

# Suppression of quarkonium in a medium

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Work done in collaboration with S. Biondini, N. Brambilla, J. Ghiglieri, J. Soto and A. Vairo

# Outline

- 1 Review
- 2 The case  $1/r \gg T \gg E \gg m_D$
- 3  $m \gg T \gg \frac{1}{r} \sim gT$ . Dissociation temperature.
- 4 Asymmetry

# Review

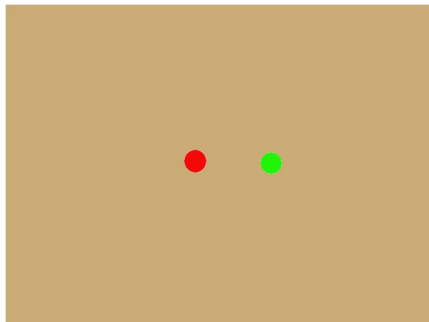
# The original idea of Matsui and Satz (1986)

- Quarkonia is quite stable in the vacuum.
- Deconfinement is due to colour screening, quantities measurable in Lattice QCD at finite temperature (static) support this. For example Polyakov loop.
- Dissociation of heavy quarkonium in heavy-ion collisions due to colour screening signals the creation of a quark-gluon plasma.

# Colour screening

$$V(r) = -\alpha_s \frac{e^{-m_D r}}{r}$$

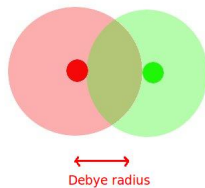
In the vacuum



# Colour screening

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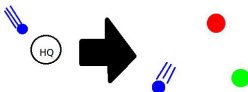
At finite temperature



## But...

- Is this really the mechanism? What is the potential? (How do we obtain the Schrödinger equation?)
- Can we extrapolate production rate from pp and pA collisions?
- Do we know how to go from thermal equilibrium to the computation of  $R_{AA}$ ?
- Is enough to assume a Bjorken evolution or do we need something more realistic?
- Finite velocity, asymmetry, heavy quark energy loss...

## Another mechanism, the decay width

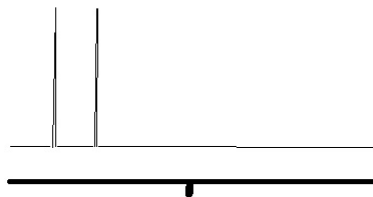


- This effect makes the peak in the spectral function broader. It can arrive to a point where it is so broad that it does not make sense to speak of a bound state anymore.



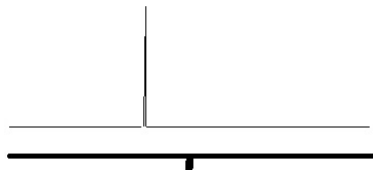
# (Very) Qualitative spectral function

$$T = 0$$



# (Very) Qualitative spectral function

Only screening



# (Very) Qualitative spectral function

Decay width



## Laine et al. perturbative potential (2007)

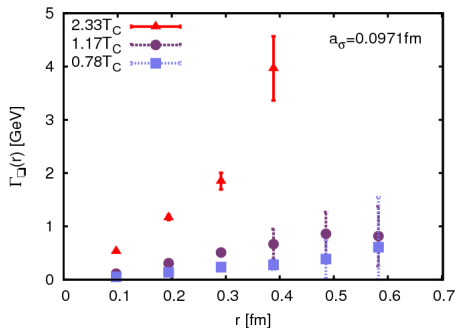
$$V(r) = -\alpha_s C_F \left[ m_D + \frac{e^{-m_D r}}{r} \right] - i\alpha_s T C_F \phi(m_D r)$$

with

$$\phi(x) = 2 \int_0^\infty \frac{dz z}{(z^2 + 1)^2} \left( 1 - \frac{\sin(zx)}{zx} \right)$$

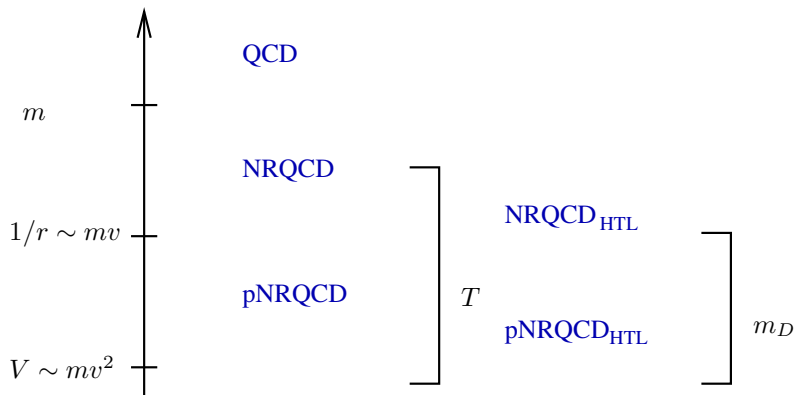
- This potential was obtained through the Wilson loop in Minkowski space at finite temperature.
- It has an imaginary part that has to be related with a decay width.

