

# Axions in Particle Physics.

**Andreas Ringwald**

Annual Retreat of GRK and PRISMA  
Kloster Johannisberg, D  
20 September 2017

# Strong Case for Physics Beyond the Standard Model

- > Discovery of Higgs boson marks completion of SM particle content

Drei Generationen der Materie (Fermionen)

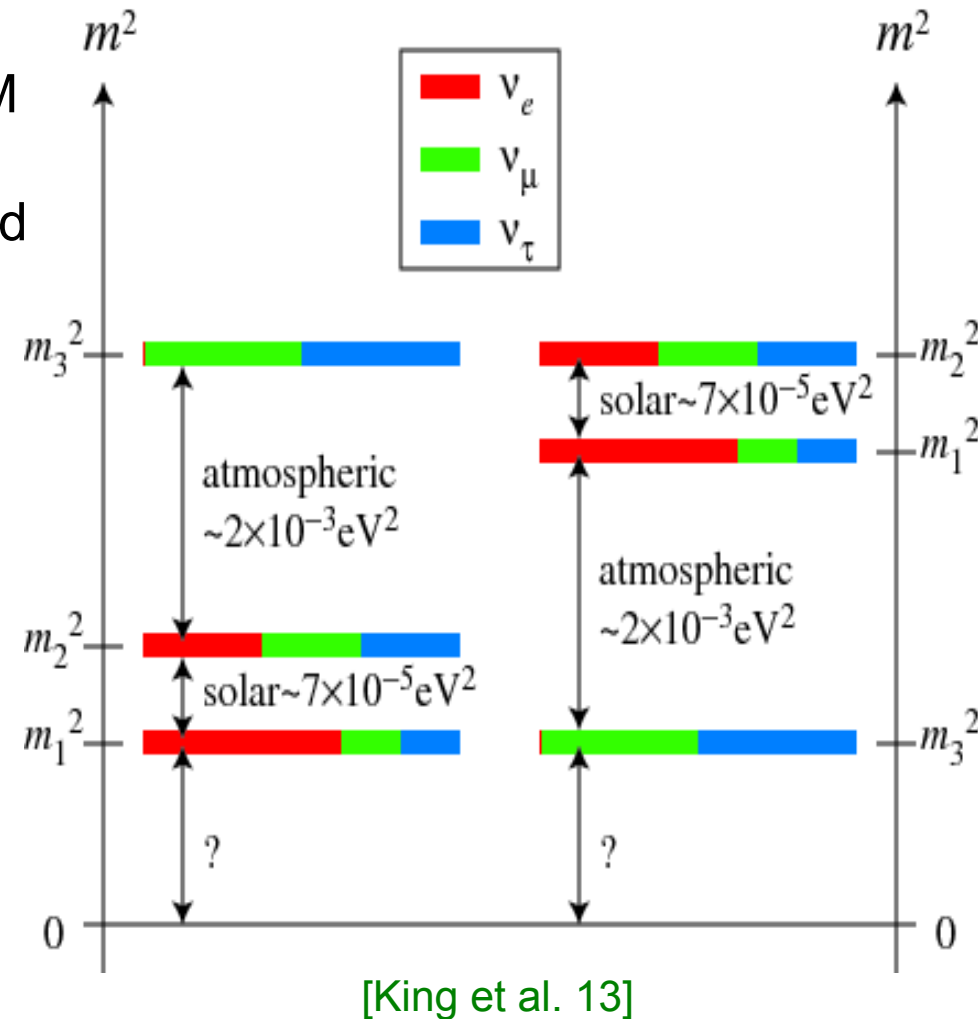
	I	II	III		
Masse →	2,3 MeV	1,275 GeV	173,07 GeV	0	125,9 GeV
Ladung →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	0
Spin →	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	0
Name →	<b>u</b> up	<b>c</b> charm	<b>t</b> top	<b>γ</b> Photon	<b>H</b> Higgs Boson
				0	
	4,8 MeV	95 MeV	4,18 GeV	0	
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
<b>Quarks</b>	<b>d</b> down	<b>s</b> strange	<b>b</b> bottom	<b>g</b> Gluon	
	<2 eV	<0,19 MeV	<18.2 MeV	91,2 GeV	
	0	0	0	0	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
	<b>ν<sub>e</sub></b> Elektron-Neutrino	<b>ν<sub>μ</sub></b> Myon-Neutrino	<b>ν<sub>τ</sub></b> Tau-Neutrino	<b>Z<sup>0</sup></b> Z Boson	
	0,511 MeV	105,7 MeV	1,777 GeV	80,4 GeV	
	-1	-1	-1	±1	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
<b>Leptonen</b>	<b>e</b> Elektron	<b>μ</b> Myon	<b>τ</b> Tau	<b>W<sup>±</sup></b> W Boson	<b>Eichbosonen</b>

[wikipedia]



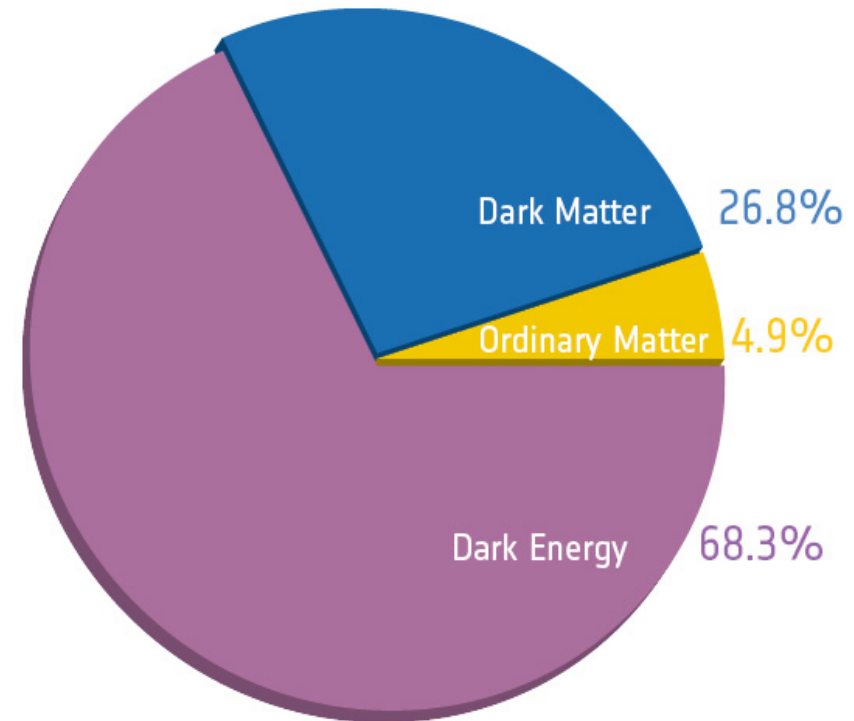
# Strong Case for Physics Beyond the Standard Model

- > Discovery of Higgs boson marks completion of SM particle content
- > Strong case for physics beyond SM (BSM) suggested by observations in particle physics, astrophysics and cosmology
  - Neutrino flavour oscillations



# Strong Case for Physics Beyond the Standard Model

- > Discovery of Higgs boson marks completion of SM particle content
- > Strong case for physics beyond SM (BSM) suggested by observations in particle physics, astrophysics and cosmology
  - Neutrino flavour oscillations
  - Dark matter

