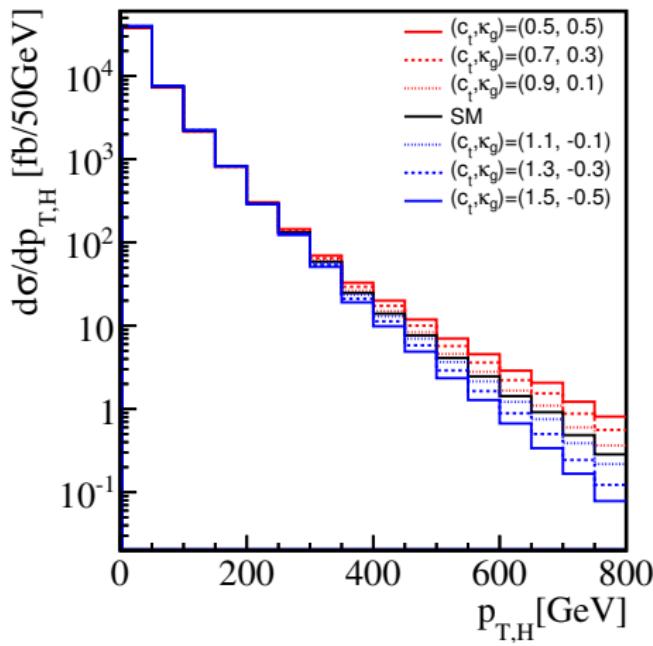


- Simple to keep single Higgs rate SM-like: $\kappa_t + \kappa_g = 1$.



- In Higgs+jet, κ_t and κ_g scale differently with energy.

Higgs Plus Jet EFT



- Impose $\kappa_t + \kappa_g = 1$.
- Can see some deviation in tail.
- Direction of deviation determines direction that relevant couplings change relative to the Standard Model.

Schlaffer, Spannowsky, Takeuchi, Weiler, Wymant, Eur.Phys.J C74

(2014) 10, 3120

Validity of EFT

- Assuming relatively large deviations from SM. How stable is EFT?
- Lowest order operator contribution to Higgs+jet
Schlaffer, Spannowsky, Takeuchi, Weiler, Wyman,
[Eur.Phys.J C74 \(2014\) 10, 3120](#); Azatov, Paul [JHEP 1401 \(2014\) 014](#); Grojean, Salvioni, Schlaffer, Weiler, [JHEP 1405 \(2014\) 022](#);
Langenegger, Spira, Strelbel [arxiv:1507.01373](#); Maltoni, Vryonidou, Zhang [JHEP 1610 \(2016\) 123](#); Grazzini, Ilnicka, Spira,
Wiesemann [JHEP 1703 \(2017\) 115](#):

$$O_1 = h G_{\mu\nu}^a G^{a,\mu\nu}$$

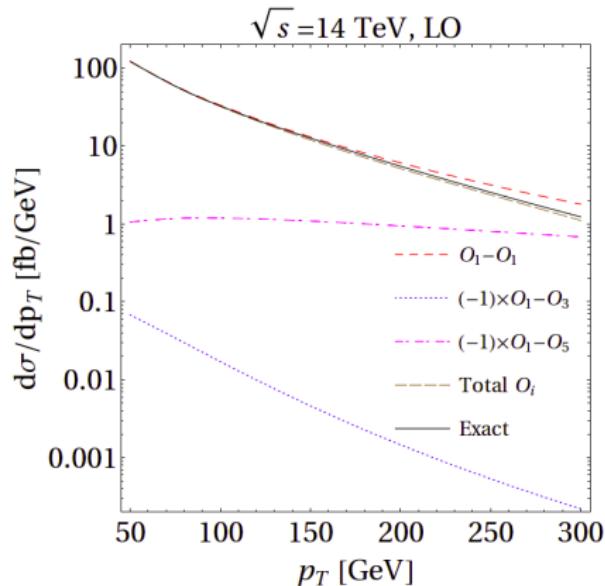
- Can have contributions from higher order operators (for on-shell Higgs): [Neill arXiv:0908.1573](#);
[Harlander, Neumann PRD88 \(2013\) 074015](#); [Dawson, IL Zeng, PRD90 \(2014\) 093007](#); [Dawson, IL, Zeng PRD91 \(2015\) 074012](#):

$$O_3 = h f_{abc} G_v^{a,\mu} G_\sigma^{b,\nu} G_\mu^{c,\sigma}$$

$$O_4 = g_s^2 h \sum_{i,j} \bar{\Psi}_i \gamma_\mu T^a \Psi_i \bar{\Psi}_j \gamma^\mu T^a \Psi_j$$

