



# *Winter Meeting Nuclear Physics, Bormio 2018*

## Precision atomic/nuclear physics measurements in Penning traps and tests of fundamental symmetries

- Precision atomic/nuclear masses
- The (anti)proton charge-to-mass ratio
- $g$ -factors of bound electrons and  $m_e$

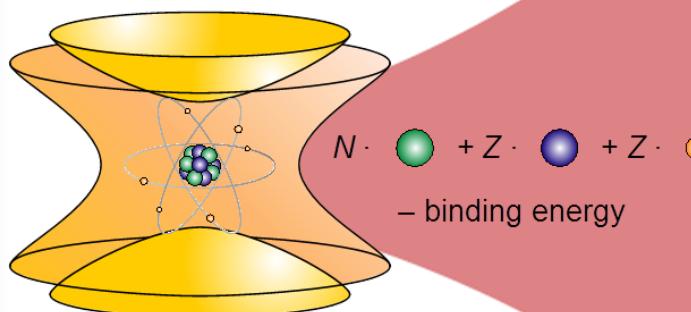


Klaus Blaum  
Jan 22<sup>nd</sup>, 2018





# Why measuring atomic masses?



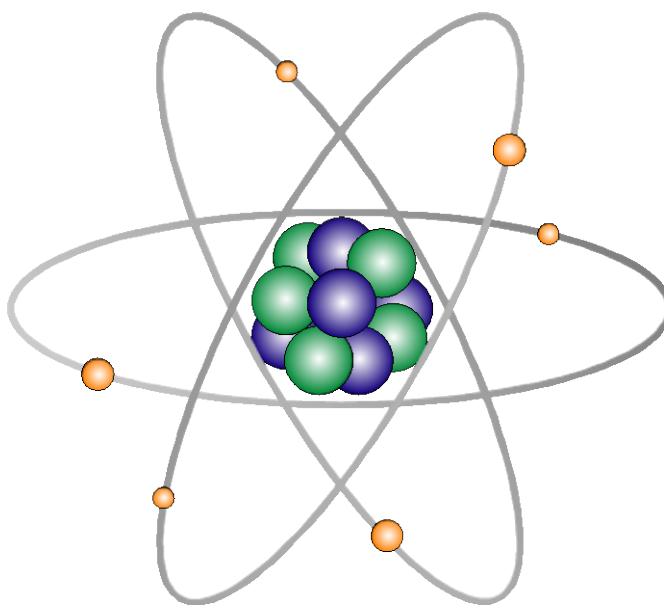
	$\delta m/m$	$\delta E$
General physics & chemistry	$\leq 10^{-5}$	1 MeV
Nuclear structure physics - separation of isobars	$\leq 10^{-6}$	100 keV
Astrophysics - separation of isomers	$\leq 10^{-7}$	10 keV
Weak interaction studies	$\leq 10^{-9}$	100 eV
Metrology - fundamental constants Neutrino physics	$\leq 10^{-10}$	eV- meV
CPT tests	$\leq 10^{-11}$	meV
QED in highly-charged ions - separation of atomic states	$\leq 10^{-11}$	eV- meV

Relative mass precision of  $10^{-9}$  and below can presently ONLY be reached by Penning-trap mass spectrometry.



# Atomic and nuclear masses

Masses determine the atomic and nuclear binding energies reflecting all forces in the atom/nucleus.



$$= N \cdot \text{ } + Z \cdot \text{ } + Z \cdot \text{ } - \text{binding energy}$$

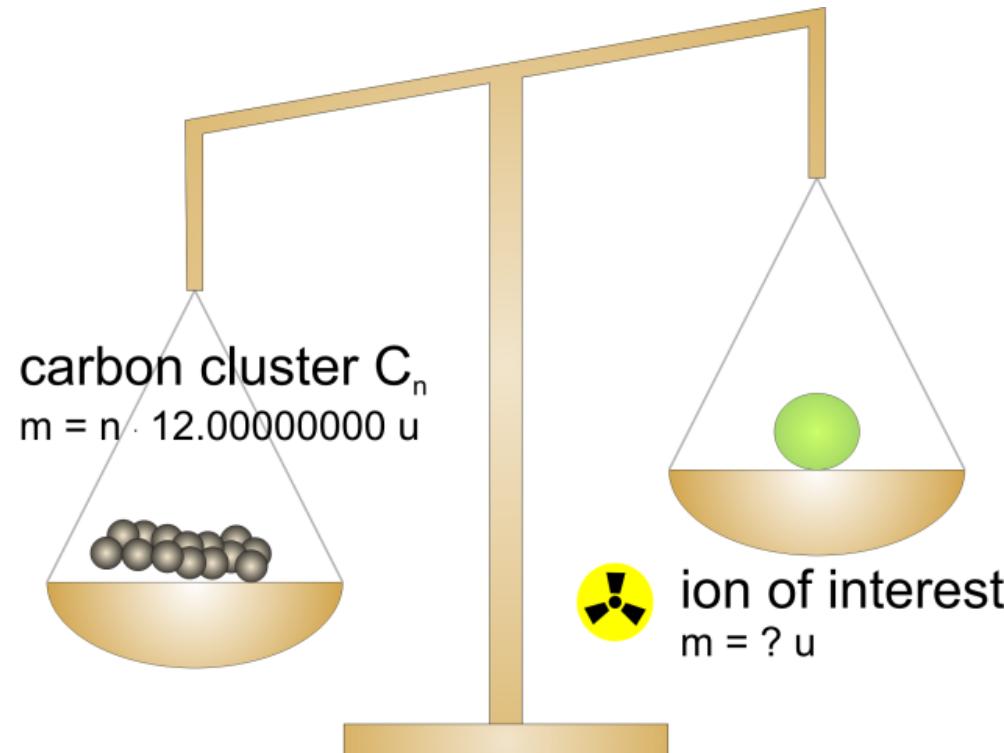
$$m_{\text{Atom}} = N \cdot m_{\text{neutron}} + Z \cdot m_{\text{proton}} + Z \cdot m_{\text{electron}} - (B_{\text{atom}} + B_{\text{nucleus}})/c^2$$

