

# Studies of deconfined matter at the LHC with ALICE

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A. Andronic – GSI Darmstadt  
on behalf of the ALICE Collaboration

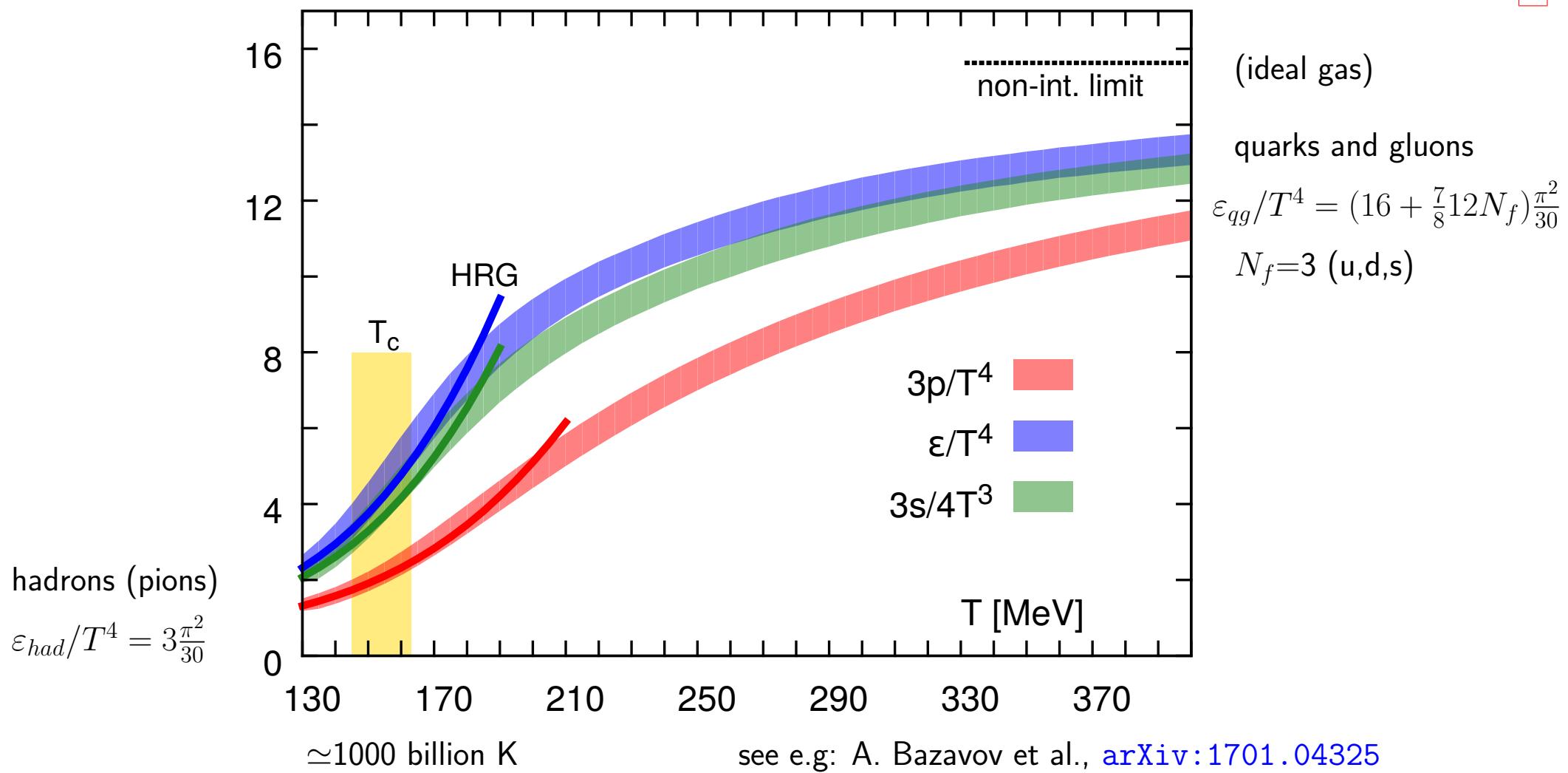


- 
- Introduction: hot QCD (quark-gluon) matter; ALICE apparatus
  - Hadrons with light-flavor ( $u,d,s$ ) and the QCD phase diagram
  - Quarkonium and deconfined matter
  - Jet quenching (if time allows)
  - Summary

# Lattice QCD predicts a phase transition

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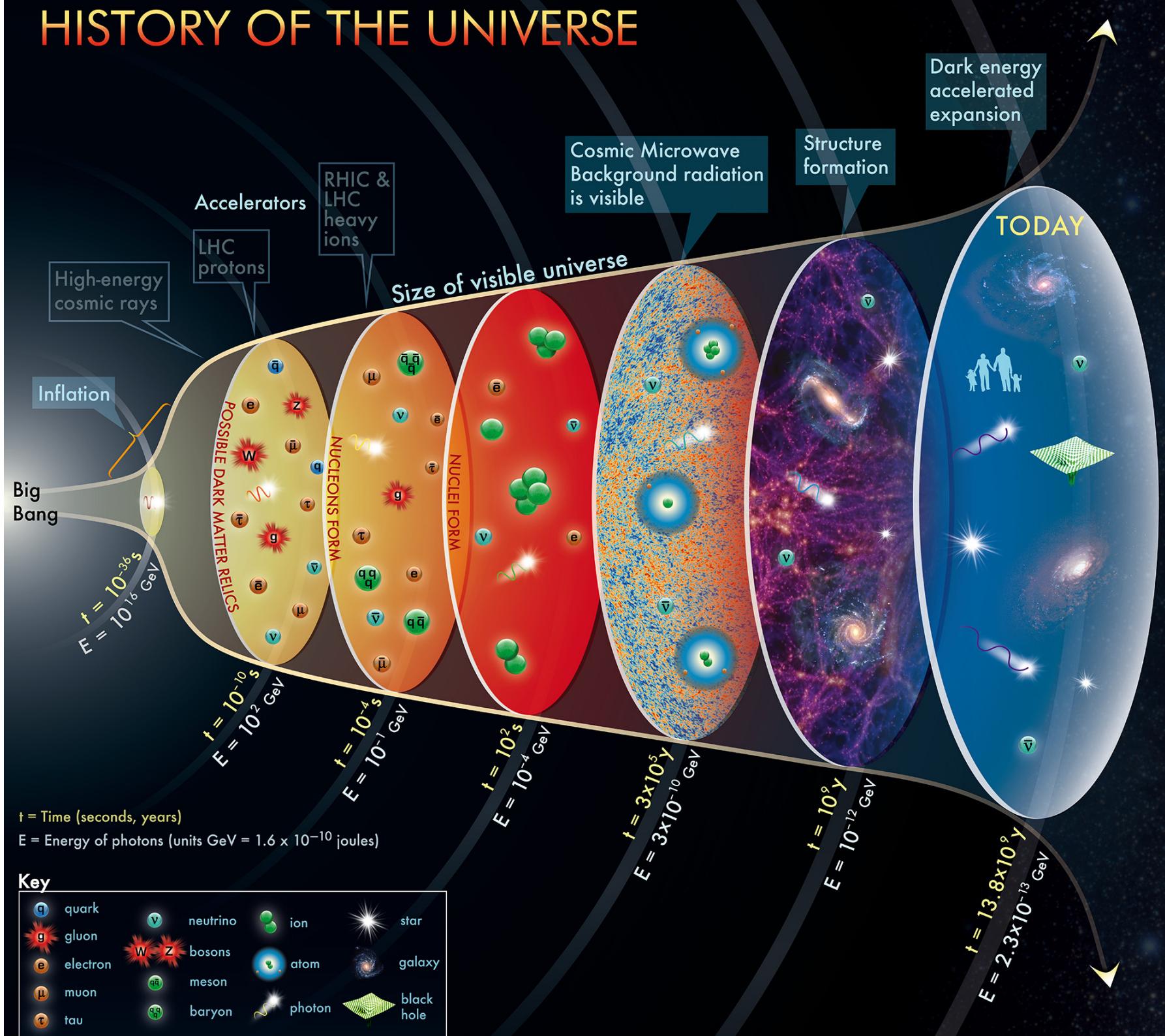


transition is a crossover, Y. Aoki et al., *Nature* 443 (2006) 675

$T_c \simeq 145\text{-}164$  MeV,  $\varepsilon_c \simeq (0.18 - 0.5)$  GeV/fm<sup>3</sup>, or  $(1.2\text{-}3.1)\varepsilon_{nuclear}$

numerical solutions of QCD on a discrete space-time grid (sophisticated formalism, huge computers)

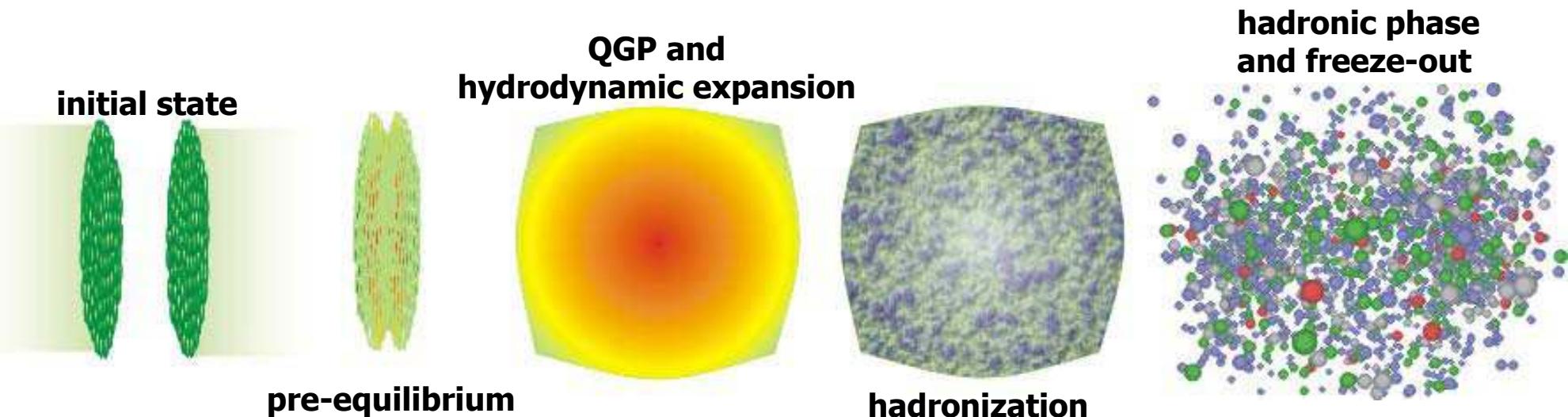
# HISTORY OF THE UNIVERSE



# How to "simulate" in laboratory the early Universe?

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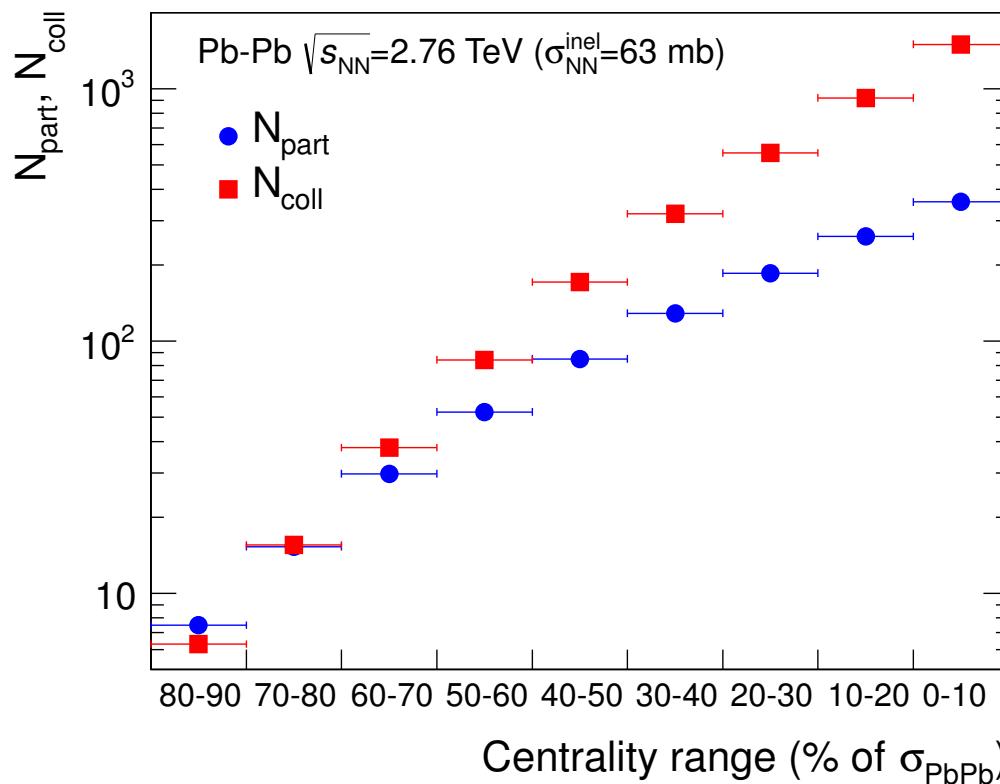


$$t \simeq 10^{-23} \text{ s}, V \simeq 10^{-40} \text{ m}^3$$

1. initial collisions ( $t \leq t_{coll} = 2R/\gamma_{cm}c; R_{Pb} \simeq 7 \text{ fm}$ )
2. thermalization: equilibrium is established ( $t \lesssim 1 \text{ fm}/c = 3 \times 10^{-24} \text{ s}$ )
3. expansion ( $\sim 0.6c$ ) and cooling ( $t < 10-15 \text{ fm}/c$ ) ...deconfined stage?
4. hadronization (quarks and gluons form hadrons)
5. chemical freeze-out: inelastic collisions cease; particle identities (yields) frozen
6. kinetic freeze-out: elastic collisions cease; spectra are frozen ( $t+ = 3-5 \text{ fm}/c$ )

# What are the "control parameters"

- Energy of the collision (per nucleon pair,  $\sqrt{s_{NN}}$ )
  - Centrality of the collision (number of “participating” nucleons,  $N_{part}$ )  
[at high energies geometric concepts valid: “participant-spectator” picture]  
measured in percentage of the geometric cross section ( $\sigma_{AB} = \pi(R_A + R_B)^2$ )
- NB: we sort the collisions offline, based on detector signals*

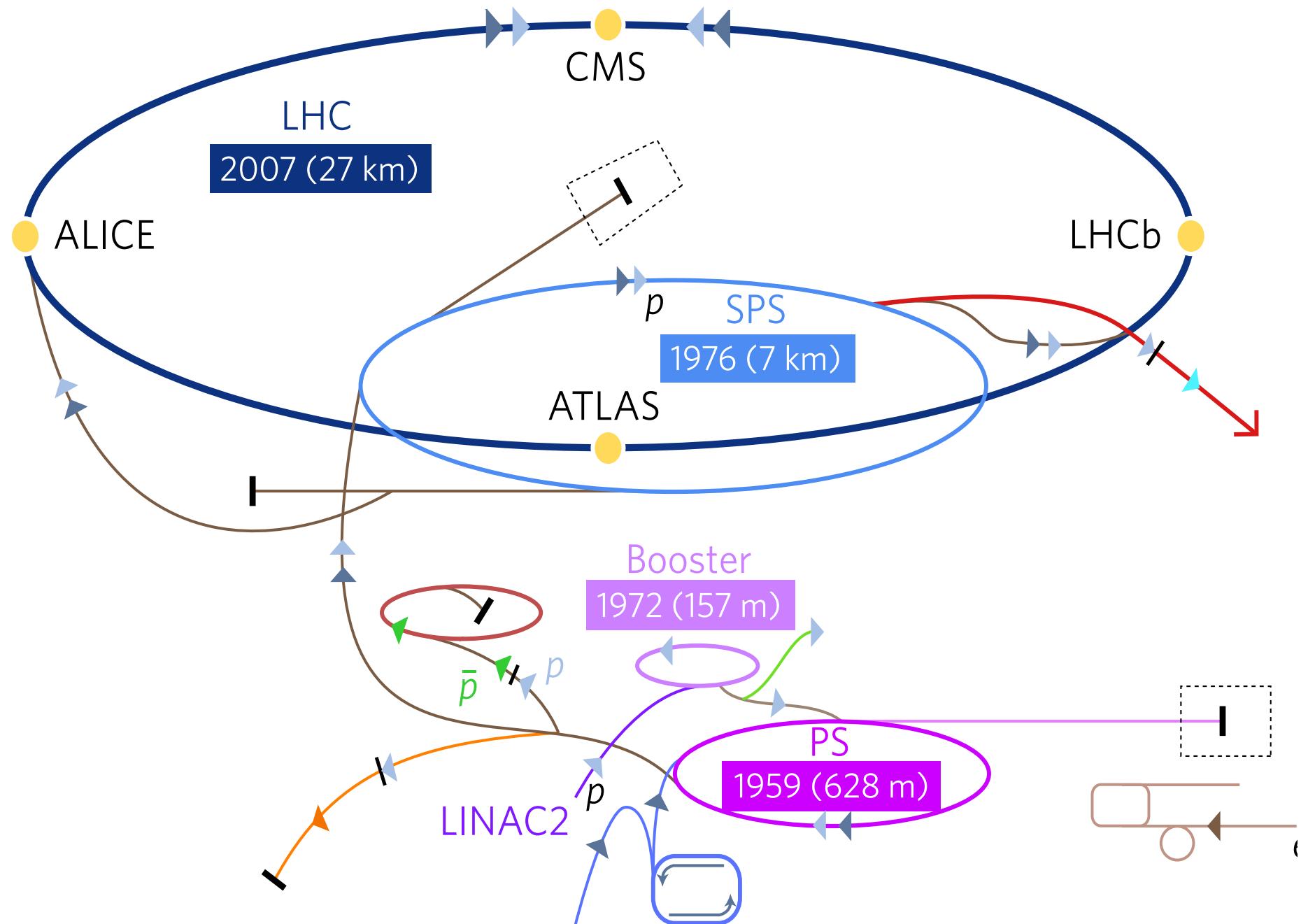


...while often taking as reference the measurement in proton-proton collisions (at the same energy), for “hard probes” (pQCD) scaled by the number of collisions corresponding to the given centrality class

# The accelerator complex at CERN

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# The accelerator complex at CERN

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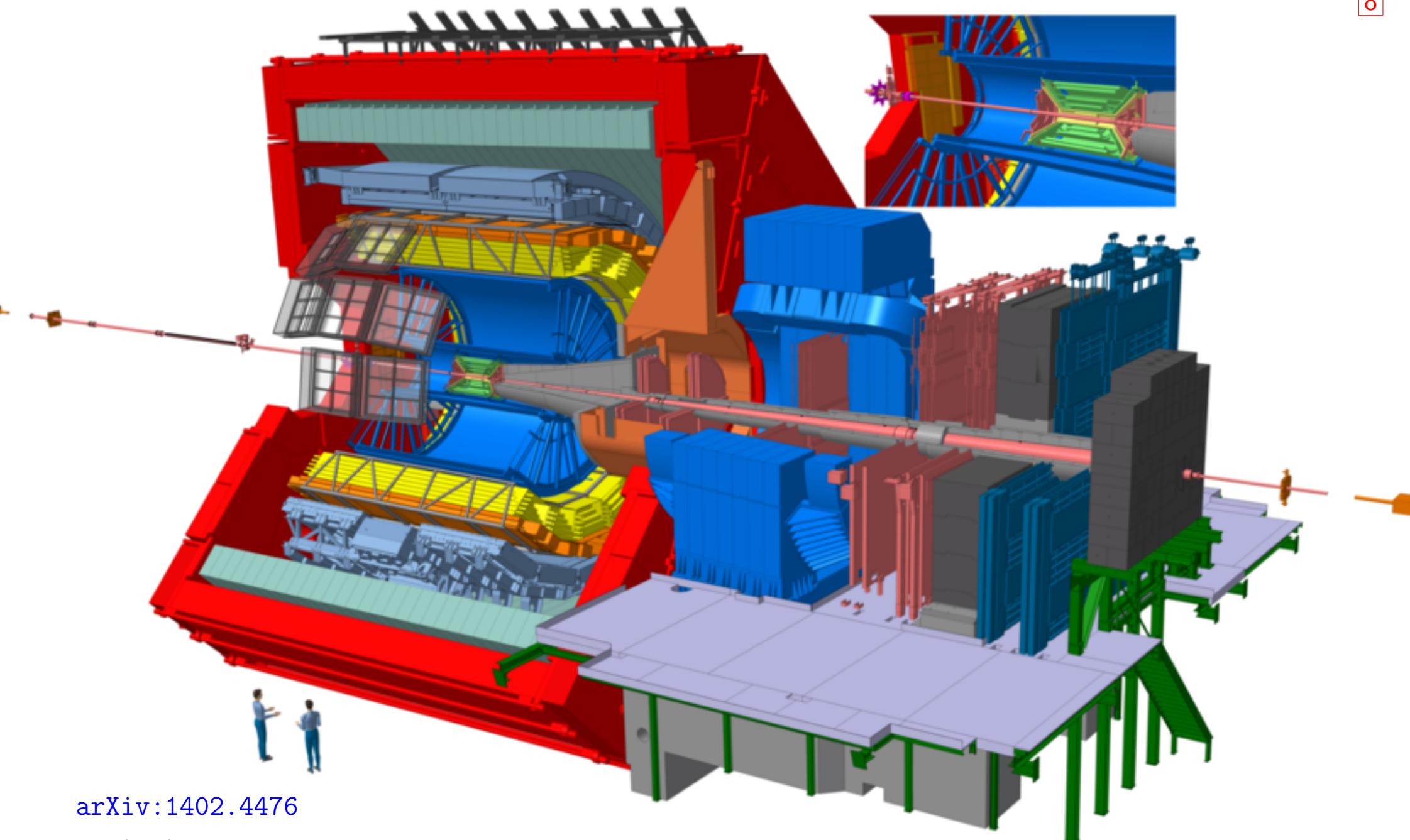
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# The ALICE apparatus