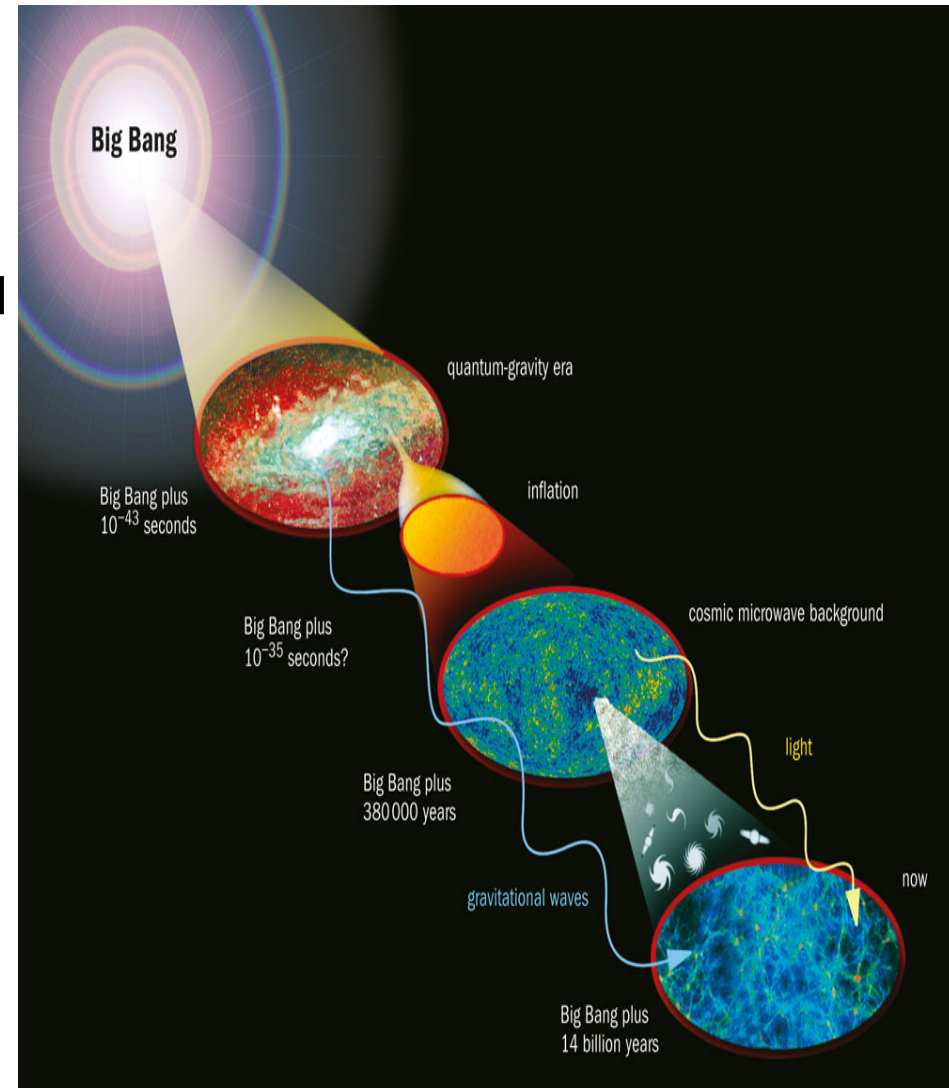


[PLANCK]



# Strong Case for Physics Beyond the Standard Model

- Discovery of Higgs boson marks completion of SM particle content
- Strong case for physics beyond SM (BSM) suggested by observations in particle physics, astrophysics and cosmology
  - Neutrino flavour oscillations
  - Dark matter
  - Inflation
  - Baryon asymmetry

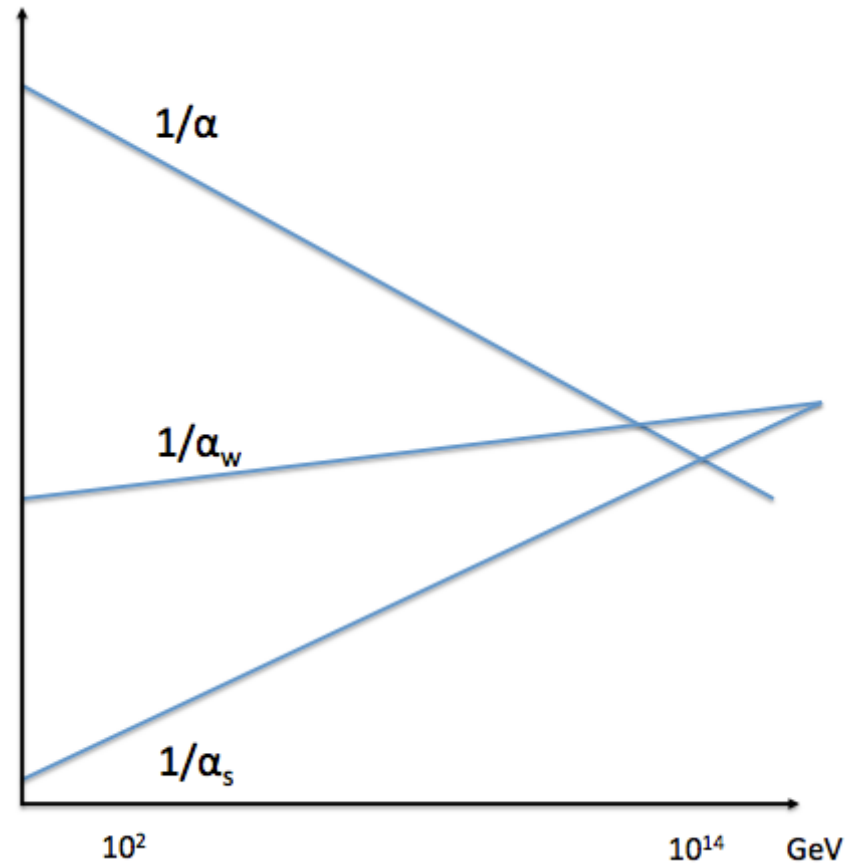


[[physicsworld.com](http://physicsworld.com)]



# Strong Case for Physics Beyond the Standard Model

- > Discovery of Higgs boson marks completion of SM particle content
- > Strong case for physics beyond SM (BSM) suggested by observations in particle physics, astrophysics and cosmology
  - Neutrino flavour oscillations
  - Dark matter
  - Inflation
  - Baryon asymmetry
  - Unification?
  - Naturalness?
    - Cosmological constant (dark energy)
    - Hierarchy between weak scale and Planck scale
    - Non-observation of strong CP violation



[StackExchange]



# Topological Theta Term and Strong CP Problem

> Most general gauge invariant Lagrangian of QCD:

$$\mathcal{L}_{\text{QCD}} = -\frac{1}{4} G_{\mu\nu}^a G^{a,\mu\nu} + \bar{q} (i\gamma_\mu D^\mu - \mathcal{M}_q) q - \frac{\alpha_s}{8\pi} \theta G_{\mu\nu}^a \tilde{G}^{a,\mu\nu}$$

- Parameters: strong coupling  $\alpha_s$ , quark masses  $\mathcal{M}_q = \text{diag}(m_u, m_d, \dots)$  and theta angle  $\theta$  [Belavin et al. '75; 't Hooft '76; Callan et al. '76; Jackiw, Rebbi '76]



# Topological Theta Term and Strong CP Problem

- > Most general gauge invariant Lagrangian of QCD:

$$\mathcal{L}_{\text{QCD}} = -\frac{1}{4} G_{\mu\nu}^a G^{a,\mu\nu} + \bar{q} (i\gamma_\mu D^\mu - \mathcal{M}_q) q - \frac{\alpha_s}{8\pi} \theta G_{\mu\nu}^a \tilde{G}^{a,\mu\nu}$$

- Parameters: strong coupling  $\alpha_s$ , quark masses  $\mathcal{M}_q = \text{diag}(m_u, m_d, \dots)$  and theta angle  $\theta$  [Belavin et al. '75; 't Hooft '76; Callan et al. '76; Jackiw, Rebbi '76]

- > Topological theta term  $\propto G_{\mu\nu}^a \tilde{G}^{a,\mu\nu} \propto \mathbf{E}^a \cdot \mathbf{B}^a$  violates P and T, and thus CP





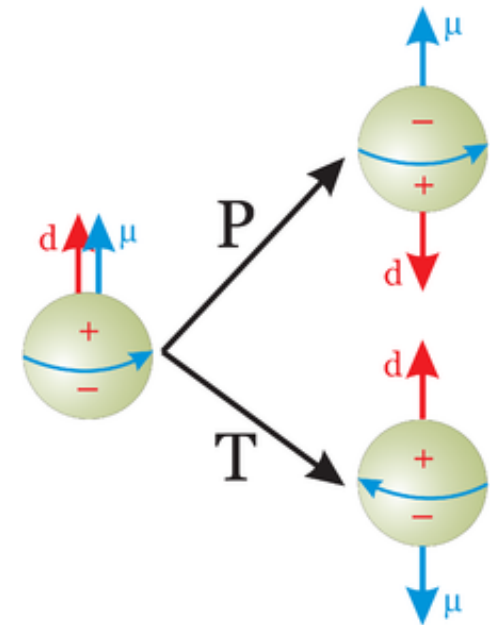
# Topological Theta Term and Strong CP Problem