$$\delta m/m < 10^{-10}$$



$$\delta m/m = 10^{-6} - 10^{-8}$$

# How to weigh an atom



$$v_{c,1}$$

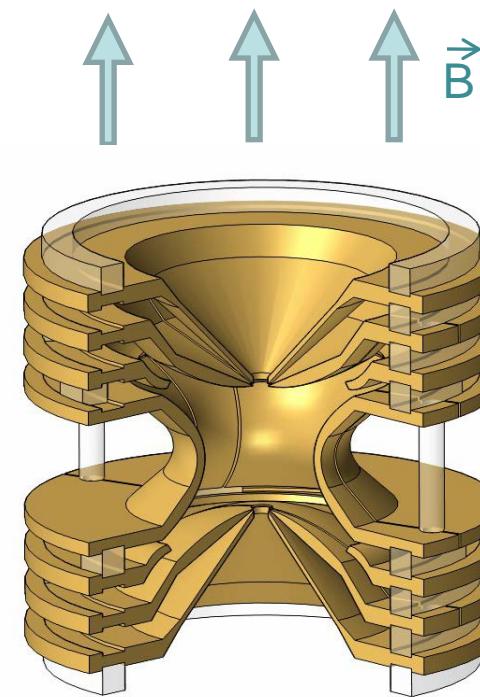
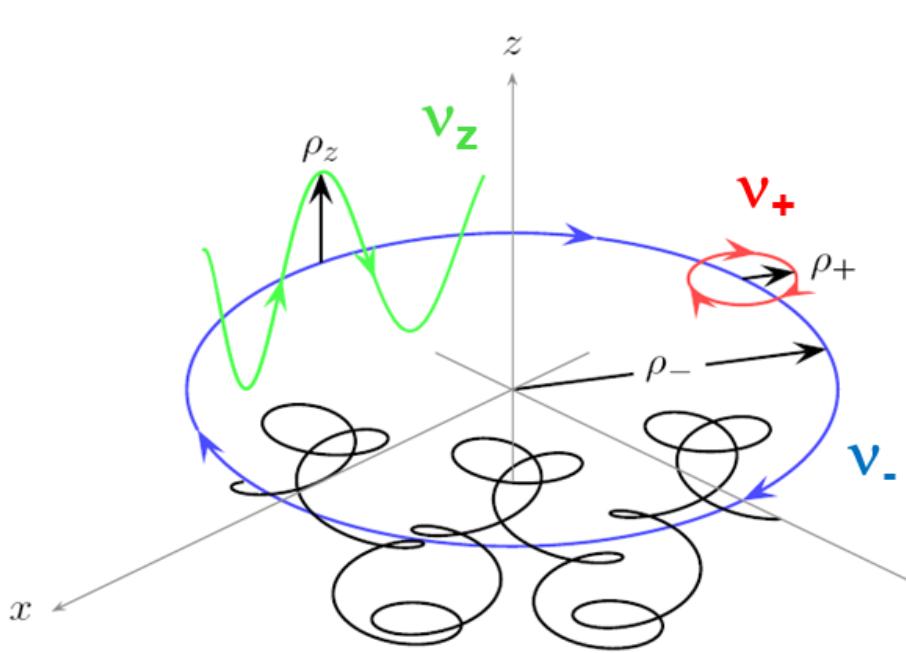
$$v_{c,2}$$



$$\frac{v_{c,1}}{v_{c,2}}$$



# Storage of ions in a Penning trap



The free cyclotron frequency is inverse proportional to the mass of the ion!

$$\omega_c = qB / m_{ion}$$

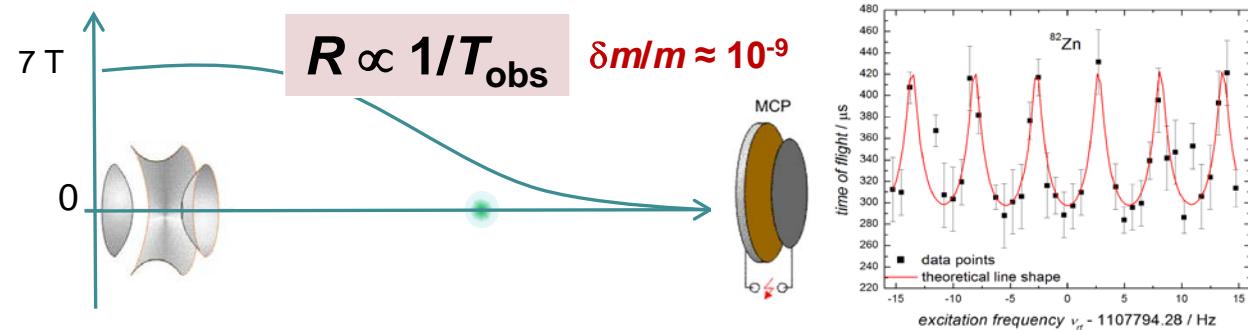
**Invariance theorem:**  $\omega_c^2 = \omega_+^2 + \omega_-^2 + \omega_z^2$

$$\omega_c = \omega_+ + \omega_-$$

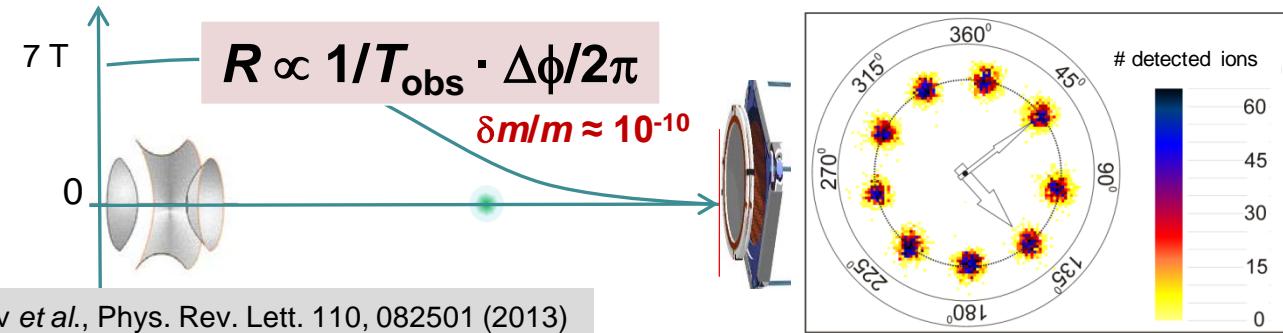
L.S. Brown, G. Gabrielse, Rev. Mod. Phys. 58, 233 (1986).