$$O_5 = g_s h \sum_i G_{\mu\nu}^a D^\mu \bar{\Psi}_i \gamma^\nu T^a \Psi_i$$

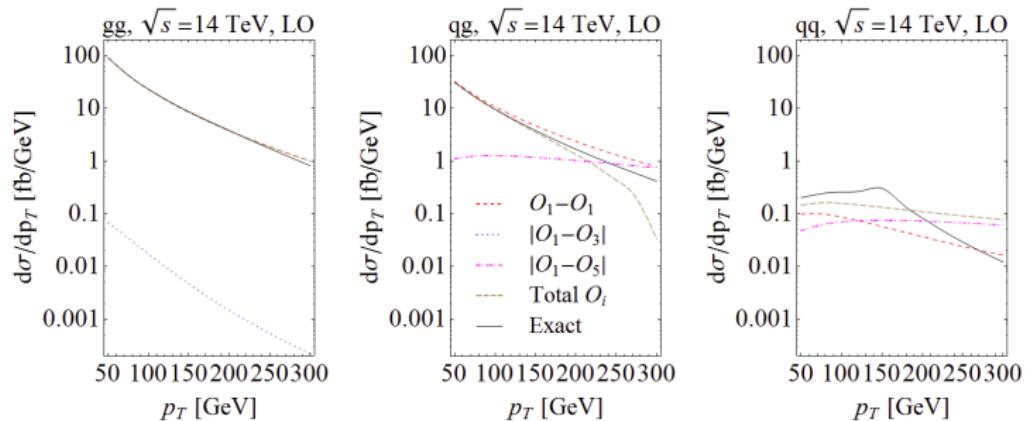
Validity of EFT at LO in QCD



Dawson, IL, Zeng, PRD90 (2014) 093007

- Using SM values of Wilson coefficients.
- $O_5 = g_s h \sum_i G_{\mu\nu}^a D^\mu \bar{\Psi}_i \gamma^5 T^a \Psi_i$, becomes increasingly important at high p_T

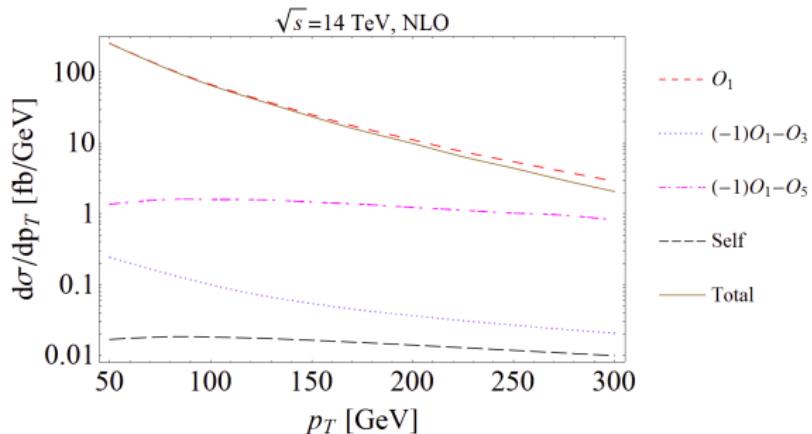
Validity of EFT at LO in QCD



Dawson, IL, Zeng, PRD90 (2014) 093007

- $O_5 = g_s h \sum_i G_{\mu\nu}^a D^\mu \bar{\Psi}_i \gamma^\nu T^a \Psi_i$ important for qg channel.
- qg channel increasingly important at high p_T .
- Large cancellation between O_1 and O_5 in qg channel.

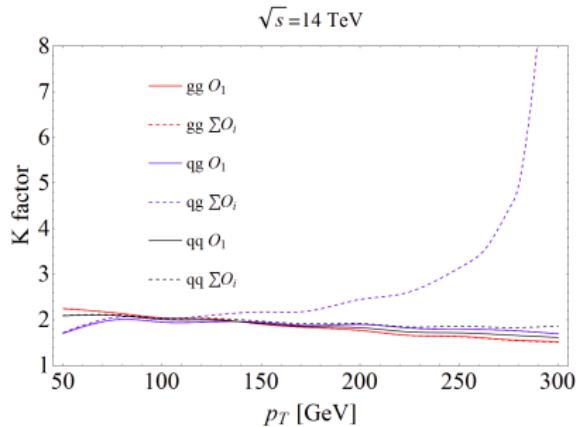
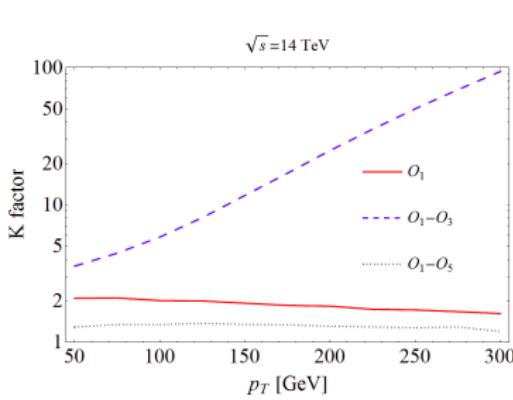
Validity of EFT at NLO in QCD



Dawson, IL, Zeng, PRD90 (2014) 093007

- At NLO $O_3 = h f_{abc} G_v^{a,\mu} G_\sigma^{b,\nu} G_\mu^{c,\sigma}$ no longer plunging at high p_T .