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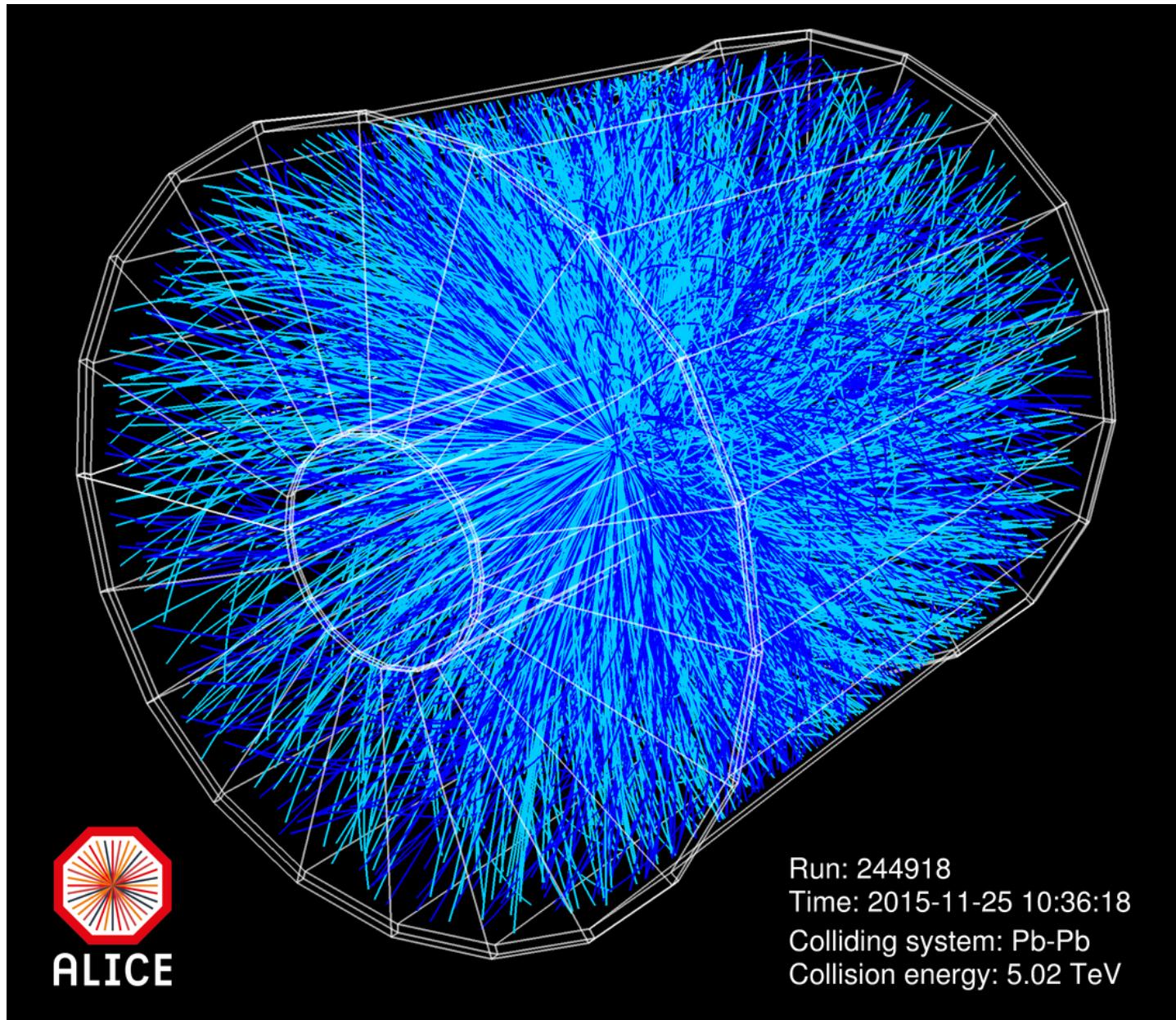
arXiv:1402.4476

ALICE Collaboration: 37 countries, 176 institutions, 1800 members

# Nucleus-nucleus collisions at the LHC

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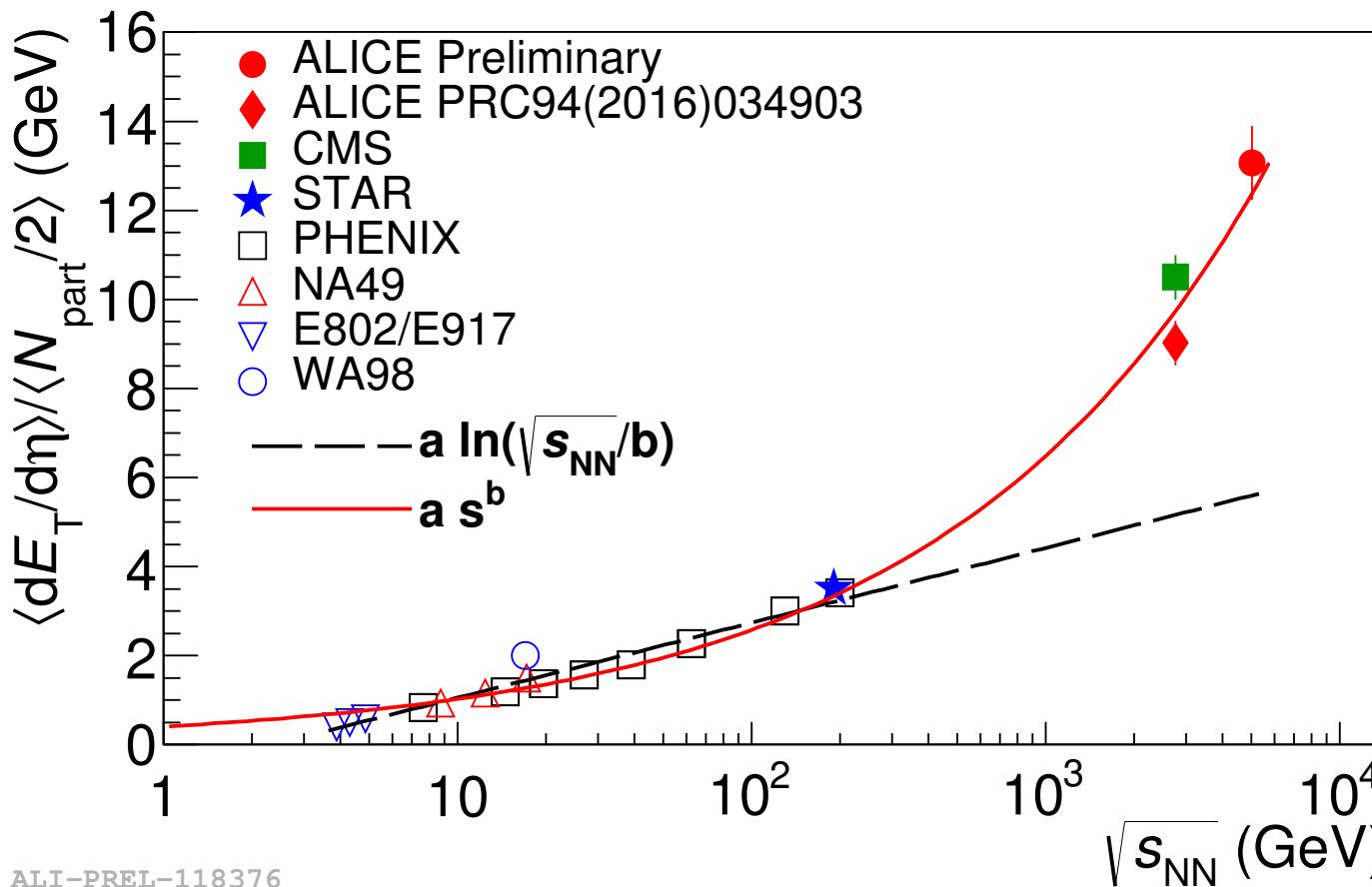
a picture of a central collision (about 3200 primary tracks in  $|\eta| < 0.9$ ); “Camera”: Time Projection Chamber

[ 5 m length, 5 m diam.; 500 mil. pixels; we take a few 100 pictures per second (and are preparing to take 50000) ]

# Nucleus-nucleus collisions: energy density

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$E_T$ : transverse energy  
(energy built from  $p_T$ )

$\varepsilon_{LHC} \simeq 20 - 40 \text{ GeV/fm}^3$   
(much above  $\varepsilon_c$ )

$\varepsilon_{FAIR} \lesssim 1 \text{ GeV/fm}^3$   
(around  $\varepsilon_c$ )

self-similar (Hubble-like) homogeneous (hydrodynamic) expansion of the fireball in the longitudinal (beam) direction  
("Bjorken model", J.D. Bjorken, PRD 27 (1983) 140)

$$\text{Energy density: } \varepsilon = \frac{1}{A_T} \frac{dE_T}{dy} \frac{1}{c\tau}$$

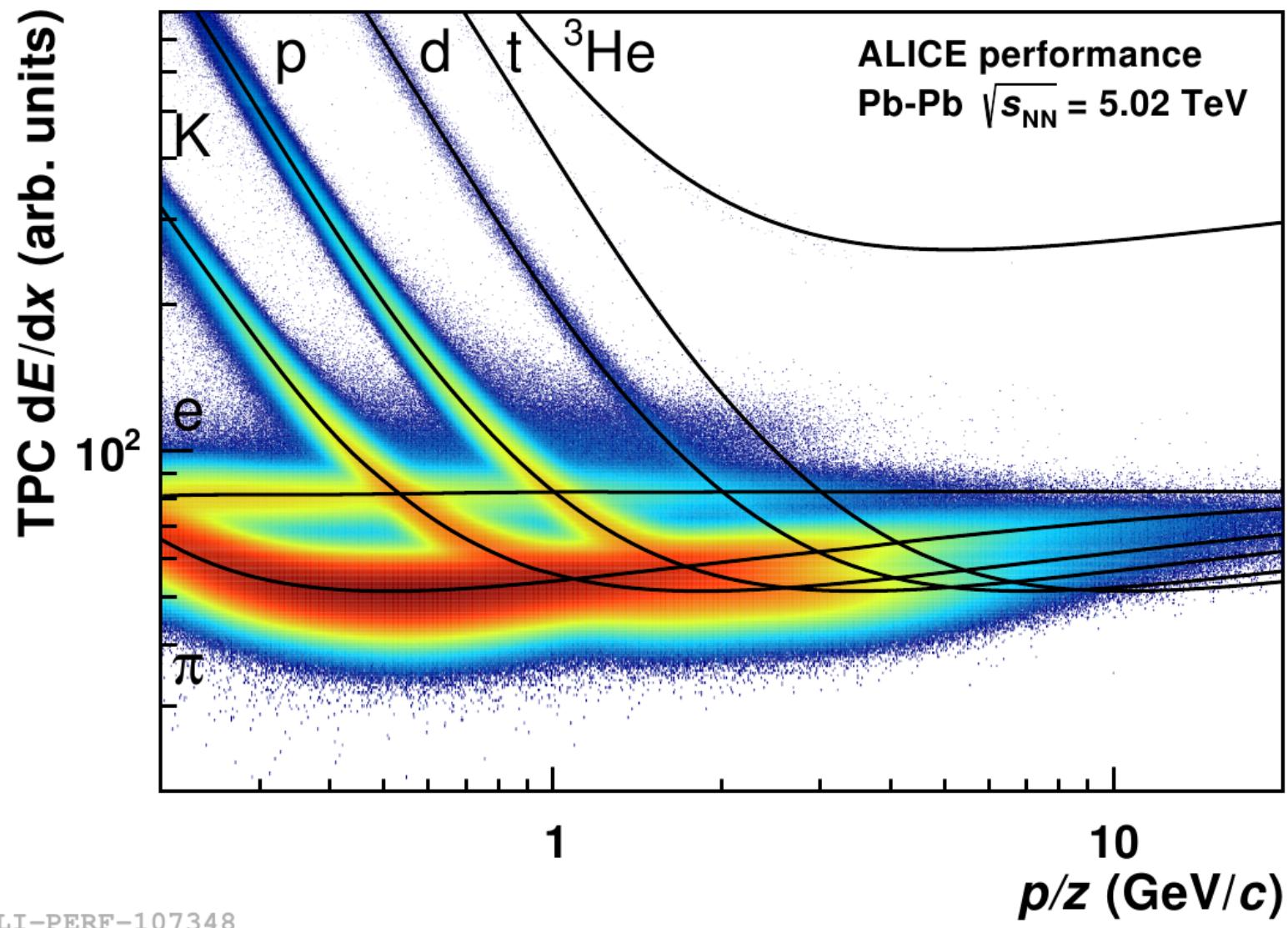
-  $A_T = \pi R^2$ : transverse area (Pb-Pb:  $A_T = 154 \text{ fm}^2$ )

-  $\tau \simeq 1 \text{ fm}/c$ : formation time (establishing the equilibrium) ... not measurable!

# Particle identification

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ALI-PERF-107348

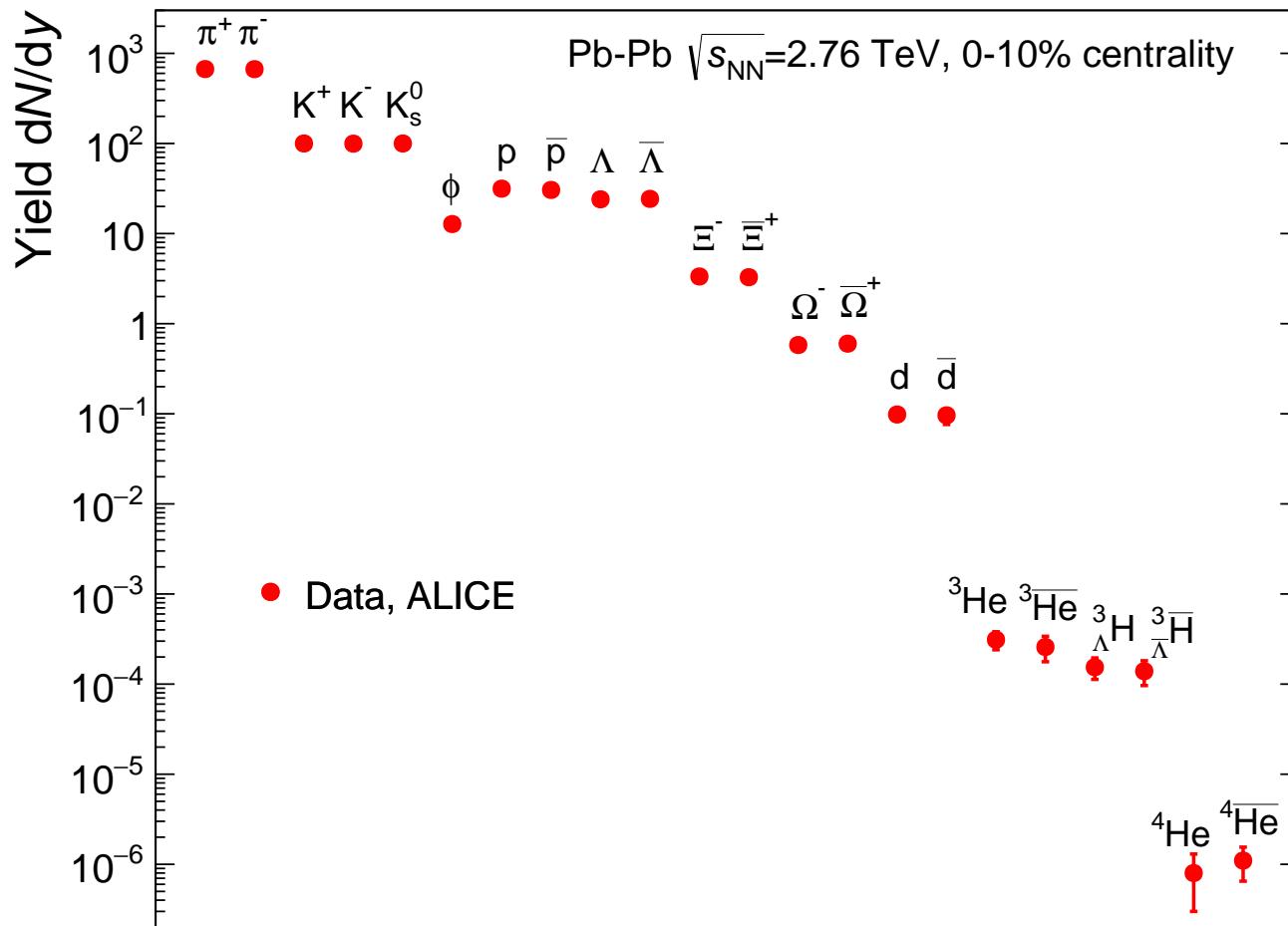
$dE/dx$ : truncated mean of 159 samples along a track; resolution: 5.8%

lines: Bethe-Bloch parametrization    particles and antiparticles are shown

# Hadron yields

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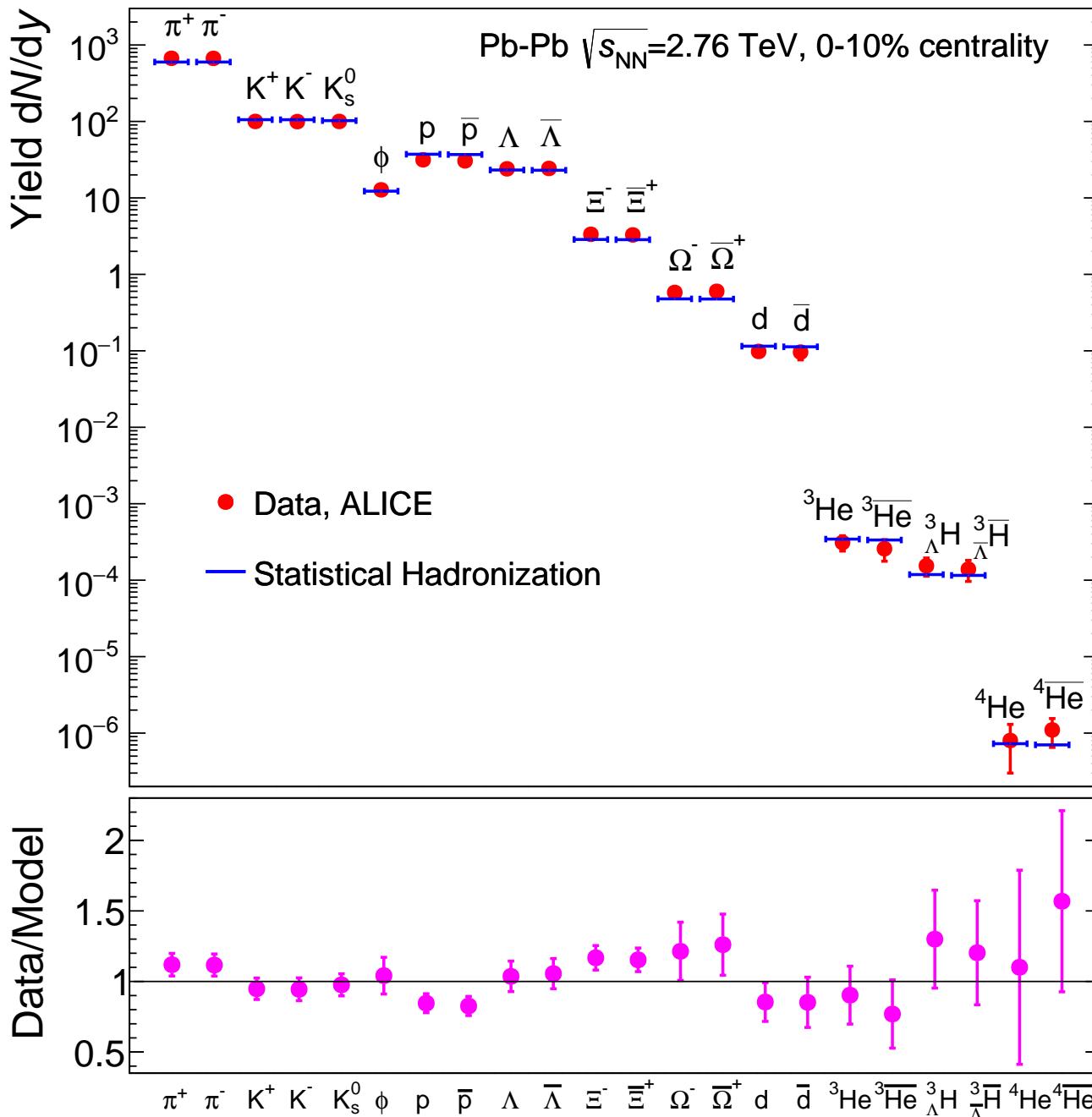
Matter and antimatter are produced in equal amounts in high-energy Pb-Pb collisions at the LHC

Mass hierarchy in production

# Hadron yields and statistical hadronization

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Matter and antimatter are produced in equal amounts in high-energy Pb-Pb collisions at the LHC