# Imaginary potential on the lattice



Computed using Maximum Entropy Method.  
Rothkopf, Hatsuda and Sasaki (2011)

# Effective field theories



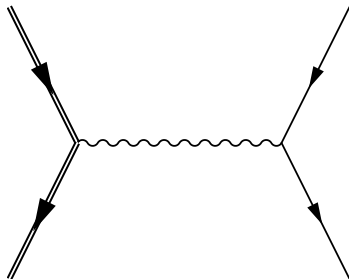
(Brambilla, Ghiglieri, Petreczky And Vairo, M. A. E and Soto)

## Energy scales for zero temperature heavy quarkonium

Heavy quarkonium at  $T = 0$  is a system with a lot of different energy scales.

For example, for computing the decay of  $J/\psi$  to electrons...

- We need annihilation cross section of the quark and the anti-quark to electrons. The energies involved are of the order of  $m_c$ .



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- We also need the probability that the quark and the anti-quark are at the same point, this is given by the wave-functions. The energies involved are of the order of  $1/r$ .

$$\Psi_{ab}(\mathbf{r})$$

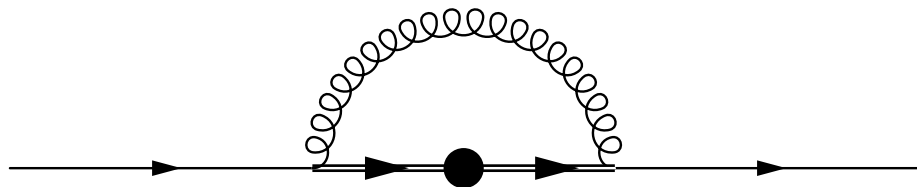


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- If we want to make a precision computation, we need to include the effects of the color octet component of  $J/\psi$ . The energy involved here is of order of the binding energy.



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# Heavy quarkonium is non-relativistic

In a perturbative computation of the binding energy.

$$E = m_Q \alpha_s \sum_{n=0}^{\infty} \alpha_s^n A_n(v)$$

because  $v$  is small we can not know the size of  $A_n(v)$ , for example, it could go like  $1/v$ .

If we use EFT the computation is an expansion in both  $v$  and  $\alpha_s$ .

$$E = m_Q \alpha_s v^2 \sum_{n,m} \alpha_s^n v^m B_{n,m}$$

now  $B_{n,m}$  is of order 1.

In perturbation theory  $v \sim \alpha_s$ .

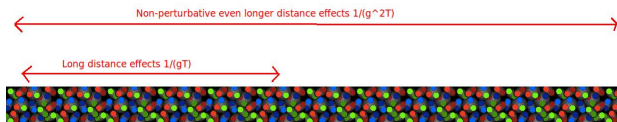
# Energy scales in a thermal bath

In the weak-coupling regime

- We have an almost free gas of quarks and gluons with typical energy  $\pi T$ .
- At long distances (order  $\frac{1}{gT}$ ), non-trivial collective phenomena arise, as for example chromoelectric static fields screening.
- At even longer distances (order  $\frac{1}{g^2 T}$ ), non-perturbative phenomena arise, as for example chromomagnetic static fields screening.

# Energy scales in a thermal bath

In the weak-coupling regime



# Heavy quarkonium in a thermal bath

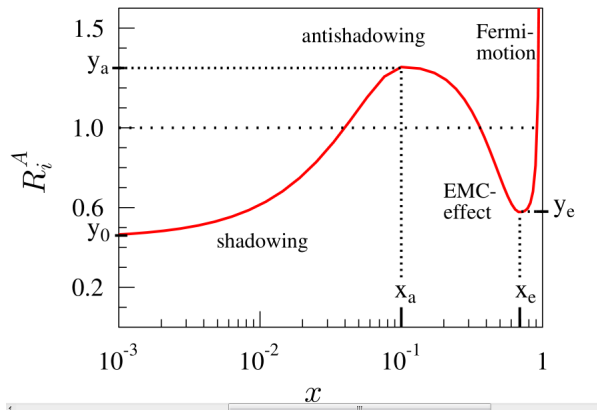
In this case we have to combine the two types of energy scales.

- The energy scales typical of a non-relativistic bound state.  $m_Q$ ,  $\frac{1}{r}$  and  $\Delta E$ .
- The energy scales of a weakly-coupled quark-gluon plasma.  $\pi T$ ,  $gT$ ...

Depending on the relation of  $T$  with the energy scales of the bound state we are going to have very different physical situations.

# Extrapolation of production

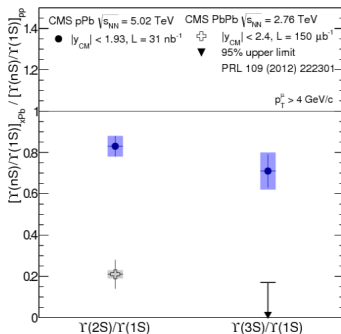
- Parton content in a nuclei is not number of nucleons time parton content of a proton.



Eskola, Paukkunen and Salgado (2009)

# Extrapolation of production

- Parton content in a nuclei is not number of nucleons time parton content of a proton.



Taken from Abdulsalam talk in Quark matter.



