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# **Neutrino Interactions**

Minerba Betancourt International Neutrino Summer School 2018 May 28 2018

## Outline

- History and Introduction
- Neutrino beam
- Neutrino interactions and neutrino cross sections
- Ingredients to compute cross sections
  - Flux



### How did we discover neutrinos?

- Radioactivity: Nucleus emits particle due to nuclear instability
- While studying the beta decay, the energy did not seem to be conserved in beta decay?
  - We know energy is always conserved
  - Energy can neither be created nor destroyed only can be transformed into a different form
- In 1930, Pauli postulated the neutrino

Dear Radioactive Ladies and Gentlemen,

I have done a terrible thing.

I have postulated a particle that cannot be detected







## **The Discovery of Anti-Neutrino (1956)**

- Artificially produced neutrinos from nuclear reactors
  - Emits around 10 trillion anti-neutrinos per cm<sup>2</sup>/s
- Inverse Beta decay

$$\bar{\nu}_e + p \rightarrow e^+ + n$$



### 1995 Nobel Prize







### **The Solar Neutrino Problem (1968)**

- Nuclear reactions in the core of the sun produce Ve
- In 1968, Ray Davis's HomeStake experiment measured the Ve that arrives at earth using a huge tank of cleaning fluid solar neutrino+chlorine atom->electron+argon atom



Cleaning fluid



### 2002 Nobel Prize



• Davis published the first results indicating that only 1/3 of the neutrinos were observed, i.e. the solar neutrino problem



### **Another Interaction Neutral Current**

- In 1973 first example of NC observed at Gargamelle bubble chamber filled with freon
  - 700,000 pictures!









### **Other Neutrino Flavors**

- In 1988 the muon neutrino was discovered at Nacional de Brookhaven lab
  - The first accelerator neutrino beam (5GeV protons on Be target)





• In 2000, the third neutrino (tau neutrino) was discovered at DONUT (Fermilab).







## **The Atmospheric Neutrino Anomaly**

- Cosmic rays hit the earth isotropically
- People expected:

 $\frac{\Phi_{\nu_{\mu}}(Up)}{\Phi_{\nu_{\mu}}(Down)} = 1$ 

 However, Super-Kamiokande found

 $\frac{\Phi_{\nu_{\mu}}(Up)}{\Phi_{\nu_{\mu}}(Down)} = 0.54 \pm 0.04$ 

neutrino oscillation



cost

ATMOSPHERIC NEUTRINOS

cost

### **Standard Model Neutrino Interactions**

• Lagrangian for electroweak interactions:

$$L_{\text{int}} = i \frac{g}{\sqrt{2}} \Big[ j_{\mu}^{(+)} W^{\mu} + j_{\mu}^{(-)} W^{\mu+} \Big] + i \Big[ g \cos \theta_W j_{\mu}^{(3)} - g' \sin \theta_W j_{\mu}^{(Y/2)} \Big] Z^{\mu} + i \Big[ g \sin \theta_W j_{\mu}^{(3)} + g' \cos \theta_W j_{\mu}^{(Y/2)} \Big] A^{\mu}$$

- First term: charged current interactions (W<sup>+</sup>,W<sup>-</sup> exchange)
- Second term: neutral current interactions (Z<sup>0</sup> exchange)
- Third term: electromagnetic interactions (photon exchange)
- Electron charge:  $e = g \sin \theta_W = g' \cos \theta_W$

Neutrinos only couple to W and  $Z^0$ 



Charged Current (CC) interactions

via a W-boson

Neutral Current (NC) interactions via a Z-boson





### **Different Neutrino Sources**

• Different neutrino sources determine the range of energies



- Few GeV energy range neutrinos are very important for accelerator neutrino oscillations
- Reviewing a few neutrino interactions relevant to neutrino oscillation at the few GeV region

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### How to make a neutrino beam



### **Neutrinos From Accelerators**

• A beam of protons interact with a target and produce pions and kaons



- Focusing system (2 horns, with current, emitting B field)
- Decay region (large pipe, filled with helium)
- Monitors and absorbers
- Neutrino beam produces mainly  $\nu_{\mu}$  and a small component of  $\nu_{e}$



## **Addressing the Remaining Questions**

- Is there CP violation in the lepton sector
- What is the mass hierarchy? (sign of  $\Delta m_{32}^2$ )



 $P[\nu_{\mu} \rightarrow \nu_{e}] \neq P[\overline{\nu}_{\mu} \rightarrow \overline{\nu}_{e}]$ ?