Best fit:

$$T_{CF} = 156.5 \pm 1.5 \text{ MeV}$$

$$\mu_B = 0.7 \pm 3.8 \text{ MeV}$$

$$V = 5280 \pm 410 \text{ fm}^3$$

*chemical freeze-out*

Laboratory creation of a piece of hot Universe when 10  $\mu\text{s}$  old,  $T \simeq 10^{12} \text{ K}$

[arXiv:1710.07531](https://arxiv.org/abs/1710.07531)

[arXiv:1710.09425](https://arxiv.org/abs/1710.09425)

# Thermal fit of hadron abundances

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$$n_i = N_i/V = -\frac{T}{V} \frac{\partial \ln Z_i}{\partial \mu} = \frac{g_i}{2\pi^2} \int_0^\infty \frac{p^2 dp}{\exp[(E_i - \mu_i)/T] \pm 1}$$

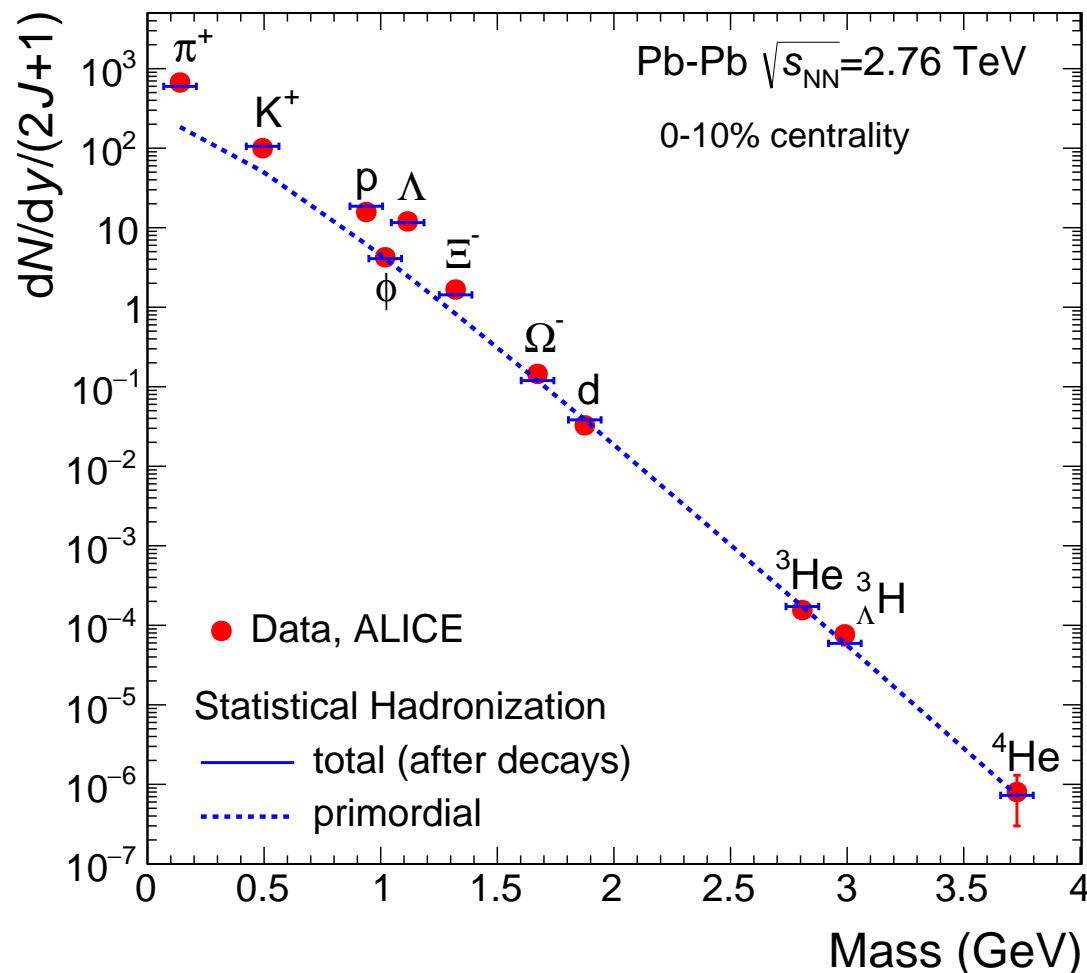
quantum nr. conservation ensured via chemical potentials:

$$\mu_i = \mu_B B_i + \mu_{I_3} I_{3i} + \mu_S S_i + \mu_C C_i$$

Latest PDG hadron mass spectrum (up to 3 GeV, 500 species)

$$\text{Minimize: } \chi^2 = \sum_i \frac{(N_i^{exp} - N_i^{therm})^2}{\sigma_i^2}$$

$$N_i: \text{hadron yield} \Rightarrow (T, \mu_B, V)$$

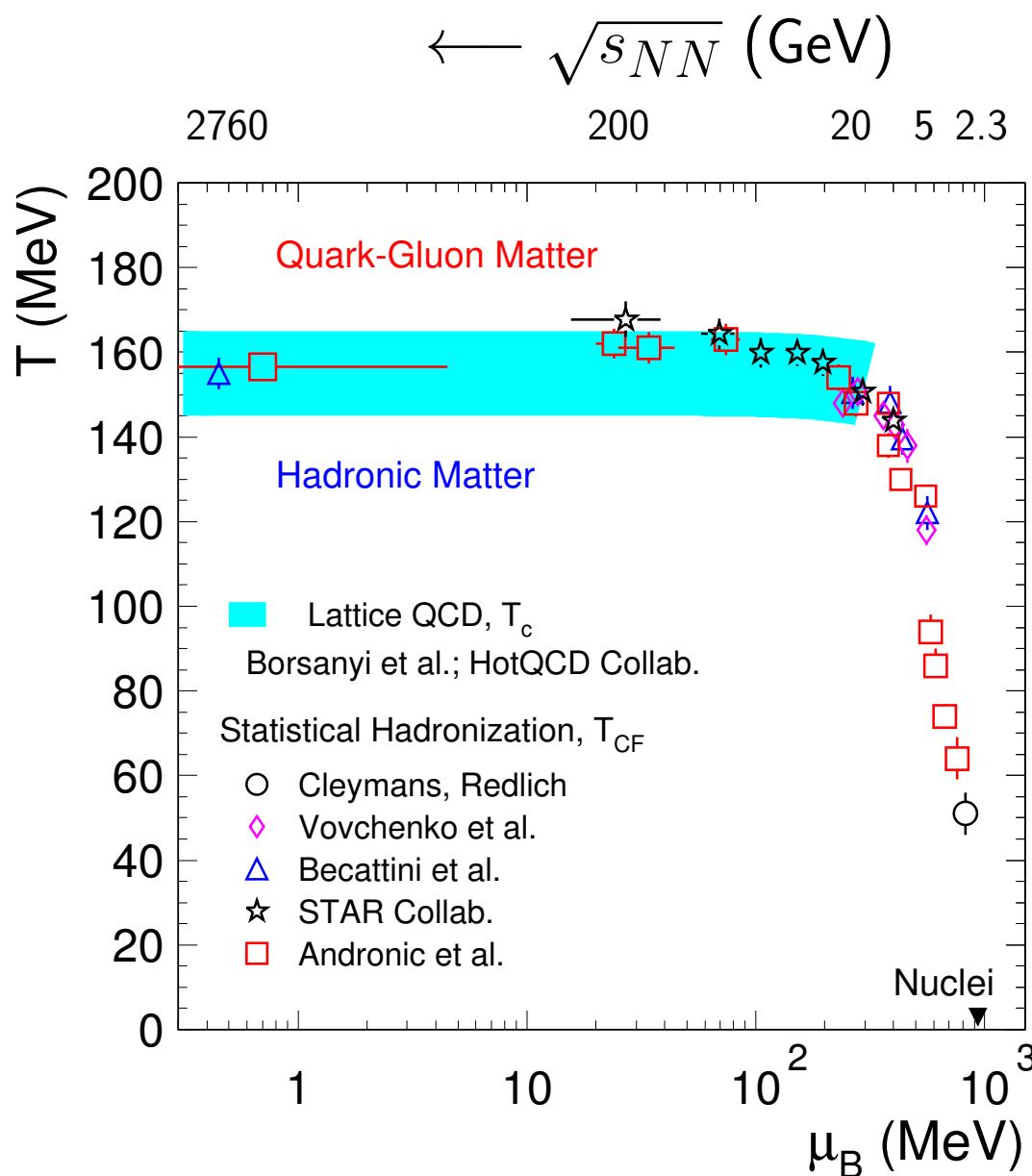


The hadron abundances are in agreement with a chemically-equilibrated system  
*...but how can a loosely-bound deuteron “survive” at  $T=156$  MeV?*

# Chemical freeze-out and the phase diagram of QCD

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at LHC, remarkable “coincidence” with Lattice QCD results

at LHC ( $\mu_B \simeq 0$ ): purely-produced (anti)matter ( $m = E/c^2$ ), as in the Early Universe

$\mu_B > 0$ : more matter, from “remnants” of the colliding nuclei

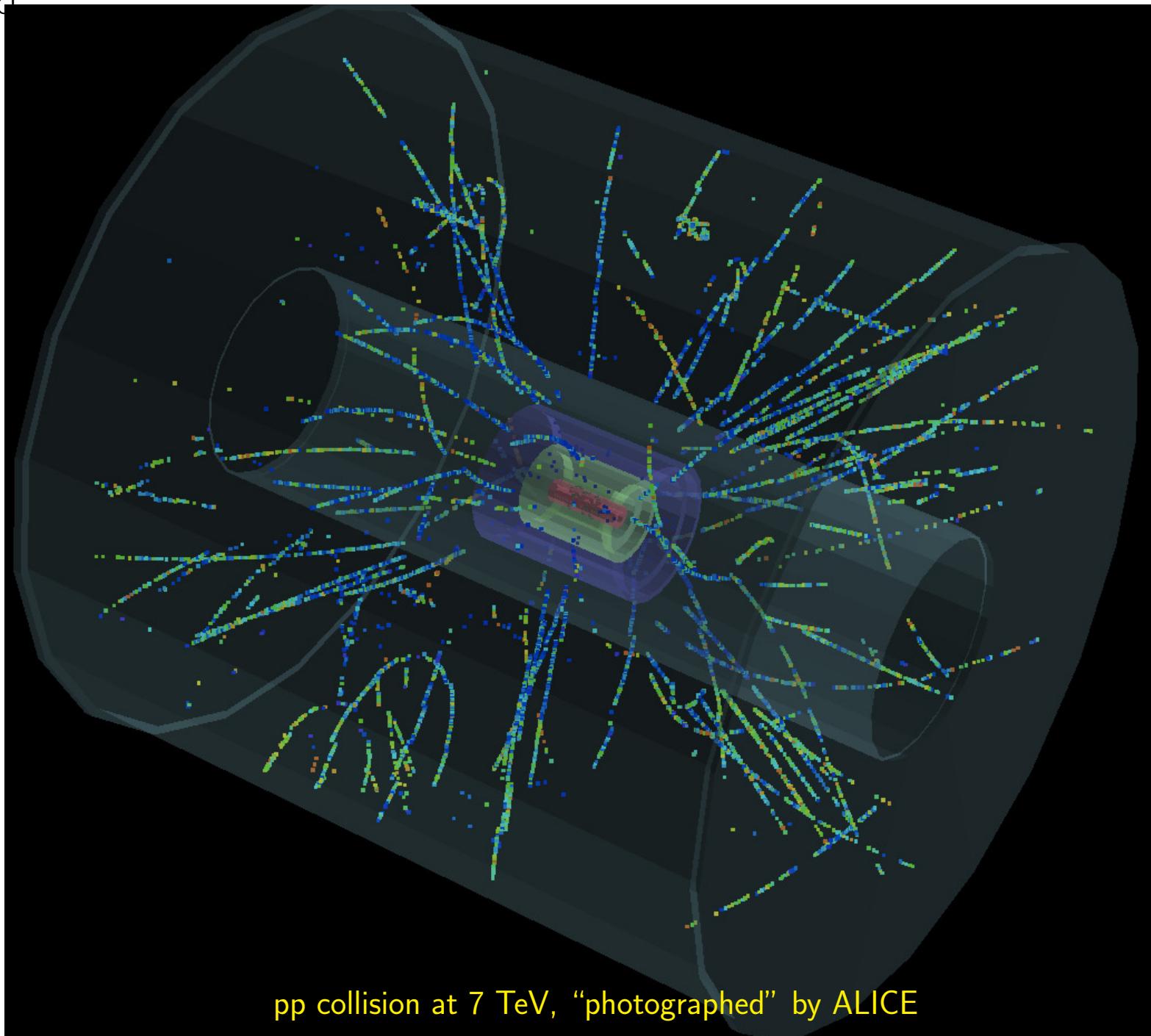
$\mu_B \gtrsim 400$  MeV: *the critical point awaiting discovery*

$\mu_B$  is a measure of the net-baryon density, or matter-antimatter asymmetry

# Proton collisions at the LHC

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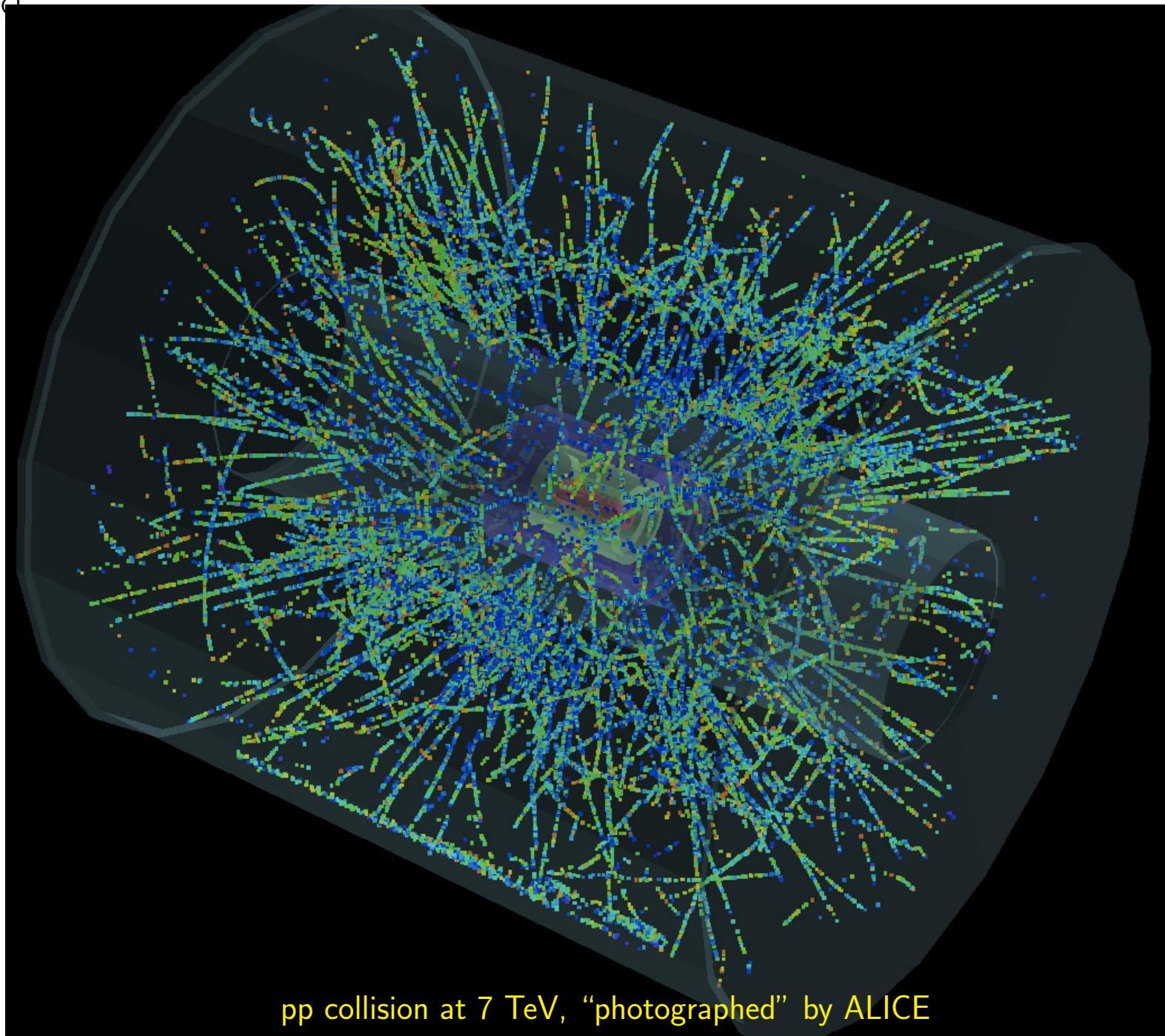
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# Proton collisions at the LHC

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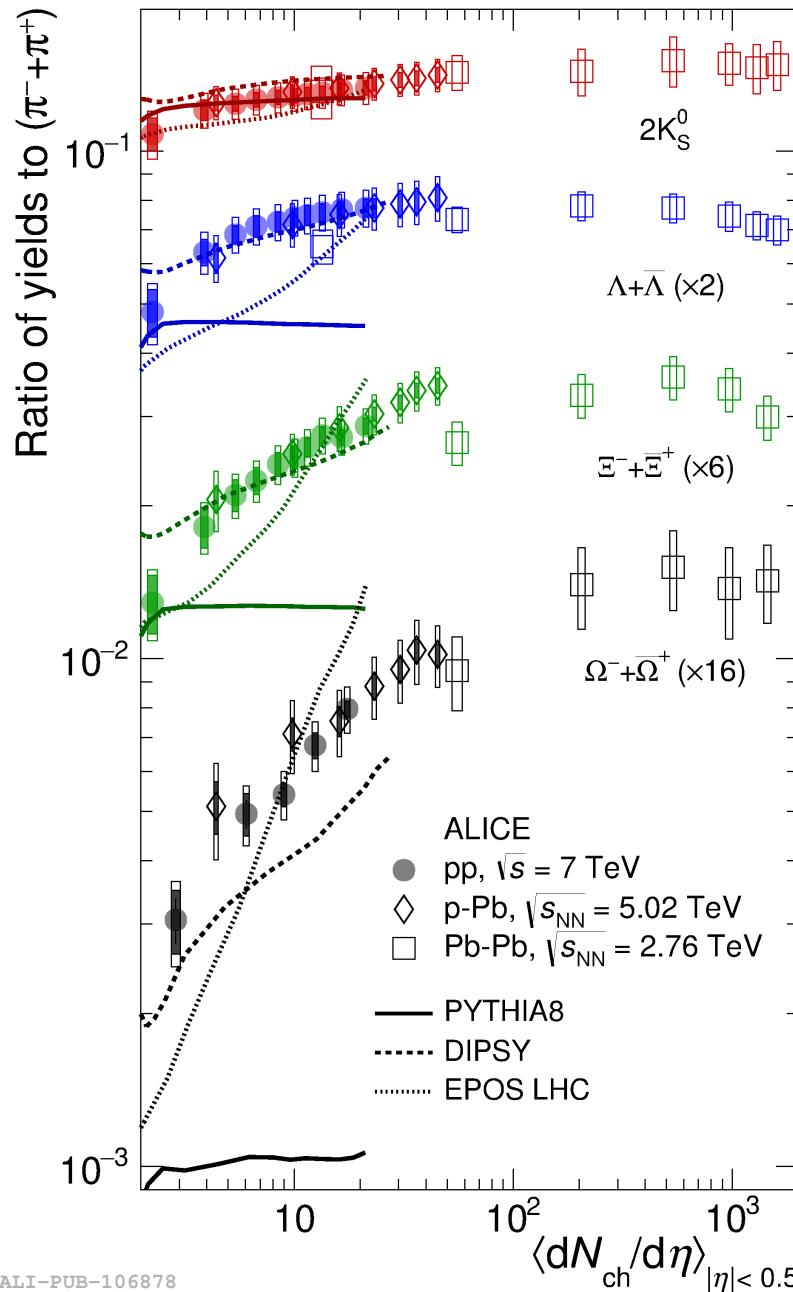
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# Hyperon production - from small to large systems

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(big geometric) fireball in Pb–Pb reached with violent pp and p–Pb collisions

(grand canonical) statistical description works well in Pb–Pb (with  $T$  of QCD phase boundary)

*is the same mechanism at work in small systems (at large multiplicities)?*

string hadronization models do not describe data well

...new ideas are being put forward

Fischer, Sjöstrand, JHEP 01 (2017) 140

“thermodynamical string fragmentation”