- > Most general gauge invariant Lagrangian of QCD:

$$\mathcal{L}_{\text{QCD}} = -\frac{1}{4} G_{\mu\nu}^a G^{a,\mu\nu} + \bar{q} (i\gamma_\mu D^\mu - \mathcal{M}_q) q - \frac{\alpha_s}{8\pi} \theta G_{\mu\nu}^a \tilde{G}^{a,\mu\nu}$$

- Parameters: strong coupling  $\alpha_s$ , quark masses  $\mathcal{M}_q = \text{diag}(m_u, m_d, \dots)$  and theta angle  $\theta$  [Belavin et al. '75; 't Hooft 76; Callan et al. '76; Jackiw, Rebbi '76]

- > Topological theta term  $\propto G_{\mu\nu}^a \tilde{G}^{a,\mu\nu} \propto \mathbf{E}^a \cdot \mathbf{B}^a$  violates P and T, and thus CP
- > Most sensitive probe of P and T violation in flavor conserving interactions: electric dipole moment of neutron



# Topological Theta Term and Strong CP Problem

- > Most general gauge invariant Lagrangian of QCD:

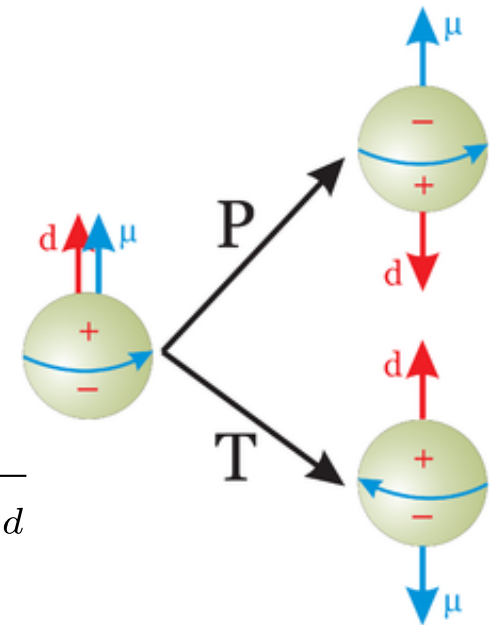
$$\mathcal{L}_{\text{QCD}} = -\frac{1}{4} G_{\mu\nu}^a G^{a,\mu\nu} + \bar{q} (i\gamma_\mu D^\mu - \mathcal{M}_q) q - \frac{\alpha_s}{8\pi} \theta G_{\mu\nu}^a \tilde{G}^{a,\mu\nu}$$

- Parameters: strong coupling  $\alpha_s$ , quark masses  $\mathcal{M}_q = \text{diag}(m_u, m_d, \dots)$  and theta angle  $\theta$  [Belavin et al. '75; 't Hooft 76; Callan et al. '76; Jackiw, Rebbi '76]

- > Topological theta term  $\propto G_{\mu\nu}^a \tilde{G}^{a,\mu\nu} \propto \mathbf{E}^a \cdot \mathbf{B}^a$  violates P and T, and thus CP

- > Most sensitive probe of P and T violation in flavor conserving interactions: electric dipole moment of neutron; prediction:

$$d_n \sim e\theta \frac{m_*}{m_n^2} \sim 6 \times 10^{-17} \theta \text{ e cm}; \quad m_* = \frac{m_u m_d}{m_u + m_d}$$



# Topological Theta Term and Strong CP Problem

- > Most general gauge invariant Lagrangian of QCD:

$$\mathcal{L}_{\text{QCD}} = -\frac{1}{4} G_{\mu\nu}^a G^{a,\mu\nu} + \bar{q} (i\gamma_\mu D^\mu - \mathcal{M}_q) q - \frac{\alpha_s}{8\pi} \theta G_{\mu\nu}^a \tilde{G}^{a,\mu\nu}$$

- Parameters: strong coupling  $\alpha_s$ , quark masses  $\mathcal{M}_q = \text{diag}(m_u, m_d, \dots)$  and theta angle  $\theta$  [Belavin et al. '75; 't Hooft 76; Callan et al. '76; Jackiw, Rebbi '76]

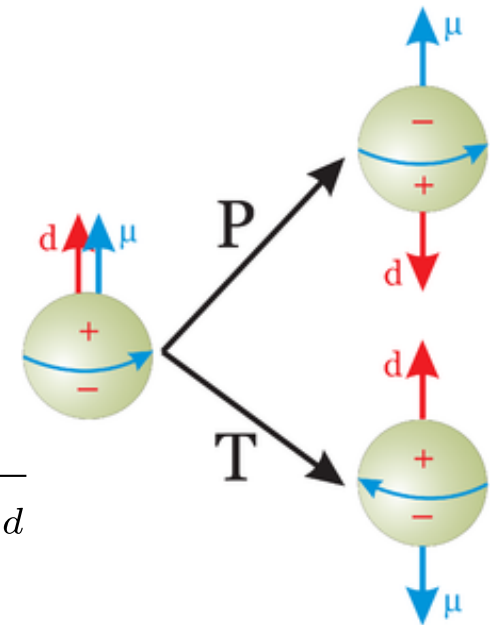
- > Topological theta term  $\propto G_{\mu\nu}^a \tilde{G}^{a,\mu\nu} \propto \mathbf{E}^a \cdot \mathbf{B}^a$  violates P and T, and thus CP

- > Most sensitive probe of P and T violation in flavor conserving interactions: electric dipole moment of neutron; prediction:

$$d_n \sim e\theta \frac{m_*}{m_n^2} \sim 6 \times 10^{-17} \theta \text{ e cm}; \quad m_* = \frac{m_u m_d}{m_u + m_d}$$

- > Experiment: [Baker et al. 06]

$$|d_n| < 2.9 \times 10^{-26} \text{ e cm} \Rightarrow |\theta| < 10^{-9}$$



# Topological Theta Term and Strong CP Problem

- > Naturalness?
  1. Cosmological constant (dark energy)
  2. Hierarchy between weak scale and Planck scale
  3. Non-observation of strong CP violation
- > 1. and 2. can be „solved“ by anthropic selection in multiverse
- > Fails for 3!
  - No anthropic argument for  $|\theta| < 10^{-9}$
- > Dynamical solution of 3. most required!



[Quantamagazine]

# Topological Theta Term and Strong CP Problem

> If  $\theta$  were a dynamical field, its vacuum expectation value would be zero.  
Correspondingly: strong CP problem solved

- Partition function in terms of Fourier series of Euclidean path integrals over gauge fields with fixed topological charge

$$Z(\theta) = \sum_{Q=-\infty}^{+\infty} \exp[i\theta Q] Z_Q, \quad Q = \int d^4x \frac{\alpha_s}{8\pi} G_{\mu\nu}^b \tilde{G}^{b,\mu\nu} \equiv \int d^4x q(x)$$

$$Z_Q = \int_Q [dG][dq][d\bar{q}] \exp \left[ - \int d^4x \left\{ \frac{1}{4} G_{\mu\nu}^a G_{\mu\nu}^a + i\bar{q}\gamma_\mu D_\mu q - \bar{q}_R \mathcal{M} q_L - \bar{q}_L \mathcal{M}^\dagger q_R \right\} \right]$$

- $Z_Q$  positive
- Vacuum energy density in QCD

$$\epsilon_0(\theta) \equiv -\frac{1}{\mathcal{V}} \ln \left[ \frac{Z(\theta)}{Z(0)} \right], \quad -\pi \leq \theta \leq \pi$$

has absolute minimum at  $\theta = 0$

[Vafa, Witten '84]



# Topological Theta Term and Strong CP Problem

➤ If  $\theta$  were a dynamical field, its vacuum expectation value would be zero. Correspondingly: strong CP problem solved

- Partition function in terms of Fourier series of Euclidean path integrals over gauge fields with fixed topological charge