- Use simulations to extrapolate from near detector to far detector  $\sigma_{\nu\mu} {\longrightarrow} > \sigma_{\nu e}$
- We definitely need a nuclear model to convert from produced to detected energy spectra and topologies in the near and the far detectors
- This illustrates the significance of precise knowledge of neutrino interactions physics needed for oscillation studies



### Long-baseline Experiments: What can we learn?

- Use a high intensity beam of neutrinos from Fermilab
- Construct detectors at far locations: MINOS+ at 735 Km (ended data-taking), NOvA at 810 km (taking data) and DUNE at 1300 km (in design)

$$P[\nu_{\mu} \rightarrow \nu_{e}] \neq P[\overline{\nu}_{\mu} \rightarrow \overline{\nu}_{e}] ?$$



The NOMAD detector [29] consisted of an active target of 44 drift chambers with a total fiducial mass of 2.7 tons, located in a 0.4 Tesla dipole magnetic field as shown in Fig. 1. The  $X \times Y \times Z$  total volume of the drift chambers is about  $300 \times 300 \times 400$  cm<sup>3</sup>. Drift chambers [37], made of low Z material served

The MINERVA Experimonato Menerove

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### **Cross Section Experiments**

- Modern neutrino experiments us
  - Different detector technologie:
    - Oxygen, carbon, iron, liquid ar
  - Different neutrino beams
- Common goal for all the experin
  - Study neutrino interactions

UAI Magnet

P0DECal

Barrel ECal



Downstream

ECal



Design, calibration, and performance of the MINERvA detector Nuclear Inst. and Methods in Physics Research, A, Volume 743



T2K

Mir



### **Detector Technologies**



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### **Neutrino Energies for Different Experiments**



**Plot courtesy of Phil Rodrigues** 



### Quasi-elastic scattering (QE)



**Resonance production (RES)** 



**Deep Inelastic scattering (DIS)** 



The neutrino scatters elastically off the nucleon ejecting a nucleon from the target



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## **Neutrino Cross Section**

- What is the cross section?
  - A measure of the probability of an interaction occurring



## **Charged Current Interactions**

### Quasi-elastic scattering (QE)



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#### In More Deta Model Comparisons Quas Ratio to GENIE Antineutrino Shape Only Jasi-MINER $vA \bullet \overline{v}$ Tracker $\rightarrow$ CCQE 1.8 1 NuWro RFG M<sub>4</sub>=1.35 data 1.6 GENIE RFG M<sub>A</sub>=0.99 ----- NuWro RFG M<sub>A</sub>=0.99 + TEM Ratio to GENIE Ratio to GENIE NuWro RFG M<sub>A</sub>=0.99 — NuWro SF M<sub>A</sub>=0.99 Muon ring at Super-K pproxima 1 1.4 in Super1.2 Image : T2K MINER 0 3.0 Events / .05 GeV<sup>2</sup> 0 0.6 0.4 2 R Patterson wine and cheese, NOvA v charged-current candidate Recor Events / .05 GeV<sup>2</sup> NuWro RFG RFG RFG $\mathbf{SF}$ 0.8 +TEMModel 0.6

0.99

0.99

1.35

0.99

 $M_A$  (GeV)

0.4

0.2

n<mark>alized</mark> POT

 $M_A$ 

### **Cross Section is one of the largest systematics**

PRL 116, 181801 (2016)

PHYSICAL REVIEW LETTERS

week ending 6 MAY 2016

#### Measurement of Muon Antineutrino Oscillations with an Accelerator-Produced Off-Axis Beam

Cross section is one of the largest systematic uncertainties for oscillation experiments like T2K as an example



TABLE IV. Percentage change in the number of one-ring  $\mu$ -like events before the oscillation fit from  $1\sigma$  systematic parameter variations, assuming the oscillation parameters listed in Table III and that the antineutrino and neutrino oscillation parameters are identical.