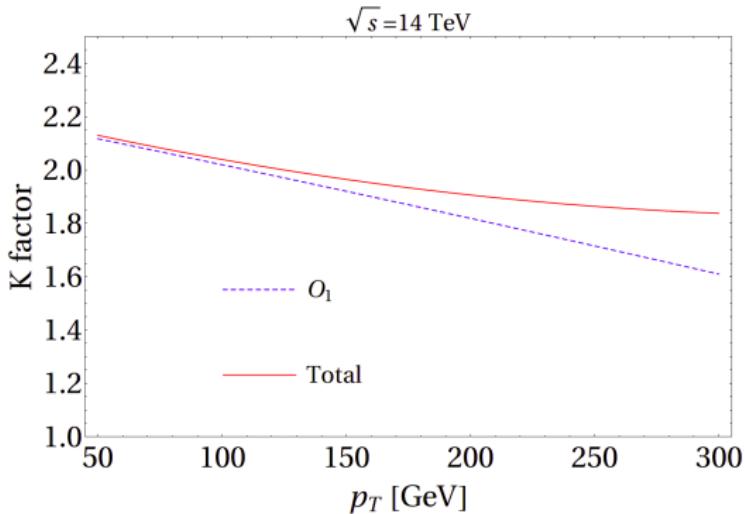
Validity of EFT at NLO in QCD



Dawson, IL, Zeng, PRD90 (2014) 093007

- K-factor for $O_3 = h f_{abc} G_v^{a,\mu} G_\sigma^{b,\nu} G_\mu^{c,\sigma}$ is gigantic.
 - LO contribution exceptionally small.
 - Still small contribution.
- qg K-factor blows up.
 - Cancellation between O_1 and $O_5 = g_s h \sum_i G_{\mu\nu}^a D^\mu \bar{\Psi}_i \gamma^\nu T^a \Psi_i$ at LO.
 - O_1 and O_5 receive different K-factors, spoil cancellation.

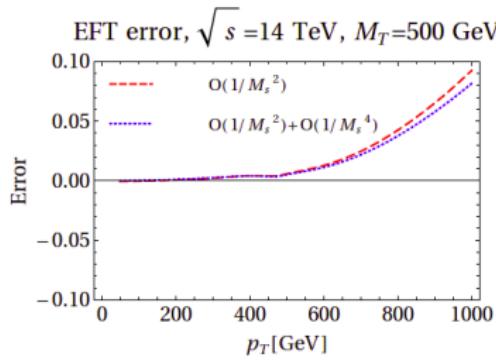
Validity of EFT at NLO in QCD



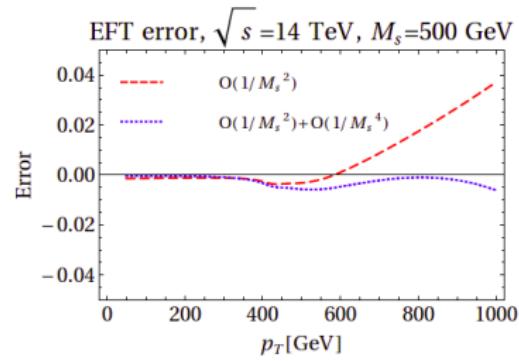
Dawson, IL, Zeng, PRD90 (2014) 093007

- Even with K-factors blowing up by operator or channel, overall behavior is mild.

Validity of EFT for New Physics



Top Partner



Scalar Triplet

Dawson, IL, Zeng, Phys.Rev. D91 (2015) 074012

- Comparing higher order EFT to exact result.
- Lowest order EFT valid within a few percent.
- Convergence depends on UV completion.

Simplified Models and EFTs

Scalar Singlet

- Add a real gauge singlet, scalar singlet S to SM:

$$V(\Phi, S) = V_\Phi(\Phi) + V_{\Phi S}(\Phi, S) + V_S(S)$$

- Higgs potential:

$$V_\Phi(\Phi) = -\mu^2 \Phi^\dagger \Phi + \lambda (\Phi^\dagger \Phi)^2$$

- Scalar singlet potential:

$$V_S(S) = b_1 S + \frac{b_2}{2} S^2 + \frac{b_3}{3} S^3 + \frac{b_4}{4} S^4$$

- Mixing terms:

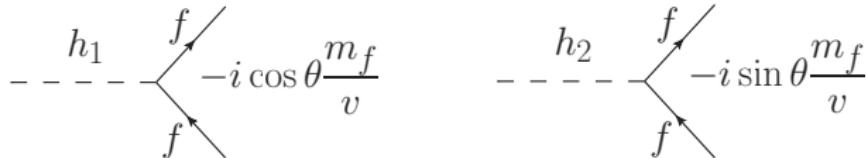
$$V_{\Phi S}(\Phi, S) = \frac{a_1}{2} \Phi^\dagger \Phi S + \frac{a_2}{2} \Phi^\dagger \Phi S^2$$

- After electroweak symmetry breaking, have two mass eigenstates:

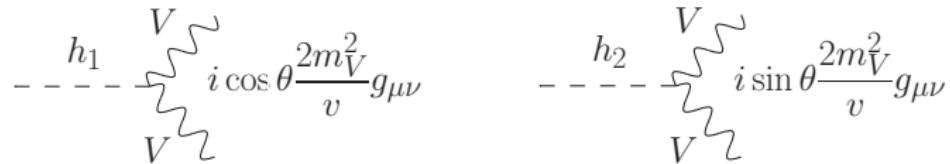
- h_1 with mass $m_1 = 125$ GeV.
- h_2 with mass $m_2 > m_1$.