# Extrapolation of production

- Parton content in a nuclei is not number of nucleons time parton content of a proton.
- The formation time of quarkonium is of order of the thermalization time  $\frac{1}{E} \sim 0.5 fm$ .

# Computation of $R_{AA}$

From EFT related approaches

$$R_{AA} \propto e^{-\int dt \Gamma(T_{eff}(t))}$$

Strickland (2012), Nenzig and Wolschin (2014)

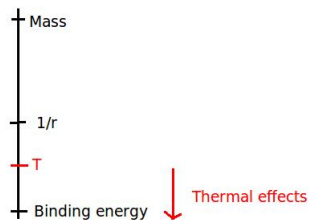
Using open quantum system like equations

$$\partial_t \rho = -i[H, \rho] + \sum_i (C^i \rho C^{i\dagger} - \{C^{i\dagger} C^i, \rho\})$$

Akamatsu (2014)

The case  $1/r \gg T \gg E \gg m_D$

# Thermal effects



- The physical results that come from energy scales higher than the temperature are not affected by the thermal bath.

$$\frac{1}{e^{q/T} \pm 1}$$

- Consequence: The EFT resulting from integrating out degrees of freedom higher than  $T$  are still valid for this situation.
- These are NRQCD and pNRQCD.

- Gives exactly the same results as QCD for all Green functions evaluated at distances bigger than  $\frac{1}{m_Q}$ .
- One can always compute the NRQCD from QCD (matching) using perturbation theory because  $m_Q \gg \Lambda_{QCD}$ .
- This EFT is also useful for Lattice computations as the UV cutoff of this theory is much smaller than  $m_Q$ .
- Suppressions in  $\frac{1}{m_Q}$  that are not obvious from QCD are trivially seen with this Lagrangian.

$$\mathcal{L}_{NRQCD} = \mathcal{L}_g + \mathcal{L}_q + \mathcal{L}_\psi + \mathcal{L}_\chi + \mathcal{L}_{\psi\chi}$$

$$\mathcal{L}_g = -\frac{1}{4}F_{\mu\nu}^a F^{\mu\nu a} + \frac{d_2}{m_Q^2}F_{\mu\nu}^a D^2 F^{\mu\nu a} + d_g^3 \frac{1}{m_Q^2} g f_{abc} F_{\mu\nu}^a F_{\alpha}^{\mu b} F^{\nu\alpha c}$$

$$\mathcal{L}_\psi = \psi^\dagger \left( iD_0 + c_2 \frac{\mathbf{D}^2}{2m_Q} + c_4 \frac{\mathbf{D}^4}{8m_Q^3} + c_F g \frac{\boldsymbol{\sigma} \cdot \mathbf{B}}{2m_Q} + c_D g \frac{\mathbf{D} \cdot \mathbf{E} - \mathbf{E} \cdot \mathbf{D}}{8m_Q^2} \right. \\ \left. + i c_S g \frac{\boldsymbol{\sigma} \cdot (\mathbf{D} \times \mathbf{E} - \mathbf{E} \times \mathbf{D})}{8m_Q^2} \right) \psi$$

$$\mathcal{L}_\chi = c.c \text{ of } \mathcal{L}_\psi$$

$$\mathcal{L}_{\psi\chi} = \frac{f_1(^1S_0)}{m_Q^2} \psi^\dagger \chi \chi^\dagger \psi + \frac{f_1(^3S_1)}{m_Q^2} \psi^\dagger \boldsymbol{\sigma} \chi \chi^\dagger \boldsymbol{\sigma} \psi + \frac{f_8(^1S_0)}{m_Q^2} \psi^\dagger T^a \chi \chi^\dagger T^a \psi \\ + \frac{f_8(^3S_1)}{m_Q^2} \psi^\dagger T^a \boldsymbol{\sigma} \chi \chi^\dagger T^a \boldsymbol{\sigma} \psi$$

There are still simplifications that are not obvious from NRQCD.



Thermal effects are going to see the bound state as a color dipole.

$$\begin{aligned} \mathcal{L}_{pNRQCD} = & \int d^3\mathbf{r} \text{Tr} \left[ S^\dagger (i\partial_0 - h_s) S \right. \\ & \left. + O^\dagger (iD_0 - h_o) O \right] + V_A(r) \text{Tr}(O^\dagger \mathbf{r} g \mathbf{E} S + S^\dagger \mathbf{r} g \mathbf{E} O) \\ & + \frac{V_B(r)}{2} \text{Tr}(O^\dagger \mathbf{r} g \mathbf{E} O + O^\dagger O \mathbf{r} g \mathbf{E}) + \mathcal{L}_g + \mathcal{L}_q \end{aligned}$$

- Gives the same results as QCD and NRQCD for Green functions evaluated at distances much bigger than  $r$ .
- The matching between NRQCD and pNRQCD can be done perturbatively if  $\frac{1}{r} \gg \Lambda_{QCD}$ .
- The degrees of freedom for the heavy quarks are now a color singlet field and a color octet field.
- Using pNRQCD provides automatically with a Coulomb resummation.