Source of uncertainty (number of parameters)	$\delta n_{\rm SK}^{\rm exp}/n_{\rm SK}^{\rm exp}(\%)$
ND280-unconstrained cross section (6)	10.0
Flux and ND280-constrained cross section (31)	3.4
Super-Kamiokande detector systematics (6)	3.8
Pion FSI and reinteractions (6)	2.1
Total (49)	11.6

T2K's uncertainties, from PRL 116, 181801 (2016)



### **Another reason Why We Need to Understand Nuclear Effects**

- Plus if the near and far detector are made of different materials, we need to worry about A dependence of nuclear effects
- For example, T2K uses near detector carbon measurements even though the far detector is made of water



#### **T2K Near Detector**



#### **T2K Far Detector**



### **Nuclear Effects**

- Fermi motion: In a nucleus, the target nucleon has a momentum.
   Modeled as Fermi gas that fills up all available state until some Fermi momentum
- Pauli blocking: Pauli exclusion principle ensures that states cannot occupy states that are already filled
- Multi nucleon interactions
- Final state interactions









### **Example of Nuclear Effects (Final State Interaction)**

• Final state interaction (FSI):

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- Due to final state interactions, particles can interact with nucleons and pions can be absorbed before exiting the nucleus and other nucleons get knocked out



### **Example of Nuclear Effects (Final State Interactions)**



clear effects modify the true/reco neutrino energy relationship and final-state ticle kinematics





## Example of Nuclear Effects (multi-nucleon interaction)[2p2h]

 Nuclear effects modify the neutrino energy, for example multi-nucleon interactions (Meson exchange current or short range correlations)



nucleons

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- The resulting di-nucleon pair undergoes final state interaction and produce low energy protons and neutrons which we do not detect well
- Multi-nucleon processes smear the reconstructed neutrino energy

Vμ

- Solid lines: multi nucleon contributions
- Dashed lines: genuine CCQE events



# **Neutrino Interactions**





- We do not know:
  - Initial state bound nucleon momenta
  - Bound nucleon cross section
  - Multi-nucleon correlated states
  - Final state interactions
- Several challenges from the theoretical model side and experimental side to understand neutrino interactions



# The University of Chicago<sup>1</sup>, Fermilab<sup>2</sup>, University of Minne

 $(\frac{u}{4})^{2}$ 

# **Elastic Scattering**

### ormalism:

$$\frac{Q^{2}}{4M^{2}}F_{A}^{2} - (1 - \frac{Q^{2}}{4M^{2}}) \frac{Q^{2}}{4M^{2}} + \frac{Q^{2}}{4M^{2}}(1 - \frac{Q^{2}}{4M^{2}})(\xi F_{2})^{2} + \frac{Q^{2}}{M^{2}}(1 + \frac{Q^{2}}{4M^{2}})(F_{A}^{3})^{2} + \frac{Q^{2}}{M^{2}} + \frac{Q^{2}}{4M^{2}})(F_{A}^{3})^{2} + F_{P}^{2}) + F_{A}^{2} + F_{A}^{2} + 2F_{P}|^{2} - 4(1 + \frac{Q^{2}}{4M^{2}})((F_{V}^{3})^{2} + F_{P}^{2})] + F_{2}^{2} + \frac{M^{2}}{M^{2}}Re\left[(F_{1} - \tau\xi F_{2})F_{V}^{3*} - (F_{A}^{*} - \frac{Q^{2}}{2M^{2}}F_{P})F_{A}^{3})\right] + \frac{1}{4}\left\{F_{A}^{2} + F_{1}^{2} + \tau(\xi F_{2})^{2} + \frac{Q^{2}}{M^{2}}(F_{A}^{3})^{2}\right\}$$

ely, there are just 6 Fam 
$$F_A(0)$$
  
 $(1 - \frac{q^2}{M_A^2})^2$ 

1 Smith, C.H., 1972, Phys. Rep. C3, 261.

Ge VAR hyexpans periments suchnase K2K, SviBar and MINOS find similar

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# **Fittin**

malism • We perform a j FNAL 1983 deu **Expansion** axial f C depend on the • Each data set is As discussed in the Introduction, Deuterium<sup>1</sup> ngs. The dipole

