

# Electroweak cosmology

Thomas Konstandin

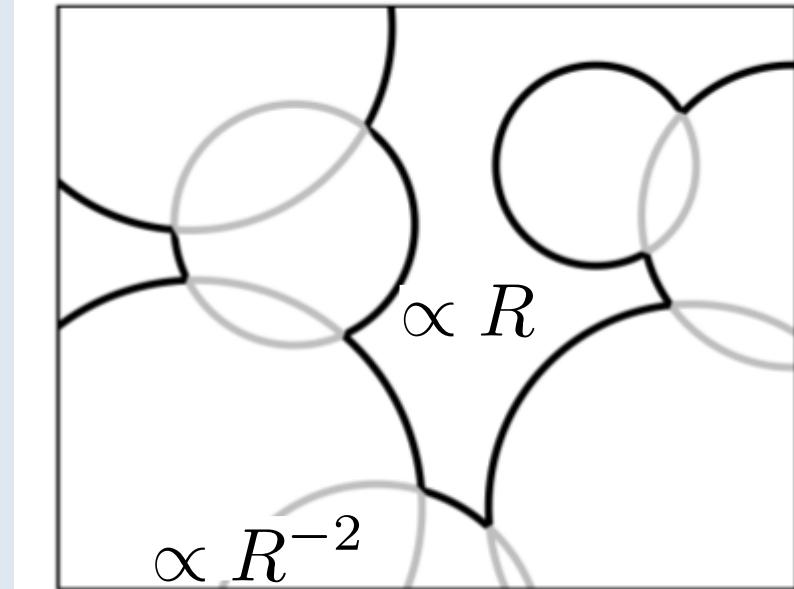
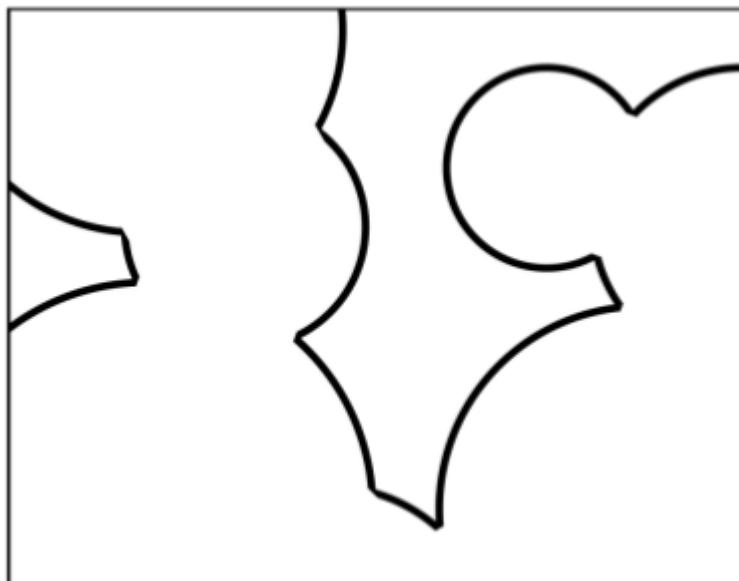


LISA WG, MITP Mainz, Oct 17, 2017

# Motivation

Gravitational waves from bubble dynamics:  
Beyond the Envelope

Ryusuke Jinno<sup>a,b</sup> and Masahiro Takimoto<sup>b,c</sup>



# Motivation

## 3.2 Analytic expressions

Now we present the analytic expressions for the GW spectrum. After a short calculation (see Appendix A–C), we obtain the single-bubble spectrum

$$\Delta^{(s)} = \int_{-\infty}^{\infty} dt_x \int_{-\infty}^{\infty} dt_y \int_{v|t_{x,y}|}^{\infty} dr \int_{-\infty}^{t_{\max}} dt_n \int_{t_n}^{t_x} dt_{xi} \int_{t_n}^{t_y} dt_{yi}$$

$$\frac{k^3}{3} \left[ \begin{array}{l} e^{-I(x_i, y_i)} \Gamma(t_n) \frac{r}{r_{xn}^{(s)} r_{yn}^{(s)}} \\ \times \left[ j_0(kr) \mathcal{K}_0(n_{xn\times}, n_{yn\times}) + \frac{j_1(kr)}{kr} \mathcal{K}_1(n_{xn\times}, n_{yn\times}) + \frac{j_2(kr)}{(kr)^2} \mathcal{K}_2(n_{xn\times}, n_{yn\times}) \right] \\ \times \partial_{txi} [r_B(t_{xi}, t_n)^3 D(t_x, t_{xi})] \partial_{tyi} [r_B(t_{yi}, t_n)^3 D(t_y, t_{yi})] \cos(kt_{x,y}) \end{array} \right], \quad (3.2)$$