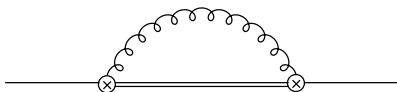
## From $pNRQCD$ to $pNRQCD_{HTL}$

Now we take into account thermal effects. For this we integrate out degrees of freedom with virtuality of order  $T^2$  and we go from  $pNRQCD$  to a new EFT  $pNRQCD_{HTL}$ .

- In the gluons and light quarks sector of  $pNRQCD_{HTL}$  we will have the usual Hard Thermal Loop action.
- The potential of the singlet and the octet will have thermal corrections

## Integrating out the $T$ scale, Leading order in $\alpha_s$

Now we take into thermal effects into the singlet potential



$$-ig^2 C_F \frac{r^i}{D-1} \mu^{4-D} \int \frac{d^D k}{(2\pi)^D} \frac{i}{E - h_o - k_0 + i\eta} [k_0^2 D_{ii}(k_0, k) + k^2 D_{00}(k_0, k)] r^i$$

All the thermal bath information is encoded in the gluon propagator  $D$ .

## Integrating out the $T$ scale, Leading order in $\alpha_s$

Because  $T \gg E$  we must expand the octet propagator

$$\frac{1}{E - h_o - k_0 + i\eta} = \frac{1}{-k_0 + i\eta} - \frac{E - h_o}{(-k_0 + i\eta)^2} + \dots$$

It is a polynomial in  $(E - h_o)$

$$E - h_o = E - h_s - (V_o - V_s) = E - h_s - \Delta V$$

- If we only take into account  $\Delta V = \frac{N_c \alpha_s}{2r}$  we are doing the static limit.
- If we only take into account  $E - h_s$  up to trivial color factors we are doing the QED case.

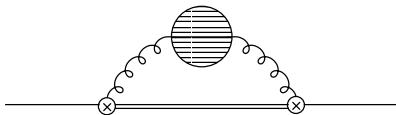
## Integrating out the $T$ scale, Leading order in $\alpha_s$

$$\delta V_S = \frac{\pi}{9} N_c C_F \alpha_s^2 T^2 r + \frac{2\pi}{3m} C_F \alpha_s T^2 + \frac{\alpha_s C_F I_T}{3\pi} \left[ -\frac{N_c^3 \alpha_s^3}{8 r} - \frac{N_c(N_c+2C_F)\alpha_s^2}{mr^2} + \frac{4(N_c-2C_F)\pi\alpha_s}{m^2} \delta^3(\mathbf{r}) + N_c \frac{\alpha_s}{m^2} \left\{ \nabla_{\mathbf{r}}^2, \frac{1}{r} \right\} \right]$$

There is an infrared divergence

$$I_T = \frac{2}{\epsilon} + \ln \frac{T^2}{\mu^2} - \gamma_E + \ln(4\pi) - \frac{5}{3}$$

## Integrating out the $T$ scale, next to leading order in $\alpha_s$



$$\begin{aligned} \delta V_s^{(2\text{ loops})} = & -\frac{3}{2}\zeta(3) C_F \frac{\alpha_s}{\pi} r^2 T m_D^2 + \frac{2}{3}\zeta(3) N_c C_F \alpha_s^2 r^2 T^3 \\ + i \left[ \frac{C_F}{6} \alpha_s r^2 T m_D^2 \left( -\frac{2}{\epsilon} + \gamma_E + \ln \pi - \ln \frac{T^2}{\mu^2} + \frac{2}{3} - 4 \ln 2 - 2 \frac{\zeta'(2)}{\zeta(2)} \right) \right. \\ & \left. + \frac{4\pi}{9} \ln 2 N_c C_F \alpha_s^2 r^2 T^3 \right] \end{aligned}$$

This contribution was first found in the static limit by Brambilla, Ghiglieri, Petreczky and Vairo.

# Computations in the $m\alpha_s^2$ scale

- Because  $T \gg m\alpha_s^2$

$$\frac{1}{e^{\beta k} - 1} \rightarrow \frac{T}{k} - \frac{1}{2} + \dots$$

- For gluons with  $k_0 \sim m\alpha_s^2$  and virtuality  $\Lambda^2 \sim (m\alpha_s^2)^2$  the HTL Lagrangian has to be taken into account but does not need to be resummed. We call this the **off-shell region**.
- For gluons with  $k_0 \sim m\alpha_s^2$  but virtuality  $\Lambda^2 \lesssim m_D^2$  the HTL Lagrangian has to be resummed. We call this the **collinear region**.
- The results coming from this energy scale can not be reproduced by a potential.