# Detection techniques

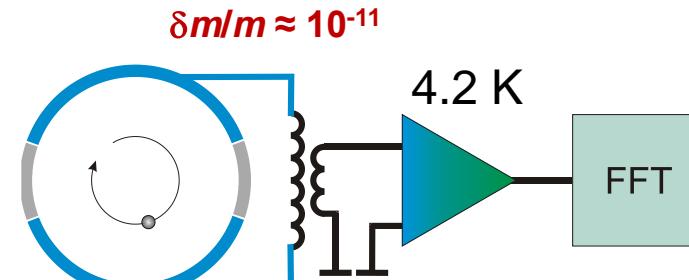
## Destructive time-of-Flight detection



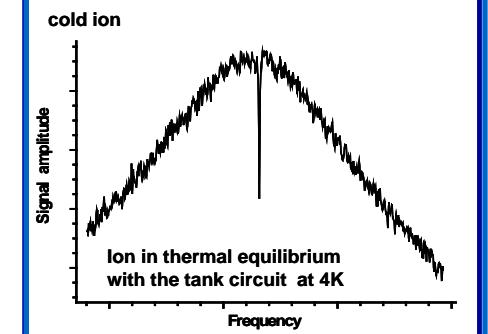
## Destructive phase-imaging detection



## Non-destructive induced image current detection



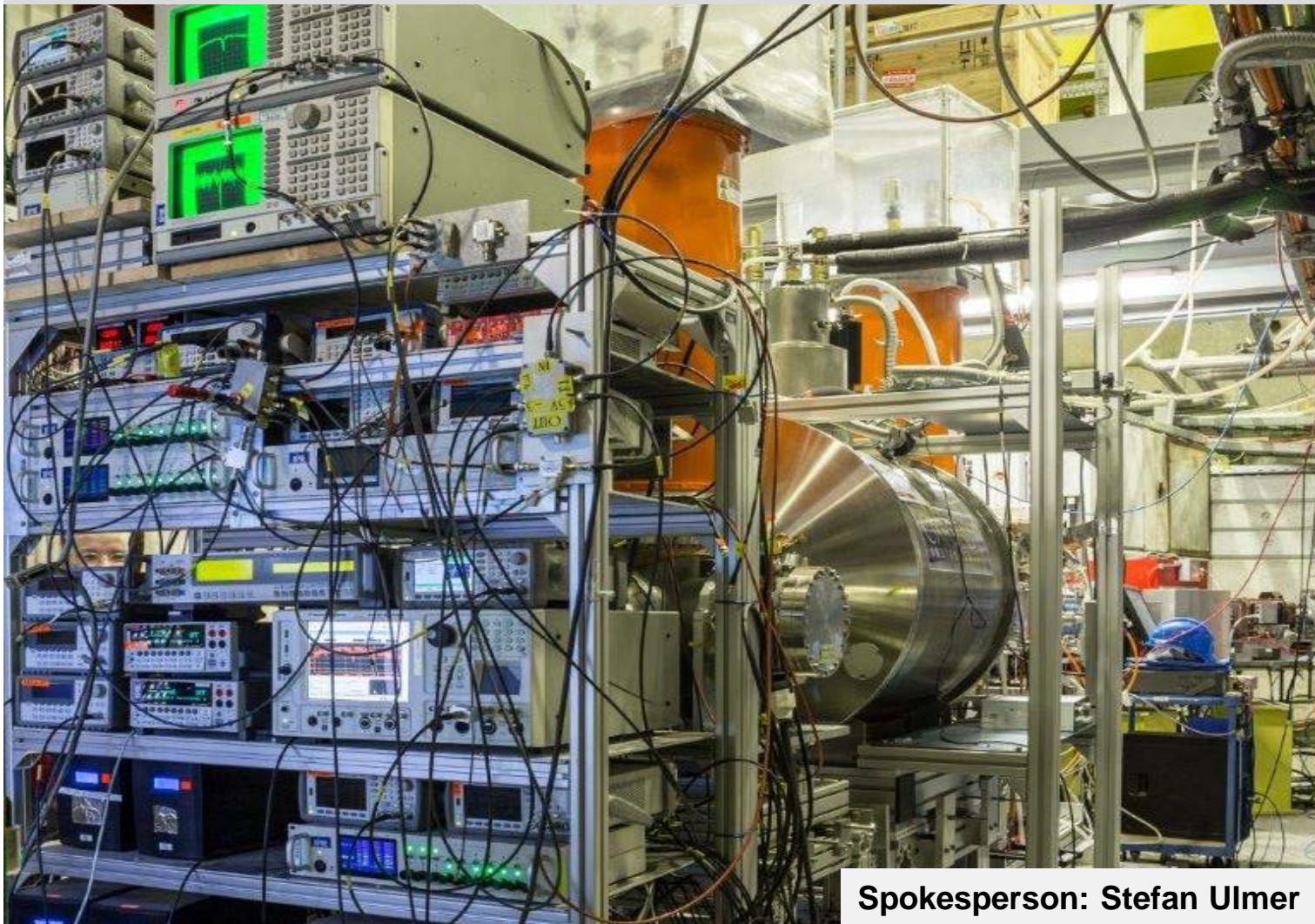
S. Sturm et al., Phys. Rev. Lett. 107, 143003 (2011)





# BASE: A Penning-trap setup at CERN

A balance for protons and antiprotons.