Relevant Feynman Diagrams

- Couplings to fermions:

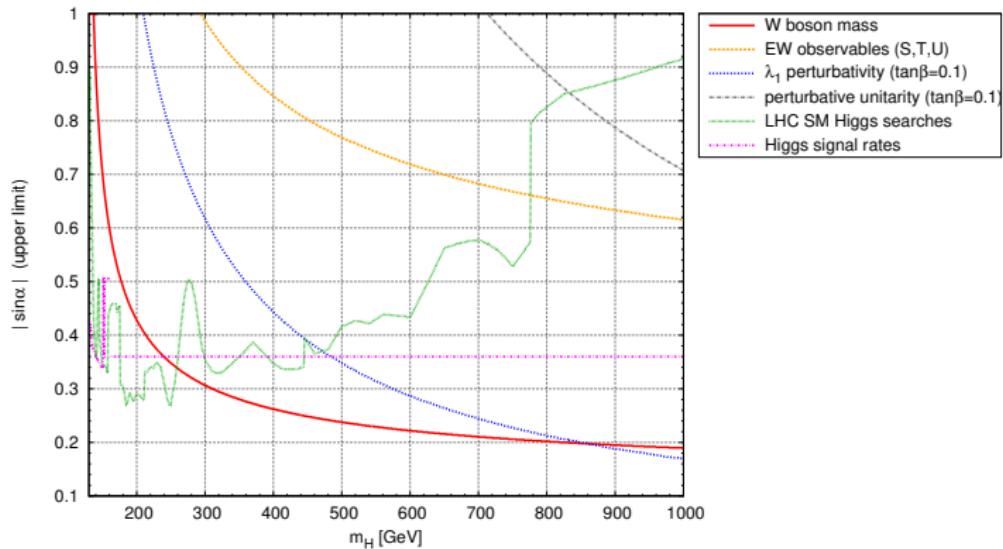


- Couplings to gauge bosons:



- Higgs rates only depend on $\cos^2 \theta$.
 - Branching ratios unchanged.
 - Production rate suppressed by $\cos^2 \theta$.
 - Simple interpretation of Higgs results.
- Since h_2 couplings to fermions and gauge bosons proportional to SM coupling, it is produced through same mechanisms as SM Higgs boson.

Current Limits



Robens, Stefaniak EPJ C76 (2016) 268

- See also Falkowski, Gross, Lebedev JHEP 1505 (2015) 057; Buttazzo, Sala, Tesi JHEP 1511 (2015) 158

Stability of Simplified Models

- In singlet model, Higgs precision measurements simply bound the mixing angle.
- Perturb the model with an EFT:

$$\mathcal{L} = g_s^2 \frac{c_{gg}}{\Lambda} S G^{\mu\nu,a} G_{\mu\nu}^a + \frac{c_{BB}}{\Lambda} g'^2 S B^{\mu\nu} B_{\mu\nu} + \frac{c_{WW}}{\Lambda} g^2 S W^{\mu\nu,a} W_{\mu\nu}^a.$$

- After scalar mixing, these operators introduce new interactions between the gauge bosons and the Higgs.

WW and ZZ Couplings

- New terms in Feynman Rules of observed Higgs boson:

$$\text{--- } h \text{ ---} \begin{array}{c} V \\ \swarrow \quad \searrow \\ - - - \end{array} i \cos \theta \frac{2m_V^2}{v} g_{\mu_1 \mu_2} + 16i \sin \theta \frac{m_V^2}{\Lambda v^2} c_{VV} (p_{1,\mu_2} p_{2,\mu_1} - g_{\mu_1 \mu_2} p_1 \cdot p_2)$$

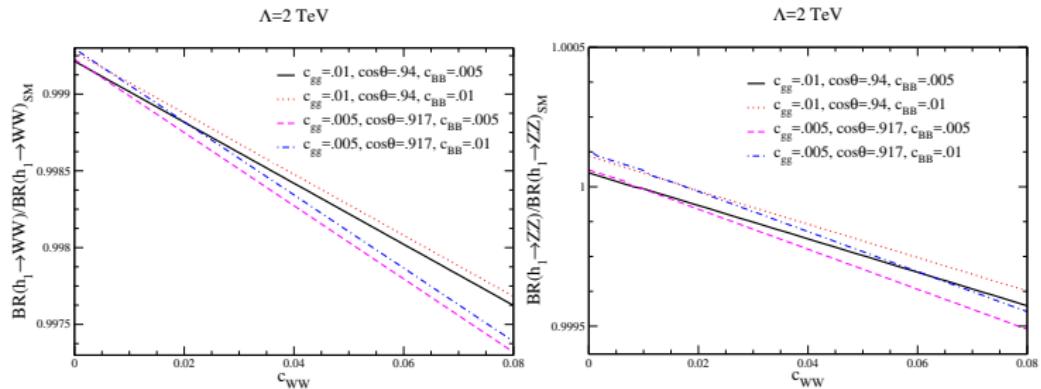
- $c_{ZZ} = c_{WW} \cos^4 \theta_W + c_{BB} \sin^4 \theta_W$
- Since original term is large, expect new EFT terms to make a small difference.