# Fluctuations of relative hadron production

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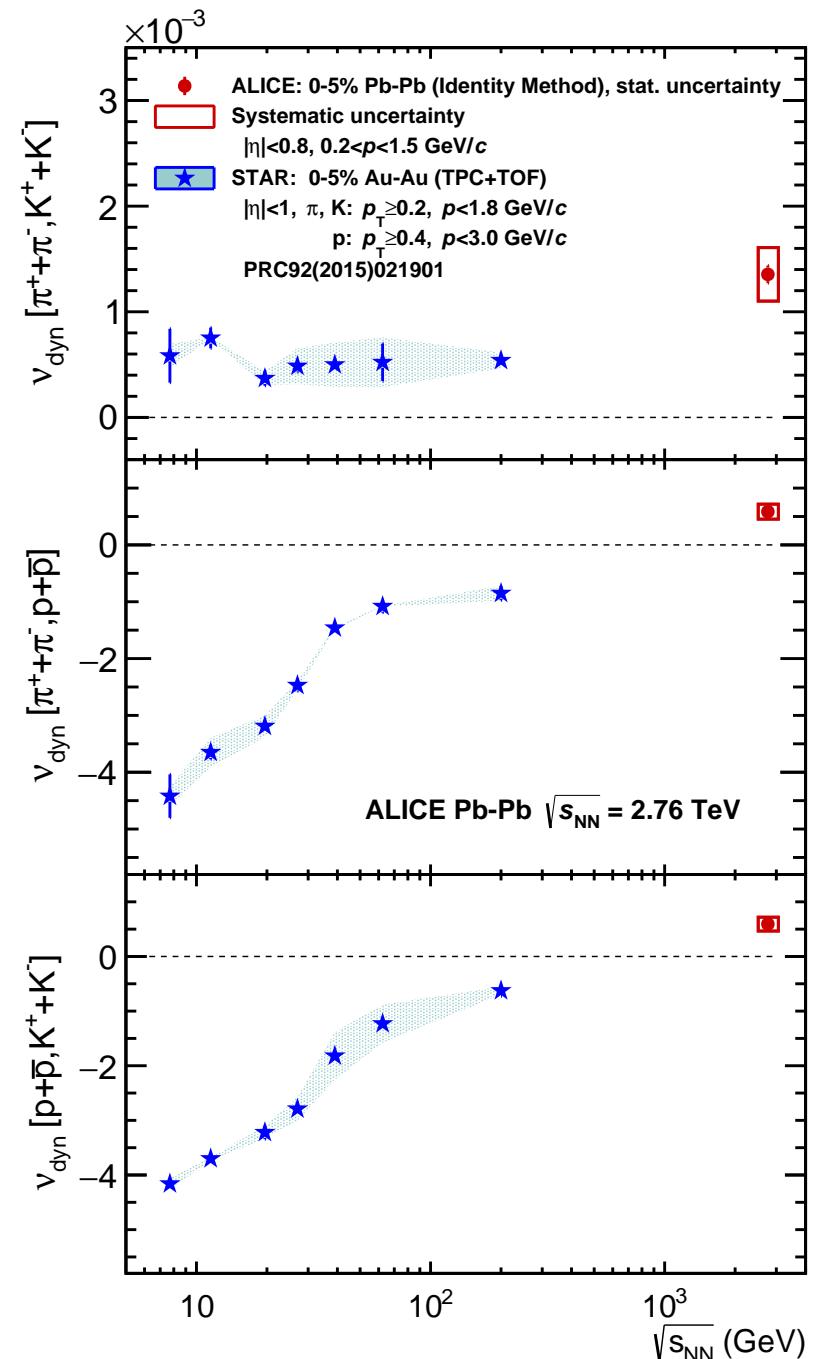
quantified by

$$\nu_{\text{dyn}}[A, B] = \frac{\langle N_A(N_A-1) \rangle}{\langle N_A \rangle^2} + \frac{\langle N_B(N_B-1) \rangle}{\langle N_B \rangle^2} - 2 \frac{\langle N_A N_B \rangle}{\langle N_A \rangle \langle N_B \rangle}$$

the relative strength of fluctuations of species  $A$  and  $B$  - relative strength of correlations between species  $A$  and  $B$   
(event-by-event)

$\nu_{\text{dyn}}[A, B] = 0$  if  $A$  and  $B$  are produced in a statistically independent way

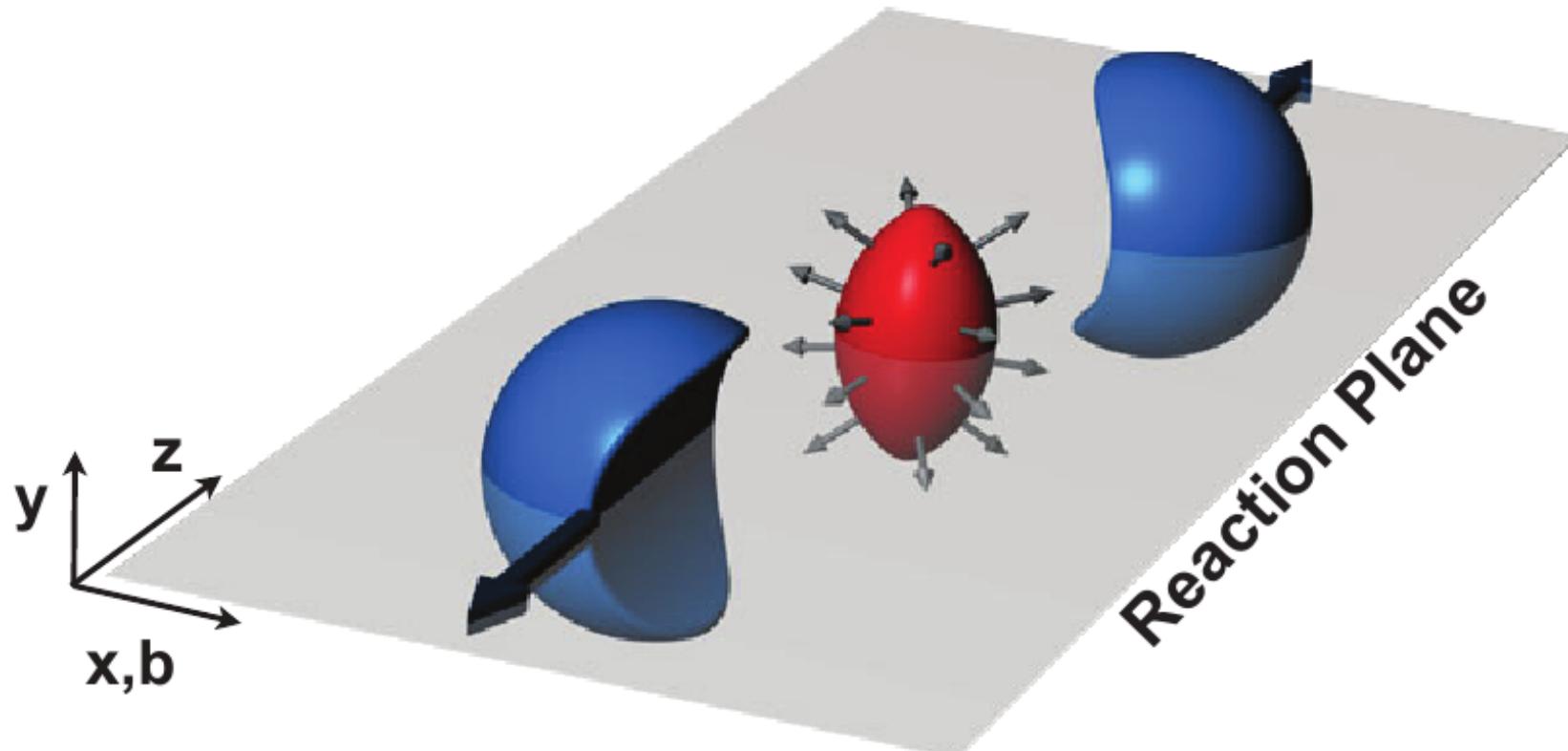
arXiv:1712.07929



# Collective flow

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R. Snellings, [arXiv:1102.3010](https://arxiv.org/abs/1102.3010)

$$\frac{dN}{d\varphi} \sim [1 + 2v_1 \cdot \cos(\varphi) + 2v_2 \cdot \cos(2\varphi) + \dots]$$

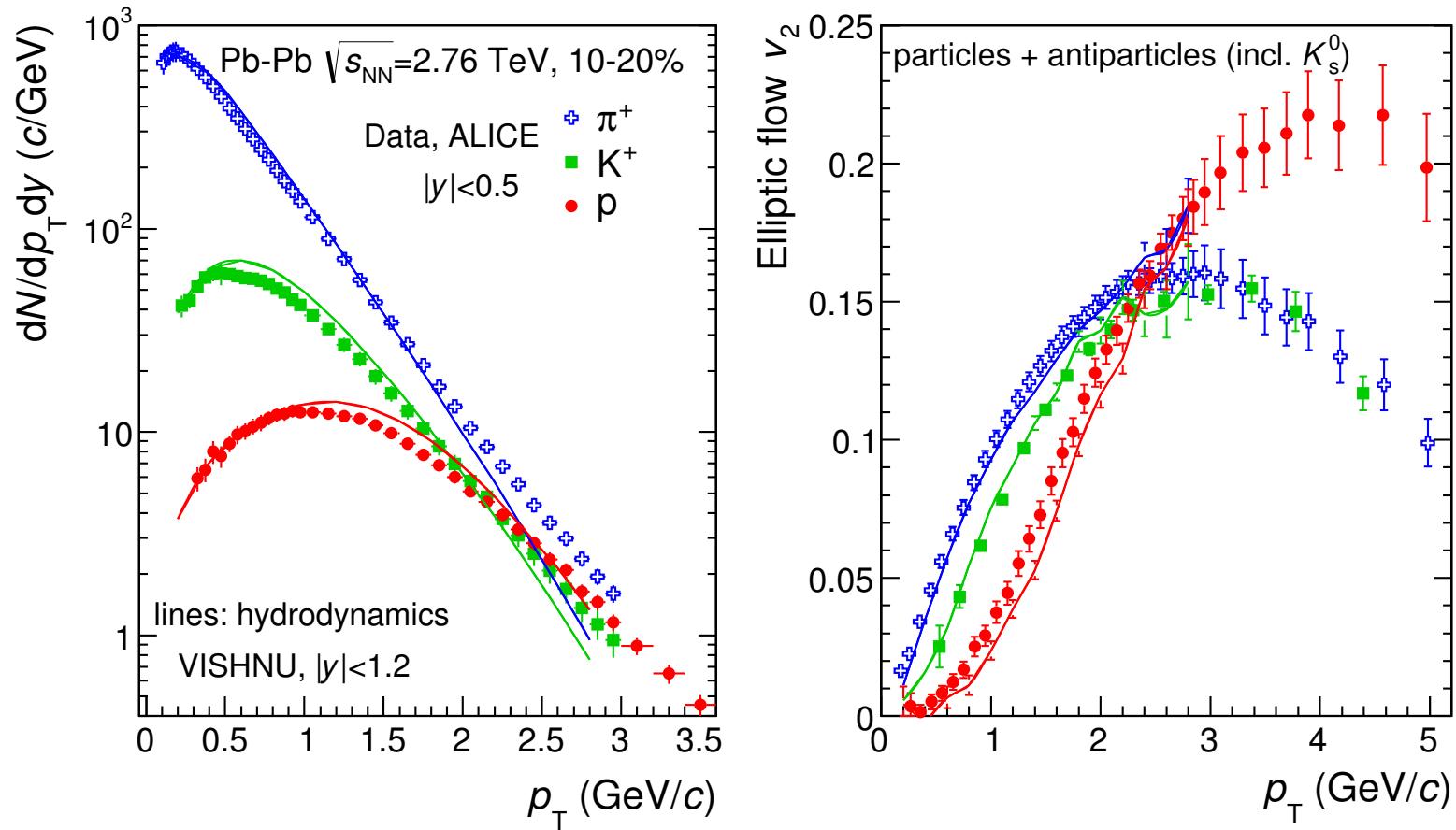
$\varphi$  is azimuthal angle with respect to reaction plane

$v_2 = \langle \cos(2\varphi) \rangle$  we call *elliptic flow*,  $v_3 = \langle \cos(3\varphi) \rangle$  *triangular flow* (coefficients)

# Data and hydrodynamics

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mass dependence due to collective flow

hydrodynamic models reproduce the data with a very small viscosity/entropy density,  $\eta/s$  ( $\sim T\lambda c_s$ )

lower bound conjectured (AdS/CFT):  $\eta/s \geq 1/4\pi$

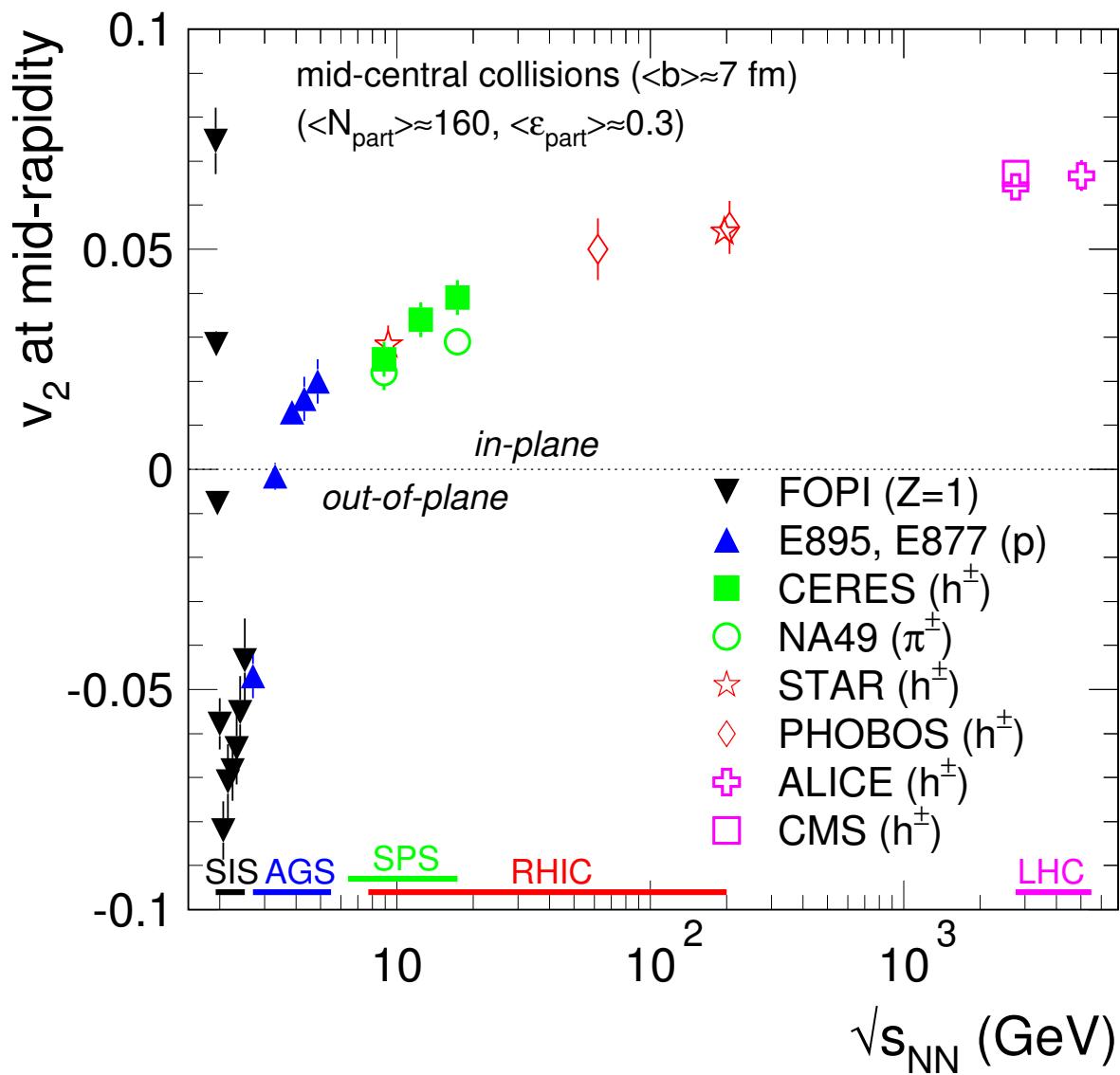
Kovtun, Son, Starinets, PRL 94 (2005) 111601

Data:  
[PRC 88 \(2013\) 044910](#)  
[JHEP 06 \(2015\) 190](#)  
 VISHNU:  
[PRC 89 \(2014\) 034919](#)

# Elliptic flow: energy dependence

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$v_2 > 0$  at high energies: “free” fireball (almond-shape) expansion (“genuine” elliptic flow)

hydrodynamic description determined by  $\eta/s$  and *initial conditions* (matter/energy fluctuations of colliding nuclei)

...constrained by correlations between  $v_n$  coeff., [arXiv:1709.01127](https://arxiv.org/abs/1709.01127)

we do also “event-shape engineering”, [arXiv:1709.04723](https://arxiv.org/abs/1709.04723)

# Quark interlude

up to now we only considered hadrons built with  $u, d, s$  quarks  
...these are light, masses from a few MeV ( $u, d$ ) to  $\sim 90$  MeV ( $s$ )

what about heavier ones?

...for instance  $c$ , which weights about 1.2 GeV

produced in pairs ( $c\bar{c}$ ) in initial hard collisions ( $t \sim \hbar c/(2m_c) \leq 0.1$  fm/c)

observable:  $R_{AA} = \frac{dN_{AA}/dp_T dy}{N_{coll} \cdot dN_{pp}/dp_T dy}$ , the nuclear modification factor

one meson, the  $J/\psi$  (a bound state of  $c$  and  $\bar{c}$ , charmonium) is of particular interest

# Charmonium and deconfined matter

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the original idea: Matsui & Satz, PLB 178 (1986) 178

"If high energy heavy-ion collisions lead to the formation of a hot quark-gluon-plasma, then color screening prevents  $c\bar{c}$  binding in the deconfined interior of the interaction region."

Refinements: "sequential suppression":

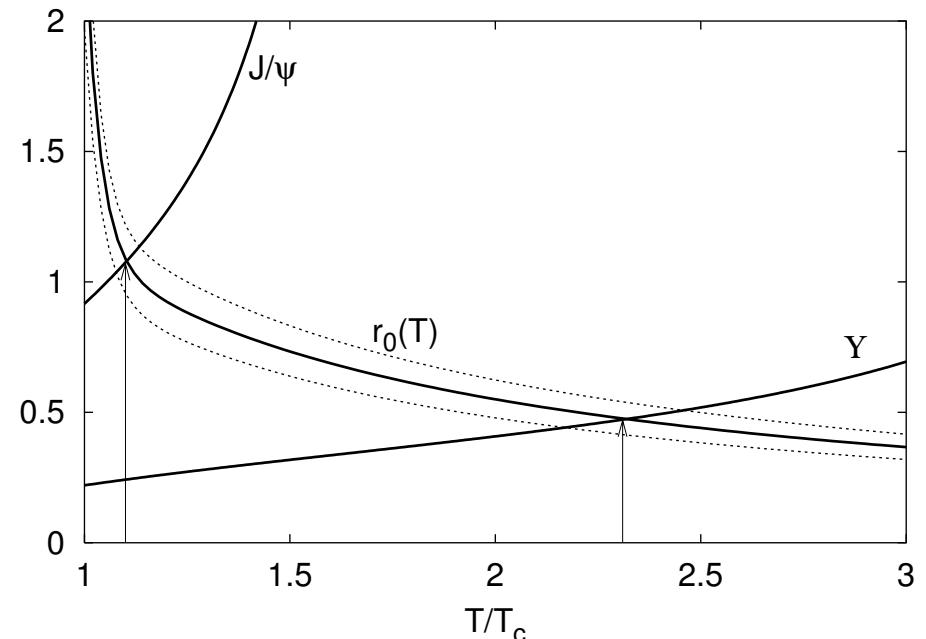
Digal et al., PRD 64 (2001) 75

no  $q\bar{q}$  bound state if

$$r_{q\bar{q}}(T) > r_0(T) \simeq 1/(g(T)T)$$

$r_0$  Debye length in QGP

$\Rightarrow q\bar{q}$  "thermometer" of QGP



Thermal picture ( $n_{partons} = 5.2T^3$  for 3 flavors)

for  $T=500$  MeV:  $n_p \simeq 84/\text{fm}^3$ , mean separation  $\bar{r}=0.2$  fm  $< r_{J/\psi}$

# Models ...implementing Debye screening and more

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## Statistical hadronization model

all charm quarks are produced in primary hard collisions ( $t_{c\bar{c}} \sim 1/2m_c \simeq 0.1 \text{ fm}/c$ )  
...survive and thermalize **in QGP** (thermal, but not chemical equilibrium)  
charmed hadrons are formed at chemical freeze-out together with all hadrons  
“generation” ...no  $J/\psi$  survival in QGP (full screening)

if supported by data,  $J/\psi$  loses status as “thermometer” of QGP  
...and gains status as a powerful observable for the phase boundary

Braun-Munzinger, Stachel, PLB 490 (2000) 196; NPA 789 (2006) 334, PLB 652 (2007) 259

# Models ...implementing Debye screening and more

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## Statistical hadronization model

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Braun-Munzinger, Stachel, PLB 490 (2000) 196; NPA 789 (2006) 334, PLB 652 (2007) 259

## Transport models

implement screening picture with space-time evolution of QGP (hydrodynamics)  
continuous destruction and “(re)generation” (“recombination”)

Thews et al., PRC 63 (2001) 054905 ...