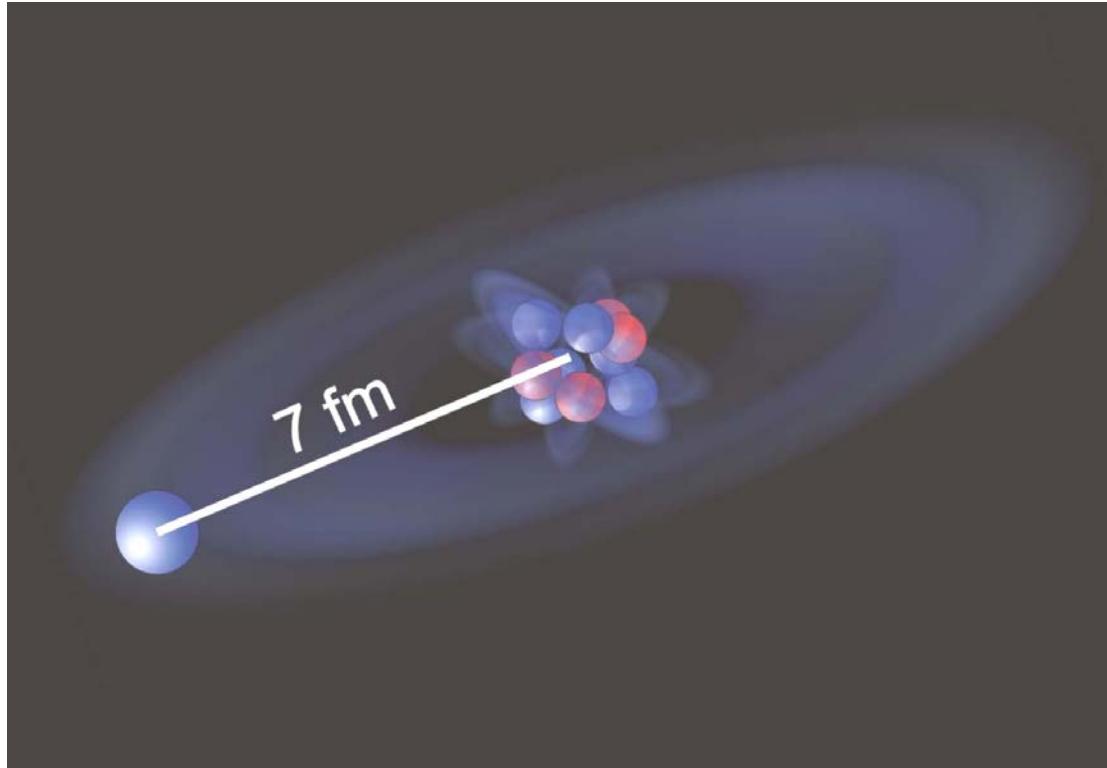


Spokesperson: Stefan Ulmer



# Atomic masses I

## Nuclear magic numbers



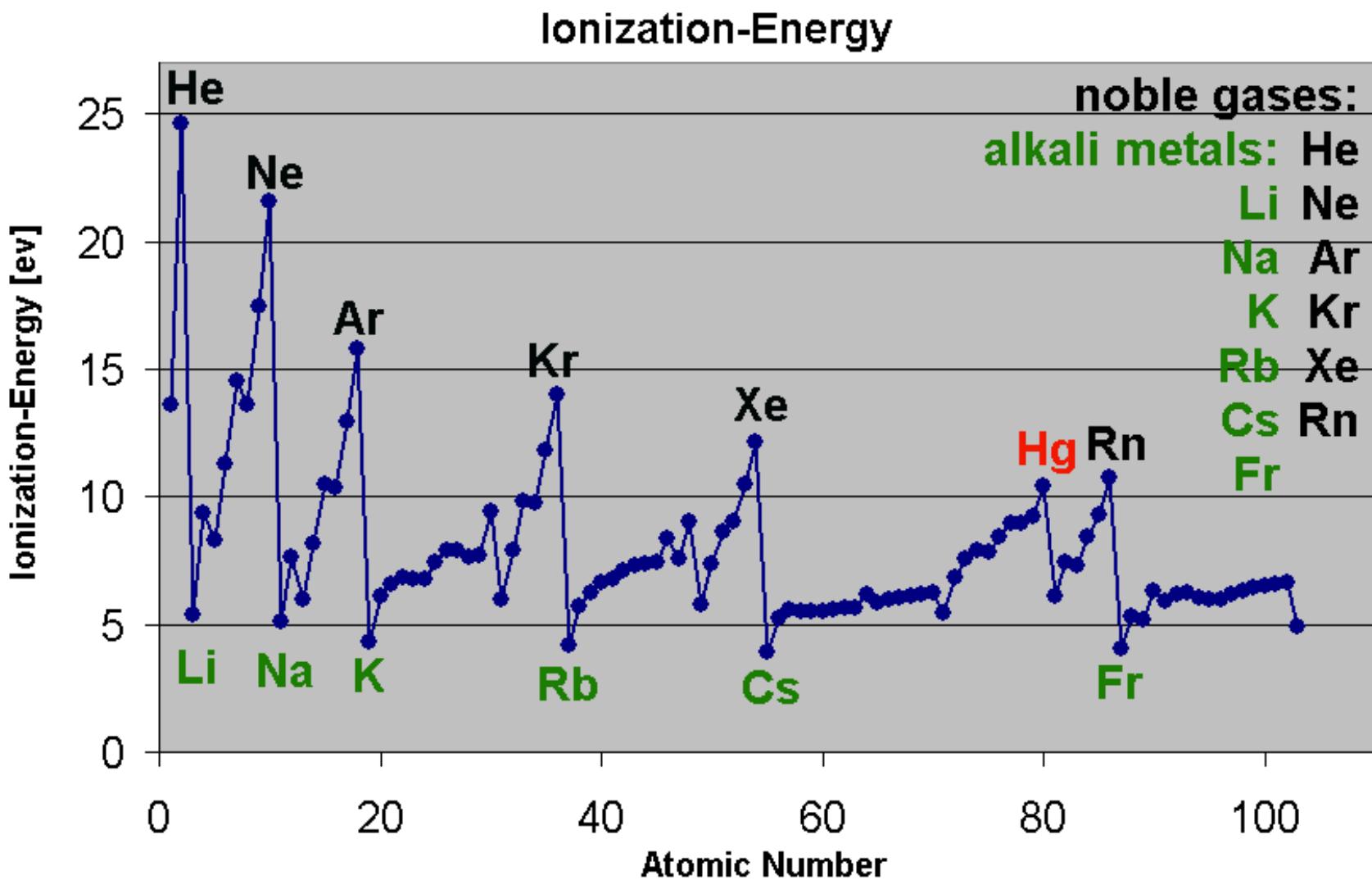
ISOLTRAP (CERN), SHIPTRAP (GSI), TRIGATRAP (Mainz)

M. Block, S. Eliseev, V. Manea, L. Schweikhard, A. Schwenk





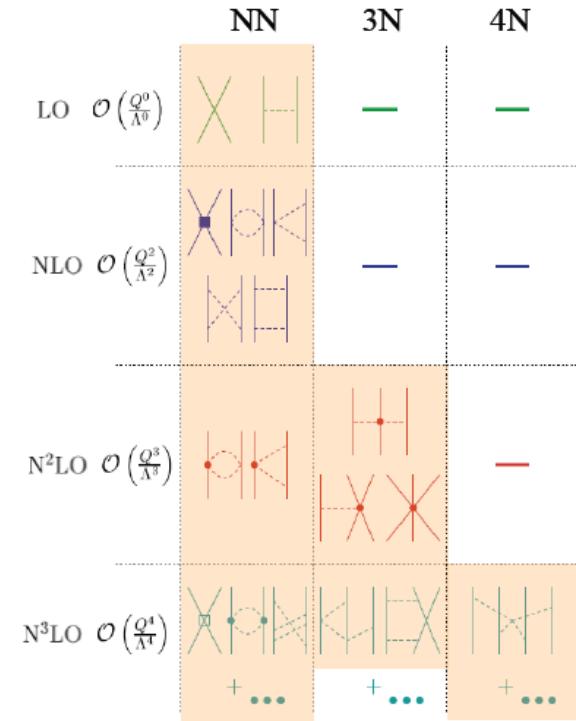
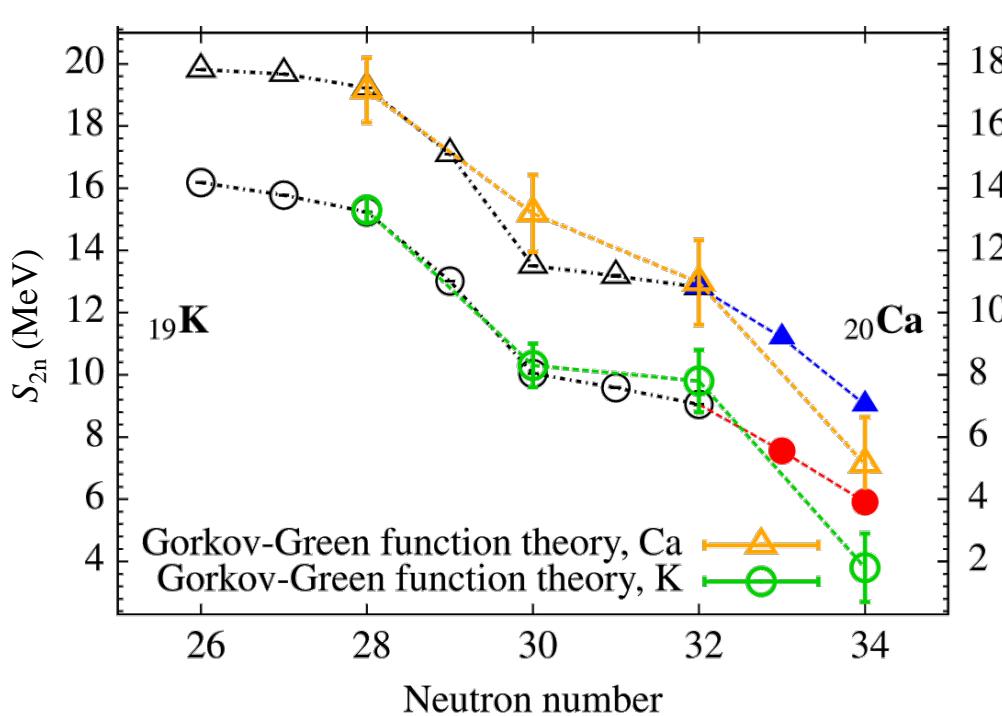
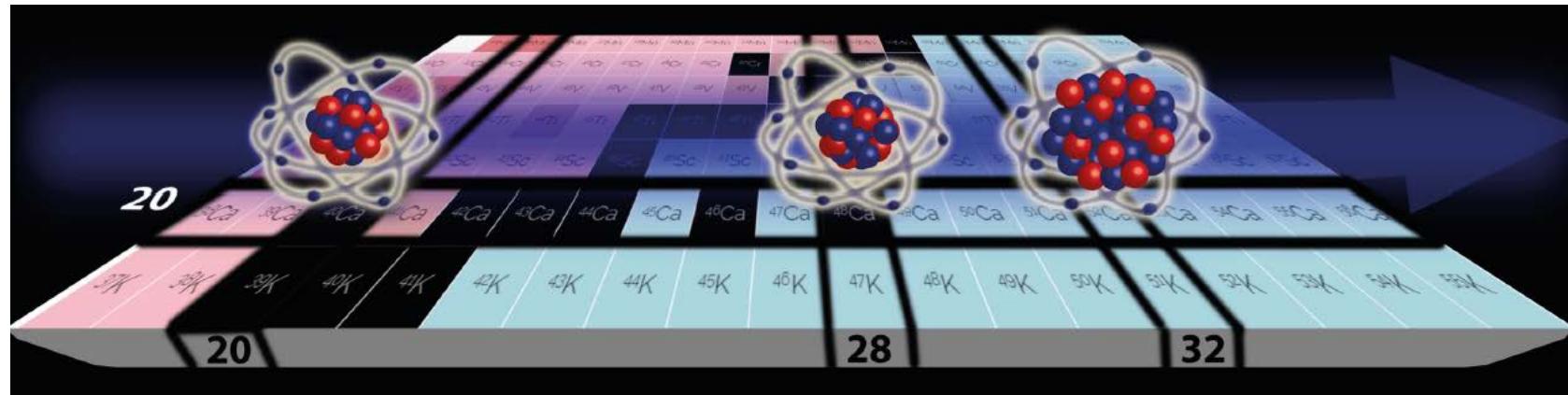
# Atomic and nuclear structure: Basics