WW and ZZ Couplings

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 \end{array}
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Dawson, IL PRD95 (2017) 015004

$\gamma\gamma$, $Z\gamma$, gg couplings

- Now have “tree-level” couplings to $\gamma\gamma$, $Z\gamma$, and gg :

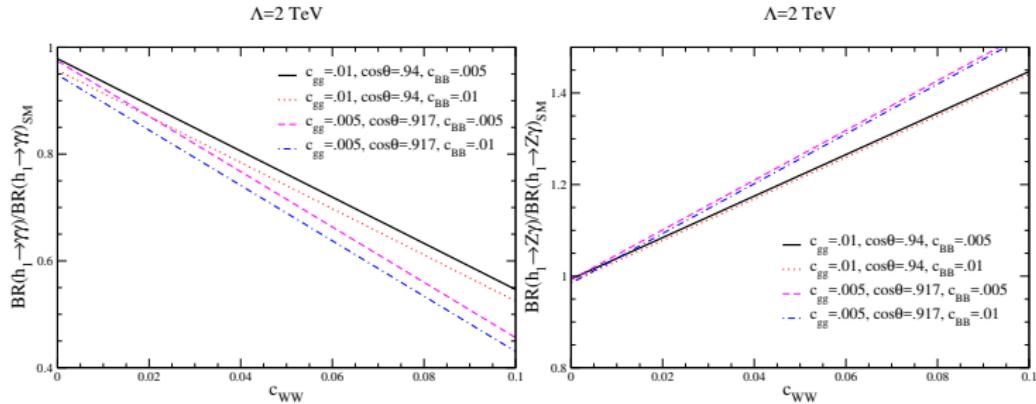
$$\text{--- } h \text{ --- } \begin{array}{c} \gamma \\ \swarrow \quad \searrow \\ \gamma \end{array} 4i \sin \theta e^2 \frac{c_{BB} + c_{WW}}{\Lambda} (p_{1,\mu_2} p_{2,\mu_1} - g_{\mu_1 \mu_2} p_1 \cdot p_2)$$

$$\text{--- } h \text{ --- } \begin{array}{c} g \\ \nearrow \quad \nwarrow \\ g \end{array} 4i \sin \theta g_s^2 \frac{c_{gg}}{\Lambda} (p_{1,\mu_2} p_{2,\mu_1} - g_{\mu_1 \mu_2} p_1 \cdot p_2)$$

$$\text{--- } h \text{ --- } \begin{array}{c} Z \\ \swarrow \quad \searrow \\ \gamma \end{array} 4i \sin \theta e^2 \frac{c_{WW} \cos^2 \theta_W - c_{BB} \sin^2 \theta_W}{\cos \theta_W \sin \theta_W \Lambda} (p_{1,\mu_2} p_{2,\mu_1} - g_{\mu_1 \mu_2} p_1 \cdot p_2)$$

- These were originally loop induced couplings.

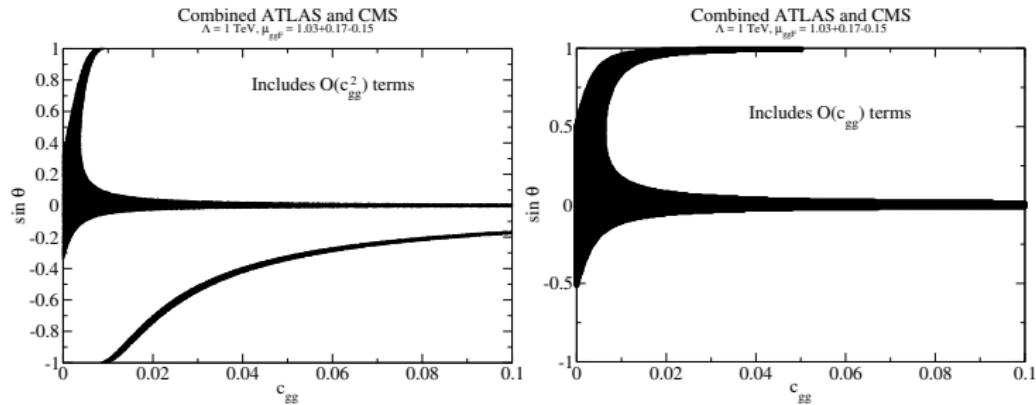
Branching ratios of Observed Higgs



Dawson, IL PRD95 (2017) 015004

- New interactions can significantly effect the $\gamma\gamma$ and $Z\gamma$ decays of the observed Higgs boson.

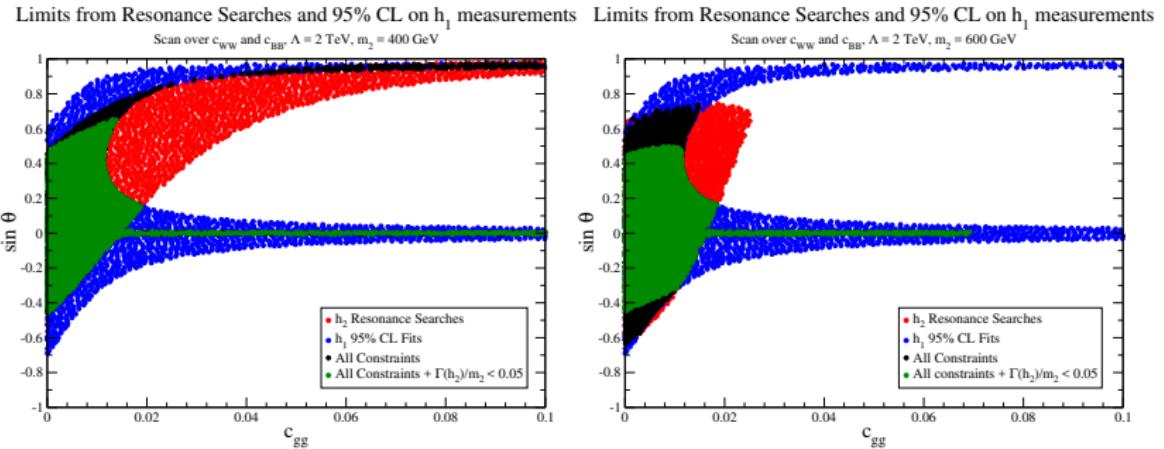
Additional EFT on overall signal strength