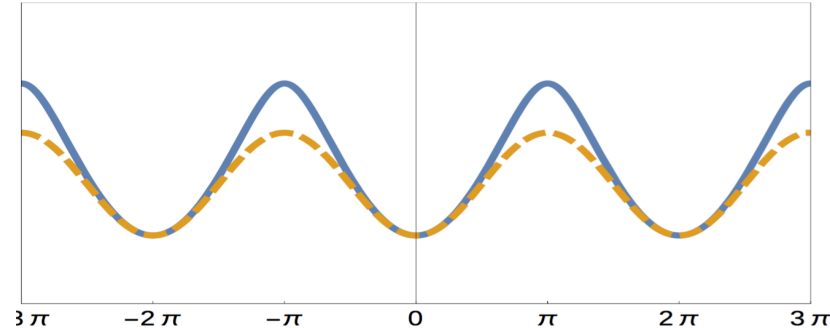
$$Z(\theta) = \sum_{Q=-\infty}^{+\infty} \exp[i\theta Q] Z_Q, \quad Q = \int d^4x \frac{\alpha_s}{8\pi} G_{\mu\nu}^b \tilde{G}^{b,\mu\nu} \equiv \int d^4x q(x)$$

$$Z_Q = \int_Q [dG][dq][d\bar{q}] \exp \left[ - \int d^4x \left\{ \frac{1}{4} G_{\mu\nu}^a G_{\mu\nu}^a + i\bar{q}\gamma_\mu D_\mu q - \bar{q}_R \mathcal{M} q_L - \bar{q}_L \mathcal{M}^\dagger q_R \right\} \right]$$

- $Z_Q$  positive
- Vacuum energy density in QCD

$$\epsilon_0(\theta) \equiv -\frac{1}{\mathcal{V}} \ln \left[ \frac{Z(\theta)}{Z(0)} \right], \quad -\pi \leq \theta \leq \pi$$

has absolute minimum at  $\theta = 0$



➤ Chiral EFT allows to calculate vacuum energy density: [Grilli di Cortona et al. '16]

$$\epsilon_0(\theta) \simeq m_\pi^2 f_\pi^2 \left[ 1 - \frac{\sqrt{m_u^2 + m_d^2 + 2m_u m_d \cos \theta}}{m_u + m_d} \right]$$

[Di Vecchia, Veneziano '80]



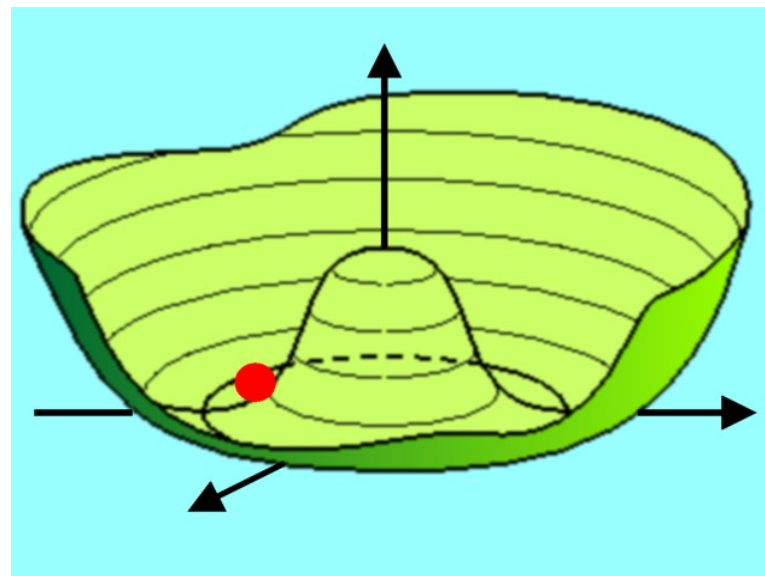
# Axionic Solution of Strong CP Problem

➤ A singlet complex scalar field  $\sigma$  featuring a global  $U(1)_{PQ}$  symmetry is added to SM

➤ Symmetry is broken by vev  $\langle \sigma \rangle = v_{PQ}/\sqrt{2}$

$$\sigma(x) = \frac{1}{2} (v_{PQ} + \rho(x)) e^{iA(x)/v_{PQ}}$$

- Excitation of modulus:  $m_\rho \sim v_{PQ}$
- Excitation of angle: NGB  $m_A \ll v_{PQ}$



[Raffelt]

# Axionic Solution of Strong CP Problem

> A singlet complex scalar field  $\sigma$  featuring a global  $U(1)_{PQ}$  symmetry is added to SM

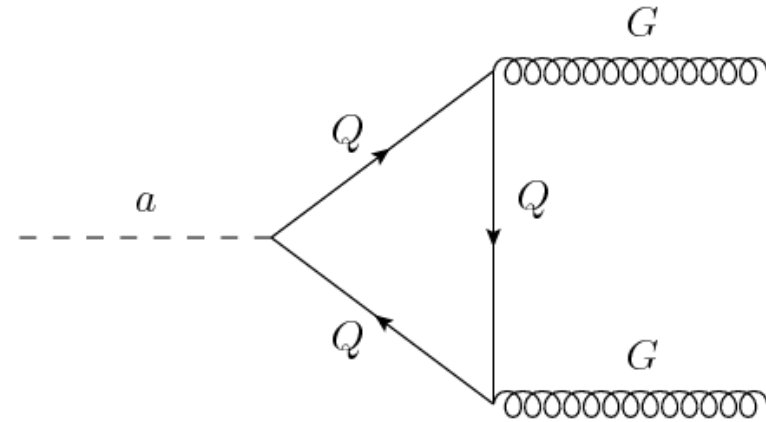
> Symmetry is broken by vev  $\langle \sigma \rangle = v_{PQ}/\sqrt{2}$

$$\sigma(x) = \frac{1}{2} (v_{PQ} + \rho(x)) e^{iA(x)/v_{PQ}}$$

- Excitation of modulus:  $m_\rho \sim v_{PQ}$
- Excitation of angle: NGB  $m_A \ll v_{PQ}$

> Quarks (SM or extra) carry PQ charges such that  $U(1)_{PQ}$  is anomalously broken due to gluonic triangle anomaly

$$\partial_\mu J_{U(1)_{PQ}}^\mu = -\frac{\alpha_s}{8\pi} N G_{\mu\nu}^a \tilde{G}^{a\mu\nu} - \frac{\alpha}{8\pi} E F_{\mu\nu} \tilde{F}^{\mu\nu}$$





# Axionic Solution of Strong CP Problem

> A singlet complex scalar field  $\sigma$  featuring a global  $U(1)_{PQ}$  symmetry is added to SM

> Symmetry is broken by vev  $\langle \sigma \rangle = v_{PQ}/\sqrt{2}$

$$\sigma(x) = \frac{1}{2} (v_{PQ} + \rho(x)) e^{iA(x)/v_{PQ}}$$

- Excitation of modulus:  $m_\rho \sim v_{PQ}$
- Excitation of angle: NGB  $m_A \ll v_{PQ}$

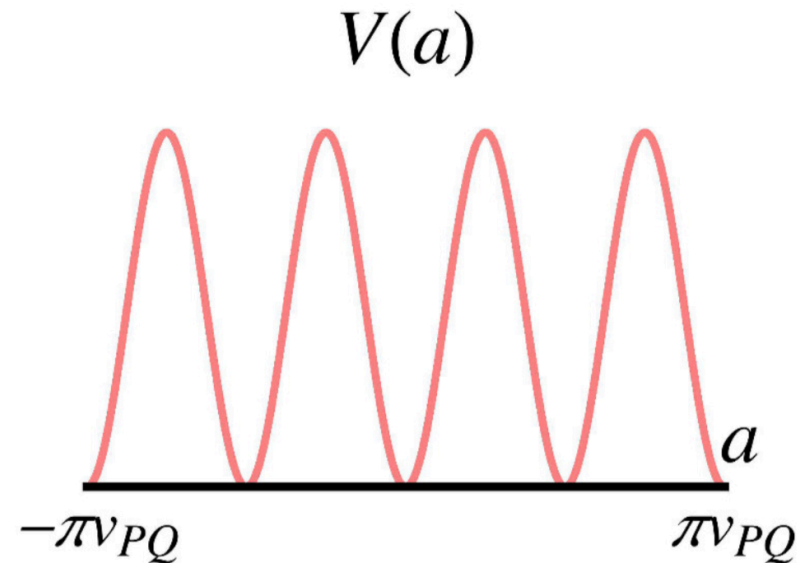
> Quarks (SM or extra) carry PQ charges such that  $U(1)_{PQ}$  is anomalously broken due to gluonic triangle anomaly

$$\partial_\mu J_{U(1)_{PQ}}^\mu = -\frac{\alpha_s}{8\pi} N G_{\mu\nu}^a \tilde{G}^{a\mu\nu} - \frac{\alpha}{8\pi} E F_{\mu\nu} \tilde{F}^{\mu\nu}$$