“TAMU”, PLB 664 (2008) 253, NPA 859 (2011) 114, EPJA 48 (2012) 72

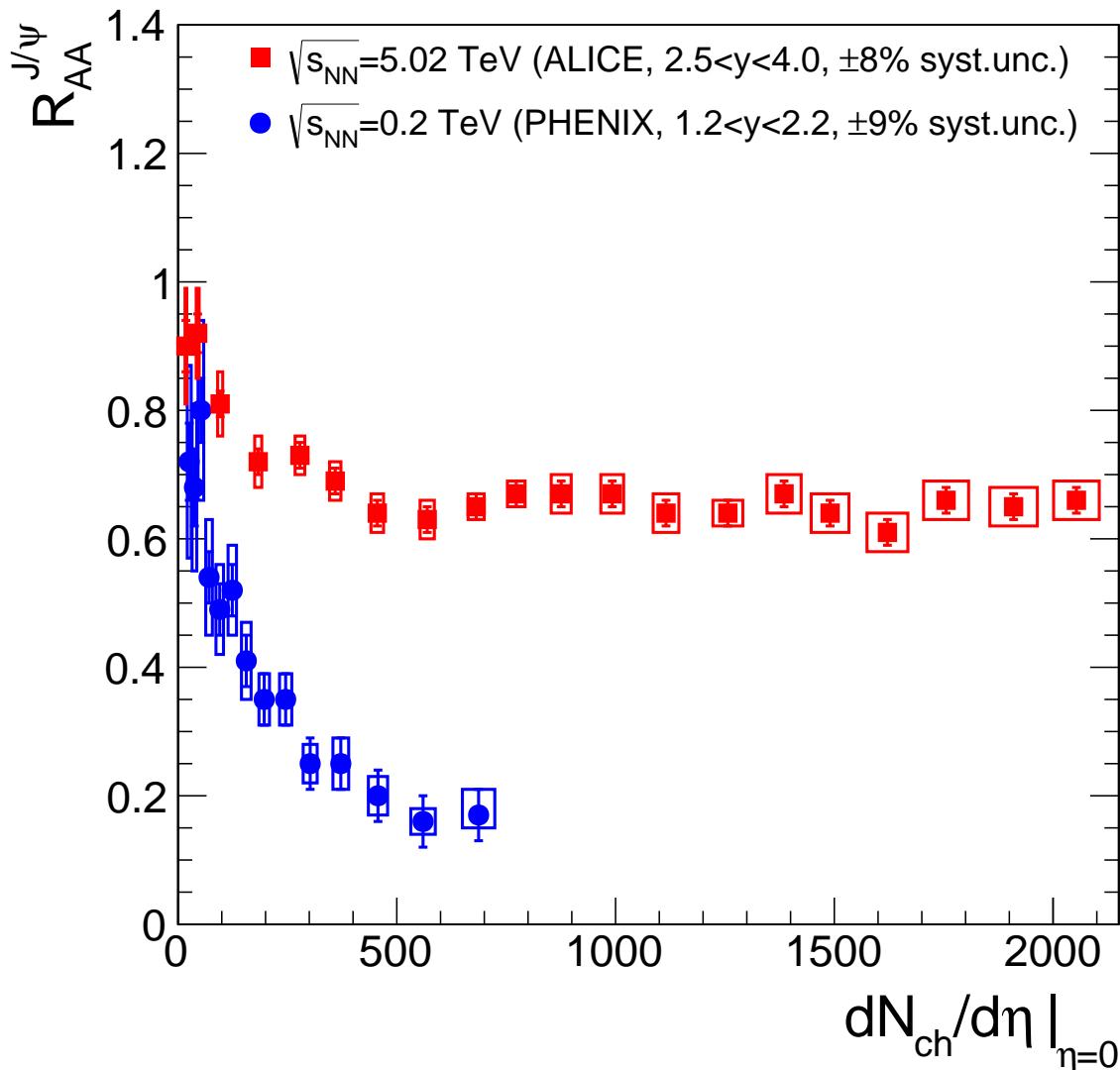
“Tsinghua”, PLB 607 (2005) 107, PLB 678 (2009) 72, PRC 89 (2014) 054911

Strickland, Bazow, NPA 879 (2012) 25

# Charmonium data at RHIC and the LHC

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$$R_{AA} = \frac{dN_{AA}/dp_T dy}{N_{coll} \cdot dN_{pp}/dp_T dy}$$

nuclear modification factor

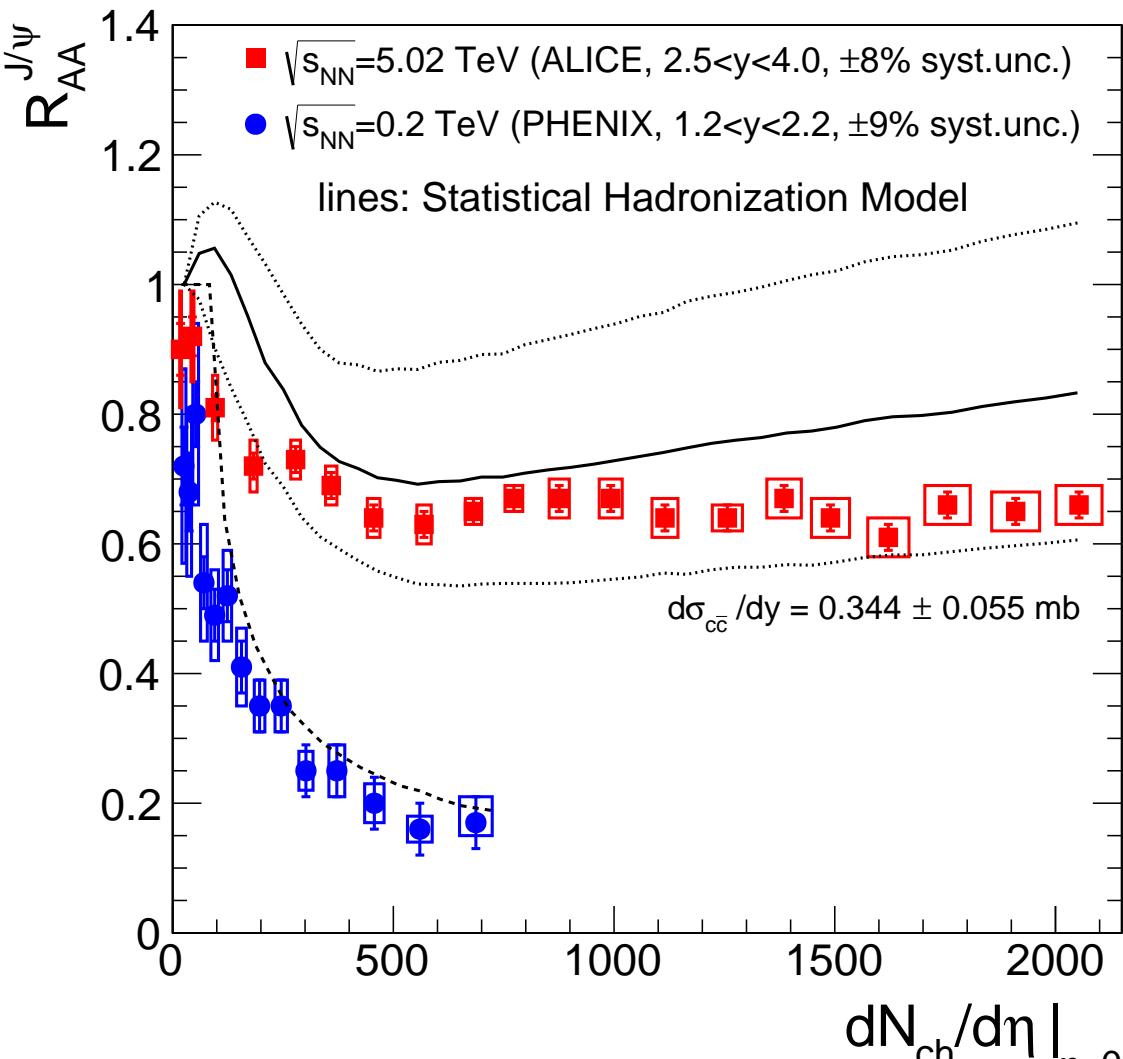
- "suppression" at RHIC (PHENIX)
- dramatically different at the LHC

$dN_{ch}/d\eta \sim \varepsilon$  ( $> 20 \text{ GeV/fm}^3$ , for  $dN_{ch}/d\eta \simeq 2000$ )

# Charmonium data at RHIC and the LHC

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$$dN_{ch}/d\eta \sim \varepsilon (>20 \text{ GeV/fm}^3, \text{ for } dN_{ch}/d\eta \simeq 2000)$$

$$R_{AA} = \frac{dN_{AA}/dp_T dy}{N_{coll} \cdot dN_{pp}/dp_T dy}$$

nuclear modification factor

- "suppression" at RHIC (PHENIX)
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Statistical Hadronization Model

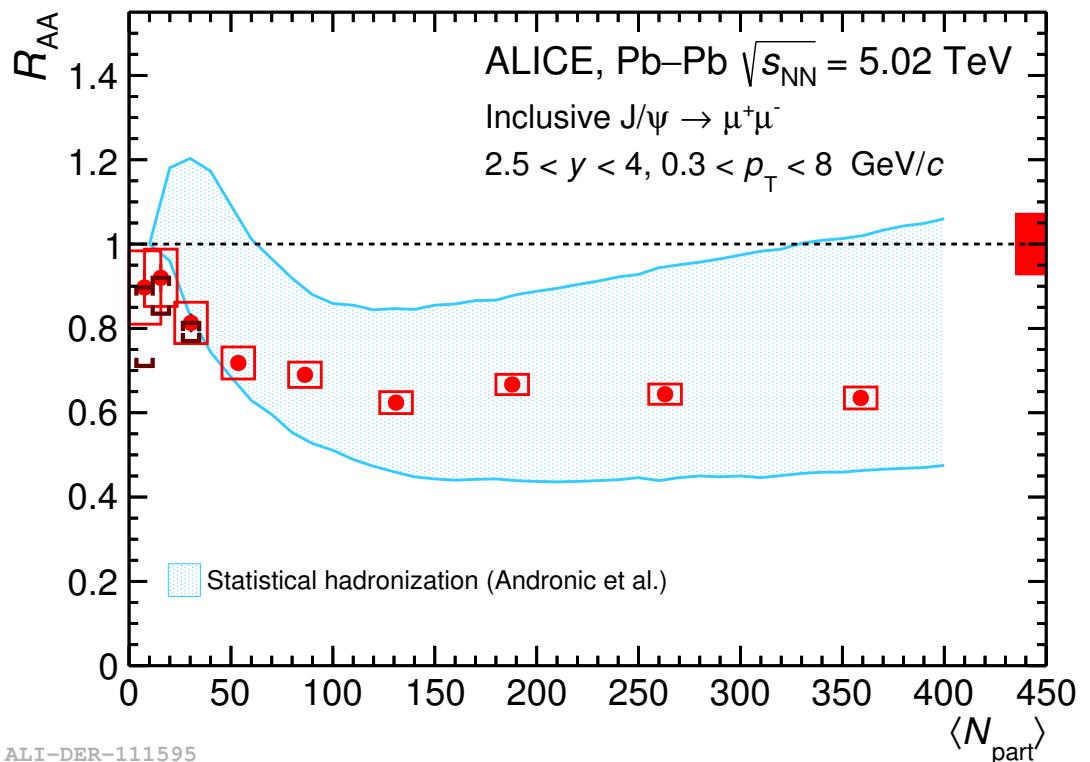
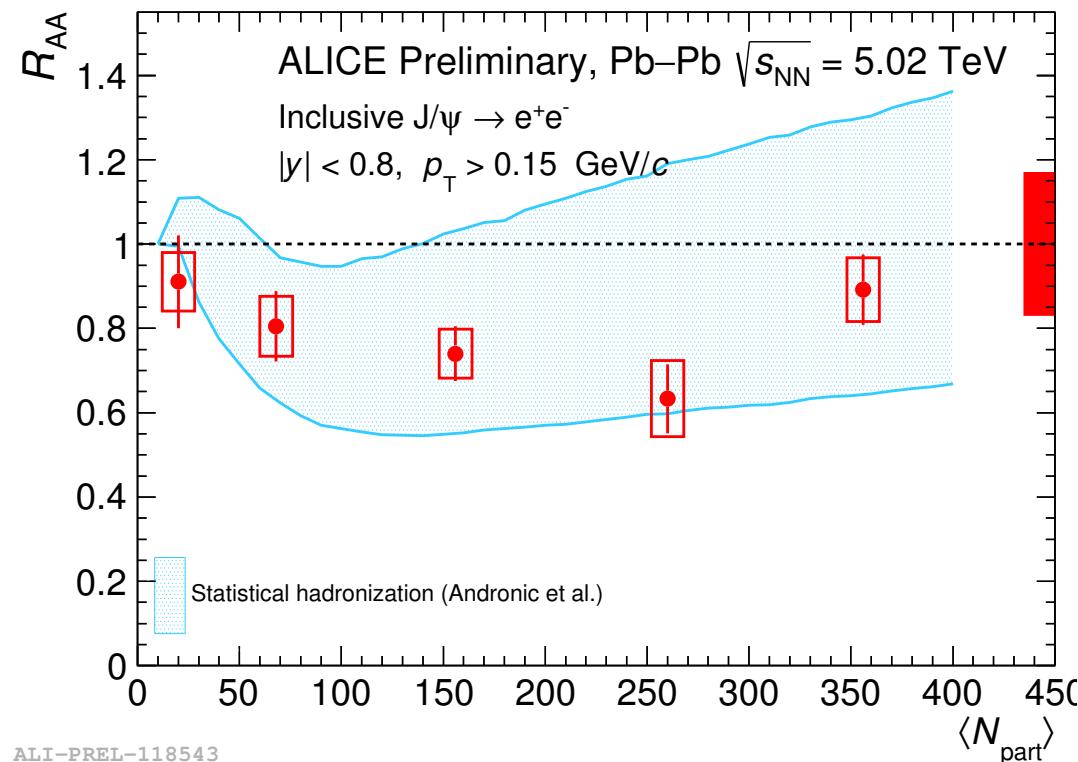
$$N_{J/\psi} \sim (N_{c\bar{c}}^{dir})^2$$

$J/\psi$  is another observable (charm)  
for the phase boundary  
calculations are for  $T=156 \text{ MeV}$

# $J/\psi$ data and the statistical model

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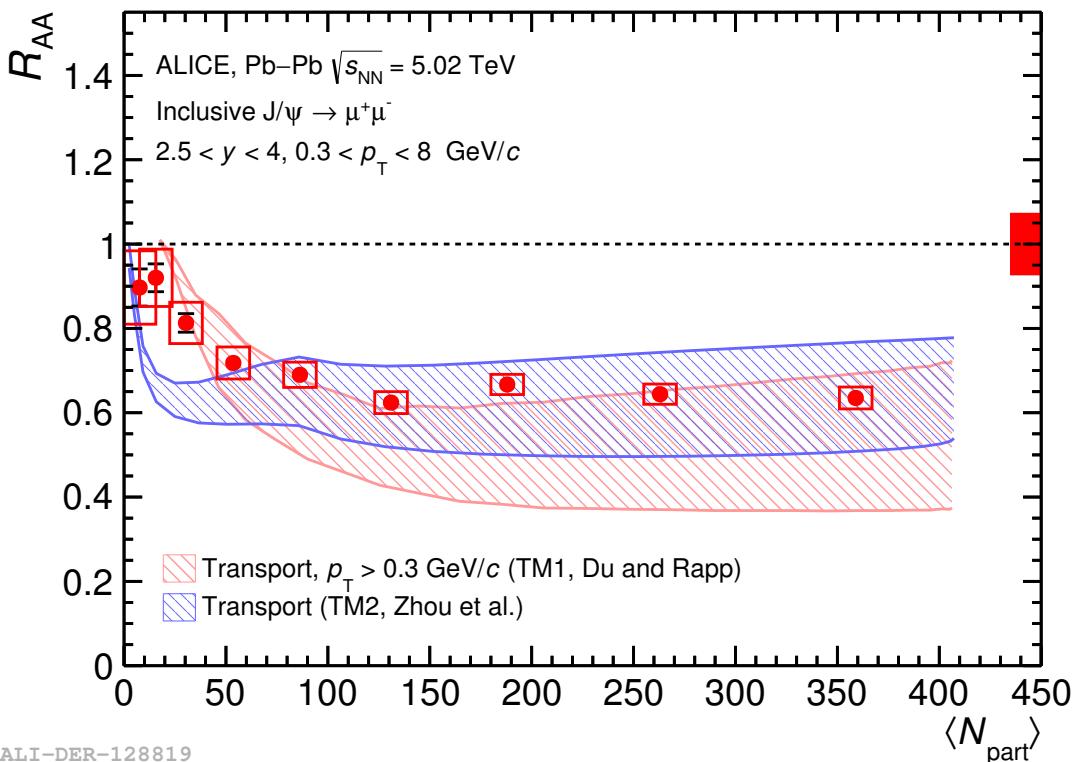
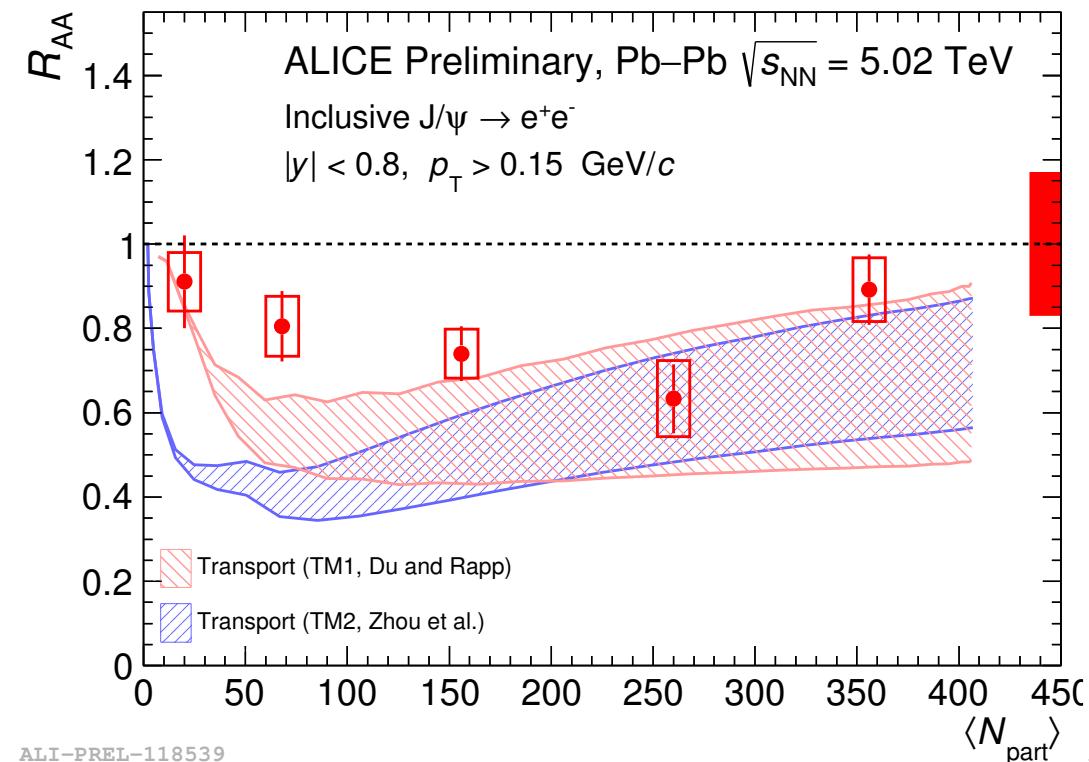
ALICE, PLB 766 (2017) 212

The statistical hadronization model assumes full thermalization of charm quarks, full dissociation of  $J/\psi$  mesons in QGP and formation at the hadronization within this model, the “thermometer” status is lost, but  $J/\psi$  (charm) becomes a remarkable observable for the QCD phase boundary (hadronization)