30 nstrained from neutron  $m_A$ 7 • • • 'en the introduction, ax e Introduction, an expansio<sup>10</sup>  $r_{A}$ , V1a 5 28, R1 (2002)





<sup>1</sup> the NOMAD active target is nearly isoscalar  $(n_n : n_p = 47.56\% : 52.43\%)$  and consists mainly of Carbon; a detailed de-

## **Axial Form Factor**

- A model independent description of the axial form factor called z-expansion is derived in Phys. Rev. D84 (2011)
- The form factor can be expressed as a power series of a new variable z

$$F_A(q^2) = \sum_{k=0}^{k_{\max}} a_k z(q^2)^k$$

- where the expansion coefficients  $a_k$  are dimensionless numbers representing nucleon structure information  $\frac{\times 10^{-39}}{\times 10^{-39}}$
- Derived from first principles of QCD
- Extensively used in meson decay



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### **Including multi nucleon Interactions (2p2h)**

 Inclusion of the multi nucleon emission channel (np-nn) gives better agreement with data
 An explanation of this puzzle

An explanation of this puzzle



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### **Including Random Phase Approximation (RPA)**

- Analogous to screening of electric charge in a dielectric
- For neutrino scattering in a nucleus, imagine the W as having a weak charge and polarizing the nuclear medium
- Calculated using Random phase approximation (RPA), PRC 70, 055503 (2004)
- Suppress cross sections at low four momentum transfer Q<sup>2</sup>





### **Double Differential Cross Section (Neutrinos)**

• Muon longitudinal  $P_{Z_{\mu}}$  and transverse momentum  $P_{T_{\mu}}$  are measurable quantities  $\frac{d^{2}\sigma}{dP_{T_{\mu}}dP_{Z_{\mu}}} \qquad \widehat{\mathbf{g}}$ 



### **Resonance Production**

- Next important channel for neutrino oscillation and increasing the W toward the QCD list
- Most experiments use the Rein-Sehgal model for resonance production
  - More recent models by M. Athat, Salamanca-Valencia, M. Pascos



Old bubble chamber deuterium data

Recent reanalysis of deuterium data finds consistency between ANL and BNL



Callum Wilkinson, et al., Phys. Rev. C70(2004) 055503

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### **Pion Production and Final State Interactions**

- MINERvA has measured pion  $\pi^+$  and  $\pi^0$  production
- Both prefer slightly softer pions than GENIE's final state cascade model predicts





### **Comparing MINERvA and MiniBooNE measurements**

- No models describe all data sets well
  - MiniBooNE <E>~1 GeV: best theory models (GIBUU) strongly disagree in shape
  - MINERvA <E>=4 GeV: Event generator has shape but not magnitude





### **Neutrino Deep-Inelastic Scattering**

- Deep inelastic neutrino-nucleon scattering reactions have large q2 (q<sup>2</sup>>>m<sup>2</sup><sub>N</sub>,  $E_{v}>>m_{N}$ )  $v_{l}(p)+N \rightarrow l^{-}(p')+X$
- Quark-Pardon model valid due to asymptotic freedom of QCD, which makes quarks behave as free point-like particles
- Using Mandelstam variables in DIS

$$s = (p + p_N)^2 \approx 2ME_v = 2ME$$
  

$$Q^2 = -q^2 = -(p + p')^2 = 4EE' \sin^2 \frac{\theta}{2}$$
  

$$W^2 = E_X^2 - p_X^2 = -Q^2 + 2Mv + M^2$$
  

$$v = \frac{q \cdot p_N}{M} = E - E'$$

$$x = \frac{-q^2}{2q \cdot p_N} = \frac{Q^2}{2M\nu}$$
$$y = \frac{q \cdot p_N}{p \cdot p_N} = \frac{\nu}{E} = \frac{Q^2}{2MEx}$$