> No strong CP problem, since NGB field acts as x-dependent theta parameter:

$$\mathcal{L} \supset -\frac{\alpha_s}{8\pi} \frac{A(x)}{f_A} G_{\mu\nu}^a \tilde{G}^{a\mu\nu} - \frac{\alpha}{8\pi} \frac{E}{N} \frac{A(x)}{f_A} F_{\mu\nu} \tilde{F}^{\mu\nu}; \quad f_A = v_{PQ}/N$$

QCD dynamics:  $\langle A(x) \rangle = 0$



$$V(A) \simeq m_\pi^2 f_\pi^2 \left[ 1 - \frac{\sqrt{m_u^2 + m_d^2 + 2m_u m_d \cos(NA/v_{PQ})}}{m_u + m_d} \right]$$

[Peccei,Quinn 77; Weinberg 78; Wilczek 78]

A ... Axion



# Axion Couplings to SM at Energies Below QCD Scale

$$\mathcal{L} = \frac{1}{2} \partial_\mu A \partial^\mu A - \frac{1}{2} m_A^2 A^2 - \frac{\alpha}{8\pi} \frac{C_{A\gamma}}{f_A} A F_{\mu\nu} \tilde{F}^{\mu\nu} + \frac{1}{2} \frac{C_{Af}}{f_A} \partial_\mu A \bar{\psi}_f \gamma^\mu \gamma_5 \psi_f$$

> Axion mass:  $m_A = 57.0(7) \left( \frac{10^{11} \text{ GeV}}{f_A} \right) \mu\text{eV}$  [Weinberg '78; ... Borsanyi et al. '16]



# Axion Couplings to SM at Energies Below QCD Scale

$$\mathcal{L} = \frac{1}{2} \partial_\mu A \partial^\mu A - \frac{1}{2} m_A^2 A^2 - \frac{\alpha}{8\pi} \frac{C_{A\gamma}}{f_A} A F_{\mu\nu} \tilde{F}^{\mu\nu} + \frac{1}{2} \frac{C_{Af}}{f_A} \partial_\mu A \bar{\psi}_f \gamma^\mu \gamma_5 \psi_f$$

- > Axion mass:  $m_A = 57.0(7) \left( \frac{10^{11} \text{ GeV}}{f_A} \right) \mu\text{eV}$  [Weinberg '78; ... Borsanyi et al. '16]
- > Couplings of axion to SM suppressed by powers of

$$f_A = v_{\text{PQ}}/N \gg v = 246 \text{ GeV}$$

rendering the axion „invisible“

[Kim 79; Shifman, Vainshtein, Zakharov 80; Zhitnitsky 80; Dine, Fischler, Srednicki 81; ...]



# Axion Couplings to SM at Energies Below QCD Scale

$$\mathcal{L} = \frac{1}{2} \partial_\mu A \partial^\mu A - \frac{1}{2} m_A^2 A^2 - \frac{\alpha}{8\pi} \frac{C_{A\gamma}}{f_A} A F_{\mu\nu} \tilde{F}^{\mu\nu} + \frac{1}{2} \frac{C_{Af}}{f_A} \partial_\mu A \bar{\psi}_f \gamma^\mu \gamma_5 \psi_f$$

> Axion mass:  $m_A = 57.0(7) \left( \frac{10^{11} \text{ GeV}}{f_A} \right) \mu\text{eV}$  [Weinberg '78; ... Borsanyi et al. '16]

> Couplings of axion to SM suppressed by powers of

$$f_A = v_{\text{PQ}}/N \gg v = 246 \text{ GeV}$$

rendering the axion „invisible“

[Kim 79; Shifman, Vainshtein, Zakharov 80; Zhitnitsky 80; Dine, Fischler, Srednicki 81; ...]

> Photon coupling:  $C_{A\gamma} = \frac{E}{N} - 1.92(4)$  [Kaplan 85; Srednicki '85]

> Nucleon couplings: [Grilli di Cortona et al. '16]

$$C_{Ap} = -0.47(3) + 0.88(3)C_{Au} - 0.39(2)C_{Ad} - 0.038(5)C_{As} \\ - 0.012(5)C_{Ac} - 0.009(2)C_{Ab} - 0.0035(4)C_{At},$$

$$C_{An} = -0.02(3) + 0.88(3)C_{Ad} - 0.39(2)C_{Au} - 0.038(5)C_{As} \\ - 0.012(5)C_{Ac} - 0.009(2)C_{Ab} - 0.0035(4)C_{At}$$



# Axion Couplings to SM at Energies Below QCD Scale

$$\mathcal{L} = \frac{1}{2} \partial_\mu A \partial^\mu A - \frac{1}{2} m_A^2 A^2 - \frac{\alpha}{8\pi} \frac{C_{A\gamma}}{f_A} A F_{\mu\nu} \tilde{F}^{\mu\nu} + \frac{1}{2} \frac{C_{Af}}{f_A} \partial_\mu A \bar{\psi}_f \gamma^\mu \gamma_5 \psi_f$$

> Axion mass:  $m_A = 57.0(7) \left( \frac{10^{11} \text{ GeV}}{f_A} \right) \mu\text{eV}$  [Weinberg '78; ... Borsanyi et al. '16]

> Couplings of axion to SM suppressed by powers of

$$f_A = v_{\text{PQ}}/N \gg v = 246 \text{ GeV}$$

rendering the axion „invisible“

[Kim 79; Shifman, Vainshtein, Zakharov 80; Zhitnitsky 80; Dine, Fischler, Srednicki 81; ...]

> Photon coupling:  $C_{A\gamma} = \frac{E}{N} - 1.92(4)$  [Kaplan 85; Srednicki '85]

> Nucleon coupling **model-independent** [Grilli di Cortona et al. '16]

$$C_{Ap} = -0.47(3) + 0.88(3)C_{Au} - 0.39(2)C_{Ad} - 0.038(5)C_{As} \\ - 0.012(5)C_{Ac} - 0.009(2)C_{Ab} - 0.0035(4)C_{At},$$

$$C_{An} = -0.02(3) + 0.88(3)C_{Ad} - 0.39(2)C_{Au} - 0.038(5)C_{As} \\ - 0.012(5)C_{Ac} - 0.009(2)C_{Ab} - 0.0035(4)C_{At}$$



# Axion Couplings to SM at Energies Below QCD Scale

$$\mathcal{L} = \frac{1}{2} \partial_\mu A \partial^\mu A - \frac{1}{2} m_A^2 A^2 - \frac{\alpha}{8\pi} \frac{C_{A\gamma}}{f_A} A F_{\mu\nu} \tilde{F}^{\mu\nu} + \frac{1}{2} \frac{C_{Af}}{f_A} \partial_\mu A \bar{\psi}_f \gamma^\mu \gamma_5 \psi_f$$

- > Axion mass:  $m_A = 57.0(7) \left( \frac{10^{11} \text{ GeV}}{f_A} \right) \mu\text{eV}$  [Weinberg '78; ... Borsanyi et al. '16]

- > Couplings of axion to SM suppressed by powers of

$$f_A = v_{\text{PQ}}/N \gg v = 246 \text{ GeV}$$

rendering the axion „invisible“

[Kim 79; Shifman, Vainshtein, Zakharov 80; Zhitnitsky 80; Dine, Fischler, Srednicki 81; ...]