# J/ $\psi$ data and transport models

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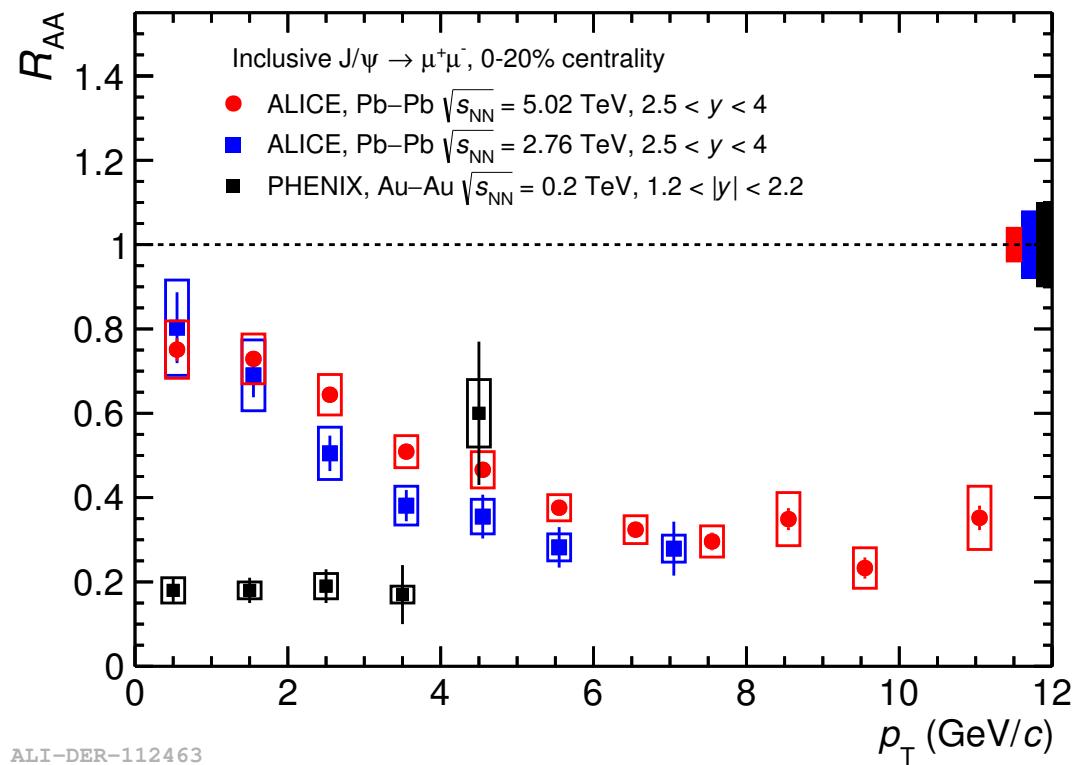
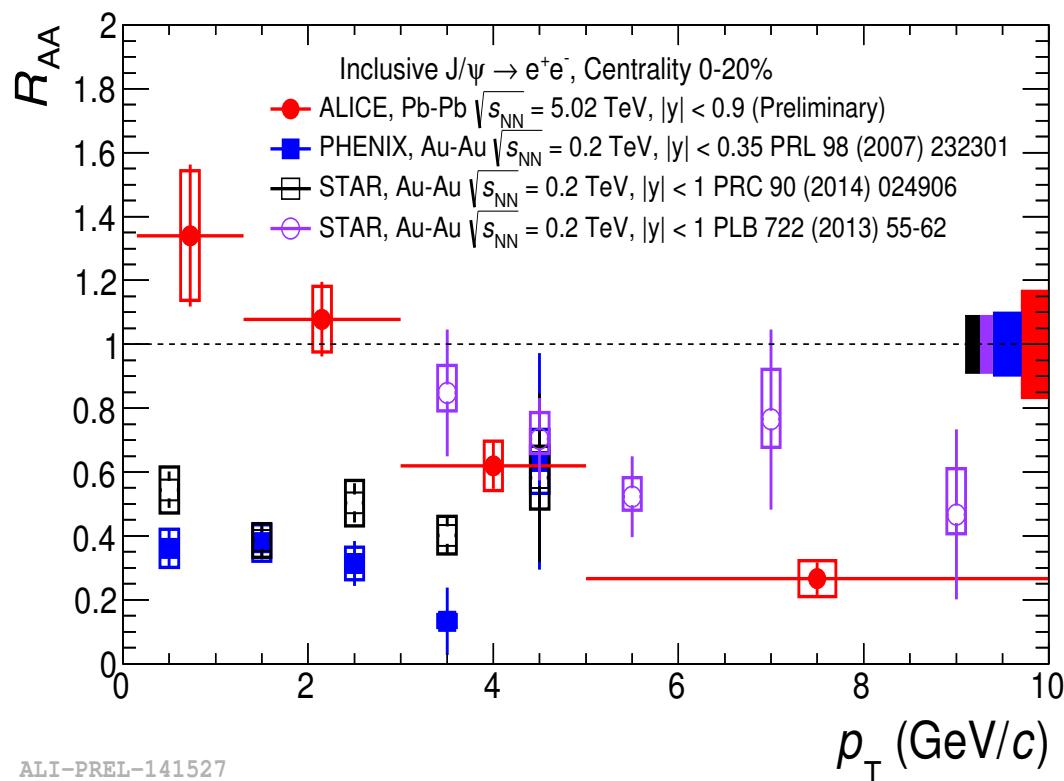
ALICE, PLB 766 (2017) 212

Transport models assume continuous dissociation and formation during the whole lifetime of QGP (time evolution of  $T$  constrained by other measurements)  
(employ smaller uncert. of  $d\sigma_{c\bar{c}}/dy$ )

# $J/\psi$ production vs. $p_T$

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ALICE, JHEP 06 (2015) 055

as expected, (re)generation is a low- $p_T$  phenomenon  
significantly different trend at the LHC compared to RHIC

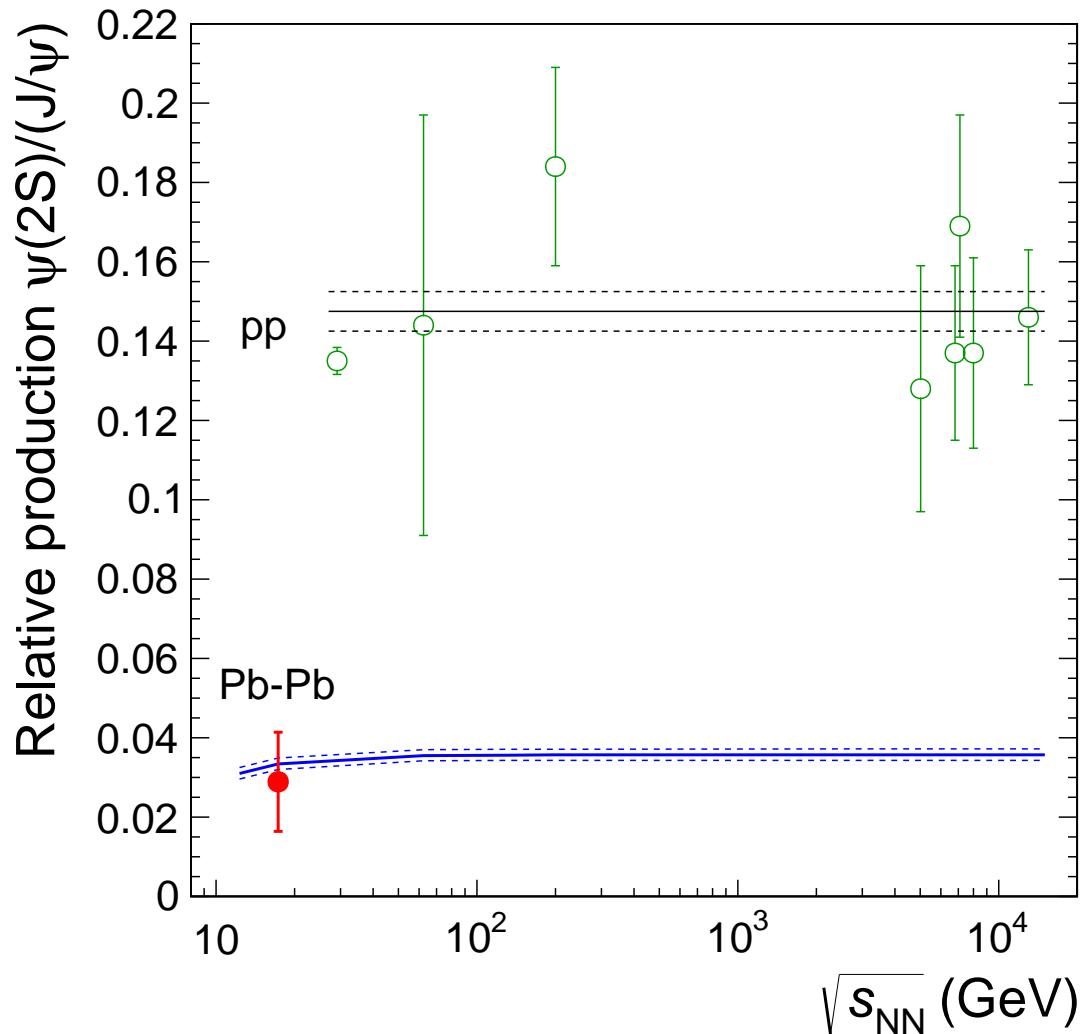
$J/\psi$  at high- $p_T$  suppressed as consequence of charm energy loss in QGP

# Charmonium production

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Production of excited states crucial to investigate ...possible with HL-LHC



statistical description, [arXiv:1710.09425](https://arxiv.org/abs/1710.09425) ...transport models predict larger relative production

# Summary

- in nucleus-nucleus collisions we create a (small:) chunk of the hot early Universe
  - ...a highly-dynamic and collective system; we measure observables for various stages
- measured energy densities are well above the values expected for deconfinement
- collective flow (developed early in the deconfined stage) described by hydrodynamics; allows extraction of  $\eta/s$
- abundance of hadrons with light quarks consistent with chemical equilibration
  - the thermal model provides a simple way to access the QCD phase boundary
  - ...but is it more than a 1st order description (of loosely-bound objects)?
  - ...and what fundamental point does it make about hadronization?
- we see (re)combination of charm quarks at the LHC ...either over the full history of QGP or at the phase boundary
  - ...conclusion expected with the ALICE upgrade (HL-LHC, 2021-2029)
- some of the features in heavy-ion collisions are observed in high-multiplicity pp and p-Pb collisions
- *not shown but available in spare slides*
  - we measure strong jet quenching (parton energy loss) in quark-gluon matter
  - jet quenching data (for light and heavy-flavor hadrons) described by theoretical models; allows extraction of transport coefficients (in range  $T = (1 - 3)T_c$ )

# Additional slides

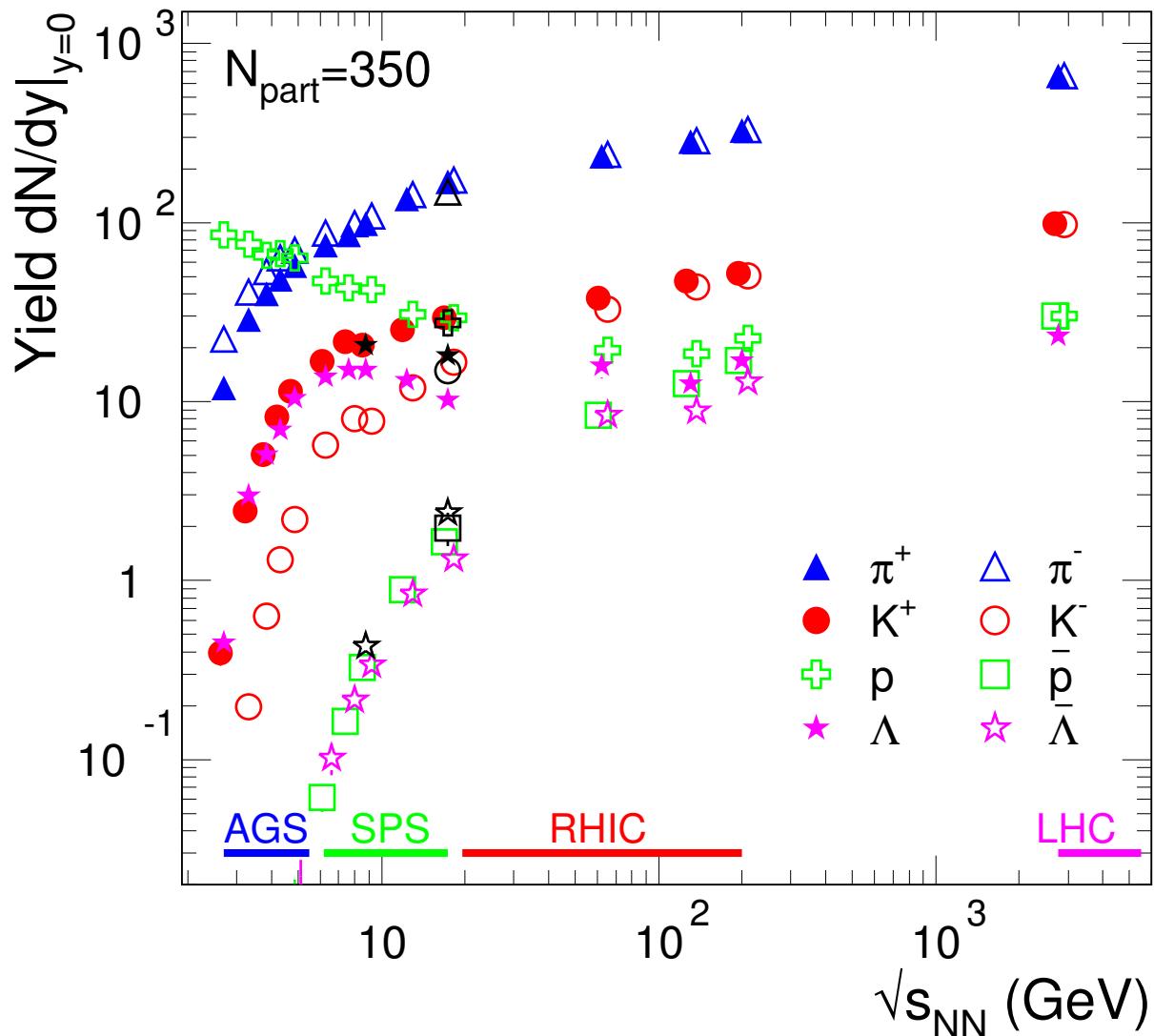
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# Overview of hadron production

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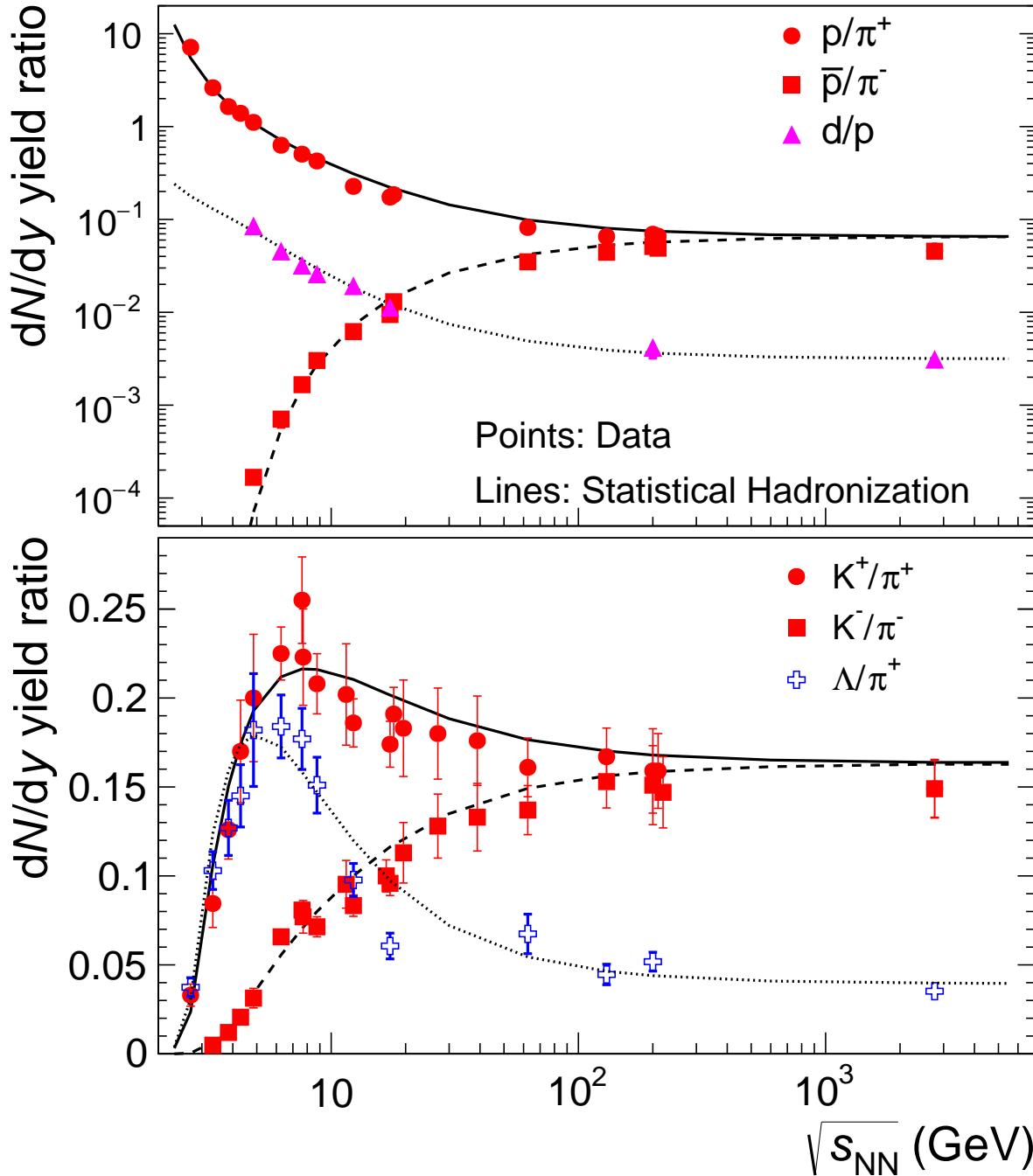
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- lots of particles, mostly newly created ( $m = E/c^2$ )
- a great variety of species:  
 $\pi^\pm$  ( $u\bar{d}, d\bar{u}$ ),  $m=140$  MeV  
 $K^\pm$  ( $u\bar{s}, \bar{u}s$ ),  $m=494$  MeV  
 $p$  ( $uud$ ),  $m=938$  MeV  
 $\Lambda$  ( $uds$ ),  $m=1116$  MeV  
also:  $\Xi(dss)$ ,  $\Omega(sss)$ ...
- mass hierarchy in production ( $u, d$  quarks: remnants from the incoming nuclei)

# The grand (albeit partial) view at hadron production

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Data:

AGS: E895, E864, E866,  
E917, E877

SPS: NA49, NA44

RHIC: STAR, BRAHMS

LHC: ALICE

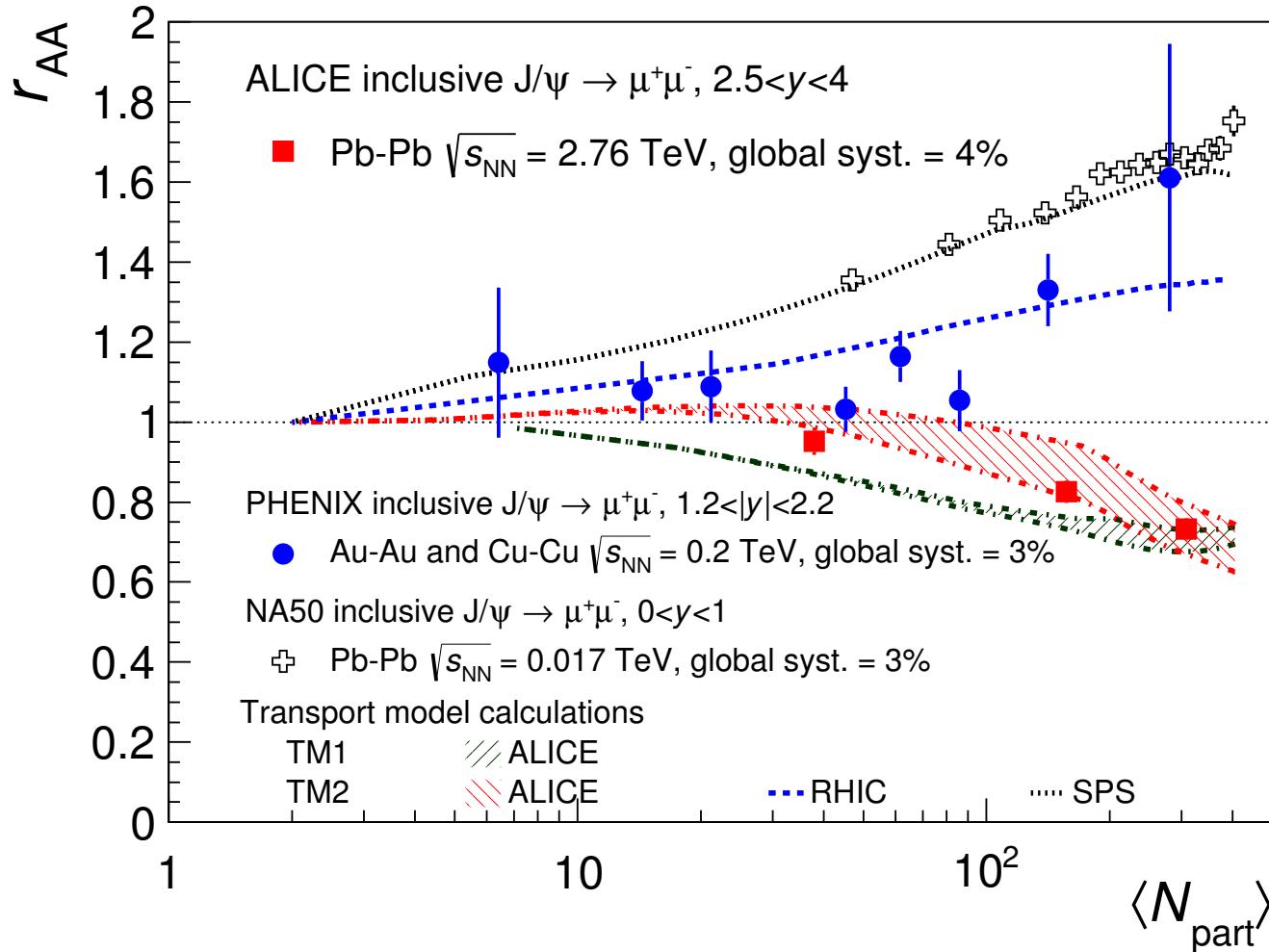
NB: no contribution from weak decays

data consistent with smooth behaviour vs. energy

# Mean transverse momentum of $\text{J}/\psi$ mesons

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$$r_{AA} = \frac{\langle p_T^2 \rangle_{AA}}{\langle p_T^2 \rangle_{pp}}$$