Dawson, IL PRD95 (2017) 015004

- Similarly new interaction with gg can significantly effect production rate.
- Fit to the combined gluon fusion signal strength at 7+8 TeV.
 - $\mu_{ggF} = \frac{\sigma_{ggF}}{(\sigma_{ggF})_{SM}}$
- Additional EFT coupling to the gluon field strength greatly changes fit.
 - At $c_{gg} = 0$ get usual limits on $\sin \theta$ from signal strength measurements.
 - Away from $c_{gg} = 0$, can get very different allowed values for $\sin \theta$
 - Also important to carefully count EFT.

All Constraints



Dawson, IL PRD95 (2017) 015004

- Constraints from Higgs measurements, scalar resonance searches, and narrow width requirement.
- Complementary information.

Conclusions

- Investigated the effects of anomalous couplings on W^+W^- production.
 - Although strongly constrained at LEP, anomalous quark-gauge boson couplings significantly change fits to anomalous couplings.
 - LHC is at higher energy, new effects arise and assumptions have to be revisited.
 - Non-interference between SM and EFT is still in effect at NLO.
 - Public code available: WWEFT@NLO

https://quark.phy.bnl.gov/Digital_Data_Archive/dawson/ww_2017/WWEFT_NLO.tar.gz

- Higgs Physics:
 - Distributions and off-shell measurements important for constraining EFT.
 - Higgs+jet:
 - Informative to look beyond the dimension-6 EFT.
 - Interesting interplay between higher order operators and different production channels.
 - Different K-factors for different operators can change the LO QCD story.
 - Convergence of EFT depended on UV completion.

Conclusions

- Simplified models+EFT:
 - We hope that simplified models are a relatively good approximation of physics at LHC.
 - Perturbed the simplest of simplified models by an EFT.
 - The interpretation of Higgs physics changes dramatically in the presence of new operators.

Thank You

EXTRA SLIDES

Matching ATGCs in two prescriptions

- Had 5 dimension-6 operators, only three independent combinations.
- In Warsaw basis:

$$\begin{aligned}\delta g_1^Z &= \frac{v^2}{\Lambda^2} \frac{1}{\cos^2 \theta_W - \sin^2 \theta_W} \left(\frac{\sin \theta_W}{\cos \theta_W} C_{HWB} + \frac{1}{4} C_{HD} + \delta v \right) \\ \delta \kappa^Z &= \frac{v^2}{\Lambda^2} \frac{1}{\cos^2 \theta_W - \sin^2 \theta_W} \left(2 \sin \theta_W \cos \theta_W C_{HWB} + \frac{1}{4} C_{HD} + \delta v \right) \\ \delta \lambda^Z &= \frac{v}{\Lambda^2} 3 M_W C_{3W}\end{aligned}$$

- Anomalous coupling language generic enough that any basis can be matched onto it.

W^+W^- production

- Operators affecting ATGCs:

$$\begin{aligned} O_{3W} &= \epsilon^{abc} W_\mu^{av} W_v^{bp} W_p^{cu} & O_{HD} &= |\Phi^\dagger D_\mu \Phi|^2 & O_{HWB} &= \Phi^\dagger \sigma^a \Phi W_{\mu\nu}^a B^{\mu\nu} \\ O_{H\ell}^{(3)} &= i \left(\Phi^\dagger \overleftrightarrow{D}_\mu \sigma^a \Phi \right) \bar{\ell}_L \gamma^\mu \sigma^a \ell_L & O_{ll} &= (\bar{\ell}_L \gamma^\mu \ell_L)(\bar{\ell}_L \gamma_\mu \ell_L) \end{aligned}$$

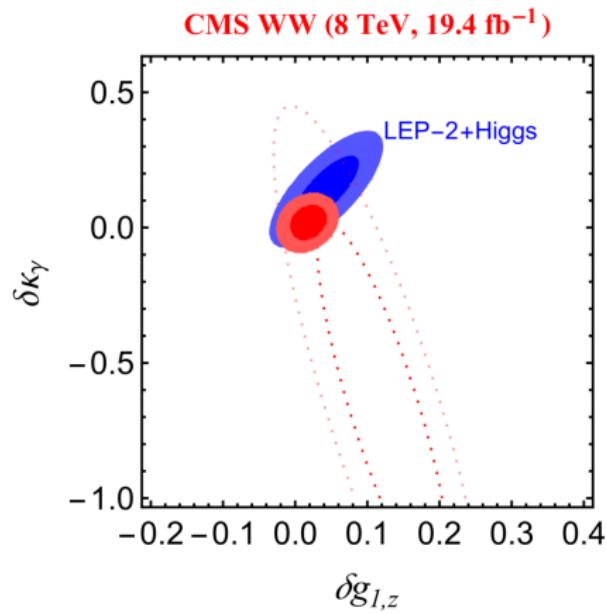
- In the EW sector have to choose input parameters: G_F, M_W, M_Z
- EFT alters relationships between other parameters and input parameters:

$$g_Z \rightarrow g_Z + \delta g_Z \quad v \rightarrow v(1 + \delta v) \quad s_W^2 \rightarrow s_W^2 + \delta s_W^2,$$

where $s_W = \sin \theta_W$, $c_W = \cos \theta_W$ and

$$\begin{aligned} g_Z &= \frac{g}{\cos \theta_W} \quad s_W^2 = 1 - \frac{M_W^2}{M_Z^2} \quad G_F = \frac{1}{\sqrt{2}v^2} \\ \delta v &= C_{H\ell}^{(3)} - \frac{1}{2} C_{\ell\ell} \quad \delta \sin_W^2 = -\frac{v^2}{\Lambda^2} \frac{s_W c_W}{c_W^2 - s_W^2} \left[2s_W c_W \left(\delta v + \frac{1}{4} C_{HD} \right) + C_{HWB} \right] \\ \delta g_Z &= -\frac{v^2}{\Lambda^2} \left(\delta v + \frac{1}{4} C_{HD} \right) \end{aligned}$$

Amplitude Squared vs. Linear Pieces



Falkowski *et al* JHEP 1702

- Red filled: Full Amplitude Squared.
- Red dashed: only linear pieces

“Model Independent” Parameterization

- SM effective field theory (EFT):

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_{n=1}^{\infty} \sum_k \frac{c_{n,k}}{\Lambda^n} O_{n,k}$$

- Typically restrict to flavor universal and baryon number conserving operators:
 - $n = 1$: neutrino mass [Weinberg PRL43 \(1979\)](#)
 - $n = 2$: 59 independent operators [Buchmüller, Wyler, NPB 268 \(1986\)](#); [Grzadkowski, Iskrzynski, Misiak, Rosiek, JHEP1010](#); [Giudice, Grojean, Pomaral, Rattazi JHEP0706](#); [Contino, Ghezzi, Grojean, Muhlleitner, Spira JHEP1307](#)
- There are global analyses of SMEFT [Corbett, Eboli, Goncalves, Gonzalez-Fraile, Plehn, Rauch JHEP 1508; Butler, Eboli, Gonzalez-Fraile, Gonzalez-Garcia, Plehn, Rauch JHEP 1607](#); [Berthier, Trott JHEP 1505](#); [Falkowski, Riva JHEP 1502; Brivio, Trott arXiv: 1706.08945 \[hep-ph\]etc.](#)
- Choices have to be made. Examples of sets of operators:
 - SILH: “Strongly interacting light Higgs” [Giudice, Grojean, Pomaral, Rattazzi JHEP 0706 \(2007\) 045](#)
 - HISZ [Hagiwara, Ishihara, Szalapski, Zeppenfeld PRD48 \(1993\) 2182](#)
 - “Warsaw Basis” [Grzadkowski, Iskrzynski, Misiak, Rosiek JHEP 1010 \(2010\) 085](#)
- Choice of operators different among bases, but complete bases are equivalent.

Refit Experimental Results

- Define χ^2 :

$$\Delta\chi^2 = \mathbf{y}^T \mathbf{C}^{-1} \mathbf{y}$$

where

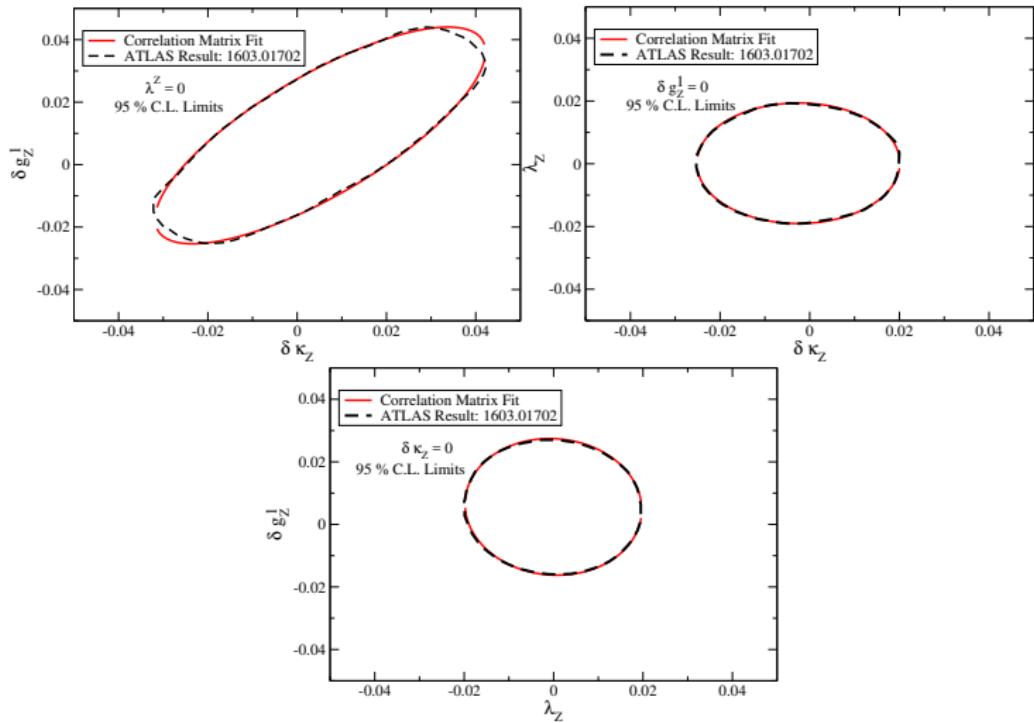
$$\mathbf{y}^T = (\delta g_1^Z - \mu_{g_1^Z}, \delta \kappa^Z - \mu_{\kappa^Z}, \lambda^Z - \mu_{\lambda^Z})$$