and the double-bubble spectrum

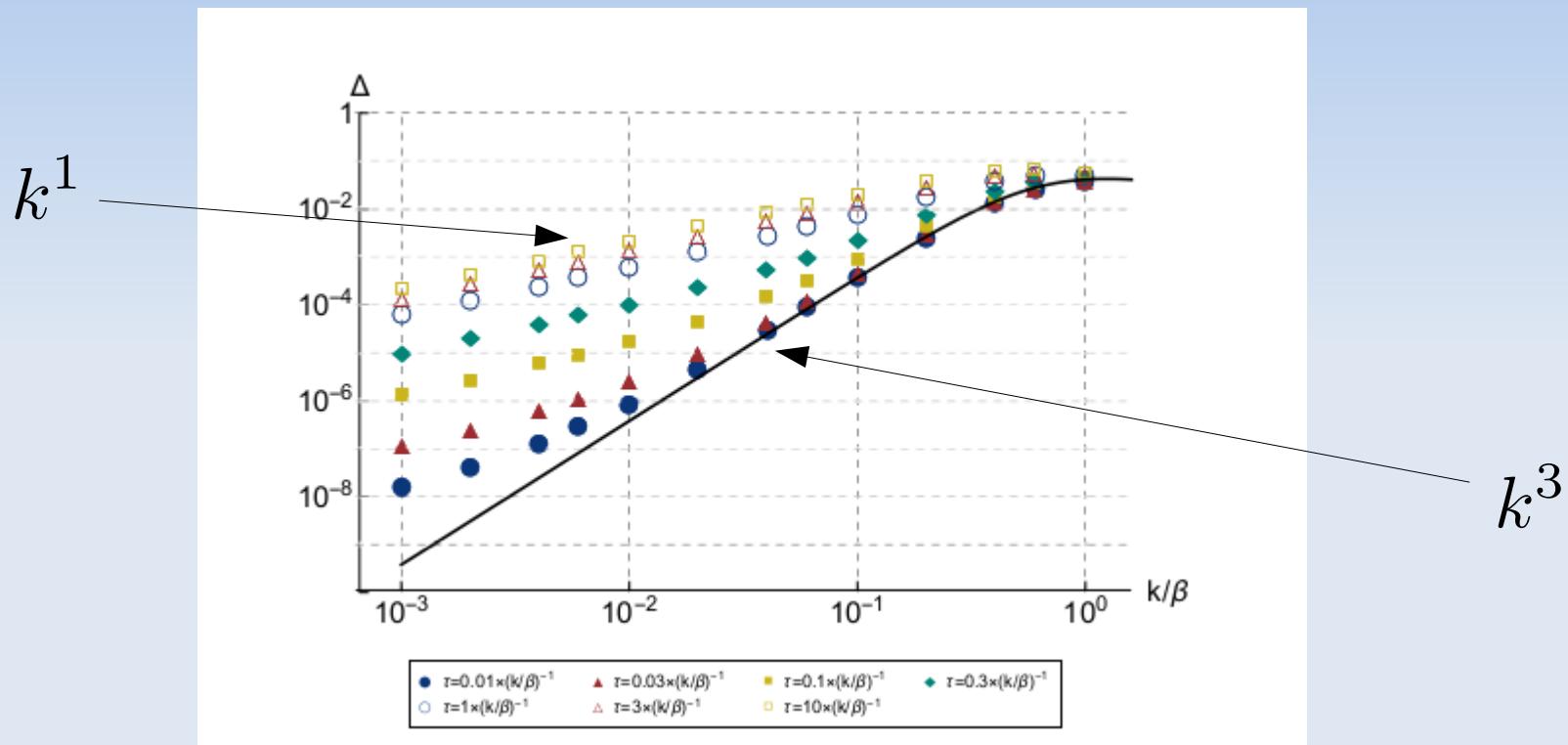
$$\Delta^{(d)} = \int_{-\infty}^{\infty} dt_x \int_{-\infty}^{\infty} dt_y$$

$$\int_0^{\infty} dr \int_{-\infty}^{t_x} dt_{xn} \int_{-\infty}^{t_y} dt_{yn} \int_{t_{xn}}^{t_x} dt_{xi} \int_{t_{yn}}^{t_y} dt_{yi} \int_{-1}^1 dc_{xn} \int_{-1}^1 dc_{yn} \int_0^{2\pi} d\phi_{xn, yn}$$