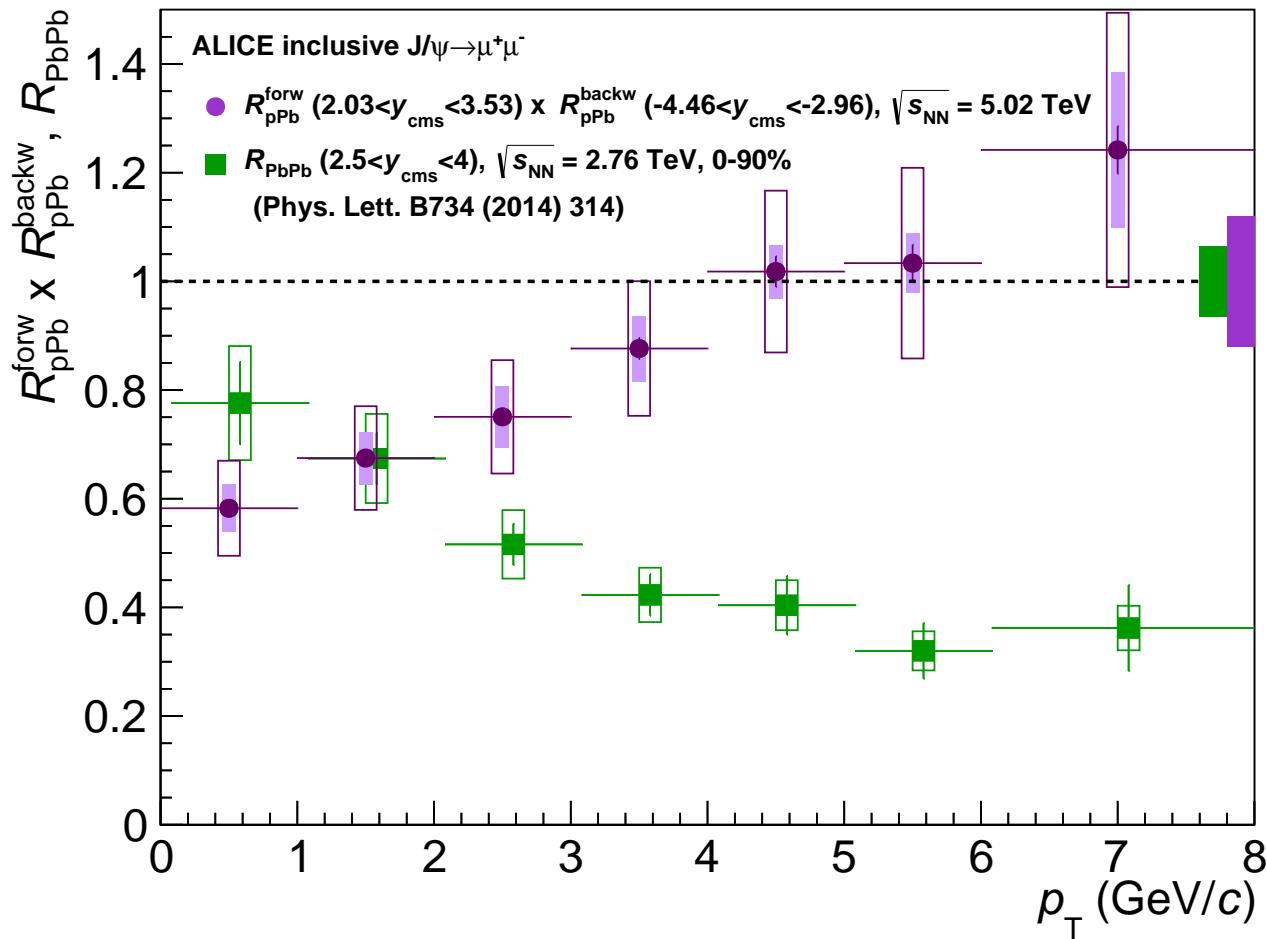
ALICE, JHEP 05 (2016) 179

softening of  $p_T$  is significant at the LHC, clear indication of (re)generation thermalization of charm quarks demonstrated by collective flow of D and  $\text{J}/\psi$

# $\text{J}/\psi$ production vs. $p_{\text{T}}$

A. Andronic - ALICE

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ALICE, JHEP 06 (2015) 055

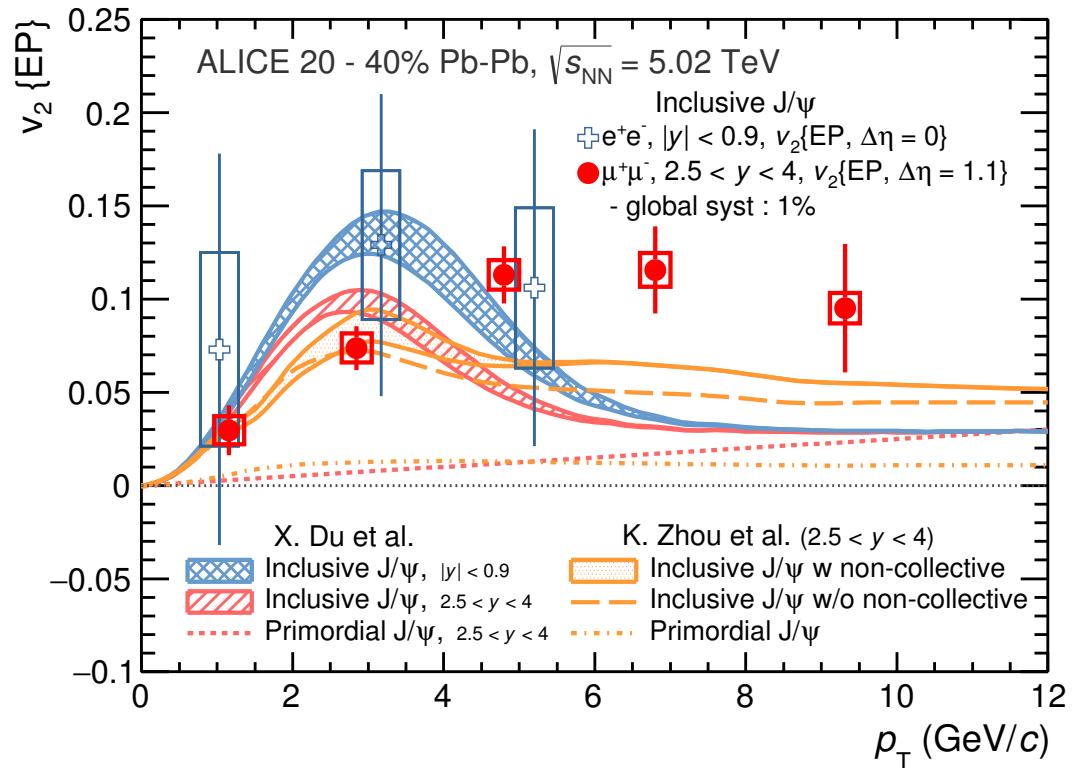
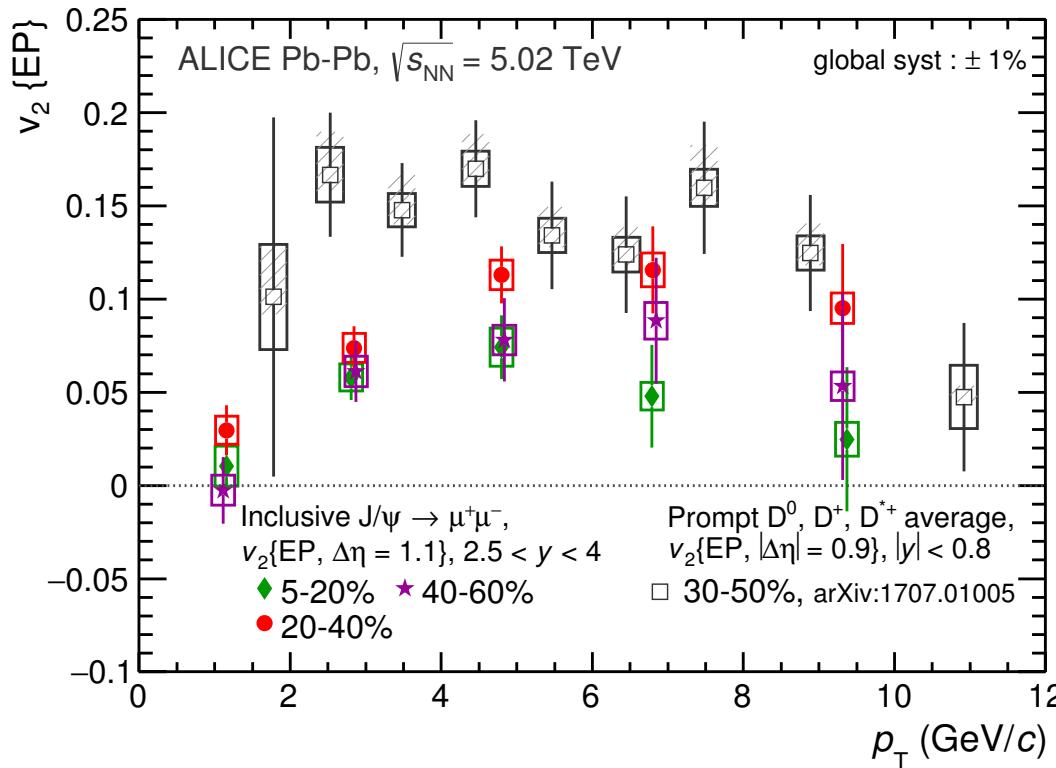
Distinct differences between Pb–Pb and p–Pb; crucial support that low- $p_{\text{T}}$   $\text{J}/\psi$  are from (re)generation (while at high- $p_{\text{T}}$  outcome of charm energy loss in QGP)

for mid-rapidity: Run 1 data stat.-limited; Run 2 data will bring significance

# J/ $\psi$ and D mesons exhibit collective flow

A. Andronic - ALICE

5



ALICE, PRL 119 (2017) 242301

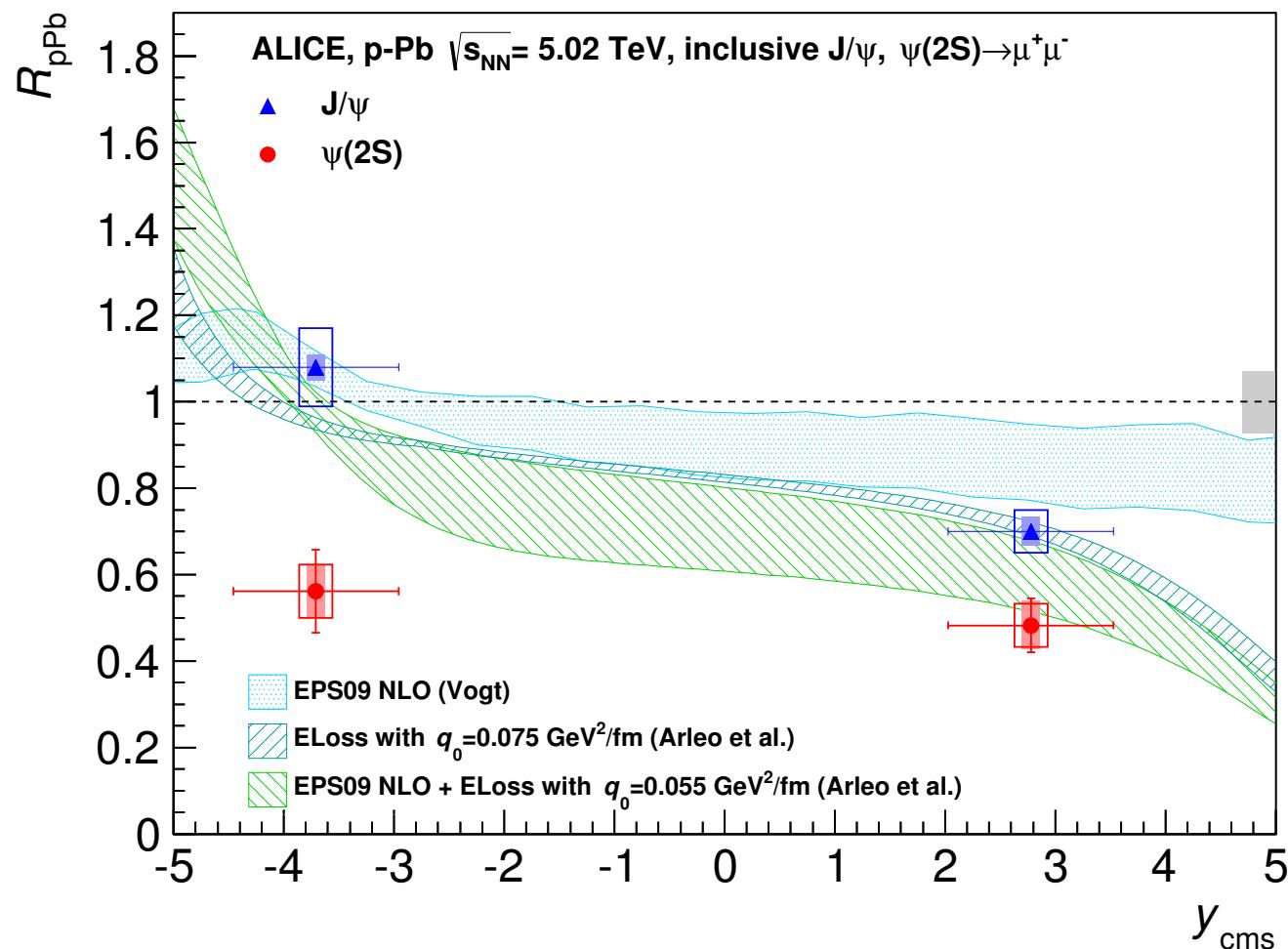
Implies thermalization of charm quarks ...full thermalization? (high- $p_T$ ?)

...and how to make distinction between statistical and dynamical production?

# Charmonium production in p–Pb collisions

A. Andronic - ALICE

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ALICE, [JHEP 12 \(2014\) 073](#)

(at least in first order) models give same result for  $\psi(2S)$  as for  $J/\psi$  in data, difference predominantly at low  $p_T$

# Probing early stages

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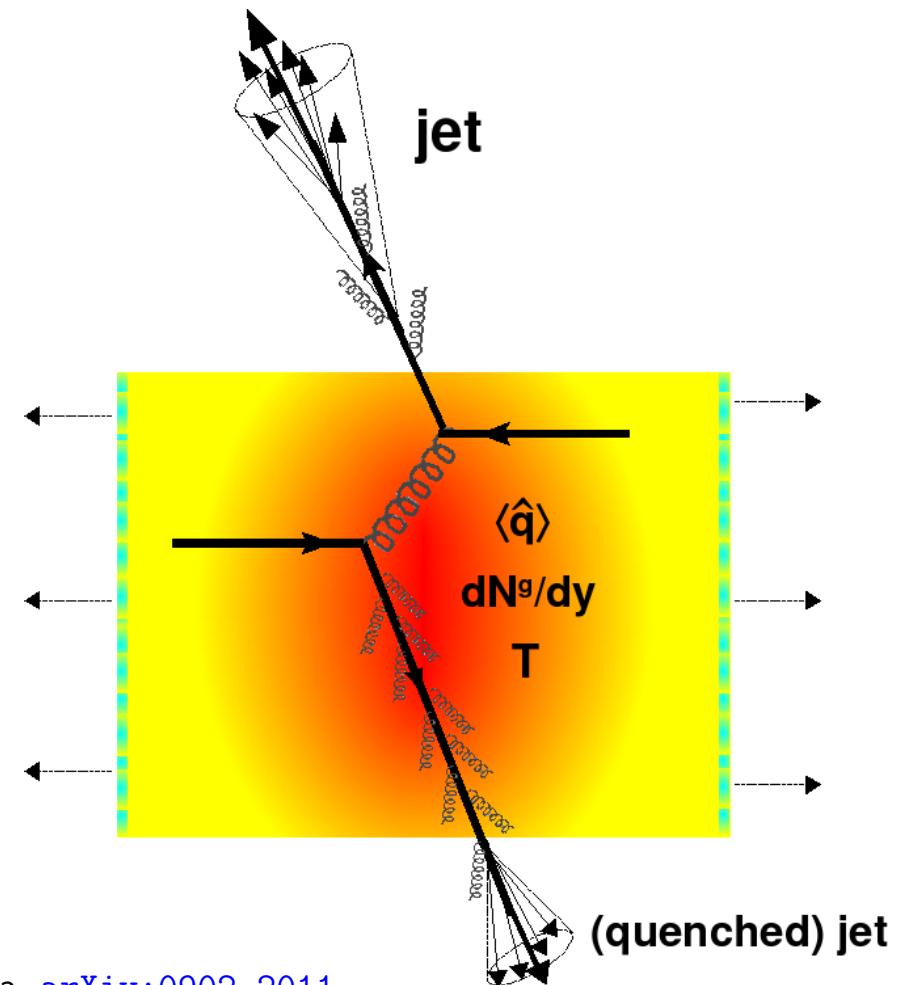
...with "hard probes" ( $m \gg T$ ): jets or high- $p_T$  hadrons (or heavy quarks)  
produced very early in the collision,  $t \simeq 1/m$   
(jets - sprays of hadrons from high-speed quarks)

- $q, \bar{q}, g$  travel through QGP, lose energy
- hadronize (neutralize color picking up partners from the vacuum)
- hadrons fly towards detectors

...where we observe a deficit at high momenta ( $p_T$ ): "jet quenching"  
(Bjorken, [FERMILAB-PUB-82-059-T](#) )

quantified by the nuclear modification factor:

$$R_{AA} = \frac{dN_{AA}/dp_T dy}{N_{coll} \cdot dN_{pp}/dp_T dy}$$



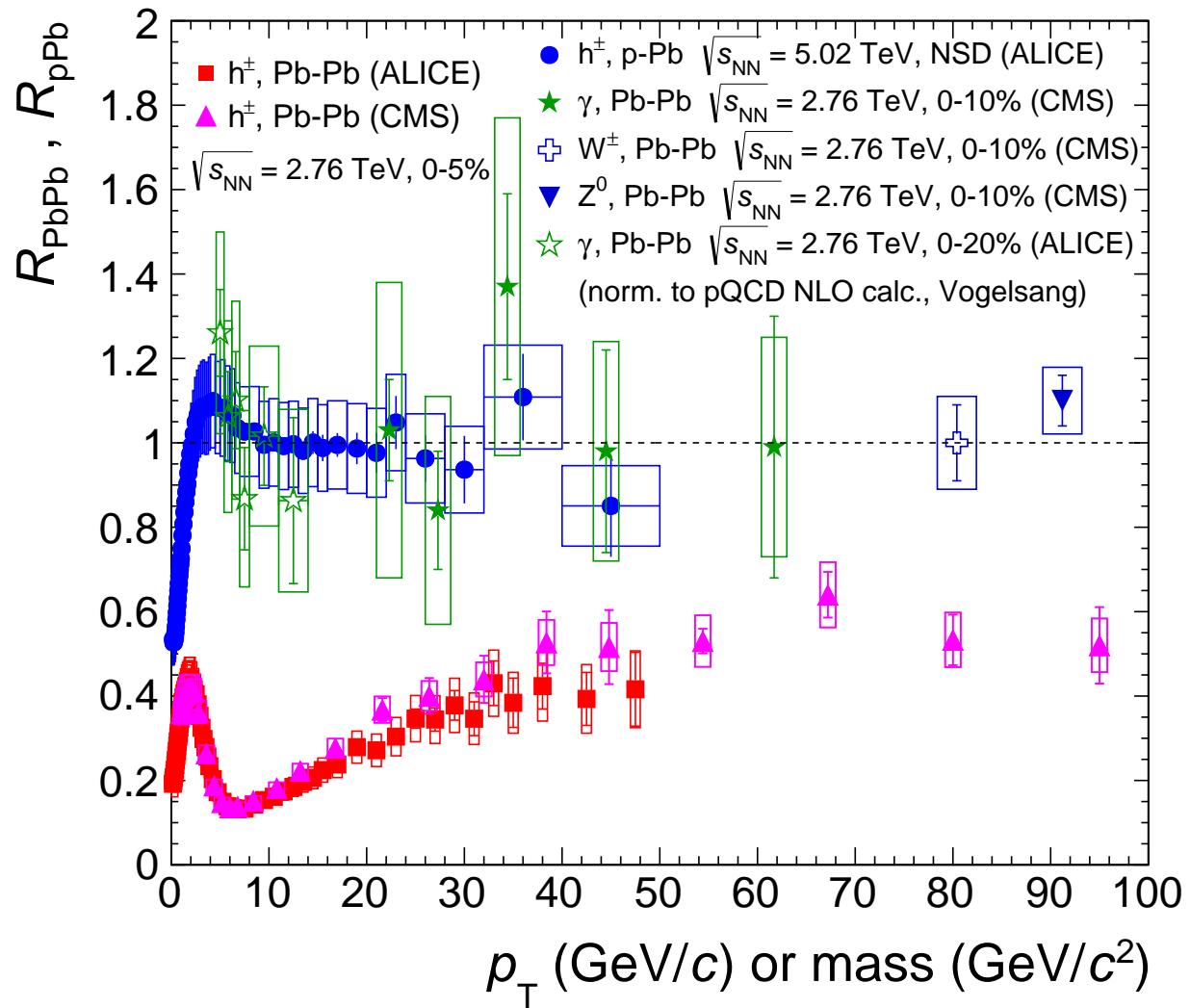
D. d'Enterria, [arXiv:0902.2011](#)

# Jet quenching at the LHC

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...measured with "leading hadrons" ( $h^\pm$ )  
(carry largest fraction of parton  $p_T$ )



a thermal component,  $p_T \lesssim 6 \text{ GeV}/c$  (scaling with  $N_{\text{part}}$ ) determined by gluon saturation and collective flow

strong suppression, reaching a factor of  $\sim 7$ ,  $p_T \simeq 7 \text{ GeV}/c$

...not seen with EW observables  
( $\gamma, W^\pm, Z^0$ ) ...ALICE  $\gamma$  / pQCD NLO calc.