- > Photon coupling:  $C_{A\gamma} = \frac{E}{N} - 1.92(4)$  [Kaplan 85; Srednicki '85]

- > Nucleon coupling **model-independent** [Grilli di Cortona et al. '16]

$$C_{Ap} = -0.47(3) + 0.88(3)C_{Au} - 0.39(2)C_{Ad} - 0.038(5)C_{As} \\ - 0.012(5)C_{Ac} - 0.009(2)C_{Ab} - 0.0035(4)C_{At},$$

$$C_{An} = -0.02(3) + 0.88(3)C_{Ad} - 0.39(2)C_{Au} - 0.038(5)C_{As} \\ - 0.012(5)C_{Ac} - 0.009(2)C_{Ab} - 0.0035(4)C_{At}$$

- > Electron coupling very model-dependent



# Axion-Like Particles (ALPs)

- Extending the SM by further well-motivated global symmetries may lead to even more Nambu-Goldstone bosons:
  - Global lepton number symmetry: [Majoron](#) [Chikashige et al. 78; Gelmini, Roncadelli 80]
  - Global family symmetry: [Familon](#) [Wilczek 82; Berezhiani, Khlopov 90]

$$\mathcal{L} \supset -\frac{\alpha_s}{8\pi} \frac{C'_{ig}}{f_{a'_i}} a'_i G_{\mu\nu}^b \tilde{G}^{b,\mu\nu} - \frac{\alpha}{8\pi} \frac{C'_{i\gamma}}{f_{a'_i}} a'_i F_{\mu\nu} \tilde{F}^{\mu\nu} + \frac{1}{2} \frac{C'_{a'_i f}}{f_{a'_i}} \partial_\mu a'_i \bar{\psi}_f \gamma^\mu \gamma_5 \psi_f$$

- Then the particle corresponding to the excitation of the field combination

$$\frac{A(x)}{f_A} \equiv \frac{C'_{ig}}{f_{a'_i}} a'_i(x)$$

is the [axion](#)

- Particle excitations of the fields orthogonal to this field combination are called [Axion-Like-Particles \(ALPs\)](#)
- String theory suggests a plenitude of ALPs [Witten 84; Conlon 06; Arvanitaki, Dimopoulos, Dubovsky, Kaloper, March-Russell 10; Cicoli, Goodsell, AR 12]



# A Minimal Model of Particle Physics and Cosmology

- > Unify PQ U(1) symmetry with lepton symmetry: add vector-like quark and three right-handed SM-singlet neutrinos to SM [Shin 87; Dias et al. '14]

$$\mathcal{L} \supset - \left[ Y_{u_{ij}} q_i \epsilon H u_j + Y_{d_{ij}} q_i H^\dagger d_j + G_{ij} L_i H^\dagger E_j + F_{ij} L_i \epsilon H N_j + \frac{1}{2} Y_{ij} \sigma N_i N_j + y \tilde{Q} \sigma Q + y_{Q_{di}} \sigma Q d_i + h.c. \right]$$

$q$	$u$	$d$	$L$	$N$	$E$	$Q$	$\tilde{Q}$	$\sigma$
1/2	-1/2	-1/2	1/2	-1/2	-1/2	-1/2	-1/2	1





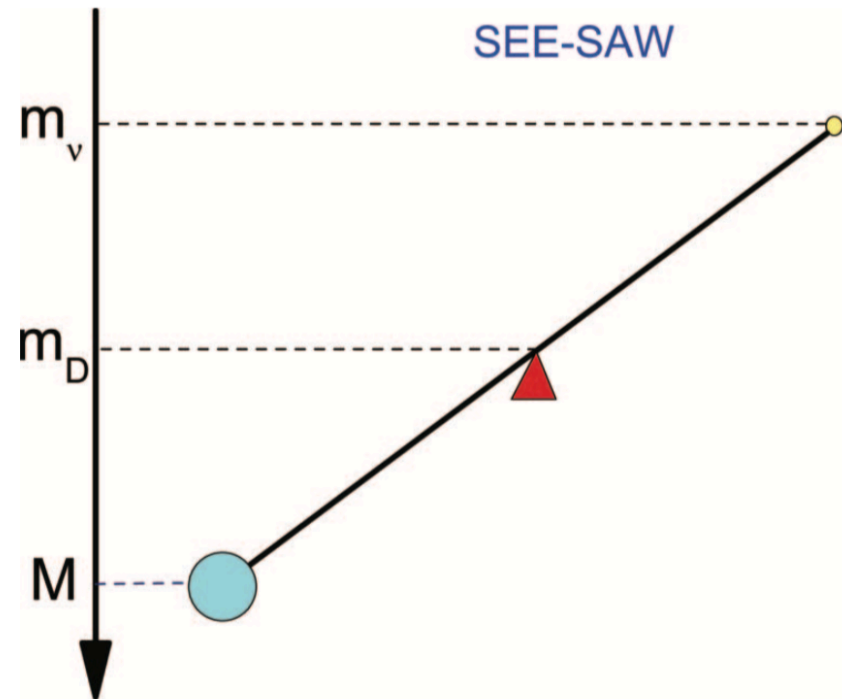
# A Minimal Model of Particle Physics and Cosmology

- > Unify PQ U(1) symmetry with lepton symmetry: add vector-like quark and three right-handed SM-singlet neutrinos to SM [Shin 87; Dias et al. '14]

$$\mathcal{L} \supset - \left[ Y_{u_{ij}} q_i \epsilon H u_j + Y_{d_{ij}} q_i H^\dagger d_j + G_{ij} L_i H^\dagger E_j + F_{ij} L_i \epsilon H N_j + \frac{1}{2} Y_{ij} \sigma N_i N_j + y \tilde{Q} \sigma Q + y_{Q_{d_i}} \sigma Q d_i + h.c. \right]$$

1. No strong CP problem
2. See-saw explanation of active neutrino masses

$$m_\nu = 0.04 \text{ eV} \left( \frac{10^{11} \text{ GeV}}{v_\sigma} \right) \left( \frac{-F Y^{-1} F'^T}{10^{-4}} \right)$$



# A Minimal Model of Particle Physics and Cosmology

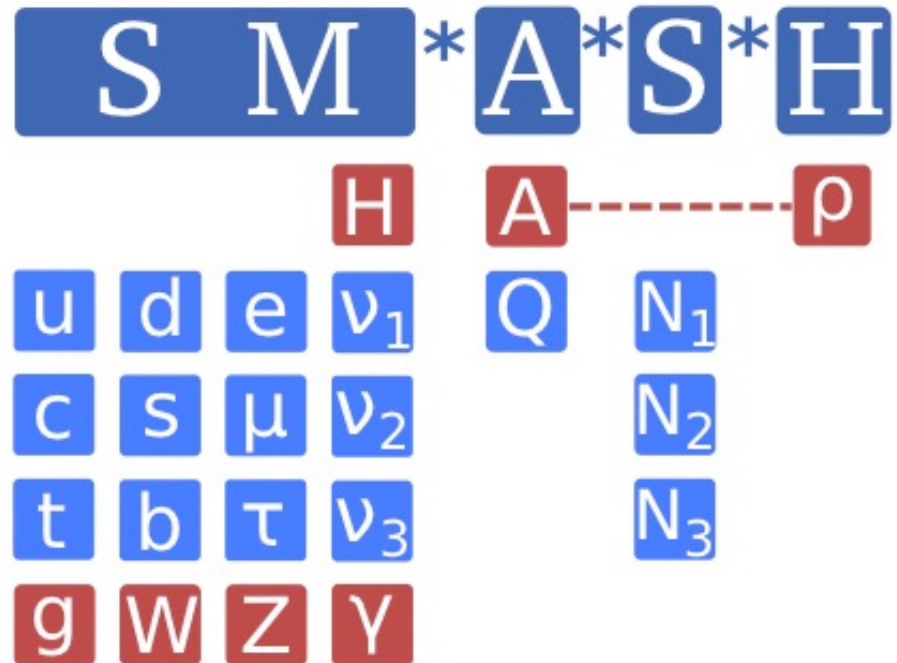
- > Unify PQ U(1) symmetry with lepton symmetry: add vector-like quark and three right-handed SM-singlet neutrinos to SM [Shin 87; Dias et al. '14]

$$\mathcal{L} \supset - \left[ Y_{u ij} q_i \epsilon H u_j + Y_{d ij} q_i H^\dagger d_j + G_{ij} L_i H^\dagger E_j + F_{ij} L_i \epsilon H N_j + \frac{1}{2} Y_{ij} \sigma N_i N_j + y \tilde{Q} \sigma Q + y_{Q d i} \sigma Q d_i + h.c. \right]$$