# New magic number ( $N=32$ ) and 3N-forces

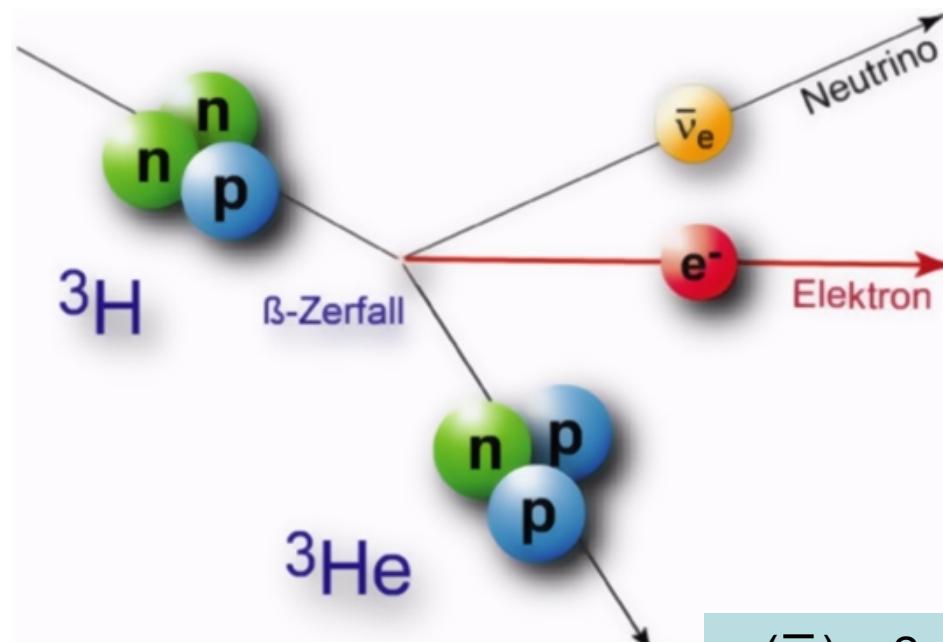
MAX PLANCK INSTITUTE  
FOR NUCLEAR PHYSICS





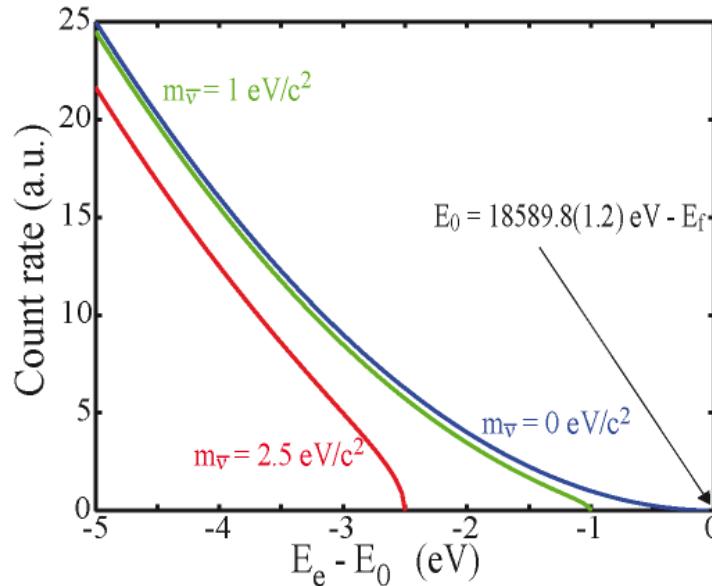
# Masses II

## Neutrino physics applications



# THe-TRAP for KATRIN

## A high-precision $Q(^3\text{T}-^3\text{He})$ -value measurement



$Q_{lit} = 18\ 592.01(7)\ \text{eV}$  [E. Myers, PRL (2015)]

We aim for:  $\delta Q(^3\text{T} \rightarrow ^3\text{He}) = 20\ \text{meV}$   
 $\delta m/m = 7 \cdot 10^{-12}$



$\Delta T < 0.02\ \text{K/d}$  at  $24^\circ\text{C}$   
 $\Delta B/B < 10\ \text{ppt/h}$        $\Delta x \leq 0.1\ \mu\text{m}$

First  $^{12}\text{C}^{4+}/^{16}\text{O}^{6+}$  mass ratio measurement at  $\delta m/m = 1.4 \cdot 10^{-11}$  performed.



# Atomic masses III

## Test of CPT symmetry



BASE: CERN, GSI, Hannover, Mainz, MPIK, RIKEN

A. Mooser, Ch. Ospelkaus, W. Quint, S. Smorra, S. Ulmer, J. Walz



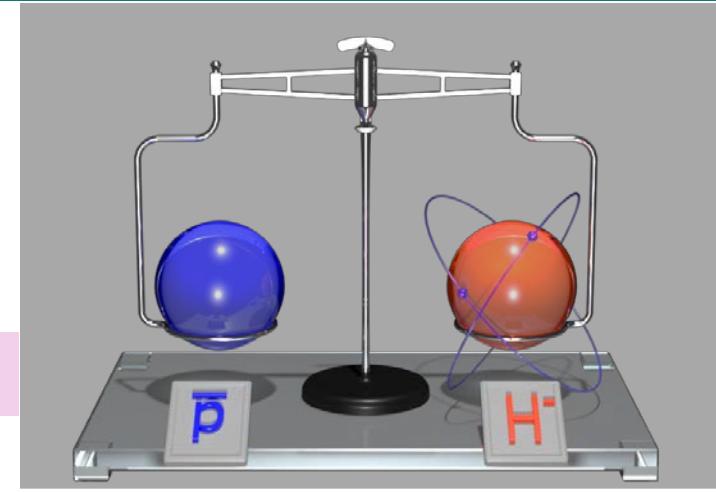


# Most stringent baryonic CPT test

Compare charge-to-mass ratios  $R$   
of  $p$  and  $\bar{p}$ :

$$(q/m)_{\bar{p}} / (q/m)_p = 1.000\ 000\ 000\ 001 \text{ (69)}$$

S. Ulmer *et al.*, Nature 524, 196 (2015)



It is not that easy!

$$m_{H^-} = m_p \left( 1 + 2 \frac{m_e}{m_p} + \frac{\alpha_{\text{pol}, H^-} B_0^2}{m_p} - \frac{E_b}{m_p} - \frac{E_a}{m_p} \right)$$