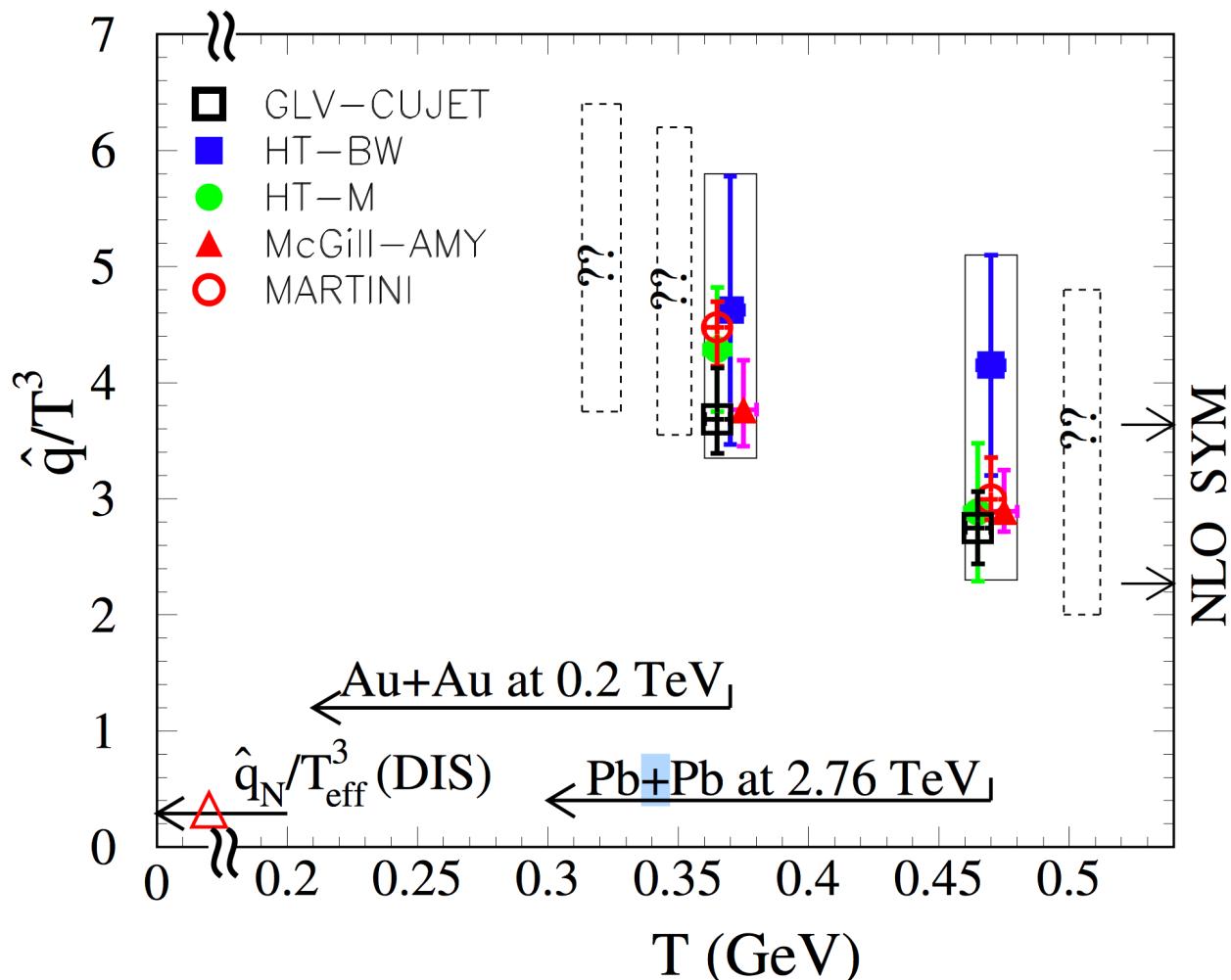
not seen in p-Pb collisions  
( $p_T \lesssim 3 \text{ GeV}/c$ , gluon saturation)

ALICE, EPJ C 74 (2014) 3054 and refs.  
therein

# Jet quenching: transport coefficient

A. Andronic - ALICE

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An initial quark with energy of 10 GeV at the center of a most-central A–A collision

JET Collab., PRC 90 (2014) 014909

transport coefficient:

$$\hat{q} = d\langle p_T^2 \rangle / dx$$

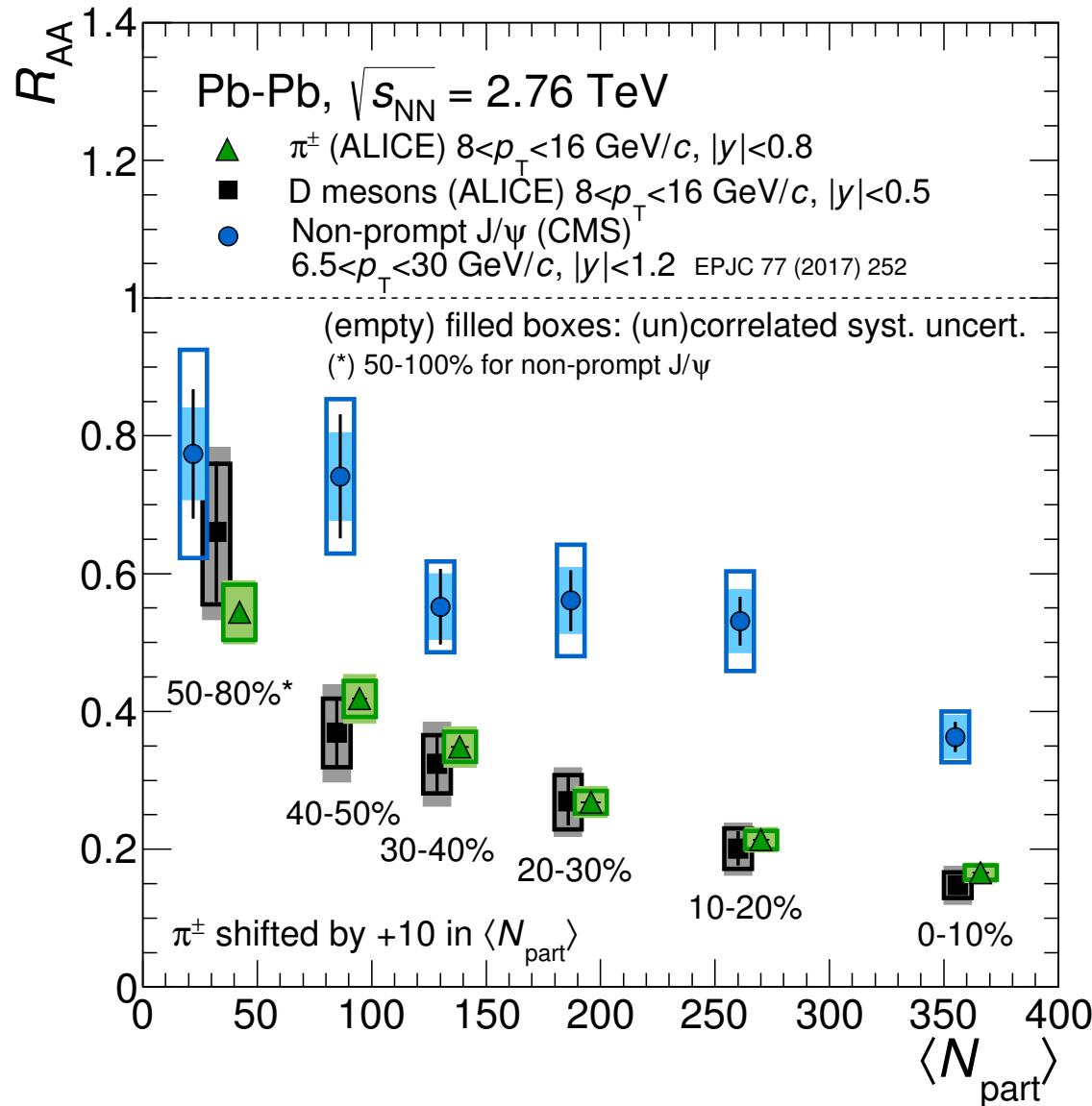
(proportional to gluon density)

The data of Run 2 (about to be published) are significantly more precise

# In-medium energy loss as a function of quark mass

A. Andronic - ALICE

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D mesons are as much suppressed as pions at high  $p_T$

...is expected ordering vs. quark mass

$$\Delta E_b < \Delta E_c < \Delta E_{u,d,s} < \Delta E_g$$

established in data?

(naively:  $\Delta E \sim 1 - R_{AA}$ )

to some extent, yes

JHEP 11 (2015) 205

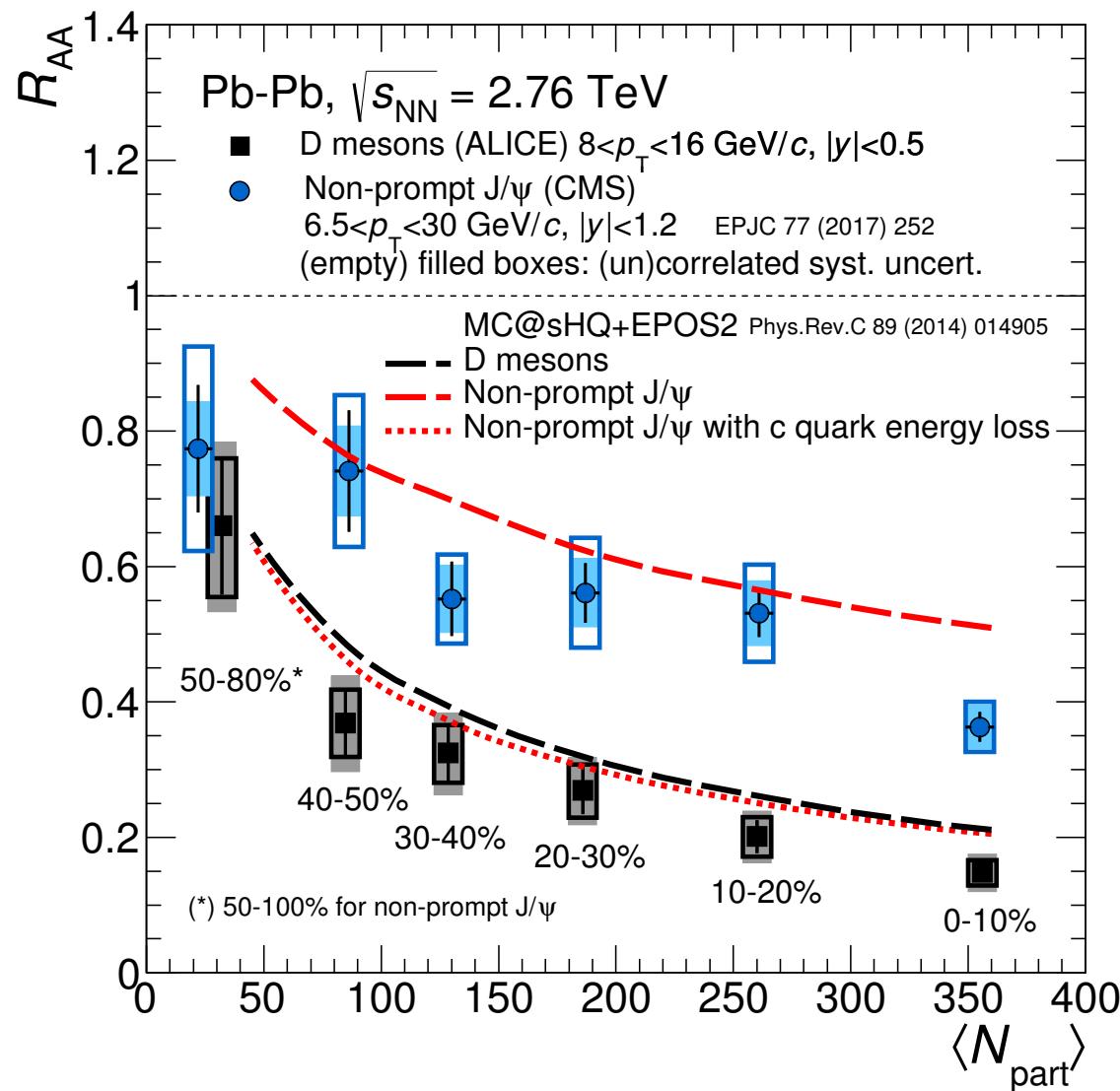
ALICE-PUBLIC-2017-004

on-going effort: determine heavy quark (momentum) diffusion coefficient  
...calculable in lattice QCD Banerjee et al., Phys. Rev. D 85 (2012) 014510

# In-medium energy loss as a function of quark flavor

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Theoretical model(s) reproduce the data (reasonably) well

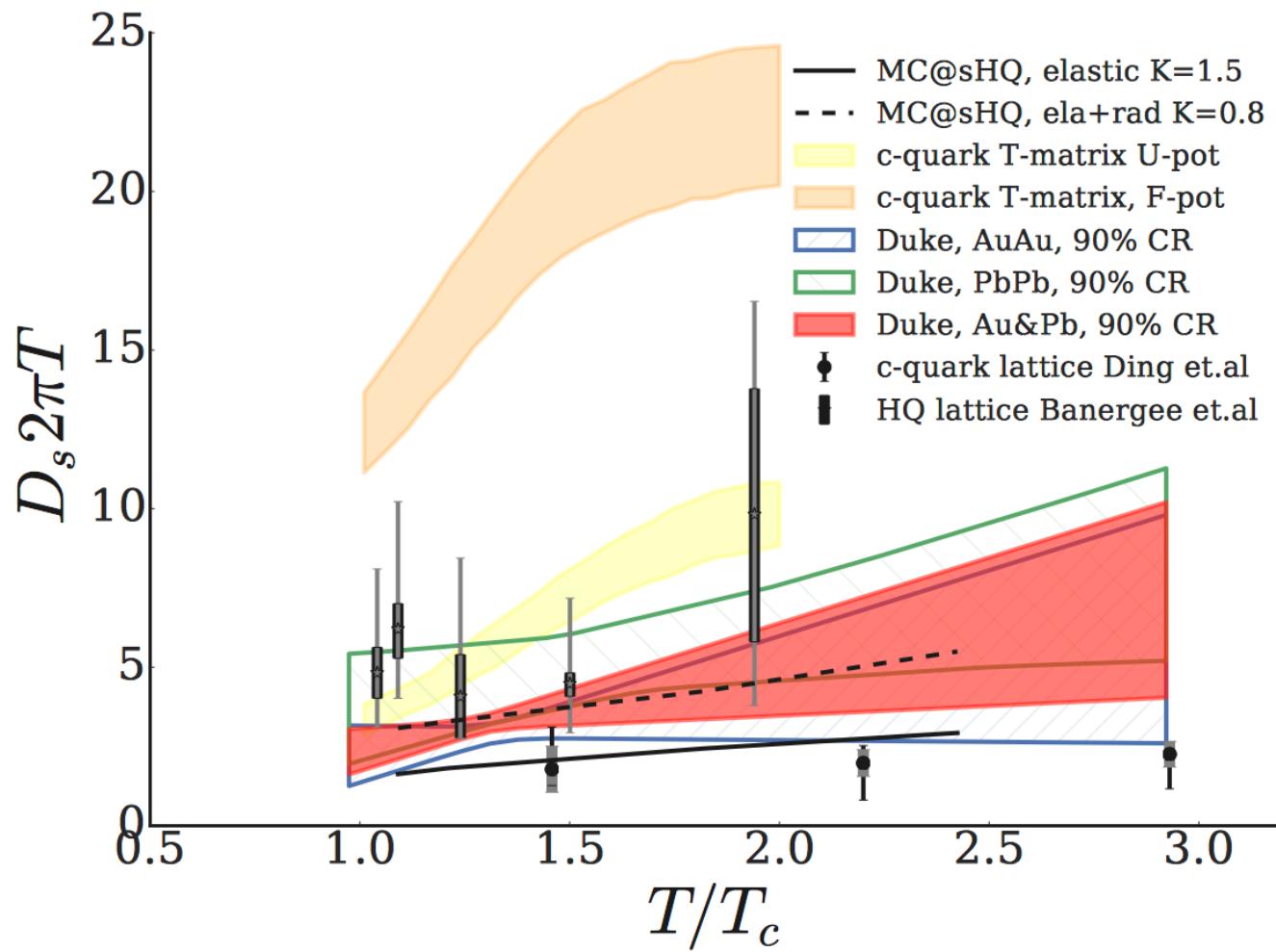
JHEP 11 (2015) 205

ALICE-PUBLIC-2017-004

# Charm diffusion coefficient

A. Andronic - ALICE

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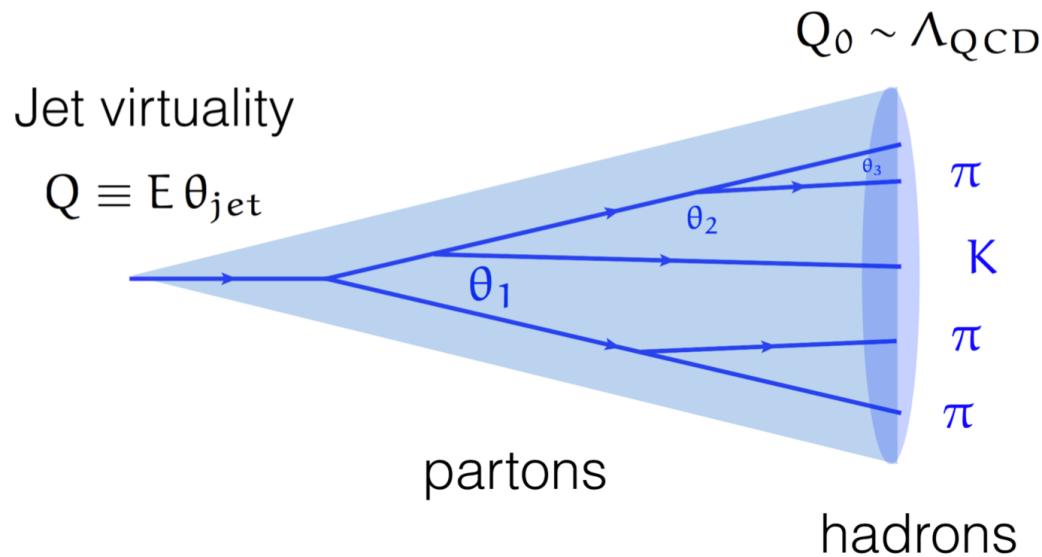
heavy quark spatial diffusion coefficient  $D_s = 4T^2/\hat{q}$

# Jets

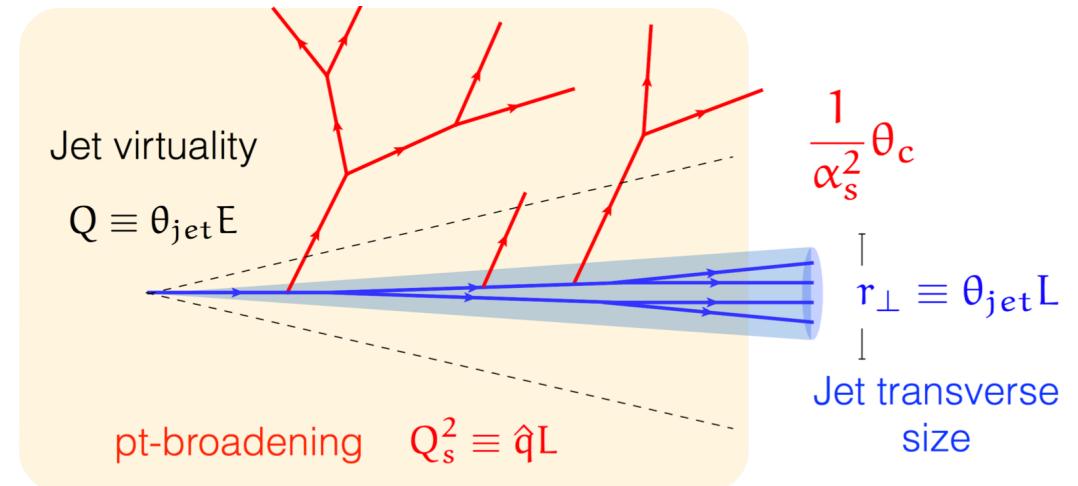
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...in vacuum



...in medium



$E$ :  $E_T$  or  $p_T$ ;  $\theta_{jet}$ : opening angle ( $R$  or  $\Delta R$ )

Y. Mehtar-Tani, [arXiv:1602.01047](https://arxiv.org/abs/1602.01047)

# Advantage of heavy quarks

Their mass,  $m_c \simeq 1.2$  GeV,  $m_b \simeq 4.6$  GeV, is much larger than  $T$   
(so we are sure they do not originate in thermal processes ...but pQCD processes)

Are produced in pairs ( $c\bar{c}$ ) in initial hard collisions ( $t \sim 1/(2m_c) \leq 0.1$  fm/c)

Their identity (flavor) is assured to be preserved from early times of production  
throughout the QGP phase (until hadronization:  $c \rightarrow D$ ;  $b \rightarrow B$ )

*Expectation:*

Due to high mass the gluon radiation by HQ is suppressed at small angles  
this is called "the dead-cone effect"

Consequence: hierarchy in energy loss:

$$\Delta E_b < \Delta E_c < \Delta E_{u,d,s} < \Delta E_g$$

At the LHC, there are about 100  $c\bar{c}$  pairs produced in a central Pb–Pb collisions  
(not all are measurable, though)