Transport Theory for Energetic Nuclear Reactions

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56th International Winter Meeting on Nuclear Physics

Bormio (Italy), January 22 - 26, 2018



Outline



- Basics
- Types of Transport Models
- 2 Successes & Failures
 - *E*₀/*A* at *ρ* > *ρ*₀
 - $S(\rho)$ from π^-/π^+
- 3 Comparison Project
 - Code Comparison Effort
 - Full-Run Comparisons
 - Box Comparisons
- 4 TuQMD Example
- 5 Conclusions



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Comparison Project

TuQMD Example

Conclusions

Need for Transport

Many repeated elementary interactions

- Central Nuclear Collisions
- Isotope Production
- Energetic Hadron-Nucleus Collision
- ν Detection
- Technological Applications

• ...



Degrees of Freedom

Choice depends on energy and application

- Nucleons
- Clusters
- Pions, Baryon Resonances
- Kaons, Strange Baryons
- Photons



Neutron Proton Pion

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Dominant degrees of freedom <u>must</u> be included; other may be treated perturbatively.

Phase-space distribution (in configuration space and momentum) ⇔ Wigner function

$$f(\mathbf{p};\mathbf{R},T) = \int d\mathbf{r} \,\mathrm{e}^{-i\mathbf{p}\mathbf{r}} \langle \hat{\psi}_{H}^{\dagger}(\mathbf{R}-\mathbf{r}/2,T) \,\hat{\psi}_{H}(\mathbf{R}+\mathbf{r}/2,T)
angle$$



Statistical Description

Phase-space distribution

$$f(\mathbf{p};\mathbf{R},T) = \int d\mathbf{r} \,\mathrm{e}^{-i\mathbf{p}\mathbf{r}} \langle \hat{\psi}_{H}^{\dagger}(\mathbf{R}-\mathbf{r}/2,T) \,\hat{\psi}_{H}(\mathbf{R}+\mathbf{r}/2,T) \rangle$$

Dynamics: Particles move through noisy medium: stochastic + deterministic impact of the medium on the particle - collisions + mean field

Descriptions invoke Boltzmann equation:

$$\frac{\partial f}{\partial t} + \frac{\partial \epsilon}{\partial \boldsymbol{p}} \frac{\partial f}{\partial \boldsymbol{r}} - \frac{\partial \epsilon}{\partial \boldsymbol{r}} \frac{\partial f}{\partial \boldsymbol{p}} = \mathcal{K}^{<} (1 \mp f) - \mathcal{K}^{>} f$$

Left-hand deterministic impact

Right-hand stochastic









Transport for Reactions

Introduction

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Means of Learning on EOS at $\rho > \rho_0$



Transport for Reactions

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- Boltzmann Equation Type
 - Examples: GIBUU, IBUU, pBUU, RVUU
 - Pros: Well-defined equation, derivable from microscopic theory, solved; easy Pauli principle & mean-field
 - Cons: No fluctuations
- Molecular Dynamics
 - Examples: IQMD, CoMD, TuQMD, UrQMD
 - Pros: Good fluctuations late in reactions
 - Cons: Wrong fluctuations initially, troubles with Pauli & mean-field, too much phenomenology?
- Antisymmetrized Molecular Dynamics (AMD)
 - Pros: Excellent initial states, good mean field & Pauli
 - Cons: Troubles with final states, dose of phenomenology



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EOS in Central Reactions

Reaction plane: plane in which the centers of initial nuclei lie Spectators: nucleons in the reaction periphery, little disturbed by the reaction

Participants: nucleons that dive into compressed excited matter

Nuclear EOS deduced from the features of collective flow in reactions of heavy nuclei

Collective flow: motion characterized by significant space-momentum correlations, deduced from momentum distributions of particles emitted in the reactions

Euler eq. in $\vec{v} = 0$ frame:

$$m_N
ho rac{\partial}{\partial t} \, ec{v} = -ec{
abla}
ho$$



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EOS and Flow Anisotropies

EOS assessed through reaction plane anisotropies characterizing particle collective motion

Hydro? Euler eq. in $\vec{v} = 0$ frame: $\left| m_N \rho \frac{\partial}{\partial t} \vec{v} = -\vec{\nabla} \rho \right|$

where *p* - pressure. From features of *v*, knowing Δt , we may learn about *p* in relation to ρ . Δt fixed by spectator motion

For high *p*, expansion rapid and much affected by spectators

For low *p*, expansion sluggish and completes after spectators gone

Simulation by Shi (pBUU)





Sideward Flow Systematics

Deflection of forwards and backwards moving particles away from the beam axis, within the reaction plane

Au + Au Flow Excitation Function

Note: K used as a label

PD, Lacey & Lynch (pBUU)

The sideward-flow observable results from dynamics that spans a ρ -range varying with the incident energy



Successes & Failures 000000000000

TuQMD Example

2nd-Order or Elliptic Flow

Another anisotropy, studied at midrapidity: $v_2 = \langle \cos 2\phi \rangle$, where ϕ is azimuthal angle relative to reaction plane





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Au+Au V2 Excitation Function





Subthreshold Meson (K/ π) Production



Ratio of kaons per participant nucleon in Au+Au collisions to kaons in C+C collisions vs beam energy

filled diamonds: KaoS data

open symbols: theory Fuchs *et al*

Kaon yield sensitive to EOS because multiple interactions needed for production, testing density The data suggest a relatively soft EOS