# A 3-fold improved proton mass



$$m_p = \frac{1}{6} \frac{\nu_c(^{12}\text{C}^{6+})}{\nu_c(p)} m(^{12}\text{C}^{6+})$$

$$m_p = 1.007\ 276\ 466\ 583\ (15)(29)\ u$$

$$\frac{\delta m_p}{m_p} = 3.2 \cdot 10^{-11}$$



# Atomic masses IV

The mass of the electron –  
A fundamental constant



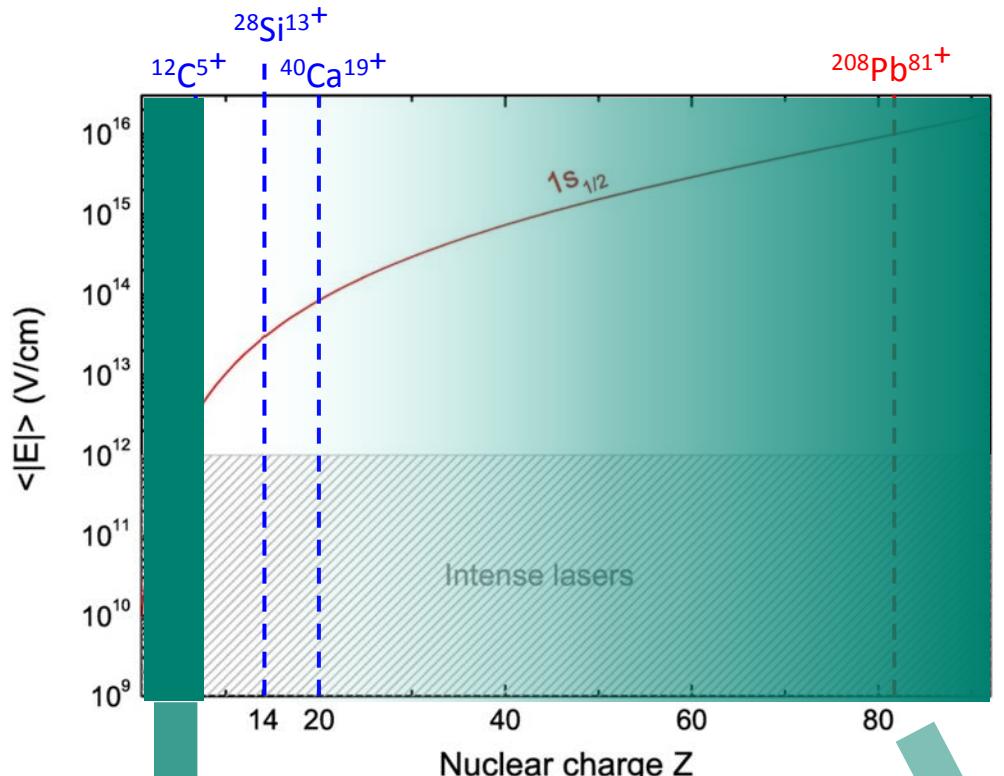
HCl-Trap: GSI, Mainz, MPIK, St. Petersburg

Z. Harman, Ch. Keitel, F. Köhler-Langes, W. Quint, V. Shabaev, S. Sturm





# Quantum electrodynamics of bound states

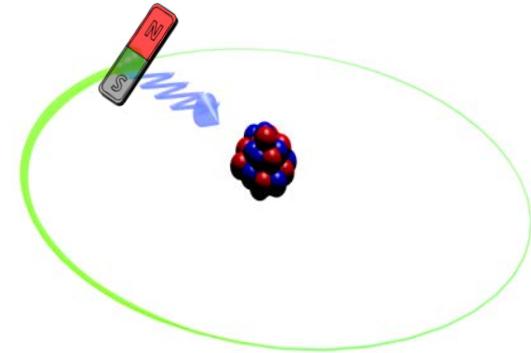


Low field strength

Extract fundamental  
constants (electron mass,  
fine structure constant)

High to ultra-high  
field strength

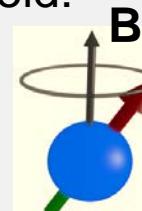
The Standard Model in  
extreme conditions



# Measurement principle

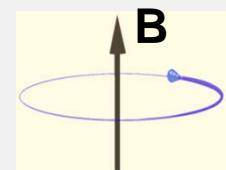
Measurement of the Larmor frequency  
in a well-known magnetic field:

$$\omega_L = \frac{g}{2} \frac{e}{m_e} B$$



Measurement of the free cyclotron  
frequency to determine the  
magnetic field:

$$\omega_c = \frac{q_{ion}}{m_{ion}} B$$



$$g = 2 \frac{\omega_L}{\omega_c} \frac{q_{ion}}{m_{ion}} \frac{m_e}{e} = 2 \Gamma \frac{q_{ion}}{m_{ion}} \frac{m_e}{e}$$

Measured by independent precision experiments

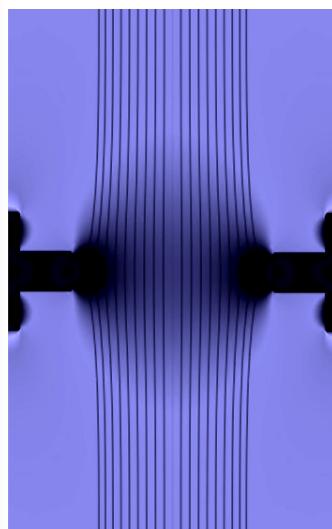
has to be determined



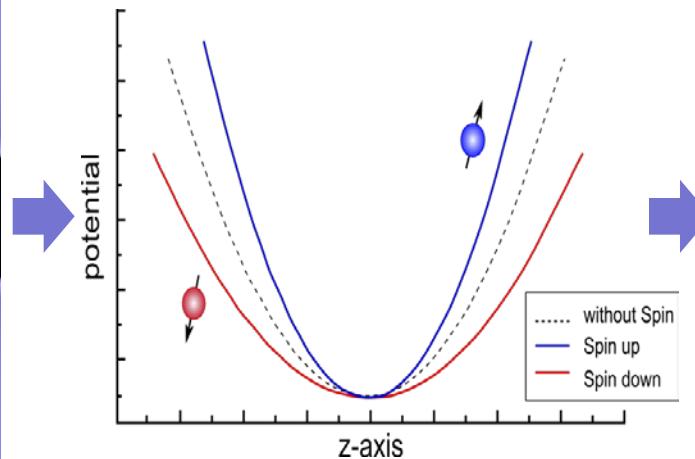
# Continuous Stern-Gerlach effect

- Larmor frequency cannot be detected directly
- Microwaves probe spin transition

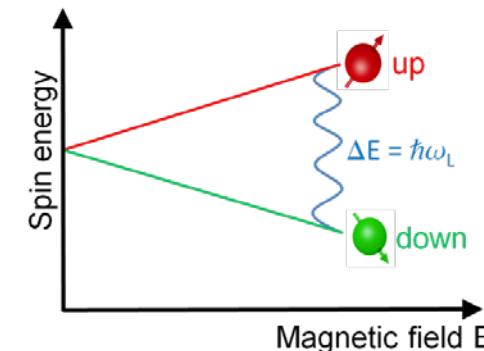
How to detect a successful spinflip ?