- With 3-parameter fit require that $\Delta\chi^2 < 7.815$.
- Fit to the 2D plots and find means and covariant matrix:

$$\mu_{g_1^Z} = 0.00935, \quad \mu_{\kappa^Z} = 0.00518, \quad \mu_{\lambda^Z} = -0.000185$$

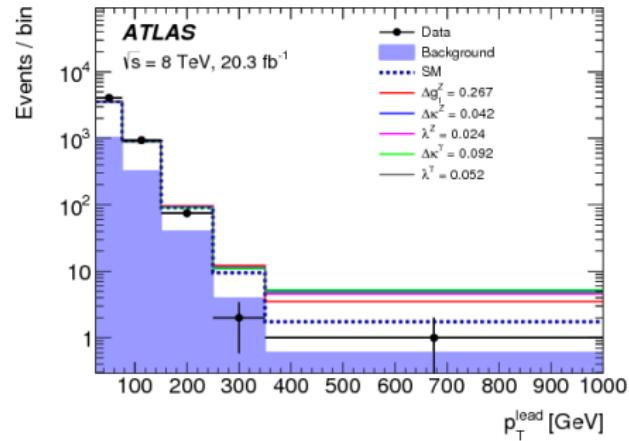
$$\mathbf{C} = \begin{pmatrix} 1.55 & 1.28 & -0.0563 \\ 1.28 & 1.76 & -0.0455 \\ -0.0563 & -0.0455 & 0.511 \end{pmatrix} \times 10^{-4}$$

Refit Experimental Results



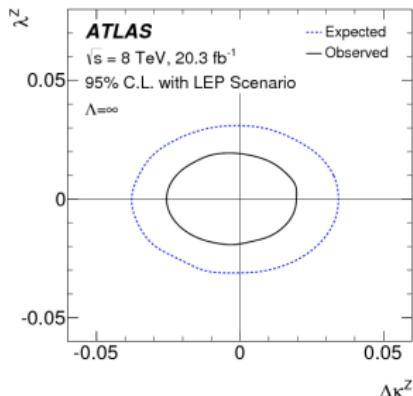
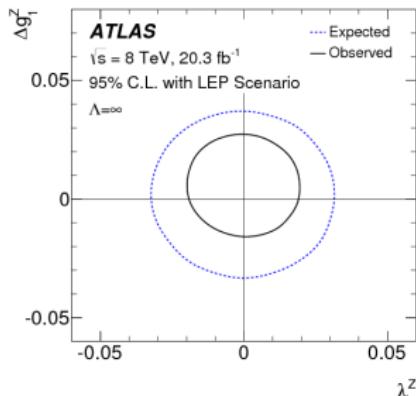
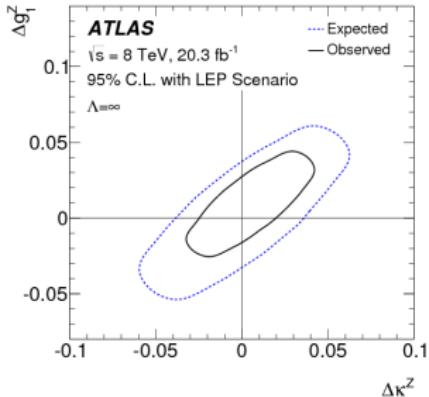
Refit Experimental results

- ATGCs limits from ATLAS JHEP 1609.
- In practice want to take differential distributions from experimental collaborations, extract constraints on anomalous couplings.
- Problem: we do not decay the W^+ .



Refit Experimental results

- Solution: repurpose ATLAS ATGC 95% C.L. [JHEP 1609](#).
- Each 2D plot set 3rd parameter to zero.
- Can fit ellipsoid.

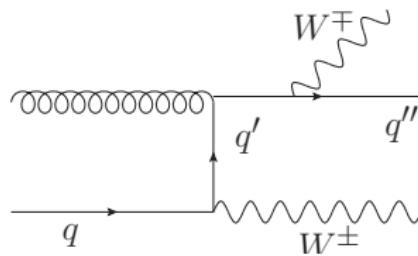


Refit Experimental Results

- Check by comparing to 1D results: set two of the ATGCs to zero:

	95% C.L. limit Using Previous Number	ATLAS 95% C.L. limit JHEP 1609
δg_1^Z	[-0.0162,0.0274]	[-0.016,0.027]
$\delta \kappa^Z$	[-0.0252,0.0201]	[-0.025,0.020]
λ^Z	[-0.0189,0.0192]	[-0.019,-0.019]

Large Sudakov Logarithms



- LO Story:
 - SM calculation is unitary and growth with energy cancels.
 - Anomalous quark couplings spoil cancellation and allow for non-unitary behavior.
 - Even though small, the effects grow with energy.
- NLO story:
 - SM K-factor huge due to large Sudakov logarithms, grows with energy.
 - No cancellations for anomalous quark couplings to spoil.
 - Anomalous quark couplings not as enhanced relative to SM as energy grows.