## Contribution from the $m\alpha_s^2$ scale

$$\delta E_{n,l} = -\frac{\pi\alpha_s C_F T m_D^2 a_0^2 n^2}{3} [5n^2 + 1 - 3l(l+1)]$$

$a_0$  is the Bohr radius of the fundamental state.

$$\begin{aligned} \delta\Gamma_{n,l} = & \frac{1}{3} N_c^2 C_F \alpha_s^3 T - \frac{16}{3m} C_F \alpha_s T E_n + \frac{8}{3} N_c C_F \alpha_s^2 T \frac{1}{mn^2 a_0} \\ & + \frac{2E_n \alpha_s^3}{3} \left\{ \frac{4C_F^3 \delta_{l0}}{n} + N_c C_F^2 \left( \frac{8}{n(2l+1)} - \frac{1}{n^2} - \frac{2\delta_{l0}}{n} \right) + \frac{2N_c^2 C_F}{n(2l+1)} + \frac{N_c^3}{4} \right\} \\ & - \frac{\alpha_s C_F T m_D^2}{6} \left( \frac{2}{\epsilon} + \ln \frac{E_1^2}{\mu^2} + \gamma_E - \frac{11}{3} - \ln \pi + \ln 4 \right) a_0^2 n^2 [5n^2 + 1 - 3l(l+1)] \\ & + \frac{2\alpha_s C_F T m_D^2}{3} \frac{C_F^2 \alpha_s^2}{E_n^2} I_{n,l} \end{aligned}$$

$$I_{n,l} = \frac{E_n^2}{C_F^2 \alpha_s^2} \int \frac{d^3 k}{(2\pi)^3} |\langle n, l | \mathbf{r} | \mathbf{k} \rangle|^2 \ln \frac{E_1}{E_n - k^2/m}$$

## Contribution from the $m\alpha_s^2$ scale. Comments

At  $T = 0$  the  $c_D$  coefficient from NRQCD has an IR divergence.

$\delta E^{US}|_{T=0}$  has an UV divergence.

Both cancel out.

At finite  $T$  some of the corrections to the potential in  $pNRQCD_{HTL}$  can be encoded in a correction to  $c_D$  so that it is IR safe. The  $V_s$  potential has an IR divergence proportional to  $T^3$ .

$\delta E^{US} = \delta E^{US}|_{T=0} + \delta E^{US}|_T$  has only an UV divergence proportional to  $T^3$ .

Both cancel out.



Final result.  $m\alpha_s \gg T \gg m\alpha_s^2 \gg m_D$

Sum of all thermal bath induced terms. (Non-thermally induced terms coming from the  $m\alpha_s^2$  scale are subtracted).

$$\begin{aligned} \delta E_{n,l}^{(\text{thermal})} = & \frac{\pi}{9} N_c C_F \alpha_s^2 T^2 \frac{a_0}{2} [3n^2 - l(l+1)] + \frac{\pi}{3} C_F^2 \alpha_s^2 T^2 a_0 \\ & + \frac{E_n \alpha_s^3}{3\pi} \left[ \log \left( \frac{2\pi T}{E_1} \right)^2 - 2\gamma_E \right] \left\{ \frac{4C_F^3 \delta_{l0}}{n} + N_c C_F^2 \left[ \frac{8}{n(2l+1)} - \frac{1}{n^2} - \frac{2\delta_{l0}}{n} \right] \right. \\ & \left. + \frac{2N_c^2 C_F}{n(2l+1)} + \frac{N_c^3}{4} \right\} \\ & + \frac{2E_n C_F^3 \alpha_s^3}{3\pi} L_{n,l} \\ & + \frac{a_0^2 n^2}{2} [5n^2 + 1 - 3l(l+1)] \left\{ - \left[ \frac{3}{2\pi} \zeta(3) + \frac{\pi}{3} \right] C_F \alpha_s T m_D^2 \right. \\ & \left. + \frac{2}{3} \zeta(3) N_c C_F \alpha_s^2 T^3 \right\} \end{aligned}$$

where  $E_n = -\frac{mC_F^2 \alpha_s^2}{4n^2}$ ,  $a_0 = \frac{2}{mC_F \alpha_s}$  and  $L_{n,l}$  is the Bethe logarithm.

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For a general number of colors  $N_c$  ( $C_F = (N_c^2 - 1)/(2N_c)$ ):

$$\delta E_{n,l}^{(\text{thermal})} = \frac{\pi}{9} N_c C_F \alpha_s^2 T^2 \frac{a_0}{2} [3n^2 - l(l+1)] + \frac{\pi}{3} C_F^2 \alpha_s^2 T^2 a_0 \quad \sim m\alpha_s^5 \frac{T^2}{E^2}$$

$$m\alpha_s^5 \sim \left\{ \begin{array}{l} + \frac{E_n \alpha_s^3}{3\pi} \left[ \log \left( \frac{2\pi T}{E_1} \right)^2 - 2\gamma_E \right] \left\{ \frac{4C_F^3 \delta_{l0}}{n} + N_c C_F^2 \left[ \frac{8}{n(2l+1)} - \frac{1}{n^2} - \frac{2\delta_{l0}}{n} \right] \right. \\ \left. + \frac{2N_c^2 C_F}{n(2l+1)} + \frac{N_c^3}{4} \right\} \\ + \frac{2E_n C_F^3 \alpha_s^3}{3\pi} L_{n,l} \end{array} \right.$$

$$m\alpha_s^6 \frac{T^3}{E^3} \sim + \frac{a_0^2 n^2}{2} [5n^2 + 1 - 3l(l+1)] \left\{ - \left[ \frac{3}{2\pi} \zeta(3) + \frac{\pi}{3} \right] C_F \alpha_s T m_D^2 + \frac{2}{3} \zeta(3) N_c C_F \alpha_s^2 T^3 \right\}$$

where  $E_n = -\frac{mC_F^2 \alpha_s^2}{4n^2}$ ,  $a_0 = \frac{2}{mC_F \alpha_s}$  and  $L_{n,l}$  is the Bethe logarithm.