Comparison Project

TuQMD Example

Conclusions

Constraints from Flow on EOS

Au+Au flow anisotropies: $\rho \simeq (2 - 4.6)\rho_0$. No one EOS yields both flows right. Discrepancies: inaccuracy of theory Most extreme models for EOS can be eliminated





PD, Lacey & Lynch + Fuchs + Hong + others

Neutron Matter:

Uncertainty in symmetry energy



Pions as Probe of High- ρ Symmetry Energy B-A Li PRL88(02)192701: $S(\rho > \rho_0) \Rightarrow n/p_{\rho > \rho_0} \Rightarrow \pi^-/\pi^+$



Dedicated Experimental Efforts

SAMURAI-TPC Collaboration (data taken; 8 countries and 43 researchers): comparisons of near-threshold π^- and π^+ and also *n-p* spectra and flows at RIKEN, Japan. NSCL/MSU, Texas A&M U Western Michigan U, U of Notre Dame GSI, Daresbury Lab, INFN/LNS U of Budapest, SUBATECH, GANIL China IAE, Brazil, RIKEN, Rikkyo U Tohoku U, Kvoto U

LAMPS TPC at RAON (S Korea): triple GEM, 3π sr





Introduction

Successes & Failures

Comparison Project

TuQMD Example

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Conclusions

FOPI Au+Au π^-/π^+ Data?

Reisdorf et al. (FOPI) NPA781(07)459



Circumstantial Evidence for a Soft Nuclear Symmetry Energy at Suprasaturation Densities



FOPI π^-/π^+ Reproduced by pBUU spectively of $S_{\rm er}(q) = S_{\rm e} (q/q_{\rm e})^{\gamma}$.

... irrespectively of $S_{int}(\rho) = S_0 (\rho/\rho_0)^{\gamma}$:



S NSCL

Jun Hong & PD PRC90(14)024605

... Other probes possible, but general problem of model ambiguity remains!

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Code Comparison Project

BUU type	Code correspondents	Energy range	QMD type	Code correspondents	Energy range
BLOB	P. Napolitani, M. Colonna	0.01 0.5	AMD	A. Ono	0.01 0.3
GIBUU-RMF	J. Weil	0.05 40	IQMD-BNU	J. Su, F. S. Zhang	0.05 2
GIBUU-Skyrme	J. Weil	0.05 40	IQMD	C. Hartnack, J. Aichelin	0.05 2
IBL	W. J. Xie, F. S. Zhang	0.05 2	CoMD	M. Papa	0.01 0.3
IBUU	J. Xu, L. W. Chen, B. A. Li	0.05 2	ImQMD-CIAE	Y. X. Zhang, Z. X. Li	0.02 0.4
pBUU	P. Danielewicz	0.01 12	IQMD-IMP	Z. Q. Feng	0.01 10
RBUU	K. Kim, Y. Kim, T. Gaitanos	0.05 2	IQMD-SINAP	G. Q. Zhang	0.05 2
RVUU	T. Song, G. Q. Li, C. M. Ko	0.05 2	TuQMD	D. Cozma	0.1 2
SMF	M. Colonna, P. Napolitani	0.01 0.5	UrQMD	Y. J. Wang, Q. F. Li	0.05 200

Leaders in the effort: Jorg Aichelin, Evgeni Kolomeitsev, <u>Betty Tsang + others</u> Jun Xu *et al.* PRC93(16)044609, Yingxun Zhang *et al.* arXiv:1711.05950



Premise

- Specify the same physics inputs for different transport codes
- Compare outputs
- elastic collisions only
- constant isotropic cross section $\sigma = 40 \text{ mb}$
- soft EOS + momentum-independent mean-field
- Full-run comparisons
- Controlled simplified conditions
 - * collisions in a box \leftarrow approach to equilibrium
 - * mean field in a box
 - * Next: Δ + π production in a box...



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Full Runs: Stability of Initial Density





Density Evolutions for Molecular Dynamics

100 MeV/nucleon Au + Au at b = 7 fm



General characteristics the same but differences in details

From Differences in Dynamics to Observables

Au + Au at b = 7 fm





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Periodic Box Comparions

- 1. Elastic Collisions Only
- 2. Mean-Field Only
- 3. Delta Production & Absorption...





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Comparison Project

TuQMD Example

Collisions w/Pauli: Stability of Fermi-Dirac Systems initialized with Fermi-Dirac at ρ_0 and T = 5 MeV





Molecular codes progress towards Boltzmann distribution (dashed line). Blocking of collisions? Zhang et al. arXiv:1711:05950

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Box: Collision Frequency





Way Forward

Different codes perform differently in different tests Some do well

After each sweep procedures are identified that lead to satisfactory performance and are recommended for all codes, e.g. initialization

In consequence of the code comparisons, the codes are rebuilt

E.g. TuQMD



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Example: Rebuilt TuQMD

Dan Cozma arXiv: 1706.01300

Rebuilt density initializations and Pauli principle





FOPI-LAND & ASYEOS Elliptic-Flow Data

Data Cozma PRC88(13)044912



400 MeV/mucl Au + Au data above + other, particularly more differential



Constraints on Symmetry Energy Parameters





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Conclusions

- Transport theory is indispensible in many situations
- ⇒ It is means to learn on nuclear properties at supranormal densities
- It has been used to extract constraints on nuclear pressure at supranormal densities from flow data!
- The ability to learn from finer details in data, especially at lower energies, calls for stringent quality control of the theory
- The community effort produces quality standards, helps to sort out the best procedures and prune out mistakes
- This helps to elevate the level of validity of conclusions reached using transport, e.g. TuQMD

Thanks to the authors participating in the code comparisons!



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