### **Neutrino Deep Inelastic Scattering**

• Scattering off protons

$$\frac{d\sigma_{cc}(v_{\mu}p)}{dxdy} = \frac{G_{F}^{2}ME}{\pi} 2x \left\{ \left[ d(x) + s(x) \right] + \left[ \overline{u}(x) + \overline{c}(x) \right] (1-y)^{2} \right\} \\ \frac{d\sigma_{cc}(v_{\mu}p)}{dxdy} = \frac{G_{F}^{2}ME}{\pi} 2x \left\{ \left[ u(x) + c(x) \right] (1-y)^{2} + \left[ \overline{d}(x) + \overline{s}(x) \right] \right\}$$



• Structure functions

$$F_{2}^{\nu p}(x) = 2x[d(x) + \bar{u}(x) + s(x) + \bar{c}(x)]$$
  

$$xF_{3}^{\nu p}(x) = 2x[d(x) - \bar{u}(x) + s(x) - \bar{c}(x)]$$
  

$$F_{2}^{\bar{\nu}p}(x) = 2x[u(x) + c(x) + \bar{d}(x) + \bar{s}(x)]$$
  

$$xF_{3}^{\bar{\nu}p}(x) = 2x[u(x) + c(x) - \bar{d}(x) - \bar{s}(x)]$$

• Neutron (isospin symmetry)

$$F_{2}^{\nu n}(x) = 2x [u(x) + \overline{d}(x) + s(x) + \overline{c}(x)]$$
  
$$xF_{3}^{\nu n}(x) = 2x [u(x) - \overline{d}(x) + s(x) - \overline{c}(x)]$$



# **DIS Scattering Data**

- NuTeV experiment at Fermilab studied DIS scattering
- NuTeV collected over 3 million event 20 GeV<E<400 GeV

F2 measurement on Iron



- Data agrees with charge lepton data for x<0.5
- NuTeV F2 and xF3 agrees with theory for medium x
  - At low x different Q2 dependence
  - At high x (x>0.6) NuTeV is systematically higher



# **Deep Inelastic From MINERvA**

- MINERvA produced deep inelastic ratios from nuclear targets to study x dependent nuclear effects
- We have a x range from the low x shadowing region through the EMC region
- The simulation used in the analysis assumes the same x-dependent nuclear effects for C, Fe and Pb based on charged lepton scattering



The data suggest additional nuclear shadowing in the lowest x bin (0 < x < 0.1) than predicted in lead, it is at a value of x and Q2 where shadowing is not normally found in charged lepton nucleus scattering

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In the MEC region (0.3<x<0.75), we see good agreement between data and simulation

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# **Neutrino Cross Section**

 Let's concentrate on each of the ingredients to compute the cross section



- Neutrino Flux
  - Considering the procedure from MINERvA experiment as an example

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### Hadronic Cascade in the Target

- The primary beam interactions in the target: proton on carbon
- Secondary and tertiary interactions in the target: proton, pion, kaon, etc
- Interaction outside of the target: proton, pion, kaon on aluminum, iron, helium, etc





### Parents for electron neutrino





### **Hadronic Cascade in the Target**

- These interactions are non-perturbative QCD
- The simulation uses a model
  - MINERvA uses geant4.2.p03 and FTFP\_BERT as hadronic model



Big discrepancies between predictions from hadronic models



### What are the sources for the Systematic Uncertainties?

### • Focusing Uncertainties





A current is pulsed through two aluminum horns to create a toroidal magnetic field

• Hadronic interactions:



	Particle production	X <sub>F</sub>	Reference
NA49 pC @158 GeV	$\pi^{\pm}$	<0.5	Eur.Phys.J. C49 (2007) 897
	K±	<0.2	G. Tinti Ph.D. thesis
	р	<0.9	Eur.Phys.J. C73 (2013) 2364



Neutrino Energy (GeV)