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$$\begin{aligned} \Gamma_{n,l}^{(\text{thermal})} = & \frac{1}{3} N_c^2 C_F \alpha_s^3 T + \frac{4}{3} \frac{C_F^2 \alpha_s^3 T}{n^2} (C_F + N_c) \\ & + \frac{2E_n \alpha_s^3}{3} \left\{ \frac{4C_F^3 \delta_{l0}}{n} + N_c C_F^2 \left[ \frac{8}{n(2l+1)} - \frac{1}{n^2} - \frac{2\delta_{l0}}{n} \right] + \frac{2N_c^2 C_F}{n(2l+1)} + \frac{N_c^3}{4} \right\} \\ & - \left[ \frac{C_F}{6} \alpha_s T m_D^2 \left( \ln \frac{E_1^2}{T^2} + 2\gamma_E - 3 - \log 4 - 2 \frac{\zeta'(2)}{\zeta(2)} \right) + \frac{4\pi}{9} \ln 2 N_c C_F \alpha_s^2 T^3 \right] \\ & \quad \times a_0^2 n^2 [5n^2 + 1 - 3l(l+1)] \\ & + \frac{8}{3} C_F \alpha_s T m_D^2 a_0^2 n^4 I_{n,l} \end{aligned}$$

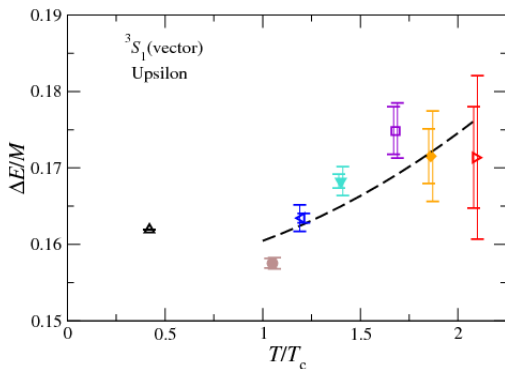
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$$\begin{aligned}
 m\alpha_s^5 &\sim \Gamma_{n,l}^{(\text{thermal})} = \frac{1}{3} N_c^2 C_F \alpha_s^3 T + \frac{4}{3} \frac{C_F^2 \alpha_s^3 T}{n^2} (C_F + N_c) \sim m\alpha_s^5 \frac{T}{E} \\
 &\quad + \frac{2E_n \alpha_s^3}{3} \left\{ \frac{4C_F^3 \delta_{l0}}{n} + N_c C_F^2 \left[ \frac{8}{n(2l+1)} - \frac{1}{n^2} - \frac{2\delta_{l0}}{n} \right] \right\} + \frac{2N_c^2 C_F}{n(2l+1)} + \frac{N_c^3}{4} \\
 m\alpha_s^6 \frac{T^3}{E^3} &\sim \left\{ - \left[ \frac{C_F}{6} \alpha_s T m_D^2 \left( \ln \frac{E_1^2}{T^2} + 2\gamma_E - 3 - \log 4 - 2 \frac{\zeta'(2)}{\zeta(2)} \right) + \frac{4\pi}{9} \ln 2 N_c C_F \alpha_s^2 T^3 \right] \right. \\
 &\quad \left. \times a_0^2 n^2 [5n^2 + 1 - 3l(l+1)] + \frac{8}{3} C_F \alpha_s T m_D^2 a_0^2 n^4 I_{n,l} \right\}
 \end{aligned}$$

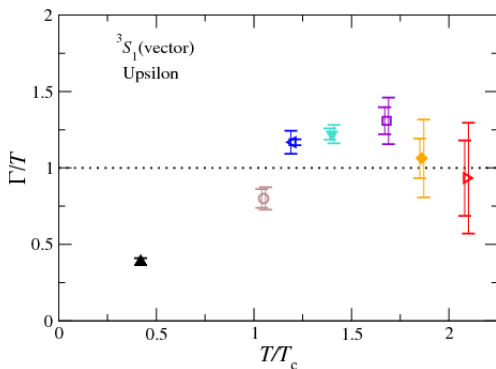
## Check results, compare with lattice

Comparison of MEM lattice computation (Aarts, Allton, Kim, Lombardo, Oktay, Ryan, Sinclair and Skullerud (2011)) with our computations in the  $1/r \gg T \gg E \gg m_D$  regime fitting  $\alpha_s$ .



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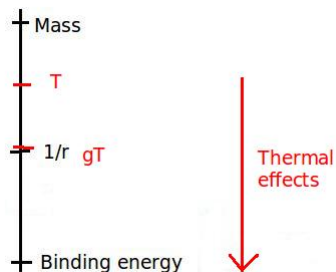
# Conclusions

- For this temperature we can reach a high precision. Order  $m\alpha_s^5$  in the energy and decay width.
- This can be interesting for bottomonium. Above the dissociation temperature of charmonium but below the one of bottomonium.
- This temperature is above  $T_c$  so perturbation theory might be reliable.