$$\frac{k^3}{3} \left[ \begin{array}{l} \Theta_{sp}(x_i, y_n) \Theta_{sp}(x_n, y_i) e^{-I(x_i, y_i)} \Gamma(t_{xn}) \Gamma(t_{yn}) \\ \times r^2 \left[ j_0(kr) \mathcal{K}_0(n_{xn}, n_{yn}) + \frac{j_1(kr)}{kr} \mathcal{K}_1(n_{xn}, n_{yn}) + \frac{j_2(kr)}{(kr)^2} \mathcal{K}_2(n_{xn}, n_{yn}) \right] \\ \times \partial_{txi} [r_B(t_{xi}, t_{xn})^3 D(t_x, t_{xi})] \partial_{tyi} [r_B(t_{yi}, t_{yn})^3 D(t_y, t_{yi})] \cos(kt_{x,y}) \end{array} \right]. \quad (3.3)$$

10 integrations?

# Motivation



# Motivation

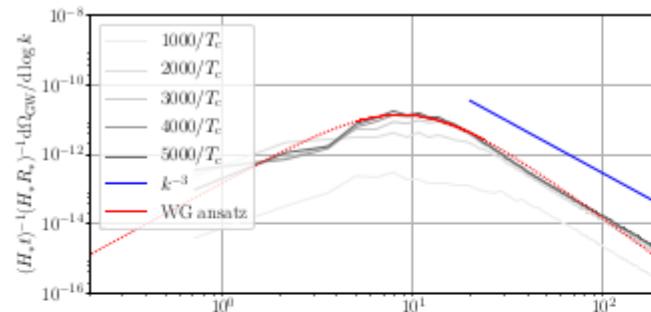
## Shape of the acoustic gravitational wave power spectrum from a first order phase transition

Mark Hindmarsh,<sup>1, 2, \*</sup> Stephan J. Huber,<sup>1, †</sup> Kari Rummukainen,<sup>2, ‡</sup> and David J. Weir<sup>2, §</sup>

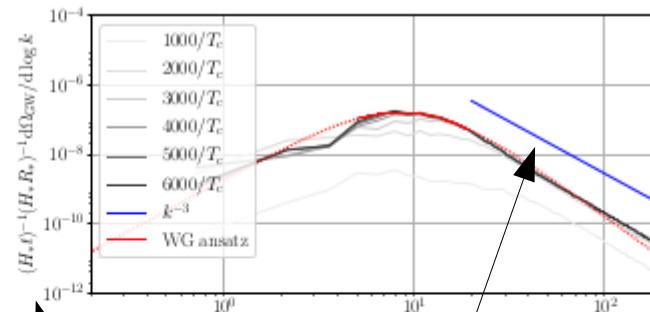
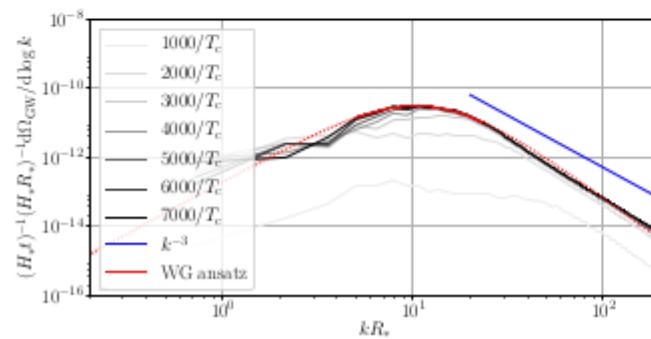
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(Dated: April 20, 2017)



(a) Weak,  $v_w = 0.92$



(b) Intermediate,  $v_w = 0.92$

$$k^{-3}$$

enhancement  $\beta/H$

# Envelope redux

## Gravitational Wave Production by Collisions: More Bubbles

Stephan J. Huber<sup>(1)</sup> and Thomas Konstandin<sup>(2)\*</sup>

$$\frac{dE_{GW}}{d\omega d\Omega} = 2G\omega^2 \Lambda_{ij,lm}(\hat{\mathbf{k}}) T_{ij}^*(\hat{\mathbf{k}}, \omega) T_{lm}(\hat{\mathbf{k}}, \omega),$$

where  $T_{ij}(\hat{\mathbf{k}}, \omega)$  denotes the stress-energy tensor in Fourier space