### How do we use Data to Correct the simulations?

• A weight is applied to the v based on its hadronic interaction history

 $correction(x_F, p_T, E) = \frac{f_{Data}(x_F, p_T, E = 158GeV) \times scale(x_F, p_T, E)}{f_{MC}(x_F, p_T, E)}$ 

 $f(x_F, p_T) = E d^3\sigma/dp^3 =$  invariant production cross-section







### **Flux Prediction and Uncertainty**







### Low-v Technique

- Using charged-current scattering with lower hadronic recoil energy
- The v is the energy transferred to the recoil system:  $v=E(neutrino)-E_{\mu}$
- In the limit of small V, the charged current cross section for neutrinos and antineutrinos is approximately constant

$$\frac{d\sigma}{dv} = A\left(1 + \frac{B}{A}\frac{v}{E} - \frac{C}{A}\frac{v^2}{E^2}\right)$$

- As  $v/E \to 0$   $\frac{d\sigma}{dv} \to A$
- A measurement of the low-V interaction rate as a function of neutrino energy is equivalent to a measurement of the shape of the neutrino flux
- Technique used in different experiments
  - In 2006 NuTeV experiment used 5- 20GeV low-V cut (M.Tzanov at al. Phys. Rev. D74 012008)
  - in 2010 MINOS experiment used 3- 50GeV low-V cut (P.Adamson et al.) Phys. Rev. D 81,072002



### **Low-Nu Technique**

• Neutrino flux from the low-v method





## **Constrained flux vs Low-nu**

• Comparing with the flux constrained with hadron production data





### **Flux Constraint using Neutrino-Electron Scattering**

• Well understood electroweak process

$$\frac{d\sigma(v_{\mu}e^{-} \rightarrow v_{\mu}e^{-})}{dy} = \frac{G_{F}^{2}m_{e}E_{v}}{2\pi} \left[ \left(\frac{1}{2} - \sin^{2}\theta_{W}\right)^{2} + \sin^{4}\theta_{W}(1-y)^{2} \right]$$

 $G_F$  and  $\theta_W$ : well-known electroweak parameters



- Very small cross section (~1/2000 of nu-nucleon scattering)
- Very forward electron final state
  - Good angular forward electron final state
- Signal in MINERvA is a single electron moving in the beam direction









### Signal and Backgrounds (Neutrino-Electron Scattering) at MINERvA

• Signal is a mixture of  $v_{\mu}e^{-}, \overline{v_{\mu}}e^{-}, v_{e}e^{-}$  and  $\overline{v_{e}}e^{-}$ 



• We cannot distinguish neutrino type

 $v_{\mu}e^{-}$  and  $\overline{v}_{\mu}e^{-}:91\%$  $v_{e}e^{-}$  and  $\overline{v}_{e}e^{-}:9\%$ 



## **Event Selection**

• Using Mandelstam variables

 $t = \frac{s}{2} (1 - \cos \theta^*) \qquad y = -\frac{1}{2} (1 - \cos \theta^*) \quad \text{in CM frame} \implies t = -sy$  $u = -2E_v E_e (1 - \cos \theta) \quad \text{in lab frame}$ 

$$s + t = -u$$
  

$$s(1 - y) = 2E_v E_e (1 - \cos \theta)$$
  

$$2m_e (1 - y) = E_e \theta^2$$
  
Since  $0 < y < 1$ ,  $E_e \theta^2 < 2m_e$ 



- Neutrino interaction does not always produce only single electron or single photon from  $\pi^0$
- Non-single particle activity affects dE/ dx





### **Results**

• Electron neutrino events after background subtraction and efficiency correction:



$$123.8 \pm 17.0 \text{ (stat)} \pm 9.1 \text{ (sys)}$$

• Using data the flux is constrained



• The total uncertainty on the NuMi neutrino flux reduces from 9% to 6%



### **Neutrino Cross Section**

• We reviewed some neutrino interactions and techniques to constraint the flux, tomorrow we will study in detail each step to compute the cross section



$$\sigma = \frac{N}{\phi T \epsilon}$$