- $m \gg T \gg \frac{1}{r} \sim gT$ . Dissociation temperature.

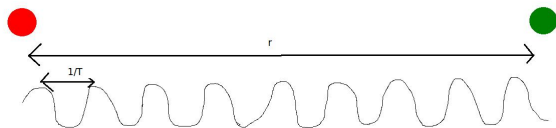


# Thermal effects



Now we can start with NRQCD Lagrangian at  $T = 0$ . Thermal effects can be included in a new EFT called  $NRQCD_{HTL}$ .

# Thermal effects



- Effects at the energy scale  $T$  are going to see heavy quarks as elements that are very far away from each other.
- We will have to average this thermal fluctuations in the gluons that are interchanged by the heavy quarks.

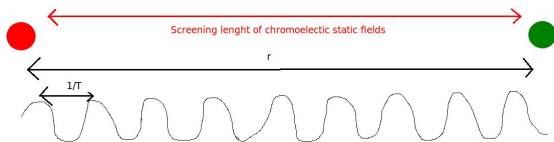
- We will have HTL corrections in the gluon and light quarks propagators. In fact, this is going to be the more relevant change for bound states phenomenology.
- NLO corrections to heavy quark sector.

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- NLO corrections to heavy quark sector.

Why is it NLO?

- In the Coulomb gauge at the scale  $T$ , only the spatial gluons are thermalized:  $A_j$ .
- In this gauge  $A_0$  is not modified by the temperature at LO up to the scale  $gT$ .
- The coupling of heavy quarks with  $A_j$  is always multiplied at least by one power of  $\frac{1}{m_Q}$ .

# $NRQCD_{HTL} \rightarrow pNRQCD_{HTL}$



- After averaging thermal fluctuations we find HTL propagator.
- This HTL modification is a leading order effect in the  $A_0$  field at distances  $r$  because  $\frac{1}{r} \sim m_D$ .
- The LO potential is going to be modified, and this can break the bound state.

The potential at  $m \gg T \gg m\alpha_s$

$$V(r) = -\frac{\alpha_s e^{-m_D r}}{r} - \alpha_s m_D + \frac{i16\alpha_s^2 C_F T^3}{\pi m_D^2} \left( \frac{\pi^2 (m_D^{lq})^2}{4T^2 g^2} + g(m_c \beta) + \frac{m_c^2}{2T^2 (e^{\beta m_c} + 1)} \right) \phi(m_D r),$$

- We consider the effect of the charm mass that can be important for bottomonium. The  $m_c \rightarrow 0$  result was first found by Laine, Philipsen, Romatschke and Tassler.
- $m_D^{lq}$  is the Debye mass that is found in the  $m_c \rightarrow \infty$  limit.
- $g(0) = \frac{\pi^2}{12}$  and goes exponentially to zero at large values of  $m_c \beta$ .

$$\phi(x) = 2 \int_0^\infty \frac{dz z}{(z^2 + 1)^2} \left[ \frac{\sin(zx)}{zx} - 1 \right]$$

# The dissociation temperature

- The temperature when the imaginary part of the potential is of the same order of magnitude as the real part is lower than the temperature where screening is important for bound states (in the limit of weak coupling).
- If both screening and dissipation are a perturbation the bound state survives.
- If the imaginary part of the potential is bigger than the real part then the bound state does not exist anymore.
- It is natural then to propose as dissociation temperature the temperature where the real part of the potential is as big as the imaginary part.

$$\frac{1}{a_0^3} = 16\alpha_s(\pi T)C_F T^3 \left( \frac{\pi^2(m_D^{lq})^2}{4T^2g^2} + g(m_c\beta) + \frac{m_c^2}{2T^2(e^{\beta m_c} + 1)} \right).$$

# Dissociation temperature for charmonium

Assuming  $g$  small and  $\frac{1}{a_0} \gg m_D$ . For  $J/\psi$

$\alpha_s$	$T_d$ (MeV)
$\alpha_s(\pi T)$	230
$\alpha_s(2\pi T)$	280

Too close to  $T_c$ ?



# Dissociation temperature for bottomonium

For  $\Upsilon(1S)$

$\alpha_s$	$T_d$ (MeV)
$\alpha_s(\pi T)$	440
$\alpha_s(2\pi T)$	500

Compatible with recent Lattice calculations.

For example, Aarts et al. in 2010 found that  $T_d > 2.1 T_c$ .

# Dependence of bottomonium dissociation with charm mass

$m_c$ (MeV)	$T_d$ (MeV)
$\infty$	480
5000	480
2500	460
1200	440
0	420

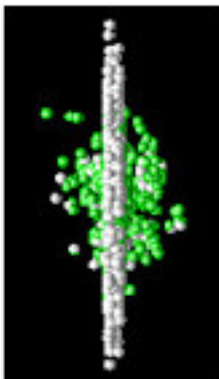
**Table:** Dissociation temperature for Upsilon (1S) for different values of the charm mass

# Conclusions

- The dissociation temperature is found when the temperature is much higher than the inverse of the typical radius.
- In the limit of  $g \rightarrow 0$  the dominant dissociation mechanism is the imaginary part of the potential.
- The results found in this approximation are not very far away from Lattice results, although  $g$  is not so small.