$$T_{ij}(\hat{\mathbf{k}}, \omega) = \frac{1}{2\pi} \int dt e^{i\omega t} \int d^3x e^{-i\omega \hat{\mathbf{k}} \cdot \mathbf{x}} T_{ij}(\mathbf{x}, t),$$

and  $\Lambda$  is the projection tensor for the transverse-traceless part

$$\Lambda_{ij,lm}(\hat{\mathbf{k}}) = \delta_{il}\delta_{jm} - 2\hat{\mathbf{k}}_j\hat{\mathbf{k}}_m\delta_{il} + \frac{1}{2}\hat{\mathbf{k}}_i\hat{\mathbf{k}}_j\hat{\mathbf{k}}_l\hat{\mathbf{k}}_m - \frac{1}{2}\delta_{ij}\delta_{lm} + \frac{1}{2}\delta_{ij}\hat{\mathbf{k}}_l\hat{\mathbf{k}}_m + \frac{1}{2}\delta_{lm}\hat{\mathbf{k}}_i\hat{\mathbf{k}}_j.$$

$$\Omega_{GW*} = \omega \frac{dE_{GW}}{d\omega} \frac{1}{E_{tot}} = \kappa^2 \left( \frac{H}{\beta} \right)^2 \left( \frac{\alpha}{\alpha+1} \right)^2 \Delta(\omega/\beta, v_b), \quad (13)$$

where we used the definition of the Hubble constant

$$H^2 = \frac{8\pi G \rho_{tot}}{3} = \frac{8\pi G (\rho_{vac} + \rho_{rad})}{3}, \quad (14)$$

and defined the dimensionless function  $\Delta$  as

No dependence on  $H!$

$$\Delta(\omega/\beta, v_b) = \frac{\omega^3}{\beta^3} \frac{3v_b^6 \beta^5}{2\pi V} \int d\hat{\mathbf{k}} \Lambda_{ij,lm} C_{ij}^* C_{lm}. \quad (15)$$

# Integrations

$$\frac{dE_{GW}}{d\omega d\Omega} = 4G\rho_{vac}^2\kappa^2v_b^6\omega^2(|C_+|^2 + |C_-|^2), \quad (\text{A2})$$

$$C_{\pm}(\omega) = \frac{1}{6\pi} \sum_n \int dt e^{i\omega(t-z_n)} (t-t_n)^3 A_{n,\pm}(\omega, t), \quad (\text{A3})$$

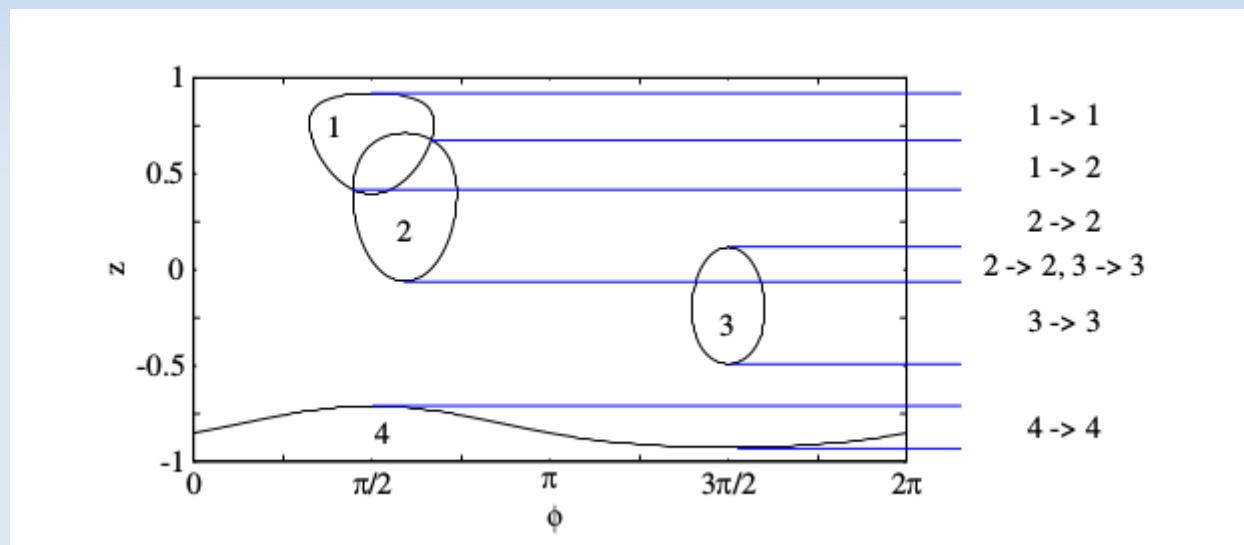
$$A_{n,\pm}(\omega, t) = \int_{-1}^1 dz e^{-iv_b\omega(t-t_n)z} B_{n,\pm}(z, t), \quad (\text{A4})$$

$$B_{n,+}(z, t) = \frac{(1-z^2)}{2} \int_{S'_n} d\phi \cos(2\phi), \quad B_{n,-}(z, t) = \frac{(1-z^2)}{2} \int_{S'_n} d\phi \sin(2\phi). \quad (\text{A5})$$