SM \* Axion \* See-saw \* Higgs portal inflation

[Ballesteros, Redondo, AR, Tamarit, 1608.05414]

1. No strong CP problem
2. See-saw explanation of active neutrino masses
3. Axion dark matter
4. Explains matter-antimatter asymmetry by thermal leptogenesis
5. Higgs portal inflation



# Axion in SO(10) GUT

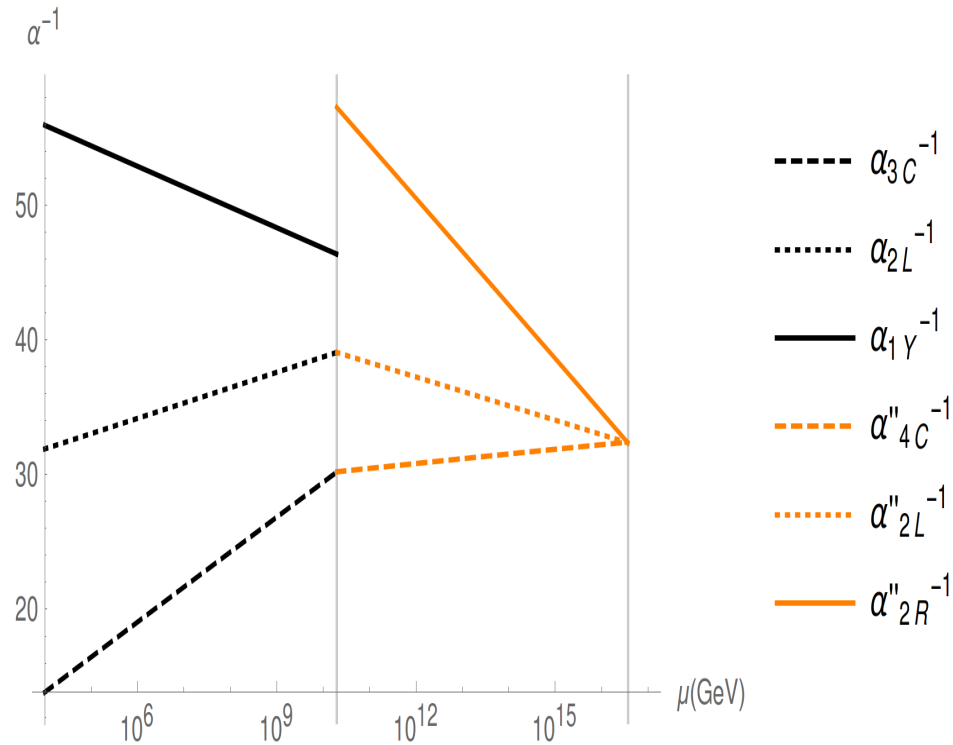
- > SO(10) GUT automatically features right-handed sterile neutrinos
  - Neutrino masses and mixing
  - Baryogenesis via leptogenesis
- > PQ extension of non-SUSY SO(10) GUT provides in addition
  - Predictivity of fermion masses/mixing
  - Solution of strong CP problem
  - Axion dark matter

$$Q = \begin{pmatrix} u_1 & u_2 & u_3 & \nu \\ d_1 & d_2 & d_3 & e \end{pmatrix},$$
$$Q^c = \begin{pmatrix} d_1^c & d_2^c & d_3^c & e^c \\ -u_1^c & -u_2^c & -u_3^c & -\nu^c \end{pmatrix}$$



# Axion in SO(10) GUT

- > SO(10) GUT automatically features right-handed sterile neutrinos
  - Neutrino masses and mixing
  - Baryogenesis via leptogenesis
- > PQ extension of non-SUSY SO(10) GUT provides in addition
  - Predictivity of fermion masses/mixing
  - Solution of strong CP problem
  - Axion dark matter
- > Intermediate SSB step required:

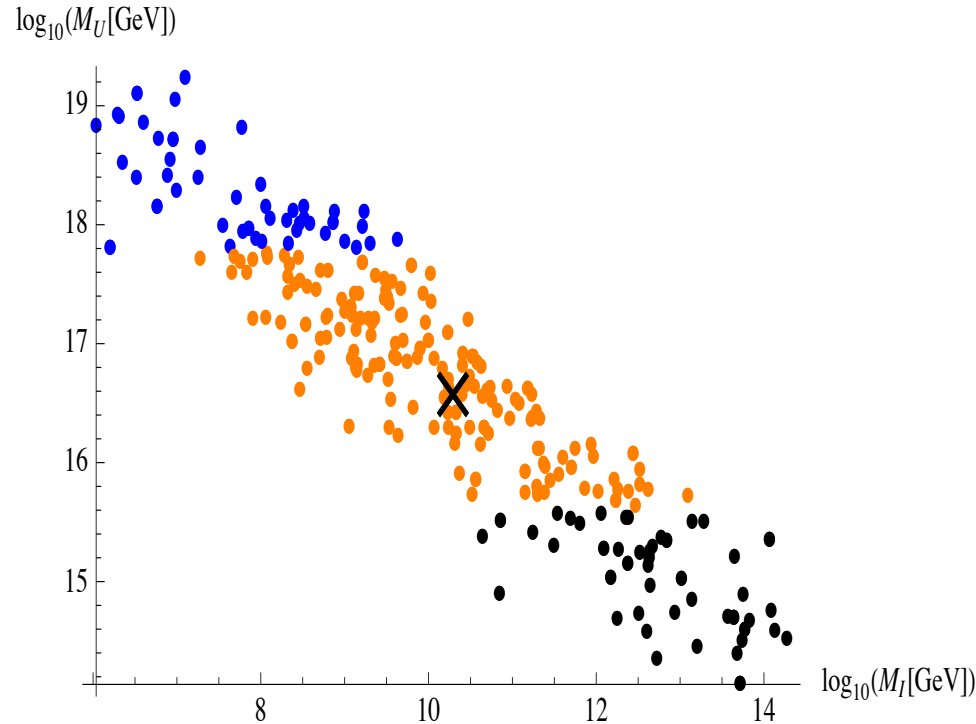


$$SO(10) \xrightarrow{M_U - 210H} SU(4)_C \times SU(2)_L \times SU(2)_R \xrightarrow{M_1 - 126H} SU(3)_C \times SU(2)_L \times U(1)_Y \xrightarrow{M_Z - 10H} SU(3)_C \times U(1)_Y$$



# Axion in SO(10) GUT

- > SO(10) GUT automatically features right-handed sterile neutrinos
  - Neutrino masses and mixing
  - Baryogenesis via leptogenesis
- > PQ extension of non-SUSY SO(10) GUT provides in addition
  - Predictivity of fermion masses/mixing
  - Solution of strong CP problem
  - Axion dark matter
- > Intermediate SSB step required:



[Ernst,AR,Tamarit in prep.]

$$SO(10) \xrightarrow{M_U-210_H} SU(4)_C \times SU(2)_L \times SU(2)_R \xrightarrow{M_I-126_H} SU(3)_C \times SU(2)_L \times U(1)_Y \xrightarrow{M_Z-10_H} SU(3)_C \times U(1)_Y$$

- > Imposing PQ symmetry,

[Ernst,AR,Tamarit in prep.]

$$16_F \rightarrow 16_F e^{i\alpha}, \quad 10_H \rightarrow 10_H e^{-2i\alpha}, \quad \overline{126}_H \rightarrow \overline{126}_H e^{-2i\alpha}, \quad 210_H \rightarrow 210_H e^{4i\alpha}$$

predicts  $1.9 \times 10^{-11} \text{eV} < m_A < 2.2 \times 10^{-9} \text{eV}$



# Axion in SO(10) GUT

> SO(10) GUT automatically features right-handed sterile neutrinos

- Neutrino masses and mixing
- Baryogenesis via leptogenesis

> PQ extension of non-SUSY SO(10) GUT provides in addition

- Predictivity of fermion masses/mixing
- Solution of strong CP problem
- Axion dark matter