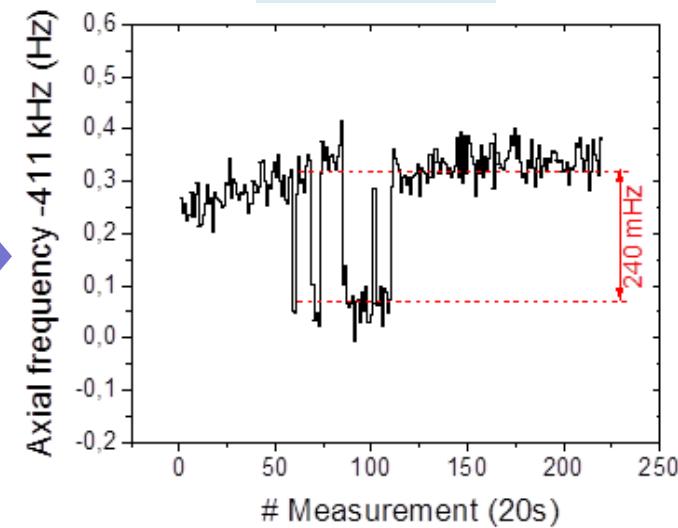
Ferromagnetic ring  
→ magnetic bottle



Spin dependent  
trapping potential



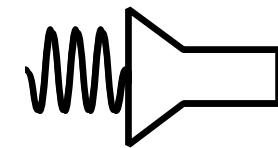
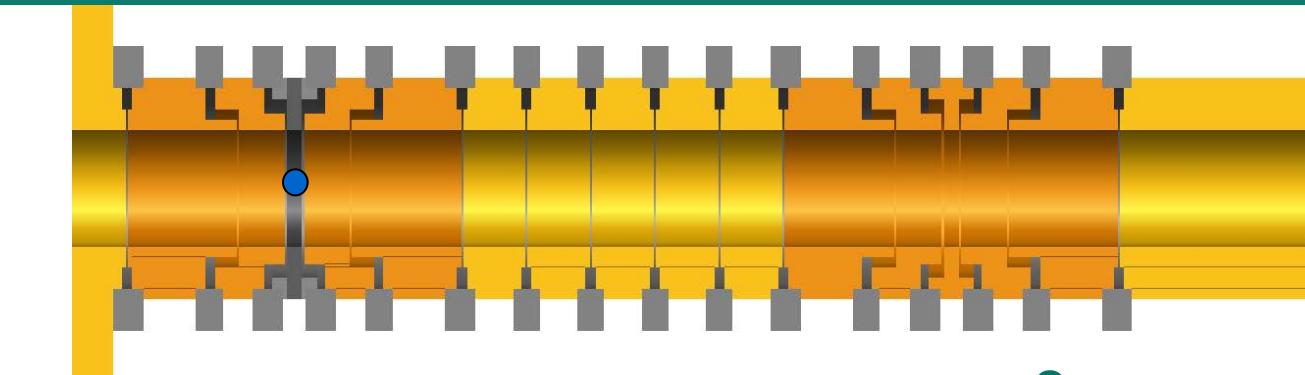
$$\omega_z = \sqrt{\frac{2e_0 U_0}{md_0^2}}$$



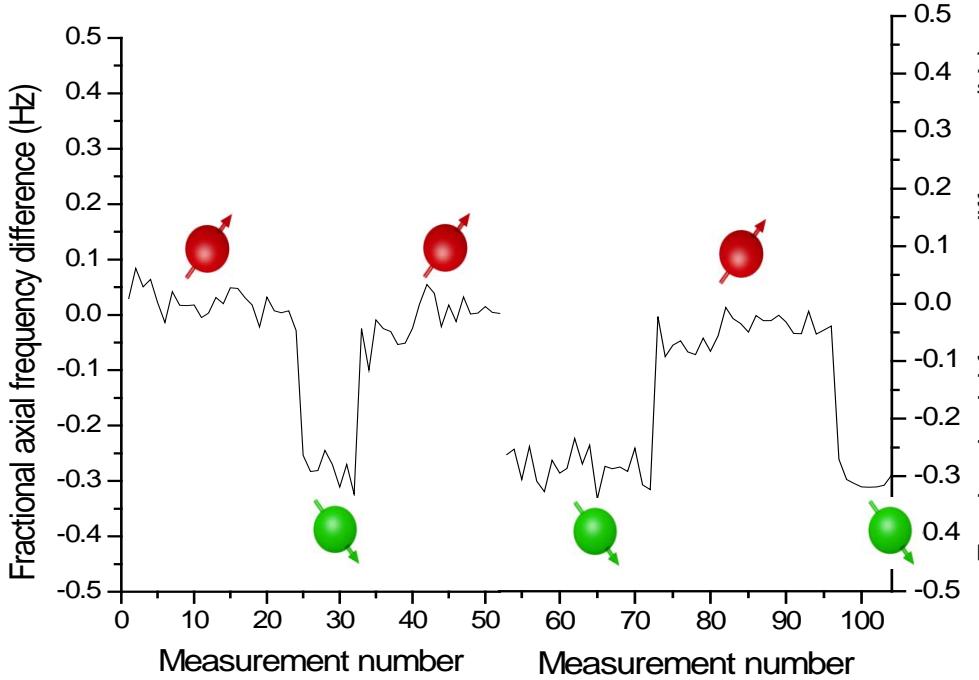
Tiny axial frequency difference  
between spin up and down.



# g-factor measurement process



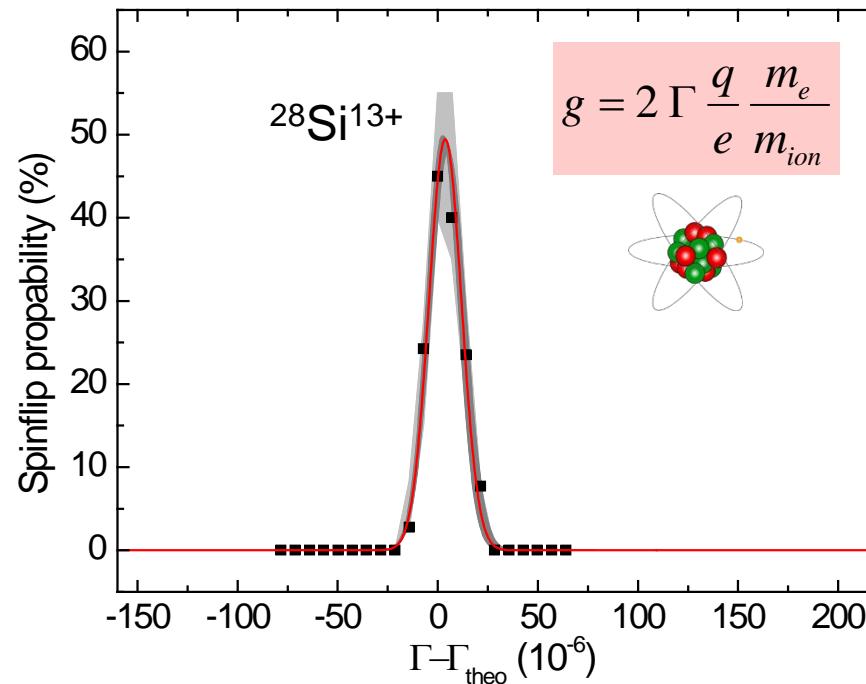
One measurement cycle



- Detection of spin-orientation in analysis trap **2-3min**
- Transport to precision trap **20s**
- Measurement of eigenfrequencies and simultaneous irradiation with microwaves **10min**
- Transport to analysis trap **20s**
- Detection of spin orientation in analysis trap  
→ Spin flip in the precision trap?