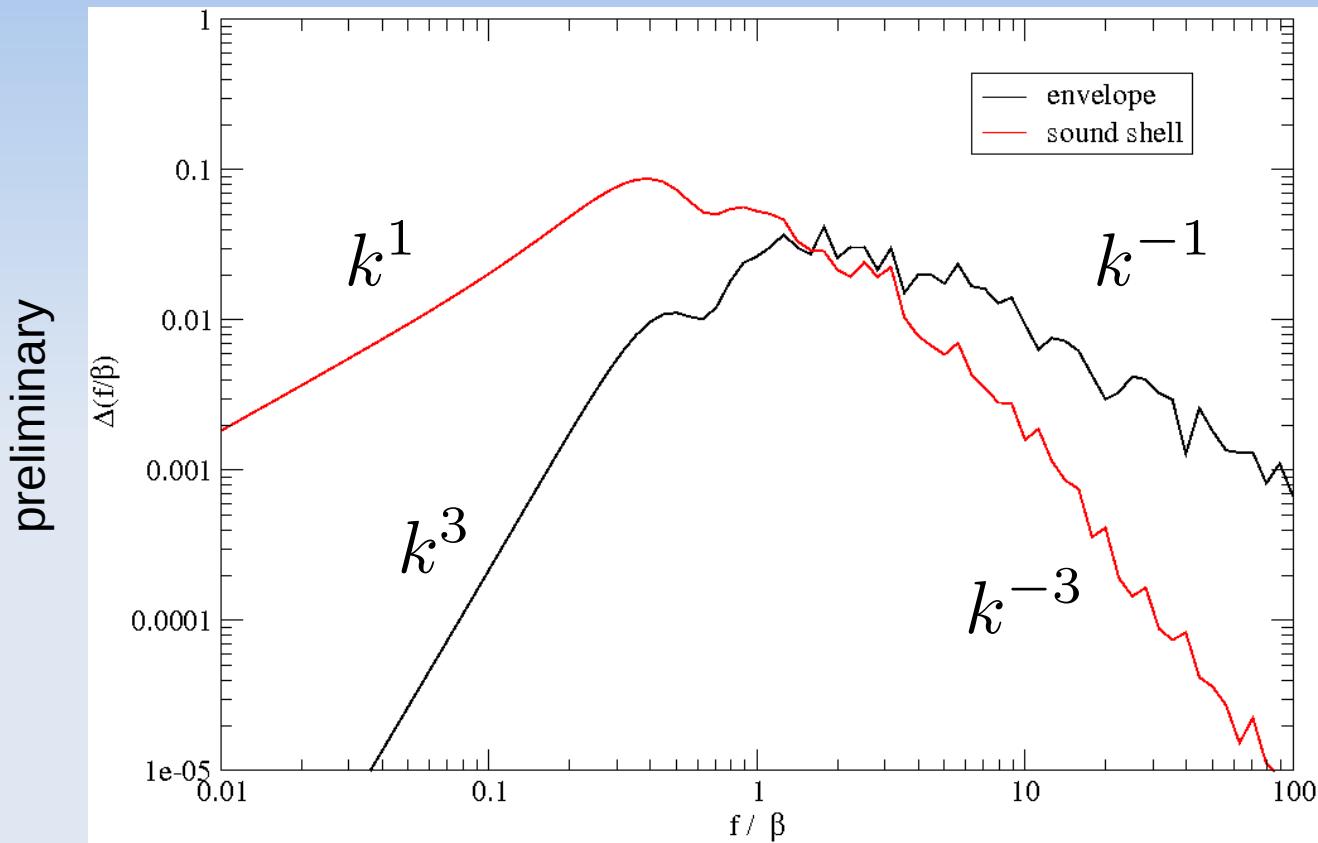
3 integrations, done  $10^{11}$  times, 1 CPU hour

do the first integration analytically!

# Integrations



# Results



all integrals are finite

peak a little lower

amplitude a bit higher