# Asymmetry

# Motivation



Initial state is very asymmetric, clearly a preferred direction.

# Different temperature regimes

- $T \gg 1/r \sim m_D$   
Already done. Burnier, Laine and Vepsalainen. Dumitru, Guo and Strickland. Philipsen and Tassler.
- $T \sim 1/r$  or  $1/r \gg T \gg m_D \gg E$   
Too difficult. For the future. Need computation of vacuum polarization in an asymmetric plasma with  $T \sim \mathbf{k} \gg k_0$ .
- $1/r \gg T \gg E \gg m_D$   
Explained here. Relevant for  $\Upsilon$ .

# The distribution function

Instead of thermal distribution functions

$$F\left(\frac{q}{T}\right)$$

We use

$$F\left(\frac{\sqrt{q_{\perp}^2 + \xi q_z^2}}{T}\right)$$

$z$  is a preferred direction. Other choices used in the bibliography can be done by redefining  $T$ .

# Outline of the computation

- Start with pNRQCD Lagrangian.



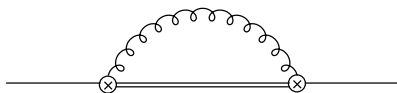
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# Outline of the computation

- Start with pNRQCD Lagrangian.
- Match pNRQCD to  $pNRQCD_{HTL}$ . Effects of the scale  $T$  encoded in a redefined potential.
- Do the computation of the effects of the scale  $E$  in  $pNRQCD_{HTL}$

# The diagram to compute



Structure

$$r^i r^j J^{ij}(T, E)$$

Decompose

$$J^{ij}(T, E) = \delta^{ij} F_1(T, E) + n^i n^j F_2(T, E)$$

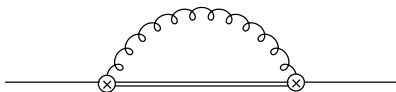
$n^i$  unit vector in  $z$  direction.

If  $\xi \rightarrow 0$  then  $F_2 \rightarrow 0$ .

## Matching $pNRQCD$ to $pNRQCD_{HTL}$

$$\delta V_s = \frac{\pi\alpha_s C_F T^2}{3} \left( \frac{2}{M} + \frac{N_c \alpha_s r}{4} + \frac{N_c \alpha_s (\mathbf{rn})^2}{4} \right) \frac{\tan^{-1}(\sqrt{\xi})}{\sqrt{\xi}} \\ + \frac{\pi\alpha_s^2 C_F N_c T^2}{12\xi r} (r^2 - 3(\mathbf{rn})^2) \left( 1 - \frac{\tan^{-1}(\sqrt{\xi})}{\sqrt{\xi}} \right)$$

## Contribution from scale $E$



Correction to the decay width

# Final result

Binding energy

$$\begin{aligned} \delta E = & \left( \frac{2\pi\alpha_s C_F T^2}{3M} + \frac{\pi\alpha_s^2 C_F N_c T^2 a_0^2 n^2}{18} [5n^2 + 1 - 3l(l+1)] \right) \frac{\tan^{-1}(\sqrt{\xi})}{\sqrt{\xi}} \\ & + \frac{\pi\alpha_s^2 C_F N_c T^2 a_0^2 n^2}{36} \langle 2l00|l0\rangle \langle 2l0m|lm\rangle [5n^2 + 1 - 3l(l+1)] \times \\ & \times \left( \frac{\tan^{-1}(\sqrt{\xi})}{\sqrt{\xi}} \left( 1 + \frac{3}{\xi} \right) - \frac{3}{\xi} \right) \end{aligned}$$

# Final result

Decay width

$$\begin{aligned} \Gamma_n = & \left( -\frac{16\alpha_s C_F T E_n}{3M} + \frac{8\alpha_s^2 C_F N_c T}{Mn^2 a_0} + \frac{\alpha_s^3 C_F N_c^2 T}{3} \right) \frac{\text{Sinh}^{-1}(\sqrt{\xi})}{\sqrt{\xi}} \\ & + \left( -\frac{4\alpha_s C_F T E_n}{M} - \frac{\alpha^2 C_F N_c T}{Mn^2 a_0} + \frac{\alpha_s^3 C_F N_c^2 T}{4} \right) \langle 2100|10\rangle \langle 210m|lm\rangle \times \\ & \times \left[ \frac{\left(1 + \frac{2\xi}{3}\right) \text{Sinh}^{-1}(\sqrt{\xi}) - \sqrt{\xi}\sqrt{1+\xi}}{\xi^{3/2}} \right] \end{aligned}$$

# Conclusions

- We are doing advances in understanding what happens out of equilibrium.
- The asymmetry in the regime  $T \gg m_D \sim \frac{1}{r}$  has been studied by others authors. With EFT we can understand  $\frac{1}{r} \gg T \gg E \gg m_D$ .
- Missing regimes will be understood when we have the gluon polarization in an asymmetric plasma (not in HTL approximation).