# g-factor resonance of a single $^{28}\text{Si}^{13+}$ ion



$$g_{\text{exp}} = 1.995\ 348\ 958\ 7\ (5)(3)(8)$$

$$g_{\text{theo}} = 1.995\ 348\ 958\ 0\ (17)$$

Electron mass can be improved by a factor of >10 if repeated for  $^{12}\text{C}^{5+}$ .

Most stringent test of BS-QED in strong fields.

Theory colleagues: Harman, Keitel, Zatorski

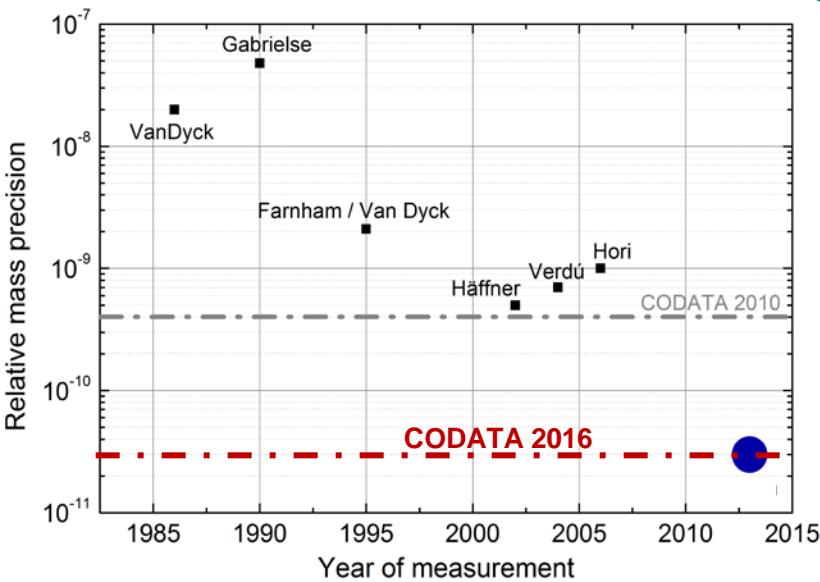
S. Sturm *et al.*, Phys. Rev. Lett. 107, 023002 (2011)  
A. Wagner *et al.*, Phys. Rev. Lett. 110, 133003 (2013)

# A 13-fold improved electron mass

Electron mass from ultra-high precision  
*g*-factor of hydrogenlike carbon:

$$m_e = \frac{g_{\text{theo}}}{2} \frac{\omega_c}{\omega_L} \frac{e}{q_{\text{ion}}} m_{\text{ion}}$$

Harman, Keitel, Zatorski



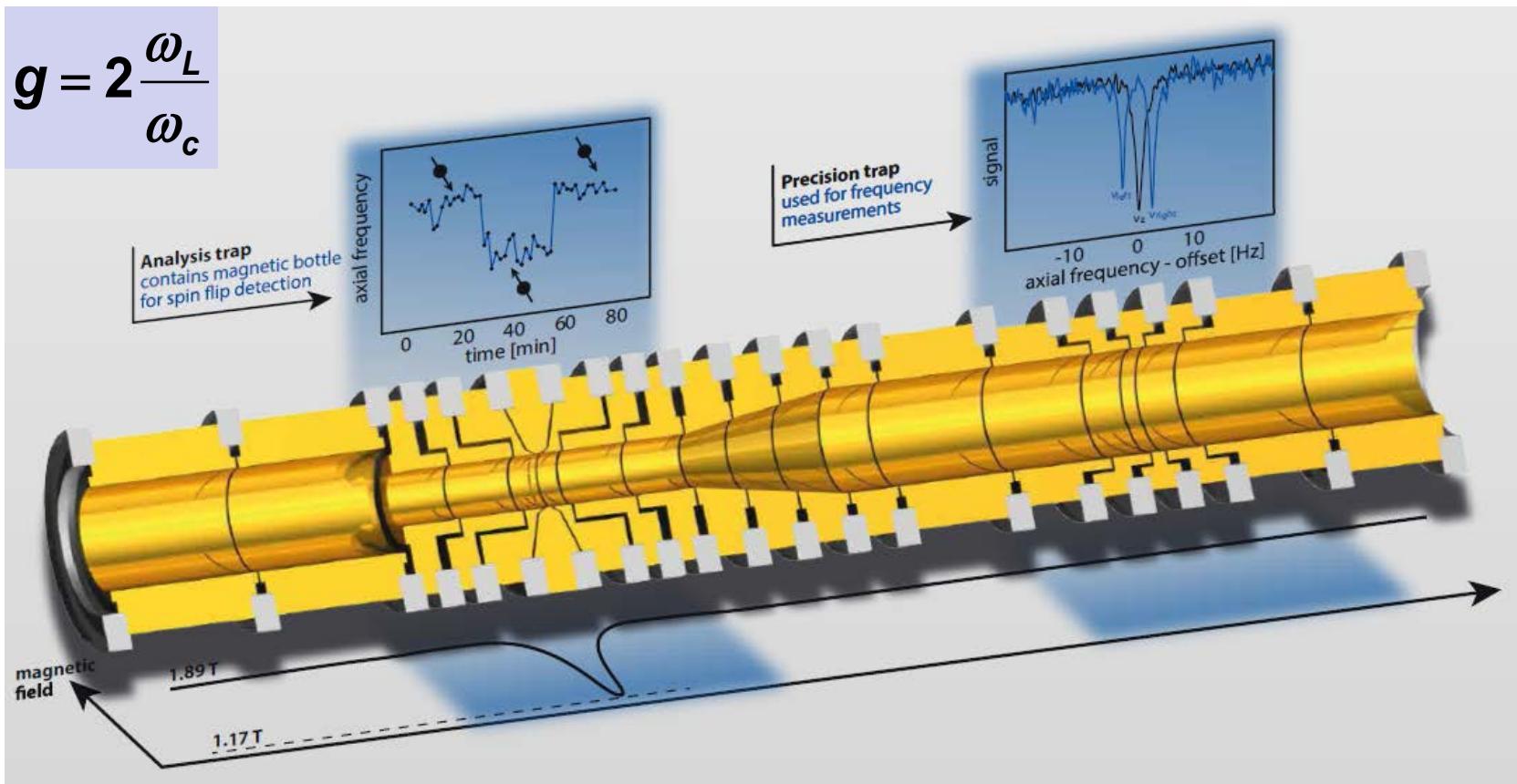
$$m_e = 0.000548579909067(14)(9)(2)u$$

A factor of 13  
improved value !

S. Sturm et al., Nature 506, 467 (2014)



# The (anti-)proton magnetic moment



$$\mu_p = 2.79284734462(82) \mu_N$$

(0.3 ppb)

G. Schneider et al., Science 358, 1081 (2017)

$$\mu_{\bar{p}} = -2.7928473441(42) \mu_N$$

(1.5 ppb)

Ch. Smorra et al., Nature 550, 371 (2017)



# Conclusion

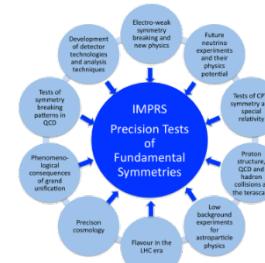
***Exciting results in high-precision experiments with stored and cooled exotic ions have been achieved!***

***Presently running or planned experiments:***  
the mass of the neutron  
improved  $E=mc^2$  test  
improved value for  $\alpha$   
(anti-)p g-factor measurement

**Thanks a lot for the invitation  
and your attention!**



**Max Planck Society**



**IMPRS-PTFS**



**Adv. Grant MEFUCO**



**Helmholtz Alliance**