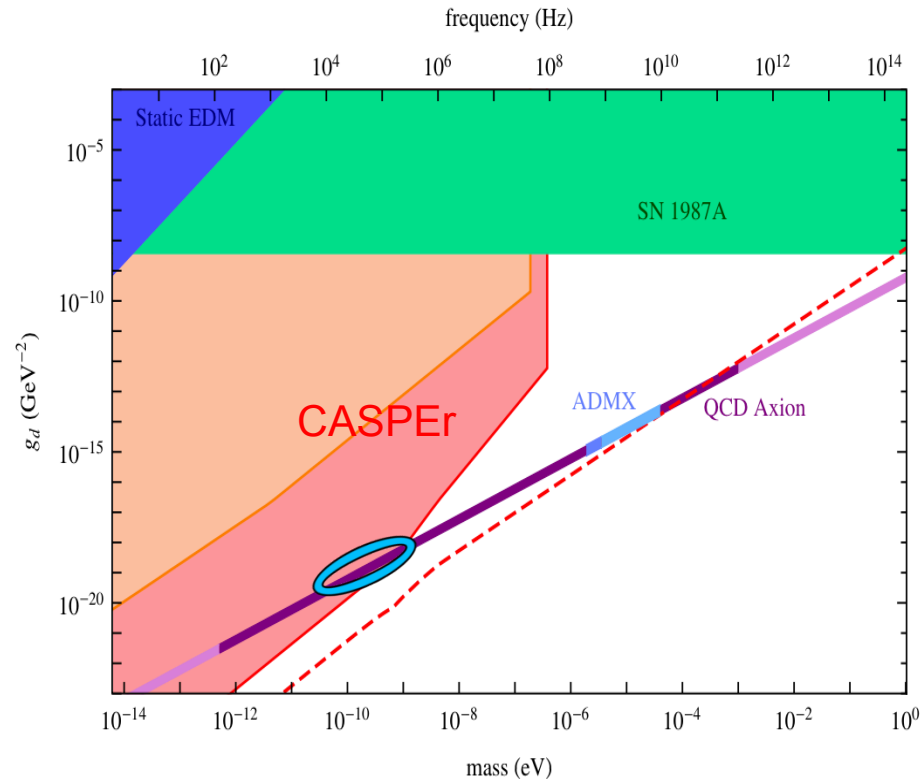
> Intermediate SSB step required:

$$SO(10) \xrightarrow{M_U \sim 210 \text{ GeV}} SU(4)_C \times SU(2)_L \times SU(2)_R \xrightarrow{M_1 \sim 126 \text{ GeV}} SU(3)_C \times SU(2)_L \times U(1)_Y \xrightarrow{M_Z \sim 10 \text{ GeV}} SU(3)_C \times U(1)_Y$$

> Imposing PQ symmetry,

$$16_F \rightarrow 16_F e^{i\alpha}, \quad 10_H \rightarrow 10_H e^{-2i\alpha}, \quad \overline{126}_H \rightarrow \overline{126}_H e^{-2i\alpha}, \quad 210_H \rightarrow 210_H e^{4i\alpha}$$

predicts  $1.9 \times 10^{-11} \text{ eV} < m_A < 2.2 \times 10^{-9} \text{ eV}$



[Budker et al. 14]

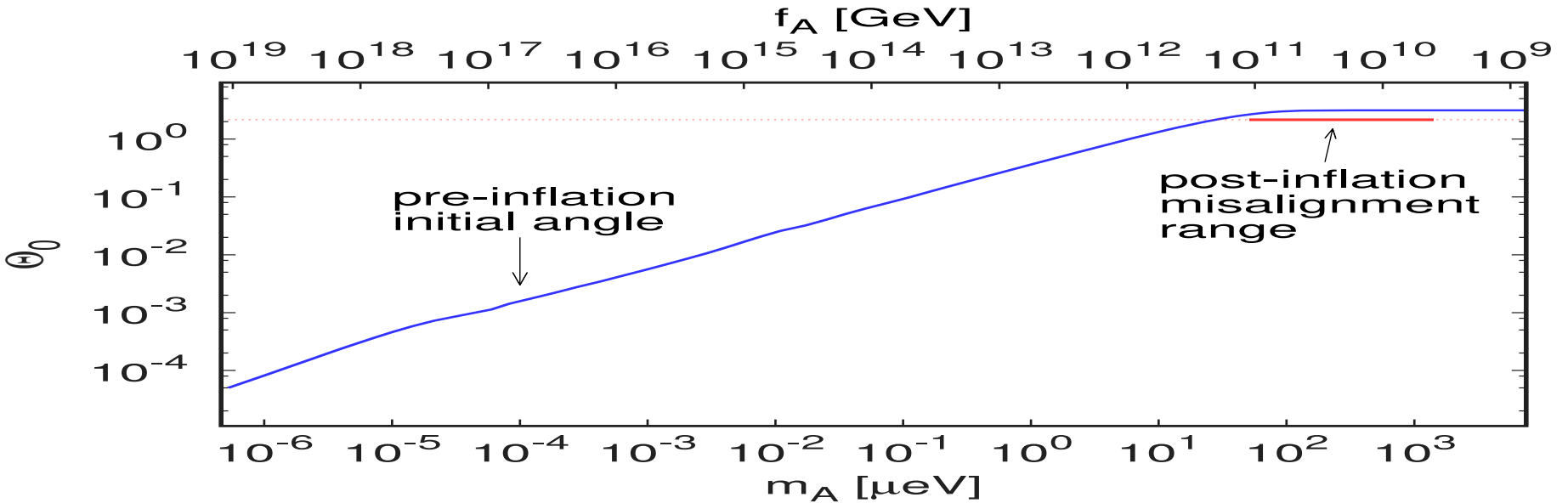
[Ernst, AR, Tamarit in prep.]



# Axion in SO(10) GUT

➤ Adding singlet  $S$  and imposing PQ symmetry predicts  $m_A \gtrsim 10^{-11}$  eV

$$16_F \rightarrow 16_F e^{i\alpha}, \quad 10_H \rightarrow 10_H e^{-2i\alpha}, \quad \overline{126}_H \rightarrow \overline{126}_H e^{-2i\alpha}, \quad 210_H \rightarrow 210_H, \quad S \rightarrow S e^{4i\alpha}$$



CASPEr

ABRACADABRA

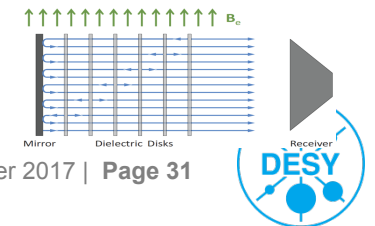
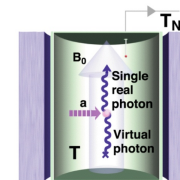
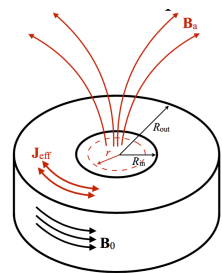
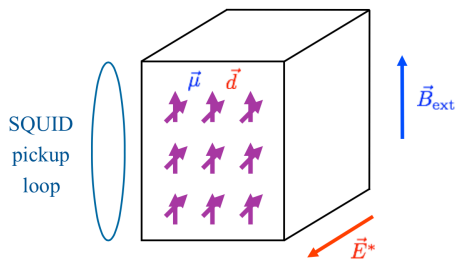
ADMX

MADMAX BRASS

HAYSTACK ORPHEUS

CULTASK ORGAN

QUAX



# Summary

- > Unlike other naturalness problems (cosmological constant, weak scale), smallness of  $\theta$  can not be justified by anthropic reasoning
- > Plenty of UV extensions of SM can provide an axionic solution of the strong CP problem
- > Strong CP problem solved for any value of decay constant
- > Axion mass in terms of decay constant very well determined
- > Couplings to photons and nucleons somewhat, to electrons strongly model-dependent
- > Tomorrow: Axions in Astrophysics and Cosmology
- > Suggest phenomenologically interesting ranges for decay constant

